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A generic approach to explicit simulation of uncertainty in the NEMO ocean model

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Received: 12 December 2014 – Accepted: 5 January 2015 – Published: 27 January 2015

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Published by Copernicus Publications on behalf of the European Geosciences Union.

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Abstract

In this paper, a simple and generic implementation approach is presented, with the aim of transforming a deterministic ocean model (like NEMO) into a probabilistic model. With this approach, several kinds of stochastic parameterizations are implemented to simulate the non-deterministic effect of unresolved processes, unresolved scales, unresolved diversity. The method is illustrated with three applications, showing that uncertainties can produce a major effect in the circulation model, in the ecosystem model, and in the sea ice model. These examples show that uncertainties can produce an important effect in the simulations, strongly modifying the dynamical behaviour of these three components of ocean systems.

1 Introduction

The first requirement of an ocean model is the definition of the system that the model is going to represent. As illustrated in Fig. 1, this usually amounts to defining an appropriate separation between the system (\mathcal{A}) and the environment (\mathcal{B}). For instance, in this study, we always use a stand-alone ocean model, which means that the atmosphere is not included in the system (\mathcal{A}), but in the environment (\mathcal{B}). A key property of any ocean model is also the separation between resolved scales (in \mathcal{A}) and unresolved scales (in \mathcal{B}), defining the spectral window that the model is going to represent. In a similar way, marine ecosystems are too complex to be entirely included in \mathcal{A} . They can only be represented by a limited number of variables C_i , $i = 1, \dots, n$, providing a synthetic picture of the ecosystem, while the remaining biogeochemical diversity is included in \mathcal{B} .

Even if the union of the two systems \mathcal{A} and \mathcal{B} could be assumed deterministic, this is in general not true for system \mathcal{A} alone. The future evolution of \mathcal{A} does not only depend on its own dynamics and initial condition, but also on the interactions between \mathcal{A} and \mathcal{B} . This means that the only two ways of obtaining a deterministic model for \mathcal{A} are either to assume that the evolution of \mathcal{B} is known (as usually done for the atmosphere in

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stand-alone ocean models) or to assume that the effect of β can be parameterized as a function of what happens in \mathcal{A} (as usually done for unresolved scales and unresolved diversity). It is however important to recognize that this is always an approximation and that β is often an important source of uncertainty in the predictions made for \mathcal{A} .

To obtain a reliable predictive model for \mathcal{A} (in the sense given in Brier, 1950; Toth et al., 2003), a consistent description of this uncertainty should be embedded in the model itself. This transforms the deterministic model into a probabilistic model, which fully characterizes the quantity of information that the model contains about \mathcal{A} . Two important advantages of this probabilistic approach are (i) to allow objective statistical comparison between model and observations (by providing sufficient conditions to invalidate the model, see for instance Candille et al., 2005), and (ii) to provide a weak model constraint to data assimilation problems (by including a coherent description of model uncertainty). The objective of the modeller also changes: instead of designing a deterministic model as close as possible to observations, a probabilistic model that is both reliable (not yet invalidated by observations) and as informative as possible about \mathcal{A} must be designed.

In practice, for a complex system, it is usually impossible to compute explicitly the probability distribution describing the forecast. In general, only a limited size sample of the distribution can be obtained through an ensemble of model simulations, as routinely done in any ensemble data assimilation system (see Evensen, 1994). Ensemble simulations are produced by randomly sampling the various kinds of uncertainty (in the dynamical laws, in the forcing, in the parameters, in the initial conditions, ...) in their respective probability distribution (Monte Carlo simulations). To allow objective comparison with observations or to correctly deal with model uncertainties in data assimilation problems, non-deterministic models are thus needed in many ocean applications. The most direct approach to introduce an appropriate level of randomness in ocean models is to use stochastic processes mimicking the effect that unresolved processes (in β) produce on the system (\mathcal{A}).

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Stochastic parameterizations, explicitly simulating model uncertainty were first applied to ensemble weather forecasting by Buizza and coauthors Buizza et al. (1999) about 15 years ago. Since then, stochastic parameterizations have emerged as a quickly developing area of research in meteorology Palmer et al. (2005). In oceanography, however, most state of the art dynamical models are still deterministic. Up to now, the development of stochastic dynamical equations has been mainly focusing on stochastic parameterization of Reynolds stresses in idealized ocean modelling systems (see Frederiksen et al., 2012a; Kitsios et al., 2013 for a review). Only a few exploratory studies have attempted to explicitly simulate uncertainties in realistic dynamical ocean models: this has been done for the ocean circulation Brankart (2013), for the ocean ecosystem Arhonditsis et al. (2008), and for the sea ice dynamics Juricke et al. (2013). These preliminary studies nonetheless already show that uncertainties can play a major role in dominant dynamical behaviours of marine systems.

In line with these studies, the objective of this paper is to propose a generic implementation of these stochastic parameterizations, and to investigate several applications in which the randomness of the ocean system may be an important issue. This is synthetically implemented in the ocean model (see Sect. 2) by adding one additional module providing appropriate random processes to any non-deterministic component of the system (circulation, ecosystem, sea ice). The method is designed to be simple enough to allow a quick check of the effect of uncertainties in the system, and flexible enough to apply to various sources of uncertainty (atmosphere, unresolved scales, unresolved diversity, ...). Three applications are then illustrated in Sect. 3 showing that the explicit simulation of uncertainty can be important in a wide variety of ocean systems, by stimulating important non-deterministic dynamical behaviours. The first application (circulation model) is the same application as in Brankart (2013), but this previous paper only presented the average effect of the stochastic parameterization, whereas the focus is here on the randomness that is produced in the large scale ocean circulation. The second application (ecosystem model) is a first attempt to apply stochastic parameterizations and to explicitly simulate randomness in a basin-scale ocean ecosystem

model. The third application (sea ice model) is an attempt to reproduce the parameterization developed in Juricke et al. (2013) in our ocean model using the generic implementation presented in Sect. 2, and to illustrate the randomness that is generated in the interannual variability of sea ice thickness.

2 Stochastic formulation of NEMO

The ocean model used in this study is NEMO (Nucleus for a European Model of the Ocean), as described in Madec et al. (2008). NEMO is the European modelling framework for oceanographic research, operational oceanography, seasonal forecast and climate studies. This model system embeds various model components (see <http://www.nemo-ocean.eu/>), including a circulation model (OPA, Océan PARallélisé), ecosystem models, with various levels of complexity (e.g. LOBSTER, LOCEAN Simulation Tool for Ecosystem and Resources), and a sea-ice model (LIM, Louvain-la-Neuve Ice model). The purpose of this section is to shortly describe the three kinds of stochastic parameterizations that have been implemented in NEMO, and to show that, from a technical point of view, they can be unified in one single new module in NEMO, feeding the various sources of randomness in the model. (More technical details about this module can be found in the Appendix.)

2.1 Order n autoregressive processes

The starting point of our implementation of stochastic parameterizations in NEMO is to observe that many existing parameterizations are based on autoregressive processes, which are used as a basic source of randomness to transform a deterministic model into a probabilistic model. A generic approach is thus to add one single new module in NEMO, generating processes with appropriate statistics to simulate each kind of uncertainty in the model (see examples in Sect. 3).



In practice, at every model grid point, independent Gaussian autoregressive processes $\xi^{(i)}$, $i = 1, \dots, m$ are first generated using the same basic equation:

$$\xi_{k+1}^{(i)} = a^{(i)} \xi_k^{(i)} + b^{(i)} w^{(i)} + c^{(i)} \quad (1)$$

where k is the index of the model timestep; and $a^{(i)}$, $b^{(i)}$, $c^{(i)}$ are parameters defining the mean ($\mu^{(i)}$) SD ($\sigma^{(i)}$) and correlation timescale ($\tau^{(i)}$) of each process:

- for order 1 processes, $w^{(i)}$ is a Gaussian white noise, with zero mean and SD equal to 1, and the parameters $a^{(i)}$, $b^{(i)}$, $c^{(i)}$ are given by:

$$\begin{cases} a^{(i)} = \varphi \\ b^{(i)} = \sigma^{(i)} \sqrt{1 - \varphi^2} \\ c^{(i)} = \mu^{(i)} (1 - \varphi) \end{cases} \quad \text{with} \quad \varphi = \exp(-1/\tau^{(i)}) \quad (2)$$

- for order $n > 1$ processes, $w^{(i)}$ is an order $n - 1$ autoregressive process, with zero mean, SD equal to $\sigma^{(i)}$; correlation timescale equal to $\tau^{(i)}$; and the parameters $a^{(i)}$, $b^{(i)}$, $c^{(i)}$ are given by:

$$\begin{cases} a^{(i)} = \varphi \\ b^{(i)} = \frac{n-1}{2(4n-3)} \sqrt{1 - \varphi^2} \\ c^{(i)} = \mu^{(i)} (1 - \varphi) \end{cases} \quad \text{with} \quad \varphi = \exp(-1/\tau^{(i)}) \quad (3)$$

In this way, higher order processes can be easily generated recursively using the same piece of code implementing Eq. (1), and using successively processes from order 0 to $n - 1$ as $w^{(i)}$. The parameters in Eq. (3) are computed so that this recursive application of Eq. (1) leads to processes with the required SD and correlation timescale, with the additional condition that the $n - 1$ first derivatives of the autocorrelation function are

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equal to zero at $t = 0$, so that the resulting processes become smoother and smoother as n is increased. AR(2) processes (with other specifications) have already been applied in several studies Berloff (2005); Wilks (2005), and will be used in this paper in the sea ice model application (see Sect. 3.3).

Second, a spatial dependence between the processes can easily be introduced by applying a spatial filter to the $\xi^{(i)}$. This can be done either by applying a simple filter window on the $\xi^{(i)}$ 2-D or 3-D matrices: $\tilde{\xi}^{(i)} = \mathcal{F}[\xi^{(i)}]$, or by solving an elliptic equation: $\mathcal{L}[\tilde{\xi}^{(i)}] = \xi^{(i)}$. In both cases, the filtering operator could be made flow dependent, or more generally, the filter characteristics could be modified according to anything that is resolved by the ocean model (in system \mathcal{A} in Fig. 1). Technically, this only requires that the description of the ocean model is made available to the filtering routines. This filtering option (using a simple Laplacian filter) is used in the sea ice application (see Sect. 3.3).

Third, the marginal distribution of the stochastic processes can also be easily modified by applying a nonlinear change of variable (anamorphosis transformation) to the $\xi^{(i)}$ before using them in the model $\hat{\xi}^{(i)} = \mathcal{T}[\xi^{(i)}]$. This idea is similar to what is done in ensemble data assimilation methods to transform variables with non-Gaussian marginal distribution into Gaussian variables Bertino et al. (2003); Béal et al. (2010); Brankart et al. (2012). For instance, this method can be very useful if the description of uncertainties in the model requires positive random numbers. In this case, anamorphosis transformation can be applied to transform the Gaussian $\xi^{(i)}$ into positive $\hat{\xi}^{(i)}$ with lognormal or gamma distribution. This anamorphosis option (using a gamma distribution) is used in the sea ice application (see Sect. 3.3).

Overall, this method provides quite a simple and generic way of generating a wide class of stochastic processes. However, this also means that new model parameters are needed to specify each of these stochastic processes. As in any parameterization of lacking physics, a very important issue is then to tune these new parameters using either first principles, model simulations, or real-world observations. This key problem of assessing the parameters involved in Eq. (1) cannot be addressed in the present

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paper, and we can only provide a very brief overview of the nature of the problem. Many existing studies (e.g. Frederiksen et al., 2012b; Achatz et al., 2013; Grooms and Majda, 2013) already addressed the problem of choosing the coefficients of the ARn processes to simulate the Reynolds stresses in atmospheric and oceanic flows. Considerable progress has been made for this important problem, but not all unresolved processes have received so much attention, and it is often still difficult to figure out how to derive the parameters of the ARn processes.

In the three applications described in Sect. 3 for instance, there is still no theoretical guidelines to tune the parameters, and this can only be done by comparing the results to higher resolution models or to observations. This is why no quantitative assessment of the parameters will be attempted in this paper. Nevertheless, our point of view is that, for these three applications, the problem would have been considerably more difficult with a deterministic parameterization of unresolved processes, since no deterministic simulation could fit the observations exactly. By explicitly simulating uncertainties, we can describe the actual random behaviour of the system (see Fig. 1); ensemble simulations can be objectively compared to observations (using probabilistic methods, see Brier, 1950; Toth et al., 2003; Candille et al., 2005); and the model (including the stochastic parameters) can be rejected as soon as the ensemble is not reliable. Unknown parameters could also be tuned by solving inverse problems, until ensemble reliability is achieved.

2.2 Stochastic perturbed parameterized tendency

A first way of explicitly simulating uncertainties in meteorological weather forecast was introduced about 15 years ago in the ECMWF ensemble forecasting system Buizza et al. (1999). Their basic idea was to separate the model tendency (\mathcal{M}) into non-parameterized (\mathcal{NP}) and parameterized (\mathcal{P}) tendencies ($\mathcal{M} = \mathcal{NP} + \mathcal{P}$). The non-parameterized tendency (\mathcal{NP}) contains all processes that are fully resolved by the model, and can be assumed free of uncertainties. The parameterized tendency (\mathcal{P}) contains the parameterization of the effect of unresolved processes (system \mathcal{B} in

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Fig. 1), which is essentially uncertain. The stochastic parameterization is then introduced by multiplying the parameterized tendency (\mathcal{P}) by a random noise, explicitly simulating the uncertainties in \mathcal{P} . The basic motivation was to produce ensemble forecasts with enhanced dispersion to improve their reliability (i.e. their consistency with available observations). This technique is still used today in the ECMWF operational forecasting system.

This kind of stochastic parameterization is also meaningful in ocean models, and it can be directly applied in the model using the generic implementation described in Sect. 2.1. This can be done by using one or several of the $\xi^{(i)}$ given by Eq. (1) as multiplicative noise for the various terms of the parameterized tendency:

$$\frac{dx}{dt} = \mathcal{N} \mathcal{P}(\mathbf{x}, \mathbf{u}, \mathbf{p}, t) + \sum_{i=1}^m \mathcal{P}^{(i)}(\mathbf{x}, \mathbf{u}, \mathbf{p}, t) \xi^{(i)}(t) \quad \text{with} \quad \sum_{i=1}^m \mathcal{P}^{(i)} = \mathcal{P} \quad (4)$$

where t is time; \mathbf{x} , the model state vector; \mathbf{u} , the model forcing; and \mathbf{p} , the vector of model parameters. In this case, the mean of the $\xi^{(i)}$ must be set to 1, assuming that the model parameterized tendencies are unbiased, and the other statistical parameters (SD, time and space correlation structure, marginal distribution) are free to be adjusted to any reasonable assumption about the uncertainties. In ocean models, this stochastic parameterization can be applied to any parameterization of unresolved processes (see Fig. 1), as for instance the diffusion operators, simulating the effect of unresolved scales, the air-sea turbulent fluxes, the parameterization of the various functions of the ecosystem dynamics, usually describing the unresolved biologic diversity, . . . An example of this SPPT parameterization is given in the ecosystem application (see Sect. 3.2).

2.3 Stochastic parameterization of unresolved fluctuations

Another way of explicitly simulating uncertainties in ocean models is to directly represent the effect of unresolved scales in the model equations using stochastic processes. Unresolved scales can indeed produce a large scale effect as a result of the nonlinear-

ity of the model equations. Important nonlinear terms in ocean model are for instance: the advection term, the seawater equation of state, the functions describing the behaviour of the ecosystem, . . . Concerning the advection term, the effect of unresolved scales is usually parameterized as an additional diffusion, while for the other terms it is most often ignored. However, in many cases, a direct way of simulating this effect would be to generate an ensemble of random fluctuations $\delta \mathbf{x}^{(i)}$ with the same statistical properties as the unresolved scales, and to average the model operator over the ensemble:

$$\frac{d\mathbf{x}}{dt} = \frac{1}{m} \sum_{i=1}^m \mathcal{M}(\mathbf{x} + \delta \mathbf{x}^{(i)}, \mathbf{u}, \mathbf{p}, t) \quad \text{with} \quad \sum_{i=1}^m \delta \mathbf{x}^{(i)} = 0 \quad (5)$$

This corresponds to an averaging of the model equations over a set of fluctuations $\delta \mathbf{x}^{(i)}$ representing the unresolved scales. The zero mean fluctuations $\delta \mathbf{x}^{(i)}$ can produce an average effect (corresponding to an interaction between \mathcal{A} and \mathcal{B} in Fig. 1) as soon as the model \mathcal{M} is nonlinear. In this parameterization, the number of independent fluctuations (m) and the statistics for each of them should be chosen to simulate the properties of the unresolved scales as accurately as possible.

Obviously, the main difficulty with this method is to generate fluctuations $\delta \mathbf{x}^{(i)}$ with the right statistics to faithfully correspond to the statistics of unresolved processes. As a first very simple approach, this can be done using one or several of the $\xi^{(i)}$ given by Eq. (1), either by assuming that the statistics of $\delta \mathbf{x}^{(i)}$ can be directly approximated by the simple statistical structure of autoregressive processes $\xi^{(i)}$, or by assuming that $\delta \mathbf{x}^{(i)}$ can be computed as a joint function of the model state \mathbf{x} and the autoregressive processes $\xi^{(i)}$. For example, if the fluctuations can be assumed proportional to the large scale gradient $\nabla \mathbf{x}$ of the state vector, the fluctuations $\delta \mathbf{x}^{(i)}$ could be computed as the scalar product of $\nabla \mathbf{x}$ with random walks $\xi^{(i)}$:

$$\delta \mathbf{x}^{(i)} = \xi^{(i)} \cdot \nabla \mathbf{x} \quad (6)$$

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This particular case corresponds to the stochastic parameterization proposed in Brankart (2013) to simulate the effect of unresolved scales in the computation of the horizontal density gradient because of the nonlinearity of the seawater equation of state. Examples of this parameterization are given in the circulation model application (Sect. 3.1) and in the ecosystem application (Sect. 3.2).

2.4 Stochastic parameterization of unresolved diversity

Another general source of uncertainty in ocean models is the presence of various dynamical behaviours, which are not all resolved by the model. For instance, marine ecosystems always contain a wide diversity of species, which cannot be described separately by the model, and which must be aggregated in a limited number of state variables. In a similar way, sea ice can display a wide variety of dynamical behaviours, which cannot always be resolved by ocean models. As unresolved scales, unresolved diversity generates uncertainties in the evolution of the system, which can be explicitly simulated using a similar approach:

$$\frac{dx}{dt} = \frac{1}{m} \sum_{i=1}^m \mathcal{M}(x, u, p + \delta p^{(i)}, t) \quad (7)$$

where $\delta p^{(i)}$ are random parameter fluctuations representing the various possible dynamical behaviours that are simultaneously present in the system.

The application of this method requires a statistical description of the uncertainties in the parameters; and again, as a first approach, this can be parameterized using one or several of the $\xi^{(i)}$ given by Eq. (1). As a particular case, this method includes the stochastic parameterization proposed in Juricke et al. (2013) to explicitly simulate uncertainties in ice strength in a finite element ocean model. It was thus very easy to apply the same scheme in the ice component of NEMO, as an example of this parameterization (see Sect. 3.3).

3 Impact on model simulations

The purpose of this section is now to illustrate the impact of the stochastic parameterizations presented in Sect. 2 in various components of NEMO: in the ocean circulation component in Sect. 3.1, in the ocean ecosystem in Sect. 3.2, and in the sea ice dynamics in Sect. 3.3. The focus of the discussion will be on the probabilistic behaviour of the system (\mathcal{A}) as a result of the uncertainties (the interaction with \mathcal{B} in Fig. 1). All applications have been performed using the same generic code implementing the stochastic formulation of NEMO described in Sect. 2.

3.1 Stochastic circulation model

As a result of the nonlinearity of the seawater equation of state, unresolved potential temperature (T) and salinity (S) fluctuations (in system \mathcal{B}) have a direct impact on the large scale density gradient (in system \mathcal{A}), and thus in the horizontal pressure gradient through the thermal wind equation. As shown in Brankart (2013), this effect can be simulated using the scheme described in Sect. 2.3, by applying Eq. (5) to the equation of state:

$$\rho^{\text{stoch}}(T, S) = \frac{1}{m} \sum_{i=1}^m \rho(T + \delta T^{(i)}, S + \delta S^{(i)}) \quad \text{with} \quad \sum_{i=1}^m \delta T^{(i)} = 0, \sum_{i=1}^m \delta S^{(i)} = 0 \quad (8)$$

where $\delta T^{(i)}$ and $\delta S^{(i)}$ explicitly simulate the unresolved fluctuations of potential temperature and salinity. These fluctuations are generated using random walks following Eq. (6), with parameters for the $\xi^{(i)}$ given in Table 1 (i.e. the same parameterization as in Brankart, 2013). This stochastic parameterization simulates the exchange of potential energy between resolved and unresolved scales, which results from the nonlinearity of the equation of state (see Brankart, 2013 for more details). As for the Reynolds stresses, this should be strongly constrained by physical principles, but we will stick here to the parameters proposed in Brankart (2013), which were derived from a comparison with higher resolution reanalysis data.

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It is interesting to note (as a complement to what is explained in Brankart, 2013) that there is a close similarity between this stochastic correction of the large scale density and the semi-prognostic method proposed in Greatbatch et al. (2004); Greatbatch and Zhai (2006). In both cases indeed, the only correction applied to the model occurs in the thermal wind equation through a direct correction of density, while the conservation equation driving the evolution of potential temperature, salinity and horizontal velocity are all kept unchanged. We can thus be certain that the stochastic parameterization displays the same nice conservation properties as the semi-prognostic method, in particular there is no direct modification of the T , S properties of the water masses, no enhanced diapycnal mixing and thus no compromise with the fact that the ocean interior should primarily flow close to the neutral tangent plane. The modification of the thermohaline structure of the ocean is only produced indirectly through a modification of the main currents.

The first impact of the stochastic T and S fluctuations is indeed on the mean circulation simulated by the model. This mean effect in a low resolution global configuration of NEMO (the ORCA2 configuration, see Madec and Imbard, 1996 for more detail) has been described in detail in Brankart (2013). In summary, the density correction is important (and quite systematically negative because of the convexity of the equation of state) along the main fronts separating the subtropical and subpolar gyres. The mean pathway of the mean current is thus modified, significantly reducing the biases of the deterministic model. In particular, the Gulf Stream pathway no longer overshoots and the structure of the Northwest corner becomes more realistic. The impact on the mean circulation is similar to what can be obtained with the semi-prognostic-method Greatbatch et al. (2004), in which the density correction is diagnosed from observations, whereas the stochastic model behaves as an autonomous dynamical system.

The second effect of the stochastic T and S fluctuations is to generate random variability in the system. Because of the nonlinearity of the equation of state, the small scales constantly modify the structure of the large scale density, and thus the pathway of the large scale circulation. There is a constant flux of information from system \mathcal{B}

(small scales) to system \mathcal{A} (large scales), which is represented in the stochastic model by the random processes $\xi^{(i)}$, and which is totally absent in the deterministic model. This effect is illustrated in Fig. 2, which displays the pattern of sea surface height (SSH) in several key regions of the Atlantic: the Northwest corner (top panels), the Brazil–Malvinas Confluence Zone (middle panels), and the Agulhas Current retroflection (bottom panels). In the non-stochastic simulation, in absence of interannual variability of the atmospheric forcing (as in Brankart, 2013), the interannual variability is extremely weak (see Penduff et al., 2011 for a precise quantification): this is why only one typical year is shown, since all years would all appear identical. In the stochastic simulation however, not only the mean SSH pattern is modified (as shown in Brankart, 2013), the interannual variability is also strongly enhanced, and thus becomes more compatible with the intrinsic large-scale SSH variability that is obtained from higher resolution model or from satellite altimetric measurements (as diagnosed in Penduff et al., 2011). This intrinsic variability (produced in absence of any interannual variability in the atmospheric forcing) is a good proxy to the dispersion that would be observed in a truly probabilistic ensemble forecast. In a high resolution model, this dispersion in the large-scale behaviour can only result from the interaction with the mesoscale (as explained in Penduff et al., 2011). In the low resolution ORCA2 configuration, this unpredictable and intrinsically variable behaviour of the large scales is here (at least partially) restored by a stochastic parameterization of the effect of the mesoscale (which is in system \mathcal{B}) on the large scale density. It must be mentioned however that such a small size sample is not sufficient to provide an accurate quantitative information on the magnitude of this effect. To give more precise quantitative results, further tuning and validation of the stochastic parameterization are required.

To further explore the effect of these uncertainties, we are currently applying the same stochastic parameterization to a $1/4^\circ$ resolution model configuration of the North Atlantic (NATL025). The results (obtained with the parameters listed in Table 1) indicate that the stochastic parameterization tends to produce a mean effect on the Gulf Stream pathway, and to decorrelate the mesoscale patterns produced in different mem-

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bers of the ensemble. The first questions that we would like to address with this kind of simulation are whether it is possible to better tune the stochastic parameterization using reference data, whether the ensemble dispersion can explain a substantial part of the misfit with altimetric observations, and thus whether this kind of ensemble can be used to assimilate SSH measurements in NATL025. And then, as a longer term perspective, maybe the stochastic processes $\xi^{(i)}$ can be used as a control vector for data assimilation, which would therefore display the same nice conservation properties as the semi-prognostic method Greatbatch et al. (2004).

3.2 Stochastic ecosystem model

There are many sources of uncertainty in marine ecosystem models. To simplify the discussion, only two classes of uncertainty will be considered here: uncertainties resulting from unresolved biologic diversity and uncertainties resulting from unresolved scales in biogeochemical tracers (see Fig. 1). On the one hand, to simulate uncertainties resulting from unresolved diversity, we will use the SPPT scheme described in Sect. 2.2 and multiply the “source minus sink” terms (SMS_k) of the ecosystem model by a multiplicative noise:

$$\text{SMS}_k^{\text{stoch}}(C_I) = \text{SMS}_k^{\text{ref}}(C_I) \times \xi^{(k)} \quad (9)$$

where C_I are the biogeochemical tracer concentrations, and $\xi^{(k)}$ are autoregressive processes obtained from Eq. (1), with parameters given in Table 1. To simulate unresolved diversity, the scheme described in Sect. 2.4 would probably have been more natural, but in view of the large number of parameters in the ecosystem model, the SPPT scheme is much easier to implement as a first approach. On the other hand, to simulate uncertainties resulting from unresolved scales, we will use the scheme described in Sect. 2.3, by applying Eq. (5) to the SMS terms:

$$\text{SMS}_k^{\text{stoch}}(C_I) = \frac{1}{m} \sum_{i=1}^m \text{SMS}_k^{\text{ref}}(C_I + \delta C_I^{(i)}) \quad \text{with} \quad \sum_{i=1}^m \delta C_I^{(i)} = 0 \quad (10)$$



where $\delta C_l^{(i)}$ explicitly simulate the unresolved fluctuations of biogeochemical tracer concentrations. These fluctuations are generated using random walks following Eq. (6), with parameters for the $\xi^{(i)}$ given in Table 1. (Since little is known about uncertainties in the ecosystem model, we just used here reasonable values for the parameters.)

As a first approach, the impact of these two stochastic parameterizations has been studied in a low resolution global ocean model, based on the ORCA2 configuration coupled with the LOBSTER ecosystem model (using exactly the same model settings as in the previous section). The ecosystem model (see Lévy et al., 2005 for more details) is a simple model including only 6 compartments (C_k , $k = 1, \dots, 6$): phytoplankton, zooplankton, nitrate, ammonium, dissolved organic matter, and detritus. The behaviour of this model is here illustrated in Fig. 3 by the surface phytoplankton in the North Atlantic for 15 June (in the second year of simulation). As compared to the deterministic simulation (top left panel), the stochastic simulation with the SPPT scheme (top right panel) does not modify very strongly the general behaviour of the system (despite the 50 % SD multiplicative noise), but substantially increase the patchiness of the surface phytoplankton concentration. This suggests the conjecture that uncertainties (in particular unresolved diversity) may partly explain the patchiness of satellite ocean colour images. Conversely, the stochastic simulation of unresolved scales (bottom left panel) does not increase patchiness, but can significantly affect the local behaviour of the system, sometimes increasing or decreasing the production (whether the second derivative of the SMS term is positive or negative). At first sight, these two sources of uncertainty are thus insufficient to explain the considerable misfit between model simulation and ocean colour data.

As an additional experiment, the two stochastic parameterizations have then been used together (bottom right panel), by simply generating a sufficient number of autoregressive processes (corresponding to the two columns together in Table 1) to feed the two schemes. This result shows that there is a strong interaction between the two schemes, leading to a deep modification of the general behaviour of the system, and to enhanced patchiness as compared to the SPPT scheme alone. In our view, this di-

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rectly leads to the idea that uncertainties may be an important ingredient to understand the dynamical behaviours of marine ecosystems, and to make the model distribution consistent with ocean colour observations (in magnitude and pattern). It must be noted however that these experiments only represent a first attempt to explicitly simulate uncertainties in the ecosystem component of NEMO, and that further studies are needed before any meaningful quantitative result can be obtained.

3.3 Stochastic sea ice model

One of the main difficulties of sea ice models is to correctly simulate the wide diversity of ice dynamical behaviours. Among ice characteristics, the most sensitive parameter is certainly the ice strength P^* . In simple ocean models (as in LIM2 in NEMO), P^* is assumed constant, whereas, in more complex models (as in LIM3 in NEMO), the variations of P^* can be explicitly resolved as a function of the various types of ice simultaneously present at every model grid point. The impact of uncertainties in P^* has already been studied in the work of Juricke and coauthors Juricke et al. (2013) using a finite element ocean model (FESOM), coupled to a simple sea ice model similar to LIM2. The purpose of this section is to reproduce their parameterization in NEMO/LIM2 using the generic technical approach described in Sect. 2. This can be done very easily, almost without any additional implementation effort, using the scheme described by Eq. (7) with $m = 1$ and

$$P^* + \delta P^* = P^* \times \xi \quad (11)$$

where ξ is one of the autoregressive processes given by Eq. (1), with parameters given in Table 1. The parameters are chosen to be close to the stochastic parameterization in Juricke et al. (2013). Specificities are the use of order 2 instead of order 1 autoregressive processes, and the use of a gamma marginal distribution instead of another kind of positive distribution in Juricke et al. (2013).

This stochastic parameterization has been applied to a low resolution global ocean configuration of NEMO, again without interannual variability in the atmospheric forcing

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(using the same model settings as in Brankart, 2013). The behaviour of the model is here illustrated in Fig. 4 by the ice thickness in the Arctic at the end of March (when the ice extension is close to its maximum). As compared to the deterministic simulation (top left panel), the first impact of the stochastic parameterization is to systematically increase ice thicknesses, especially in the regions of old ice (North of Greenland and Western Canada), and to slightly decrease the ice extension. These two mean effects are very similar to what is described in Juricke et al. (2013), and cannot be reproduced by a simple uniform modification of P^* .

On the other hand, the stochastic fluctuations of P^* also generate random variability in the system. As for SSH in Sect. 3.1, the interannual variability of ice thickness pattern is extremely weak in ORCA2 without interannual variability of the atmospheric forcing (which is why only one typical year is shown in Fig. 4). In the stochastic simulation however, not only the mean ice thickness pattern is modified (as for SSH in Fig. 2), the interannual variability (which is again a good proxy to ensemble dispersion as explained in Sect. 3.1) is also strongly enhanced. What is expected from these results is thus that the explicit simulation of uncertainties can provide us an adequate basis for probabilistic comparison with sea ice observations, and help us producing reliable ensemble forecasts for sea ice data assimilation problems. Consequently, it might also be that this stochastic approach represents a worthwhile alternative to explicit resolution of sea ice diversity (as in LIM3).

4 Conclusions

In this paper, a simple and generic implementation approach has been presented, with the purpose of transforming a deterministic ocean model (like NEMO) into a probabilistic model. With this method, it is possible to easily implement various kinds of stochastic parameterization mimicking the non-deterministic effect of unresolved processes, unresolved scales, unresolved diversity, ... It has been shown indeed that ocean systems can often display a random behaviour, which needs to be explicitly represented

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in ocean models. Ensemble simulations are then required to sample all possible behaviours of the system. Getting a correct overview of all dynamical possibilities is necessary to objectively compare models to observations, and to use the model as a weak constraint in ocean data assimilation problems.

This technique has been applied to several applications, showing that randomness is ubiquitous in ocean systems: in the large-scale circulation (e.g. because of the effect of unresolved scales through the nonlinear equation of state), in the ecosystem model, (e.g. because of the effect of unresolved scales and unresolved biogeochemical diversity), and in the sea ice dynamics. (e.g. because of the unresolved diversity of sea ice characteristics). In each of these applications, uncertainty can be viewed as an essential dynamical characteristic of the system, which can modify our understanding of the ocean behaviour. As for any complex system, constructing ocean models using optimal (but imperfect) components can often be worse (less robust) than using unreliable components dealing explicitly with their respective inaccuracy. The ocean is like a dice rolling on the table of a casino: we are unable to grasp all subtleties of its movements, and we can only sample from all possible outcomes of the game using probabilistic models.

Appendix A: Implementation issues

All examples of stochastic parameterizations described in this paper have been performed with the same generic tool that we have implemented in NEMO. The purpose of this appendix is to describe this tool, and to show that it could be easily adapted to work in any other modelling system.

The computer code is made of one single FORTRAN module, with 3 public routines to be called by the model (in our case, NEMO):

- The first routine (sto_par, see Algorithm 1) is a direct implementation of Eq. (1), applied at each model grid point (in 2-D or 3-D), and called at each model time step (k) to update every autoregressive process ($i = 1, \dots, m$). This routine also

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includes a filtering operator, applied to $w^{(i)}$, to introduce a spatial correlation between the stochastic processes.

- The second routine (sto_par_init, see Algorithm 2) is an initialization routine mainly dedicated to the computation of parameters $a^{(i)}, b^{(i)}, c^{(i)}$ for each autoregressive process, as a function of the statistical properties required by the model user (mean, SD, time correlation, order of the process, ...). This routine also includes the initialization (seeding) of the random number generator.
- The third routine (sto_rst_write) writes a “restart file” with the current value of all autoregressive processes to allow restarting a simulation from where it has been interrupted. This file also contains the current state of the random number generator. In case of a restart, this file is then read by the initialization routine (sto_par_init), so that the simulation can continue exactly as if it was not interrupted.

Algorithm 1 sto_par

```

for all (map  $i = 1, \dots, m$  of autoregressive processes) do
  Save map from previous time step:  $\xi_- \leftarrow \xi_i$ 
  if (process order is equal to 1) then
    Draw new map of random numbers  $w$  from  $\mathcal{N}(0, 1)$ :  $\xi_i \leftarrow w$ 
    Apply spatial filtering operator  $\mathcal{F}_i$  to  $\xi_i$ :  $\xi_i \leftarrow \mathcal{F}_i[\xi_i]$ 
    Apply precomputed factor  $f_i$  to keep SD equal to 1:  $\xi_i \leftarrow f_i \times \xi_i$ 
  else
    Use previous process (one order lower) instead of white noise:  $\xi_i \leftarrow \xi_{i-1}$ 
  end if
  Multiply by parameter  $b_i$  and add parameter  $c_i$ :  $\xi_i \leftarrow b_i \times \xi_i + c_i$ 
  Update map of autoregressive processes:  $\xi_i \leftarrow a_i \times \xi_- + \xi_i$ 
end for
  
```

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**Algorithm 2** sto_par_init

Initialize number of maps of autoregressive processes to 0: $m \leftarrow 0$

for all (stochastic parameterization $k = 1, \dots, p$) **do**

Set m_k , the number of maps of autoregressive processes required for this parameterization

Increase m by m_k times the process order o_k : $m \leftarrow m + m_k \times o_k$

end for

for all (map $i = 1, \dots, m$ of autoregressive processes) **do**

Set order of autoregressive processes

Set mean (μ_i), standard deviation (σ_i) and correlation timescale (τ_i) of autoregressive processes

Compute parameters a_i, b_i, c_i as a function of μ_i, σ_i, τ_i

Define filtering operator \mathcal{F}_i

Compute factor f_i as a function of \mathcal{F}_i

end for

Initialize seeds for random number generator

for all (map $i = 1, \dots, m$ of autoregressive processes) **do**

Draw new map of random numbers w from $\mathcal{N}(0, 1)$: $\xi_i \leftarrow w$

Apply spatial filtering operator \mathcal{F}_i to ξ_i : $\xi_i \leftarrow \mathcal{F}_i[\xi_i]$

Apply precomputed factor f_i to keep standard deviation equal to 1: $\xi_i \leftarrow f_i \times \xi_i$

Initialize autoregressive processes to $\mu + \sigma \times w$: $\xi_i \leftarrow \mu + \sigma \xi_i$

end for

Read maps of autoregressive processes and seeds for the random number generator from restart file, if any

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This module has been used to produce the 3 examples of stochastic parameterization given in the paper, with the parameters given in Table 1. The same set of basic routines has thus been applied to simulate the random walks of the stochastic equation of state in Sect. 3.1, the random perturbation of the ecosystem model in Sect. 3.2, and the random sea ice dynamics in Sect. 3.3. Moreover, as can be seen from Algorithms 1 and 2, these parameterizations can easily be applied altogether or separately.

In summary, what is proposed here is a very simple algorithmic solution to transform a deterministic model into a probabilistic model. It is easy to adapt to many kinds of model, and generic enough to deal with many other sources of uncertainty. This is obviously not intended to be the final theoretical or technical solution for simulating uncertainties, The algorithms and framework proposed in this study only provide a first-guess solution, which is simple enough to make a first quick evaluation of the effect of a given source of uncertainty, and flexible enough to easily evolve as a better understanding of the problem is progressively obtained.

Acknowledgements. This work has received funding from the European Community's Seventh Framework Programme FP7/2007-2013 under grant agreements 283367 (MyOcean2) and 283580 (SANGOMA), with additional support from CNES. The calculations were performed using HPC resources from GENCI-IDRIS (grant 2014-011279).

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Table 1. Parameters of autoregressive processes for all applications described in this paper. The number of processes is the number of autoregressive processes used in each stochastic parameterization (sometimes multiplied by 3 to produce one process for each component of the random walks). The mean, SD and correlation timescale are the parameters $\mu^{(i)}$, $\sigma^{(i)}$ and $\tau^{(i)}$ used in Eqs. (2) and (3). For the stochastic parameterization of the equation of state (circulation model), the SD are multiplied by $\sin \phi$ for ORCA2, and by $\sin 2\phi$ for NATL025, where ϕ is latitude.

	Circulation model		Ecosystem		Sea ice
	ORCA2	NATL025	unresolved diversity	unresolved scalesF	unresolved diversity
Number of processes	6×3	1×3	6	1×3	1
Order of processes	1	1	1	1	2
Mean value	0	0	1	0	0
SD	$\sigma_{xy} = 4.2$ $\sigma_z = 1$	$\sigma_{xy} = 1.4$ $\sigma_z = 0.7$	0.5	$\sigma_{xy} = 3$ $\sigma_z = 1$	1.
Correlation timescale	12 days	10 days	3 days	12 days	30 days
Spatial filtering	no	no	no	no	Laplacian
Anamorphosis	no	no	no	no	gamma

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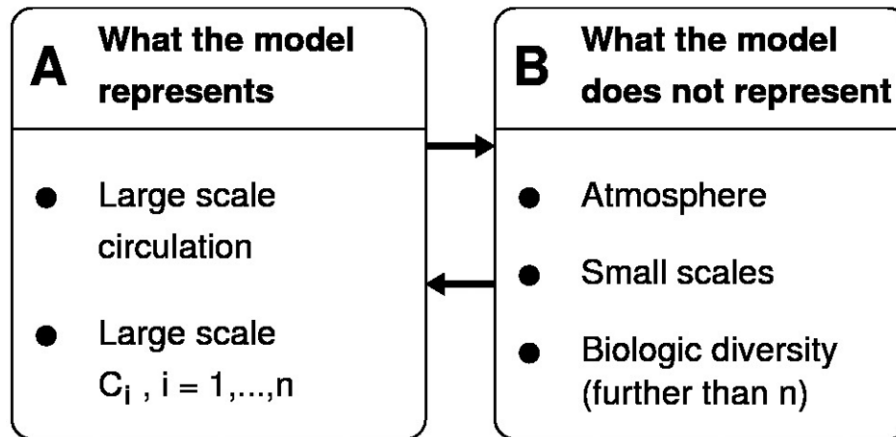


Figure 1. Schematic of the separation between resolved and unresolved processes (systems A and B). Even if $A \cup B$ can be assumed deterministic, system A alone is not deterministic in general, because of the interactions with system B .

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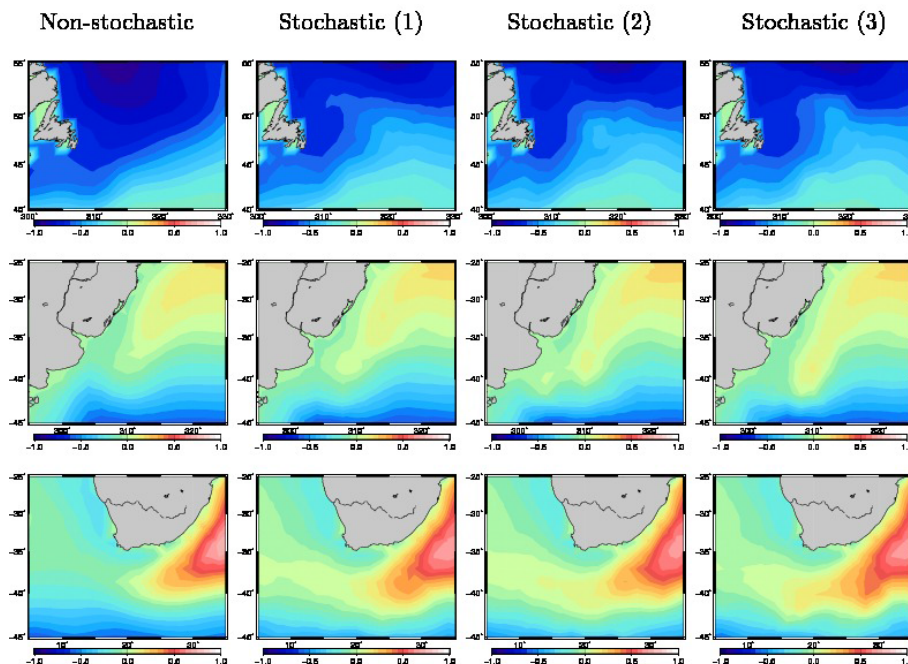


Figure 2. Sample of sea surface height patterns (in meters), illustrating the intrinsic interannual variability generated by the stochastic parameterization of the equation of state in a low resolution global ocean model configuration (ORCA2): northwest corner of the North Atlantic drift (top panels), Brazil–Malvinas Confluence Zone (middle panels), and Agulhas Current retroflexion (bottom panels).

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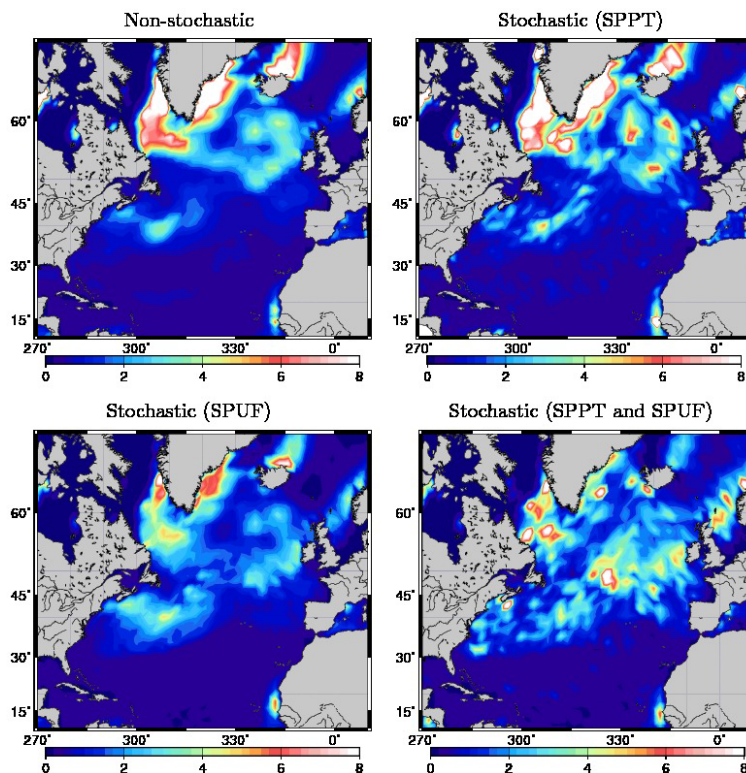


Figure 3. Surface phytoplankton concentration (in mmol-N m^{-3}) for 15 June as obtained with various stochastic parameterizations of uncertainties in the ecosystem model: no stochastic parameterization (top left panel), stochastic simulation of unresolved diversity (top right panel), stochastic simulation of unresolved scales (bottom left panel), stochastic simulation of unresolved diversity and unresolved scales (bottom right panel).

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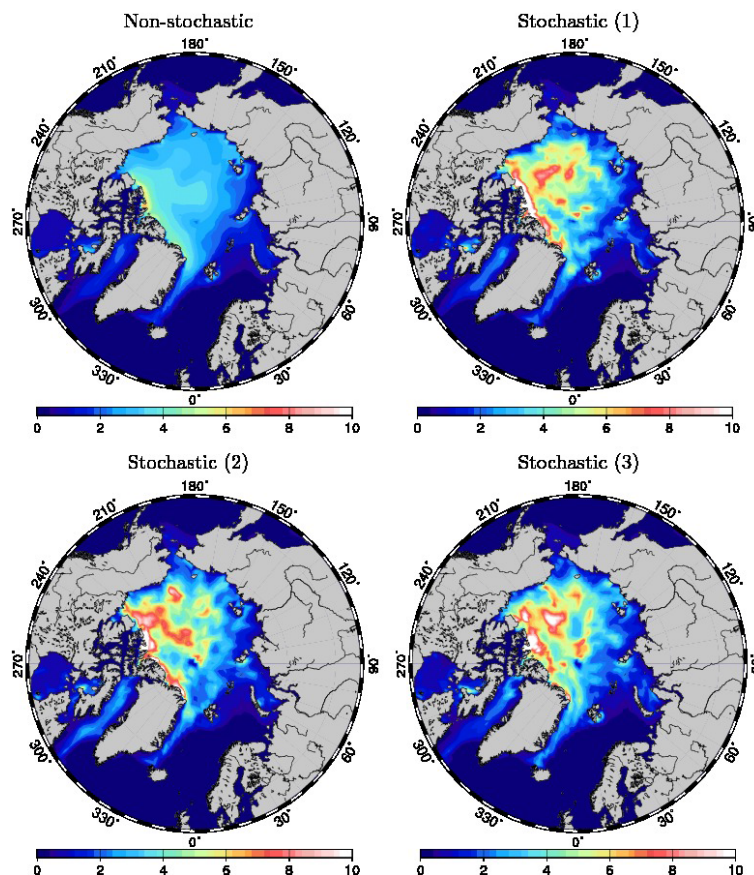


Figure 4. Sample of ice thickness patterns (in meters) in winter (end of March), illustrating the intrinsic interannual variability generated by the stochastic parameterization of ice strength in a low resolution global ocean model (ORCA2).