

1 **Sensitivity of Chemistry-Transport Model Simulations to the Duration of Chemical and**  
2 **Transport Operators: A Case Study with GEOS-Chem v10-01**

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14

15 **Abstract**

16 Chemistry-transport models involve considerable computational expense. Fine temporal  
17 resolution offers accuracy at the expense of computation time. Assessment is needed of the  
18 sensitivity of simulation accuracy to the duration of chemical and transport operators. We conduct  
19 a series of simulations with the GEOS-Chem chemistry-transport model at different temporal and  
20 spatial resolutions to examine the sensitivity of simulated atmospheric composition to operator  
21 duration. Subsequently, we compare the species simulated with operator durations from 10 min to  
22 60 min as typically used by global chemistry-transport models, and identify the operator durations  
23 that optimize both computational expense and simulation accuracy. We find that longer transport

24 operator duration increases concentrations of emitted species such as nitrogen oxides and carbon  
25 monoxide since a more homogeneous distribution reduces loss through chemical reactions and dry  
26 deposition, depending on the chemical regime. The increased concentrations of ozone precursors  
27 increase ozone production at longer transport operator duration. Longer chemical operator duration  
28 decreases sulfate and ammonium but increases nitrate due to feedbacks with in-cloud sulfur  
29 dioxide oxidation and aerosol thermodynamics. The simulation duration decreases by up to a factor  
30 of 5 from fine (5 min) to coarse (60 min) operator duration. We assess the change in simulation  
31 accuracy with resolution by comparing the root mean square difference in ground-level  
32 concentrations of nitrogen oxides, secondary inorganic aerosols, ozone and carbon monoxide with  
33 a finer temporal or spatial resolution taken as “truth”. Relative simulation error for these species  
34 increases by more than a factor of 5 from the shortest (5 min) to longest (60 min) operator duration.  
35 Chemical operator duration twice that of the transport operator duration offers more simulation  
36 accuracy per unit computation. However, relative simulation error from coarser spatial resolution  
37 generally exceeds that from longer operator duration; e.g. degrading from  $2^\circ \times 2.5^\circ$  to  $4^\circ \times 5^\circ$   
38 increases error by an order of magnitude. We recommend prioritizing fine spatial resolution before  
39 considering different operator durations in offline chemistry-transport models. We encourage  
40 chemistry-transport model users to specify in publications the durations of operators due to their  
41 effects on simulation accuracy.

## 42 **1 Introduction**

43 Global and regional chemistry-transport models (CTMs) have a wide range of applications in  
44 studies of climate, air quality, and biogeochemical cycling. The last few decades have witnessed  
45 rapid development of modeling sophistication to tackle these issues, but that development is  
46 associated with increasing computational expense. Typically, Eulerian models divide the

47 atmosphere into numerous ( $10^4$ - $10^8$ ) grid boxes and solve the mass continuity equation to simulate  
48 atmospheric composition. The concentrations of simulated species are sensitive to the duration of  
49 operators (e.g., chemistry, transport) used in the CTM. Attention is needed to understand how  
50 operator duration affects model performance.

51 Numerous studies have examined the sensitivity of simulations to grid resolution for ozone (Jang  
52 et al., 1995; Esler et al., 2004; Ito et al., 2009; Yu et al., 2016), ozone production efficiency (Liang  
53 and Jacobson 2000), and ozone sensitivity to precursor emissions (Cohan et al., 2006; Henderson  
54 et al., 2010). Simulation error increases proportional to the size of the horizontal grid (Wild and  
55 Prather, 2006; Prather et al., 2008). Biases can be reduced by simulating sub grid scale processes  
56 such as emission plumes from point sources (Sillman et al., 1990; Valin et al., 2011), aircraft  
57 exhaust (Kraabøl et al., 2002), ship exhaust (Vinken et al., 2011), mineral dust emissions (Ridley  
58 et al., 2013), and lightning (Cooper et al., 2014). The spatial and temporal resolution of the  
59 meteorological fields used in CTMs can also influence model processes (Bian et al., 2009). The  
60 spatiotemporal variation of carbon monoxide is better represented with finer grid resolution (Wang  
61 et al., 2004; Chen et al., 2009; Yan et al., 2014). Moreover, fine horizontal resolution is important  
62 for air quality exposure assessment and health impact studies (Punger and West, 2013; Fountoukis  
63 et al., 2013; Thompson et al., 2014; Li et al., 2015). Fine vertical resolution can better represent  
64 convection (Rind et al., 2007; Arteta et al., 2009). Simulations are also sensitive to operator  
65 durations (Mallet et al., 2007; Santillana et al., 2016), however, few studies have examined this  
66 sensitivity.

67 CTMs solve the continuity equation for tens to hundreds of chemical species, each with number  
68 density  $n$ , for individual grid boxes defined in the Eulerian model.

$$69 \quad \frac{\partial n}{\partial t} = -\nabla \cdot nU + P - L \quad (1)$$

70  $\partial n/\partial t$  represents the local temporal evolution of  $n$ .  $-\nabla \cdot nU$  represents the transport flux divergence  
71 term, where  $U$  is the wind velocity vector.  $P$  and  $L$  are the local production and loss terms  
72 respectively. Typically, the above equation is discretized in space, and the continuity equation is  
73 simulated as a system of coupled non-linear partial differential equations with chemical and  
74 transport operators. These chemical and transport operators are usually simulated sequentially  
75 through operator splitting to increase computational efficiency (Hundsdoerfer and Verwer, 2003).  
76 The transport operator involves solving the 3-D advection equation using efficient numerical  
77 schemes (Prather, 1986; Lin and Rood, 1996). The chemical operator representing the temporal  
78 evolution of local sources and sinks involves numerically solving a system of coupled ordinary  
79 differential equations using efficient solvers (Jacobson and Turco, 1994; Damian et al., 2002). The  
80 integration timestep in a differential equation solver is important for efficient and accurate solution  
81 (Jacobson and Turco, 1994). Moreover, the model accuracy is affected by the duration of chemical  
82 and transport operators (Mallet and Sportisse, 2006; Mallet et al., 2007), and the order in which  
83 these operators are applied (Sportisse, 2000; Santillana et al., 2016). The operator splitting method  
84 requires the coupling between individual operators to be negligible over the operator duration.  
85 However, reducing operator durations increases computational expense. Attention is needed to this  
86 tradeoff.

87 We examine the sensitivity of a CTM to operator duration by conducting a series of simulations at  
88 different horizontal resolutions and operator durations. We then identify the optimal operator  
89 duration from the range of operator durations from 10 min to 60 min usually used by global CTMs  
90 (e.g., Horowitz et al., 2003; Huijnen et al. 2010). Section 2 describes the sensitivity simulations,  
91 the method to quantify the simulation error, as well as the method to identify the simulation  
92 operator durations that best account for both computational expense and simulation accuracy.

93 Comparison of the sensitivity simulations, description of resolution-dependent errors, and the  
94 identification of appropriate chemical and transport operator durations are examined in section 3.

## 95 **2 Materials and Methods**

### 96 **2.1 GEOS-Chem simulations**

97 We conduct a series of sensitivity simulations with the GEOS-Chem CTM (version 10-01;  
98 [www.geos-chem.org](http://www.geos-chem.org)) at different horizontal resolutions and operator durations to examine the  
99 individual sensitivities to chemical and transport operator durations. The GEOS-Chem model (Bey  
100 et al., 2001) is used by about 100 research groups worldwide to simulate the oxidant-aerosol  
101 system. GEOS-Chem has the capability to be driven with several generations of assimilated  
102 meteorological data from the Goddard Earth Observing System (GEOS) at the NASA Global  
103 Modeling Assimilation Office (GMAO). For computational expedience, GEOS-Chem global  
104 simulations are often conducted using horizontal resolutions of either  $4^\circ \times 5^\circ$  or  $2^\circ \times 2.5^\circ$  degraded  
105 from the native resolution of GEOS meteorology. GEOS-Chem also has the capability for nested  
106 regional simulations where the global model provides dynamic boundary condition to the regional  
107 grids (Wang et al., 2004; Chen et al., 2009; Zhang et al., 2011; van Donkelaar et al., 2012). We  
108 use the GEOS-5 (or GEOS-5.2.0) meteorology available at a native horizontal resolution of  $0.5^\circ \times$   
109  $0.667^\circ$  (Rienecker et al., 2008). It includes three-hour averaged 2-D fields such as mixed layer  
110 depth, and six-hour averaged 3-D fields such as zonal and meridional wind, and convective mass  
111 flux. The height of the lowest level of the model is approximately 130 meters above the sea level,  
112 with 47 vertical levels.

113 GEOS-Chem performs species advection (A), vertical mixing (V), cloud convection (Z) and wet  
114 deposition (W) for every transport operator duration (T), as well as dry deposition (D), emissions

115 (E), photolysis (P), and chemistry (G) for every chemical operator duration (C) in the following  
116 order,

$$117 \quad A(T) \cdot D(C) \cdot E(C) \cdot V(T) \cdot Z(T) \cdot P(C) \cdot G(C) \cdot W(T) \quad (2)$$

118 The traditional transport operator durations are 30 minutes at  $4^\circ \times 5^\circ$  resolution, 15 minutes at  $2^\circ$   
119  $\times 2.5^\circ$  resolution, and 10 min at  $0.5^\circ \times 0.67^\circ$  resolution. The traditional chemical operator durations  
120 have varied from either 60 min or twice the transport operator duration based on the Strang  
121 operator splitting scheme (Strang, 1968) which follows  $T \cdot C \cdot T \cdot T \cdot C \cdot T$  order repetitively with  
122  $C = 2 \times T$ . Transport operations are repeated twice before a chemical operation when  $C = 2 \times T$ .  
123 We also test an alternate splitting scheme which follows  $T \cdot C \cdot T \cdot C$  order repetitively with  $C =$   
124  $T$ .

125 Advection is based on the multi-dimensional flux-form semi-Lagrangian advection scheme (Lin  
126 and Rood, 1996; Lin et al., 1994), with an additional pressure-fixer algorithm implemented for the  
127 conservation of species mass (Rotman et al., 2004). Transport by convection is coupled (Balkanski  
128 et al., 1993; Wu et al., 2007) with gas-aerosol wet deposition (Liu et al., 2001; Wang et al., 2011;  
129 Amos et al., 2012). GEOS-Chem uses an internal integration timestep of 5 min for convective  
130 mixing. We use a non-local boundary layer mixing scheme for vertical transport (Holtslag and  
131 Boville, 1993, Lin and McElroy, 2010).

132 Emissions are processed through the HEMCO module (Keller et al., 2014). A resistance-in-series  
133 method is used for dry deposition of species (Wesely, 1989; Wang et al., 1998; Zhang et al., 2001;  
134 Fisher et al., 2011).

135 GEOS-Chem uses a Sparse Matrix Vectorized GEAR II chemistry solver (Jacobson and Turco,  
136 1994; Jacobson, 1995; 1998). The oxidant-aerosol chemistry simulation includes organic and black

137 carbon (Park et al., 2003), mineral dust (Fairlie et al., 2007; Zender et al., 2003; Ginoux et al.,  
138 2001), sea salt (Alexander et al., 2005; Jaegle et al., 2011), and the sulfate-nitrate-ammonium  
139 system (Park et al., 2004). The photolysis frequency is calculated (Mao et al., 2010; Eastham et  
140 al., 2014) at the middle of the chemical operator duration using the Fast-JX algorithm (Bian and  
141 Prather, 2002). Simulation of gas-aerosol interactions are performed by aerosol extinction effects  
142 on photolysis rates (Martin et al., 2003), and heterogeneous chemistry (Jacob, 2000) including  
143 aerosol uptake of  $\text{N}_2\text{O}_5$  (Evans and Jacob, 2005) and  $\text{HO}_2$  (Mao et al., 2013). The ISORROPIA II  
144 thermodynamic module (Fontoukis and Nenes, 2007) performs aerosol-gas partitioning (Pye et al.,  
145 2009).

146 We conduct simulations for 2010 July at two horizontal resolutions of  $4^\circ \times 5^\circ$  and  $2^\circ \times 2.5^\circ$  globally,  
147 and  $0.5^\circ \times 0.667^\circ$  over the North America ( $140^\circ\text{W}$ – $40^\circ\text{W}$ ,  $10^\circ\text{N}$ – $70^\circ\text{N}$ ) and East Asia ( $70^\circ\text{W}$ –  
148  $150^\circ\text{W}$ ,  $11^\circ\text{S}$ – $55^\circ\text{N}$ ) nested regions. We use the  $4^\circ \times 5^\circ$  global simulation to archive dynamic  
149 boundary conditions every three hours for the nested simulations. We use one month spin up with  
150 each GEOS-Chem simulation to reduce the influence of initial conditions.

## 151 **2.2 Computing platform**

152 We conduct all simulations on the same computing platform to compare their computational  
153 performance. We use the Glooscap cluster of the Atlantic Computational Excellence Network  
154 (ACENET) Consortium of Canadian Universities (<http://www.ace-net.ca/wiki/Glooscap>). The  
155 operating system is Linux 4.8. We use Intel Fortran compiler version 12. Each GEOS-Chem  
156 simulation is submitted as a 16-thread parallelized job on a single node.

157 We calculate the CPU time for the month of July for each operator separately using the Fortran-  
158 intrinsic routine, CPU\_TIME. We found this value identical to the one calculated using the Linux

159 command ‘qacct -j’. To reduce the effects of other jobs on the shared cluster, we repeat simulations  
160 five times, while excluding data output operations to minimize sensitivity to system input/output,  
161 and use the median to represent CPU time.

### 162 **2.3 Assessing the relative simulation error**

163 We treat the simulation with the shortest operator duration as the most accurate. This approach  
164 exploits the reduction in error associated with coupling across operators as operator duration  
165 diminishes. Assessing simulation error versus operator duration through comparison with  
166 observations is impaired by imperfect model processes, by the sparseness of measurements, and  
167 by model-observation representativeness biases. We take as “truth” the concentrations simulated  
168 with a chemical operator duration (C) of 10 minutes and a transport operator duration (T) of 5  
169 minutes (represented as C10T05). Finer resolutions are computationally prohibitive. We define the  
170 relative simulation error  $E_{sim}^s$  for species  $s$  as the root mean square error (RMSE) of the species  
171 concentrations simulated with the finest resolution (“truth”) and the simulation under consideration  
172 ( $Sim$ ), normalized by the concentrations in simulation “truth”,

$$173 \quad E_{sim}^s = \frac{\sqrt{N} \sqrt{\sum_{i=1}^{i=N} (Truth_i^s - Sim_i^s)^2}}{\sum_{i=1}^{i=N} Truth_i^s} \quad (3)$$

175 where,  $i$  represents a particular grid box, with a total number of  $N$  grid boxes of interest. RMSE in  
176 the numerator is chosen instead of absolute difference to more heavily penalize extrema.  
177 Normalization with the mass of the “true” simulation is intended to cross-compare  $E_{sim}^s$  of different  
178 species.  $E_{sim}^s$  captures the variation of a species  $s$  from the “true” simulation.



179 Here, we focus on four key species relevant to atmospheric chemistry, namely nitrogen oxides  
 180 ( $\text{NO}_x = \text{NO} + \text{NO}_2$ ), secondary inorganic aerosols (SIA: sum of sulfate, nitrate and ammonium),  
 181 ozone ( $\text{O}_3$ ), and carbon monoxide (CO). These species represent a range of lifetimes from a day  
 182 ( $\text{NO}_x$ ) to weeks (CO). The focus on SIA is designed to devote more attention to chemically active  
 183 species than to mineral dust and sea salt. We sample the instantaneous values of simulated ground-  
 184 level concentrations of these atmospheric species every 60 min to span the diurnal variation of  
 185 chemical environments. We focus on concentrations in July near the Earth's surface when and  
 186 where chemical and transport timescales tend to be short.

## 187 **2.4 Identifying the optimal operator duration**

188 A practical way to select optimal chemical and transport operator durations is to identify the  
 189 simulation with the lowest error ( $E_{sim}^s$ ) per unit of computation time. To quantify the simulation  
 190 accuracy per unit CPU time, we propose a simple metric, the CPU-time adjusted Composite  
 191 Normalized Error (CNE) which represents a tradeoff between the simulation accuracy, and the  
 192 associated computation expense. This is performed by normalizing the relative simulation error  
 193  $E_{sim}^s$  for species  $s$  by the CPU time  $t$  for the simulation under consideration  $t_{sim}$  and for a reference  
 194 simulation  $t_{ref}$ , and taking the mean of four species.

$$195 \quad CNE = \left( \frac{1}{4} \times \sum_s \frac{E_{sim}^s}{E_{ref}^s} \right) \times \left( \frac{t_{sim}}{t_{ref}} \right) \quad (4)$$

197 We normalize  $E_{sim}^s$  by the reference  $E_{ref}^s$  so that the CPU-time adjusted Composite Normalized  
 198 Error for each species is of similar magnitude. The variation of CNE across operator durations is  
 199 unaffected by the choice of reference simulation; C10T10 used here. The relative value of CPU

200 time versus simulation accuracy is subjective and depends on scientific objective. This definition  
201 of CNE gives equal weighting to the respective cost of CPU time and simulation accuracy. The  
202 simulation with the lowest CNE is used to identify an optimal chemical and transport operator  
203 duration.

### 204 **3 Results and discussion**

205 Figure 1 shows the computational performance for the series of GEOS-Chem simulations  
206 conducted here. The CPU time decreases by factors of 3-5 from fine to coarse operator duration.  
207 The CPU time increases by about a factor of 4 from  $4^\circ \times 5^\circ$  to  $2^\circ \times 2.5^\circ$  and another factor of 2 to a  
208 single nested simulation at  $0.5^\circ \times 0.667^\circ$ . This linearity implies that grid boxes are sufficiently large  
209 that CPU time is proportional to the number of grid boxes, and that transport integration timesteps  
210 constrained by the Courant-Freidrich-Lewy criterion (Courant et al., 1967) are largely unaffected  
211 by changes to grid box size at these resolutions. Comparison of individual CPU times for chemical  
212 and transport operators shows that performing a single cycle of all chemical operations takes ~4  
213 times that of a single cycle of transport operations at the global scale. This factor is reduced for  
214 nested simulations due in part to the additional CPU time for simulating boundary conditions.

215 Figure 2 illustrates the sensitivity of the simulations to chemical and transport operators at  $2^\circ \times$   
216  $2.5^\circ$  horizontal resolution. The left column shows the species concentrations for the “true”  
217 simulation (C10T05). The middle column shows the difference in species concentrations from  
218 doubling the transport operator duration. Increasing the transport operator duration tends to  
219 increase concentrations of emitted species like CO and NO<sub>x</sub> over source regions since species are  
220 more uniformly mixed by long operator durations before loss processes such as deposition and  
221 chemistry occur. More homogeneous fields have lower dry deposition rates as a larger fraction is

222 mixed aloft, and lower chemical loss rates depending on the chemical regime. The increase in CO  
223 over source regions is partly associated with decreases in OH. Increasing concentrations of ozone  
224 precursors increases ozone production ( $P[O_3]$ ). Wild and Prather (2006) similarly found that ozone  
225 production increases at coarser horizontal resolution. Increasing the transport operator duration  
226 increases SIA components, especially over the source regions of East Asia, North India, and North  
227 America.

228 The right column in Fig. 2 shows the change in species concentrations from increasing the  
229 chemical operator duration. Hydroxyl radical concentrations increase,  $NO_x$  concentrations  
230 decrease, and  $P[O_3]$  decreases with increasing chemical operator durations over source regions.  
231 Berntsen and Isaken (1997) found that the error introduced by coarser chemical operator durations  
232 is higher in polluted regions than the clean background due to the increased time lag, and invariant  
233 production and loss across rapid chemical cycles. A longer chemical operator duration decreases  
234 sulfate and ammonium but increases nitrate over source regions. Inspection of  $SO_2$  and  $H_2O_2$  fields  
235 indicates that sulfate formation through  $H_2O_2$  in clouds decreases at longer chemical operator  
236 durations. In turn,  $SO_2$  and  $NH_3$  concentrations increase at longer chemical operator durations due  
237 to the corresponding decreases in ammonium sulfate or ammonium bisulfate. The additional free  
238 ammonia at longer chemical operator durations tends to promote regional ammonium nitrate  
239 formation depending on local thermodynamics. An increase of total SIA mass with the increasing  
240 chemical operator duration is driven by nitrate and ammonium, and partially compensated by a  
241 reduction in sulfate, especially downwind of source regions. We find similar spatial patterns for  
242 other operator duration combinations, and other horizontal resolutions.

243 Figure 3 shows the sensitivity of simulated species to changes in operator duration (C20T10 to  
244 C10T05) at two other horizontal resolutions (global  $4^\circ \times 5^\circ$ , and nested North America  $0.5^\circ \times 0.67^\circ$

245 simulations) considered here. Spatial patterns of monthly mean ground-level concentrations, and  
246 absolute differences are similar, albeit with finer spatial heterogeneity resolved in the nested  
247 simulation. However, some resolution dependent differences do arise reflecting nonlinear  
248 feedbacks.

249 Figures 4 shows the relative simulation error for nitrogen oxides, secondary inorganic aerosols,  
250 ozone and carbon monoxide with varying operator durations at  $2^\circ \times 2.5^\circ$  horizontal resolution.  
251 Relative simulation errors for all these major species increase by more than a factor of 5 from the  
252 shortest to longest operator duration. Errors increase fairly smoothly with increasing chemical and  
253 transport operator duration until the transport operator duration exceeds 30 min. Then errors  
254 increase by an order of magnitude for long lived species of  $O_3$  and CO. Relative simulation errors  
255 for other horizontal resolutions follows similar pattern. These relative errors are comparable to  
256 typical model-observation errors of  $\sim 30\%$  for  $NO_x$  (Boersma et al., 2008; Hudman et al., 2006)  
257 and 20 - 40% for SIA (Philip et al., 2014; Heald et al., 2012), while smaller than typical model-  
258 observation errors of  $\sim 20\%$  for ozone (Zhang et al., 2011; Wang et al., 2009) and 10 - 20% for CO  
259 (Duncan et al., 2007; Shindell et al., 2006).

260 Figure 5 shows the difference in simulated species at  $2^\circ \times 2.5^\circ$  horizontal resolution for the GEOS-  
261 Chem traditional (C30T15) minus the finest operator durations considered (C10T05). The spatial  
262 variation for the monthly mean ground-level concentrations is generally within 5-15% for short  
263 lived species like  $NO_x$  and SIA, and within 1% for longer lived species like  $O_3$  and CO. Santillana  
264 et al. (2016) similarly found an upper limit of 10% for operator splitting errors. However, the  
265 maximum hourly spatial variation can exceed 50% for short lived species and 5% for longer lived  
266 species. The spatial pattern of extrema resembles that of the monthly mean, albeit with more  
267 heterogeneity from synoptic variation.

268 We also examined the diurnal variation and vertical profile of extrema. Extrema arise from all  
269 times of day with a slight tendency for larger values for NO<sub>x</sub> at night, for ozone near sunrise and  
270 sunset, and for SIA and CO near noon. Zonal mean vertical profiles exhibit largest differences in  
271 the lower troposphere for NO<sub>x</sub> and SIA, with more homogeneous differences throughout the  
272 troposphere for O<sub>3</sub> and CO. Near the subtropical jets of the upper troposphere O<sub>3</sub> and CO have  
273 maximum extrema of up to 3%.

274 Figure 6 shows the CPU-time adjusted Composite Normalized Error for the GEOS-Chem  
275 simulations at various horizontal resolutions and operator durations. The CNE is significantly  
276 higher with C = T than C = 2 x T. We confirmed this tendency with different choices of “truth”  
277 (such as C05T05, C10T10) or reference (such as C10T05) simulations. This finding motivates the  
278 traditional approach of using C = 2 x T in GEOS-Chem simulations. Applying the chemical  
279 operator as frequently as the transport operator (with C = T) appears to increase computation cost  
280 with little benefit in accuracy. The CNE for all three horizontal resolutions have noisy minima  
281 with a chemical operator duration of 20 min and a transport operator duration of 10 min (C20T10).  
282 A unit of computation time has a similar efficiency for a small range of operator durations from  
283 10 min to 20 min. We found similar patterns in the variation of CNE with operator durations with  
284 CNE calculated for selected domains, such as over Northern Hemisphere, nested model regions,  
285 land grid boxes, and over the entire troposphere. We conducted additional simulations at 4° x 5°  
286 horizontal resolution for January 2011 with a spin up of 7 months, and found similar patterns in  
287 CNE.

288 The relative simulation error decreases by 40-50% (Fig. 4) by changing the operator duration from  
289 the traditional (C30T15) to the optimal (C20T10) at 2° x 2.5° horizontal resolution. The relative

290 spatial variations are <20% for NO<sub>x</sub> and SIA, and <1% for O<sub>3</sub> and CO. However, the CPU time  
291 increases by 20% by the decrease in operator duration.

292 Table 1 shows the relative simulation error at 4° x 5° horizontal resolution with “truth” at 2° x 2.5°  
293 resolution (C10T05) to investigate the tradeoff between horizontal resolution and operator  
294 duration. The simulation error for all species at 4° x 5° resolution increases by an order of  
295 magnitude compared to 2° x 2.5° resolution for any choice of operator duration tested here. The  
296 error in this configuration is insensitive to operator duration, and dominated by representativeness  
297 differences due to spatial structure resolved at 2° x 2.5° resolution, but not at 4° x 5° resolution.  
298 Nonlinear chemistry at different horizontal resolutions (e.g., Wild and Prather, 2006) also plays a  
299 role. Numerical errors due to advection processes generally exceed those from operator splitting  
300 (e.g., Prather et al., 2008; Santillana et al., 2016). We therefore recommend prioritizing horizontal  
301 resolution over operator duration for offline CTMs using time-averaged meteorological fields as  
302 tested here. As meteorological fields used in CTMs become available at finer temporal and spatial  
303 resolution, the value of shorter operator duration should further increase. We encourage the CTM  
304 users to specify the durations of operators in publications due to its effect on simulation accuracy.

#### 305 **4 Conclusions**

306 The computational expense of chemistry-transport models warrants investigation into their  
307 efficiency and accuracy. Solving the continuity equation in CTMs through operator splitting  
308 method offers numerical efficiency, however, few studies have examined the implications of  
309 operator duration on simulation accuracy. We conducted simulations with the GEOS-Chem model  
310 for multiple choices of operator duration from 10 min to 60 min as typically used by global CTMs.  
311 We found that longer transport operator durations increase ozone precursors and ozone production

312 over source regions since a more homogeneous distribution reduces loss through chemical  
313 reactions and dry deposition. Longer chemical operator durations decrease  $\text{NO}_x$  and ozone  
314 production over source regions. Longer chemical operator durations reduce sulfate and ammonium  
315 concentrations, however increase nitrate due to feedbacks with in-cloud  $\text{SO}_2$  oxidation and local  
316 aerosol thermodynamics.

317 We investigated the computational efficiency with the GEOS-Chem model, and found that the  
318 simulation computation time decreases by up to a factor of 5 from fine (C10T05) to coarse  
319 (C60T60) operator duration. The chemical operator consumes about four times the CPU time of  
320 the transport operator. We subsequently compared the root mean square differences in the ground-  
321 level concentrations of nitrogen oxides, secondary inorganic aerosols, ozone and carbon monoxide  
322 with a finer temporal or spatial resolution taken as “truth”, and estimated the relative simulation  
323 error. The relative simulation error for these species increases by more than a factor of 5 from the  
324 shortest to longest operator duration.

325 In order to account for simulation accuracy with computational cost, we proposed a metric, CPU-  
326 time adjusted Composite Normalized Error that identifies the operator duration with respect to  
327 CPU cost. We recommend the approach of using  $C = 2 \times T$  for all horizontal resolutions. The CNE  
328 exhibits a noisy minimum for a chemical operator duration of 20 min and transport operator  
329 duration of 10 min for the range of operator durations and horizontal resolutions considered here.  
330 Nonetheless, the relative simulation error from changing horizontal resolution exceeds that from  
331 changing operator durations within a horizontal resolution. We recommend prioritizing fine spatial  
332 resolution before considering different operator durations in offline CTMs with time-averaged  
333 archived meteorological fields as tested here. The importance of shorter operator durations should  
334 increase with the availability of time-averaged meteorological fields at higher temporal resolution.

335 Short operator durations could offer even greater benefits to simulation accuracy in online CTMs  
336 that offer meteorological fields at temporal resolutions closer to operator duration. We encourage  
337 the CTM users to specify in publications the durations of operators due to their effects on  
338 simulation accuracy.

### 339 **Code Availability**

340 The GEOS-Chem code is freely accessible to the public, by following the guidelines in  
341 <http://wiki.geos-chem.org/>). This work used GEOS-Chem version 10-01.

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723 Table 1: Comparison of mean\* relative simulation error versus horizontal resolution, with “truth”  
724 defined at 2° x 2.5° horizontal resolution

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Species	Mean relative simulation error (unitless)	
	4° x 5° resolution	2° x 2.5° resolution
Nitrogen oxides	2.1	0.092
Secondary inorganic aerosols	1.0	0.14
Ozone	0.17	0.004
Carbon monoxide	0.36	0.005

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727 \* Mean taken for operator durations  $\leq 30$  min.

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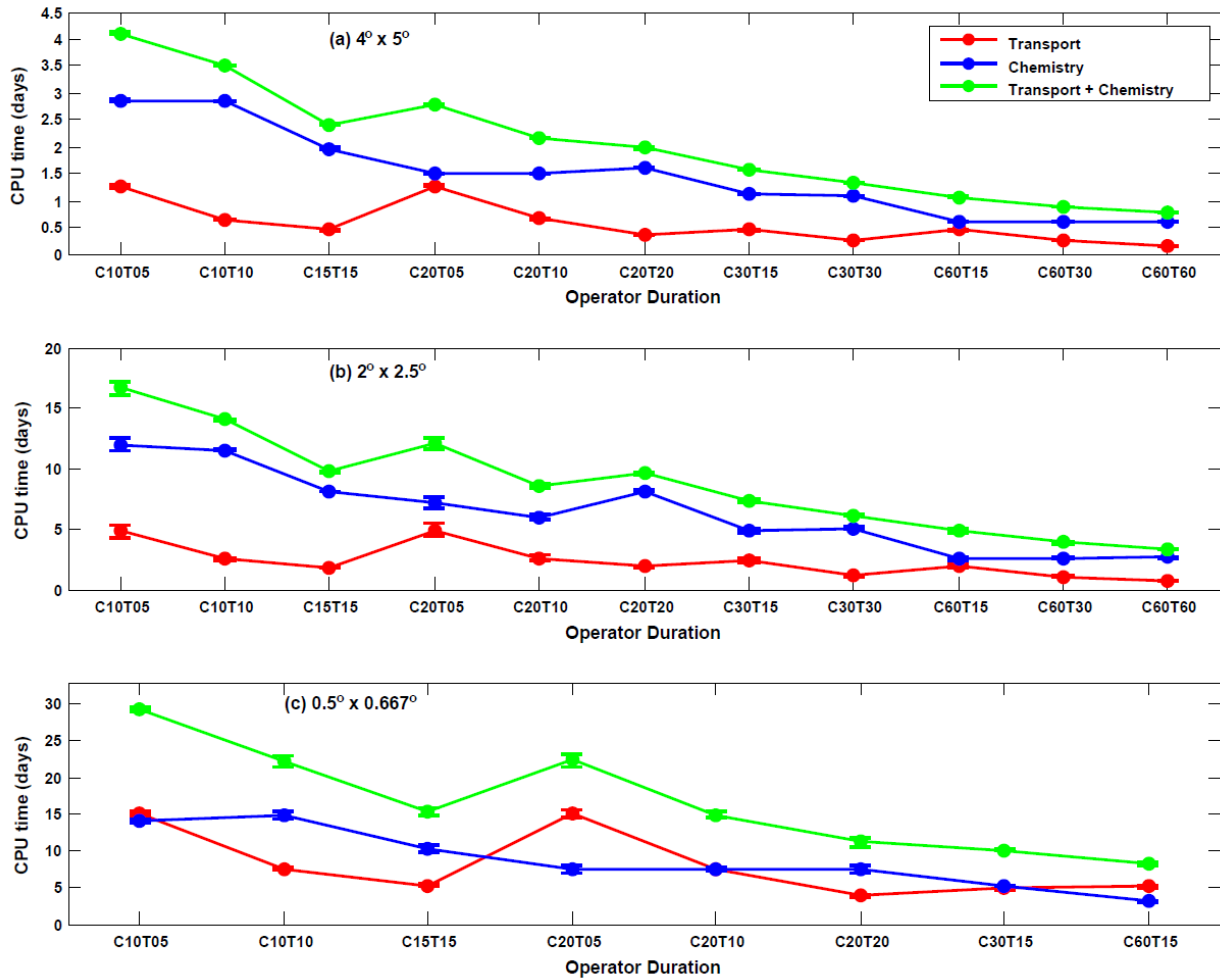
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741 Figure 1: CPU time for GEOS-Chem simulations with various operator durations at three  
 742 horizontal resolutions. Global simulations are at  $4^\circ \times 5^\circ$  (top) and  $2^\circ \times 2.5^\circ$  (middle) resolutions.

743 The bottom panel contains results for the average of two nested regions North America and East

744 Asia at  $0.5^\circ \times 0.667^\circ$  resolution. Colored lines represent the CPU time for simulating transport (red)

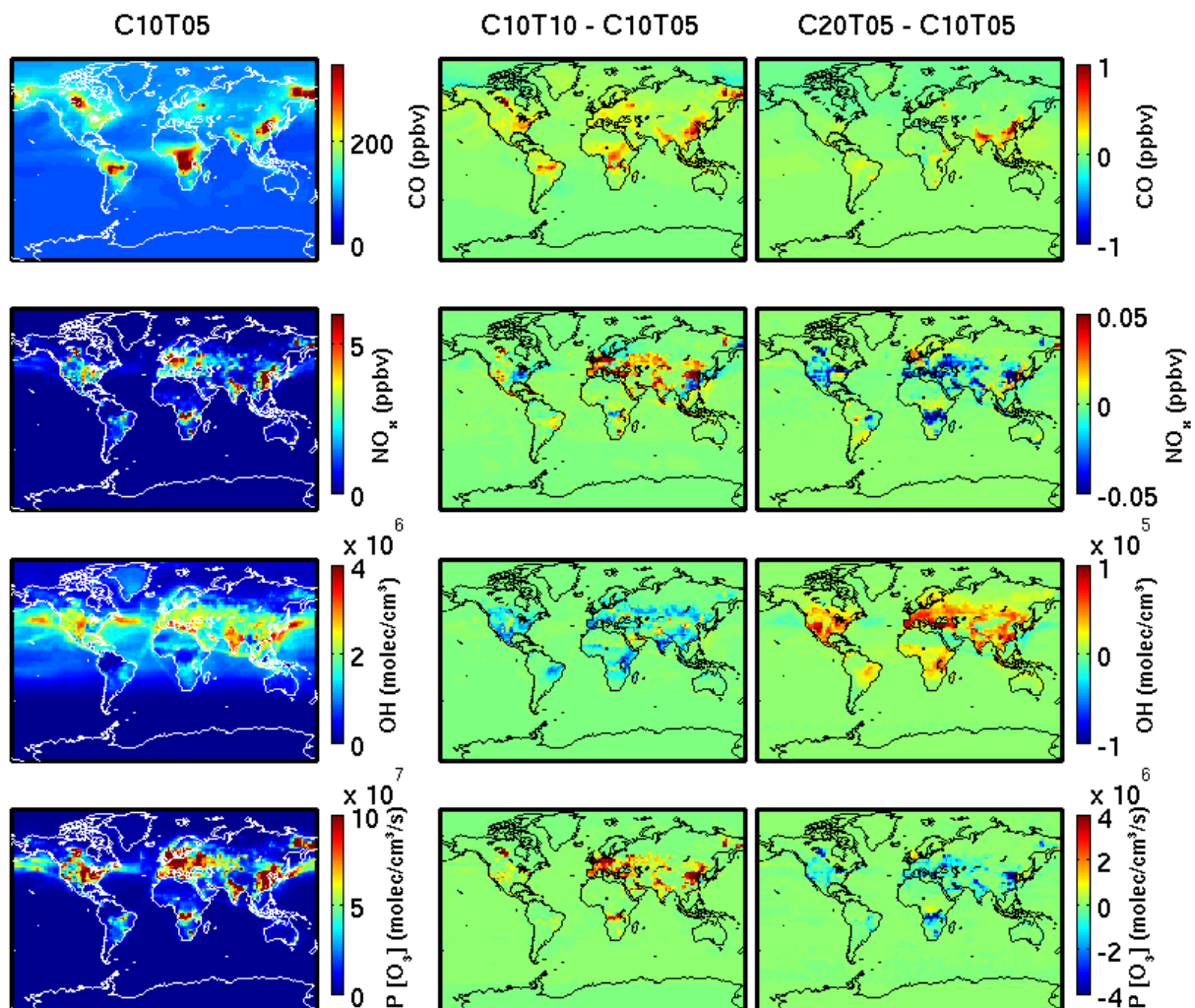
745 and chemical (blue) operators, and the sum of the two (green). Error bars represent standard error

746 over five simulations. Simulations are represented in the abscissa as CccTtt with chemical operator

747 duration, C = cc minutes, and transport operator duration, T = tt minutes.

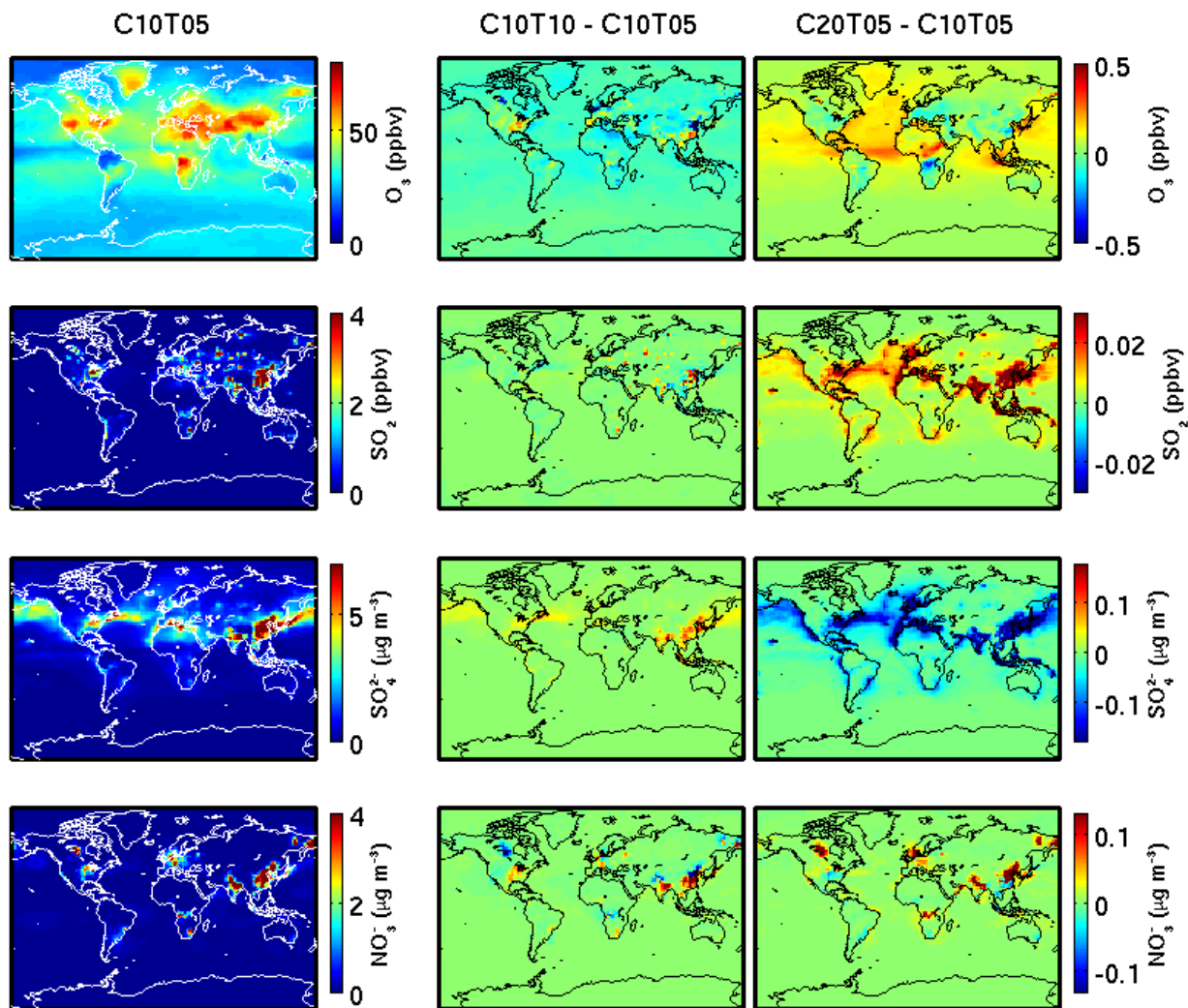
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 751 Figure 2a: Sensitivity of simulated species to the duration of chemical and transport operators. The  
 752 left column contains monthly mean ground-level concentrations simulated with the shortest  
 753 operator duration considered (C10T05) at  $2^\circ \times 2.5^\circ$  horizontal resolution. Other columns contain  
 754 the absolute differences from doubling the transport operator duration to C10T10 (middle), and  
 755 doubling the chemical operator duration to C20T05 (right). Each row from top to bottom  
 756 represents carbon monoxide (CO), nitrogen oxides ( $\text{NO}_x$ ), hydroxyl radical (OH), and the  
 757 production of ozone ( $\text{P}[\text{O}_3]$ ). Simulations are represented as CccTtt with chemical operator  
 758 duration, C = cc minutes, and transport operator duration, T = tt minutes.

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761 Figure 2b: As described in Fig. 2a, but each row from top to bottom represents ozone (O<sub>3</sub>), sulfur  
 762 dioxide (SO<sub>2</sub>), sulfate (SO<sub>4</sub><sup>2-</sup>), and nitrate (NO<sub>3</sub><sup>-</sup>) respectively.

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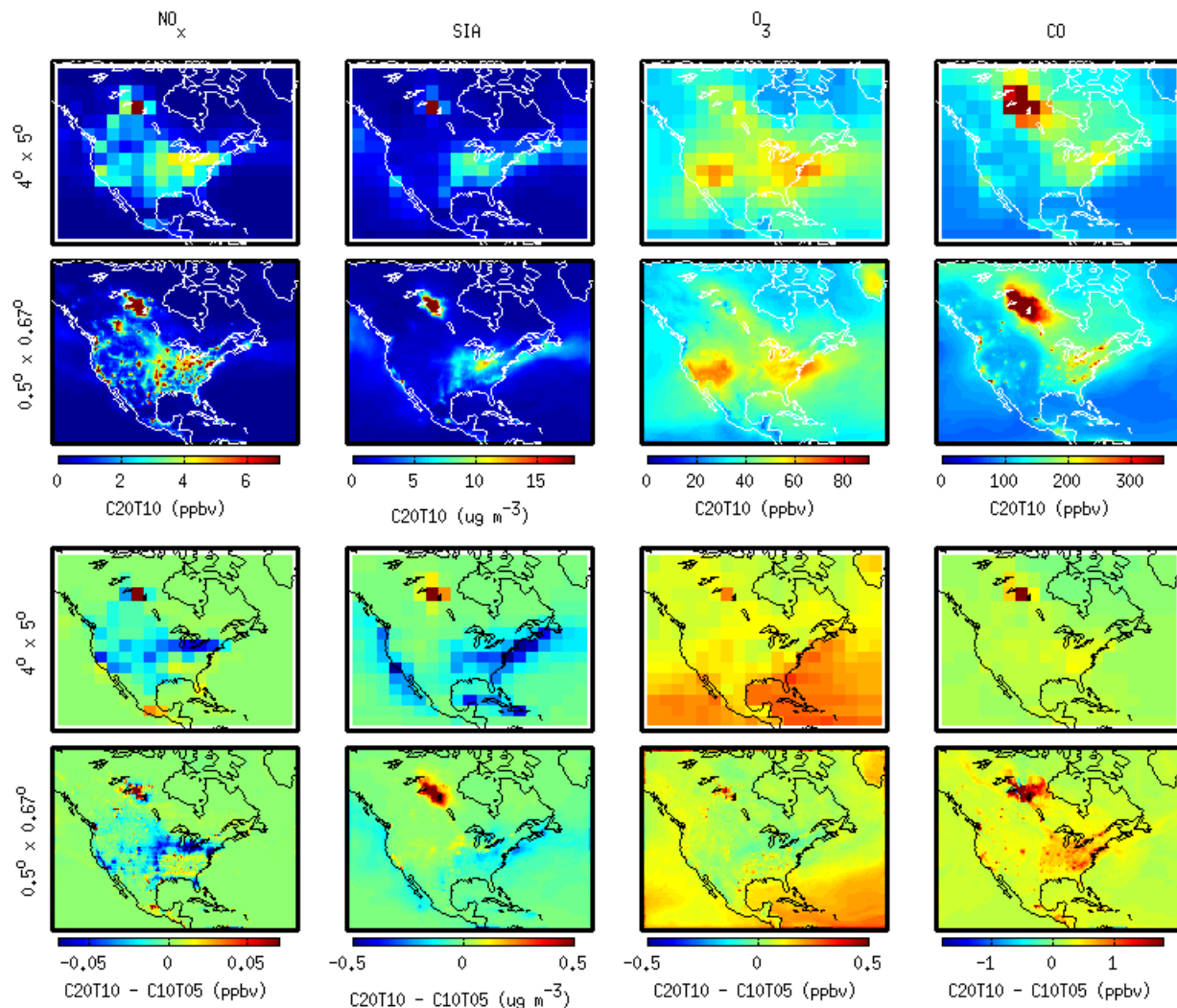
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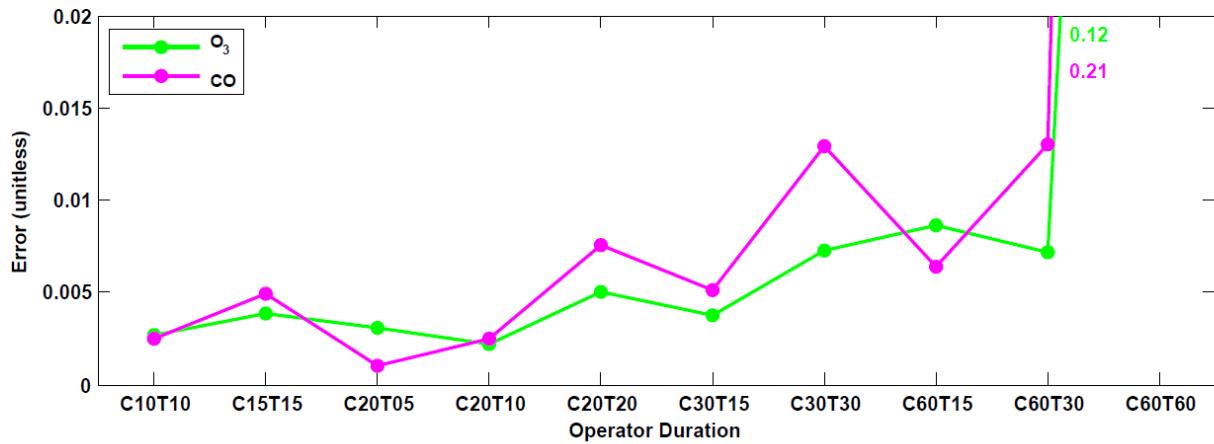
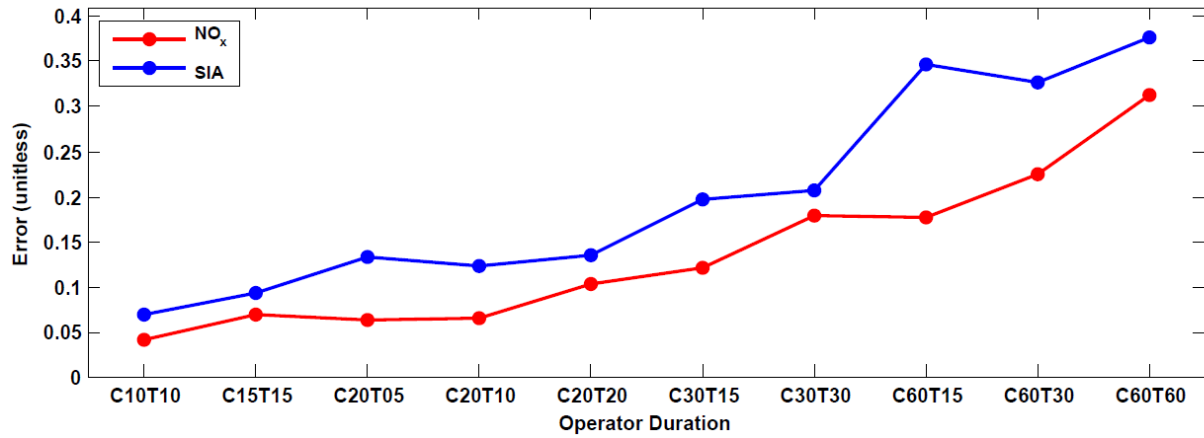
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 770 Figure 3: Sensitivity of simulated species to changes in operator duration (C20T10 to C10T05) at  
 771 two different horizontal resolutions over North America (global  $4^\circ \times 5^\circ$ , and nested  $0.5^\circ \times 0.67^\circ$   
 772 simulations). The top two rows contain monthly mean ground-level concentrations simulated with  
 773 the C20T10 operator duration for  $4^\circ \times 5^\circ$  (top row) and  $0.5^\circ \times 0.67^\circ$  (second row) resolutions. The  
 774 two lowest rows contain the monthly mean differences (C20T10 minus C10T05) for  $4^\circ \times 5^\circ$  (third  
 775 row) and  $0.5^\circ \times 0.67^\circ$  (bottom row) resolutions. Each column from left to right represents nitrogen  
 776 oxides ( $\text{NO}_x$ ), secondary inorganic aerosols (SIA), ozone ( $\text{O}_3$ ), and carbon monoxide (CO).  
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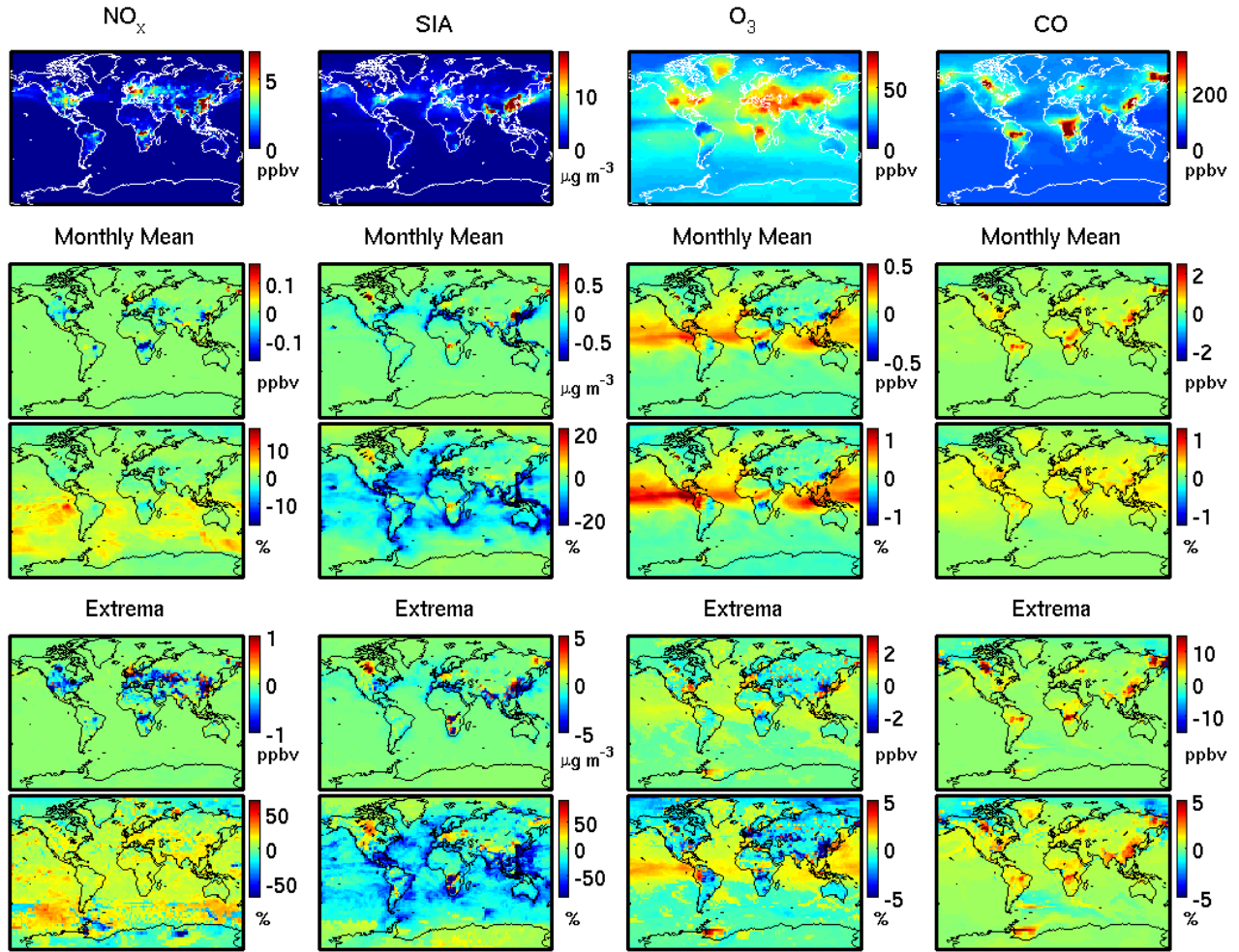
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779 Figure 4: Relative simulation error of different species ( $E_{sim}^s$ , eq. 3) for GEOS-Chem with various  
 780 operator durations at  $2^\circ \times 2.5^\circ$  horizontal resolution. Colored lines and dots represent the relative  
 781 simulation error for nitrogen oxides (NO<sub>x</sub>; red), secondary inorganic aerosols (SIA; blue), ozone  
 782 (O<sub>3</sub>; green), and carbon monoxide (CO; magenta). Simulations are represented in the abscissa as  
 783 CccTtt with chemical operator duration, C = cc minutes, and transport operator duration, T = tt  
 784 minutes.

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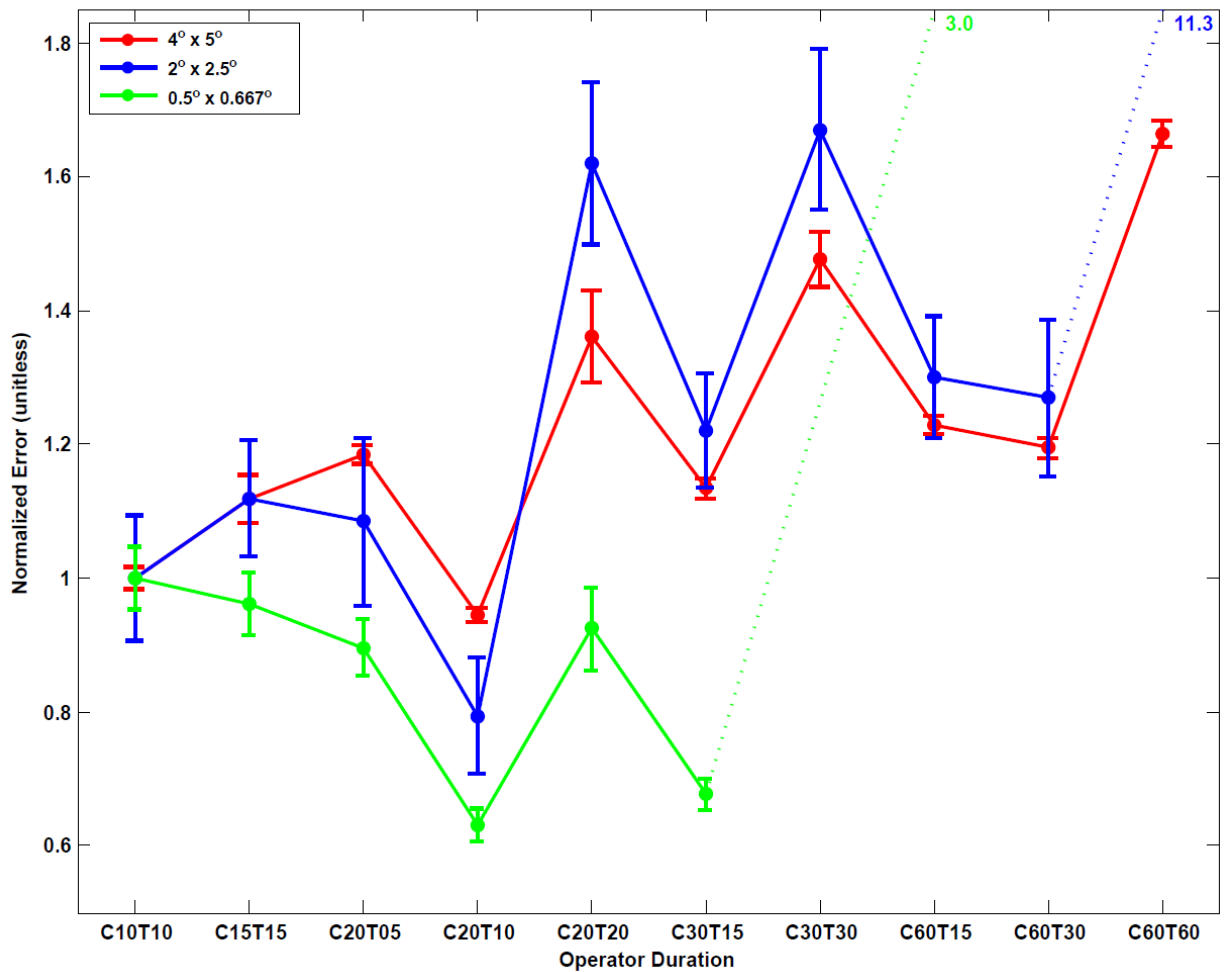
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790 Figure 5: Effect on simulated species of changing from the GEOS-Chem traditional operator  
 791 durations (C30T15) to the shortest operator durations considered (C10T05). The top row contains  
 792 monthly mean ground-level concentrations simulated with the C30T15 operator duration at  $2^\circ \times$   
 793  $2.5^\circ$  horizontal resolution. The next two rows contain the monthly mean differences (C30T15  
 794 minus C10T05) for absolute (second row) and relative (third row) differences. The two lowest  
 795 rows contain the maximum differences (C30T15 minus C10T05) for absolute (fourth row) and  
 796 relative (bottom row) differences. Each column from left to right represents nitrogen oxides ( $\text{NO}_x$ ),  
 797 secondary inorganic aerosols (SIA), ozone ( $\text{O}_3$ ), and carbon monoxide (CO).



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799 Figure 6: CPU-time adjusted Composite Normalized Error (CNE, eq. 4) for GEOS-Chem  
800 simulations with various horizontal resolutions and operator durations. Colored lines and dots  
801 represent the CNE for the global simulations at 4° x 5° (red) and 2° x 2.5° (blue), and the nested  
802 simulations at 0.5° x 0.667° (green) horizontal resolutions. Error bars represent standard error in  
803 CPU time. Simulations are represented in the abscissa as CccTtt with chemical operator duration,  
804 C = cc minutes, and transport operator duration, T = tt minutes.