



This discussion paper is/has been under review for the journal Geoscientific Model Development (GMD). Please refer to the corresponding final paper in GMD if available.

Singular vector based targeted observations of chemical constituents: description and first application of the EURAD-IM-SVA

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Received: 2 June 2015 – Accepted: 10 July 2015 – Published: 10 August 2015

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Published by Copernicus Publications on behalf of the European Geosciences Union.

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8, 6267–6307, 2015

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Abstract

Measurements of the large dimensional chemical state of the atmosphere provide only sparse snapshots of the state of the system due to their typically insufficient temporal and spatial density. In order to optimize the measurement configurations despite those limitations, the present work describes the identification of sensitive states of the chemical system as optimal target areas for adaptive observations. For this purpose, the technique of singular vector analysis (SVA), which has been proved effective for targeted observations in numerical weather prediction, is implemented into the chemical transport model EURAD-IM (EUROpean Air pollution and Dispersion – Inverse Model) yielding the EURAD-IM-SVA. Besides initial values, emissions are investigated as critical simulation controlling targeting variables. For both variants, singular vectors are applied to determine the optimal placement for observations and moreover to quantify which chemical compounds have to be observed with preference. Based on measurements of the airship based ZEPTEr-2 campaign, the EURAD-IM-SVA has been evaluated by conducting a comprehensive set of model runs involving different initial states and simulation lengths. Since the considered cases are restricted in terms of considered chemical compounds and selected areas, they allow for a retracing of the results and a confirmation of their correctness. Our analysis shows that the optimal placement for observations of chemical species is not entirely determined by mere transport and mixing processes. Rather, a combination of initial chemical concentrations, chemical conversions, and meteorological processes determine the influence of chemical compounds and regions. We furthermore demonstrate that the optimal placement of observations of emission strengths is highly dependent on the location of emission sources and that the benefit of including emissions as target variables outperforms the value of initial value optimisation with growing simulation length. The obtained results confirm the benefit of considering both initial values and emission strengths as target variables and of applying the EURAD-IM-SVA for measurement decision guidance with respect to chemical compounds.

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1 Introduction

In meteorology and atmospheric chemistry, both data assimilation and inverse modelling seek to combine observations from a given observation network set-up with a model to reduce forecast errors. In contrast, the objective of targeted observations is to optimize the observation network for data assimilation and ensuing simulations applying a given model (Berliner et al., 1998).

In numerical weather prediction, the optimal adaption of observations is a commonly investigated problem. It is typically studied to obtain a better estimate of initial values (Palmer, 1995). Events of explosive cyclogenesis at the North American east coast are often of highest relevance for European weather development and its forecast, and are therefore frequently taken as study objects to obtain better configured observation sites and times. In order to find sensitive initial states, Lorenz (1965) introduced the application of singular vectors to numerical weather prediction by estimating the atmospheric predictability of an idealized model. Singular vectors determine the directions of fastest linear perturbation growth over a finite time interval and identify thereby sensitive system states, where small variations of considered input parameters lead to a significant forecast change. The identified sensitive system states are optimal target areas for adaptive observations, which help to optimize the information content of our monitoring capabilities and grant a better control of the dynamic system evolution by data assimilation. Likewise, this method can be effectively used for campaign planning. Buizza et al. (2007) investigated the results of field campaigns applying singular vector based targeted observations, including FASTEX (Fronts and Atlantic Storm-Track Experiment), NORPEX (North-Pacific Experiment), CALJET (California Land-falling JETs Experiment), the Winter Storm Reconnaissance Programs (WSR99 /WSR00) and NATReC (North Atlantic THORPEX Regional Campaign), and stated that targeted observations are more valuable than observations taken in random areas. Yet, the extent of the impact is strongly dependent on regions, seasons, static observing systems, and prevailing weather regimes.

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The successful application of singular vector analysis within numerical weather prediction motivated to transfer this analysis method to chemical modelling, where studies attending targeted observations are rare. Khattatov et al. (1999) gave the earliest stimulus for adaptive observations of chemical compounds. By investigation of the linearised model, Khattatov et al. (1999) inferred, that a linear combination of 9 initial species' concentrations is sufficient to adequately forecast the concentrations of the complete set of 19 simulated species 4 days later. Hence, the problem of targeted observations of chemical compounds deals not only with the optimal placement of adaptive measurements, but also with the optimal set of chemical compounds to be measured. Liao et al. (2006) introduced the application of singular vector analysis to chemical weather prediction by estimating optimal adaptive measurements for chemical compounds. While Liao et al. (2006) especially focused on the optimal placement of observations, a later study (Goris and Elbern, 2013) adapted singular vector analysis following the objective of Khattatov et al. (1999) and applied the theory to identify the optimal set of chemical compounds to be measured.

Initial values are not the only uncertainty when considering atmospheric chemical modelling. Errors in boundary conditions, emission rates, and meteorological fields add to the uncertainty of the chemical forecast (Liao et al., 2006). With progressing simulation time, the forecast solution is driven more by emission and less by initial values. While trace gas emissions are a forcing mechanism of prime importance for reactive chemistry simulations, they are not known exactly enough (e.g. Granier et al., 2011). This feature enforces the inclusion of emission rates in the data assimilation procedure (Elbern et al., 2007) and the need of targeting adaptive measurements for emission rates. In a first step, Goris and Elbern (2013) applied both emissions and initial values as target variables for singular vector analysis in a box-model context, yielding a relevance ranking of chemical compounds to be measured, while the optimal placement of those compounds is beyond the scope of zero-dimensional simulations.

In this work, the approach of Goris and Elbern (2013) was generalized for a 3-dimensional chemistry transport model. The newly developed model set-up offers

5 a comprehensive application of singular vector analysis by combining the idea of Goris and Elbern (2013) with the approach of Liao et al. (2006). Its objective is the detection of sensitive locations and species for atmospheric chemistry transport models. Specifically, the following questions are addressed: (i) which chemical species have to be measured with priority, and (ii) where is the optimal placement for observations of these components? Both questions are addressed with respect to emission strengths and initial species concentrations.

10 The present paper is organized as follows: The theory of singular vector analysis is presented in Sect. 2, where the application on initial uncertainties and emission factors is described as well as the application of special operators. Singular vector analysis (SVA) is implemented into the 3-dimensional chemical transport model EURAD-IM (EUROpean Air pollution and Dispersion – Inverse Model, e.g., Elbern, 1997; Elbern and Schmidt, 1999; Elbern et al., 2007) yielding the EURAD-IM-SVA, which is described in Sect. 3. In order to test and validate the EURAD-IM-SVA, we focus on the model set-up of the ZEPTEr-2 campaign (Zeppelin based tropospheric chemistry experiment, Part 2, Oebel et al., 2010; Wintel et al., 2013). The ZEPTEr-2 campaign study configurations are described in Sect. 4. Results of singular vector analyses with respect to initial values and emission rates are presented in Sect. 5. Finally, the results of this work are summarized in Sect. 6.

20 **2 Singular vector analysis for chemical models: theoretical background**

25 The application of singular vector analysis to atmospheric chemical modelling allows for studying the influence of different kinds of uncertainties on the chemical forecast evolution. Within this work, we target the largest uncertainties in initial values and emissions and their evolution, which both strongly determine the chemical system's evolution. A brief outline of the theoretical background of this application is presented in the following (see also Goris and Elbern, 2013, for a comprehensive discussion).

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2.1 Initial values as target variables

A deterministic chemical forecast is processed by a model operator, \mathcal{M}_{t_1, t_F} , propagating concentrations of a multitude of chemical species, $\mathbf{c} \in \mathbf{R}^n$, (denoted in mass mixing ratios) forward in time:

$$\mathbf{c}(t_F) = \mathcal{M}_{t_1, t_F} \mathbf{c}(t_1), \quad \text{with } t_1 : \text{initial time, } t_F : \text{final time.} \quad (1)$$

For a three-dimensional transport-model, the initial state of this equation is not entirely known, but has to be estimated relying on both former model results and assimilated observations. It is therefore subject to possible error growths. The evolution of an initial uncertainty or an initial error, $\delta \mathbf{c}(t_1)$, which is sufficiently small to evolve linearly within a given limited time interval, can be modelled by the tangent linear model, \mathbf{L}_{t_1, t_F} (Kalnay, 2002):

$$\delta \mathbf{c}(t_F) = \mathbf{L}_{t_1, t_F} \delta \mathbf{c}(t_1). \quad (2)$$

Our search for the most unstable initial uncertainty, $\delta \mathbf{c}(t_1)$, can be described as the search of the phase space direction, $\delta \mathbf{c}(t_1)$, which results in maximum error growth, $g(\delta \mathbf{c}(t_1))$, at the end of the simulation:

$$\max_{\delta \mathbf{c}(t_1) \neq 0} \left(g^2(\delta \mathbf{c}(t_1)) = \frac{\|\delta \mathbf{c}(t_F)\|_2^2}{\|\delta \mathbf{c}(t_1)\|_2^2} \right) = \max_{\delta \mathbf{c}(t_1) \neq 0} \frac{\delta \mathbf{c}(t_1)^\top \mathbf{L}_{t_1, t_F}^\top \mathbf{L}_{t_1, t_F} \delta \mathbf{c}(t_1)}{\delta \mathbf{c}(t_1)^\top \delta \mathbf{c}(t_1)}, \quad (3)$$

where, for convenience, the squared error growth is maximised (Goris and Elbern, 2013). Here, $\mathbf{L}_{t_1, t_F}^\top$ denotes the adjoint model and $\mathbf{L}_{t_1, t_F}^\top \mathbf{L}_{t_1, t_F}$ the Oseledec operator. Since the Oseledec operator is symmetric, Rayleigh's principle can be applied (see, for example, Parlett, 1998). Accordingly, the problem (Eq. 3) can be solved by calculating the eigenvector $\mathbf{v}_1(t_1)$ assigned to the largest eigenvalue λ_1 of the following eigenvalue problem:

$$\mathbf{L}_{t_1, t_F}^\top \mathbf{L}_{t_1, t_F} \mathbf{v}(t_1) = \lambda \mathbf{v}(t_1). \quad (4)$$

The eigenvector, $\mathbf{v}_1(t_1)$, of the Oseledec operator equals the right singular vector, $\mathbf{v}_1(t_1)$, of the tangent-linear operator, \mathbf{L}_{t_1, t_E} . The singular value σ_1 equals the square root of the associated eigenvalue, λ_1 , and is the maximum value of the error growth, $g(\delta\mathbf{c}(t_1))$. It defines the amount of error growth at the end of integration time.

5 Weight matrix and projection operator

To allow for the calculation of relative error growths and for placing foci on limited sets of chemical compounds and limited areas, we extend the analysis above by applying two special operators, namely weight matrix, $\mathbf{W}_t \in \mathbf{R}^{n \times n}$, and projection operator, $\mathbf{P}_t \in \mathbf{R}^{n \times n}$:

$$\mathbf{W}_t := \text{diag}\left(\mathbf{c}^{i,j,k,s}(t)\right)_{i,j,k,s} \quad \text{and}$$

$$\mathbf{P}_t := \text{diag}(p_i)_{i=1,\dots,n}, \quad p_i = \begin{cases} 1 & \forall i \in \mathcal{P}(t) \\ 0 & \text{otherwise,} \end{cases} \quad (5)$$

Since the weight matrix contains concentration of chemical species (here, s denotes the considered species, while (i, j, k) denotes the considered numerical grid point), application of the inverse weight matrix yields relative perturbations and prevents the uncertainties of species with larger concentrations to dominate the error growth.

The projection operator allows for analysis of a limited set, $\mathcal{P}(t)$, of chemical species and grid points by setting the entries of the perturbations to zero when they are not within the chosen set of species and regions (Barkmeijer et al., 1998).

With the help of projection operator and weight matrix, we can consider the relative impact of a limited set of perturbations at initial time, t_1 , on a limited set of perturbation at time t :

$$\delta\mathbf{c}_{\text{pr}}(t) := \mathbf{W}_t^{-1} \mathbf{P}_t \mathbf{L}_{t_1, t} \mathbf{P}_{t_1} \delta\mathbf{c}(t_1) \quad (6)$$

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(where $\delta \mathbf{c}_{\text{pr}} \in \mathbf{R}^n$ is denoted as the projected relative error). The associated squared projected relative error growth $g_{\text{pr}}^2(\delta \mathbf{c}_{\text{pr}}(t_1))$ is given by:

$$g_{\text{pr}}^2(\delta \mathbf{c}_{\text{pr}}(t_1)) := \frac{\|\delta \mathbf{c}_{\text{pr}}(t_F)\|_2}{\|\delta \mathbf{c}_{\text{pr}}(t_1)\|_2} = \frac{\|\mathbf{W}_{t_F}^{-1} \mathbf{P}_{t_F} \mathbf{L}_{t_1, t_F} \mathbf{W}_{t_1} \delta \mathbf{c}_{\text{pr}}(t_1)\|_2}{\|\delta \mathbf{c}_{\text{pr}}(t_1)\|_2^2} \quad (7)$$

subject to

$$[\delta \mathbf{c}_{\text{pr}}(t_1)](j) = \begin{cases} \left[\frac{\delta c(t_1)}{c(t_1)} \right](j) & \forall j \in \mathcal{P}_{t_1} \\ 0 & \text{otherwise,} \end{cases} \quad (8)$$

Here, $[\mathbf{x}](j)$ denotes the j th component of a vector \mathbf{x} . The phase space direction that maximizes the Rayleigh quotient (Eq. 7) and ensures condition (Eq. 8) is the solution $\mathbf{v}_{\text{pr}1}(t_1) \in \mathbf{R}^n$ of the symmetric eigenvalue problem:

$$\mathbf{B}_{\text{pr}}^T \mathbf{B}_{\text{pr}} \mathbf{v}_{\text{pr}}(t_1) = \lambda_{\text{pr}} \mathbf{v}_{\text{pr}}(t_1), \quad \text{where } \mathbf{B}_{\text{pr}} := \mathbf{W}_{t_F}^{-1} \mathbf{P}_{t_F} \mathbf{L}_{t_1, t_F} \mathbf{W}_{t_1} \mathbf{P}_{t_1}, \quad (9)$$

assigned to the largest eigenvalue $\lambda_{\text{pr}1}$ (see Goris and Elbern, 2013, for a derivation of the eigenvalue problem). We refer to the solution as projected relative singular vector, since it is the right singular vector of the operator \mathbf{B}_{pr} . The square root of the eigenvalue $\lambda_{\text{pr}1}$ is the associated projected relative singular value $\sigma_{\text{pr}1}$.

2.2 Emissions as target variables

Emissions ($\mathbf{e}(t)$) impact the final state, $\mathbf{c}(t_F)$, according to the differential equations, which describe the chemical evolution:

$$\frac{d\mathbf{c}}{dt} = \mathbf{f}(\mathbf{c}(t)) + \mathbf{e}(t). \quad (10)$$

Like initial values, emissions are subject to uncertainties or errors, since their estimate is dependent on imperfect models and observation. Yet, emissions vary in time, leading

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to uncertainties or errors, $\delta \mathbf{e}(t)$, at each time step $t \in [t_1, t_F]$. Consequently, the associated directions of largest error growth differ for each time step and their identification results in one application of singular vector analysis per time step, $t \in [t_1, t_F]$. In order to reduce the degrees of freedom to keep ill-posedness of the optimization problem and computational expenditure under control, we define a time invariant vector of emission factors, \mathbf{e}_f , instead, representing the amplitude of a prescribed diurnal emission profile (Elbern et al., 2007). This is a reasonable constraint as the daily evolution of emissions is far better known than the total emitted amount in a grid cell. Further, the application of \mathbf{e}_f has the advantage of resulting in only one singular vector analysis per time interval, $[t_1, t_F]$. The associated results quantify for which grid cell and which chemical species further emission strength assessment is most beneficial.

Introducing the vector of emission factors, \mathbf{e}_f , Eq. (10) reformulates to

$$\frac{d\mathbf{c}}{dt} = f(\mathbf{c}(t)) + \mathbf{E}(t) \mathbf{e}_f, \quad (11)$$

where, $\mathbf{E}(t)$ is a diagonal matrix with the vector of emission $\mathbf{e}(t)$ on its diagonal. The tangent linear model integration of Eq. (10) reads

$$\delta \mathbf{c}(t_F) = \tilde{\mathbf{L}}_{t_1, t_F} \delta \mathbf{z}(t_1) = \left(\mathbf{L}_{t_1, t_F}, \mathbf{L}_{t_1, t_F}^e \right) \begin{pmatrix} \delta \mathbf{c}(t_1) \\ \delta \mathbf{e}_f \end{pmatrix}. \quad (12)$$

Since emission factors already denote a relative measure, we consider henceforth only the relative impact of their uncertainty:

$$\delta \tilde{\mathbf{c}}_r(t_F) := \mathbf{W}_{t_F}^{-1} \delta \tilde{\mathbf{c}}(t_F). \quad (13)$$

The tilde denotes that we consider a perturbation caused by uncertainties in emission only (i.e., $\delta \mathbf{c}(t_1) = 0$ for expository purposes). With these restrictions, the squared relative error growth, $\tilde{g}_r^2(\delta \mathbf{e}_f)$, reads:

$$\tilde{g}_r^2(\delta \mathbf{e}_f) := \frac{\|\delta \tilde{\mathbf{c}}_r(t_F)\|_2^2}{\|\delta \mathbf{e}_f\|_2^2} = \frac{\delta \mathbf{e}_f^T \mathbf{L}_{t_1, t_F}^{eT} \mathbf{W}_{t_F}^{-T} \mathbf{W}_{t_F}^{-1} \mathbf{L}_{t_1, t_F}^e \delta \mathbf{e}_f}{\delta \mathbf{e}_f^T \delta \mathbf{e}_f}. \quad (14)$$

According to Rayleigh's principle, the phase space direction that maximizes the ratio (Eq. 14) is the eigenvector $\tilde{\mathbf{v}}_{r1}$ of the eigenvalue problem

$$\mathbf{L}_{t_i, t_F}^e \mathbf{W}_{t_F}^{-T} \mathbf{W}_{t_F}^{-1} \mathbf{L}_{t_i, t_F}^e \tilde{\mathbf{v}}_r = \tilde{\lambda}_r \tilde{\mathbf{v}}_r, \quad (15)$$

assigned to largest eigenvalue $\tilde{\lambda}_{r1}$. As the solution equals the right singular vector of the operator $\mathbf{W}_{t_F}^{-1} \mathbf{L}_{t_i, t_F}^e$, it is denoted as relative singular vector with respect to emission uncertainties. Its associated singular value $\tilde{\sigma}_{r1}$ is the square root of $\tilde{\lambda}_{r1}$.

A focal set of initial and final perturbations can be examined with help of the projection operator, \mathbf{P}_t (defined in Eq. 5). The associated projected relative singular vector for the error growth of emission factor uncertainties can be calculated following paragraph "Weight matrix and projection operator" of Sect. 2.

3 Model design

3.1 The inverse European air pollution and dispersion model (EURAD-IM)

For the design of a model enabling 3-dimensional singular vector analysis of chemical species and their temporal evolution, we implement the theory as described in Sect. 2 in a chemistry transport model. Our chemistry model of choice is the EUROpean Air pollution and Dispersion – Inverse Model (EURAD-IM, e.g., Elbern, 1997; Elbern and Schmidt, 1999; Elbern et al., 2007). EURAD-IM is an advanced Eulerian model operating from European down to local scale by applying a nesting technique with the smallest horizontal resolution available being 1 km. The horizontal grid design is based on Lambert conformal conic projections and employs the Arakawa C grid stencil (Arakawa and Lamb, 1977). The vertical grid structure of the EURAD-IM is defined by a terrain following σ -coordinate system. Due to the general focus on tropospheric applications in this work, the upper boundary is 100 hPa. Between surface and 100 hPa 23 vertical model layers are defined.

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Newly coded tangent linear routines have been checked for consistency with corresponding forward and adjoint modules. For consistency with the forward model, the gradient check ratio (Navon et al., 1992) is applied, defined as

$$d = \frac{\text{FWD}(\mathbf{x} + \alpha\delta\mathbf{x}) - \text{FWD}(\mathbf{x})}{\text{TLM}(\alpha\delta\mathbf{x})}. \quad (17)$$

The abbreviations `FWD` and `TLM` denote parts of the forward model and their associated tangent linear routines (allowing for piecewise code-checking), α is a scalar parameter. While α approaches zero, the ratio (Eq. 17) should converge towards one, until the limits of numerical precision are reached and convergence falters. Within these limits, the new tangent linear routines demonstrate the required characteristics of Eq. (17) for considered test cases. The gradient ratio check indicates the accuracy of the tangent linear assumption. Application of the tangent linear model is only justified, if the considered perturbation is small enough to ensure $d \approx 1$.

Consistency of tangent linear and adjoint model can be tested by inspecting the validity of the following equation:

$$(\text{TLM}(\delta\mathbf{x}))^\top (\text{TLM}(\delta\mathbf{x})) = \delta\mathbf{x}^\top \text{ADJ}(\text{TLM}(\delta\mathbf{x})), \quad (18)$$

(Navon et al., 1992), where `ADJ` denotes associated parts of the adjoint model. When testing Eq. (18) for the newly implemented tangent linear routines, single routines as well as the complete model demonstrate correctness.

The central task of the EURAD-IM-SVA is the detection of singular vectors and their associated singular values. Two methods have been implemented for solving the eigenvalue problems: the power method (Mises and Pollaczek-Geiringer, 1929) and a distributed memory version of the implicitly restarted Arnoldi method (PARPACK, Maschho and Sorensen, 1996; Lehoucq et al., 1998; Sorensen, 1996). While the power method converges iteratively to the dominant eigenpair $(\lambda_1, \mathbf{v}_1)$, PARPACK has the ability to calculate the k largest eigenvalues and their associated eigenvectors by one iteration cycle. PARPACK relies on the Lanczos and the Arnoldi process, dependent on

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the properties of the considered matrix A . If A is symmetric, an algorithmic variant of the Implicitly Restarted Lanczos Method (IRLM) is used, otherwise a variant of the Implicitly Restarted Arnoldi Method (IRAM) is employed. Specifically, we apply the PARPACK routines “PSNAUPD” (features the computation of the matrix-vector product) and “PSNEUPD” (features the computation of the requested eigenvalues and eigenvectors). PARPACK has the important advantage that it only needs a matrix-vector product instead of an explicit representation of the matrix A . Since the eigenvalue problems in this work include operators, PARPACK is perfectly tailored to our needs.

4 Case study: measurement campaign ZEPTEr-2

We apply the set-up of the measurement campaign ZEPTEr-2 (Zeppelin based tropospheric chemistry experiment, Part 2, Oebel et al., 2010; Wintel et al., 2013) to test and validate the EURAD-IM-SVA.

ZEPTEr-2 deployed the airship ZEPPELIN NT as a platform to measure the distribution of different trace gases, aerosols, and short-lived radicals in the planetary boundary layer. During the campaign, 25 flights were carried out within a 100 km radius of the home base at Friedrichshafen airport (FDH), southern Germany. Vertical profiles of trace gases were measured above different surface types, including Lake Constance, and surrounding forests.

ZEPTEr-2 was supported by daily 3-D-var analyses and chemical forecasts modelled with the EURAD-IM. The ZEPTEr-2 setup of the EURAD-IM allows for a practical application of the theory of targeted observations. Here, we apply singular vector analysis to identify the most sensitive locations and chemical compounds with respect to their impact on the final concentration of ozone. This study is designed to give insight into example applications of singular vectors in future campaigns by answering the following questions:

Q_C: Which of the chemical compounds O₃, NO, NO₂, HCHO, CO, HONO, and OH has to be measured with priority to provide an improved forecast for given ozone profiles?

Q_L: Where is the optimal location for observations of these components?

(where Q_C denotes “question with regard to compounds”, and Q_L “question with regard to location”).

We choose all spatial projections to contain grid-points with ZEPTEr-2 measurements and all compound-wise projections to focus only on chemical compounds measured during the ZEPTEr-2 campaign. In this manner, it is revealed how singular vector analyses can support the set up of an optimal campaign design when the chemical compounds to be measured and an approximate measurement route are already set. At final time, we focus specifically on vertical measurement profiles, since measurement profiles grant a larger magnitude of the optimal initial perturbation than single ZEPTEr-2 measurement points (the location of the vertical measurement profile at final time is denoted as “final profile VP(t_F)” henceforth). For local projection at initial time, it is not reasonable to focus on locations of measurements solely, since thereby (a) spatial optimization is omitted and (b) the dynamics of the system are very limited, resulting in nearly negligible eigenvalues. Hence, no local projection was chosen. Yet, the approximate measurement route is kept by considering only those final profiles VP(t_F) that contain ZEPTEr-2 measurements at initial time, in the centre of their backward wind plume. Since only hourly initial times can be considered (due to the current EURAD-IM configuration), 17 simulation intervals meet the conditions described above. More details about the considered cases can be found in Table 1. Cases that share the same final profile VP(t_F) are indicated with the same case number and subsequent distinctive letters.

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EURAD-IM-SVA configuration

The configuration of the EURAD-IM-SVA applied in this study is based on the ZEPTE-2 setup of the EURAD-IM. Here, RACM-MIM (Geiger et al., 2003) has been chosen as chemistry mechanism, while meteorological fields are provided by MM5 simulations (NCAR Mesoscale Meteorological Model, Grell et al., 1994). The ZEPTE-2 grid configuration of the EURAD-IM consists of a coarse European grid with a horizontal resolution of 45 km and a time step length of 600 s, and three nested grids with horizontal resolutions of 10, 5, and 1 km and time step lengths of 240, 120, and 60 s, respectively. The finest grid (ZP3) covers the region of Lake Constance. Since all flight trajectories are located within the ZP3-grid, the ZP3-domain is sufficient for the considered case study. Due to its high horizontal resolution, the ZP3-grid provides a good representativeness of the measurements. In order to reduce the CPU time needed by singular vector calculations, the horizontal size of the ZP3-domain was reduced resulting in a ZPS-domain with $N_x = 111$, $N_y = 96$. Figure 1 illustrates the horizontal position of the ZPS-domain. It was assured, that all flight trajectories remain within the ZPS-grid. For a reference state in the centre of the ZPS-domain, Table 2 lists the vertical grid structure in terms of height above ground.

Emission estimates of the ZEPTE-2 setup are provided by the cooperative program EMEP (European Monitoring and Evaluation Programme) with a horizontal resolution of 50 km. The data consists of annual emissions of CO, SO₂, NO_x, NH₃, VOC, and particulates (PM_{2.5}, PM₁₀) provided for 11 anthropogenic source-sectors. Since the horizontal resolution of the EMEP emission data is not adequate for the considered ZPS-grid, the horizontal resolution of the emission was refined. For the refinement, land cover data sets of COordination of INformation on the Environment (CORINE) and of United States Geological Survey Global Land Cover Characterization (USGS-GLCC) were combined with data from GIS (Geographic Information Systems). In this manner of downscaling, emission data sets with a horizontal resolution of 1 km were generated, where consistency with the overlying EMEP emission data set is ensured. Emissions

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of small towns and busy roads are well resolved. An example for CO-emissions on the ZPS-grid can be found in Fig. 1.

Initial concentrations of all simulations are taken from 3-D-var assimilation runs, conducted for the ZEPTEr-2 campaign. Here, assimilation was accomplished every four hours, starting at 02:00 UTC, and observational data of NO₂, NO, SO₂O₃, CO, C₆H₆, PM_{2.5}, and PM₁₀ were assimilated.

5 Results and discussion

In this section, elementary examples are demonstrated, illustrating performance and interpretation of singular vectors for observation targeting. The section is divided between initial value based singular vectors and those determined by emission rates. For both measures, we identify both optimal locations and optimal chemical compounds for additional measurements.

5.1 Singular vectors with respect to initial uncertainties

The conducted singular vector calculations are based on the tangent linear model assuming that small perturbations evolve linearly within the simulation time. In order to grant meaningful results, this assumption has to be validated first. We apply Eq. (17) for validation and insert the chemical initial conditions of each simulation as x and the resulting singular vectors as perturbation, δx . Results demonstrate that $|1.0 - d| \leq 0.001$ is achieved by reducing α to 0.1 (which equals a relative initial disturbance of 10%) for each of the simulations. Hence, ratios are close enough to one, to ensure that the tangent linear approximation is sufficiently accurate.

5.1.1 Optimal placement of observations

An evident point of interest for chemistry is the relation between singular vectors resulting from passive tracer advection-diffusion, as merely controlled by meteorological

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parameters, and those which are also affected by reactive chemistry. Their differences can be visualised via horizontal and vertical placement (for a definition of horizontal and vertical placement see Appendix A1). In case of the latter, the left panel of Fig. 2 displays the vertical profile of the optimal horizontal placement, broken down for the lower 15 model levels, for a passive tracer “ozone” and reactive ozone for case 2a. It can be seen that up to a height limit of approximately 450 m (level 8), initial values of both passive and reactive chemistry demonstrate a similar influence per height level. The faster levelling of the reactive chemistry profile above level 8 indicates that initial values of higher levels are first transported into lower air masses before chemical production processes take place. The same pattern is seen for all considered cases and all considered chemical compounds (right panel, Fig. 2) with varying lower height limits for the faster levelling of reactive chemistry. These results can be expected as ozone production is initiated by chemical production processes at lower elevation or, in the case of ozone itself, ozone decomposition at lower elevation. Concerning differences in the levelling of different chemical compounds, we find that the relevance of measurements of O_3 and CO decreases slower than the relevance of measurements of NO and HCHO, independent of initial time t_1 or simulation length (see Fig. 2). It can be assumed that this feature is linked to differing vertical profiles.

Examination of the horizontal placement (for a definition of horizontal placement see Appendix A1) of all cases confirms, that the placement of passive tracer and ozone generally diverge more in higher model levels (as seen in Fig. 3 for case 8a). Since the horizontal placement disregards effects of the vertical placement distribution and of different species magnitudes, a broader 0.01 isopleth in higher model levels (as seen in Fig. 3) means that neighbouring grid cells show only small differences in placement importance. In comparison to passive tracer ozone, reactive ozone reveals smaller isopleths at lower elevation and broader isopleths in higher model levels. The latter indicates varying chemical concentrations in lower air masses driven by locations of production sources and photochemical lifetimes. Even though ozone itself is not emitted into the atmosphere, its precursors are strongly influenced by emissions, leading

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to a highly variable distribution of ozone in lower levels of the troposphere, while it is relatively uniform in higher model levels.

Results reveal furthermore that the horizontal placement of all considered chemical compounds usually coincides. Remarkable differences within the chemical placement are only discovered for cases 6, 7a, 8b, and 10 and can be explained by varying initial concentrations within the otherwise advection controlled placement area. The horizontal distribution at the lowest level for case 6 is displayed in Fig. 4 for ozone (left panel) and NO (right panel). The westward orientation of the influence area displays the up-wind domain of the Friedrichshafen target location, and shows a fairly evenly distributed domain for possible ozone measurements. It can be assumed that this area is mostly controlled by transport and diffusion processes. In contrast, Fig. 4b indicates the areas of sensitivity for NO, covering 3 disconnected sub-domains enclosed by the ozone sensitivity area. These patches are associated with NO emission areas, and indicate the sensitivity of the ozone evolution to direct interaction with NO in the nearby area of Friedrichshafen, and also to indirect interaction (via NO_2) for the longer distance area at the westerly map border.

The analysed ZEPTEr-2 cases share a relative short simulation interval (the longest simulation interval lasts 3 h 15 min) and a local projection on the final profile $\text{VP}(t_F)$. Both features restrict the dynamics of the system. It can be expected that the chemical placements are likely to differ more when choosing longer simulation intervals (as it is the case in simulations done by Liao et al., 2006).

5.1.2 Measurement priority of chemical compounds

Optimal compounds for additional measurements can be determined via the relative ranking defined in Appendix A2. Here, we consider the influence of compounds O_3 , NO, NO_2 , HCHO, CO, HONO, and OH on the ozone evolution.

Figure 5 provides an example of the relative ranking of O_3 and CO for model level 1 (ground level). Note that if a case is not depicted for a particular level, then the

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number of grid points (i, j, k) that hold $\sqrt{\sum_s v(i, j, k, s)^2} > 10^{-4}$ equals zero. Results of all cases reveal that O_3 is ranked first for more than 95 % of the considered grid points for all cases. None of the other species reveals such a distinct behaviour. Yet, it is possible to come to the following conclusions: (1) O_3 has most relevance among the considered chemical compounds, (2) NO, NO_2 , HCHO, and CO show medium relevance, and (3) OH and HONO have least relevance. In most cases, the relevance of OH is ranked 7th, while HONO is ranked 6th. In lower air masses, NO and NO_2 tend to be ranked 2nd or 3rd, while HCHO tends to be ranked 3rd or 4th and CO 4th or 5th. The revealed measurement priority meets our expectations as NO_x , CO, and Volatile Organic Compounds are important precursors of ozone (Seinfeld and Pandis, 1998). Here, the considered cases are in general NO_x sensitive (see also Goris and Elbern, 2013).

We also find that the measurement priority of NO is higher for simulations starting during noon hours, while it is lower for simulations starting in the morning or in afternoon/evening time frames. This feature is related to the initial mixing ratio of NO which is close to zero during night-time (Seinfeld and Pandis, 1998).

5.2 Singular vectors with respect to emission uncertainties

Prior to analysing the singular vectors with respect to emission factors, the linearity assumption is tested by inserting the calculated perturbations of largest error growth in Eq. (17). Reducing α to 0.1 (which equals an emission factor disturbance of 10 %) ensures $|1.0 - d| \leq 0.01$ for each considered case. Note, that in most cases even $|1.0 - d| \leq 0.001$ is achieved. Therefore, the tangent linear approximation is considered to be sufficiently accurate.

The optimisation of observational networks with respect to measurements of emissions itself is somewhat artificial, as only for very special cases flux tower observations of CO_2 and, even more sparsely, other greenhouse gases, are available. Nevertheless, formally it can be applied in very much the same way as for initial values and, for reac-

tive emission sources under conditions with sufficiently large Damköhler numbers and small background concentrations, traditional observations in emitting areas can serve as Supplement.

In case of the ZEPTER-2 configuration, the surface level is the only level that incorporates emissions. Furthermore, O₃, HONO, and OH are not emitted and are therefore not considered for analysis.

5.2.1 Optimal placement of observations

Figure 6 exhibits an example for formaldehyde (HCHO), which is both emitted into and produced in the atmosphere. Correspondingly, a spatial comparison between singular vectors of initial values and emission rate optimisation will reveal spatial differences. It can be seen from the map that, influenced by the spatial distribution of the emission fields, the area for optimal observations of emissions is close to the final profile, while the area of optimal observations of initial values is in a larger distance. This outcome is valid for all cases and can be explained by the fact that the target area for emissions is the result of an optimisation over the entire simulation interval. The target area of initial values can only be located within the area of the backward plume at its initial time, yet the target area of emissions can be any point within the entire advection trace area of the backward plume. Hence, the optimal placement of observations of emissions is strongly influenced by locations of emission sources within this plume (Fig. 6). The importance of emission sources is confirmed by the smaller extent of the target area of emissions, in comparison to initial values. Since the horizontal singular vector sections have unit length for a fixed compound and a fixed model level, a small extent of the target area shows that the additional value of observations is relatively high at few grid points and decreases sharply for the surrounding grid points.

Comparing the target area of emissions for different compounds, we find that the target areas differ quite substantially in some cases. This feature occurs due to different emission source strengths for different compounds and will be explained in more detail at the end of the next section.

5.2.2 Relevance ranking of chemical compounds

In response to question Q_C , a relevance ranking of the emission influences of NO, NO₂, HCHO, and CO is assessed in this section (see Appendix A2). Note, that species O₃, OH, and HONO are not emitted and therefore not to be taken into account.

Results for all considered levels and species are depicted in Fig. 7. It is found that (1) the influence of NO emissions is most important, and (2) emissions of NO₂ tend to have the second most influence, while (3) in the majority of cases, the importance of emissions of CO and HCHO alternates between third and fourth rank. This result is to be expected, as NO_x, CO, and Volatile Organic Compounds are the most important precursors of the ozone production. Dependent on the existing mixing ratio, the ozone production is NO_x or VOC sensitive (Seinfeld and Pandis, 1998; Goris and Elbern, 2013). Here, the considered cases are all NO_x sensitive.

Figure 8 serves to give an idea about the location dependence of the ranking of emission influences of HCHO and CO for case 2a. Based on the analyses of all 17 cases, the following conclusions can be drawn: (1) The importance of emissions of HCHO tends to increase in urban plumes at the expense of the influence of emissions of CO and NO, and (2) the influence of emissions of CO tends to increase at busy roads. As compensation, the influence of emissions of HCHO and NO decreases. These findings are consistent with the modelled strength of different emission sources per compound.

5.3 Magnitudes of singular values

The singular values of our calculations determine the relative error growths of uncertainties in initial values and emissions, respectively. Table 3 captures the singular values for the ZEPTEr-2 calculations for both target variables (initial values and emissions) for simulations with a shared final profile $VP(t_F)$.

We find that the influence of singular values with respect to initial values decreases with growing simulation length, whereas the influence of singular values with respect to emissions increases (Table 3). This behaviour is expected since continuous emissions

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and their uncertainties affect the chemical evolution at every time step. Therefore, the emission sensitivity increases with each added time-step. Uncertainties in initial values, on the other hand, influence the forecast mostly at initial time, with declining importance with time.

Furthermore, Table 3 reveals that, for most of the calculated cases, the magnitude of the singular values is smaller than 1, meaning that the final perturbation is smaller in magnitude than the perturbation of initial values or emission rates. Considering that we apply singular vector analyses to find the initial and emission uncertainties that cause the largest error growth, a small error-growth seemingly suggests that the benefit of singular vector analysis is small. However, it should be considered, that we analyse only very restricted cases. Due to the focus on vertical profiles, the final projections cover only 5 to 10 grid points and it can be expected that the magnitude of the final ozone perturbation is smaller in amount than the magnitude of the locally not focused initial value perturbation. For emission rates, the dynamics of the system is mainly limited by two features. Firstly, the final species projection is on ozone, but ozone itself is not emitted. Secondly, the final local projection is on a vertical profile, whose vertical extensions range between model level 1 and model level 10. Since the emissions influence neither the entire vertical profile nor the concentration of ozone directly, some integration time is needed before the effect of emissions on the final perturbation becomes apparent. Despite those restrictions, case 8a and case 8b (and case 5b for initial value optimisation) show singular values greater than 1, proving the value of singular vector analysis even in the case of strongly restricted dynamics.

6 Summary and conclusions

EURAD-IM has been augmented to allow for singular vector decomposition (SVA), resulting in the new EURAD-IM-SVA model. Purpose of the EURAD-IM-SVA is the calculation of the most sensitive chemical configuration with respect to initial values and emissions. The calculated sensitive configurations can be utilized to stabilize the

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chemical forecast by targeting sensitive system states for additional measurements. In this manner, the new tool can be especially applied for effective campaign-planning.

In the framework of the model augmentation, newly coded or embedded routines are tested for accuracy. Within the limits of numerical precision, single routines as well as the complete model demonstrate correctness. Subsequently, the EURAD-IM-SVA is evaluated by conducting a set of case studies based on the accomplished ZEPTE-2 campaign. Here, we evaluate the importance of measurements with regards to their ability of improving the forecast for locally predetermined ozone profiles. We investigate the influence of additional measurements of O_3 , NO, NO_2 , HCHO, CO, HONO, and OH. Since the considered simulation cases consider only the chemistry of ozone production and advection-diffusion dynamics in selected areas, they allow for a retracing of the results and a confirmation of their correctness. Elementary examples are presented, illustrating performance and interpretation of singular vectors for observation targeting.

Results of the singular vector decomposition with respect to initial values reveal that the optimal placement for additional observations is linked to height, with observations being more important at lower elevation where most of the chemical production of ozone takes place. Here, optimal target areas are controlled by mixing ratios of ozone precursors and their photochemical lifetimes, as well as transport and diffusion processes. In terms of a relevance ranking of chemical species, the measurement priority of species is differing location-wise, dependent on initial concentrations and the importance of the precursor in the chemical formation of ozone. Overall, O_3 has most relevance among the considered species, while NO, NO_2 , CO, and HCHO show medium relevance, and OH and HONO have least relevance. The revealed measurement priority meets our expectations as NO_x , CO, and Volatile Organic Compounds are important precursors of ozone (Seinfeld and Pandis, 1998).

The singular vector decomposition with respect to emissions shows that optimal placement of measurements of emission factors is strongly dependent on the location of emission sources. When considering the relevance ranking of considered emitted species, we find that, for most cases, the influence of emissions of NO is most impor-

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tant, followed by emissions of NO_2 , which of course, are chemically closely linked. In these cases, a choice between both compounds for measurement network design may follow practical considerations. The importance of emissions of CO and HCHO, in the majority of cases, alternates between third and fourth rank.

5 Considering the error growth of uncertainties in initial values and emission strength, we find that the influence of singular values with respect to initial values decreases with growing simulation length, whereas the influence of singular values with respect to emissions increases. Due to short simulation intervals and focus on selected ozone profiles at the end of the simulation, the error growth is smaller than 1 in most of
10 the cases, meaning that the final uncertainty is smaller in percentage than the initial uncertainty. Yet, there are also cases that show singular values greater than 1 proving the value of singular vector analysis even in the case of strongly restricted dynamics.

Altogether, the case study shows that the newly designed EURAD-IM-SVA is a powerful tool, which identifies critical chemical species and chemical locations with respect to initial values and emissions. Both optimal placement of measurements and
15 relevance ranking of chemical compounds confirm the benefit of singular vectors for measurement selection guidance. This can be applied for effective campaign-planning. Further, the detected directions of largest error growth can be employed to initialize ensemble forecasts and to model covariances.

20 Appendix: Usage of singular vectors for determining targeted observations

For 3-dimensional chemical transport models, a singular vector \mathbf{v} comprises vector entries $v(i, j, k, s)$ for each chemical species s and each grid point (i, j, k) (i and j indicate horizontal grid coordinates, while k denotes the considered vertical model level), referring to each species' local sensitivity to perturbations of initial values or
25 emissions. This set of vector entries can be analysed in terms of (a) optimal placement of observations and (b) measurement priority of considered species.

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A1 Horizontal and vertical placement

The optimal observation location for a given species s is determined by the magnitudes of the singular vector entries $v(i, j, k, s)$ with i, j, k variable and s fixed. Accordingly, the grid point with largest magnitude defines the optimal placement for a considered species s .

We analyse the optimal placement in terms of vertical and horizontal optimal placement. The horizontal placement disregards effects of the vertical distribution and of different species' magnitudes, answering the question of optimal placement in a given horizontal plane:

$$v_h(i, j, k, s) = \frac{v(i, j, k, s)}{|v(k, s)|}, \quad \text{with} \quad |v(k, s)| := \sqrt{\sum_{i=1}^{i_{\max}} \sum_{j=1}^{j_{\max}} v(i, j, k, s)^2}. \quad (\text{A1})$$

Here, each horizontal section of the singular vector \mathbf{v} with fixed level k and fixed species s is scaled by its length $|v(k, s)|$. In this manner, the combined singular vector entries of each horizontal plane of a given species have unit-length and allow for a horizontal placement comparison between species. The modified singular vector \mathbf{v}_h with entries $v_h(i, j, k, s)$ is referred to as horizontal singular vector.

Likewise, for the vertical placement, we want to yield placement priorities with respect to vertical levels. Since $|v(k, s)|$ determines the length of the optimal perturbation of model level k and species s , it reveals the height dependent relevance of each species. In order to disregard effects of species' magnitudes, the length $|v(k, s)|$ is scaled by the length of all perturbations associated with species s :

$$v_v(k, s) = \frac{|v(k, s)|}{|v(s)|}, \quad \text{with} \quad |v(s)| := \sqrt{\sum_{i=1}^{i_{\max}} \sum_{j=1}^{j_{\max}} \sum_{k=1}^{k_{\max}} v(i, j, k, s)^2}. \quad (\text{A2})$$

The vector \mathbf{v}_v with entries $v_v(k, s)$ is defined as vertical singular vector. In terms of optimal placement, both vertical and horizontal singular vectors allow for direct comparison of local sensitivities of different species.

A2 Relative rankings of chemical compounds

A relevance ranking (or measurement priority) of the associated chemical compounds can be established for each grid point (i, j, k) by arranging the associated singular vector entries $v(i, j, k, s)$ according to magnitude.

Since the relevance ranking of species s may differ for each considered grid point (i, j, k) , we are interested in gaining a more comprehensive picture. Accordingly, we select an area that is large enough to contain different air masses (here: all grid points with $\sqrt{\sum_s v(i, j, k, s)^2} > 10^{-4}$). Within the considered area, we establish a relative ranking $rk(k, s)$ for each species s and each model level k . Each relative ranking $rk(k, s)$ comprises the relative ranks $rk^m(k, s)$, $m = 1, \dots, n$ (where n is the number of considered species). The relative rank $rk^m(k, s)$ simply counts how often species s is ranked m th within the considered area of level k and then divides this number by the number of considered grid points:

$$rk^m(k, s) := \frac{\sum_i \sum_j \rho(i, j) \cdot r(i, j)}{\sum_i \sum_j \rho(i, j)}, \quad \rho(i, j) := \begin{cases} 1, & \text{if } \sqrt{\sum_s v(i, j, k, s)^2} > 10^{-4} \\ 0, & \text{elsewhere,} \end{cases} \quad (\text{A3})$$
$$r(i, j) := \begin{cases} 1, & \text{if } s \text{ is ranked } m\text{th in } (i, j, k) \\ 0, & \text{elsewhere.} \end{cases}$$

In this manner a general relevance ranking is provided for the selected area.

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Code availability

The code controlling the Singular Value Decomposition is stored locally at the Rhenish Institute for Environmental Research as well as at the Jülich Supercomputer Centre (JSC) of Research Centre Jülich. It is available by request via email (n

Acknowledgements. The authors are especially grateful to Dirk Poppe for numerous fruitful discussions. This study was supported by the virtual institute for Inverse Modelling of the Atmospheric Chemical COmposition (IMACCO) in the framework of the Helmholtz-Impuls- und Vernetzungsfonds (grant VH-VI-117) and by the German Federal Ministry of Education and Research through the ZEPTEP-2 project (grant 01LP0803A). All simulations utilized the Kinetic PreProcessor (KPP) developed by Valeriu Damian, Adrian Sandu, Mirela Damian, Florian A. Potra, and Gregory R. Carmichael. Many thanks to Adrian Sandu for his technical assistance. Technical and computational support was provided by the Jülich Supercomputer Centre (JSC) of Research Centre Jülich. A large and central part of the case studies has been computed on the JSC supercomputer JUROPA. Access given to this computational resources is highly appreciated. This work would not have been possible without the meteorological analysis for the initial values of MM5 obtained from the European Centre for Medium-Range Weather Forecasts (ECMWF) and the emission estimates provided by the cooperative program EMEP (European Monitoring and Evaluation Programme).

The article processing charges for this open-access publication were covered by a Research Centre of the Helmholtz Association.

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Table 1. List of all singular vector simulations included in the ZEPTEr-2 case study. Initial time (t_I) and final time (t_F) of simulation are given in UTC, the length of the simulation (time) is given in hours and minutes. $VP(t_F)$ denotes the location of the vertical measurement profile at final time, FDH designates Friedrichshafen airport, LC Lake Constance, FoA Forest of Altdorf, and Mengen denotes the city of Mengen.

| Case | Flight | Date | t_I | t_F | time | $VP(t_F)$ |
|------|--------|--------|-------|-------|------|-----------|
| 1a | 02 | 18 Oct | 12:00 | 13:30 | 1:30 | LC |
| 1b | 02 | 18 Oct | 13:00 | 13:30 | 0:30 | LC |
| 2a | 02 | 18 Oct | 11:00 | 14:00 | 3:00 | FDH |
| 2b | 02 | 18 Oct | 12:00 | 14:00 | 2:00 | FDH |
| 3 | 03 | 18 Oct | 15:00 | 17:35 | 2:35 | FDH |
| 4a | 04 | 19 Oct | 09:00 | 12:15 | 3:15 | FoA |
| 4b | 04 | 19 Oct | 10:00 | 12:15 | 2:15 | FoA |
| 5a | 05 | 19 Oct | 14:00 | 15:20 | 1:20 | FoA |
| 5b | 05 | 19 Oct | 15:00 | 15:20 | 0:20 | FoA |
| 6 | 06 | 20 Oct | 08:00 | 10:45 | 2:45 | FDH |
| 7a | 07 | 20 Oct | 13:00 | 14:45 | 1:45 | LC |
| 7b | 07 | 20 Oct | 14:00 | 14:45 | 0:45 | LC |
| 8a | 08 | 24 Oct | 16:00 | 18:00 | 2:00 | FDH |
| 8b | 08 | 24 Oct | 17:00 | 18:00 | 1:00 | FDH |
| 9a | 21 | 7 Nov | 10:00 | 11:25 | 1:25 | Mengen |
| 9b | 21 | 7 Nov | 11:00 | 11:25 | 0:25 | Mengen |
| 10 | 23 | 7 Nov | 18:00 | 20:50 | 2:50 | FDH |

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Table 2. Vertical grid structure of the EURAD-IM-SVA for the reference state 47.85° N, 9.50° E. Given are model level (ML) and height above ground (HT) in meter (m). The superscripts ⁺ and ⁻ indicate upper and lower boundary of the associated layer.

| ML | HT ⁻ (m) | HT ⁺ (m) |
|----|---------------------|---------------------|
| 23 | 10 937.5000 | 14 009.1934 |
| 22 | 8766.0986 | 10 937.5000 |
| 21 | 7060.0742 | 8766.0986 |
| 20 | 5643.5728 | 7060.0742 |
| 19 | 4426.4463 | 5643.5728 |
| 18 | 3355.8394 | 4426.4463 |
| 17 | 2397.9038 | 3355.8394 |
| 16 | 2040.8547 | 2397.9038 |
| 15 | 1696.9287 | 2040.8547 |
| 14 | 1446.9795 | 1696.9287 |
| 13 | 1203.4612 | 1446.9795 |
| 12 | 1005.1839 | 1203.4612 |
| 11 | 810.9417 | 1005.1839 |
| 10 | 658.3343 | 810.9417 |
| 9 | 508.1113 | 658.3343 |
| 8 | 396.9637 | 508.1113 |
| 7 | 287.0776 | 396.9637 |
| 6 | 214.5087 | 287.0776 |
| 5 | 142.4796 | 214.5087 |
| 4 | 106.6640 | 142.4796 |
| 3 | 70.9805 | 106.6640 |
| 2 | 35.4280 | 70.9805 |
| 1 | 0.0042 | 35.4280 |

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Table 3. Singular values (SV) with respect to initial values (iv) and emissions (em). $VP(t_F)$ denotes the considered final profile (numbers according to Table 1) and ML the associated model levels. Only simulations with a shared final profile $VP(t_F)$ are listed, “a” marks the simulation with the shorter simulation interval and “b” the simulation with the longer simulation interval. $t(a)$ and $t(b)$ are the associated simulation lengths.

| $VP(t_F)$ | ML | $t(a)$ | $t(b)$ | $SV_{iv}(a)$ | $SV_{iv}(b)$ | $SV_{em}(a)$ | $SV_{em}(b)$ |
|-----------|------|--------|--------|--------------|--------------|--------------|--------------|
| 1 | 3–10 | 0:30 | 1:30 | 0.622 | 0.338 | 0.010 | 0.027 |
| 2 | 1–5 | 2:00 | 3:00 | 0.329 | 0.239 | 0.093 | 0.096 |
| 4 | 3–9 | 2:15 | 3:15 | 0.351 | 0.277 | 0.055 | 0.072 |
| 5 | 2–9 | 0:20 | 1:20 | 1.006 | 0.524 | 0.059 | 0.112 |
| 7 | 3–10 | 0:45 | 1:45 | 0.613 | 0.422 | 0.034 | 0.046 |
| 8 | 1–7 | 1:00 | 2:00 | 1.614 | 1.517 | 1.325 | 2.760 |
| 9 | 1–9 | 0:25 | 1:25 | 0.807 | 0.689 | 0.035 | 0.038 |

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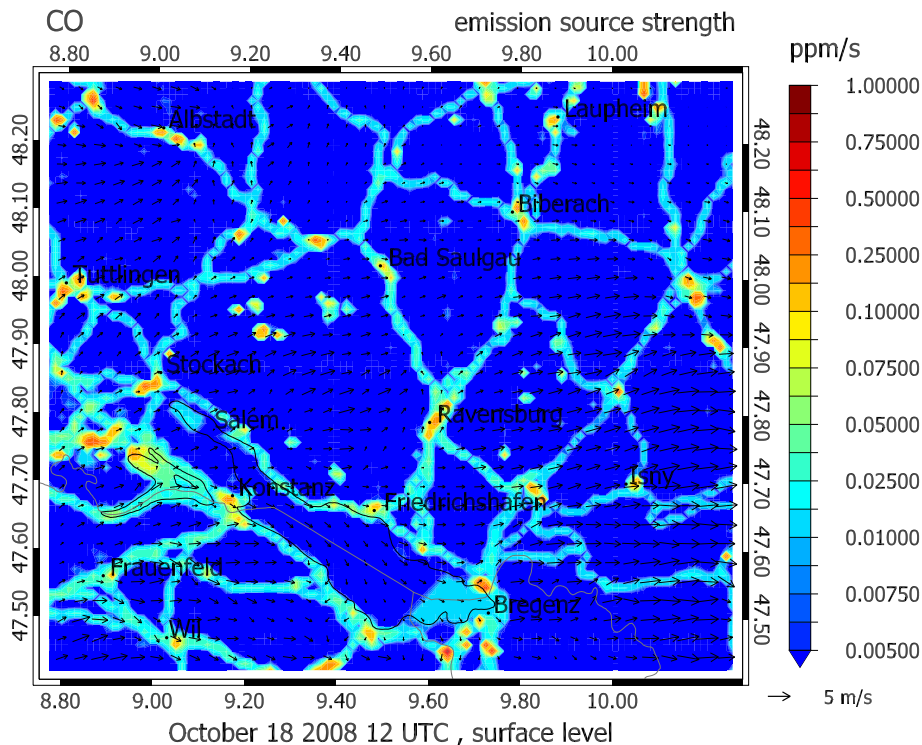


Figure 1. CO emission source strength (ppm s^{-1}) at surface level of the ZPS-grid for the 18 October 2008, 12:00 UTC. Black arrows indicate direction and strength of surface winds.

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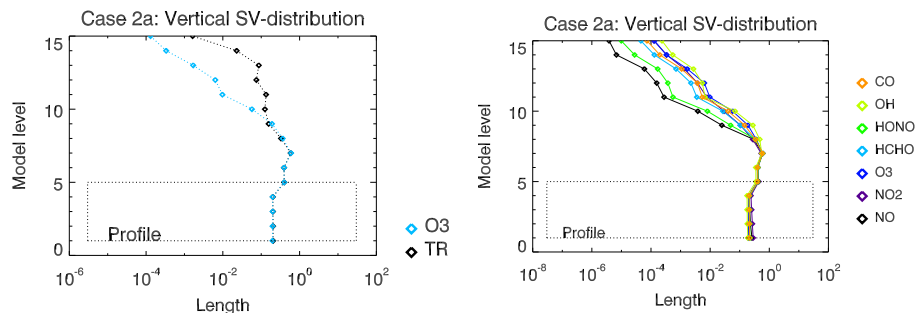


Figure 2. Optimal vertical placement for case 2a. Illustrated is the length of the vertical singular vector per model level for passive tracer and ozone (left panel) as well as CO, OH, HONO, O₃, NO₂, and NO (right panel). Color coding of each compound is denoted to the right of each panel. The black box indicates the height of the final profile $VP(t_F)$.

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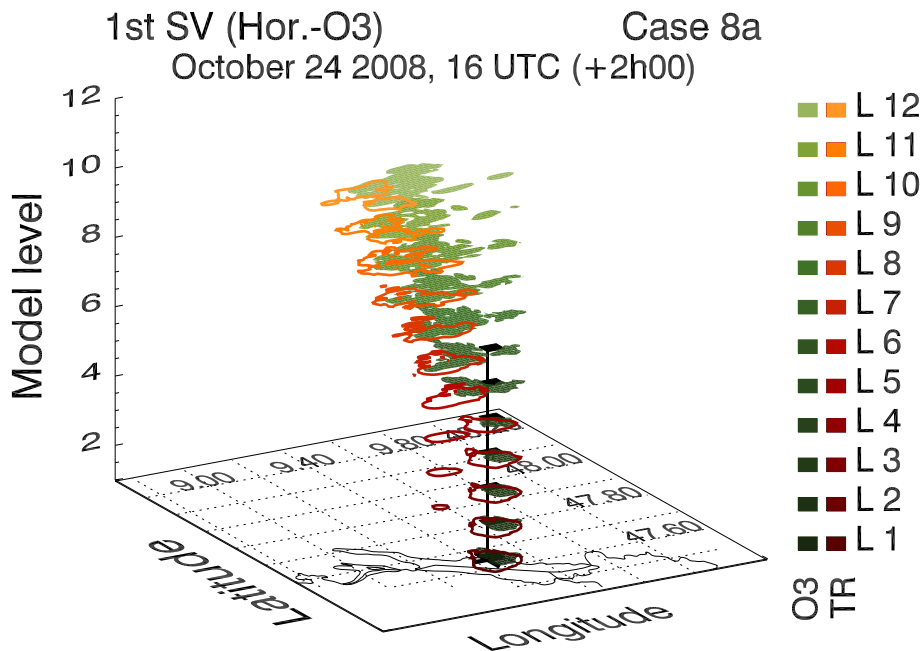


Figure 3. Optimal horizontal placement for case 8a. Shown are 0.01-isopleths of the horizontal singular vector for passive tracer (red framed shading) and ozone (green filled shading). The final profile $VP(t_F)$ is marked with a black line, the black cross indicates its horizontal position. Case numbers and simulation intervals are given on top of each panel.

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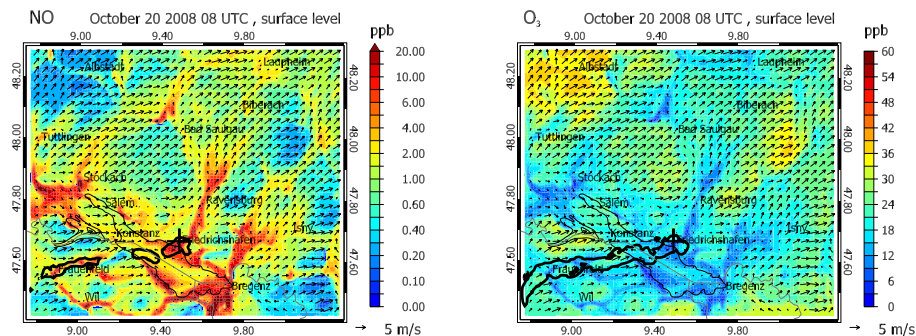


Figure 4. Initial concentrations and optimal horizontal placement of NO (left panel) and O₃ (right panel) at surface level for case 6. The 0.01-isopleths of the optimal horizontal placement are indicated with black lines, and the horizontal position of the final profile VP(t_F) is marked with a black cross. Date and time are denoted above each panel.

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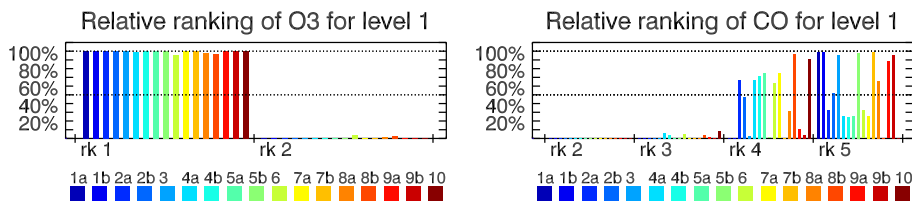


Figure 5. Relative ranking of the impact of initial uncertainties of O₃ (left panel column) and CO (right panel column) for model level 1 for all 17 case studies. Relative ranks are denoted below each bar plot. A rank m is only depicted, if the associated chemical compound is ranked m th for at least one considered grid point. The color coding of each case is denoted below each panel.

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1st SV (HCHO) CASE 5a
 October 19 2008 14 UTC +1h20

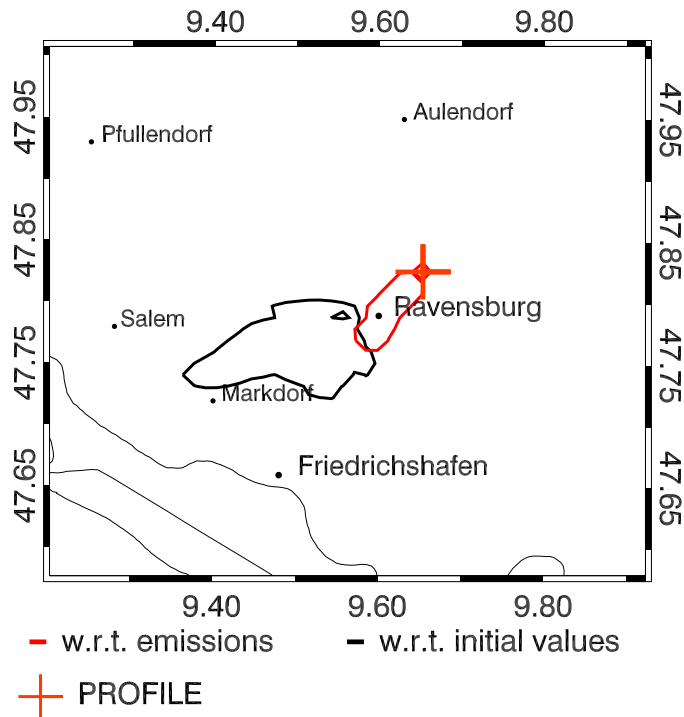


Figure 6. Optimal horizontal placement of emissions and initial values for HCHO at surface level for case 5a. 0.01-isopleths of the optimal horizontal placement are indicated with a black line (initial values) and a red line (emissions). The horizontal position of the final profile $VP(t_F)$ is indicated with a red cross.

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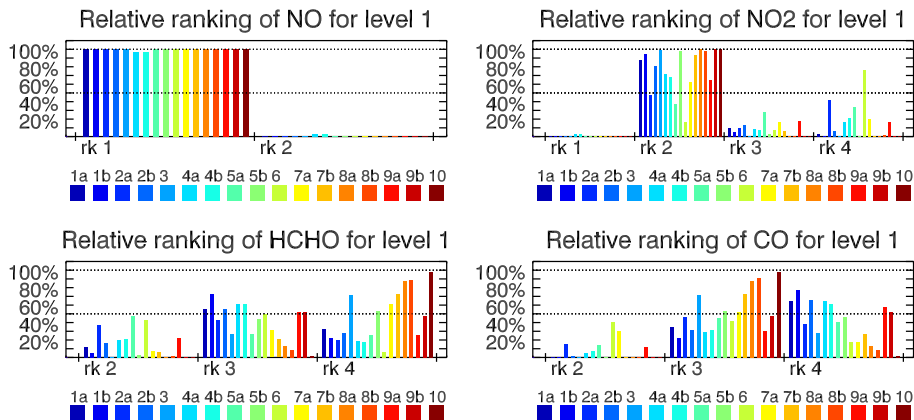


Figure 7. Relative ranking of the impact of emission uncertainties of NO (top left), NO₂ (top right), HCHO (bottom left), and CO (bottom right) for model level 1 (surface) for all 17 case studies. Plotting conventions as in Fig. 5.

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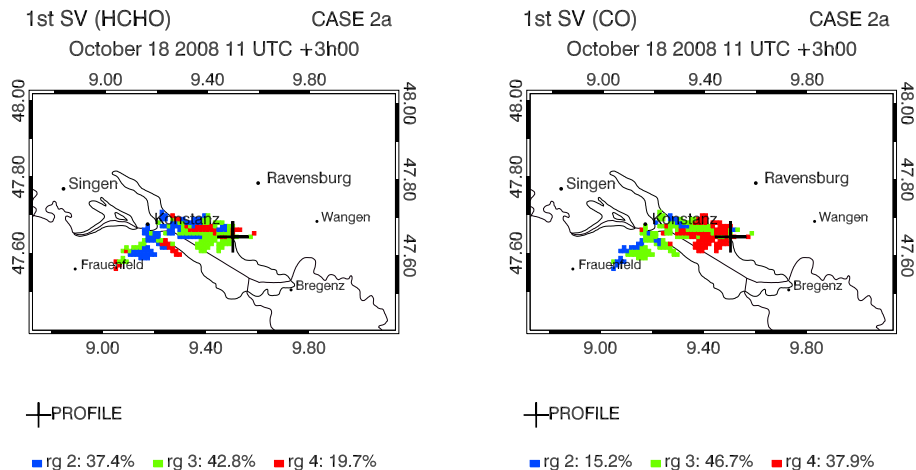


Figure 8. Spatially dependent relevance rankings of emission uncertainties of HCHO (left) and CO (right) at surface level for case 2a. The color coding each ranks is denoted below each panel. The horizontal position of the final profile $VP(t_F)$ is indicated with a black cross.

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