Response to reviewer #1 comments

We thank the anonymous reviewer #1 for their review and note that they have identified that "the new solver can capture the dynamical, time-dependent features of nitrate partitioning that are not properly by equilibrium assumption".

We take their point about the paper being "somewhat lengthy". However, when writing the paper we considered carefully whether or not we could shorten the paper, and concluded that the level of detail provided is important and will help to ensure clarity and rigour.

In our response here we address each of the points made by the reviewer in the order that is given in his/her review:

Major Comments

1) Throughout the manuscript, the particle phase is referred to as 'liquid phase'. Many recent studies have suggested that there might be multiple liquid phases (aqueous/organic) in an aerosol particle. Therefore, I suggest changing 'liquid' to 'aqueous' in the text. We agree entirely and have changed the terminology.

2) Eq. 4 and p. 8, l. 15: Usually the effective Henry's law constant H* for acids includes the acid dissociation constant Ka, i.e. $H^* = H (1 + Ka/[H+])$ EqI Does the fact that you assume H2SO4 as being completely dissociated lead from EqI to Eq-4? Would your approach be applicable using EqI for acids that are not completely dissociated?

The total dissociation of acids assumption and the negligence of OH in the ion balance introduce a simplification into the formalism that allows us to focus on other important phenomena, such as the numerical stiffness property of the system and the related computational efficiency. The partial dissociation of acids and the presence of OH each add one additional degree of freedom to the system, that increases the degree/order of any relevant resolving/differential equation accordingly. For instance, within the dynamical solver, neglecting OH reduces Eq. 8 to a second order differential equation rather than third order, and also matches the similar approach taken in the thermodynamic scheme PD-FiTE. Most importantly, within the chemical equilibrium solver, and in relationship with its analytic approach, the simplification allowed us to take the chemical interaction of the dissolving species into account. If the partial dissociation of the dissolving species and H2SO4, and OH were taken into account, the resolving equation for one dissolving base or acid would be of the 5th degree. If only the partial dissociation of H2SO4 is taken into account, which is done in the circumstance of one dissolving species, the resolving equation is still of the 3rd degree. As one of the underlying reason for the numerical stiffness is chemical interaction, it is necessary to restrict the degree of the resolving equation to a value that is manageable. We have added the following paragraph underneath equation 4 to explain these circumstances more appropriately.

"In the preceding expression, the partial dissociation property of the dissolving species is neglected, which is an underlying assumption for HyDiS-1.0. It will allow us to reduce the number of degrees of freedom of the considered chemical system by one unit for each dissolving species. In doing so other properties, such as the species' chemcial interaction, may be taken into account more throroughly, as analytical solutions may be derived along with a critical reduction of the degree of the respective resolving equations. We have seen in the preceding section that the chemical interaction between acids and bases plays an essential role to the numerical stiffness property of the system."

3) Currently, the number of interacting species is limited to three. Will it possible to rigorously extend the solver to more compounds, given the complex composition of ambient atmospheric aerosol? In line with the preceding point, the number of dissolving species may not be consistently augmented beyond this number, unless the chemical interaction of the dissolving species will necessarily be accounted for less thoroughly within the chemical equilibrium solver. We have added the following sentence for clarity.

"Similarly, the number of dissolving species whose chemical interaction may be fully taken into account may not exceed three, as no analytical solution is readily available to an equation beyond the fourth degree."

4) The discussion of the model results (both box and global) in Sections 4.2 and 5.3., respectively, are poorly connected to the figures. All figure panels should be labeled a, b, c, etc and the discussion should be tied more closely to the individual panel so that it is easier to reader to follow. In accordance with the suggestion made by the reviewer we have numbered all panels of Figures 5-16 and linked them more thoroughly with the text.

5) It is not clear what the 'entire microphysical box model' (e.g., p. 28, l. 32; and Table 1) includes. How far is a comparison of the microphysical model meaningful to the chemical model that includes the new solver? Does using the new solver in the microphysical model lead to redundancy? We have reshaped the explanation of how the percentage computational expense of HyDiS within the box model runs is obtained. Also, we have mentioned the processes that are comprised within the Glomap microphysical scheme and given more details on the implementation of HyDiS within this scheme.

6) The comparison to the efficiency of previous models is only touched on briefly (end of Section 5.4). Given the extensive length of the current manuscript already, I am not asking for a detailed discussion/ However, a brief statement of the ability of the model by Zaveri et al. (2008) to reproduce the dynamical features as opposed to equilibrium assumptions should be added. In general, how well did the model by Zaveri et al., to observations?

The reviewer asks for an extension of the comparison of HyDiS to other gas/particle exchange schemes with respect to the global aerosol composition. In principle, we agree with the reviewer about the relevance of such a comparison. However, a comparison to other schemes is not trivial and will require a lengthy analysis. At this point a comparison would be premature, as certain important processes, such

as particle cristallization and the dissolution of HCl, are not currently included in TOMCAT-GLOMAP, and certain other processes, such as heterogeneous chemistry and aerosol organic species, are not taken into account for the present preliminary simulations. For these reasons, we limited the analysis herein to solver computational efficiency and numerical reliability considerations, along with a preliminary assessment of the relevance of nonequilibrium dynamics as the one intended main plus of the solver relative to equilibrium approaches.

Minor Comments

p. 2 l. 11: At most RH values, the amount of water exceeds the amount of solute mass, e.g. (Liao and Seinfeld, 2005). Do you mean here the increase of particle size due to solute mass and its associated water? We mean both the increase of particle mass via efficient interaction of nitrate+ammonium and the amount of water that goes with it. The interaction of ammonium and nitrate may be efficient to the point that the loss of the particle water mass via the reduction of hygroscopicity along with the acidicity of the aqueous phase does not exceed the gain of particle mass via the chemical interaction of ammonium, nitrate and water. Clarified.

p. 61. 3: Do you mean ' the concentration of the dissolving species in the aerosol aqueous phase'? Expression corrected for improved clarity.

p. 11 l. 17: This is unclear, in particular for the conditions described here. 1) Make clear that the aqueous s phase 'is predicted to loose protons'. 2) One would assume that under the acidic conditions described here, there is a huge excess of protons. Sentence is clarified.

p. 14 l. 26: Are these parameters (activity coefficients, liquid water content, and dissociation) held constant throughout the simulation or during one time step? The mentioned variables are not considered as such by the analytical scheme. They are updated at the outer iteration level of the chemical equilibrium solver, this is clarified further down in the text, however cannot be mentioned here as the reader would not be able to follow at this point.

p. 16 l. 21: What is the extent to which the pH varies within the iteration? Are these extreme values or are they realistic over the course of a time step, when aerosol might be exposed to ambient conditions? Extreme variations of the particle pH occur frequently in the course of the execution of the equilibrium solver, and they are not necessarily related to exceptionally rapid modifications of ambient conditions. The extreme variability of particle pH is the most characteristic feature of the numerical stiffness property of dissolution, and occurs under all polluted conditions for c> 1ppb approximately, with the diurnal cycle of temperature serving as one of the potential sources of sufficient perturbation (used in the box model experiments) in the context of an overall time step of 15 or 30 minutes. In this context, the convergence of the pH variability to less than 0.1 is an appropriate prerequisite for one outer iteration that updates the parameters, and a subsequent round of internal iterations with a renewed massive variability of the pH. We refer to Section 2 for further detail on the numerical stiffness properties of chemically interacting species via pH.

p. 17 l. 9: The wording is ambiguous, I think. The convergence criterion is stricter; however, the value is DEcreased from 0.1 to 0.01. If I misunderstood this, clarify. The convergence criterion is increased from 0.001 to 0.01. The criterion for this choice is set to 0.1. Clarified.

p. 18 Eq. 29: Does 'a' have a physical meaning? What is the range of meaningful

values for this parameter? The proportionality constant has a qualitative physical meaning, as it stands for the amount of chemical interaction that one is willing to take into account in terms of the determination of the length of the internal time step of the dynamic solver. Although it has this qualitative physical meaning, it is hard to figure out how this would physically translate into a mathematical expression. Notwithstanding, this latter issue is of limited relevance, as the proportionality constant has another more relevant meaning, as it conditions the number of internal time steps of the dynamic solver. If a size class would require more internal time steps due to numerical constraints, it would be assumed to be in equilibrium whether this is accurate or not. It is clear that the computational expense will be roughly proportional to this number. We have chosen 'a' for the number of internal time steps to be limited to roughly 3. This number was shown by the box model experiments to produce reasonably accurate results, even under numerically stiff conditions of strong chemical interaction. It should be noticed at this point that a larger overall time step might require an accordingly smaller proportionality constant, unless the accuracy of the results might be critically diminished. The text was modified for more clarity.

p. 19 1. 18: What are the physical/chemical parameters that determine equilibration time of a dissolving species? Is it e.g. solubility (Henry's law constant) or something else? Could threshold values be given above/below which equilibration is achieved in short time, relatively to the model time steps? By virtue of Eq. 15 the equilibration time is given by the ratio of the difference between the equilibrium and the momentary atmospheric concentration of the dissolving species in the aqueous phase, and the potential of the dissolved species to evaporate from particle surface or the potential of the dissolving species to condense onto the particle surface, whichever potential is the largest. This quantity may be seen as a normalized degree of saturation of the aqueous phase, which correlates with the equilibration time. By virtue of the proportionality factor 'a' and the definition of the distinction criterion between equilibrium and dynamic simulation, the critical equilibration time is defined relative to the overall time step of the model: a particle is considered to be in equilibrium if its equilibration takes less than half the overall time step of the model. Due to its multivariable dependence no individual threshold value may be given that would determine a short equilibration time. We refer to the explanations around Eq. 15 for explanations within the manuscript on this question.

p. 20 l. 13: Does 'a' here have the same meaning as in Eq. 29? If not, choose a different symbol to avoid confusion. The notation of the second coefficient is changed to 'b'.

p. 23 l. 23: Not clear what 'its' refers to here. Corrected.

p. 23 l. 22 and 24: Spell our ADDEM, MANIC. Now spelled.

p. 24 l. 1: What are the particle sizes for the various modes? Mode sizes now indicated.

p. 24 l. 31: Is the temperature dependence of HNO3 dissolution very different than that of NH3? Can you support this trend by numbers (T-dependence of H?)? The temperature dependence of the solubility of HNO3 and NH3 is explained more thoroughly and references are added.

p. 26 l. 3ff.: Are there any simultaneous measurements of NH3 partitioning in gas and

particle phase that show similar trends of subsaturation? The observed undersaturation concerns a twofold phenomenon, each related to a particular kind of numerical stiffness. On the one hand, the aqueous phase remains undersaturated as it tends to equilibrate very slowly in the context of the slow transit of the semi-volatiles through the gas phase. This dynamical phenomenon is now mentioned in the Introduction (Zaveri et al., 2008). On the other hand, the surface pressure of one dissolving species remains underneath the ambient pressure, depending on the choice that is made by the solver as a function of its configuration. This artificial phenomenon is related to the extreme numerical stiffness via particle pH and chemical interaction that is encountered at 100 ppb, which appears to cause a relative imprecision of the solver. This artifact has very little influence on the predicted concentrations of the dissolved species, because these are several orders of magnitude larger than the proton concentration. We point to the explanations that are given within Section 4.2 around Figure 10.

p. 27 l. 14/15: What is different in terms of (physico)chemical properties of chloride

and nitrate vs ammonium that could explain their different behavior? The reason for the similarity of ammonium under dynamic and equilibrium conditions may be illustrated with the coarse mode. The particle pH is too low for the solubility of ammonia to be high, such that the equilibration time of ammonium remains relatively low. Furthermore, nitric acid and hydrochloric acid are competitors, as nitric acid drives out the latter and replaces it, and particle pH remains unaffected, which in turn tends to keep the solubility of ammonia low but constant. The only factor that affects the solubility of ammonia is its temperature dependance, which also results in a quick almost instantaneous adaptation, to the overall effect that the equilibrium and dynamic concentrations of ammonium are almost equal. We have added 2 sentences for explanation.

p. 27 l. 31: 'Particle concentrations' usually refers to mass or number concentration of particles. Do you mean 'the concentration of ammonia and chloride in the aqueous phase'? Corrected.

p. 29 l. 20: What is included as sulphur chemistry? Both gas and aqueous phase processes? When sulphate is formed in the aqueous phase, does it contribute to the species that are equilibrated between the phases? An explanation is added to the text.

p. 32 l. (1)5: Reword: ": : : the ambient concentration of ammonia over the Southern Ocean is predicted to be lower by 10-25% than predicted by the equilibrium approach" or similar in order to clarify that you compare two model results. Inserted.

p. 32 l. 28: Is this very low nitric acid concentration in the Arctic in agreement with

observations? The question of the validation of the model predictions against observations (and other models) certainly is an important one. Adams et al. (1999) give a few data points for their simulated mixing ratio of ammonia close to the western coast of Alaska during the Arctic summer. Their values of 2-5 ppt are similar to our estimations under the equilibrium assumption. With the hybrid configuration we obtain approx. 10 ppt. In their measurements off the east coast of Baffin Island during Summer 2014, Wentworth et al. (2016) find ammonia mixing ratios of around 30 ppt. With the hybrid configuration we obtain a simulated mixing ratio of approx. 10 ppt, with the equilibrium configuration we obtain a piprox. 1/3 of this value. It thus seems that non-equilibrium dynamics play an important role and that our simulations get the order of magnitude right in the Arctic. Having said this, the observed and the simulated within our answer to the 6th major comment, the validation of the model results will be performed in much greater detail in follow-on publications, as the present largely focuses on solver presentation and numerical validation. We have modified the text to clarify the circumstance that we compare two model results.

Fig. 1, caption: 1) Is the particle size the wet radius? At what RH?; 2) Could you mark the steps 1-3 in the figure (e.g. by shading or vertical lines)? 1) the dry radius is given, this circumstance is now indicated along with the relative humidity of 80%, 2) the regimes are now marked as requested.

Fig. 6, 7, 9 and 10 should have a somewhat more detailed caption. What does the 10 ppb etc refer to? The figure caption is reformulated and more details are added to Figs. 5 and 8, respectively.

Fig. 11: Some of the text in the figure is very blurry, e.g., 'HCl', 'soluble nucl.' In the top panel and 'OH, NO2' (?) in the bottom panel. The resolution of the figure is improved.

Fig. 12: In the caption only two panel (top and bottom) are described, but there are three panels (top, middle, bottom) shown. Clarify and improve caption. The figure caption has been partially reworded.

Technical comments: thank you for indicating these, all worked in.

Additional Reference:

Wentworth, G. R., Murphy, J. G., and Croft, B., et al.: Ammonia in the summertime Arctic marine boundary layer: sources, sinks, and implications, Atmos. Chem. Phys., 16, 1937–1953, 2016.

Response to reviewer #2 comments

We thank the anonymous reviewer #2 for their review.

We feel strongly the reviewer overstates the severity of the issues he identifies. It seems to us that many if not all of the reviewer's major comments are related to weaknesses in the clarity of the manuscript. We have revised the manuscript to address this, giving additional explanation where appropriate.

There are 3 elements the reviewer identifies as together meaning major revisions would be required before publication in GMD:

(1) "(...) (T)he box model tests and global modeling results presented do not clearly demonstrate the accuracy of the solver against a benchmark method and fail to properly evaluate its efficiency (for a chosen level of accuracy) or directly compare it with previously published solvers."

We assert strongly that our use of the fully dynamic implementation of the Jacobson (1997) scheme as a benchmark to test the hybrid dissolution solver is entirely justified. The potential of the embedded fully dynamic scheme to serve as a benchmark is documented in the literature (Zaveri et al., 2008). Similarly, this manuscript builds on the previous testing of the thermodynamic scheme against AIM (Topping et al., 2009), and there should be no need to redo this here.

(2) "The new solver is also incomplete because it presently appears to ignore gas-particle mass transfer to solid particles, which may be present under low relative humidity conditions."

Our paper describes a hybrid solver to calculate the dissolution of inorganic gases into the aerosol aqueous phase. We agree that we should perhaps have stated more clearly that aerosol solid phase processes are not included. However, the purpose of the paper is to describe and evaluate the new solver in the box model, and assess its numerical reliability and computational efficiency within the framework of a global model. We content strongly that the paper is consistent and adequate as being directed towards these aspects.

(3) "The manuscript is lengthy and a bit confusing in various places due to imprecise notations and terminologies."

We acknowledge that the paper is long, but when writing it, we considered carefully to what extent it should be shortened. We concluded that the level of detail provided is important and will help to ensure reproducibility of results and to rigorously describe the solver. We note that reviewer 1 states that "all parts seem essential and show the logical steps from development, over sensitivity studies in a box model to application in a global model."

We also are puzzled that the reviewer regards the use of 'size bin' and 'size increment', 'dissolving' and 'non-dissolving', the way Eq. 9 is introduced and an apparent typing error in Eq. 15 as major issues,

while the large amount of effort that was put into the explanation of the solver appears not to find any credit.

Finally, some of the reviewer's concerns, like the confusion around Figure 1, could have been easily addressed via a question to the authors.

Within the following we will address the points of the reviewer in the order given within his/her comment.

Major comments:

1) "The new hybrid solver described here treat dynamic (and equilibrium) gas-particle partitioning of HNO3, HCl, and NH3 for aqueous particles only. The implicit oversimplifying assumption is that all aerosol particles are always fully deliquesced at all relative humidities. This assumption may not hold at low relative humidities (below about 35-40%) where dissolved salts can effloresce to form a solid phase. The solver also ignores heterogeneous uptake of HNO3 on dust particles containing calcite, which is an important sink for nitrate. The proposed solver is therefore incomplete and premature for implementation in a global atmospheric transport model. These are major weaknesses that must be rectified before the present work can be considered for publication."

The reviewer observes that the heterogeneous and solid phase processes are not treated by the solver, and maintains that its implementation within a global model is premature. We agree that solid phase processes are not included and that these play an important role for the aerosol inorganc composition. The revised manuscript now makes it much clearer that these processes are not included and gives reference for papers which include them and assess their effects.

Also, we would like to stress that the paper is clearly set out to describe and evaluate a new solver for the reversible dissolution of inorganic species into the aerosol liquid phase. As stated within Section 5.1, the solver is implemented into a global model to verify that it is able to give realistic results for the full parameter space encountered in a global 3D chemistry-aerosol transport model, to demonstrate the importance of the non-equilibrium property of dissolution, and to evaluate its computational efficiency.

All of these do not require a complete mechanism of aerosol/gas exchange. Given the explanations of Section 5.1, we had assumed that the discussion of the global modelling results within Section 5.3 would be understood from this perspective.

We have made additions to the conclusion and Section 5 that emphasize the limitations of the global simulations in the context of their scope.

2) "Page 2, Lines 24-25: The literature review of dynamic partitioning solvers is inadequate as there is lot more work done than what's discussed here. In addition to Capaldo et al. (2000) and Zaveri et al. (2008), the following papers describe different approaches to dynamically solving partitioning of

HNO3, HCl, and NH3, which need to be properly discussed. Also, MOSAIC is incorrectly classified under the hybrid approach as it always performs fully dynamic mass transfer for all size bins."

The reviewer has drawn our attention to the fact that the discussion of the literature requires improvement. We have expanded the discussion on the basis of the additional references that were provided, as Jacobson (1997), (2002) and (2005) are discussed within Section 4.1 in the context of the motivation for the choice of the benchmark scheme, and Zhang and Wexler (2006) and Wexler and Seinfeld (1992) in the Introduction. We preferred to discuss Wexler and Seinfeld (1992) rather than (1991), because the earlier appears to be the more relevant one.

3) "Figure 1. There are quite a few things that I don't understand in this example/figure:

a) This example is shown before the different solvers are introduced in section 3, so it is not clear which solver was used to illustrate this example. Please clarify. Also what relative humidity was used? b) According to the text on page 3 and the figure caption, the initial particles are pure H2SO4 with radius 50 μ m and the number concentration 100 cm-3? If this is correct, then nearly all of the NH3 will be absorbed into the particles in less than 10 s. But since the gas-phase NH3 does not change appreciably with time, I am assuming the initial radius is 0.05 μ m (not 50 μ m).

c) Assuming the radius is $0.05 \mu m$, why does it take NH3 about 200 s before it begins to dissolve appreciably into H2SO4 particles? My calculation shows that NH4/SO4 molar ratio reaches approx. 0.8 at 200 s.

d) Why does substantial amount of HNO3 gas dissolve in H2SO4 particles during the first 200 s when NH3 hasn't yet neutralized the acidity to some extent?

e) Why are there no oscillations for the time step of 10 s?

f) Please clearly define in the caption the short forms for terms used in the legend: "part" and "atm".

g) Are the units on the Y-axis [molecule m-3(air)] for both gas- and particle-phase species concentrations?

h) Why do the gas- and particle-phase concentrations of become equal (blue line and green line) after 400 s for both NH3 and HNO3?"

The reviewer points to Figure 1 and asks for clarification. First, the reviewer diagnosed correctly that the initial size of the particles is not 50 micrometres but rather 50 nanometres. Second, a great deal of the confusion might have arisen due to what seems to be a lack of sufficient clarity on what is exactly shown within Figure 1. The graph does not compare the gas phase molecule number concentration against the gas phase equivalent concentration of molecules in the liqud phase but rather against the partial pressure at particle surface, which is expressed as a molecule number concentration equivalent via the perfect gas law (as given by the terms 'particle surface concentration' and 'pressure' in the figure caption). For this reason, the accuracy of the dynamic formalism is actually demonstrated by the figure, as the particle surface pressures tend to the gas phase partial pressures in the process of system equilibration.

These explanations should clarify the reviewer's points b), c), d), g) and h).

Concerning question a), the graphs were produced with the same fully dynamic approach that is used later on as a benchmark to demonstrate the accuracy of the hybrid solver, that is the Jacobson 1997 scheme used at fixed time step (see below).

This relates then to the reviewer's point e): The 10 second run does not oscillate because close to equilibrium the Jacobson scheme proves to be sufficiently stable when the time step is in accordance with the dynamical properties of the simulated system and its characteristic equilibration time interval. The oscillation is the result of an initial overshoot close to equilibrium, followed by consecutive of under- and overshoots. Both equilibrium regimes, the steady state and the artificial oscillation regime, are stable, meaning that if the system was sufficiently perturbed at equilibrium, it could quite well be that the system would oscillate at a time step of 10 seconds, just as it could remain at steady state at a time step of 30 seconds if brought sufficiently close to it.

As to point f), we have added an explantion of 'part' and 'atm' to the figure caption. Short additions were made to the figure caption (and within Section 3 for point e) that should correct and clarify the issues raised by the reviewer.

4) "What is the difference between "size bin" and "size increment"? If they mean the same thing, then please stick with "size bin." Otherwise, please clearly define a "size increment." "

The difference between size bin and increment is close to none, we have used them as synonyms. We scrapped both 'increment' and 'bin', and replaced them with the term 'class', for the reason that 'bin' is frequently used in the literature context in reference to a 'bin' in opposition to a 'modal' model, although this distinction might not be totally clear and appropriate either.

5) "Page 5, Line 16: What are the "dissolving" and "non-dissolving (=passive)" species considered in this work? It's not clear what a "non-dissolving" species even means. This terminology becomes especially confusing on page 8, lines 10-15, where a monoacid is treated as "dissolving" but the anions and cations are treated as "nondissolving" in Eq. 11. This equation is supposed to give H+ ion concentration from the difference between anions and cations, so I don't understand why the additional term "c_i" is even included here."

We changed the terminology, as 'non-dissolving' is scrapped for 'passive' to remain, which is now introduced by formal definition along with 'dissolving'. The monoacid within Eq. 11 is the only species whose semi-volatile and time-depending nature is considered at this point: it is the dissolving species while all others are passive. We feel this change in terminology and the adaptations to the text clarify the issue.

6) "The derivation of Eq. 9 is also very confusing. First, please clearly define the terms a, b, and c of the generic differential equation $dx/dt = ax^2 - bx + c$. Then show the solution using the same notations."

We partially followed the reviewer's request, and reformulated the expression of Equation 9, as we now state parameters a, b and c. However, it is not reasonably possible to formulate the solution as an explicit function of these parameters. This is the reason why parameters λ and B had been introduced in the first place. Note that there was a typing error within Eq. 9, which is corrected as the parameter b is squared now inside the square root function.

7) "Will the numerator in Eq. 15 always be positive? What happens if a species in a given bin has a tendency to evaporate during a time step (e.g., HNO3 displacing HCl from sea salt)?" It has to be ensured that the numerator of Equation 15 is always positive. Within the solver this is ensured via the use of the absolute value function. The fact that it was missing here is due to a typing error, which we corrected.

8) "How does the dynamic solver handle simultaneous mass transfer of H2SO4, HNO3, HCl, and NH3 to a size distributed aerosol? It seems mass transfer of H2SO4 is not included in the derivation of the dynamic solver equations. Also, none of the box model test cases include gas phase H2SO4 that condenses along with HNO3, HCl, and NH3."

H2SO4 is not currently treated by HyDiS as (1) it is assumed to be non-volatile and (2) the condensation of non-volatiles is formally considered to be a separate process. In principle it could be treated as a semi-volatile species by the solver if found appropriate and termodynamic data is made available, and provided that some slight adaptations to the chemical equilibrium solver are made, considering that the maximum number of chemically fully interacting species that may be accounted for by the solver may not exceed 3. Non-volatile species are treated within the combined condensation and nucleation routine of the microphysics scheme. HyDiS is the last routine to be invoked by the aerosol model. Concurrent condensation of H2SO4 and dissolution of HNO3 and NH3 is not shown within the box modelling experiments as we put priority on showing the transition of the system towards forced dynamic equilibrium. We have made changes within Section 4 and Section 5.2 for improved clarity with respect to these circumstances.

Question 9 is split in two:

9a) "While the present box model tests are useful in showing the benefits of the hybrid solver over the equilibrium approach, they do not demonstrate the accuracy of the new dynamic solver introduced here. To evaluate accuracy, it is necessary to compare the dynamic solver for monodisperse aerosol (similar to the example shown in Figure 1) and 4 size bins (as already shown in series 1 and 2) against a benchmark dynamic solver (e.g., LSODE) with strict error tolerances for a range of initial gas concentrations (of H2SO4, HNO3, HCl, and NH3) and aerosol sizes, concentrations, and compositions."

The reviewer assumes that the credibility of the benchmark solver that we use is not given and that an established stiff solver of ordinary differential equations, like lsode, should be used instead. We acknowledge that the reviewer's suggestion is justified in the context of insufficient explanation of our

methodology and the lack of clarity that surrounded Figure 1. However, although Zaveri et al 2008 used lsode as a benchmark, this is no absolute proof that it is the better choice in any case. We actually believe that the Jacobson 1997 Analytical Predictor for Dissolution (APD) we use as a benchmark is more appropriate, for the reasons that we will now expand upon. A solver may serve as a benchmark, if it is (1) mathematically precise, (2) formally different from the one it is compared against, and (3) compatible with the numerical formalism it is embedded in. First, although it has a propension for oscillations at larger timesteps, the Jacobson 1997 APD is mathematically sound, as by inspection for an internal timestep $\delta t \rightarrow 0$ its numerical integration method tends to the mathematically correct solution. Its capacity to deliver precise results is illustrated by Zaveri et al 2008 (though for the Jacobson 2005 semi-implicit version of the APD, which is formally similar to a large degree), as lsode and the APD tend to give similar results. Second, for Zaveri et al the use of the fully dynamic 1997 exponential APD as a benchmark was not appropriate as formally too close to its 2005 semi-implicit cousin. With HyDiS and its mixed dynamic and equilbrium approach, its selective setting to equilibrium of species within non-equilibrium bins and its use of the pseudo-transition approach, the fully dynamic APD is formally dissimilar. Third, the APD is the better match to HyDiS and its numerical formalism: (1) it is already in use in combination with an as large as possible timestep for species in bins that are simulated dynamically, a comparison between the hybrid and the fully dynamical runs may thus serve to demonstrate that HyDiS chooses the internal timestep without loss of *relative* accuracy, and (2) the APD actually tends to be more precise than lsode provided that the internal timestep is set to an appropriate value. Isode solves for all species within all size bins concurrently, while the APD solves for all size bins however separately for each species, which might appear to be a clear advantage for lsode. However, lsode keeps the parameters constant during the entire overall timestep Δt , while the APD updates them after each internal timestep δt . For a chemical process that involves relatively constant parameters lsode definitely is the better stiff solver, but for dissolution and its stiffness causing fast changing parameters, as given by the water content, the activity coefficients and surface pressure, it might not be. Quite on the contrary, it will introduce an amount of imprecision that will not be readily quantifiable. It is thus hard to tell whether the use of lsode is more accurate via the accurate simultaneous solution of a system of stiff ODE's, or actually less accurate via the variability of the parameters. The only ways we can think of to overcome this uncertainty would be to (1) compare runs with activity coefficients and water content held constant, which might not be the best choice for the purpose of solver verification, or (2) attempt to formally resolve the higly non-linear properties of the parameters via their explicit inclusion as variables, which would be using a sledgehammer to crack a nut at best or might turn out to be not feasible at worst, or (3) drastically reduce the overall timestep at which lsode is used, to an order of magnitude that is more or less similar to the one that is used internally by the APD, which would be largely tantamount to the use of the APD as a benchmark solver, as demonstrated by Zaveri et al 2008. For all of these reasons we chose to use the Jacobson 1997 scheme, which is mathematically precise if the internal timestep is chosen appropriately. This we did by simple inspection, as sketched within Figure 1 for a monodisperse aerosol and total species amounts of 1 ppt: 30 seconds induce oscillation, and 10 seconds are precise to the extent that the simulation is graphically indistinguishable from a run at a much shorter timestep (therefore not shown). We have added a paragraph to the text in order to describe and motivate our choice of the APD as the benchmark solver.

9b) "The predicted equilibrium (after sufficient time) gas and aerosol concentrations (including aerosol pH) for the monodisperse test cases must also be compared to a benchmark thermodynamics model such as AIM (available online) to evaluate the accuracy of the thermodynamics treatment in the present solver. For example, see the dynamic solver evaluation done in Zaveri et al. (2008). Such an evaluation against a benchmark solver is especially warranted in the light of the several discrepancies found in the results of the dynamic solver shown in Figure 1 (see #3)."

The reviewer suggests that we use AIM as a benchmark for the equilibrium solver. Interestingly this is a possibility that we had considered before submission but ultimately had decided against it. From our point of view, the scope of this publication is not so much whether the equilibrium that is determined is accurate thermodynamically (this was done by Topping et al 2009), but rather whether the solver is numerically correct, which is demonstrated as fully dynamic and hybrid runs converge towards full equilibrium, thus validating each other mutually. Also, as pointed out by the reviewer, the online version of AIM does not allow for a size discretized aerosol. We would thus have to add another experiment with a monodisperse aerosol to an already lengthy paper. We have added one sentence detailing that the thermodynamic scheme was tested against AIM by others.

10) "The main goal of the present work is to introduce a new hybrid solver that is computationally efficient. But since any solver can be made efficient by compromising its accuracy, it becomes necessary to evaluate computational efficiency as a function of accuracy. The CPU costs presented for the various dynamic solvers in Table 1 are of little use without stating their accuracies against a benchmark solver (see #9)."

The reviewer asserts that the CPU times are of little use in the absence of a reliable reference as given by a benchmark solver. For the reasons given within 9a) we believe that the Jacobson 1997 APD, if used appropriately, actually is a valuable benchmark solver. No changes to the text apart those made in the context of point 9a).

11) "As the authors have already acknowledged, the comparison of the computational cost of the present solver with that of MOSAIC is fraught with many issues: different model configurations and chemical/physical complexities, computer hardware and computing architectures, etc. Also, the 125 μ s CPU cost for MOSAIC quoted here includes microphysical calculations (in addition to gas-particle mass transfer and thermodynamics) whereas the 20 μ s given for the present hybrid solver appears to be for gas-particle mass transfer and thermodynamics calculations only. Furthermore, the CPU costs given in Table 5 for cases 4-7 (aqueous particles only) range from approx. 20-40 μ s (depending on the case, hardware, and compiler), which is more directly comparable to the CPU cost presented here for the hybrid solver. Having said that, the accuracy and efficiency of both solvers should be evaluated for the same set of problems on the same machine for the comparison to be meaningful."

The reviewer states that a comparison with MOSAIC in terms of CPU time as done within the manuscript is of questionable relevance due to dissimilarity of both the computing facilities that are

used and the schemes themselves. We agree that the relevance of the comparison is limited. However, in this respect we do not believe that the comparison would not carry meaningful information. The fact that we overlooked that for MOSAIC the microphysics are included in their estimation of CPUtime does not affect our conclusion that the expense should be of the same order of magnitude, thus demonstrating our due caution. We believe that our conclusion carries a useful piece of information to the reader, considering that a more detailed assessment is reserved to a global modelling framework that is more comparable, which is not currently available to us. The reviewer might have suggested to carry out the comparison with box model simulations instead, as done by Zaveri et al 2008. The relevance of box model comparisons of computation time is also limited, as these may not be representative to the parameter space that is encountered within a global modelling environment. Likewise, cases 4-7 within Zaveri 2008 might not be representative to the computational expense that is encountered in relationship with fully liquid particles, as the small particle sizes, which should require a smaller timestep, are not assessed with the given monodisperse setups. At this point, we have to mention that reviewer #1 seems to appreciate and does not criticize the way we established the comparison of CPUtime, on the contrary he would favour a similar comparison between the simulated and the observed aerosol composition. Within this partially conflicting situation we would like to leave it to the editor as to whether more CPUtime comparisons are essential, and as to how these should be done. In the meantime, we have further relativised our assessment within Sections 5.4 and also 6, in accordance with the reviewer's observations.

The following questions will be answered together, as related:

12) "Table 2: In GLOMAP sea-salt chloride is treated as non-volatile. Then how do H2SO4 and HNO3 condense on sea salt aerosol without evaporating HCl? Non-volatile treatment of HCl becomes problematic especially for condensation of HNO3, because both HNO3 and HCl are semivolatile and the extent of HNO3 partitioning crucially depends on HCl." and 13) "How is HNO3 uptake on calcite containing dust particles treated in GLOMAP?"

The reviewer asks a question with respect to the representation of the volatility of HCl in the context of sea salt within Glomap, and the representation within Glomap of gas/solid phase exchange with respect to calcite. We are aware that these are important questions for the simulation of the atmospheric aerosol, although of limited relevance in the context of the present publication (see (1)). HyDiS may account for the chemical interaction of a maximum of 3 dissolving species. As such it may account for the interaction of HNO3, NH3 and HCl, provided that they are comprised within the atmospheric chemistry scheme of the hosting aerosol model. As mentioned within Section 5.2, we cannot treat HCl as a semi-volatile in the present version of Tomcat-Glomap. Gas/solid phase exchange is not currently part of Glomap and it is a process that is not treated by HyDiS, this also applies to calcite. We have made additions to Sections 5.2 and 6 that detail these limitations.

Minor Comments

p. 21. 10: order of acid and base is changed.

Fig. 11: resolution of figure is improved.

Size-resolved simulations of the aerosol inorganic composition with the new hybrid dissolution solver HyDiS-1.0 – <u>d</u>Description, evaluation and first global modelling results

François Benduhn^{1,2}, Graham W. Mann¹, Kirsty J. Pringle¹, David O. Topping⁴³, Gordon McFiggans⁴³, Kenneth S. Carslaw¹

¹School of Earth and Environment, University of Leeds, Leeds, UK.

²Max Planck Institute for Chemistry, Mainz, Germany.

5

³National Centre for Atmospheric Science, School of Earth and Environment, University of Leeds, Leeds, UK.

⁴³Centre for Atmospheric Science, School of Earth, Atmospheric and Environmental Science, The University of Manchester,
 Manchester, UK.

Correspondance to: François Benduhn (benef5@yahoo.fr)

Abstract. The dissolution of semi-volatile inorganic gases such as ammonia and nitric acid into the aerosol <u>liquidaqueous</u> phase has an important influence on the composition, hygroscopic properties and size distribution of atmospheric aerosol particles. The representation of dissolution in global models is challenging due to inherent issues of numerical stability and

- 15 computational expense. For this reason, simplified approaches are often taken, with many models treating dissolution as an equilibrium process. In this paper we describe the new dissolution solver HyDiS-1.0 that was developped for the global size-resolved simulation of aerosol inorganic composition. The solver applies a hybrid approach, which allows some particle size incrementclasses to establish instantaneous gas-particle equilibrium while others are treated time dependently (or dynamically). Numerical accuracy at a competitive computational expense is achieved by using several tailored numerical
- 20 formalisms and decision criteria, such as for the time- and size-dependent choice between the equilibrium and dynamic approaches. The new hybrid solver is shown to be in good to excellent agreement with a fully dynamic <u>benchmark</u> solver and to have numerical stability across a wide range of numerical stiffness conditions encountered within the atmosphere. We present first results of the solver's implementation into a global aerosol microphysics and chemistry transport model. We find that (1) the new solver predicts surface concentrations of nitrate and ammonium in reasonable agreement with
- 25 observations over Europe, the US and East Asia; (2) models that assume gas-particle equilibrium will not capture the partitioning of nitric acid and ammonia into Aitken mode sized particles, and thus may be missing an important pathway whereby secondary particles may grow to radiation and cloud-interacting size; and (3) the new hybrid solver's computational expense is modest, at around 10% of total computation time in these simulations.

1 Introduction

The inorganic composition of <u>the aqueous phase of atmospheric aerosol particles</u> is continuously subject to exchange with the gas phase. Whereas H_2SO_4 condenses irreversibly under tropospheric conditions, semi-volatile species such as H_2O , HNO_3 , HCl and NH₃ may re-evaporate from the aerosol <u>aqueous</u> phase depending on the temperature and chemical

5 composition of the atmosphere. NH₃ combines with <u>H₂O water in the aerosol liquid phase</u> to give NH₄OH, which along with HNO₃ and HCl tends to dissociate in the aerosol <u>aqueous</u> liquid phase, with water taking the role of a solvent. This combination of condensation and partial dissociation is usually referred to as gas-particle conversion or dissolution. The dissolution of semi-volatile gases into the aerosol phase has an ambiguous effect on aerosol particle size. The

dissolution of NH₃ within acidic H₂SO₄ particles decreases their hygroscopicity, resulting in a decrease in water content and

- 10 particle size, while chemical interaction between a dissolving acid and a dissolving base, such as <u>NH₃ and HNO₃ and NH₃</u>, may result in a substantial increase in particle size due to the considerable amount of dissolved massiter and water that is <u>bound by it</u>. Variations in particle size and hygroscopicity affect aerosol-radiation and aerosol-cloud interactions, with influences on climate processes such as atmospheric circulation and the water cycle. Because the chemical composition of particles varies substantially with size, the effects of these semi-volatile gases are non-uniform across the particle size
- 15 distribution. Dissolution affects atmospheric chemistry via its influence on atmospheric composition and also impacts aerosol heterogeneous chemistry via the aerosol surface and the pH of the aerosol <u>liquidaqueous</u> phase. Finally, the dissolution-mediated modification of the aerosol radiative properties will also affect the photolysis reactions within the atmosphere. The potential of dissolved inorganic species, especially NH₃ and HNO₃, to act upon these climatologically relevant factors is high, as they are a major constituent of the atmospheric aerosol, especially in polluted areas (e.g. Adams et
- 20 al., 1999, Feng and Penner, 2007, Metzger and Lelieveld, 2007, Pringle et al., 2010, Morgan et al., 2010). The global simulation of the aerosol inorganic <u>aqueous</u> chemistry is computationally expensive due to the complexity of the process and the numerical stiffness property of the related differential equations. The so-far adopted approaches may be divided into equilibrium approaches (e.g. EQUISOLV, Jacobson et al., 1996, Jacobson, 1999b; ISORROPIA, Nenes at al., 1998, Fountoukis and Nenes, 2007; EQSAM, Metzger et al., 2002a, Metzger and Lelieveld, 2007), and selectively dynamic
- 25 so-called hybrid approaches (HDYN, Capaldo et al., 2000, see also, Trump et al., 2015); and fully dynamic approaches (MOSAIC, Zaveri et al., 2008). The motivation for equilibrium approaches is that the stiffness of the system leads to numerical instability that may involve prohibitive computational expense when integrated in time. Hybrid approaches seek to reduce the computational expense by assuming that only a fraction of the aerosol size distribution is in equilibrium with the gas phase. This fraction in equilibrium is usually the smaller end of the size distribution, which would require the shortest
- 30 integration time step if treated kinetically. The remaining fraction of the <u>size</u> distribution is treated dynamically because the larger particles are not in equilibrium with the gas phase, as shown by theoretical studies (Wexler and Seinfeld, 1990; Meng and Seinfeld, 1996) and model investigations that demonstrate a much better agreement with observations (e.g. Hu et al., 2008).

The obvious advantage of a fully dynamic approach is its accuracy, provided that the mathematical stiffness properties of dissolution are tackled through the choice of an appropriate numerical integration scheme. Although fully dynamic solvers may prove to be computationally efficient, due to numerical and system dynamical constraints to the choice of the time step, their computational efficiency cannot be increased beyond a certain threshold, unless they yield imprecise and/or unstable

- 5 results (Zaveri et al., 2008). Hybrid schemes have been criticised, as they may not be able to fully resolve the dynamics of the cuncurrent dissolution of several species that interact chemically due to their partial equilibrium assumption. In particular, due to competition effects smaller particles may, in some conditions, not be at equilibrium in the presence of larger non-equilbrium particles (Wexler and Seinfeld, 1992). The equilibrium assumption may thus lead to a misrepresentation of the redistributing flux of semi-volatile species within a size discretized aerosol through the gas phase
- 10 (Zaveri et al., 2008). Although this latter misrepresentation appears to be inherent to any partial equilibrium assumption, the extent and the frequency of occurrence of the resulting inaccuracy remains unclear. Inherent limitations to the hybrid approach may prove to be overcome satisfactorily if the choice of the fraction of the size spectrum that is assumed to be in equilibrium is carefully made. Also, these limitations need to be balanced against the fact that a hybrid approach may enable a more accurate representation of other system dynamical properties, such as the species' chemical interaction. The
- 15 computational efficiency is another fundamental aspect of a global modelling scheme, and it is therefore important that its time stepping is flexible and not limited in principle.

In t<u>T</u>his study <u>describes and evaluates</u> the new hybrid solver <u>HyDiS version 1.0 forof</u> the dissolution of <u>semi-volatile</u> inorganics into the aerosol <u>aqueousparticle</u> phase <u>HyDiS version 1.0 is described in detail</u>. The solver <u>usesis based on</u> a <u>hybridnew mechanformalism</u> that <u>strives to</u> combines computational efficiency with <u>an</u> accurate representation of the

- 20 dynamical property of the process. To achieve this, the solver makes use of existing numerical methods and concepts, such as the semi-implicit and semi-analytical integration method for dissolution that was developed by Jacobson (1997), the mixed time integration method (Zhang and Wexler, 2006; Zaveri et al., 2008) or the analytical approach for the estimation of the equilibrium composition (Nenes et al., 1998), some of them modified fundamentally. Other methods are novel as they have been developed specifically for the purpose of HyDiS-1.0. All of these numerical methods are applied within different
- 25 branches of an overall formalism that is based on the system dynamical and numerical properties of dissolution and assorted with a set of specific decision criteria for the distinction among dynamical regimes. The solver is not a complete gas-particle exchange solver, as it does not take into account the exchange between the gas phase and the particle solid phase, does not consider neither the existence of mixed phase particles nor the role of organics. Section 2 describes the dynamical properties of the simultaneous dissolution of several inorganic compounds and the numerical constraints these put on the design of an
- 30 efficient hybrid solver. Section 3 explains the mechanism of the solver in detail. Section 4 evaluates the solver against fully dynamical model runs in a box model configuration. Finally Section 5 presents first results from an implementation of the scheme into a 3-D chemistry transport model to demonstrate its computational efficiency and numerical reliability.

2 Dynamical properties of dissolution

2.1 Non-linear properties

To understand what turns dissolution into a tedious numerical problem, it is necessary to analyse its dynamical properties in detail. This section analyses these properties using the example of HNO_3 and NH_3 dissolving into an aqueous solution of

- 5 H_2SO_4 . The concurrent dissolution of a base and an acid into an acidic solution is characterised by a positive feedback phenomenon involving the two dissolving species. Initially, the dissolution of HNO_3 is impeded via the strong acidicity property of H_2SO_4 . Conversely, the continuous neutralisation of an acidic solution by a dissolving base such as NH_3 will eventually prevent the dissolution of further basic matter. However, in the presence of both a dissolving acid and base, the continuous neutralisation by the base may be effectively counterbalanced by the dissolving acid, thus giving way to further
- 10 dissolution of basic matter. The effective interaction between the two dissolving chemicals causes numerical stiffness, as there is one variable, in this case the pH of the solution, that is contrarily influenced by the two dissolving species. The transition from an initially binary solution of H_2SO_4 and H_2O to a solution in equilibrium with gas phase HNO₃ and NH₃ may be divided into 3 stages (see Fig. 1):

1) Initial neutralisation of the particle. The solubility of NH₃ is high, while the particle is too acidic for large amounts of

15 HNO₃ to dissolve. In an atmosphere with significant amounts of HNO₃ and NH₃ there is a momentary contrast of their equilibration times because particulate HNO₃ tends to be in equilibrium with the atmosphere whilst NH₃ partitions quickly into the liquidaqueous phase in the presence of a large pressure gradient.

2) Efficient interaction between HNO_3 and NH_3 . Both species are dissolving because the pH is high enough for HNO_3 and still low enough for NH_3 to dissolve. During this phase particle pH serves as the factor that controls the dissolution of both

20 species.

3) Asymptotic convergence towards equilibrium. The interaction of HNO_3 and NH_3 is reduced as each species is separately close to equilibrium with the <u>liquidaqueous</u> phase.

Dynamically speaking the system is kinetically limited during Stage 1 via the contrast of the particle surface and atmospheric pressures of NH₃. Consequently, during this stage NH₃ is the driving species, while HNO₃ may be described as the following

- species. In contrast, during Stage 2 the system is chemically limited. It is the stage of effective interaction between NH_3 as a base and HNO_3 as an acid. The pressure contrast between the <u>liquidaqueous</u> and the gas phase of both NH_3 and HNO_3 is substantial enough for the interaction to be fast. Stage 3 is also chemically limited, however both species are close to equilibrium. In contrast to the preceding, it is the stage of ineffective interaction between the acidic and the basic species, as their effective dissolution is hampered by the lack of pressure contrast. As will be seen in the next section, the specific
- 30 dynamical properties of each stage also entail specific numerical issues.

2.2 Numerical stiffness properties

A chemical system may be said to be numerically stiff if its interacting variables show disparate equilibration times, such that the time step of numerical integration has to be adapted to those variables that drive the system and vary quickly (e.g. Zaveri et al., 2008). Here, we choose to generalize the concept of numerical stiffness to the following *ad hoc* definition: A

5 system of one or more variables is numerically stiff when its dynamical properties require an integration time step that is small in comparison to the amount of time that is required for its transition to equilibrium.
 Following this definition each of the above stages of equilibration of the particle liquidaqueous phase with the gas phase may

be associated with a specific form of numerical stiffness, as follows:

1) During Stage 1 the following species' equilibration time is much shorter than the one of the driving species. This property

10 points to the usual definition of numerical stiffness, except that the species with the shorter equilibration time is not driving the system. A time step that is too large causes consecutive over- and undershoots for the following species, which may result in oscillating model results. Furthermore, under some conditions the oscillations may grow from time step to time step, and may eventually produce non-physical values.

2) During Stage 2 the system is evolving rapidly in the presence of moderate vapour pressure gradients and efficient

- 15 chemical interaction. A scheme of numerical integration that catches the interactive nature of the system may still misrepresent its dynamics when the time step is inappropriately large. Figure 1 shows a clear deviation of the large time step values from the small time step values during this stage, such that inaccurate model results may be obtained if the transition time through this stage is sufficiently large relative to the integration time step of the model.
- 3) The numerical stiffness associated with Stage 3 may be described as follows: Each species taken individually shows an equilibration time that is short relative to the entire transition period. As explained for Stage 1 and shown by Fig. 1, this may result in an oscillatory behaviour, with the inherent risk of non-physical values. As the chemical interaction between the dissolving species is considerable, the propensity for oscillation is substantial and more pronounced than within Stage 1, as shown by Figure 1.

4) Finally, numerical stiffness may arise as follows. During Stage 3, the system is interacting chemically, albeit the

- 25 liquidaqueous phase is typically close to its equilibrium composition. However, effective chemical interaction may also set in early on in connection with low vapour pressure gradients. The resulting situation is thus a hybrid between Stage 2 and 3. We found this form of stiffness to occur in the context of elevated HNO₃ and NH₃ concentrations that result in the formation of ammonium nitrate particles. During the formation process of ammonium nitrate the fraction of dissolving species remaining within the gas phase typically becomes very low. However, in the presence of size-resolved aerosol particles that
- 30 are in disequilibrium among each other, their equilibration timescale will become very long, as the equilibration flux needs to transit through the bottleneck of low gas phase concentrations, thus resulting in further numerical stiffness. In Figure 1 the concentrations of ammonia and nitric acid are too low for this variety of numerical stiffness to occur. The artefacts obtained

remind those associated with the numerical stiffness that may occur during Phase 2. Whereas the third variety of numerical stiffness may arise on its own, the fourth variety always transitions slowly to the third one.

3 Solver description

The hybrid dissolution solver treats dissolution selectively as a dynamic or static process. Accordingly, both dynamic and

- 5 equilibrium formulations of dissolution were developed and implemented into an appropriate decision framework. The dynamic and equilibrium sub-solvers are specified within sections 3.1 and 3.2, respectively, whereas their formal linkage is detailed within section 3.3. An alternative dynamic scheme is presented within section 3.4, which allows the bias in equilibrium solutions in relationship with computational efficiency considerations to be reduced. Finally, section 3.5 provides an overview on the entire mechanism, linking the formalism of the solver to the numerical stiffness properties of
- 10 dissolution.

Namingotational conventions:

The reversible condensation and dissolution of semi-volatile species into the aerosol aqueous phase is simulated with the HyDiS-1.0 dissolution solver. For reasons of convenience, these species will henceforth be qualified as *dissolving* species. As given by the formalism of the solver the semi-volatile nature of some species is neglected at times. Species whose semi-

15 volatile nature is momentarily neglected and non-volatile species are bound together via their common qualification as *passive* species.

In the following subscript letters i,j,k,n,t relate a variable to an aerosol size <u>binclass</u> i, a dissolving species j, a <u>non dissolving</u> (=passive) species k, at a particular integration time step or equilibration iteration number n, at a time t, respectively. Exceptionally they may be placed as superscripts in order to differentiate from various additional variable attributes.

20 Exponents occur as numbers only.

3.1 Dynamic dissolution

The flux of dissolving molecules *n* onto a particle surface element *dS* is (e.g., Pruppacher and Klett, 1997):

$$d\left(\frac{\partial n_j}{\partial t}\right) = \nabla \cdot \left(\frac{D}{kT} \nabla p\right) dS ,$$

Eq. 1

25 where $D[m^2 s^{-1}]$ is the Brownian diffusion coefficient in the gas phase corrected for condensation in the dynamic regime and for sticking efficiency, $k[JK^{-1}]$ is the Boltzmann constant, T[K] is the absolute air temperature, and p[Pa] is the partial pressure of the diffusing species. Assuming pseudo-equilibrium and constant temperature within the volume of air within which diffusion takes place, one obtains after integration over particle surface:

$$\frac{\partial c}{\partial t} = 4\pi r D N \left(C - \frac{p_s}{kT} \right),$$

Eq. 2

5 where $c [m^{-3}]$ is the aerosol liquidaqueous phase number concentration of the dissolving species (molecule number per unit volume air), r [m] is the radius of the aerosol particles, $N [m^{-3}]$ is the aerosol particle number concentration, $C [m^{-3}]$ is the gas phase number concentration of the dissolving species, and p_s is the vapour pressure of the dissolving species at the particle surface.

Surface partial pressure may be related to the number concentration of dissolved molecules via the so-called dimensionless Henry coefficient H', which for a mono-acid is defined as follows (Jacobson, 1999a):

$$H' = \frac{ckT}{p_s} = \frac{NN_A m_w}{\gamma_{HA}^2 [H^+]} kTH$$

Eq. 3

where $m_w [kg]$ is the aerosol water mass per particle, $N_A [mol^{-1}]$ is the Avogadro constant, $\gamma_{HA} [-]$ is the mean molal activity coefficient of the dissolving monoacid HA, $[H^+]$ is the molal proton concentration in the aerosol <u>liquidaqueous</u> phase and H15 $[mol^2 kg^{-2} Pa]$ is the Henry constant of the dissolving mono-acid given by:

$$H = \frac{\gamma_{HA}^2 \left[H^+ \right] \left[A^- \right]}{p_s}$$

Eq. 4

Similar expressions may be derived for a dissolving base.

10

In the preceding expression, the partial dissociation property of the dissolving species is neglected, which is an underlying

- 20 assumption for HyDiS-1.0. It will allow us to reduce the number of degrees of freedom of the considered chemical system by one unit for each dissolving species. In doing so other properties, such as the species' chemcial interaction, may be taken into account more throroughly, as analytical solutions may be derived along with a critical reduction of the degree of the respective resolving equations. We have seen in the preceding section that the chemical interaction between acids and bases plays an essential role to the numerical stiffness property of the system.
- 25 In contrast to the Henry constant, the dimensionless Henry coefficient does not express a physical law. Its value expresses the ratio between the partial pressure of the dissolved molecules if they were evaporated and their actual surface pressure. These values are unequal due to chemical interaction among the species that make up the aerosol liquidaqueous phase, and

the resulting partial dissociation of the dissolving acid or base. As such the dimensionless Henry coefficient is not a constant, but varies as a function of the pH and the mean activity coefficient. This feature will turn out to be important when Eq. 2Eq. 2 is numerically integrated in time.

Within the framework of a discretised representation of aerosol particle sizes, dissolution of several species may take place

5 onto several aerosol size <u>binclasses</u> simultaneously. If only one species is considered and the chemical interaction of several species is neglected, then an implicit semi-analytical solution may be derived when the following equation that results from the combination of Eq. 2Eq. 2 and Eq. 3Eq. 3 is considered:

$$\frac{\partial c_i(t)}{\partial t} = 4\pi r_{i,t} D_{i,t} N_{i,t} \left(C_{t+\delta t} - \frac{c_i(t)}{H'_{i,t}} \right).$$

10 Combining the semi-analytical solution of the preceding equation (Jacobson, 19979a):

$$c_{i,t+\delta i} = H'_{i,t} C_{t+\delta i} + \left(c_{i,t} - H'_{i,t} C_{t+\delta i}\right) \exp\left(-\frac{4\pi r_{i,t} D_{i,t} N_{i,t}}{H'_{i,t}} \delta t\right)$$

with the mass balance equation:

$$C_{t+\delta t} + \sum_{i} c_{i,t+\delta t} = C_{tot}$$

15

yields for $C_{t+\delta t}$ (Jacobson, 199<u>7</u>9a):

$$C_{t+\delta t} = \frac{C_{tot} - \sum_{i} c_{i,t} \exp\left(-\frac{4\pi r_{i,t} D_{i,t} N_{i,t}}{H'_{i,t}} \, \delta t\right)}{1 + \sum_{i} H'_{i,t} \left(1 - \exp\left(-\frac{4\pi r_{i,t} D_{i,t} N_{i,t}}{H'_{i,t}} \, \delta t\right)\right)}.$$

Eq. 8

Although the preceding set of equations is unconditionally stable, as shown by inspection for $\delta t \rightarrow \infty$, $c_i = H'_i C$ and $C = C_{tot}$ 20 $/(1 + \Sigma H'_i)$, such that no unphysical values may occur, it should be noted that the convergence to a static equilibrium between the aerosol liquidaqueous phase and the gas phase is not unconditionally ensured: the solution given by Eq. 6Eq. 6 and Eq. 8Eq. 8 is disconnected from the pH of the particle liquidaqueous phase, as the dimensionless Henry coefficient is held

Eq. 5

Eq. 7

Eq. 6

constant. In addition, the simultaneous dissolution of several species affects the mean activity coefficient, which is also held constant. The integration time step may thus not be chosen arbitrarily otherwise oscillatory behaviour may occur.

The preceding semi-analytical solution is therefore best used under conditions of relatively quick variations of the gas phase concentrations and a relatively stable pH of the aerosol <u>liquidaqueous</u> phase, as for instance in the presence of a large

5 amount of sulphuric acid. In the event of a monoacid dissolving into a particle with a highly variable particle pH and a relatively stable gas phase concentration, the following semi-analytical solution may prove to yield more stable results:

$$c_{i,t+\delta t} = \frac{\lambda_1 + \lambda_2 B(\lambda_1, \lambda_2) \exp((\lambda_2 - \lambda_1) \delta t)}{a(1 + B(\lambda_1, \lambda_2) \exp((\lambda_2 - \lambda_1) \delta t))},$$

with:

$$B(\lambda_{1},\lambda_{2}) = \frac{ac_{i,t} - \lambda_{1}}{\lambda_{2} - ac_{i,t}}, \qquad B(\lambda_{1},\lambda_{2}) = \frac{ac_{i,t} - \lambda_{1}}{\lambda_{2} - ac_{i,t}},$$

$$10 \quad \frac{a = \frac{k_{i,t}\gamma_{HA}^{2}}{\alpha^{2}HkT}, \quad \alpha = N_{i,t}N_{A}M_{w}, \quad k_{i,t} = 4\pi r_{i,t}D_{i,t}N_{i,t}}{\lambda_{1,2} = -0.5 \cdot a\sigma_{i,t} + /-\sqrt{0.25 \cdot a\sigma_{i,t} + ak_{i,t}C}} \qquad \lambda_{1,2} = -0.5 \cdot b + /-\sqrt{0.25 \cdot b^{2} + ac}$$

$$\sigma_{i,t} = \left(\sum_{k} n_{k}A_{k,i,t} - \sum_{k} m_{k}B_{k,i,t}\right) \qquad b = a\sigma_{i,t}, \quad c = k_{i,t}C, \quad \sigma_{i,t} = \left(\sum_{k} n_{k}A_{k,i,t} - \sum_{k} m_{k}B_{k,i,t}\right)$$
Eq. 10

Eq. 9 Eq. 9 is a semi-analytical solution to the generic differential equation $dx/dt = -ax^2 - bx + c$ resulting from the combination of Eq. 2Eq. 2, Eq. 4Eq. 4 and the ion balance equation given by:

$$H_{i,t}^{+} = c_{i,t} + \sum_{k} n_k A_{k,i,t} - \sum_{k} m_k B_{k,i,t}$$

15

where c_i denotes the dissolving monoacid for which Eq. 9 is solved, and $A_k [m^{-3}]$ and $B_k [m^{-3}]$ stand for are passive nondissolving (as indicated by the choice of subscript k) anions A^{n-} and cations B^{m+} in the aerosol liquidaqueous phase, respectively.

In accordance with Eq. 4. Note that as an approximation the dissolving monoacid is assumed to dissociate entirely. The liquidaqueous phase of the atmospheric aerosol contains in general a variable fraction of sulphuric acid whose degree of dissociation should be taken into account when calculating particle pH. Within the preceding equation OH is presumed to be

Eq. 11

Eq. 9

negligible relative to H^+ . Similarly to the negligence of the partial dissociation property of the dissolving species, t \mp his assumption is an underlying simplification within the framework of the hybrid solver described in this paper. A model H⁺=0 is thus to be associated with an actually neutral pH=7. In this context Eq. 6Eq. 6 may yield a negative concentration of H⁺, both via an evaporating acid and a condensing base, as the variation of the pH is not taken into account within the

normalised Henry coefficient H'. In this context, which adds to the numerical stiffness property's requirements, the choice of 5 an appropriate time step δt is all the more essential.

Both the choice between Eq. 6Eq. 6 and Eq. 9Eq. 9, and the choice of an appropriate time step require an appropriate criterion that stands for a representative variation of the gas and liquidaqueous phase compositions and/or the typical amount of time to reach that variation. In the framework of these equations, which neglect chemical interactions among several

species dissolving concurrently, the characteristic variation or time scale of the aerosol liquidaqueous phase is inherently 10 specific to each dissolving species. Consequently, the time step that will ultimately be chosen must not exceed the one that is characteristic of the species that for some specific reason is chosen as the most relevant one. The specific upper time step limit to be used in conjunction with the above equations should therefore fulfil the following condition:

$$\delta t_{j,i,t} = \kappa_{\delta t} t_c^{j,i,t}, \quad \kappa_{\delta t} \leq 1,$$

Eq. 12

Eq. 13

15

 $\kappa_{\delta t}$ being the numerical time step criterion for dissolution in the dynamic mode. In this study we choose $\kappa_{\delta t} = 1.0$. The characteristic equilibration time t_c of the aerosol particles contained in size incrementclass i with respect to a dissolving and supposedly non-interacting species *j* may be related to an approximate equilibrium composition, solving:

$$\left(\left[H^{+} \right]_{eq}^{i,j,t} \right)^{2} + \left(\alpha_{i,t} - \sigma_{r}^{i,j,t} \right) \left[H^{+} \right]_{eq}^{i,j,t} - \alpha_{i,t} \sigma_{r}^{i,j,t} - \frac{\alpha_{i,t} A_{tot}^{i,j,t}}{\beta_{i,t}} = 0$$

$$\sigma_{r}^{i,j,t} = \frac{\sigma_{i,t}}{\beta_{i,t}}, \quad \alpha_{i,t} = \beta_{i,t} \frac{HkT}{\left(\gamma_{HA}^{i,t} \right)^{2}}, \quad \beta_{i,t} = N_{i} N_{A} m_{w}^{i,t}$$

20

where σ is the molal proton concentration in the aerosol liquidaqueous phase as given by the passive non-dissolving species. Eq. 13Eq. 13 gives the equilibrium proton concentration in the aerosol liquidaqueous phase following dissolution of the monoacid HA_i . Note that σ_r is conserved, as the particle water mass, the mean activity coefficient of the dissolving species and the degree of dissociation of sulphuric acid that is required for the estimation of σ_r are supposed to remain constant as an

25

approximation. The preceding equation is obtained when Eq. 4Eq. 4 and Eq. 11Eq. 11 are inserted into the aerosol size incrementclass relevant mass conservation equation of the dissolving species:

$$A_{tot}^{i,j,t} = C_{j,t} + c_{i,j,t}$$

11

The approximate equilibrium concentration $C_{eq}^{i,j,t}$ may then be obtained using Eq. 11Eq. 11.

Considering Eq. 5 Eq. 5, the amount of time to reach that equilibrium naturally exceeds:

5
$$\frac{t_{c}^{i,j,t} = \frac{1}{4\pi r_{i,t} N_{i,t} D_{j,t}} \cdot \frac{c_{eq}^{i,j,t} - c^{i,j,t}}{\max\left(C_{j,t}, \frac{c_{i,j,t}}{H_{i,j,t}'}\right)} t_{c}^{i,j,t} = \frac{1}{4\pi r_{i,t} N_{i,t} D_{j,t}} \cdot \frac{\left|c_{eq}^{i,j,t} - c^{i,j,t}\right|}{\max\left(C_{j,t}, \frac{c_{i,j,t}}{H_{i,j,t}'}\right)}.$$

As indicated by Eq. 6Eq. 6, the equilibration time is determined by an asymptotic variation of the amount of dissolved molecules: when the solution is getting closer to equilibrium, the pressure gradient, which acts as driving force, diminishes by the same amount. It is our purpose to assess for each individual species a characteristic time interval that is representative

- 10 of the kinetic constraints to dissolution. This time interval clearly cannot be infinite. We have seen above that Stages 2 and 3 of the particle <u>liquidaqueous</u> phase equilibration correspond to a period of effective or ineffective chemical interaction that is driving the evolution of the pressure gradient. The individual species' kinetically limited equilibration time is illustrated by the time interval of Stage 1. Its order of magnitude is generally not obtained as a function of the pressure gradient, which may reflect the chemical interaction during Stage 2 or 3, but rather by the *potential* of the gas phase or the <u>liquidaqueous</u>
- 15 phase to generate a condensation or evaporation mass flux, as expressed in the above equation.

Eq. 15Eq. 15 defines a characteristic time interval that may serve as maximum integration time step to the dynamic dissolution solver. It reflects the physical nature of its purpose and has the additional advantage of being computationally inexpensive. Among several size increment<u>classes</u>, the smallest value needs to be chosen in order to avoid numerical instability due to competition among the size <u>binclasses</u>. Equilibration is eventually driven by chemical interaction during

20 Stages 2 and 3, but this phenomenon cannot set in within a time interval that is smaller than the one required for individual species equilibration. For this reason it is possible to choose the maximum value among the dissolving species within one size increment<u>class</u>, and the overall integration time step reads:

$$\delta t_t = \min_i \left(\max_j \left(t_c^{i,j,t} \right) \right), \quad \delta t_t \le \Delta t$$

Eq. 16

25 where δt_t is the internal numerical integration time step chosen by the dynamic solver, and Δt is the relevant external time step of the model the dissolution solver is embedded into.

Eq. 15

The related approximate equilibrium concentration $C_{eq}^{j,t}$ and surface pressures $p_{S,eq}^{i,j,t}$ may serve to distinguish between gas and <u>liquidaqueous</u> phase driven dissolution. Dissolution is assumed to be <u>liquidaqueous</u> phase driven when the relative variation of the gas phase concentration is less than 1% of the relative variation of \mathbf{f} the surface pressure:

$$\frac{\left|C_{eq}^{j,t}-C^{j,t}\right|}{C^{j,t}} < \kappa_{g,l}^{i,j,t} \frac{\left|p_{S,eq}^{i,j,t}-p_{S}^{i,j,t}\right|}{p_{S}^{i,j,t}}, \quad \kappa_{g,l}^{i,j,t} = 0.01,$$

5

10

 $\kappa_{g,l}$ being the distinction criterion between gas and <u>liquidaqueous</u> phase driven dissolution in the dynamic mode.

When found to be <u>liquidaqueous</u> phase driven the semi-analytical scheme given by <u>Eq. 9Eq. 9</u> and <u>Eq. 10Eq. 10</u> for a dissolving mono-acid is preferred over <u>Eq. 6Eq. 6</u> and <u>Eq. 8Eq. 8</u>. The more numerically stable earlier solution is only preferred when within one time increment the species-specific variability of particle pH is substantially higher than the corresponding variability of the gas phase. The <u>liquidaqueous</u> phase driven solution should be avoided whenever possible, as it is computationally more expensive and does not provide a semi-analytical framework that accounts for the interdependence of the aerosol size <u>increment</u> classes.

Dynamic dissolution as given by Eq. 5Eq. 5 requires the dimensionless Henry coefficient (Eq. 3Eq. 3), which depends on particle pH and the mean activity coefficient of the dissolving species. The time dependence of the activity coefficient is

- 15 relatively low but the pH may span several orders of magnitude within one time increment. The high variability of particle pH reflects the numerical stiffness properties that are typical of concurrent dissolution of chemically interacting species (see above). According to Eq. 16Eq. 16, the time step is chosen such that it should be shorter than the typical time interval of chemical interaction. However, in a global model, transport may perturb species concentrations in such a way as to upset the equilibration tendencies of chemically interacting species. Under this circumstance the liquidaqueous phase may be rendered
- 20 completely out of balance. The use of the approximate analytical equilibrium pH as given by the roots of Eq. 13Eq. 13 proved to be an efficient fix to this transport-added numerical instability issue. Instability occurs whenever the liquidaqueous phase <u>is predicted</u>tends to lose-more protons, and in combination with a relatively large time increment would tend to lose <u>more</u>-within one time increment than it-actually contains. This tendency may be easily checked by comparing the chemically driven change in protons by a dissolving base or an evaporating acid (Eq. 13Eq. 13) with the amount of protons available.
- 25 The dynamic dissolution solver takes an implicit approach towards particle pH, via the use of the approximate equilibrium pH, rather than an explicit approach, when the proton demand exceeds half of the number of protons present:

$$(c_{H,eq}^{i,j,t} - c_{H}^{i,t}) > -\kappa_{pH} \cdot c_{H}^{i,t}, \quad \kappa_{pH} = 0.5,$$

Eq. 18

Eq. 17

 κ_{pH} being the distinction criterion between implicit and explicit particle pH for dynamic dissolution.

Within this section we have given semi-analytical solutions to dynamic gas phase and <u>liquidaqueous</u> phase-limited dissolution and defined a criterion that allows these regimes to be distinguished. Furthermore we have derived a characteristic equilibration time that may be used to determine an appropriate integration time step. It is based on the observation that single species equilibration time is strictly shorter than equilibration resulting from chemical interaction

- 5 among several species. The overall integration step is derived as the smallest size-specific value, chosen within the ensemble of the largest species-specific value within each size increment<u>class</u>. Finally we have defined a criterion to distinguish between the use of the momentary and estimated equilibrium pH with the gas phase driven solutions to dynamic dissolution. With these criteria and characterisitc time interval, it is ensured that dynamic solver chooses a time step that is as large as possible while numerical stability remains ensured. Still, under particular circumstances the numerical stiffness is such that
- 10 the time step requirements would constrict computational efficiency. For this reason the dynamic solver can only develop its full potential in association with an efficient equilibrium solver.

3.2 Equilibrium dissolution

This section describes a new numerical formalism for the equilibration of the aerosol particle composition with the gas phase. The underlying principle of the solver is to use semi-analytical solutions that take into account the interactive nature

- 15 of the problem as much as possible. The solver has certain *ad hoc* properties. The number of dissolving species that are linked through chemical interaction cannot exceed three. The number of particle size <u>incrementclasses</u> should not exceed the typical framework of a modal representation of the aerosol size distribution, that is 3-4 size <u>incrementclasses</u>. These properties come as a limit to its flexibility, however, they help optimize the accuracy and the computational expense of the scheme considerably.
- 20 In analogy to the dynamic solver, distinction is made between a regime of gas phase-limited equilibration and a regime limited by chemical interaction. In terms of the equilibrium solver, gas phase-limited equilibration corresponds to an initial stage of approximate equilibration with large variations to the dissolving species in both phases. The formalism allows for a succession of quick iterations delivering an approximate solution. Chemically limited interaction is handled during a second stage. It is both formally and numerically more complex, and therefore computationally more expensive. The equilibrium 25 solver is thus divided into two independent sub-solvers that are linked by appropriate decision criteria.

3.2.1 Gas phase driven equilibration

The gas phase driven equilibration sub-solver uses a variational method. For each dissolving species, particle size increment<u>classes</u> are treated conjointly. Chemical interaction, water content, sulphuric acid dissociation and activity coefficients are taken into account via simple iterations. The resolving equation for single species dissolution into one

30 aerosol size increment<u>class</u> is quadratic in $[H^+]$ (see Eq. 13Eq. 13). Due to this quadratic dependence, there is no analytical

solution for multiple size <u>incrementclasses</u>, so the quadratic dependence has to be approximated with a partial linearisation, as follows.

The ion and mass balance equations, and Henry's law read variationally, for a dissolving acid:

$$\begin{split} \delta C_{j,n} &= -\sum_{i} \delta c_{i,j,n} \\ \delta c_{i,j,n} &= \delta c_{H}^{i,n} \\ H_{j} &= \frac{\left(c_{i,j,n-1} + \delta c_{i,j,n}\right) \left(c_{H}^{i,n-1} + \delta c_{H}^{i,n}\right)}{r_{i,j} \left(C_{j,n-1} + \delta C_{j,n}\right)}, \quad r_{i,j} = \left(\frac{\gamma_{HA,i}^{2}}{kT_{i}N_{A}^{2}N_{i}^{2}M_{w,i}^{2}}\right)^{-1} \end{split}$$

5

The previous expressions for the Henry's law and the ion balance may be combined using the following linearisation assumption:

$$(c_{i,j,n-1} + c_H^{i,n-1}) \cdot \delta c_{i,j,n} + \delta c_{i,j,n}^2 \approx \delta c_{i,j,n} \cdot (c_{i,j,n-1} + c_H^{i,n-1} + \delta c_{inv}^{i,j,n}),$$
Eq. 20

Eq. 19

10 yielding:

$$\delta c_{i,j,n} = \frac{H_j r_{i,j}}{c_{i,j,n-1} + c_H^{i,n-1} + \delta c_{inv}^{i,j,n}} \delta C_{j,n} + \frac{H_j r_{i,j} C_{j,n-1}}{c_{i,j,n-1} + c_H^{i,n-1} + \delta c_{inv}^{i,j,n}} - \frac{c_{i,j,n-1} c_H^{i,n-1}}{c_{i,j,n-1} + c_H^{i,n-1} + \delta c_{inv}^{i,j,n}},$$
Eq. 21

where δc_{inv} is the invariant variation of the dissolving species in the <u>liquidaqueous</u> phase following its equilibration with a constant gas phase.

15 Consistently, δc_{inv} may be assessed solving the square equation resulting from Eq. 19Eq. 19 for $\delta C_{j,t}=0$. Eq. 21Eq. 21 may then be inserted into the mass balance expression of Eq. 19Eq. 19 leading to a solution of the type $\delta C_{j,t} \Sigma (1+a_i) = \Sigma b_i$.

For a dissolving base an equivalent expression to Eq. 21Eq. 21 is reached by analogy to Eq. 19Eq. 19. However, here the non-linear relationship between the gas and the liquidaqueous phase at equilibrium does not arise via the second degree relationship $\delta C_j = f(\delta c_j^2)$ but rather from $\delta C_j = f(1/\delta c_j)$. Under this circumstance linearisation is obtained when the variation of

20 the gas phase counterpart in the denominator of the following expression is neglected:

$$\delta c_{i,j,n} = \frac{-c_{i,j,n-1} + H_j r_{i,j} (C_{j,n-1} + \delta C_{j,n}) c_H^{i,n-1}}{1 + H_j r_{i,j} (C_{j,n-1} + \delta C_{j,n})},$$

Eq. 23

with:

$$H_{j} = \frac{c_{i,j,n-1} + \delta c_{i,j,n}}{r_{i,j} \left(c_{H}^{i,n-1} + \delta c_{H}^{i,n} \right) \left(C_{j,n-1} + \delta C_{j,n} \right)}, \quad r_{i,j} = \left(\frac{K_{H20} \gamma_{B}}{kT \gamma_{H}} \right)$$

5

Via the combination of Eq. 22Eq. 22 with the mass balance equation (see Eq. 19Eq. 19) the variation of the gas phase due to a dissolving base may then be obtained in similar fashion.

The variational approximations developed in this section resemble analytic solutions to the equilibration of a non-chemically interactive species dissolving into a size-resolved aerosol. Due to their approximate character these methods require iteration

10 for each dissolving species notwithstanding that they assume certain variables to be constant and neglect chemical interaction among the dissolving species.

3.2.2 Chemically driven equilibration

Gas phase-limited dissolution is driven by the partial pressure gradient between the particle surface and the gas phase, and is relatively independent of the non-linearities due to chemical interaction among several dissolving species. The application of

- 15 a computationally efficient variational solver that is based on iterations proves to be advantageous under this circumstance. The same does not apply to chemically limited dissolution for which numerical instability may easily occur via the pH, and the number of iterations required may turn out to be very elevated due to numerical stiffness. Analytical solutions (Nenes et al., 1998) offer the advantage of being unconditionally stable and computationally inexpensive. In the context of the concurrent dissolution of several species into a size discretized aerosol they nevertheless have several drawbacks. (1) For
- 20 two or three dissolving species the equilibration of the aerosol liquidaqueous phase requires the analytical solution of an equation of the third and the fourth degree, respectively (see below). The high degree of precision that is necessitated by equations of such an elevated degree may not be readily obtained for numerically stiff systems. Similarly, the number of dissolving species whose chemical interaction may be fully taken into account may not exceed three, as no analytical solution is readily available to an equation beyond the fourth degree. (2) In the presence of a non-linear system, a
- 25 comprehensive analytical solution may not be obtained (see above), entailing the need for iterative treatment, if the equilibrium composition is to be determined with a high degree of confidence. (3) It is not possible to solve analytically for chemically interacting species within_several aerosol size increment<u>classes</u> (see previous section), which adds to the need for iterative treatment.

In the following, the derivation of the resolving equation of equilibrium pH is described for the example of several acidic species. Similar equations may be derived for any combination of dissolving bases and acids. Activity coefficients, particle liquid water content and the degree of dissociation of sulphuric acid are <u>not predicted by the analyical scheme as they are</u> <u>includedtreated</u> as <u>parameterseonstants</u> (for one dissolving species, the dissociation of sulphuric acid is taken into account

5 analytically, however, see below). The variables are therefore the gas phase and <u>liquidaqueous</u> phase concentrations of the dissolving species within one size <u>binclass</u> and the particle pH within that <u>binclass</u>. We are thus dealing with a system of 2n+1 equations, *n* being the number of dissolving species. The governing equations are equivalents of Eq. 19Eq. 19, these read generically:

(1)
$$A_{j} = \frac{x_{i} y_{i,j}}{Y_{j}}$$
 (1) $A_{j} = \frac{x_{i} y_{i,j}}{Y_{j}}$
(2) $Y_{j}^{tot} = Y_{j} + y_{i,j} + \sum_{k \neq i} y_{k,j}$ (2) $Y_{j}^{tot} = Y_{j} + y_{i,j} + \sum_{l \neq i} y_{l,j}$,
(3) $x_{i} = \sum_{j}^{n} y_{i,j} + \sum_{k} a_{i,k}$ (3) $x_{i} = \sum_{j}^{n} y_{i,j} + \sum_{k} a_{i,k}$

10

Eq. 24

where *a* stands for <u>thea certain number of non dissolving passive</u> ionic species contained in the particle <u>liquidaqueous</u> phase such as sulphate, bisulphate, and <u>the balanced amount of cations and anions that</u>-passive cations resulting from sea salt dissociation. Eq. 24Eq. 24(1) stand for the Henry's law (c.f. Eq. 4Eq. 4), equations (2) for the mass balances (c.f. Eq. 7Eq. 7) and (3) for the ion balance (c.f. Eq. 11Eq. 11). The sea salt ions may be grouped together as they will not contribute to the

15 <u>variability of the pH during equilibration.</u>

The resolving equation for particle equilibrium pH is obtained when Eq. 24Eq. 24(1) are solved for Y_j and then inserted into Equations-Eq. 24(2). These in turn are then solved for $y_{i,j}$ which are then inserted into the ion balance equation. One obtains then a polynomial for x_i (=H⁺) whose degree is equivalent to the number of dissolving species plus one (d=n+1). When the above system is solved for any of Y_j or $y_{i,j}$ without solving for x_i before, the resolving equation is of degree d=n+2. This stresses the primordial importance of particle pH for chemical equilibration as it acts as a linkage among the concurrently dissolving species. It is possible to include sulphuric acid dissociation in the above system (with constant activity coefficients only). Under that circumstance the degree of the resolving equation for x_i is d=n+2. In order to limit computational expense and to limit the degree of the resolving equation to four (d<5) in the presence of three dissolving species, sulphuric acid dissociation was not included in the analytical equilibrium solver described here, except when the

25 solver equilibrates for only one dissolving species.

3.2.3 Equilibrium solver implementation

The implementation of the preceding formalisms of chemically and gas phase driven equilibration into a unified equilibrium solver requires an effective criterion of distinction between these two regimes. The variational formalism allows for quick equilibration within the size-discretized aerosol. When equilibrium is almost reached in terms of the individual species'

5 pressure gradient, the system becomes driven by chemical interaction, and the efficiency of the formalism decreases rapidly. For this reason an appropriate distinction criterion between chemical and gas phase driven equilibration is:

$$\kappa_{c,g}^{j} = \frac{\left|C_{j,n} - C_{j,n-1}\right|}{C_{j,n-1}}$$

Eq. 25

The minimum value for gas phase driven equilibration chosen in this study is $\kappa_{c,g}=0.1$. When equilibration is initiated in the 10 gas phase driven mode, $\kappa_{c,g}$ decreases with each iteration. Once the threshold is reached, equilibration is switched to the chemically driven mode, upon which $\kappa_{c,g}$ increases again as chemical interaction will trigger higher exchange fluxes. In order to avoid oscillations between the chemical and the gas phase mode, a switch back from chemically to gas phase driven equilibration is formally excluded.

- The equilibrium solver follows an iterative scheme. Both the gas phase driven and the chemically driven equilibration mechanism do not account for the variability of the activity coefficients, the particle water content and, in most circumstances, the degree of dissociation of sulphuric acid. Within the chemical sub-solver, equilibration for these variables is carried out on an *internal* level of iterations. The maximum number of internal iterations was set to 5, as a number that reconciles the need for numerical stability and the limitation of computational expense. The chemically driven scheme solves equilibrium for all dissolving species within one particle size <u>incrementclass</u>. For this reason an *external* level of iterations is
- 20 required that accounts for equilibrations among the size increment<u>classe</u>s. Its maximum number was set to 20, which was found to be sufficient under the numerically stiff conditions that are typical to chemically driven dissolution. In general there is an inclination for the smaller particle size increment<u>classe</u>s to have a lower condensation sink than the larger ones. For this reason, the larger size increment<u>classe</u>s eventually tend to act as process drivers although their equilibration requires more time. The chemically driven equilibrium scheme iterates consequently in the reverse size order. The gas phase driven scheme
- 25 solves for all aerosol size increment<u>classes</u> simultaneously. Limited chemical interaction as reflected in the variability of certain variables like the activity coefficients and the water content may be jointly tackled within a common iteration level. The iteration level of the gas phase driven scheme is therefore formally identical to the external level of chemically driven equilibration, and the associated total number of iterations is also limited to 20.

Chemically driven equilibration at the internal iteration level is dominated by the variation of pH. For this reason a 30 representative criterion of convergence at this level is:

$$\kappa_{conv,\text{int}}^{i} = \frac{\left|c_{H}^{i,n} - c_{H}^{i,n-1}\right|}{c_{H}^{i,n-1}}$$

Eq. 26

A sufficient degree of equilibration is assumed to be reached at the internal level when $\kappa_{conv,int} < 0.1$. At the external level the degree of convergence is estimated with the following criterion:

5
$$\kappa_{conv,ext}^{i,j} = \frac{|c_{i,j,n} - c_{i,j,n-1}|}{c_{i,j,n-1}}$$

Eq. 27

In this study convergence is assumed to be reached when $max(\kappa_{convext}^{i,j}) < 10^{-3}$. Under the circumstance of several competitive aerosol size increment<u>classes</u> and pronounced chemical interaction, the quantity of dissolvable matter in the gas phase may become very limited (see above). The resulting numerical stiffness sharply increases the amount of external iterations necessary for equilibration under the chemically driven scheme. A criterion to diagnose this numerically stiff equilibration situation is:

$$\kappa_{conv,stiff} = \frac{\max\left(\kappa_{conv,ext}^{i,j}\right)^{n-1} - \max\left(\kappa_{conv,ext}^{i,j}\right)^{n}}{\max\left(\kappa_{conv,ext}^{i,j}\right)^{n-1}}.$$

Eq. 28

When $\kappa_{conv,stiff}$ is found to be inferior to 0.1, then convergence among size increment<u>classes</u> is assumed to be inhibited by 15 slow transition of the dissolving species through the gas phase and the external convergence criterion Eq. 27Eq. 27 is increased from 10⁻³ to 10⁻². An increase of the convergence criterion reduces the precision of the equilibrium solver, and in consequence appears to affect the accuracy of the hybrid solver as a whole. Dynamically speaking, it turns out that this need not be the case. Knowing that this type of numerical stiffness comes with a sharp elongation of the transition period to equilibrium, some of the size increment<u>classes</u> that the solver attempts to equilibrate will not reach equilibrium within the 20 overall time step of the model. This circumstance will be taken into account, as their composition will be corrected separately according to the concept of pseudo-transition, which is described in the following section.

3.3 Hybrid solver implementation

25

The formal combination of the dynamic and equilibrium solvers requires the definition of an appropriate decision criterion for distinction between these two regimes. The reduction of computation time is the compelling reason for the preference of a hybrid formalism over a fully dynamic one, which would obviously be the more accurate one. According to Eq. 16Eq. 16.

the time step of the dynamic solver tends to be much more limited by individual size <u>incrementclasses</u>, among which the smallest value is chosen, than by the individual species in terms of their characteristic equilibration time. It is therefore advantageous to assume a maximum number of size <u>incrementclasses</u> to be in equilibrium. Among the size <u>incrementclasses</u> considered not to be equilibrium, some species may still be set to equilibrium. Although this latter choice would not allow

- 5 for an increase of the time step of dynamic dissolution, as the maximum characteristic time interval is chosen for each size increment<u>class</u>, it would still have a positive influence on numerical stability if it targets the most numerically stiff species. From its underlying principle, this approach may be considered to be a minimalistic version of a mixed time integration method (Zhang and Wexler, 2006; Zaveri et al., 2008), as the choice to simulate the temporal evolution of some species explicitly while others would be supposed to equilibrate instantaneously is based on the consideration of their specific
- 10 characteristic time interval.

The characteristic time interval for dynamic dissolution is tailored to the numerical stability requirements of the dynamic dissolution solver. It differs from the actual equilibration time, as it does not take into account chemical interaction, and appears to be quite specific, as it does not consider the actual partial pressure gradient. It will now be argued why the decision criterion between the equilibrium and the dynamic regime may follow a similar approach. First, the pressure

- 15 gradient is only a momentary snapshot of the saturation state the particle is in. Chemical interaction actually determines the equilibration time in many if not most cases. Typically, during most of the process of equilibration a strong gradient will be conserved in time. The gradient will only become smaller once the solution is close to equilibrium. Second, pronounced chemical interaction requires small time steps due to its related numerical stiffness. It should therefore be avoided as much as possible, and the corresponding size incrementclasses should be put to equilibrium. Their composition would have to be
- 20 corrected by other means in order to ensure that the solver is as accurate as possible.

The ideal criterion of choice between the dynamic and the equilibrium solver should therefore:

1) Determine the size <u>incrementclasses</u> that are clearly in equilibrium due to their actual equilibration time being much shorter than the overall time increment of the model.

2) Determine the dissolving species that are clearly in equilibrium among the remaining size incrementclasses.

25 3) Identify circumstances of pronounced chemical interaction whose dynamical treatment would entail prohibitive computational expense.

The distinction criterion may therefore be stated as follows:

$$\kappa_{teq}^{i,j} = a \cdot t_c^{i,j},$$

Eq. 29

where *a* is an *ad hoc* proportionality constant. Then, a sufficient condition for the particle in size $\frac{\text{binclass}}{\text{class}} i$ to be in equilibrium with respect to the species *j* would be:

$$\kappa_{teq}^{i,j} < \Delta t$$

Eq. 30

- 5 where ∆t is the overall time step of the model the dissolution solver is imbedded into. The proportionality factor a within Eq. 29Eq. 29 has a double physical and numerical meaning, as itbasically stands for represents the amouextent of chemical interaction beyond individual species equilibration that should is chosen to be taken into accountreated dynamically, and the maximum number of internal time steps that one is willing to accept, considering a balance between the computational efficiency and accuracy requirements of the solver. In this study a=2.0, such that the number of internal time steps would be be to two at this point. The complete formalism of the solver will further complicate this picture.
 - A complementary choice criterion between the dynamic and equilibrium solver is introduced as follows. When an aerosol size <u>incrementclass</u> is put into the equilibrium mode, its influence on the mass balance of the dissolving species is disconnected from the ones kept in the dynamic mode. Due to their formal separation a choice must be made on the order in which dynamic and equilibrium dissolution are calculated. In this study the dynamic solver is carried out first on grounds of
- 15 the tendency that the corresponding size increments have the larger condensation sink. Furthermore, from a dynamical point of view, it is plausible that faster reacting particles adapt to slower ones rather than the other way around. In consequence, the influence of the equilibrium size incrementclasses on the mass balance should be kept as low as possible, as given by:

$$\kappa_{meq}^{i,j} = \frac{\left|c_{eq}^{i,j} - c_{i,j}\right|}{c_{tot}^{j}},$$

Eq. 31

20 where κ_{meq} is the distinction criterion between the dynamic and equilibrium mode by reason of mass balance considerations. In this study mass balance conditions are supposed to be fulfilled when $\kappa_{meq} < 0.1$.

A size <u>incrementclass</u> is put into equilibrium mode when it fulfils both the mass balance and the equilibration time criteria with respect to all the dissolving species it contains. The mass balance criterion may thus lead to an increase of the number of time steps required by the dynamic solver, as some size <u>incrementclasses</u> that may be found to be dynamically close to

25 equilibrium may not be found so in terms of their mass. As the mass balance criterion does not catch chemical interaction either, as it also follows the gas phase driven approach, the size <u>incrementclasses</u> that are numerically stiff are still effectively filtered out, and the overall computational efficiency is preserved.

Decision on which species are placed into the equilibrium regime within a size increment<u>class</u> that is otherwise treated dynamically follows an analogous approach. However, due to numerical stability considerations, the equilibration time

criterion is applied exclusively under this circumstance, and only those species may be put in equilibrium that do not act as chemical driver within the size <u>incrementclass</u> under consideration. The chemical driver to dissolution is defined to be the species that shows the longest equilibration time. For computational efficiency, equilibrium species are treated non-iteratively using the analytical solutions that have been derived for chemically driven equilibration (see above).

- 5 Size increment<u>classes</u> in the dynamic mode are rechecked after each internal time step against the remaining fraction of the overall time step. In consequence, the equilibration time criterion is adapted sequentially to the remaining integration time interval via $\kappa_{teq} < \Delta t \delta t$, where δt stands for the cumulative amount of time that has been integrated over so-far. Through this procedure, the maximum number of time steps required by the dynamic solver may still increase by one after each time increment. In practice, however, the probability for this to happen several times is very low as the characteristic equilibration
- 10 time t_c is formulated in a way that it is relatively invariant (see above). The number of time steps required by the dynamic solver thus typically does not exceed three in the absence of mass balance constraints.

If an aerosol size <u>incrementclass</u> is put into the equilibrium mode, it is kept on hold for treatment by the equilibrium solver until the dynamic solver has finished. It might seem appropriate to redirect these size <u>binclasses</u> to time-resolved dissolution, on the basis of regular rechecks of their dynamical statute after each time increment of the dynamic solver. However, such a

15 procedure would be inconsistent, as those <u>binclasses</u> previously chosen to be in the dynamic mode would have evolved in time in the meantime. On the other hand, it is possible to return equilibrium species within a size <u>incrementclass</u> to the dynamic mode, as in this circumstance dynamic and equilibrium dissolution have been carried out simultaneously.

3.4 Pseudo-transition correction

On grounds of the above criterion (3) for distinction between the dynamic and the equilibrium mode, size incrementclasses that are numerically stiff are set to equilibrium, notwithstanding their actual dynamical state. In order to correct for the consequent bias the following formalism is adopted. For every dissolving species the equilibration time is estimated- after each external iteration increment of the chemical sub-solver. The equilibration time considered here is not equivalent to the characteristic time interval for dynamic dissolution t_c , but rather stands for the actual species specific equilibration time in a framework of effective chemical interaction that is marked by low pressure gradients. Eq. 2Eq. 2 may provides an estimation of the actual equilibration time t_{eq} :

2.5 of the actual equilibration time t_{eq} .

$$\kappa_{pt}^{i,j,n} = t_{eq}^{i,j,n} = a \cdot \left(4\pi r_i D_j N_i\right)^{-1} \begin{vmatrix} c_{eq}^{i,j,n} - c_{i,j,t-1} \\ c_{j,t-1} - \frac{p_s^{i,j,n}}{kT} \end{vmatrix} \\\kappa_{pt}^{i,j,n} = t_{eq}^{i,j,n} = b \cdot \left(4\pi r_i D_j N_i\right)^{-1} \begin{vmatrix} c_{eq}^{i,j,n} - c_{i,j,t-1} \\ c_{eq}^{i,j,n} - c_{i,j,t-1} \\ c_{j,t-1} - \frac{p_s^{i,j,n}}{kT} \end{vmatrix},$$

Eq. 32
where κ_{pt} is the distinction criterion for numerically stiff size increment<u>classe</u>s in the *pseudo-transition mode* (see below), and <u>ab</u> is a proportionality constant that takes into account the variability of the pressure gradient during equilibration. In this study, we choose <u>ab</u>=1.0 as a first approximation. This value may be roughly justified as follows: (1) under circumstances of chemically driven equilibration, the pressure gradient tends to be relatively constant, and (2) a certain amount of the temporal variability of the pressure gradient is already being taken into account due the fact that κ_{pt} is updated after each

5 temporal variability of the pressure gradient is already being taken into account due the fact that κ_{pt} is upda external iteration, thus allowing for competition between size <u>incrementclasses</u>.

If the equilibration time is found to exceed the overall time step Δt for more than one of the dissolving species, then the species showing the largest excess is chosen as the relevant driver. For the driving species the following linear correction is made:

10
$$c_{i,j,t} = c_{i,j,t-1} + \frac{\Delta I}{t_{eq}^{i,j,n}} \left(c_{eq}^{i,j,n} - c_{i,j,t-1} \right)$$

Eq. 33

The non-driving species are then equilibrated to the newly estimated value of the driving species with the full chemically driven equilibrium sub-solver including internal iterations. This process is re-initialised at each external iteration of the chemical sub-solver, such that it becomes formally part of the equilibration process, and is repeated until full convergence.

15 Size increment<u>classes</u> whose time-resolved transition to equilibrium is mimicked with the above *a posteriori* correction method are henceforth said to be in the pseudo-transition mode.

3.5 Overview

In the previous sections we have described the numerical mechanisms that make up the new inorganic dissolution solver. Due to its hybrid nature, the solver is divided into a dynamic and an equilibrium sub-solver. The equilibrium solver allows

20 for an additional pseudo-transition correction for size increment<u>classes</u> that are not treated with a fully dynamic approach by reason of computational efficiency.

The equilibrium solver is partially based on an analytical approach, which was shown to be computationally efficient by previous modelling experience (e.g., Nenes et al., 1998). The analytical approach is chosen whenever dissolution is found to be chemically driven via effective interaction of the species contained in the aerosol <u>liquidaqueous</u> phase. In this study, the

analytical approach is followed as rigorously as possible, as the equilibrium particle pH is computed for the concurrent dissolution of several species. The degree of the resolving equation is equal to the number of dissolving species plus one (the latter standing for H^+ , OH is neglected in the ion balance equation), thus limiting the number of dissolving species that may be taken into account to three.

The dynamic solver is principally based on the semi-analytical approach followed by Jacobson (1999a). It has the advantage of solving simultaneously for an unlimited number of particle size <u>incrementclasses</u>, thus providing for their mutual competition for condensable matter in the gas phase. However, this formalism cannot account for the chemical interaction between the species. Dissolution may be very close to equilibrium for certain particular species, while it may be not for

5 certain other species, which actually serve as driving species (c.f. numerical stiffness category 1). Furthermore, dissolution may also be numerically stiff for the driving species via the variability of particle pH (stiffness category 2). Therefore a species-selective equilibrium assumption is made and a predictive (=implicit) formalism for liquidaqueous phase pH is used, respectively.

The basic functioning of the hybrid solver is depicted by the flow chart shown in Figure 2. To begin with, a characteristic

- 10 time interval is estimated for each particle size <u>incrementclass</u> in the model. A size <u>incrementclass</u> is found to be in equilibrium when its characteristic time interval corresponds to less than half the integration time step of the aerosol microphysical model the solver is embedded into, and when its equilibration requires less than 10% of the total available matter for each of the dissolving species. The characteristic time interval reflects the amount of time that would be required for the equilibration of a size <u>incrementclass</u> with respect to a particular dissolving species, thus neglecting additional
- 15 equilibration time requirements due to chemical interaction. This definition ensures that size <u>incrementclasses</u> that show numerical stiffness according to categories 3 and 4 are mostly treated by the equilibrium solver. For those size <u>incrementclasses</u> that are treated dynamically, time integration is performed at a time step that is as large as possible while numerical stability is still ensured. The time step is chosen according to the requirements of the size <u>incrementclass</u> that is closest to equilibrium. In case more than one time step is required, each of the dynamic mode <u>incrementclasses</u> is retested
- 20 whether they can be put into the equilibrium mode. After typically 1-3 dynamic time steps the composition of the equilibrium increment<u>classes</u> is calculated. In choosing to calculate equilibrium composition after the dynamic calculation finished, two goals are pursued. First, equilibrium size increment<u>classes</u> tend to consume less matter than dynamic increment<u>classes</u>, as they are ideally close to equilibrium, and hence smaller. This circumstance is of some relevance, because their mass balance is decoupled from the dynamic size increment<u>classes</u>, thus carrying the risk of artefacts due to
- 25 misrepresentation of mutual competition for condensable matter. Second, it is ensured that those size increment<u>classes</u> that come close to equilibrium during integration may still be put into the equilibrium mode, such that both numerical stability and computational efficiency can be ensured.

Figure 3 depicts the formalism of the dynamic sub-solver for one internal time step. First, each size <u>incrementclass</u> is tested for whether certain species may be assumed to be in equilibrium. This test is carried out in accordance with the above time

30 criterion for distinction between equilibrium and dynamic increment<u>classes</u>. Species that are found to be in the dynamic regime are subdivided further according to whether their equilibration is driven either by the gas phase or chemical interaction within the <u>liquidaqueous</u> phase, and, in the former case, according to the variability of particle pH. As such, gas phase limited species are integrated in time with Jacobson's semi-analytical method (Jacobson, 1999a), while <u>liquidaqueous</u>

phase limited species are integrated with an analytical method that provides for their larger numerical stiffness. The analytical method solves for one species in one size increment<u>class</u>, while the Jacobson method solves for one species in all size increment<u>classe</u>s. The particle pH associated with the Jacobson method corresponds either to its momentary value (=diagnostic approach), or, if found to be beyond a certain variability threshold, to its individual species equilibrium value

5 (=prognostic approach). In order to insure accurate partitioning among the size increment<u>classes</u>, time integration is performed in parallel irrespective of the scheme that has been chosen. Finally, for the dissolving species that have been diagnosed to be in equilibrium in some or all of the increment<u>classes</u>, the composition of the dynamic increment<u>classes</u> is updated according to the analytical approach that is adopted in the equilibrium solver (see below).

The formalism of the equilibrium sub-solver is summarized within Figure 4. Using a specific criterion, the equilibrium solver differentiates formally between so-called chemical and gas phase equilibration. In the first case equilibration is driven by chemical interaction among species dissolving simultaneously. The chemical sub-solver assesses the equilibrium composition of one size increment<u>class</u> with respect to all dissolving species using the above-described analytical approach, and iterates at an internal level for water content and activity coefficient variation, which cannot be accounted for analytically, and at an external level for interaction among the size increment<u>classes</u>. For size increment<u>classes</u> whose

- 15 equilibration is kinetically driven by the variation of the dissolving species' concentration in the gas phase, a specific solver was designed that is based on a variational method. The kinetic sub-solver presents the advantage of being computationally efficient, and solves individually for each dissolving species and simultaneously for all equilibrium size <u>incrementclasses</u>. If at least one size <u>incrementclass</u> is found to be kinetically limited for at least one dissolving species then the kinetic subsolver is used beforehand. The kinetic solver performs iterations with updated gas phase and surface pressures, water content
- 20 and activity coefficients until further equilibration is found to be entirely chemically limited. Consecutively, full equilibration is achieved with the chemical sub-solver. Size increment<u>classes</u> that are dynamically, however not chemically, close to equilibrium (numerical stiffness categories 3 and 4) are mostly tackled by the analytical solver. Especially increment<u>classes</u> that show numerical stiffness according to category 4 turn out to have an actual equilibration time that is far longer than the individual species' equilibration time. At each external iteration of the chemical solver, the composition
- 25 of these size increment<u>classes</u> is re-evaluated according to an estimation of their actual equilibration time. Size increment<u>classes</u> thus corrected are said to be in pseudo-transition and remain formally part of the equilibration process. The chemical sub-solver allows for a certain number of external iterations only. Ideally the chemical composition of the equilibrium and pseudo-transition increment<u>classes</u> converges prior to attaining the maximum number of iterations, upon which the composition of the equilibrium increment<u>classes</u> is updated accordingly and the solver is exited.

4 Box Modelling Evaluation

4.1 Box model setup

The hybrid solver was implemented in the box model version of the modal aerosol microphysics scheme GLOMAP (Mann et al., 2010). The microphysical processes are all switched off during the validation, providing for a stable unperturbed

- 5 aerosol population that is divided into 4 hydrophiylic modes (nucleation, Aitken, accumulation and coarse). The particle phase in these modes is purely liquid, consisting of aqueous HSO₄⁻, SO₄⁻², NO₃⁻, Cl⁻, NH₄⁺, and Na⁺. H⁺ is calculated via the ion balance, taking into account the partial dissociation of sulphuric acid, whilst nitric acid and hydrochloric acid are assumed to be entirely dissociated. OH⁻ is neglected all throughout the scheme. Gas phase HNO₃, HCl and NH₃ may dissolve into and evaporate from the liquidaqueous phase, with activity coefficients, surface pressures and water content assessed via
- 10 the Partial Derivative Fitted Taylor Expansion (PD-FiTE) aerosol thermodynamics scheme (Topping et al., 2009). PD-FiTE was built on the concept used in the multicomponent Taylor expansion method (MTEM) model of Zaveri et al. (2005) in which activity coefficients of inorganic solutes are expressed as a function of water activity of the solution. Unlike MTEM, PD-FiTE was designed to remove the need for defining sulphate poor and sulphate rich domains. In addition, the order of polynomials that represent interactions between binary pairs of solutes was allowed to vary to increase computational
- 15 efficiency whilst retaining an appropriate level of accuracy. Fit to simulations from the <u>Aerosol Diameter Dependent Model</u> (ADDEM, see -model (Topping et al., 2005a,b),-its the use of PD-FiTE within a dynamical framework was demonstrated for aqueous inorganic electolytes in Topping et al. (2009) and extended for inorganic-organic mixtures in Topping et al. (2012) using the <u>Microphysical Aerosol Numerical model Incorporating Chemistry (MANIC, see aerosol model (</u>Lowe et al., 2009). <u>H₂SO₄ is not currently considered as a dissolving species within HyDiS-1.0. In principle, it may treated by the solver as a</u>
- 20 chemically interacting semi-volatile species, provided that the total number of dissolving species does not exceed 3, that its suface pressure would be delivered by the thermodynamic scheme, and that slight adaptations to the chemical equilibrium solver are made. Alternatively, H₂SO₄ could be treated by the solver as a non-interacting semi-volatile species, or as a non-volatile species via a formal association of dissolution and condensation (Jacobson, 2002). Currently, H₂SO₄ is considered to be non-volatile, and its condensation is simulated within a separate routine (Spracklen et al., 2005).
- In order to test the new solver, two series of model experiments were carried out, one with particles within the 4 modes initialised as binary mixtures of H_2SO_4 and H_2O , and the other- with the finest 2 modes initialised to contain H_2SO_4 and H_2O and the 2 coarser modes (accumulation and coarse) initially containing just sea salt and H_2O . The chemical composition of sea salt was adopted from Millero et al. (2008) as Standard Mean Ocean Water (SMOW), with all cations assumed to be Na⁺. Accordingly, the adapted composition of sea salt is *a*NaCl·*b*Na₂SO₄, with *a*=0.9504 and *b*=0.0496. Within Series 1 only
- 30 HNO₃ and NH₃ are allowed to dissolve, whereas in Series 2 HCl may dissolve additionally, thus providing for a more complex system with degassing HCl from the larger modes that can then dissolve also into the smaller modes. The particle number concentrations are 1000 cm⁻³ (nucleation), 250 cm⁻³ (Aitken), 100 cm⁻³ (accumulation), and 0.1 cm⁻³ (coarse); the initial dry particle radii are 1, 25, 100 and 1000 nanometres respectively. Five-day simulations are carried out at standard

pressure and temperature conditions with an imposed diurnal temperature cycle of +-5K and relative humidity set to 80%. The particle number concentrations and the passive species are held constant for the dissolving species to converge towards a forced dynamic equilibrium.

Within each series, experiments were carried out with initial ambient volume mixing ratios of the dissolving species of 1, 10

5 and 100 ppb such that the model evolution across a range of numerical stiffness conditions may be assessed. Surface total HNO₃ and NH₃ mixing ratios (over the gas and particle phase) are at most 10 ppb in polluted regions and typically around 1 ppb or less over remote oceans (Adams et al., 1999). Gas phase HCl ranges typically from 0.001 to 0.1 ppb over the Southern Hemisphere oceans (Erickson, 1999), and is less than 10 ppb under polluted continental conditions (e.g., Eldering, 1991; Nemitz, 2004). The concentration ranges for HCl, NH₃ and HNO₃ were not primarily chosen as being representative of any particular region or environment but rather with numerical stability testing considerations in mind.

In the next subsection we examine the results from each of these series, comparing between runs with (1) the full capability of the hybrid solver including the dynamic and equilibrium sub-solvers, with pseudo-transition correction enabled within the latter (HYBR), (2) the hybrid solver excluding the dynamic sub-solver (PSEUDO), and (3) the hybrid solver under full equilibrium conditions, that is excluding both the dynamic sub-solver and the pseudo-transition correction (EQUIL). Finally,

- 15 we also show results from a benchmark run that fully resolves the modes' transition to equilibrium with the <u>embedded fully</u> <u>dynamic schemedynamic sub solver only</u> (TRANS). <u>Our choice of this scheme as benchmark may be motivated as follows.</u> A dynamic scheme may serve as a benchmark if it fulfills the following conditions: (1) it is precise, (2) it is sufficiently distinct from the scheme it is tested against, and (3) it fits the system it is supposed to solve. The dynamic scheme we use here was originally developed by Jacobson (1997). It follows a semi-implicit approach (see Eq. 5 to Eq. 8), that was
- 20 specifically developed for its computational efficiency, its unconditional stability and its relative robustness to numerical stiffness. Later on, Jacobson (2005) presented a more simple variant that does not adopt a partial analytical approach. This version is known to exhibit less of a numerical tendency to infringe the mass balance equation, to be computationally less expensive, and to be slightly less reliable formally speaking (Jacobson, 2005). We chose the earlier version for its mathematical accuracy and its related higher capacity to deal with numerical stiffness. Both variants are mathematically
- 25 accurate, as for a time step δt→0 they tend to the exact solution. The mathematical precision of the scheme has been investigated for its later variant by Zaveri et al. (2008) against a stiff solver of ordinary differential equations, and found to deliver comparable results, provided that the time step of integration that the scheme is used with is sufficiently small. This is the feature that we have investigated within Figure 1, as a the time step that is too large tends to produce oscillations. With a small enough time step the transition and equilibrium regimes will be accurately resolved, as the result will be graphically
- 30 indistinguishable from the one obtained at a time step that is even smaller. Unlike MOSAIC, HyDiS-1.0 adopts a hybrid approach, with a further simplification to apply the PSEUDO approximation in cases where the dynamic behaviour of certain species does not need to be simulated explicitly. Although the dynamic benchmark solver is embedded within the solver, HyDiS-1.0 thus adopts a formal approach that is considerably distinct. Although the scheme is simplified substantially, it

may be shown that the choice of a larger time step does not necessarily result in a sizeable loss of accuracy. Finally, the embedded dynamic scheme fits the complex system of several chemically interacting species dissolving into a sizediscretized aerosol, as it solves for all size classes concurrently and allows updating all relevant parameters after each internal time step. In conclusion, the Jacobson (1997) semi-implicit scheme fulfills all conditions to provide for a fast and

- 5 precise benchmark if the internal time step is chosen appropriately. This might be easily achieved by inspection, as sketched within Figure 1. Similarly, we found the time steps of 1 and 0.01 seconds to deliver accurate results for a size-discretised aerosol at 1 and 10 ppb, respectively. At 100 ppbUnder this circumstance, numerical stiffness-at 100 ppb is pronounced to a degree that the Jacobson (1997) scheme cannot handle dissolution into the smaller modes-cannot be handled unless a prohibitively short time step is chosen. For this reason, we do not benchmark this run against the TRANSonly show results
- 10 for the 1 and 10 ppb runs in this configuration. The degree of precision of the HYBR and the PSEUDO runs is shown by their comparision with the benchmark TRANS run, as these should yield similar results if numerically accurate. The formal accuracy of the HYBR, PSEUDO, EQUIL and TRANS runs is mutually verified as they converge towards similar equilibrium values whenever they should do so by virtue of their system dynamical properties. The formal accuracy of embedded fully dynamic scheme is also verified by Figure 1, as the ambient and surface pressures of the dissolving species
- 15 <u>equalize at equilibrium. We do not benchmark HyDiS-1.0 against a reference thermodynamic scheme herein, and point to</u> <u>Topping et al. (2009) for an assessment of the degree of accuracy that may be obtained with PD-FiTE.</u>

4.2 Box model results

Fig. 5 compares the size-resolved NH_4 and NO_3 and NH_4 predicted by the new solver under the 1 ppb NH_3 and HNO_3 and NH_3 initialised TRANS, HYBR, PSEUDO and EQUIL configurations for binary sulphuric acid particles (experiment series

- 20 1). Contents within the nucleation mode are not shown as they are negligible. For the coarse mode, the degree of saturation with respect to gas phase NH₃ and HNO₃ is also given. Much more than to the time step, this value is related to the choice whether the temporal evolution of non-equilibrium modes is assessed with the dynamic sub-solver or with the pseudo-transition approximation. As will turn out, the 1ppb run without sea-salt is the only one which the solver treats the coarse mode dissolution fully dynamically. For the other 5 hybrid experiments, dissolution into the coarse mode is calculated
- 25 applying (either partially or fully) the pseudo-transition approximation, illustrating the operation of the hybrid solver in conditions of numerical stiffness.

At 1 ppb without sea salt, ammonia is the driving species, dissolving quickly into the <u>liquidaqueous</u> phase and partially neutralising the sulphuric acid. As a consequence, the particle pH (not shown) increases initially before reducing again later once the dissolution of the weaker nitric acid starts to occur. By virtue of the temperature dependence of the Henry constant,

30 <u>n</u>Nitric acid dissolves more readily at lower temperature (Kim et al., 1993; Nenes et al. 1998), so its content is maximal in the <u>liquidaqueous</u> phase at night. By contrast, <u>the solubility of ammonia is not primarily determined by the temperature</u> variability of the Henry constant, but rather by the variability of the particle pH. Ffor these 1ppb runs, ammonium has little

diurnal variation as the sulphuric acid is not close to being fully neutralised and the comparably high variability of nitrate is compensated by the degree of dissociation of sulphuric acid. Efficient chemical interaction does not set in under these conditions, with particulate ammonium around 2 orders of magnitude higher than that of nitrate.

Results obtained with the dynamic configurations are considerably different than when equilibrium is assumed. Treating the

- 5 partitioning dynamically accounts for the much longer timescale for the nitric acid to dissolve into the coarser particles with the dynamic runs predicting much more nighttime uptake to the smaller particle modes, with a subsequent slow transfer to the coarse mode as both ammonium and nitrate evaporate during the day. By contrast, using an equilibrium partitioning approach completely misses this uptake to the finer particles, with a dramatically reduced nitrate content in all three submicron modes. After five days the bias obtained with the equilibrium assumption is still of the order of 50% for ammonium
- 10 (Fig. 5b.1-3), and of the order of 20% and 50% for nitrate (Fig. 5a.1-3) during daytime and nighttime, respectively. Note that all biases are relative to the benchmark TRANS run. The pronounced non-equilibrium conditions are revealed by the degree of saturation of the coarse mode (Figs. 5.4). While HNO₃ is close to equilibrium during the entire simulated period for all three dynamic runs, the driving NH₃ barely reaches 10% saturation after five days. The simulation of the coarse mode is fully dynamic with the HYBR configuration so the HYBR run is barely distinguishable from the TRANS run in Fig. 5. Runs
- 15 performed at 0.1 ppb (not shown) are similar, with the solver also operating well under conditions of limited chemical interaction and numerical stiffness. Similarly, the PSEUDO configuration shows a high degree of accuracy, as the ammonium mixing ratios are very close to those of the HYBR and TRANS configurations, thus demonstrating the appropriateness of its underlying assumptions under moderately polluted conditions.

Fig. 6 shows the evolution of simulated size-resolved particle composition for the experiment with 10ppb gas phase NH3
and HNO₃3 and NH₃ dissolving into sulphuric acid particles in the 4 modes. At 10 ppb full chemical interaction sets in over the course of the simulation, with effective neutralisation of sulphuric acid, mixing ratios of ammonium and nitrate and ammonium of the same order of magnitude, and surface vapour pressures close to saturation. While ammonia still acts as the initial driver of dissolution, the gas phase approaches pseudo-equilibrium within one day (not shown), thus confering a relatively high degree of numerical stiffness to the system. In these conditions, the fully dynamic configuration adopts short

- time steps while the hybrid algorithm prevalently invokes the equilibrium sub-solver due to CPU time considerations. This approximation introduces a bias (at most ~20%) into the hybrid solver, with the HYBR run (blue) now distinguishable from the TRANS run (purple) in Figure 6. However, it is relatively uncommon for nitric acid and ammonia mixing ratios to reach 10 ppb in the troposphere, even in the most polluted areas, and our results confirm the hybrid solver is reliable in numerically challenging conditions. For the PSEUDO run, the temporal evolution of the ammonium content of the coarse
- 30 mode is constantly mimicked via an approximation of its equilibration time, and a larger bias (~30%) is apparent. The equilibration time is estimated for each species individually, and does not take into account their chemical interaction. In consequence the equilibration time is over-estimated at 10 ppb, the flux of dissolving ammonia is somewhat too low and concentrations within the coarse mode are increasing too slowly. Similarly to the behaviour seen at 1 ppb, the errors incurred

with the EQUIL configuration are considerable at around 50% low-bias for fine-mode ammonium and nitrate at night and \sim 20-30% high bias for coarse mode nitrate and ammonium depending on time of the day.

At 100 ppb dissolution is fully steered by chemical interaction as nitrate and ammonium contents are almost equal (Fig. 7). Equilibrium particle pH increases to around 2.2 (not shown) and less than 5% of nitric acid and ammonia remain in the gas

- 5 phase, resulting in a high variability in both particle pH and surface vapour pressure (not shown). The resulting extreme numerical stiffness induces a slight artificial drift in the equilibrium regime (e.g., Fig. 7a.1), as the equilibrium sub-solver struggles to establish chemical equilibrium among the modes. Furthermore, the numerical stiffness results in a predominant invocation of the pseudo-transition approximation with the HYBR configuration. Whereas the HYBR run correctly chooses NH₃ as driver of chemical interaction, as is testified by the degree of saturation of the coarse mode (Figs. 7.4), and PSEUDO
- 10 quickly switches to HNO₃ as a result of its simplified dynamical assumptions, both the HYBR and the PSEUDO runs yield very similar results, thus underlining the secondary relevance of the degree of saturation for the estimation of particle composition under conditions of pronounced chemical interaction. While the accumulation mode rapidly reaches a relatively stable composition, both the Aitken and the coarse mode show a much slower equilibration, which can be explained as follows. Initially the pressure gradients are extremely high due to the high ambient concentrations. As the equilibration time
- 15 of the accumulation mode is much lower than the one of the coarse mode, and its condenstion sink much larger than the one of the Aitken mode, it may compete effectively under conditions of chemical interaction to reach equilibrium with the gas phase in less than an hour. The equilibration of the Aitken mode then takes much longer, as it struggles during the first day to compete with the slowly equilibrating coarse mode for the matter released by the accumulation mode. After 5 days, the amount of dissolved matter in the coarse mode is still overestimated by the EQUIL configuration by a factor of 8, whilst
- 20 uptake to the Aitken and the accumulation mode is biased low by a factor of 4. In conditions of ammonium nitrate formation equilibrium assumptions are thus susceptible to produce a significant bias across the entire particle spectrum whenever most of the dissolving species is in the aerosol phase and there is a substantial contrast in the equilibration time of the aerosol size incrementclasses.

Fig. 8 compares Series 2 results for ammonia, nitric acid, ammonia and hydrochloric acid at 1 ppb dissolving into an external
mixture of sulphuric acid (nucleation and Aitken modes) and sea-salt particles (accumulation and coarse modes). The
EQUIL configuration reveals a somewhat counterintuitive property, as the initial compositions of the accumulation and the
coarse mode are equal, and their equilibrium compositions are not. It appears that particles memorize the origin of chloride,
whether sea salt or dissolved hydrochloric acid: while the relative quantities of dissolved matter are equal at equilibrium, as

is testified by an equal proton concentration of approximately- pH=3.4 (not shown), the relative amounts of chloride, as

30 given by sea salt and hydrochloric acid, differ as these quantities depend on the respective condensation sink of the modes. The Aitken and the nucleation mode show a specific composition, as is testified by their equilibrium pH of approx. 0.75, which reflects their non-volatile sulphuric acid content. In the TRANS run, the coarse mode takes around 2 days to reach equilibrium composition as nitric acid dissolves slowly into the liquidaqueous phase and hydrochloric acid degases. The amount of hydrochloric acid in the accumulation mode increases as it adapts to the surplus released by the coarse mode (the inverse applies to nitric acid). This 2-day timescale for chemical equilibration of the sea salt particles is faster than the very slow equilibration of coarse sulphuric acid particles with the semi-volatile gases at 1 ppb (Figs. 5.3). The relatively high content of both nitrate and ammonium in sea salt particles at equilibrium indicates a much more effective chemical

- 5 interaction under numerically stiff conditions. This circumstance is also demonstrated by the similarity of the HYBR and the PSEUDO results in Fig. 8. Except for a very short initial period, the pseudo-transition approximation is constantly chosen with the HYBR configuration, as is testified by resolutely equal degrees of saturation of the coarse mode (Figs. 8.4). Nitrate serves as a driver, to which chloride and ammonium are equilibrated. Under moderately polluted conditions, the pseudotransition approximation produces fair results, with a small bias in coarse mode nitrate and chloride of around 20 and 10%.
- 10 respectively, due to some degree of misrepresentation of the competition between these two, while the <u>equilibration</u> of ammonium <u>proves to yieldis</u> fairly accurate <u>results in a context of short equilibration times along</u> with low ammonia solubility at low particle pH. With the TRANS configuration, the degree of saturation of the coarse mode exhibits a pronounced daily cycle (Figs. 8.4). In contrast, except for nitrate, the pseudo-transition approximation assumes saturated conditions for the non-driving species. The low related biases reveal anew the secondary importance of the
- 15 pressure gradient for a reliable simulation of particle composition under conditions of pronounced chemical interaction. The bias obtained with the equilibrium assumption is much larger for chloride and nitrate (up to a factor of two), while ammonium is again in reasonable agreement. <u>HCl and HNO₃ act as competitors, while NH₃ shows a low solubility that is conditioned by the particle pH, which in turn is relatively unaffected by the exchange process between the two acids.</u>
- Fig. 9 shows the results for sulphate and sea salt aerosols (Series 2) with the dissolving gases at 10 ppb. Under these conditions, the previously observed chemical interaction under numerically stiff conditions is pronounced further, with very slow equilibration, and nitrate and ammonium contents much higher than in the 1ppb runs. In the process of chemical interaction the sea salt particles become acidified (not shown). Within the dynamic configurations, the diurnal temperature variation prevents the modes from ever reaching momentary equilibrium, as is testified by the degree of saturation of the coarse mode (Figs. 9.4), because the forcing exerted by temperature is faster than the equilibration of the coarse mode and
- 25 the latter is in competition with the smaller modes. For this reason, ands seen in analogy to the 10 ppb dissolution into sulphate aerosol (Fig. 6), the TRANS run exhibits a much more pronounced diurnal variability of the accumulation and the Aitken modes (Figs. 9.1-2), which compensates for the relative inertia of the composition of the coarse mode (Figs. 9.3). As in the preceeding 1 ppb sea salt (Fig. 8), the HYBR configurationrun yields similar results equivalent to the PSEUDO configurationrun because the hybrid solver constantly chooses the pseudo-transition approximation to avoid small time steps
- 30 in the context of numerical stiffness. For the same reason, the degree of saturation of the coarse mode does not exhibit the pronounced daily cycle it does with the TRANS configuration for the non-driving species (Figs. 9.4). At 10 ppb dissolution into sulphate-(Fig. 6), the equilibration time of the coarse mode was overestimated in the PSEUDO run (magenta line)-with respect to the driving ammonia, resulting in an underestimation of both ammonium and nitrate (magenta versus blue line in

Figs. 6.3). The opposite applies here, with fine mode ammonium and nitrate slightly high biased in the PSEUDO (and HYBRID) runs compared to the fully dynamic simulation. In the presence of sea salt aerosol, nitric acid is chosen by the solver as the unique driver to dissolution, and the <u>aqueous phaseparticle</u> concentrations of ammonia and chloride are equilibrated to it. During the first day the solver appears to quite well catch the dynamics of the equilibration of the coarse

- 5 mode. Past this point, however, the amount of all three dissolving species is overestimated in the coarse mode, thus leading to an underestimation of the contents in the Aitken and the accumulation modes. It appears then that nitric acid does not act as the sole driver, but that hydrochloric acid figures as a secondary driver. The instantaneous equilibration of hydrochloric acid to the nitrate content of the coarse mode in the pseudo-transition regime leads to its overestimation, which via chemical interaction leads likewise to an overestimation of the content of ammonium, and via competition to opposite effects in the
- 10 smaller modesso on. The resulting bias of the hybrid solver is at most around 25% for chloride in the Aitken and accumulation mode, and up to 40% for chloride in the coarse mode. The respective biases for ammonium and nitrate are less, and in the gas phase all three dissolving species agree well throughout the simulation (not shown).

Figure 10 depicts the 100 ppb run within Series 2 with sea salt. Similarly to the 100 ppb sulphate particles, the EQUIL configuration shows a slight drift due to the extreme numerical stiffness at these very high mixing ratios, which is most

- 15 apparent for the Aitken mode. The pronounced chemical interaction property is exhibited by the fact that the particle ammonium content is almost twice that of chloride and nitrate, such that <u>no more than</u> approximately 1% of total <u>NH₃ammonia/ammonium</u> remains in the gas phase (not shown). Sea salt particles are acidified as pH=2.3, approximately (not shown). In analogy to the 1 ppb and the 10 ppb run, the HYBR and PSEUDO runs are almost identical, as the hybrid solver avoids small time steps with the choice of the pseudo-transition approximation. Similarly to 100 ppb sulphate the
- 20 Aitken mode exhibits a longer initial equilibration time than the accumulation mode <u>as a result of its competition with the</u> <u>coarse modedue to its lower condensation sink and</u>, which is exacerbated by its contrasting initial acidic property. At a later stage both the conteents within the accumulation and the Aitken mode decrease concurrently as material <u>continues to</u> partitions into the coarse mode via the gas phase. The complex pattern of the evolution of Aitken mode composition results from a combination of its higher sensitivity to other modes and the extreme conditions of numerical stiffness, to which
- 25 circumstance the concurrent numerical instability of the degree of saturation of the coarse mode may serve as an indication (see Figs. 10.4). Although—when both make use of the pseudo-transition approximation, the HYBR and the PSEUDO configurations need not produce rigourously similar results. In contrast, the results obtained by the HYBR run may depend to a certain degree on the internal time step, as the switch to the pseudo-transition approximation may occur after a partial integration over the overall time step. Although the variability of the liquidaqueous phase concentrations of ammonium
- 30 <u>remindsis similar to</u> the one of 1 ppb sulphate aerosol (Fig. 5b), the equilibration of the latter is mechanistically entirely different for it is steered by the slow <u>transitiondissolution</u> of ammonia <u>from the smaller modes</u> into the coarse mode <u>via the gas phase</u>. Thereby it is not chemically but dynamically limited, as is also reflected by the comparably low pH<u>(not shown)</u>. Within Fig. 10, both 100 ppb sea salt and even more so 100 ppb sulphate particlesaerosol exhibit a very slow, however

chemically limited, equilibration of the coarse mode at <u>a relaitvely highsimilar pH (not shown</u>). As with the 10 ppb runs (Fig. 9), the 100 ppb sea salt run shows faster equilibration of the coarse mode (Figs. 10.3) than into sulphuric acid particles (Figs. 10.1) due to more effective chemical interaction. Still, the disparities between the dynamic configurations and full equilibrium are considerable, with discrepancies of the order of 50% for the smaller modes, and of the order of 25% for the coarse mode

5 coarse mode.

Computational times for the entire simulated time period of 5 days are compared in Table 1 for the box model test cases. <u>The</u> <u>computational expense of HyDiS-1.0 is expressed</u><u>Values are given</u> as percentages of the time consumption of the <u>standard</u> <u>GLOMAP-mode aerosol microphysical scheme</u>, which comprises most notably routines for nucleation, condensation, <u>coagulation</u>, <u>cloud and precipitation scavenging</u>, <u>sedimentation and dry deposition</u>, <u>mode merging and wet oxidation</u> (see

- 10 <u>Mann et al., 2010</u>). All standard GLOMAP microphysical processes were switched off entire microphysical box model, which was not switched on for the dissolution tests above. Table 1 shows that for the test cases the time consumption of the dissolution scheme amounts to a fraction of the <u>standard GLOMAP-mode</u> aerosol microphysical schemes only. Essentially, the computational time increases with the ambient concentration of the dissolving species along with numerical stiffness. The hybrid runs appear to require more computational time than the equilibrium runs while pseudo-transition appears to be
- 15 relatively independent of ambient conditions. Two elements tend to break down the correlation between numerical stiffness and computational expense. First, the equilibrium solver diagnoses slow convergence and limits the number-the number of iterations accordingly. For this reason, the 10 ppb sea salt run requires more computation time that the 100 ppb run. Second, the hybrid solver comprises an equilibration mass criterion when distinguishing between equilibrium and dynamic modes (see above). When applied, this criterion may be related to relatively small time steps, which require a relatively high amount
- 20 of computation time. The hybrid 1 ppb sea salt run illustrates this circumstance, as strong competition between the accumulation and the coarse mode for nitric acid requires both modes to be treated dynamically.

5 First Global Modelling Results

5.1 Introduction

In this section, we describe the implementation of HyDiS-1.0 in the 3D global offline chemistry transport model TOMCAT

25 (Chipperfield, 2006) as an extension of the GLOMAP-mode aerosol microphysics module (Mann et al., 2010). The aims of this section are to (1) demonstrate that the new solver <u>reliably</u> delivers <u>physically</u> realisticsonable results in the framework of a global 3-D model, (2) assess the extent to which the equilibrium and hybrid configurations of the solver <u>may</u> lead to different size-resolved partitioning of nitrate and ammonium, and (3) to demonstrate the new solver's competitive computational expense.

5.2 Global Model Implementation and Experimental Setup

We use the "coupled-chemistry" version of the TOMCAT-GLOMAP global aerosol microphysics model, as used in Schmidt et al. (2010), which uses the same sulphur chemistry as in Mann et al. (2010) in combination with an online tropospheric chemistry scheme, allowing for interactions between gaseous sulphur species and oxidants (see Breider et al., 2010). The

- 5 TOMCAT tropospheric chemistry module provides gas phase nitric acid and ammonia concentrations, with the new solver then predicting their partitioning into the ammonium and nitrate components of each size mode. <u>The coupled TOMCAT-GLOMAP chemistry module does not currently comprise hydrochloric acid. The wet oxidation of SO₂ is assessed within <u>GLOMAP. H₂SO₄ is considered to be non-volatile, whether it originates from condensation or wet oxidation, it may not evaporate from the aqueous phase. HyDiS-1.0 simulates the influence of H₂SO₄ on the solubility of semi-volatile species via</u></u>
- 10 the particle pH and the activity coefficients, as the latter and the partial dissociation property of H_2SO_4 are assessed with the embedded thermodynamic scheme PDFiTE (see above).

Whereas in the box model simulations from section 4, only the 4 hygroscopic modes were activated, here we use the full 7mode GLOMAP configuration that includes three insoluble modes containing hydrophobic carbonaceous and dust particles. The model no longer tracks a "sea-salt" component, instead separately tracking sodium and chloride masses in the

15 accumulation and coarse mode, as well as nitrate and ammonium in each soluble mode, requiring an additional 10 aerosol tracers to be transported compared to the original configuration (see Fig.ure 11a and Fig. 11b for a comparison between the configuration of GLOMAP-mode with and without HyDiS-1.0).

The representations of the main aerosol processes are unchanged (as described in Mann et al., 2010), comprising nucleation, condensation, coagulation, cloud chemical processing, <u>cloud and precipitation scavenging</u>, sedimentation, dry deposition and

- 20 wet removal. The model set-up routines were adapted to be consistent with the chemical species taken into account by the dissolution scheme (see Table 2). Liquid water content is calculated according to Topping et al. (2009), and particle density is assessed with a new routine that takes into account particle composition following the dissolution of inorganics. As in Mann et al. (2010), sea salt is emitted into the hydrophiyilic accumulation and coarse modes but the composition of sea salt is modified assuming mole fractions of 0.024, -0.512 and 0.464 for sulphate, sodium and chloride, respectively (see above).
- 25 <u>Ammonia emissions are from Bouwman et al. (1997), with SO₂, BC and POM emissions included from anthropogenic</u> (Dentener et al. 2006) and biomass burning (van der Werf et al., 2003) sources. The dissolution solver is used to simulate the exchange of nitric acid and ammonium between the gas and the particle <u>liquidaqueous</u> phase. Within this study, exchanges of hydrochloric acid and those that involve a solid phase may not be treated due to a lack of formal representation. Heterogeneous processes and, as well as the formation of secondary organics are not taken into account, as these are
- 30 switched off. None of these processes is required with respect to the principal goal of the present global simulations, which is to verify the numerical functioning and performance of HyDiS-1.0. Ammonia emissions are from Bouwman et al. (1997), with SO₂, BC and POM emissions included from anthropogenic (Dentener et al. 2006) and biomass burning (van der Werf et al., 2003) sources.

In section 5.3 we present results from a 1-year simulation of the new model after 3 months spin-up. The simulations were carried out at T42 horizontal resolution (~2.8x2.8 degrees longitude/latitude) with 31 vertical levels on a hybrid sigma pressure coordinate.

The main transport time step for the model is 30 minutes, with the TOMCAT chemistry and GLOMAP aerosol microphysics

- 5 each solved on a 15 minute time step. As described by Spracklen et al. (2005) and used in Mann et al. (2010), GLOMAP also includes a shorter "competition time step" of 3 minutes used when the condensation and nucleation are integrated in a process-split fashion. <u>HyDiS-1.0Dissolution</u> is implemented separately from these routines. <u>Joint 15 minutes</u> <u>routine to be invoked within the GLOMAP aerosol model and is integrated with an overall time step of 15 minutes.</u> The uptake coefficient of nitric acid and ammonia are set to 0.2 and 0.1, respectively. The uptake coefficient of nitric acid is
- 10 known to be strongly temperature dependent (Van Doren et al., 1990). The uptake coefficient of ammonia appears to depend significantly on both pH and temperature (Shi et al., 1999). In the ternary H_2SO_4 , NH₃, H₂O system, it also appears to be an explicit function of the degree of neutralisation of H_2SO_4 by NH₃ (Swartz et al., 1999). The update coefficients are thus an integral part of the interactive properties of aerosol chemistry, and the values we chose may only serve as a first approximation to a question that is treated in this study. In the context of this study, the uptake coefficient plays a role in the
- 15 distinction between equilibrium and dynamic modes, as well as in the choice of the integration time step of the dynamic solver, as it determines the equilibration time. For this reason, a low uptake coefficient will tend to increase the computational expense of the solver along with numerical stiffness and the number of time steps required. The findings of Section 5.3 have to be relativised against the absence of solid phase processes in the model. The formation of crystallized ammonium nitrate and/or crystal compounds of ammonium and sulphate is accompanied by the evaporation of
- 20 ammonia and nitric acid that is in excess (see, e.g., Metzger and Lelieveld, 2007). Global model studies suggest that crystallized ammonium nitrate is mainly encountered under the cold and dry conditions of the Antarctic southern hemisphere winter, whereas the formation of ammonium sulphate particles under polluted and relatively dry conditions over the mid and low lattitude continents is mostly accompanied by the complete evaporation of particle nitrate Martin et al., 2004). In the boundary layer, about 70% of all particle nitrate was found to evaporate as it is in excess, while the remaining fraction would
- 25 be about half and half in the aqueous and in the solid phase. In line with these results, the evaporation of ammonia was found to be limited to less than 10% on global average. The widespread incidence of solid and mixed phase formation shows that the liquid aerosol assumption is a rough simplification. This is particularly true for nitrate over the continents and the high latitudes. While not required for the verification of the reliability and performance of the solver, the accurate simulation of non-equilibrium effects requires an accurate representation of all gas-particle phase exchange processes. Whenever solid or
- 30 <u>mixed phase particles occur, the present results may therefore only serve as a preliminary indication for the importance of these effects.</u>

5.3 Results

Figure 12 shows the surface Northern Hemisphere distribution of annual-mean model particulate nitrate and ammonium mass concentrations compared against observations from the CASTNET/IMPROVE, EMEP and EANET measurement networks (compiled by Pringle et al. (2010) for the year 2002). Model results are obtained with the hybrid configuration of

- 5 the dissolution solver. The solver delivers <u>physically</u> realistic amounts of particle ammonium and nitrate <u>globally</u> across both polluted and less polluted regions<u>,</u>, thus demonstrating its numerical reliability within the parameter space of the atmosphere. Simulated nitrate has a substantial low bias in North America however. <u>This inaccuracy need not be related to the model assumptions and simplifications</u>, as there are other likely causes. The amount of nitric acid dissolving into the particle phase is highly dependent on particle pH, and thus the ability to accurately predict particulate nitrate in such sulphate-rich regions.
- 10 is dependent also on the amount of sulphuric acid versus ammonia (e.g., Xu and Penner, 2012). When comparing the model values to the observations, one also needs to consider the representativeness of the monitoring site in relation to the model resolution.

Figures 13 and 14 compare <u>size-resolved</u> July 2003 nitrate and ammonia contents-<u>respectively</u>, <u>aswith</u> the left-hand and right-hand panels <u>show</u> from results with the hybrid and equilibrium configuration, respectively. Values are shown as a

- 15 molecular fraction of the sum of Na⁺, SO₄²⁻, HSO₄⁻, NH₄⁺, NO₃⁻ and Cl⁻ in the Aitken, accumulation and coarse mode liquidaqueous phase excluding water and non-soluble species. Gas phase NH₃ and HNO₃ are also shown as volume mixing ratios, with equilibrium gas phase contents shown as the relative change from values with the hybrid configuration. The pseudo-transition configuration was also assessed, however results are not shown, as they are very similar to the values obtained in the hybrid configuration. In the hybrid run considerable amounts of nitrate occur in the Aitken mode both over
- 20 the Arctic and Antarctic. The dissolution of nitric acid (Fig. 13) is highly temperature dependent and as such related to a pronounced seasonal cycle (e.g., Metzger et al., 2002b; Pringle et al., 2010). Although the Arctic is relatively warm in July and ammonia/ammonium concentrations are fairly low (of the order of 0.01 to 0.1 ppb), it may still suffice to neutralize the sulphate contained in the Aitken mode sufficiently, such that in conjunction with the relatively high relative humidity over the Arctic Sea nitrate comprises up to 90% of solutes present in particles at these sizes. The hybrid solver seems to catch the
- 25 dynamics of dissolution with respect to a discretised aerosol as it predicts that <u>themuch more</u> nitrate <u>fraction</u> is <u>most</u> <u>importantpartitioned</u> into the Aitken mode (Fig. 13a.1), the effect being particularly evident in the Arctic. In marine and remote regions sea salt is often present in the accumulation mode, and is therefore much more prone to the dissolution of nitric acid. However, the <u>competing</u> Aitken mode is faster to equilibrate such that the nitrate content of the <u>competing</u> accumulation mode remains constrained to typically less than 120% (Fig. 13a.2). The model suggests that the phenomenon
- 30 would be most even much more pronounced in the Antarctic, where the accumulation mode is dominated by sulphate. The model cannot reproduce the evaporation of excess nitric acid in a context of crystallisation of ammmonium nitrate at this point, and it thus seems likely that the simulated nitrate within the Aitken mode is overestimated at the expense of the larger particles.

The importance of the dynamics for the fractionation of nitrate is demonstrated by the comparison with the equilibrium results. The equilibrium configuration results in a significantly different partitioning, as <u>the</u> nitrate fraction in the Aitken mode is reduced due to efficient competition through the coarse mode (Fig. 13b.1 versus Fig. 13b.3). The accumulation mode (Fig. 13b.2) is squeezed between the Aitken and the coarse mode: While its nitrate content increases significantly in

5 the Antarctic, it seemingly vanishes in the Arctic, it increases significantly in the Antarctic. However, it remains unclear to what extent the model is able to reproduce the effects that occur in this region.
 The fractionation of ammonium (Fig. 14) appears to be much less dynamically driven, as sizeable amounts of ammonium are present in the Aitken, accumulation and coarse mode irrespective of the configuration of the hybrid solver. Rather, the

partitioning of ammonium seems to be primarily driven by the ratio of particle sulphate to sea salt and secondarily by the

- 10 total atmospheric ammonia content. In continental regions, ammonium typically accounts for more than 50% of the Aitken mode, with the <u>notable_exception of Antarctica and</u> North Africa which <u>isare</u> characterised by low ambient ammonia concentrations. This finding should be relatively robust with respect to the prominent formation of ammonium sulphate over the continents, as the evaporative losses of excess ammonium appear to be limited overall. In marine regions, the accumulation and coarse modes are mostly dominated by sea salt, notwithstanding that ammonia concentrations are higher in
- 15 the Northern Hemisphere.

The role of the sulphate to sea salt ratio is also apparent when comparing the global distribution of gas phase nitric acid <u>and</u> <u>ammonia</u> concentrations between the simulations with the <u>equilibrium</u> and <u>hybrid</u> <u>and equilibrium</u> configurations of the solver <u>(Fig. 13a.4 versus Fig. 13b.4, and Fig.14a.4 versus Fig. 14b.4, respectively)</u>. Significant differences are apparent at high latitudes, for which <u>it is suggested that</u> significant nitric acid fractions <u>would beare</u> present in the liquidaqueous</u> phase,

- 20 and also more clearly in marine regions where particles are mostly dominated by sea salt. Over the Southern Ocean, although total nitric acid is very low, it dissolves readily into the abundant sea salt particles. The equilibrium configuration shows much lower gas phase nitric acid concentrations, by another 90% in this region. <u>Similarly, t</u> he sensitivity of ammonia to the dynamical regime resolved by the hybrid solver is highest in those areas in which it is scarce, while changes in its size-resolved partitioning are felt to a lesser degree. Via chemical interaction with nitrate, the ambient concentration of ammonia
- 25 over the Southern Ocean <u>is predicted to be lower by 10-25% than predicted by the equilibrium approach</u> decreases by approximately 10-25% in the equilibrium regime. At <u>the high latitudes of the Northern Hemisphere</u>, higher particle ammonium leads to a decrease of the ambient concentration of ammonia of typically more than 50% in the equilibrium regime, with a reduction of more than 99% occurring over the Antarctic.

Figures 15 and 16 show the January 2004 contents of nitrate and ammonium respectively, again left-hand and right-hand 30 columns showing simulations with the hybrid and equilibrium configurations of the solver. These results should remain

relatively unaffected if the crystallization of ammonium nitrate was taken into account, as model simulations suggest that it is not a widespread occurrence during the Northern Hemisphere winter (Martin et al., 2004). Total nitric acid and ammonia are high enough over Northern Hemisphere continents for nitrate aerosol to form within the Aitken and accumulation modes even deep into the mid-latitudes during wintertime low temperature conditions, each comprising ~40-50% of total solute mole fraction over large parts of Siberia and Canada. The fraction of ammonium tends to decline with increasing latitude-as its total concentration along with its decreasing total atmospheric concentration, whereas nitrate remains substantial due to more effective partitioning at lower temperatures. The Aitken mode competes efficiently for available nitrate and ammonium with the accumulation and the coarse mode, with accumulation fractions tending to be significantly lower, and substantially

5 lower fractions in the coarse mode, especially for nitrate. Consistently, a very pronounced seasonal cycle for nitrate is revealed by comparing the January and July global surface maps (Fig. 13 versus 15). In contrast, the seasonal cycle of ammonium is less pronounced (Fig. 14 versus 16). Its dissolution appears to be less temperature dependent, as it is the result of the superposition of the temperature and the vegetation cycle.

The comparison of January equilibrium and hybrid results predictsshows similar effects as those seen for July. When the

- 10 equilibrium assumption is made, more nitrate partitions into coarse particles with the Aitken mode nitrate fraction reduced from typically 40-50% in continental regions to 30-40%, with similar figures occurring in the accumulation -mode. Likewise, the equilibrium assumption also leads to discrepancies in the gas phase concentrations of nitric acid and ammonia. Nitric acid is most affected in areas that show either low total concentration in combination with sea salt, or high liquidaqueous phase concentrations in combination with a shift in its fractionation (Fig. 15a.4). Ambient nitric acid concentrations are
- 15 consistently lower in the equilibrium regime, by typically 25-90%, except for limited areas in Siberia where ambient nitric acid is predicted to increase (Fig. 15b.4). The effect of the equilibrium assumption on ambient ammonia appears to be similarly related to its overall abundance, and triggered by chemical interaction with dissolved nitric acid in relationship to low temperatures and/or sea salt (Fig. 16a.4 versus Fig 16b.4). Over the Arctic, the equilibrium assumption reduces the low predicted ammonia in the hybrid configuration by more than another 99% via the increased dissolution of nitric acid in the
- 20 equilibrium regime reduces an already scarce ammonia by more than another 99%.

5.4 Computational expense

In this sub-section we assess the computational expense of the dissolution solver in the global model, comparing the hybrid, pseudo-transition and equilibrium configuration to a control run with dissolution disabled. (see Table 3 indicates the seasonally resolved computational expense for each of the solver configurations as a relative to control). The hybrid

- 25 configuration is most expensive in southern hemispheric winter and spring, which likely reflects increased occurrence of shorter time steps, matching with increases in CPU cost seen for the pseudo-transition configuration. In contrast, the equilibrium configuration is fastest at this time of year, being much slower in northern hemispheric winter, due to larger numbers of stiff grid boxes during the formation of nitrate aerosol. On yearly average, the hybrid configuration of the solver is only marginally more expensive than the equilibrium configuration but as seen in section 5.3 gives more accurate results.
- 30 The pseudo-transition configuration comes with more than double the amount of extra computation time. At the same time its seasonal dependence is much less pronounced. The extra amount of computational expense of the pseudo-transition configuration is most certainly related to the larger amount of multi-modal equilibration iterations required by this

configuration, as the estimation of the composition of the pseudo-transition modes is fully embedded into the iterative equilibration process among aerosol size <u>incrementclasses</u> (see above).

The absolute computation time required by the three configurations is indicated in the final column of Table 3. In analogy to the approach taken by Zaveri et al. (2008), we present this time interval as normalised per grid cell, aerosol size

- 5 increment<u>class</u> and time step. The present calculations were carried out on the phase 2a configuration of the UK national supercomputing resource "High End Computing Terrascale Resource" (HECToR)-, with 8 AMD Opteron Quad Core 2.3 GHz nodes (32 CPUs). Although we have-multiplied by the CPU number we realise that computation time is not proportional to the number of CPUs, nor is it inversely proportional to the number of size increment<u>classe</u>s. Nevertheless, the calculation may allow a useful way to roughly compare to the cost of other published solvers. The present solver was
- 10 written in a way that the number of internal time steps required by the dynamic sub-solver does not normally exceed two or three, considering that <u>incrementclasses</u> requiring a higher number of internal time steps are typically in equilibrium with respect to the overall time step. In doing so, it is ensured that the internal time step of the solver tends to increase in parallel with the overall time step. Other solvers might not follow this approach, thus adding to the complexity of comparing computational expense.
- 15 Zaveri et al. (2008) obtained an average computational expense of about 125 μs on a single INTEL Xeon single-core 3 GHz CPU (without providing any further information about the system that was used), while the expense of the new solver in the hybrid regime is less than 20 μs. However, the reader should note that MOSAIC also resolves liquid-solid phase <u>processes</u>equilibria, used 8 size <u>binclasses</u> rather than 4, that their time step was 5 minutes rather than 15, that the number of CPUs was one rather than 32, and that <u>the figure given by Zaveri et al. (2008) includes the computational expense of the</u>
- 20 <u>aerosol microphysicsinformation given on their system is insufficient to allow for a reliable comparison.</u> For this reason, a more appropriate comparison between the MOSAIC and the HyDiS-1.0 computational expense might be obtained as the figure of 20 µs is doubled for the computational expense of the microphysics within GLOMAP to be taken into account conservatively. Although, the above mentioned normalisation may filter some of the effects of these limitationselements, which may also be counterbalancing to some extent, it appears that the schemes are very dissimilar and the reader should
- 25 only take these figures as an indication that the solvers' computational expense seems to roughly be of the same order of magnitude.

6 Conclusion

Within this paper we have presented the new dissolution solver HyDiS-1.0. The formalism of the solver allows a maximum of three chemically interdependent species to dissolve conjointly, and combines an aerosol size selective equilibrium and

30 dynamic approach. Depending on tailored decision criteria <u>size classes</u> that are diagnosed to be in non-equilibrium are treated fully dynamically, species selectively dynamically or corrected with an ad hoc approximate method that relies on the estimation of the equilibration time with respect to a pre-defined driving species. <u>In particular, a certain number of specific</u> numerical schemes were developed, such as an adaptive time stepping method that largely sets the time step as a function of the overal time step of the model, and equilibrium solvers for chemically and gas-phase driven dissolution that are based on a species interactive analytical and a variational principle, respectively.

The numerical stability and accuracy of the new solver was investigated through box model experiments. In order to 5 maximise the numerical stiffness property, the box model experiments were partially performed beyond the realistic range of atmospheric concentrations of dissolving species. Full equilibrium runs have been found to exhibit a slight numerical drift under the latter conditions of extreme numerical stiffness. Results obtained with two dissolving species show a very high level of accuracy in the hybrid configuration to the extent that they are barely distinguishable from fully dynamic results. Similarly, with three dissolving species, the level of accuracy is high under the most prevalent atmospheric conditions,

- 10 except for the most polluted ones, for which a non-negligible amount of bias is discernible. The bias is related to a competition effect between more than one driving species to dissolution, for which situation we have not yet found a more accurate formalism that associates numerical stability with computational efficiency under stiff conditions. In its hybrid configuration the solver allows reproducing a certain number of remarkable dynamical phenomena, such as slow transition to equilibrium due to inter-modal competition at low gas phase concentrations or chemical interaction at high concentration
- 15 of dissolving species, or dynamical equilibrium under external forcing conditions imposed via an ambient temperature cycle. First results from an implementation of the solver in a global modelling environment of an aerosol and chemistry transport model have confirmed its computational efficiency and its formal and numerical reliability. The additional expense of computation time is of the order of 10% only in both the hybrid and equilibrium configuration, which compares favourably to a pre-existing hybrid scheme. Despite some important model limitations, tThe results obtained are to the least in
- 20 reasonable agreement with an inventory of measurement data under polluted conditions, and underline the relevance of the dynamic property of the dissolution of inorganic species for the accurate representation of aerosol composition. The validation of the solver against global measurement data sets and the evaluation of non-equilibrium effects to aerosol composition will be addressed in greater detail within follow-on publications. With respect to the existing model limitations, more development will be required for the aerosol inorganic composition to be simulated more accurately.

25 7 Code availability

The code for the dissolution solver, as used in the TOMCAT-GLOMAP simulations, can be made available to reviewers upon request via the GLOMAP code repository as maintained at the University of Leeds by Dr. Kirsty Pringle (K.Pringle@leeds.ac.uk) and Dr. Steven Pickering (isssjp@leeds.ac.uk).

References

5

15

25

Adams, P. J., Seinfeld, J. H., and Koch, D. M.: Global concentrations of tropospheric sulfate, nitrate, and ammonium aerosol simulated in a general circulation model, J. Geophys. Res._-Atmos., 104, 13791–13824, doi:10.1029/1999JD900083, 1999. Breider, T. J., Chipperfield, M. P., Richards, N. A. D., et al.: Impact of BrO on dimethylsulfide in the remote marine

Bouwman, A. F., Lee, D. S., Asman, W. A. H., et al.: A global high-resolution emission inventory for ammonia, Global Biogeochem. Cy., 11(4), 561-587, 1997.

boundary layer, Geophys. Res. Lett., 37, L02807, doi:10.1029/2009GL040868, 2010.

Capaldo, K. P., Pilinis, C., and Pandis, S. N.: A computationally efficient hybrid approach for dynamic gas/aerosol transfer in air quality models, Atmos. Environ., 34, 3617-3627, 2000.

10 Chipperfield, M. P.: New version of the TOMCAT/SLIMCAT offline chemistry transport model, Q. J. Roy. Meteor. Soc. 132, 1179–1203, 2006.

Dentener, F., Kinne, S., Bond, T., et al.: Emissions of primary aerosol and precursor gases in the years 2000 and 1750 prescribed data-sets for AeroCom, Atmos. Chem. Phys., 6, 4321–4344, doi:10.5194/acp-6-4321-2006, 2006.

Eldering, A., Solomon, P. A., Salmon, L. G., Fall, T., and Cass, G. R.: Hydrochloric acid: A regional perspective on concentration and formation in the atmosphere of Southern California, Atmos. Environ., 25A(10), 2091-2102, 1991.

Erickson III, D. J., Seuzaret, C., Keene, W. C., and Gong, S. L.: A general circulation model based calculation of HCl and ClNO₂ production from sea salt dechlorination: Reactive Chlorine Emissions Inventory, J. Geophys. Res. Atmos., 104(7), 8347-8372, 1999.

Feng, Y. and Penner, Y.: Global modeling of nitrate and ammonium: Interaction of aerosols and tropospheric chemistry, J.

20 Geophys. Res. Atmos., 112, doi:10.1029/2005JD006404, 2007.

Fountoukis, C. and Nenes, A.: ISORROPIA II: a computationally efficient thermodynamic equilibrium model for $K^+ - Ca^{2+} - Mg^{2+} - NH_4^+ - Na^+ - SO_4^{2-} - NO_3^- - Cl^- - H_2O$ aerosols, Atmos. Chem. Phys., 7, 4639-4659, doi:10.5194/acp-7-4639-2007, 2007.

Hu, X.-M., Y. Zhang, Y., Jacobson, M. Z., and Chan, C. K.: Coupling and evaluating gas/particle mass transfer treatments for aerosol simulation and forecast, J. Geophys. Res., 113, D11208, doi:10.1029/2007JD009588, 2008.

Jacobson, M. Z.: Numerical techniques to solve condensational and dissolutional growth equations when growth is coupled to reversible reactions, Aerosol Sci. Technol., 27, 491–498, 1997.

Jacobson, M. Z.: Fundamentals of Atmospheric Modeling, Cambridge University Press, Cambridge, 1999a.

Jacobson, M. Z., Studying the effects of calcium and magnesium on size-distributed nitrate and ammonium with 30 EQUISOLV II, Atmos. Environ., 33, 3635-3649, 1999b. Jacobson, M. Z.: Analysis of aerosol interactions with numerical techniques for solving coagulation, condensation, dissolution, and reversible chemistry among multiple size distributions, J. Geophys. Res., 107(D19), 4366, doi:10.1029/2001JD002044, 2002.

Jacobson, M. Z.:, A solution to the problem of nonequilibrium acid/base gas-particle transfer at long time step, Aerosol Sci. Technol., 39, 92–103, 2005.

5

15

Jacobson, M. Z., Tabazadeh, A., and Turco, R. P.: Simulating equilibrium within aerosols and nonequilibrium between gases and aerosols, J. Geophys. Res. Atmos., 101(4), 9079-9091, 1996.

Kim, Y. P., Seinfeld, J. H., and Saxena, P.: Atmopsheric gas-aerosol equilibrium I. Thermodynamic model. Aerosol Sci. Technol., 19, 157–181, 1993.

10 Lowe, D., Topping, D., and McFiggans, G.: Modelling multi-phase halogen chemistry in the remote marine boundary layer: investigation of the influence of aerosol size resolution on predicted gas- and condensed-phase chemistry, Atmos. Chem. Phys., 9, 4559–4573, doi:10.5194/acp-9-4559-2009, 2009.

Mann, G. W., Carslaw, K. S., Spracklen, D. V., Ridley, D. A., Manktelow, P. T., Chipperfield, M. P., Pickering, S. J., and Johnson, C. E.: Description and evaluation of GLOMAP-mode: a modal global aerosol microphysics model for the UKCA composition-climate model, Geosci. Model Dev., 3, 519-551, doi:10.5194/gmd-3-519-2010, 2010.

- Martin, S. T., Hung, H.-M., Park, R. J., et al.: Effects of the physical state of tropospheric ammonium-sulfate-nitrate particles on global aerosol direct radiative forcing, Atmos. Chem. Phys., 4, 183–214, 2004.
 Meng, Z. and Seinfeld, J.: Time scales to achieve atmospheric gas-aerosol equilibrium for volatile species, Atmos. Environ., 30, 2889–2900, 1996.
- Metzger, S. and Lelieveld, J.: Reformulating atmospheric aerosol thermodynamics and hygroscopic growth into fog, haze and clouds, Atmos. Chem. Phys., 7, 3163–3193, doi:10.5194/acp-7-3163-2007, 2007.
 Metzger, S., Dentener, F., Pandis, S., and Lelieveld, J.: Gas/aerosol partitioning: 1. A computationally efficient model, J. Geophys. Res. Atmos., 107(16), 4312, 10.1029/2001JD001102, 2002a.
 Metzger, S., Dentener, F., Krol, M., Jeuken, A., and Lelieveld, J.: Gas/aerosol partitioning 2. Global modeling results, J.
- Geophys. Res. Atmos., 107(D16), 4313, doi:10.1029/2001JD001103, 2002b.
 Millero, F. J., Feistel, R., Wright, D. J., and McDougall, T. J.: The composition of Standard Seawater and the definition of the Reference-Composition Salinity Scale, Deep Sea Research I, 55, 50-72, 2008.
 Morgan, W. T., Allan, J. D., Bower, K. N., Highwood, E. J., Liu, D., McMeeking, G. R., Northway, M. J., Williams, P. I., Krejci, R., and Coe, H.: Airborne measurements of the spatial distribution of aerosol chemical composition across Europe
- and evolution of the organic fraction, Atmos. Chem. Phys., 10, 4065–4083, doi:10.5194/acp-10-4065-2010, 2010.
 Nemitz, E., Sutton, M. A., Wyers, G. P., and Jongejan, P. A. C.: Gas-particle interactions above a Dutch heathland: I. Surface exchange fluxes of NH₃, SO₂, HNO₃ and HCl, Atmos. Chem. Phys., 4, 989–1005, doi: 1680-7324/acp/2004-4-989, 2004.

Nenes, A., Pandis, S. N., and Pilinis, C.: ISORROPIA: A new thermodynamic equilibrium model for multiphase multicomponent inorganic aerosols, Aquat. Geochem., 4, 123–152, 1998a.

Pringle, K. J., Tost, H., Metzger, S., Steil, B., Giannadaki, D., Nenes, A., Fountoukis, C., Stier, P., Vignati, E., and Lelieveld, JE.: Description and evaluation of GMXe: a new aerosol submodel for global simulations (v1), Geosci. Model Dev., 3, 391–

- 5 412, doi:10.5194/gmd-3-391-2010, 2010.
 Pruppacher, H. R., and Klett, J. D.: Microphysics of Clouds and Precipitation, Atmospheric and Oceanographic Sciences Library, Vol. 18, Kluwer Academic Publishers, Dordrecht, The Netherlands, 1997.
 Schmidt, A., Carslaw, K. S., Mann, G. W., Wilson, M., Breider, T. J., Pickering, S. J., and Thordarson, T.: The impact of the 1783-1784 AD Laki eruption on global aerosol formation processes and cloud condensation nuclei, Atmos. Chem. Phys., 10,
- 6025–6041, doi:10.5194/acp-10-6025-2010, 2010.
 Shi, Q., Davidovits, P., Jayne, J. T., Worsnop, D. R., and Kolb, C. E.: Uptake of gas-phase ammonia. 1. Uptake by aqueous surfaces as a function of pH, J. Phys. Chem. A, 103, 8812-8823, 1999.
 Spracklen, D. V., Pringle, K. J., Carslaw, K. S., et al.: A global off-line model of size-resolved aerosol microphysics: I. Model development and prediction of aerosol properties, Atmos. Chem. Phys., 5, 2227–2252, doi:10.5194/acp-5-2227-2005,
- 15 2005.

Swartz, E., Shi, Q., Davidovits, P., Jayne, J. T., Worsnop, D. R., and Kolb, C. E.: Uptake of gas-phase ammonia. 2. Uptake by sulfuric acid surfaces, J. Phys. Chem. A, 103, 8824-8833, 1999.

Topping, D. O., G. B. McFiggans, G. B., and Coe, H.: A curved multi-component aerosol hygroscopicity model framework. Part 1: Inorganic compounds, Atmos. Chem. Phys., 5, 1205–1222, 2005a.

- Topping, D. O., G. B. McFiggans, G. B., and Coe, H.:, A curved multi-component aerosol hygroscopicity model framework. Part 2: Including organic compounds, Atmos. Chem. Phys., 5, 1223–1242, 2005b. Topping, D. O., D. Lowe, D., and McFiggans, G.: Partial Derivative Fitted Taylor Expansion: An efficient method for calculating gas-liquid equilibria in atmospheric aerosol particles: 1. Inorganic compounds, J. Geophys. Res., 114, D04304, doi:10.1029/2008JD010099, 2009.
- 25 Topping, D. O., D., Lowe, D., and McFiggans, G.: Partial Derivative Fitted Taylor Expansion: an efficient method for calculating gas/liquid equilibria in atmospheric aerosol particles Part 2: Organic compounds, Geosci. Model Dev., 5, 1-13, doi:10.5194/gmd-5-1-2012, 2012.;

Trump, E., Fountoukis, C., Donahue, N. M., and Pandis, S. N.: Improvement of simulation of fine inorganic PM levels through better descriptions of coarse particle chemistry, Atmos. Environ., 102, 274-281, 2015.

Van der Werf, G. R., Randerson, J. T., Collatz, G. C., et al.: Carbon emissions from fires in tropical and subtropical ecosystems, Global Change Biol., 9(4), 547–562, 2003.
 Van Doren, J. M., Watson, L. R., Davidovits, P., Worsnop, D. R., Zahniser, M. S., and Kolb, C. E.: Temperature dependence of the uptake coefficients of HNO₃, HCl, and N₂O₅ by water droplets, J. Phys. Chem., 94, 3265-3269, 1990.

Wexler, A. S., and Seinfeld, J. H.: The distribution of ammonium salts among a size and composition dispersed aerosol, Atmos. Environ., 24A, 1231–1246, 1990.

Wexler, A. and Seinfeld, J. H.: Analysis of aerosol ammonium nitrate: Departures from equilibrium during SCAQS, Atmos. Environ., 26A, 579–591, 1992.

Xu, L., and Penner, J. E.: Global simulations of nitrate and ammonium aerosols and their radiative effects, Atmos. Chem. Phys., 12, 9479–9504, doi:10.5194/acp-12-9479-2012, 2012.
 Zaveri, R. A., R. C. Easter, R. C., and Wexler, A. S.: A new method for multi-component activity coefficients of electrolytes in aqueous atmospheric aerosols, J. Geophys. Res., 110, D02201, doi:10.1029/2004JD004681, 2005.

Zaveri, R. A., Easter, R. C., Fast, J. D., and Peters, L. K.: Model for Simulating Aerosol Interactions and Chemistry (MOSAIC), J. Geophys. Res., 113, D13204, doi:10.1029/2007JD008782, 2008.



Figure 1: Ambient (='atm') and particleaerosol surface (='part') partial pressures given as molecular number concentration equivalents of (a) NH_3 and (b) HNO_3 as a function of time, in a typical example of how chemical interaction may lead to oscillations and thus limit the numerical integration time step. For both species, initial ambient concentrations are equivalent to 1

- 5 ppb. Species are dissolving into a monodisperse aerosol at standard temperature and pressure conditions, relative humidity is 80%, dry particle size is r=50mm, their concentration is 100 cm⁻³. Initially, the aerosol liquidagueous phase contains no dissolved species. The temporal evolution of the partial pressures is simulated with the Jacobson (1997) scheme, integrated at fixed time steps of 10 and 30 seconds, respectively. The 3 characteristic stages of the equilibration of the particle liquidagueous phase with the gas phase are indicated apparent (I-III, see text). Phase 1 is equivalent to the initial 200 s of fast dissolution of NH₃ at almost
- 10 constant surface pressure. Phase 2 corresponds to the next 200 s during which surface pressure of NH₃ increases along with pH, thus leading to the dissolution of HNO₃. Phase 3 corresponds to the oscillating period during which the system is close to equilibrium as chemical interaction has become ineffective. Note that for both NH₃ and HNO₃ the atmospheric concentrations are sensibly equal at both timesteptime step. For the gas phase, the data obtained at a time step of 10 s (green) may thus not be distinguished from the one obtained at the larger time step (cyan).

15



Figure 2: Formalism of HyDiS-1.0 in its hybrid configuration.



Figure 3: Formalism of the dynamic solver.



Figure 4: Formalism of the equilibrium solver.



Figure 5: Box modelling evaluation of HyDiS-1.01 ppb runs with H₂SO₄ aerosol and initial mixing ratios of HNO₃(g) and NH₃(g) of 5 1 ppb (series 1, see text). The solver is run in the fully dynamic (=TRANS), hybrid dynamic and equilibrium (=HYBR), equilibrium with pseudo-dynamic correction (=PSEUDO) and full equilibrium configurations. Atmospheric volume mixing ratios

10

of ammonium and nitrate (a) and ammonium (b)in the aqueouserosol phase as a function of time for the Aitken (1), accumulation (2) and coarse (3) mode, respectively. For the coarse mode, the degree of saturation (4) with respect to ammonia and nitric acid and ammonia is also shown. A diurnal temperature cycle of T=298.15±5 K is imposed.



Figure 6: Same as Fig. 4 with initial mixing ratios of HNO₃(g) and NH₃(g) of 10 ppbfor the 10 ppb runs.



Figure 7: Same as Fig. 5 with initial mixing ratios of HNO₃(g) and NH₃(g) of 100 ppbfor the 100 ppb runs. The solver is not run in the fully dynamic configuration (=TRANS), by reason of extreme time step constraints under numerically stiff conditions.



Figure 8: 1 ppb runs Box modelling evaluation of HyDiS-1.0 with H₂SO₄ / sea salt aerosol and initial mixing ratios of HNO₃(g), NH₃(g) and HCl(g) of 1 ppbwith H₂SO₄ and sea salt aerosol (series 2, see text). The solver is run in the fully dynamic (=TRANS), hybrid dynamic and equilibrium (=HYBR), equilibrium with pseudo-dynamic correction (=PSEUDO) and full equilibrium

^{5 &}lt;u>configurations.</u> Atmospheric volume mixing ratios of <u>ammonium</u>, nitrate (a), <u>ammonium (b)</u> and chloride (c) in the a<u>queouserosol</u> phase as a function of time for the <u>nulceation</u>, Aitken (1) mode (=H₂SO₄), <u>and the</u> accumulation (2) and <u>the</u> coarse (3) mode (=sea <u>salt</u>), respectively. For the coarse mode, the degree of saturation (4) with respect to <u>nitric acid</u>, ammonia and <u>hydrochloricnitrie</u> acid is also shown. Note that due to the presence of sea salt, total chloride is larger than 1 ppb. A diurnal temperature cycle of T=298.15±5 K is imposed.



Figure 9: Same as Fig. 8 with initial mixing ratios of $HNO_3(g)$, $NH_3(g)$ and HCl(g) of 10 ppb for the 10 ppb runs. Note that due to the presence of sea salt, total chloride is larger than 10 ppb.



Figure 10: Same as Fig. 8 <u>with initial mixing ratios of HNO₃(g)</u>, NH₃(g) and HCl(g) of 100 ppbfor the 100 ppb runs. The solver is not run in the fully dynamic configuration (=TRANS), by reason of extreme time step constraints under numerically stiff conditions. Note that due to the presence of sea salt, total chloride is slightly larger than 100 ppb.

(a) GLOMAP-mode configuration for dissolution



(b) GLOMAP-mode standard configuration



Figure 11: Diagram illustrating the <u>speciecomponents</u> <u>containedresolved</u> in each size mode for the HyDiS-1.0 extended configuration of GLOMAP-mode (top) compared to that for the standard GLOMAP-mode (bottom), as described in Mann et al. (2010).

5



Figure 12: Comparison of 3-D CTM modelling results obtained with HyDiS-1.0 in the hybrid configuration (1) against observations (3), also compared directly on top of each other (2), for total aerosol nitrate (\underline{atop}), and ammonium ($\underline{bbottom}$) at ground level, <u>allboth</u> in $\mu g/m^3$ and annually averaged for the year 2002.



Figure 13: Top to bottom, July 2003 ground level nitrate fraction (-) in the Aitken (1), accumulation (2) and coarse (3) mode, and nitric acid gas phase (4) mixing ratio (ppt), obtained with the hybrid (a, on the left-column) and the equilibrium (b, on the right) configuration of HyDiS-1.0. The equilibrium gas phase mixing ratio is shown relative to the hybrid results.



Figure 14: Same as Figure 13 for ammonium (1-3) and ammonia (4).



Figure 15: Same as Figure 13 for January 2004.



Figure 16: Same as Figure 14 for January 2004.

Table 1: Box-model computation time required by HyDiS-1.0, given as fraction of the computation time used by the GLOMAP aerosol microphysical scheme.

	Sulphate Aerosol			Se	Sea Salt Aerosol		
	Hybrid	Pseudo	Equil	Hybrid	Pseudo	Equil	
1 ppb	0.31	0.29	0.16	0.74	0.40	0.30	
10 ppb	0.72	0.47	0.33	0.47	0.45	0.36	
100 ppb	0.81	0.47	0.20	0.59	0.50	0.35	

5

Table 2: Phase transition properties of aerosol components in HyDiS-1.0 extended GLOMAP:

Component	Interactive ^a	Condensable	Volatile ^b
Sulphate	Yes	Yes	No
Sodium ^c	Yes	No	No
Chloride ^d	Yes	No	No
Ammonium	Yes	Yes	Yes
Nitrate	Yes	Yes	Yes
Black carbon	No	No	No
Organic carbon	No	No	No
Dust	No	No	No

^aChemical interaction of <u>liquidaqueous</u> phase species according to Topping et al. (2009)

^bBoth volatile and condensable species are assessed with the new dissolution scheme.

10 ^cSea salt is assumed to be a mixture of NaCl and Na2SO4 (see text).

^dNon-volatile as gas phase chemistry of HCl is not available.

Table 3: 3-D CTM computation time requirements of HyDiS-1.0.

		%	CPU TIME ^b (µs)			
	APR	JUL	OCT	JAN	AVG	AVG
Hybrid	8.1	12.8	11.9	9.7	10.6	19
Pseudo	23.8	27.4	29.7	26.0	26.7	47
Equil	8.7	6.7	13.1	10.2	9.7	17

¹⁵

^aGiven as percentage of the total CPU time of the 3-D CTM without HyDiS-1.0.

^bAbsolute CPU time per grid cell, aerosol size <u>incrementclass</u> and time step (see text).