# Interactive comment on "Treatment of non-ideality in the multiphase model SPACCIM – Part 1: Model development" by A. J. Rusumdar et al.

Anonymous Referee #1

Received and published: 9 July 2015

Review of Rusumdar et al:

The paper presents a new approach to couple a generic group contribution activity coefficient model within the dynamic SPACCIM model. I fully support the author's scientific rationale for including non-ideality in general dynamic models. All too often the influence of non-ideality is ignored through considerations of computational expense at the danger of biasing sensitivity to other processes/composition dependent effects. I do however have a range of general and minor comments I believe the authors should respond to before consideration for publication. The work is clearly substantial, but the presentation of the new work is not clear to suggest the paper has the correct balance of material, which no doubt already exists. The minor comments generally revolve around typically vague statements, or professions of model improvements without appropriate contextualization.

The authors would like to thank the Anonymus Reviewer#1 for the careful consideration of the manuscript and for the constructive comments and suggestions made to improve the manuscript. According to the reviewer's comments, the authors have further improved the manuscript. All comments and changes in the manuscript are addressed below. In the case, we do not concur with the reviewer's comments, adequate reasons are given. Finally, it is noted that the manuscript was again carefully checked for language and writing inaccuracies.

#### **General comments:**

My general comments stem from section 2.3 and the apparent view from the abstract and introduction, that a new activity coefficient model has been developed to warrant the new reference 'SpactMod'. If the basis from AIOMFAC has indeed changed, this should be clearer in the document. However, on inspection of the presented equations, it seems to be the same theoretical framework as presented by Zuend et al (2008) in which case the model appears to be AOMFAC with new interaction parameters. Is this because you have not performed a full parameter refitting across all interaction terms that you have decided to rebrand the model? Section 2.3.1 covers the theoretical background behind activity models derived from the derivative of the Gibbs excess energy. I read this section with the assumption of an adjusted theoretical basis following a similar derivation. I appreciate the presentation of the background, but this section could be much shorter with reference to Zuend et al (2011) and (2008) and where the new parameters fit in the model, without the Gibbs excess terms. I note you have worked with the AIOMFAC developers in the acknowledgement but still find the presentation of already available derivations and lack of information regarding parameter refitting a pity. As I said in the introduction, I believe the work is useful and the presentation of the novelty of this work be reformulated.

# **Author's response:**

The authors would like to clarify several ambiguous formulations and misunderstandings. First, the overall goal of the present work was not the development of a new activity coefficient model. The present paper aimed at the implementation of solution non-ideality in aqueous-phase reaction kinetics in the SPACCIM framework. Therefore, we have incorporated only a "new" activity module in SPACCIM to take into account non-ideality in the multiphase chemistry, especially, for small droplets and deliquesced particles. The extensions of the kinetic framework of SPACCIM are described in Sect. 2. A main goal of the

extended approach (Fig. 2) is to provide appropriate activity coefficients for solved species. Therefore, several activity models have been tested and compared regarding their suitable applicability in order to achieve the above-mentioned objective. Several results of the comparison are presented in Subsect. 3.1 and 3.2. Overall, AIOMFAC seems to be most qualified for the aimed applications. Hence, the theoretical framework and the available parameters of AIOMFAC have been applied for the implementation of the related module in SPACCIM. However, the present study also tried to include additional parameters without any parameter fitting. The approach of mod. LIFAC can be rewritten in the AIOMFAC formalism (see Appendix A). So, we can additionally use the related parameters of this approach to consider further possible interactions not included in AIOMFAC (Zuend et al., 2008). All modifications and additional parameter of SpactMod with respect to AIOMFAC are highlighted now in the revised manuscript.

The authors agree to some point that the main concern and the role of the implemented activity module SpacMod are pointed out not adequately enough in the manuscript. In the revised version, we clarify this in several places. Furthermore the authors agree that the presentation of the used AIOMFAC framework in Sect. 3 is very detailed. However for readability and clarification of the modification, the authors consider a description of the applied AIOMFAC framework close to Zuend et al. (2008) to be necessary.

The referee is right that new parameter refitting was not performed. However, the present work was aimed at building a kinetic model framework that can access the solution non-ideality at the core based on the available interaction parameters. This paper highlights the selection and implementation of a robust activity coefficient model approach that can predict the activity coefficients in relative humidity range important for ambient deliquesced particles.

Page 4174, line20. 'based mainly on AIOMFAC'. What do you mean by 'mainly'. This forms the crux of this section. By 'mainly' it seems you are referring to a reliance on the core of previously published interaction parameters rather than an extension of the theoretical basis. Is this correct?

## **Author's response:**

With the word "mainly" the authors refer to the model derivation and the fitted interaction parameters that were given in Zuend et al. (2008) as they were the basis for the presented SpactMod implementation. The text has been revised.

Page 4180, line 26. 'it was found that [the] model produce[d] relatively better results in most cases in comparison with the parameters from standard UNFIAC only'. There are many aspects to this sentence. First, what statistics back this up? Does this cover a wide range of conditions and functionality? Where is the evidence? In addition, given that standard [parameters] in UNIFAC has been superseded by values fit to more recent and more comprehensive data sets, why is this surprising? It isn't clear based on the discussion, that needs re-writing. This falls into the same concern I have regarding presenting an activity coefficient model development in a sparsely populated scientific evaluation given the introduction of a 'new' model. On the whole, I would have thought it much better to present a more thorough assessment of how the new interaction parameters were fitted, whilst accounting for, as best as possible, mitigation of both under and over-fitting. Indeed, I was expecting more figures showing the prescribed impact of the newly fitted parameters in simple mixtures and yet found only systems that can already be accounted for?

# **Author's response:**

The statement relates to the comparison studies in Subsect. 3.2 (see Figs. 5-8). As mentioned before, we have not performed any parameter fitting (see response above). Due to the reviewers comment we have rephrased the manuscript text. Furthermore, we have added results of two new simulations (Figs. 8 and 9, new numbering) which emphasize the differences and identicalness between AIOMFAC, mod. LIFAC and SpactMod.

#### **Minor comments:**

Page 4156, line 7: 'newly considered non-ideality properties' is confusing. I presume you are referring to a study including non-ideality in the cloud model that has not been considered before. Please revise this sentence. I would suggest something like: 'The present study was aimed at presenting further development of the SPACIM model through treatment of solution non-ideality, which has never been considered before.'

## **Author's response:**

As suggested by the reviewer, the text has been changed. The text now reads: "The present study was aimed at presenting further development of the SPACIM model through treatment of solution non-ideality, which has never been considered before".

Page 4156 line 20: This minor comment feeds into my general concerns in the general comments to follow. The note that AIOMFAC was selected as a 'base' model and extended by additional interaction parameters is clear. If the theoretical basis of said model, in any way has been similar altered, it must be stated here since it would justify the use of a bespoke name for such a framework.

#### **Author's response:**

Due to the reviewer comment, the sentence has been revised as follows:

"Based on an inter-comparison of different activity coefficient models and the comparison with experimental data, AIOMFAC was selected and extended by adding additional interaction parameters from literature for mixed organic-inorganic systems."

Furthermore, it is noted that, the differences between the AIOMFAC and the SpactMod implementation are more clearly highlighted now in the revised manuscript and the appendices at several places.

Page 4156: '..the performance and the capability of the applied activity coefficient module were evaluated by...and results of other thermodynamic equilibrium models'. Please be clear here what exactly you mean by 'thermodynamic equilibrium models'. Models such as GFEMN, E-AIM, ADDEM, MOSAIC, whilst covering various scales of complexity, represent thermodynamic equilibrium models in that they search for the equilibrium end point. They rely on activity coefficient models, which technically should not be covered under the same model description

#### **Author's response:**

In this context, the authors mean the comparison with other activity coefficient models. Thus, the sentence has been changed. "other thermodynamic equilibrium models" have been replaced by "other activity coefficient models".

Page 4157, line 2: I agree activity coefficients should be mandatory but within the context of trying to determine, through process sensitivity studies, the uncertainty through their neglect is 'low enough' to be justified.

## **Author's response:**

The reviewer is right that current activity coefficient models introduce still large uncertainties and the effects of the solution non-ideality must be justified by experimental studies rather than model studies. The stated conclusion is therefore too general and definite. Thus, the sentence was slightly modified to degrade the statement.

Page 4157, line 3: 'Modeled activity coefficients implicate that turnovers of chemical processes..'. What exactly do you mean by 'turnover'? The reader will presume this is somehow related to a time related constraint?

# **Author's response:**

Here the word "turnovers" implicates the mass fluxes of the chemical processes. This is not a time related constraint.

To clarify that, the manuscript text has been revised. The revised text reads: "chemical reaction fluxes".

Page 4157, lines 5 -7. Similarly, please clarify what you mean by 'chemical ion processing'. **Author's response:** 

The authors mean that the "chemical processing of ions". Each reaction considered in the multiphase mechanism is treated as individual process. Apart from the dissociations, by which ions are formed, each ion reacts with other compounds (either organic or inorganic). Hence, the combination of all the reactions in which the particular ion participates (by formation or degradation) gives the information of chemical processing of ions in the particles.

Page 4157, line 8:'..organic compounds are partly > 1..' This kind of statement appears in a number of places throughout the document. Partly? Do you mean that a certain % of activity coefficients are greater than unity? For what conditions? Can you please clarify this.

#### **Author's response:**

Results indicate that some activity coefficients of the organic compounds considered in the multiphase mechanism were obtained >1 e.g. for alcohols, some of the di-aldehydes and for the dicarboxylic acids (except dissociated organic ions). The detailed analysis will be presented in companion paper. In the manuscript, the sentence in the abstract has been replaced by "...organic compounds are in some cases larger than 1 under deliquesced particle conditions" in order to avoid confusions. Moreover, the sentence in the Summary chapter has been revised.

Page 4158, line 18. Please introduce the relevant scale of activity coefficients at the very beginning [mole fraction or molality].

# **Author's response:**

Throughout the simulations including the sensitivity studies, activity coefficients are estimated on molality basis (please see, e.g., section 2.3.5 in the manuscript). To make this clearer at this point, we have added the basis already in the introduction.

Page 4158, line 26'..ideal solution in aerosol models has to be abandoned and non ideal behavior has to be considered.' Again, I generally support you strong view on this issue. However, it should really be contextualized. You do refer to previous studies that suggest neglect of certain inorganic-organic interactions can lead to lower errors than an attempt at their inclusion. I would suggest adding the caveat that a range of sensitivity studies, from models that can account for composition dependent processes, need to be carried out to support either inclusion or neglect.

# **Author's response:**

The sentence "Hence, the assumption of ideal solution in aerosol models has to be abandoned and non-ideal behavior has to be considered." was changed into "Hence, a recent review by Herrmann et al. (2015) suggested that for modeling of multiphase chemical processes in a concentrated solution, it is reasonable to consider the non-ideal behavior instead of assuming ideal solutions." Furthermore, a remark has been added to the manuscript regarding the need of a range of further sensitivity studies with models accounting for composition dependent processes to clarify the role of the non-ideal behavior and, overall, its inclusion or neglect in aerosol chemistry models.

Page 4159, line8: '..effort has been devoted formerly to..'. Suggest removing formerly. **Author's response:** 

We agree to the reviewers comment and have removed "formerly".

Page 4159, line 16: The comment on various numerical techniques based on energy minimization and their cost is slightly confusing. The cost of such schemes tends to derive not from the numerical core of that search, but from the cost of the activity coefficient model and the number of compounds used in calculations. Suggest adding more recent references here.

#### **Author's response:**

We approve that the number of compounds considered mainly governs the numerical costs. However, the applied numerical algorithm affects primarily the computational amount, especially, if we have in mind 3D applications where the equations have to solve in each grid cell. Nevertheless, the numerical expenses are somehow comparable for both approaches. The corresponding paragraph has been revised. The remark regarding the numerical efficiency is removed.

Page 4159, line 22.'Only very few models exist that treat partitioning to an efficient and accurate thermodynamics model'. Again, what do you mean by efficient thermodynamics model? Is SPACCIM particularly efficient? I would recommend, if this is the case, it is stated somewhere clearly. Also, MOSAIC and ADCHAM, for example, represent both extreme points in the modeling spectrum. MOSAIC was developed to face challenges associated with capturing thermodynamics in a regional model, whereas ADCHAM by appearance tried to include every process into a chamber based box model in one study.

#### **Author's response:**

The whole paragraph has been revised and the phrase "an efficient and accurate" is not included in the revised manuscript. Accurate and efficient thermodynamic module means that apart from the estimation of activity coefficients, the thermodynamic module should reliably predict water content and vapor-liquid phase equilibrium in multicomponent aerosols at a given relative humidity and temperature. We claim that SPACCIM can estimate the above mentioned. Nevertheless, MOSAIC and ADCHAM are surely also accurate and efficient models.

Page 4159, line 25 onwards. Here the authors claim that interactions between organic compounds and inorganic components have remained elusive. This was true for some-time, but has improved significantly. The discussion on the range of organic compounds treated in up-to date activity coefficient models, specifically AIOMFAC, should be included here to put the argument into context. You have already included Zuend et al (2011) in the reference list, please include this in your discussion. It might be covered elsewhere so please make sure the text flows better in a new version. Indeed, I would consider grouping distinct discussions into the same part of the text: Existing activity models, current state of interaction matrices, why this study builds on these.

#### **Author's response:**

The authors agree and have largely revised the whole paragraph in the manuscript.

Page 4160, line 4 'is an object of intense research all along the last years'. Suggest 'has been the focus of many detailed studies'.

#### **Author's response:**

The authors agree with reviewer's comment and have modified the manuscript according to the reviewer suggestion. The revised text reads: "as well as detailed thermodynamic comprehensions of its non-ideal behavior, has been focus of many detailed studies."

Page 4160, line 18: 'the kinetic description of non-ideality in SPACCIM is elaborated'. This another awkward sentence to read. I would suggest 'This paper is split into x sections. In section x, we described the inclusion of non-ideality into the SPACCIM model. . .etc'

#### **Author's response:**

Following the reviewers comment, we revised the manuscript text. The revised text reads:

"This paper split into 4 sections. In section 2, we described the implementation of solution non-ideality into the SPACCIM model. In subsequent subsections, the coupling between microphysics and multiphase chemistry models as well as the necessary adjustments of numerical schemes is discussed. In Sect. 2.3, the activity coefficient module is introduced, that is specifically designed to treat multicomponent mixed organic—inorganic aerosol particles. Section 3 presents an evaluation of the currently implemented activity coefficient module in SPACCIM."

Page 4161, line 18. Here you comment on the ability to account for a 'detailed' description of processing of gases and particles prior to cloud formation, during and after its life-cycle. Does this account for the effect of condensing components on the effected size distribution, thus microphysics, at the point of activation? Note there has been some papers discussing the impact of co-condensation on increased cloud droplet numbers.

#### **Author's response:**

In the manuscript it was clarified that: "The droplet activation depending on the particle size and composition is explicitly described (see Sehili et al., 2005 and Wolke et al., 2005)." The SPACCIM microphysical model does consider the condensation of water and the chemistry model part takes into the account the corresponding uptake of water-soluble organic and inorganic vapors. Due to the close coupling (see also Sect. 2.2.4 and 2.2.5), a feedback, e.g., due to co-condensation is considered in SPACCIM (see also Author's response on the next comment).

Due to the reviewer comment the text in Sect. 2.1 has been extended as follows:

"Changes of the chemical aerosol composition by gas scavenging and chemical reactions feed back on the microphysical processes (e.g., water condensation growth rates via changes in the Raoult term). Consequently, related processes such as co-condensation (see, e.g., Topping et al. (2013) for details) are considered in the model."

Page 4161, line20: An advanced coupling. What is it 'advanced'? Are the other developments 'advanced'?

#### **Author's response:**

"Advanced" means a (two-way) coupling between microphysics and multiphase chemistry in both directions). The feedback of chemical composition on explicit droplet activation (by Raoult term and surface tension) is considered. Furthermore, the coupling scheme is adjusted to the used implicit time integration scheme. However, as now discussed in Subsect. 2.2.6, only a simplified surface tension approach is used currently and should be advanced in future SPACCIM versions.

We replaced "advanced" to "robust and efficient" and changed the next sentence into "The coupling scheme is adjusted to the applied time integration method and provides ...".

Page 4162, line 4:' The used chemical mechanism' is awkward. I would suggest 'the chemical mechanism used is provided as an input file'.

# **Author's response:**

According to the reviewer comment, the text has been changed and now reads: "The applied multiphase chemical mechanism (including phase transfer data and kinetic reaction constants) is provided as an input file."

Page 4163, line 7, 'Mainly, the aqueous concentrations ...' what do you mean by 'mainly'? Is this a dominant feature somehow of the model development? Please clarify.

## **Author's response:**

"Mainly" was changed to "In particular".

Page 4164, line 13. Here you introduce the reliance on Henry's law coefficients. Given the drive to include non-ideality in the model, how do you know, for a wide range of atmospheric compounds, that Henry's law coefficients are more constrained that pure component vapour pressures? Do Henry's law coefficients cover the same range of functionality that has driven you to extend activity coefficient model interaction parameters?

#### **Author's response:**

The SPACCIM model is designed to treat processes of aqueous aerosol particles and cloud droplets. Therefore, the phase partitioning of soluble gas phase compounds into the aqueous phase of deliquesced and cloud phase is described based on the Henry's law. However, the Henry's law constants of an aqueous solution depend on the composition of the aqueous solution. For example, they depend on the ionic strength (electrolyte identity) of the solution.

Non-ideal electrolyte solutions are able to both suppress the uptake below the value expected for pure water uptake ("salting-out") and enhance uptake of the soluble gas ("salting-in"). The salting effects can be quantitatively described by the Setschenow equation (Sander et al. 2015). However, as reported in the review of Sander, there are unfortunately only some data available at current. Therefore, salt effects are only considered in the present SPACCIM model developments due to the consideration of the activity coefficients in the uptake calculation. Therefore, the reviewer is right in saying, that the Henry's law coefficients do not cover the same range of functionality as activity coefficient models.

According to the reviewer comment, the authors have extended the model description part (Sect. 2.2) in order to address the issue and the current limitations due to salting effects.

Page 4166, section 2.2.3. I have a few issues when reading the section regarding terminology. You introduce a saturation vapour pressure, but relate this to the molality of the compound in question. I believe you should be referring to an equilibrium vapour pressure above the solution droplet? Saturation vapour pressure relates to the vapour pressure above a solution of the pure component [liquid or solid depending on the reference state]. Indeed, you then go on to refer to a 'saturation vapour mole concentration.' This does seem to be the case since you then express the [equilibrium] vapour pressure to the concentration in the gas phase at the same conditions.

#### **Author's response:**

Due to the author's opinion, the terminology is correct.

Page 4168 line 25. 'Eq1 is used to determine the equilibration of water between the liquid and vapour phase'. Does this mean you do not account for a dynamic condensation of water to the condensed phase?! If so, this could have significant implications for the prescribed microphysics couldn't it? Perhaps I have misunderstood this.

#### **Author's response:**

The water condensation is described dynamically and simultaneously for the whole particle/droplet spectrum. Eq. (1) describes only the equilibrium for a non-activated particle. This was pointed out at the end of Subsect. 2.2.5.: "Eq. (1) has to be fulfilled simultaneously for all non-activated particle classes. The droplet activation is described explicitly and takes place for all particles, which grow over the critical radius. The condensation and evaporation of the activated droplet classes are described dynamically. The predicted saturation vapor pressure is used as input into the droplet growth equation. The coupled system for all classes has to be solved simultaneously, whereas the total amount of water (liquid or gaseous) is prescribed." However, we clarify here that Eq. (1) is only used "... for deliquescent particles."

Page 4169, line 12. Please define precisely. Does mean other developments are not particularly precise?!

# **Author's response:**

The author's mean precisely is appropriate way. We have revised the sentence as follows: "On the other hand, the description of change in droplet curvature (Kelvin effect) is treated with surface tension approaches (see Subsect. 2.2.6)."

Page 4169, line 13:'Both effects are primarily appointed by the particle composition..'. Suggest replacing 'primarily appointed' by 'influenced'.

## **Author's response:**

As suggested by the reviewer, the text has been modified. "primarily appointed" was replaced by "influenced" in the revised manuscript.

Page 4170, section 2.2.6. I have many issues with this section, which will need a significant re-write. Please add a reference for the 'almost' linear approximation. What exactly do you mean by 'almost'? Inclusion or neglect of surface tension has been the focus of many studies since the paper by Facchini et al (1999). I found it odd that there is not, at least, a brief

discussion as to why this particular equation was used. It is not enough to simply choose it based on convenience, as it isn't clear what effect it might have on your results. This particular formulation would lead to a significant decrease in surface tension at the point of activation. On the other hand, the studies of Sorjamaa et al 2004/Topping et al 2007/Prisle et al 2012 to name a few have since question the true meaning of surface tension, based on solving the Gibbs adsorption isotherm. The general study of Prisle et al 2012 indicated that using a range of models that can account for this effect can remove the previously held view of a significant impact from a decrease in surface tension but with appropriate caveats in the discussion. These studies need to be included in any discussion of any inclusion, or neglect, of a surface tension effect.

# **Author's response:**

The "Surface Tension" subsection 2.2.6 was rewritten by considering the recommendations of the reviewer.

Page 4176, line 8 'are described same as original AIOMFAC', Suggest 'described as they are in..'

#### **Author's response:**

Following the reviewers comment, we changed the text in the manuscript to "The LR interactions described as they are in original AIOMFAC".

Page 4177, lines17 – 19 really do not make sense. What exactly are you referring to with regards the statement: 'compensation of these inaccuracies is controlled by this simplification'. Please revise this.

# **Author's response:**

The uncertainties occurred by using the properties of water (instead of using compound specific di-electric constants, densities), the semi-empirical MR part describes all the interaction effects involving ions not considered by the LR and SR contributions. This includes corrections to assumptions made in the LR and SR parts with respect to approximations of physical parameters.

Due to the reviewer comment, the text has been modified as follows:

The uncertainties occurred due to the adopted assumptions to derive the LR and SR activity coefficients with respect to approximations of physical parameters, were described in the semi-empirical SR part in the original AIOMFAC (Zuend et al., 2008)

Page 4180, line 22 'are also comprised in the SR part'. Replace comprised with 'included'. **Author's response:** 

As suggested by the reviewer, "comprised" has been replaced by "included".

# Interactive comment on "Treatment of non-ideality in the multiphase model SPACCIM – Part 1: Model development" by A. J. Rusumdar et al.

## **Anonymous Referee #2**

Received and published: 21 July 2015

The authors have implemented the effects of solution non-ideality in aqueous-phase reaction kinetics in the SPACCIM modeling framework. This manuscript focuses on the model development and numerical aspects of the new treatments while a companion manuscript focuses on the results from detailed modeling studies. The manuscript is recommended for publication after the following minor comments are addressed.

The authors would like to thank the Anonymus Reviewer#2 for the careful consideration of the manuscript and for the constructive comments and suggestions made to improve the manuscript. Those are addressed below. Furthermore, we have added results of two new simulations (Figs. 8 and 9, new numbering) which emphasize the differences and identicalness between AIOMFAC, mod. LIFAC and SpactMod. Additionally, the applied SpactMod parameters are compiled in Appendix A.

#### **Comments:**

Page 4156, line 5: "...models do generally not consider..." sounds awkward. Suggest revising to "...models generally do not consider.."

## **Author's response:**

The authors agree with reviewer's comment and have modified the manuscript according to the reviewer suggestion.

Page 4156, line 6: Please define SPACCIM (all acronyms should be defined at their first use). **Author's response:** 

The acronym of SPACCIM ("Spectral Aerosol Cloud Chemistry Interaction Model") was added to the manuscript text and the whole manuscript was again checked for undefined acronyms and their definition at their first use. Furthermore, a list of all acronyms, indices and symbols are now provided in Appendix B (see also a comment below).

Page 4156, line 8: Revise "The present paper describes firstly, the performed model development including (i)..." to "The present paper firstly describes the model developments, including (i)..."

# **Author's response:**

As recommended by the reviewer, the text has been modified in the suggested way.

Page 4156, line 9: the phrase "the kinetic implementation of the non-ideality in the SPACCIM framework" is confusing. Suggest revising it to "the implementation of solution non-ideality in aqueous-phase reaction kinetics in the SPACCIM framework." Similar sentences elsewhere in the manuscript should also be revised appropriately.

# **Author's response:**

We agree to the reviewers comment. The sentence has been rephrased. Furthermore, the whole manuscript was checked for similar sentences and those were revised correspondingly.

Page 4156, line 13: delete "performed"

# **Author's response:**

Following the reviewers comment, we deleted "performed" in the manuscript text.

Page 4159, line 6: The "Zaveri et al., 2005" citation here should refer to "Zaveri, R. A., R. C. Easter, and A. S. Wexler (2005a), A new method for multicomponent activity coefficients of electrolytes in aqueous atmospheric aerosols, J. Geophys. Res., 110, D02201, doi:10.1029/2004JD004681," which is presently missing in the list of references. Then on line 11, change "Zaveri et al., 2005" to "Zaveri et al., 2005b", and make appropriate changes in the references.

#### **Author's response:**

The suggested reference was insert according to the reviewers comment.

Page 4160, line 4: The "Shrivastava et al., 2011" reference is inappropriately cited here as that work makes a highly simplified assumption for SOA partitioning and does not include interactions between organic and inorganic species. I suggest deleting it.

#### **Author's response:**

The authors agree to the reviewer's opinion and deleted the reference (Shrivastava et al., 2011) in the manuscript text.

Page 4163, line 12: Please list the total number of particle and droplet classes used in the model. Also how is the size distribution represented in each class of particle/ droplet? Is it modal or sectional approach?

#### **Author's response:**

The SPACCIM framework allows representing the size distribution of particles by a sectional approach (see Wolke et al. 2005 for details). However, the simulations in the present paper consider only a mono-disperse particle population to focus on the influence of non-ideality. A number concentration of 10<sup>8</sup> cm<sup>-3</sup> and an initial particle radius of 200 nm were used for the sensitivity studies as mentioned in Subsection 3.3.1.

This paper will greatly benefit by adding a list of all the notations used. There are many variables, subscripts, superscripts, and indices, which are difficult to keep track of without a systematic list of them.

# **Author's response:**

The authors agree with the idea of the reviewer. Thus, the revised manuscript includes a list of symbols, indices and abbreviations used in the paper.

Table 1. What is m\_s? Should the activity of a solid be unity?

#### **Author's response:**

No, the activity of solid is not treated as unity. However, the corresponding activity coefficient is equal to unity. M\_s represents to the molality of the corresponding solid. Due to the reviewer query, the revised Table 1 clarifies the issue now.

Figure 5. What model does the solid black line refer to? I believe it is AIOMFAC, but it's is not indicated in the figure by an arrow.

## **Author's response:**

The solid black line refers to E-AIM that was shown in the Figure. In the title, it was a mistake to mention the AIOMFAC. The authors apologize for this error. We have changed the text of the Figure caption in the manuscript concerning the remark of the reviewer.

# 1 Treatment of non-ideality in the multiphase model

# 2 SPACCIM- Part I: Model development

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#### Abstract

10 Ambient tropospheric deliquesced particles generally comprise a complex mixture of electrolytes, organic compounds, and water. Dynamic modeling of physical and chemical 11 12 processes in this complex matrix is challenging. Thus, up-to-date multiphase chemistry models generally do not consider non-ideal solution effects. Therefore, the present study was 13 aimed at presenting further development of the SPACCIM (Spectral Aerosol Cloud 14 15 Chemistry Interaction Model) model through treatment of solution non-ideality, which has not 16 been considered before. The present paper firstly describes the model developments including 17 (i) the implementation of solution non-ideality in aqueous-phase reaction kinetics in the SPACCIM framework, (ii) the advancements in the coupling scheme of microphysics and 18 19 multiphase chemistry and (iii) the required adjustments of the numerical schemes, especially in the sparse linear solver and the calculation of the Jacobian. Secondly, results of sensitivity 20 21 investigations are outlined aiming at the evaluation of different activity coefficient modules 22 and the examination of the contributions of different intermolecular forces to the overall 23 activity coefficients. Finally, first results obtained with the new model framework are 24 presented.

The parcel model SPACCIM was developed and, so far, applied for the description of aerosol-cloud interactions. To advance SPACCIM also for modeling physical and chemical processes in deliquesced particles, the solution non-ideality have to be taken into account by utilizing activities in reaction terms instead of aqueous concentrations. The main goal of the extended approach was to provide appropriate activity coefficients for solved species. Therefore, an activity coefficient module was incorporated in the kinetic model framework of

Gelöscht: models do generally not consider

Gelöscht: never

Gelöscht: Therefore, the present study was aimed at the further development of the SPACCIM model to treat both complex multiphase chemistry and phase transfer processes considering newly non-ideality properties of concentrated aerosol solutions. The present paper describes firstly, the performed model development including

**Gelöscht:** the kinetic implementation of the non-ideality in the SPACCIM framework,

Gelöscht: performed

1 SPACCIM. Based on an intercomparison of different activity coefficient models and the comparison with experimental data, AIOMFAC approach was implemented and extended by 2 additional interaction parameters from literature for mixed organic-inorganic systems. 3 Moreover, the performance and the capability of the applied activity coefficient module were 4 evaluated by means of water activity measurements, literature data and results of other 5 6 activity coefficient models. Comprehensive comparison studies showed that the SpactMod 7 (SPACCIM activity coefficient module) is valuable to predict the thermodynamic behavior of complex mixtures of multicomponent atmospheric aerosol particles. First simulations with a 8 9 detailed chemical mechanism have demonstrated the applicability of SPACCIM-SpactMod. 10 The simulations indicate that, the treatment of solution non-ideality might be needed for modeling multiphase chemistry processes in deliquesced particles. The modeled activity 11 coefficients implicate that chemical reaction fluxes of chemical processes in deliquesced 12 13 particles can be both decreased and increased depending on the particular species involved in 14 the reactions. For key ions, activity coefficients on the order of 0.1-0.8 and a strong 15 dependency on the charge state as well as the r.h. conditions are modeled implicating a lowered chemical processing of ions in concentrated solutions. In contrast, modeled activity 16 17 coefficients of organic compounds are in some cases larger than 1 under deliquesced particle conditions and suggest the possibility of an increased chemical processing of organic 18 compounds. Moreover, the model runs have shown noticeable differences in the pH values 19 20 calculated with and without consideration of solution non-ideality. On average, the predicted pH values of the simulations considering solution non-ideality are -0.27 and -0.44 pH units 21 22 lower under 90% r.h. and 70% r.h. conditions, respectively. More comprehensive results of detailed SPACCIM-SpactMod studies on the multiphase processing in organic-inorganic 23 mixtures of deliquesced particles are described in a companion paper. 24

Gelöscht: The main product of the performed model development is the new kinetic model approach SPACCIM-SpactMod, which utilizes activities in reaction terms instead of aqueous concentrations.

Gelöscht: was selected as base model

**Gelöscht:** other thermodynamic equilibrium models

Gelöscht: have implied

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#### 1 Introduction

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2 The troposphere is a complex multiphase and multicomponent environment with 3 simultaneous occurrence of heterogeneous chemical transformations, which potentially can alter the composition of tropospheric aerosols (Ravishankara, 1997). In order to access the 4 5 impact of physico-chemical and dynamical processes associated with aerosol particles, a 6 variety of multiphase chemistry mechanisms have been developed and coupled with 7 atmospheric models (Binkowski and Roselle, 2003; Fast et al., 2006; Seinfeld and Pandis, 8 2006). During the last decade, some progress was made evaluating the role of chemical 9 aqueous phase processes in deliquesced particles and cloud droplets (see e.g., Hallquist et al. 10 (2009); Tilgner and Herrmann (2010); Ervens et al. (2011); Tilgner et al. (2013); Guo et al. (2014)). Beside the multiphase chemistry developments and findings, the inclusion of reliable 11 12 thermodynamic modules in multiphase models is required in order to adequately calculate the particle deliquescence, associated water content, chemical reactions and phase transfer 13 14 processes in multicomponent aerosols at given conditions. Furthermore, these modules are in demand to compute the reactive mass transfer driving forces for dynamic gas-particle 15 16 partitioning of various semi-volatile species considering complex chemical transformations in aqueous phase. 17

The calculation of gas to particle partitioning of water, semi-volatile inorganic and organic compounds requires the corresponding vapor pressures, which depend on the saturation vapor pressures of pure compounds and the activity coefficients in the liquid mixture. The Köhler theory (Köhler, 1936) gives a relation between the equilibrium saturation ratio  $S_w$  of water vapor above an aqueous solution droplet and the droplet equilibrium size:

23 
$$S_{w} = \frac{p_{w}}{p_{w}^{o}} = \frac{RH}{100} = a_{w} \exp\left(\frac{2\nu_{w}\sigma_{w,s}}{RT r_{drop}}\right)$$
 (1)

where  $p_w$  is the equilibrium partial pressure of water over the solution droplet,  $p_w^o$  is the equilibrium water vapor pressure over a flat surface of pure water, RH(-) is the ambient relative humidity;  $\sigma_{w,s}(N m^{-1})$  is the droplet solution surface tension;  $R(J mol^{-1} K^{-1})$  is the universal gas constant; T(K) is the temperature;  $r_{drop}(m)$  is mean wet radius of droplet; and  $v_w(m^3 mol^{-1})$  is the partial molar volume of water. The water activity  $a_w$  is given as the product of the mole fraction of water  $x_w$  in a solution and the molality based water activity

coefficient  $\gamma_w$ , which accounts for the effects of all intermolecular interactions that takes 1 2 place in the solution. Activity coefficients give an indication of the degree of thermodynamic 3 non-ideality. Such non-ideal conditions can be expected in deliquesced particles, where, e.g., ionic strengths of about 1-45 mol L<sup>-1</sup> (Herrmann, 2003; Herrmann et al., 2015) are present. In 4 a highly concentrated solution, ions and non-water molecules are more close to each other; 5 therefore they influence each other through electrostatic forces or other physical interactions. 6 7 These intermolecular forces modify the affinity of a substance to transfer from one phase into 8 another phase or to enter into a chemical reaction. Hence a recent review by Herrmann et al. 9 (2015) suggested that for modeling of multiphase chemical processes in a concentrated 10 solution, it is reasonable to consider the non-ideal behavior instead of assuming ideal 11 solutions. Thus, activities have to be used instead of concentrations and the appropriate 12 calculation methods have to be employed in multiphase chemistry models. Consequently, a range of sensitivity studies with models accounting for composition dependent processes need 13 14 to be carried out to clarify the role of the non-ideal behavior, e.g., for the tropospheric 15 multiphase chemistry in deliquesced particles and, overall, its inclusion or neglect in aerosol 16 chemistry models. 17 In order to simulate gas/particle mass transfer in aerosol models, three main approaches (i.e., 18

In order to simulate gas/particle mass transfer in aerosol models, three main approaches (i.e., equilibrium, kinetic (or dynamic), and hybrid) have been used in literature (Zhang et al., 2004). The equilibrium approach assumes equilibrium between multiple aerosol phases and the ambient gas concentrations reach equilibrium concentrations at the particle surface instantaneously. The kinetic approach does not rely on the instantaneous equilibrium assumption. In this approach, the gas/particle mass transfer due to the difference between the ambient gas concentration and equilibrium gas concentration is explicitly simulated for each particle class. Usually, hybrid models employ the kinetic approach for coarse particles and the equilibrium approach for fine particles. Thus, an aerosol thermodynamic model is an essential part of all three gas/particle mass transfer approaches.

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Considerable effort has been devoted to develop a number of thermodynamic models with reliable accuracy and efficiency to simulate aerosol thermodynamic equilibrium. These models treat particle compositions of varying levels of complexity, often associated by the numerical technique chosen and the activity coefficient model applied. They can be divided into two types, i.e., equation-based approach and Gibbs free energy minimization approach. In the equation-based approach (e.g. ISORROPIA II, Fountoukis and Nenes (2007), Nenes et

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Gelöscht: the

**Gelöscht:** the assumption of ideal solution in aerosol models has to be abandoned and non-ideal behavior has to be considered.

Gelöscht: applied

al. (1998); EOSAM3, Metzger and Lelieveld (2007), Metzger et al. (2006); EOUISOLV II, Jacobson (1997), Jacobson et al. (1996); MARS-A, Binkowski and Roselle (2003), Saxena et al. (1986); MESA, Zaveri et al. (2005a)) a set of reactions is assumed to occur in the atmospheric chemical system (including both gas phase and aerosol phase). The equilibrium state is predicted through the solution of the nonlinear equations system. In the Gibbs free energy minimization approach (e.g. AIM, Clegg et al. (1998b, 1998a); GFEMIN, Ansari and Pandis (1999a); ADDEM, Topping et al. (2005a, 2005b); UHAERO, Amundson et al. (2006); Amundson et al. (2007)), the equilibrium state of the aerosol system is predicted through the solution of minimization of the Gibbs free energy of the system. Some of the thermodynamic models mentioned above have been compared and evaluated in several studies (Ansari and Pandis, 1999b; Zhang et al., 2000; Yu et al., 2005; Metzger et al., 2006). The equilibrium approach assumes that particles are in thermodynamic equilibrium with the corresponding gas phase, i.e., the mass transfer between the phases is instantaneous. However, this assumption must not be necessarily valid for every compound and condition, for example in case of coarse particles (e.g., Wexler and Seinfeld (1990)). Therefore, the mass transfer has to be described dynamically by using kinetic or hybrid approaches (e.g., MADM by Pilinis et al. (2000)). Such aerosol modules, that treat dynamically gas-particle partitioning of inorganic and organic gases coupled to thermodynamics modules, are developed for the more general use in 3D models (e.g., MOSAIC by Zaveri et al. (2008), MADRID by Zhang et al. (2004)) or for detailed process descriptions in laboratory (e.g., ADCHAM by Roldin et al. (2014)). As mentioned above, determining appropriate activity coefficients is required in the thermodynamic models. This was achieved by using both mixing rules and potentially more accurate techniques for calculating the activity coefficients. Attempts at realistic estimation of activity coefficients can be traced back to extensive literature for inorganic electrolyte solutions (e.g., Prausnitz et al. (1986); Pitzer (1991); Clegg et al. (1998b, 1998a); Nenes et al. (1998); Metzger et al. (2002); Topping et al. (2005a); Zaveri et al. (2005a); Fountoukis and Nenes (2007)). While the interactions between inorganic compounds are relatively wellknown, interactions between organic components as well as organic-electrolyte mixtures comprised in complex multiphase systems have remained elusive for some-time, due to the large number of organic species with highly variable properties available in the gas phase and in ambient particles. Starting with the more conceptual paper of Clegg et al. (2001), several approaches for the treatment of organic-inorganic mixtures in ambient particles were developed and incorporated in thermodynamic models (e.g., Ming and Russell (2002);

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1 Topping et al. (2005b); Erdakos et al. (2006); Metzger et al. (2006); Clegg et al. (2008); 2 Zaveri et al. (2008); Zuend et al. (2008); Zuend et al. (2011); Ganbavale et al. (2015)]. 3 Raatikainen and Laaksonen (2005) have compared different activity coefficient models, and 4 four models were extended by fitting new parameters for aqueous organic-electrolyte 5 solutions. Most of these revised activity coefficient models are based on an extension of the 6 UNIFAC concept. Erdakos et al. (2006) further developed these extended UNIFAC models. 7 Zuend et al. (2008) fitted the interaction parameters for the organic compounds (alcohols and polyols) and inorganic ions. AIOMFAC is based on the group-contribution model LIFAC 8 9 (Yan et al., 1999) and yet modified in many respects to better represent relevant species, 10 reference states, and the relative humidity range of the atmosphere. Recently, Zuend et al. (2011), Mohs and Gmehling (2013) and Ganbavale et al. (2015) proposed revised and 11 12 extended parameterizations for mixtures containing various organic functional groups, water 13 and inorganic ions. 14 Complex multiphase chemistry model dealing with deliquesced particles usually do neglect or roughly estimate the effect of solution non-ideality on the chemical processing (see, e.g., 15 16 Tilgner and Herrmann (2010); Bräuer et al. (2013); Mao et al. (2013); Tilgner et al. (2013); Guo et al. (2014)). However, model studies (e.g., Bräuer et al. (2013); Tilgner et al. (2013)) 17 18 implicated that deliquesced particles might be a potentially important medium for multiphase 19 chemistry. Thus, the present study was aimed at the implementation of solution non-ideality 20 in aqueous-phase reaction kinetics into the Spectral Aerosol Cloud Chemistry Interaction Model (SPACCIM, Wolke et al. (2005)). Accordingly, an activity module has to be 21 22 implemented in SPACCIM to provide appropriate activity coefficients for dissolved species. 23 The parcel model SPACCIM was originally developed for the dynamical description of 24 chemical and microphysical cloud processes. SPACCIM was successfully applied in several 25 process studies using the complex multiphase mechanism CAPRAM (Herrmann et al., 2005; Tilgner and Herrmann, 2010; Bräuer et al., 2013; Tilgner et al., 2013) 26 27 28

In this paper, we present an extended model approach for the kinetic description of phase transfer and complex multiphase chemistry considering the non-ideality of solutions by means of activity coefficient models. This paper split into 4 sections. In section 2, we described the implementation of solution non-ideality into the SPACCIM model. In subsequent subsections, the coupling between microphysics and multiphase chemistry models as well as the necessary adjustments of numerical schemes is discussed. In Sect. 2.3, the activity coefficient module is

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Gelöscht: (Bräuer et al., 2013; Tilgner et al., 2013)

Gelöscht: Ganbayale et al. (2015)

Gelöscht: proposed a revised and extended parameterization for mixtures containing various organic functional groups, plus water and inorganic ions. As this work incorporated the first set of parameterization from Zuend et al., 2008, and since the inorganic ions and organic functional groups are limited, we extended the interaction parameter dataset from mod. LIFAC (Kiepe et al., 2006). Since the large set of experimental data is required in order to fit the parameters, which is not focus of this study, we have taken the additional interaction parameters from mod. LIFAC and created a parameter matrix in order to estimate the activity coefficients in multicomponent mixture.

#### [1] verschoben (Einfügung)

Gelöscht: Attempts at realistic estimation of activity coefficients can be traced back to extensive literature for inorganic, organic and mixed inorganic-organic solutions (e.g., Prausnitz et al (1986): Pitzer (1991): Li et al. (1994): Yan et al. (1999); Ming and Russell (2002); Raatikainen and Laaksonen (2005); Topping et al. (2005a, 2005b); (Zaveri et al., 2005a); Erdakos et al. (2006); Clegg et al. (2008); Zuend et al. (2008); Zuend et al (2011)).Considerable effort has been devoted formerly to develop a number of thermodynamic models with reliable accuracy and efficiency to simulate aerosol thermodynamic equilibrium (e.g. AIM (Clegg et al., 1998b, a), GFEMIN (Ansari and Pandis, 1999a), ISORROPIA and ISORROPIA II (Nenes et al., 1998; Fountoukis and Nenes, 2007), EQSAM3 (Metzger et al., 2006; Metzger and Lelieveld, 2007), EQUISOLV II (Jacobson et al., 1996; Jacobson, 1997); MARS-A (Saxena et al., 1986; Binkowski and Roselle, 2003), MESA (Zaveri et al., 2005b); UHAERO (Amundson et al., 2006; Amundson et al., 2007)). Various numerical techniques were developed based on direct minimization of Gibbs free energy, which is highly accurate, yet computationally expensive (Ansari and Pandis, 1999a; Wexler et al., 2002). Most of these models assume that particles are in thermody ... [1]

Gelöscht: Pilinis et al. (2000)

Gelöscht: Zuend et al. (2011)

**Gelöscht:** ). Only very few model approaches exist so far, that treat dynamically gas-particle partitioning of inorganic and organic gases co...[2]

Gelöscht: Zaveri et al. (2008)

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[1] nach oben verschoben: Hence, the development of kinetic model frameworks for modeling of processes in multicomponent atmospheric particles, which include both a d\_...[5]

**Gelöscht:** Roldin et al. (2014)

Gelöscht: Ervens et al. (2011)

Gelöscht: ). However, such a kinetic model framework is needed to more precisely examine the role of concentrated aerosol solutions for the chemical processing of aerosol constitutes an \_\_\_\_\_[4]

Gelöscht: Wolke et al. (2005)

 introduced, that is specifically designed to treat multicomponent mixed organic-inorganic aerosol particles. Section 3 presents an evaluation of the currently implemented activity coefficient module in SPACCIM. In order to validate the model performance and the capability, the model results were compared with available measurements and other activity coefficient models such as mod. LIFAC (Kiepe et al., 2006), E-AIM (Clegg et al., 1998b, a), and AIOMFAC (Zuend et al., 2008). Furthermore, Sect. 3 presents sensitivity studies on the importance of the different interactions and first model results obtained with the new model framework.

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# 2 Methodology and model development

# 2.1 Multiphase model SPACCIM (original code)

12 In this section, a brief summary is provided for the methods used in SPACCIM original 13 code and the current limitations are outlined. The air parcel model SPACCIM was 14 developed for the description of simultaneously occurring chemical and physical processes in cloud droplets and deliquesced particles. Thus, SPACCIM combines a complex multiphase 15 16 chemistry model with a detailed cloud microphysics for a size-resolved particle/droplet 17 spectrum in a box model framework (Wolke et al., 2005). Depending on the used 18 microphysical model, external and internal mixing of aerosol can be taken into account. The 19 activation of droplets is explicitly described. Either the movement of the air parcel can follow 20 a predefined trajectory (e.g., simulated by a 3D atmospheric model) or the vertical velocity is calculated based on the parcel updraft compared to prescribed environmental conditions. 21 22 Entrainment and detrainment processes are considered in a parameterized form. The model 23 allows a detailed description of the processing of gases and particles shortly before cloud 24 formation, during the cloud life time and shortly after cloud evaporation (Sehili et al., 2005). 25 The droplet activation depending on the particle size and composition is explicitly described 26 (see Sehili et al. (2005) and Wolke et al. (2005)).

All microphysical parameters needed by the multiphase chemistry are taken over from the microphysical model. For this purpose, <u>a robust and efficient</u> coupling scheme between microphysical and multiphase chemical models is implemented. The coupling scheme <u>is</u> <u>adjusted to the applied time integration method and provides time-interpolated values of the microphysical parameters (temperature, water vapor, liquid water content) and time-averaged</u>

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- mass fluxes between different droplet classes caused by microphysical processes (e.g., by
- 2 aggregation, break up, condensation). Changes of the chemical aerosol composition by gas
- 3 scavenging and chemical reactions feed back on the microphysical processes (e.g., water
- 4 condensation growth rates via changes in the Raoult term). Consequently, related processes
- 5 <u>such as co-condensation (see Topping et al. (2013) for details) are considered in the model.</u>
- 6 The multiphase chemistry is performed for ideal solutions assuming well-mixed droplets.
- 7 Activity coefficients and the diffusion inside of the droplets are not considered. Dissociations
- 8 | are described dynamically as forward and backward reactions. The applied multiphase
- 9 chemical mechanism (including phase transfer data and kinetic reaction constants) is provided
- as an input file. Therefore, a high flexibility concerning changes in the chemical mechanism
- as an input me. Therefore, a night hexibinity concerning changes in the chemical mechanism
- or the replacement of the entire reaction system is guaranteed. For further details, the reader
- 12 is referred to the original publication by (Wolke et al., 2005). The performance of the model
- 13 was shown for both simple chemical mechanisms considering inorganic chemistry only and
- 14 for very complex mechanisms of the CAPRAM family, which contain a detailed description
- of the inorganic and organic chemistry (Herrmann et al., 2005; Tilgner and Herrmann, 2010;
- 16 Bräuer et al., 2013; Tilgner et al., 2013).

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- 17 In the published version of SPACCIM (Wolke et al., 2005), the influence of solution non-
- 18 ideality on multiphase processing was not considered. In fact, the assumption of an ideal
- 19 solution is not valid particularly for deliquescent particles, where highly concentrated
- 20 solutions are typical present. Accordingly, the chemical reaction terms in the aqueous phase
- 21 chemistry have to be modified by using the activities and therefore an activity coefficient
- 22 module has to be added. Furthermore, the feedback approach is enhanced by using the
- 23 calculated water activity for the Raoult term and by the consideration of surface tension
- 24 effects. The changes in the model code are given in the following subsection.

#### 2.2 Further development of SPACCIM

#### 26 2.2.1 Mass balance equations

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- 27 | For the consideration of solution non-ideality effects in SPACCIM, it is required that rate
- 28 expressions have to be written in terms of species activities, rather than mole fractions or
- 29 concentrations. The activity  $a_i$  of species i can be expressed by  $a_i = \gamma_i \cdot m_i = \gamma_i \cdot c_i / L$  where
- 30  $\gamma_i$  denotes the molality based activity coefficient,  $m_i$  the molality and  $c_i$  the mass

Gelöscht: used

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1 | concentration of an aqueous phase species i. The liquid water content  $\underline{L}$  is given as the water

mass in the corresponding box volume. In the proposed approach, the non-ideal behavior is

3 taken into account by means of activity coefficients. It should be emphasized that the activity

4 coefficient  $\gamma_i$  depends usually on the concentrations of all species dissolved in the solution.

5 In Eqs. (1) and (2), the mass balance equations of the modified version of SPACCIM

6 extended by the treatment of solution non-ideality are presented. In particular, the aqueous

concentrations in the original mass balance equations of the SPACCIM (see Eqs. (1) and (2)

8 in Wolke et al. (2005)) are replaced by corresponding activities.

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9 The description of both microphysical and multiphase chemical processes is performed for a

10 size-resolved particle/cloud droplet spectrum, which is subdivided into several classes

11 k = 1, ..., M. In each particle/droplet class,  $N_A$  aqueous phase species are treated, which are

12 not necessarily identical to the number of gas phase species  $N_G$ . In the parcel model

13 SPACCIM, the prognostic equations for the mass concentrations of a gas phase chemical

species  $c_{i}^{G}$  and an aqueous phase chemical species  $c_{i}^{k}$  in the  $k^{th}$  class have to take into

account the chemical productions and degradations, phase transfers, mass transport between

different classes caused by microphysical processes, and ent-/detrainment. These processes

can be described by the following mass balance equations:

$$18 \qquad \frac{d\left(c_{i^{*}}^{G}\right)}{dt} = \underbrace{R_{i^{*}}^{G}\left(t, c_{1}^{G}, ..., c_{N_{G}}^{G}\right)}_{\text{gas phase chemistry}} - \underbrace{\kappa_{i} \sum_{k} L_{k} k_{i}^{ki} \left[c_{i^{*}}^{G} - \frac{a_{i}^{k}}{H_{i}}\right]}_{\text{phase provefor}} + \underbrace{\mu \left[c_{i^{*}}^{G} - c_{ent}^{G}\right]}_{\text{outflow}}, \tag{2}$$

$$\frac{d(c_i^k)}{dt} = \underbrace{L_k R_i^A(t, a_1^k, ..., a_{N_A}^k)}_{aqueous\ phase\ chemistry} + \underbrace{\kappa_i L_k k_i^{ki} \left[c_i^G - \frac{a_i^k}{H_i}\right]}_{phase\ transfer} + \underbrace{F(c_i^1, ..., c_i^M)}_{mass\ transfer} + \underbrace{\mu \left[c_i^k - c_i^{k_{ent}}\right]}_{entrainment/outflow}, \tag{3}$$

20 with  $i^* = 1, ..., N_G$ ;  $i = 1, ..., N_A$ ; k = 1, ..., M.

In the above formulation,  $L_k$  denotes the liquid water content of the  $k^{th}$  droplet class inside

22 the box volume. The values  $a_i^k, k = 1, ..., M$ , represent the activities of species  $\underline{i}$  in the  $k^{th}$ 

23 liquid water fraction. The vector  $c^G$  stands for the concentrations of the gas phase species

and  $k_t^{ki}$  is the mass transfer coefficient. The chemical reaction terms of the corresponding

25 species are denoted by  $R_i^G$  and  $R_i^A$ . The second term on the right-hand side of the

Gelöscht: volume
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**Gelöscht:** volume fraction  $V_k/V_{box}$ 

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1 aforementioned equations describe the change of mass concentration of the soluble species

2 due to phase transfer between the gas phase and particle/cloud droplet classes. Hence, this

3 term will be referred to as the Henry term in the following. The value  $H_i$  denotes here the

dimensionless Henry's law coefficient for species  $\underline{i}$ . The prefactor  $\kappa_i$  of the Henry term is a

solubility index and defined to be equal to 1 as well as 0 for soluble and insoluble species,

respectively (see Wolke et al. (2005)). The term  $F(c_i^1, \dots, c_i^M)$  in Eq. (3) stands for the mass 6

7 transfer between different droplet classes by microphysical exchange processes (e.g. by

8 aggregation, break up, condensation). The time-dependent natural and anthropogenic

9 emissions as well as dry and wet deposition are parameterized in the last terms of the right

hand sides using a time dependent entrainment/detrainment rate  $\mu$ . One should note that, 10

above-mentioned mass balance equations are not only limited to "non-ideal" approach. 11

12 Whenever, the activity coefficients are defined as unity then this numerical model formulation

13 will reduce to the original version of SPACCIM.

#### 2.2.2 Reaction kinetics

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The first terms  $R_i^G$  and  $R_i^A$  in the right hand sides of the mass balance Eqs. (2) and (3) 15

comprise the chemical transformations (production and degradation fluxes). However, the 16

17 reaction term included in Eq. (2) is only a function of concentrations of gas phase species.

18 Since, the gas phase mixture is assumed to be behaving as an ideal gas phase mixture, the

19 non-ideality is not considered in this term.

20 Suppose, for an irreversible reaction  $A + B \rightarrow C + D$  in the aqueous phase, the reaction rate

21  $r_A$  can be written while considering the <u>solution</u> non-ideality as follows:

22 
$$r_A = -k_A \cdot [a_A] \cdot [a_B] = -k_A \cdot \gamma_A [A] \cdot \gamma_B [B],$$
 (4)

23 Here, the activities of A, B, C, and D are used instead of the concentrations. The activity of A

 $(a_A)$  is proportional to its molar concentration (either molality based or mole fraction based) 24

25 [A], where the proportional constant is the activity coefficient  $\gamma_A$  of that particular species.

The treatment of solution non-ideality was also considered for equilibrium reaction types, 26

27 which should be explained with the generic example shown as:

28 
$$v_C C + v_D D \rightleftharpoons v_A A + v_B B$$
. (5)

29 The relative quantities (i.e. thermodynamic activities) of reactants and products in an

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Gelöscht: /

1 equilibrium reaction are determined from the equilibrium relation,

$$2 \qquad \sum_{i} \left\{ a_{i} \right\}^{\lambda_{i} v_{i}} = \frac{\left\{ \mathbf{A} \right\}^{v_{A}} \cdot \left\{ \mathbf{B} \right\}^{v_{B}}}{\left\{ \mathbf{C} \right\}^{v_{C}} \cdot \left\{ \mathbf{D} \right\}^{v_{D}}} = \frac{\left( \gamma_{A}^{v_{A}} \cdot \left[ \mathbf{A} \right]^{v_{A}} \right) \cdot \left( \gamma_{B}^{v_{B}} \cdot \left[ \mathbf{B} \right]^{v_{B}} \right)}{\left( \gamma_{C}^{v_{C}} \cdot \left[ \mathbf{C} \right]^{v_{C}} \right) \cdot \left( \gamma_{D}^{v_{D}} \cdot \left[ \mathbf{D} \right]^{v_{D}} \right)} = K_{eq}, \tag{6}$$

- 3 where  $K_{eq}$  called as equilibrium coefficient,  $\{a_i\}$  is the thermodynamic activity of species i,
- 4 {A}, etc., are individual thermodynamic activities,  $\lambda_i = +1$  for products, and  $\lambda_i = -1$  for
- 5 reactants. As mentioned earlier, activity of a species A is its molality  $m_A$  multiplied by its
- 6 activity coefficient  $\gamma_A$ . A solute activity coefficient represents the deviation from ideal
- 7 behavior of the solute in solution. Hence, the concentration dependent activity coefficients are
- 8 estimated for all soluble species. Note, that the activity coefficients for neutral inorganic
- 9 species (such as  $O_{2(aq)}$ ) are defined as unity. At the same time, the activity coefficients of
- 10 radicals are also defined as unity, since their reactivity is quite fast and lifetime is rather
- 11 small. The consideration of activities in the SPACCIM framework for different types of
- species is summarized in Table 1.

#### 13 2.2.3 Phase transfer processes

- 14 The dynamical description of phase transfer processes between the gas and liquid phases in
- 15 SPACCIM is specified according to the Schwartz approach (Schwartz, 1986). During
- dissolution, the saturation vapor pressure of gas A can be determined from the equilibrium
- 17 relationship  $A_{(g)} \rightleftharpoons A_{(aq)}$ . Thus, in terms of an arbitrary gas i the Henry's law is defined as:

18 
$$p_{i,k}^s = \frac{m_i^k}{K_i^H},$$
 (7)

- where  $p_{i,k}^s$  is the saturation vapor pressure (atm) of gas phase species i over a particle in size
- bin k,  $m_i^k \pmod{kg^{-1}}$  is the molality of dissolved gas phase species i in particle class k, and
- 21  $K_i^H \text{ (mol kg}^{-1} \text{ atm}^{-1}\text{)}$  is the corresponding Henry constant. It has to be noted here that the
- 22 Henry's law constants of an aqueous solution depend on the composition of the aqueous
- 23 solution, e.g., on the electrolyte identity of the solution (ionic strength, etc.). Non-ideal
- 24 electrolyte solutions are able to both suppress the uptake ("salting-out") and enhance the
- 25 uptake ("salting-in") of soluble gases compared to value for pure water uptake (Herrmann et
- al., 2015). These salting effects can be quantitatively described by the Setschenow equation

1 (Sander, 2015). However, as reported in the review of Sander (2015), there are unfortunately

2 only limited data available. Therefore, salt effects are only considered in the SPACCIM

3 model due to the consideration of the activity coefficients in the uptake calculation. The

4 model results should be therefore treated with caution particularly at higher ionic strengths of

the solution due to the lower range of functionality of Henry's law coefficients compared to

6 the applicability range of present activity coefficient models.

7 The above-mentioned saturation vapor pressure is related to the saturation vapor mole

8 concentration  $c_{i,k}^{s}$  (mol m<sup>-3</sup>) by

$$9 p_{i,k}^s = c_{i,k}^s RT, (8)$$

where R denotes the universal gas constant in  $(atm m^3 mol^{-1} K^{-1})$  and T(K) the temperature.

11 Then, Eq. (7) can be expressed in terms of concentrations rather than molalities and partial

12 pressures as:

5

13 
$$c_{i,k}^{s} = \frac{p_{i,k}^{s}}{RT} = \frac{m_{i}^{k}}{K_{i}^{H}RT} = \frac{m_{i}^{k}}{H_{i}}.$$
 (9)

14 Here  $H_i = K_i^H RT$  stands for the dimensionless Henry constant. Considering the <u>solution</u> non-

15 ideality in the aqueous phase, the molalities  $m_i^k$  are replaced by the activities  $a_i^k = \gamma_i^k m_i^k$ .

16 Considering M classes of particles associated, we state the appropriate expression for gas-

phase loss while neglecting the Kelvin effect (following Jacobson (1997)):

$$18 \qquad \frac{dc_i^G}{dt} = -\sum_k k_i^{ki} L_k \left( c_i^G - \frac{a_i^k}{H_i} \right). \tag{10}$$

19 Eq. (10) pertains to the case of a single gas phase species equilibrating between the gas and

aqueous aerosol phases, with the mass transfer coefficient  $k_t^{ki}$  defined by

21 
$$k_t^{ki} = \left(\frac{r_k^2}{3D_i^G} + \frac{4r_k}{3v_i\alpha_i}\right),$$
 (11)

which depends on the droplet size  $r_k$ , the gas diffusion coefficient  $D_i^G$ , the molecular speed  $v_i$ 

23 and the mass accommodation coefficient  $\alpha_{i}$  of the  $i^{th}$  species. These quantities play a

24 decisive role in determining the rate of uptake of gaseous species by, and evaporation from

Gelöscht: On the other hand, the

- 1 aerosol particles, respectively, governing the timescale for a droplet to attain an equilibrium
- 2 (Schwartz, 1986).

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#### 2.2.4 Coupling scheme

- 4 The coupling between microphysics and multiphase chemistry models in SPACCIM follows
- 5 the so-called "operator splitting" technique. As described in Sehili et al. (2005), the coupling
- 6 scheme provides time-interpolated values of the meteorological variables (temperature, water
- 7 vapor, liquid water content) and generates the time-averaged mass fluxes F over the coupling
- 8 time interval. The changes in the chemical aerosol composition by gas scavenging and the
- 9 chemical reactions have a continuous feedback on the microphysical processes (e.g. water
- 10 condensation growth rates via changes in surface tension and the Raoult term/water activity).
- 11 For the "non-ideal" approach in SPACCIM, the coupling scheme is modified, since activity
- 12 coefficients have to be considered in both models. At the same time, the activity coefficients
- 13 are repeatedly required to compute the chemical transformations and the phase transfer terms
- 14 (see Sect. 2.2.2 and 2.2.3). Furthermore, the modified activity coefficients as well as the
- parameterized surface tension are delivered back to the microphysical model. Fig. 1 illustrates
- 16 this coupling strategy between microphysical and multiphase chemistry model as well as their
- 17 interexchange while considering non-ideal solutions and surface tension effects (see Sect.
- 18 2.2.6). The coupling strategy enables a continuous feedback of the multiphase chemistry on
- 19 the microphysical processes such as water condensational growth. The two models run
- separately and exchange information at every coupling time step (see Fig. 2). Moreover, both
- 21 widely separated operating models use its individual time-step control. This is necessary in
- 22 order to ensure a high flexibility regarding the usage of models with different complexities
- and numerical efficiency. The coupling between both models and the activity coefficient
- 24 module utilize well-defined interfaces for the intercommunication of codes while considering
- 25 the aqueous phase chemistry in non-ideal solutions. Furthermore, the interpolation and
- 26 averaging of the required meteorological variables and parameters are arranged and
- implemented in the same way as described in Wolke et al. (2005).

# 2.2.5 Feedback of non-ideal aqueous phase chemistry on microphysics

- 29 Microphysical processes described in SPACCIM include equilibrium growth of aerosol
- 30 particles and condensational growth of the droplets (Simmel and Wurzler, 2006). The Köhler
- 31 equation (see e.g., Köhler (1936); Pruppacher and Klett (1997)) gives the saturation ratio of

1 water vapor at particle/air interface, which depends on the chemical composition, the droplet 2 diameter and the surface tension of the particle. In SPACCIM, the non-linear relationship 3 Eq. (1) is used to determine the equilibration of water between the liquid and surrounding 4 vapor phase for non-activated particles. The water saturation pressure in Eq. (1) is affected by 5 the curvature of the particle (also known as Kelvin effect) and the water activity, which is 6 determined by the solutes (Raoult effect). Previously, Wolke et al. (2005) calculated the 7 Raoult term in the condensation rate using osmotic coefficient, according to Pruppacher and 8 Klett (1997). While, the intension was to allow the feedback of chemical particle composition 9 onto microphysics, the Raoult term was replaced by the sum of molar ratios of all soluble 10 species included in the multiphase system:

11 
$$Raoult_{chem}^{k} = \frac{\sum_{i}^{N_A} mol_{sol_i}^{k}}{mol_{w}^{k}}.$$
 (12)

Here, the quantities  $mol_{sol_i}^k$  of soluble material are obtained from the multiphase chemistry.

13 The molar water fraction  $mol_w^k$  varies and is taken directly from the microphysics. The Raoult

14 term in Eq. (12) depends on all soluble species. In the non-ideal approach of SPACCIM, the

water activity  $a_w^k$  estimated from activity coefficient module (see Sect. (2.3)), is used directly

for the Raoult term in microphysics. On the other hand, the description of change in droplet

curvature (Kelvin effect) is treated with surface tension approaches (see Subsect. 2.2.6).

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Both effects are <u>influenced</u> by the particle composition, which is continuously changed by phase transfer and multiphase processes. However, the mass concentrations of all species are kept fixed for the microphysics over a coupling time step (see Fig. 1). But the molalities and, therefore, the Kelvin and Raoult terms are changed caused by the adjustment of the <u>liquid</u> <u>water content</u>, Eq. (1) has to be fulfilled simultaneously for all non-activated particle classes. The droplet activation is described explicitly and takes place for all particles, which grow

over the critical radius. The condensation and evaporation of the activated droplet classes are described dynamically. The predicted saturation vapor pressure is used as input into the droplet growth equation. The coupled system for all classes has to be solved simultaneously,

whereas the total amount of water (liquid or gaseous) is prescribed. This leads to a nonlinear

system, which has to be solved iteratively at each microphysical time step. A more detailed

description of the iterative procedure is given in Simmel and Wurzler (2006). A new solution

of the system is obtained, and defines the equilibrium saturation ratio and the corresponding

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Gelöscht: LWCs

particle/droplet diameters. This implies changes in the corresponding liquid water contents

- and, hence, in the molalities. Consequently, the water activity and the surface tension have to
- 3 be recalculated at each microphysical time step. A description of the equilibration algorithm is
- 4 presented schematically in Fig. 2. Based on this, SPACCIM allows an ongoing feedback of
- 5 the chemical particle composition onto microphysics. Conversely, the microphysical model
- 6 provides all microphysical variables for integrating the multiphase chemical system, such as
- 7 |  $\underline{\text{liquid water content}}$ , T and the mass fluxes F at the coupling time step (see Fig. 1).

#### 2.2.6 Surface tension

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9 Surface-active substances present at the interface and organic compounds dissolved in the

10 solution can significantly influence the surface tension and thus can affect cloud droplet

11 activation and hygroscopic growth (Shulman et al., 1996; Facchini et al., 2000; Tuckermann

12 and Cammenga, 2004; Topping et al., 2007; Prisle et al., 2012). A reduction of surface

tension in atmospheric cloud and fog water samples was highlighted in several studies (e.g.,

Facchini et al. (1999); Facchini et al. (2000); Mircea et al. (2002); Nenes et al. (2002)).

Furthermore, Henning et al. (2005) and Svenningsson et al. (2006) measured a surface tension

16 lowering for organic mixtures in laboratory studies. On the other hand, Sorjamaa et al. (2004)

and Sorjamaa and Laaksonen (2006) pointed out that surface-active substances can enrich at

18 the particle/droplet surface.

A first specific relationship between water-soluble organic aerosol concentration and surface

tension has been derived by fitting the equation of Szyszkowski-Langmuir to Po Valley fog

data (Facchini et al., 1999). Model approaches that can estimate the surface tension of

22 inorganic, organic systems and mixed inorganic/organic systems were proposed by Topping

et al. (2007). Recently, sophisticated parameterizations were developed for modeling the

combined effects of both bulk-surface partitioning and surface tension on cloud droplet

activation of organic aerosols (Topping (2010); Prisle et al. (2011); Raatikainen and

26 Laaksonen (2011)). However, Prisle et al. (2012) suggested neglecting the surfactant effects

instead of employing the numerical parameterizations calculating the reduction of surface

28 tension.

29 Since the present paper is aimed at the treatment of solution non-ideality in a multiphase

chemistry model framework, the model development considered the influence of surface

tension on droplet activation, as a first step, with more simplified parameterizations of

Gelöscht: LWC

Gelöscht: LWC

- Facchini et al. (1999) and Ervens et al. (2004) only. The implementation of more advanced approaches in SPACCIM will be subject of future development efforts.
- In the present work, the following relationship proposed by Facchini et al. (1999) was implemented in the SPACCIM framework:
- 5  $\sigma_{w,s}^{k} = \sigma_{w}^{k} 0.01877 \cdot T \cdot \ln(1 + 628.14 \cdot [C^{k}]),$  (13)
- 6 where T is the temperature in K and  $C^k$  represents the concentration of WSOC (Water
- 7 | Soluble Organic Carbon, mol C  $L^{-1}$ ) in particle class k. In addition, a combined approach for
- 8 accounting for a simultaneous change in  $\sigma_{w,s}^k$  and the mean molar mass of solute  $M_{sol}$  derived
- 9 by Ervens et al. (2004) was also implemented in the present work:
- 10  $\sigma_{w,s}^k = \sigma_w^k 0.01877 \cdot T \cdot \ln(1 + 628.14 n_c c_{sol}^k),$  (14)
- 11 where  $c_{sol}^k$  is the solute concentration in (mol L<sup>-1</sup>) and  $n_{cb}$  represents the number of carbon
- 12 atoms defined by
- 13  $n_{cb} = \frac{M_{sol}}{2.2M_c}$ , (15)
- 14 | with  $M_c = 12 \text{ g mol}^{-1}$ .

15

- 2.2.7 Adjustment of numerical schemes
- 16 In order to treat aqueous phase chemistry considering newly solution non-ideality effects, the
- 17 numerical schemes used in Wolke et al. (2005) are required to adjust, mainly, (i) the time
- 18 integration scheme, (ii) the computation of Jacobian matrix and (iii) the sparse linear solver.
- 19 The system of mass balance equations (Eqs. (2) and (3)) is integrated in an implicit and
- 20 coupled manner by higher order backward differential formula (BDF) schemes (e.g., Hairer et
- 21 al. (1993)). In any implicit multistep method, the main computational task is the solution of a
- 22 non-linear equation of the form:
- 23  $\mathbf{F}(\mathbf{c}^{n+1}) = \mathbf{c}^{n+1} \mathbf{X}^{\mathbf{n}} \beta \Delta t_n \mathbf{f}(t_{n+1}, \mathbf{c}^{n+1}) = 0 ,$  (16)
- 24 where  $\mathbf{f}(t_{n+1}, \mathbf{c}^{n+1})$  stands for the right hand side of Eqs. (2) and (3),  $\beta > 0$  is a parameter of

**Gelöscht:** The calculation of droplet solution surface tension  $\sigma_{w,s}$  with simultaneous changes in solute concentration  $c_{sol}$  is almost a linear approximation:

Gelöscht: Facchini et al. (1999)

Gelöscht: , was implemented in SPACCIM ... [9]

**Gelöscht:** Ervens et al. (2004)

**Gelöscht:** was also implemented in the present work:

the integration method and  $X^n$  is a linear combination of previous values. If equation (10) is

solved by a Newton-like method, the main burden is the approximate solution of linear

3 systems of the form:

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$$4 \quad \left( \mathbf{I} - \beta \Delta t \mathbf{J} \right) \Delta \mathbf{c} = \mathbf{b} \tag{17}$$

where I denotes the identity matrix and  $\Delta t$  represents the time step size. The matrix  $\mathbf{J}$  stands

6 for an approximation of the Jacobian  $\partial \mathbf{f}(t,c)/\partial \mathbf{c}$  of the right hand side of the ordinary

differential equation (ODE) system. The vector **b** is given as:

$$\mathbf{b} = \mathbf{c}^{\mathbf{n}} - \mathbf{X}^{\mathbf{n}} - \beta \Delta t_n \, \mathbf{f} \left( t_n, c^n \right) \tag{18}.$$

9 Usually, the dimension of the linear system Eq. (17) is rather high. Large systems can be

10 solved with reasonable effort by iterative or direct sparse solvers, which utilize the special

structure of the system (sparsity, block structure, different types of coupling). Such efficient

12 solvers are already developed and applied in the former version of SPACCIM for the "ideal"

approach (see Wolke and Knoth (2002); Wolke et al. (2005) for further details).

14 In this case, the Jacobian structure of the right-hand side of the multiphase system (Eq. (2)

and Eq. (3)) for two droplet classes is shown in Fig. 3. As can be seen, the dots are usually

16 non-zero entries means that the species in the row depends on the species in the column. The

17 diagonal elements of the Jacobian describe the dependence from the species itself. These

entries can be caused by chemical reactions and phase transfer, but also by the terms from

19 microphysical fluxes and entrainment.

20 The block structure shown in Fig. 3 can be explained as follows: the blocks in the diagonal

correspond to the Jacobian of the gas phase and aqueous phase reaction terms, respectively.

The upper left block (light blue) represents the gas phase. The other two diagonal blocks

23 (blue) are related to the aqueous phase chemistry attained to have the same sparse structure.

24 The left and upper boundary blocks (green) represent the phase interchange between gas

phase species and corresponding aqueous phase species in each class, according to (Schwartz,

1986). The orange diagonal matrices include the coupling terms resulting from the mass

transfer between liquid species and the corresponding species in the other classes. These

28 sparse block matrices are generated explicitly and stored in sparse form. The linear system

29 (see Eq. (18)) is solved by a sparse LU decomposition with diagonal pivoting. An optimal

30 order of the pivot elements to avoid fill-in is determined by an adjusted Meis-Markowitz

Gelöscht: 7

Gelöscht: 8

Gelöscht: J

Gelöscht: b

Gelöscht: 9

Gelöscht: 8

- 1 strategy (Wolke and Knoth, 2002). In fact, only an appropriate approximation of the Jacobian
- 2 is required to ensure the convergence of the Newton-like method for the corrector iteration
- 3 (Eq. (17)). Therefore, the sparse factorization is stored and has to be performed only when the
- 4 Jacobian *J* is recomputed.
- 5 The adjusted numerical scheme works robust and very efficient for the "ideal" case. But these
- 6 effective approaches can only be used in the "non-ideal" case, if the special sparse and block
- 7 structure can be largely preserved. The calculation of the Jacobian has to be performed by
- 8 applying the "chain rule" for the aqueous phase reaction and mass transfer terms in the model
- 9 equations Eq. (2) and Eq. (3). These terms depend on the activities instead of the molalities in
- difference to the ideal case. While the "outer" derivatives are unchanged, the "inner"
- derivatives have to be modified. In case that  $c^k$  is the vector of all concentrations and  $L^k$  the
- liquid water content in the  $k^{th}$  droplet class, the gradient with respect to vector  $\mathbf{c}^{\mathbf{k}}$  is denoted
- 13 a

14 
$$\nabla_{\mathbf{c}^{\mathbf{k}}} = \left(\frac{\partial}{\partial \mathbf{c}_{1}^{\mathbf{k}}}, \dots, \frac{\partial}{\partial \mathbf{c}_{N_{\mathbf{k}}}^{\mathbf{k}}}\right).$$
 (19)

- 15 In the ideal approach the molalities depend only on the corresponding species itself. Then the
- 16 gradient of the molalities is given as follows:

17 
$$\nabla_{\mathbf{c}^k} m_j^k \left( c_j^k \right) = \frac{1}{L^k} (0, ..., 0, 1, 0, ..., 0)$$
 (20)

- In the above formulation, the gradient has only one entry in the  $j^{th}$  position, which conserves
- 19 the structure of the "outer" Jacobian. Contrary, while applying the chain rule, the gradient for
- 20 non-ideal solutions would be:

21 
$$\nabla_{c^k} a_j^k \left( \mathbf{c^k} \right) = \frac{c_j^k}{L_k} \cdot \left( \nabla_{c^k} \gamma_j^k \left( \mathbf{c^k} \right) \right) + \frac{1}{L_k} \cdot (0, \dots, 0, \gamma_j^k, 0, \dots, 0)$$
(21)

- where the gradient  $\nabla_{k}(\gamma_{i}^{k}(\mathbf{c}^{k}))$  of activity coefficients depends usually on all concentrations
- of the vector  $\mathbf{c}^{\mathbf{k}}$  considered in the activity calculations.
- 24 The first term in Eq. (21) is a vector with entries in several positions depending on the activity
- 25 coefficient module. This leads to "fill-in" in the corresponding lines of the Jacobian from
- 26 aqueous phase chemistry (blue blocks) and the phase transfer terms (green blocks).

Gelöscht: 20

Gelöscht: 8

Gelöscht: 1

Gelöscht: 2

- 1 Consequently, the efficient direct sparse solvers are used in SPACCIM for the linear system
- 2 cannot be utilized. However, since only a "good" approximation for the Jacobian is needed,
- 3 | the first term shown in Eq. (21) is omitted assuming that the dependency of the activity
- 4 coefficients from the concentrations can be neglected over the time step. The second term
- 5 involves the activity coefficient  $\gamma_i^k$  that yields from the derivative of the activity with respect
- 6 to molality of that particular species  $m_i$ . Although, the derivative of activity coefficients is
- 7 omitted, the same data structures are obtained as in ideal case. The second term on the right
- 8 | hand side of Eq. (21) has the same structure as on the right hand side of Eq. (20). Only the
- 9 non-zero entry in the  $j^{th}$  position changes from 1 to  $\gamma_i^k$ . This leads to modifications of the
- 10 non-zero entries in the Jacobians of the chemistry (blue blocks) and the phase transfer (green
- blocks) terms. However, the sparse structure of the systems is conserved effectively.

# 2.3 SPACCIM's activity coefficient module

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A main task in the extended approach (Fig. 2) is to provide appropriate activity coefficients for the solved species. Therefore, several suitable activity models have been tested and compared regarding their suitable applicability in order to achieve the above-mentioned objective. (see Subsect. 3.1). Overall, AIOMFAC seems to be most qualified for the aimed applications. Therefore, the implementation of the related module SpactMod was performed by using the theoretical framework and the available parameters of Zuend et al. (2008). The AIOMFAC was originally developed for systems composed of organic compounds with -CH<sub>n</sub> (n = 0,1,2,3) and -OH as functional groups. On the other hand, several authors (e.g., Gilardoni et al. (2009); Liu et al. (2009); Russell et al. (2009); Takahama et al. (2011)) reported that other individual organic compounds and compound classes have also a strong impact on multiphase chemical processing on ambient aerosols for instance, aldehydes, ketones, carboxylic acids, and multifunctional organic compounds. Moreover, the aforementioned organic compound classes are almost omnipresent in tropospheric aerosol particles and, therefore, explicitly treated in complex multiphase chemistry mechanism such as CAPRAM (see e.g., Herrmann et al. (2005); Tilgner et al. (2013). Hence, the prediction of the activity coefficients for complex multi-component aerosols, composed of various organic functional groups and electrolytes dissolved in water is the primary purpose of SpactMod. In order to treat various aerosol constituents, additional parameters were included from the mod. LIFAC approach of Kiepe et al. (2006), which can be rewritten in the AIOMFAC formalism (see

Gelöscht: 2

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Gelöscht: 1

Gelöscht: Ultimately

**Gelöscht:** In this section, we present the mixedsolvent electrolyte model that is designed to predict the activity coefficients, based mainly on AIOMFAC (Zuend et al., 2008), which is valid for systems over a wide concentration range. Appendix A1) and incorporated without new parameter fitting. A compilation of the

2 SpactMod parameters is given in Tables A1-A6. The differences to AIOMFAC are

3 highlighted.

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# 4 2.3.1 Model treatment of solution non-ideality

5 The development of thermodynamic models for mixed-solvent electrolyte systems was an

6 active area of research during the last three decades. In general, these models contain several

7 contributions to describe the system non-ideality, that define the excess Gibbs energy

8  $G^{ex}(p,T,n_i)$ :

9 
$$G^{ex}(p,T,n_j) = G_{LR}^{ex} + G_{MR}^{ex} + G_{SR}^{ex},$$
 (22)

where  $G_{LR}^{ex}$  represents the long-range (LR) electrostatic interactions,  $G_{SR}^{ex}$  is the short-range

11 (SR) contribution resulting from dipole ↔ dipole and dipole ↔ induced dipole interactions,

12 and an additional term (middle-range, MR)  $G_{MR}^{ev}$ , which accounts for ionic interactions (e.g.,

ion  $\leftrightarrow$  ion, ion  $\leftrightarrow$  dipole, ion  $\leftrightarrow$  induced dipole interactions), p is the total pressure, T the

absolute temperature, and  $n_i(j=1,...,N)$  the number of moles of component j in a system.

Accordingly, the corresponding activity coefficient  $\gamma_j^k$  of a species j with amount of moles  $n_j$ 

in the mixture are derived from expressions for the different parts of  $G^{ex}$  using the relation:

17 
$$\ln \gamma_j = \left(\frac{\partial G^{ex}/RT}{\partial n_j}\right)_{p,T,n_{fei}},$$
 (23)

where R is the universal gas constant. Correspondingly, the activity coefficients are calculated

19 from the aforementioned three different contributions:

$$20 \qquad \ln \gamma_j = \ln \gamma_j^{LR} + \ln \gamma_j^{MR} + \ln \gamma_j^{SR}. \tag{24}$$

2.3.2 The long-range contribution

The LR interactions described as they are in original AIOMFAC, based on the Debye-Hückel

theory (Debye and Hückel, 1923). In contrast to other works Li et al. (1994); Yan et al.

24 (1999); Chang and Pankow (2006), AIOMFAC uses the water properties for all solvent

25 components for density and dielectric constant of the solvent mixture, instead of using mixing

26 rules. With this assumption, the corresponding LR activity coefficient expressions for the

**Gelöscht:** the model interaction parameters were extended based on the activity coefficient model of mod. LIFAC (Kiepe et al., 2006), while using the mathematical model expressions according to

Gelöscht: Zuend et al. (2008

Gelöscht: . Thus, SpactMod allows a reliable prediction of activity coefficients of the considered organic-electrolyte mixture, flexibly, from these two approaches AIOMFAC (Zuend et al., 2008) and modified LIFAC (Kiepe et al., 2006), within a single model framework. The two different frameworks including the estimated interaction parameters are described in detail in

Gelöscht: Zuend et al. (2008)

Gelöscht: and

Gelöscht: Kiepe et al. (2006)

**Gelöscht:** , therefore, only main features are discussed here.

Gelöscht: 3

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**Gelöscht:** are described same as original AIOMFAC

1 solvents and ions are defined according to Zuend et al. (2008) as

$$2 \left[ \ln \gamma_s^{LR(x)} = \frac{2AM_s}{b^3} \left( 1 + b\sqrt{I} - \frac{1}{1 + b\sqrt{I}} - 2\ln(1 + b\sqrt{I}) \right),$$
 (25)

Gelöscht: 6

$$3 \qquad \ln \gamma_i^{LR,(x),\infty} = \frac{-z_i^2 A \sqrt{I}}{1 + b \sqrt{I}}.$$

Gelöscht: 7

(26)

4 Eq. (26) gives the activity coefficient of ion i in the mole fraction basis (x) with the reference

Gelöscht: 7

- state of infinite dilution in water, indicated by super script  $\infty$ .  $M_s$  represents the molar mass
- of solvent s and  $z_i$  is the number of elementary charges of ion i. The ionic strength
- 7  $I \text{ (mol kg}^{-1})$  is given as

$$8 I = \frac{1}{2} \sum_{i} m_{i} z_{i}^{2} (27)$$

Gelöscht: 8

9 with the Debye-Hückel parameters:

10  $A = 1.327757 \cdot 10^5 \cdot \frac{\sqrt{\rho_w}}{(\varepsilon_w T)^{\frac{3}{2}}},$  (28)

Gelöscht: 9

 $b = 6.359696 \cdot \sqrt{\frac{\rho_w}{(\varepsilon_w T)}}$  (29)

Gelöscht: 30

Gelöscht: of

- The Debye-Hückel parameters  $A(kg^{1/2} \text{ mol}^{-1/2})$  and  $b(kg^{1/2} \text{ mol}^{-1/2})$  depend on temperature T
- 13 (K), density  $\rho_w$  (kg/m<sup>3</sup>) and static permittivity  $\varepsilon_w$  (C<sup>2</sup>J<sup>-1</sup> m<sup>-1</sup>) of water, calculated based on
  - a distance of closest approach between ions (see Demaret and Gueron (1993); Antypov and
- 15 Holm (2007)).

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- Moreover, this simplification to a water-property based expression for LR activity coefficients
- 17 are favorable, due to the uncertainties to estimate unknown dielectric constants of certain
- organic compounds and maintaining the thermodynamic consistency regarding the selection
- 19 of reference states (see Raatikainen and Laaksonen (2005); Zuend et al. (2008)). In a real
- 20 mixture, solvents have densities and dielectric properties different from those of pure water.
- 21 For this reason, these simplifications of the LR part were made in other mixed solvent models
- 22 in chemical engineering and technical chemistry applications (see Iliuta et al. (2000)). The
- 23 uncertainties occurred due to the adopted assumptions to derive the LR and SR activity
- 24 coefficients with respect to approximations of parameters, were described in the semi-

Gelöscht: Compensation of these inaccuracies is controlled by this simplification, in the semi-empirical MR part as performed in original AIOMFAC (Zuend et al., 2008)

## 2 2.3.3 The Middle-range contribution

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- 3 The  $G_{MR}^{ex}$  term is the contribution of the indirect effects of the ionic interactions such as ion
- $4 \longleftrightarrow dipole$  interactions and ion  $\longleftrightarrow$  induced dipole interactions to the excess Gibbs energy. For
- 5 any mixture containing  $n_k$ , (k=1,...,s) moles of solvent k (main groups of organics and
- 6 water) and  $n_i$  moles of ion i,  $G_{MR}^{ex}$  can be expressed as described by Zuend et al. (2008):

$$\frac{G_{MR}^{ex}}{RT} = \frac{1}{\sum_{k} n_{k} M_{k}} \sum_{k} \sum_{i} B_{k,i}(I) n_{k} n_{i} 
+ \frac{1}{\sum_{k} n_{k} M_{k}} \sum_{c} \sum_{a} B_{c,a}(I) n_{c} n_{a} 
+ \frac{1}{\sum_{k} n_{k} M_{k}} \sum_{c} \sum_{a} C_{c,a}(I) n_{c} n_{a} \sum_{i} \frac{n_{i} |z_{i}|}{\sum_{k} n_{k} M_{k}} 
+ \frac{1}{\sum_{k} n_{k} M_{k}} \sum_{c} \sum_{c \geq c} R_{c,c'}(I) n_{c} n_{c'} 
+ \frac{1}{\left(\sum_{k} n_{k} M_{k}\right)^{2}} \sum_{c} \sum_{c' \geq c} \sum_{a} Q_{c,c',a} n_{c} n_{c'} n_{a}$$
(30)

8 where  $n_c$  and  $n_{c'}$  are the moles of cations,  $n_a$  are the moles of anions, and I is the ionic

9 strength as defined in Eq. (27).  $B_{k,i}(I)$  (kg mol<sup>-1</sup>) and  $B_{c,a}(I)$  (kg mol<sup>-1</sup>) are ionic strength

dependent binary interaction coefficients between solvent main groups and ions, and between

11 cations and anions, respectively.  $C_{c,a}(I)$  (kg<sup>2</sup> mol<sup>-2</sup>) are interaction coefficients between

12 cation ↔ anion pairs with respect to the total charge concentration. The coefficients

13  $R_{c,c'}(I)$  (kg mol<sup>-1</sup>) and  $Q_{c,c',a}(I)$  (kg<sup>2</sup> mol<sup>-2</sup>) are defined as binary and ternary interactions

14 involving two different cations. These binary and ternary interaction coefficients have been

introduced in AIOMFAC to improve the description of various ion combinations, specifically

16 at high ionic strength. Hence, these two terms in Eq. (30) can be vanished or neglected in

other cases, i.e. for low to moderate ionic strengths.

18 In the current approach, the MR terms of activity coefficients for the species and organic

19 | functional groups described in AIOMFAC are estimated using Eq. (30). As mentioned earlier,

Gelöscht: 8

Gelöscht: 1

Gelöscht: 1

1 the first three interaction coefficients in Eq. (30) are parameterized as functions of ionic

2 strength *I*, which are similar to the ones used for the Pitzer model of Knopf et al. (2003):

$$B_{k,i}(I) = b_{k,i}^{(1)} + b_{k,i}^{(2)} \exp(-b_{k,i}^{(3)} \sqrt{I}), \tag{31}$$

4 
$$B_{c,a}(I) = b_{c,a}^{(1)} + b_{c,a}^{(2)} \exp(-b_{c,a}^{(3)}\sqrt{I}),$$
 (32)

5 
$$C_{c,a}(I) = c_{c,a}^{(1)} \exp(-c_{c,a}^{(2)} \sqrt{I}),$$
 (33)

where  $b_{k,i}^{(1)}, b_{k,a}^{(2)}, b_{c,a}^{(1)}, b_{c,a}^{(2)}, c_{c,a}^{(1)}$  and  $c_{c,a}^{(2)}$  are adjustable parameters, which are determined by 6 7

fitting AIOMFAC activity coefficients to experimental data sets (see Zuend et al. (2008) for

further details). The parameter  $b_{ca}^{(3)}$  was used mostly to describe aqueous salt solutions 8

assuming a fixed value of 0.8  $kg^{\frac{1}{2}}$  mol<sup>\frac{1}{2}</sup>. Similarly, we have considered the same value for 9

10 the ions when the activity coefficients are estimated from AIOMFAC. Furthermore, Zuend et

al. (2008) argued that for such cases, where this value did not result in a satisfactory data fit,

 $b_{c,a}^{(3)}$  allow to vary. On the other hand, the parameter  $b_{k,i}^{(3)}$  was fixed for all mixed organic-

inorganic solutions assuming a value of 1.2 kg½ mol½. All interaction coefficients in the MR 13

part are symmetric  $B_{c,a}(I) = B_{a,c}(I)$ . Subsequently, water is defined as the reference solvent

for inorganic ions, no explicit ion  $\leftrightarrow$  water interactions are determined, i.e.,  $B_{k=H,O,i}(I)$  is

prescribed as zero for all inorganic ions. However, the effects of solution non-ideality from

cations and anions interacting with water molecules are indirectly accounted for via the cation

 $\leftrightarrow$  anion interaction coefficients,  $B_{c,a}(I)$ ,  $C_{c,a}(I)$ ,  $R_{c,c'}$  and  $Q_{c,c',a}$  as the corresponding

interaction parameters, that were determined on the basis of (organic-free) aqueous electrolyte

20 solutions.

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21 As depicted earlier, the MR interaction parameters in AIOMFAC were fitted for limited

22 organic compounds (i.e. alkyl and hydroxyl) and ions. Contrary, interaction parameters were

23 not evenly available for over all systems of current interest, i.e. to treat the organic

24 compounds and ions involved in multiphase mechanism such as CAPRAM. Hence, in this

25 study, the ion ↔ ion and organic main group ↔ ion interaction parameter database is

26 extended by incorporating parameters of the modified LIFAC approach of Kiepe et al. (2006).

27 The complete procedure of the extension of model interaction parameters is explained in

Appendix A.1.

Gelöscht: 1

Gelöscht: 2

Gelöscht: 3

## 2.3.4 The short-range contribution

- The SR contribution  $\ln \gamma_{SR}^{ex}$  to the total Gibbs excess energy in SpactMod is represented by the
- 3 modified group-contribution method UNIFAC (Fredenslund et al., 1975), as performed by
- 4 Zuend et al. (2008). AIOMFAC incorporates the revised parameter set of Hansen et al. (1991)
- 5 (standard UNIFAC) for most of the functional group interactions. Besides, these
- 6 modifications include the insertion of further inorganic ions to account for their effects on the
- 7 thermodynamic properties such as entropy and enthalpy of mixing apart from their charge-
- 8 related interactions (Li et al., 1994; Yan et al., 1999; Zuend et al., 2008). AIOMFAC utilizes
- 9 the specific UNIFAC parameterizations of Marcolli and Peter (2005) for hydroxyl and alkyl
- 10 functional groups.

1

- 11 Similar to the addition of interaction parameters derived for MR part, the same functional
- groups are also<u>included</u> in the SR part, while maintaining the compatibility with the
- 13 mathematical model expressions proposed in AIOMFAC. As Zuend et al. (2008), we used the
- 14 UNIFAC parameterizations of Marcolli and Peter (2005), which are adopted from Hansen et
- 15 al. (1991). Additionally, the revised parameterizations for the functional group COOH are
- taken from Peng et al. (2001), which differs from the parameter matrix proposed in standard
- 17 UNIFAC by Hansen et al. (1991). Since the same mathematical formulations are used in these
- 18 models and differs only in main group interaction parameters, the parameter matrix is
- 19 compatible to use. The influence of estimated activity coefficients when merging specific
- parameters from the distinctive UNIFAC parameterizations within SpactMod has been tested.
- 21 Sensitivity studies have shown, that SpactMod predict relatively better results when
- 22 combining the main functional group interaction parameters instead of using the standard
- 23 UNIFAC parameter set only (see Sect. 3.2). The interaction parameters for these organic
- 25 Other parameter set only (see Sect. 5.2). The interaction parameters for these organic
- 24 | functional groups are shown in Appendix B.
- In UNIFAC, the activity coefficient  $\gamma_j$  of a molecular component j (j can be used for solute
- 26 or solvent) in a multicomponent mixture is in general expressed as the summation of
- 27 contributions of (i) a combinatorial part (C) accounting for the geometrical properties of the
- 28 molecule and (ii) a residual part (R), which results from inter-molecular interactions:

$$\ln \gamma_j^{SR} = \ln \gamma_j^C + \ln \gamma_j^R.$$
(34)

- 30 Since ions are treated such as solvent components in the SR terms, resulting activity
- 31 coefficients in Eq. (34) are with respect to the symmetrical convention on mole fraction basis.

Gelöscht: comprised

Gelöscht: Similar to

**Gelöscht:** However, the standard UNIFAC parameter set, when the same mathematical model expressions are used.

Gelöscht: SPACCIM

Gelöscht: produce

**Gelöscht:** It was found that the model produce relatively better results in most of the cases in comparison with the parameters from standard UNIFAC only.

Gelöscht: Al

Gelöscht: 5

1 For ions, the unsymmetrical normalized activity coefficient is determined from:

$$2 \qquad \ln \gamma_i^{SR(x),\infty} = \ln \gamma_i^{SR(x)} + \ln \gamma_i^{SR(x),ref}. \tag{35}$$

3 The symmetrically normalized value at the reference state is computed from the combinatorial

4 and residual parts, by introducing the reference state conditions of the ions (setting

5 
$$x_w = 1, \sum_{s} x_s = 0 \text{ for } s \neq w \text{ and } \sum_{i} x_i = 0 \text{ } :$$

$$\ln \gamma_{i}^{SR,(x),ref} = \ln \frac{r_{i}}{r_{w}} + 1 - \frac{r_{i}}{r_{w}} + \frac{z}{2} q_{i} \left[ \ln \left( \frac{r_{w} q_{i}}{r_{i} q_{w}} \right) - 1 + \frac{r_{w} q_{i}}{r_{i} q_{w}} \right] + q_{i} \left( 1 - \ln \psi_{w,i} - \psi_{i,w} \right),$$
(36)

7 where subscript w stands for the reference solvent (water). The parameters  $q_i$  and  $r_i$  represent

the surface area and the volume, respectively, of component i. The last term on the right-hand

side of Eq. (36) reflects the residual part reference contribution and becomes zero as we

defined the SR ion ↔ solvent interactions to be zero. Fig. 4 shows the binary species

11 combinations, for which the specific parameters have been used in this study. Mean

12 interactions between ions and water are indirectly represented by the parameters of the cation

⇔anion interaction pairs according to (Zuend et al., 2008), since the aqueous solution is

defined as the reference system similar to the assumption used in conventional Pitzer models

(Pitzer, 1991). The relative van der Waals subgroup volume and surface area parameters,  $R_t$ 

and  $Q_t$ , account for pure component properties. At the same time,  $R_t$  and  $Q_t$  values for the

17 ions can be estimated from the ionic radii. In order to maintain the compatibility with the

model equations of AIOMFAC, the hydrated group volume and surface area parameters  $R_i^H$ 

and  $Q_t^H$  are calculated using an empirical parameterization given by Achard et al. (1994). For

20 those ions, the activity coefficients are estimated using the mod. LIFAC approach. Likewise,

21 the database is extended for other ions in order to estimate the activity coefficients from the

SR part. The measured apparent dynamic hydration numbers  $(N_t^{ADH})$  data are adopted from

Kiriukhin and Collins (2002) to estimate the final values  $R_t^H$  and  $Q_t^H$  instead of  $R_t$  and  $Q_t$ .

24 |  $R_t^H$  and  $Q_t^H$  are computed consistently in the model equations (see Table A2 in the Appendix)

25 by:

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$$R_t^H = R_t + N_t^{ADH} \cdot R_w,$$

(37)

Gelöscht: 6

Gelöscht: 7

Gelöscht: 7

$$1 \qquad Q_t^H = Q_t + N_t^{ADH} \cdot Q_w,$$

(38)

Gelöscht: 9

- where  $R_w$  and  $Q_w$  refer to the values of the water molecule and  $N_t^{ADH}$  are measured apparent
- dynamic hydration numbers at 303.15 K (Kiriukhin and Collins, 2002). As shown in Fig. 4,
- 4 the interactions of the ions  $Mg^{2+}$ ,  $Ca^{2+}$ ,  $F^-$ ,  $\Gamma$ ,  $OH^-$ ,  $NO_2^-$ ,  $CO_3^-$  and  $CH_3COO^-$  are
- 5 implemented from Kiepe et al. (2006). Due to the increasing interest on remaining ions
- 6 included in the multiphase mechanism CAPRAM (e.g. Fe<sup>2+</sup>, succinate, and malonate) the
- 7 activity coefficients are computed while prescribing the corresponding interaction parameters
- 8 as zero.

# 9 2.3.5 Total activity coefficients

- 10 Finally, SPACCIM's activity coefficient module (SpactMod) estimates the total activity
- 11 coefficients for each species according to the Gibbs energy (cp. Eqs. (22) and (24)). Then, the
- activity coefficient of a solvent species s is determined by Li et al. (1994); Yan et al. (1999);
- 13 Kiepe et al. (2006); Zuend et al. (2008)

$$14 \qquad \ln \gamma_s^{(x)} = \ln \gamma_s^{LR(x)} + \ln \gamma_s^{MR,(x)} + \ln \gamma_s^{SR,(x)}$$

(<u>39</u>)

- 15 Accordingly, the complete expression for the ions, with regard to the unsymmetrical
- 16 convention on molality basis at which the standard state is the hypothetical ideal solution of
- 17 unit molality at system pressure and temperature, can be written as follows:

18 
$$\ln \gamma_i^{(m)} = \left[\ln \gamma_i^{LR,(x),\infty} + \ln \gamma_i^{MR,(x),\infty} + \ln \gamma_i^{SR,(x),\infty}\right] - \ln \left[\frac{M_w}{\sum_s x_s^* M_s}\right] + M_w \sum_{i'} m_{i'}$$
(40)

- where  $M_s$  is the molar mass of solvent component s,  $x_s^*$  its salt-free mole fraction, and  $m_{i'}$ , is
- 20 the molality of ion i'. The last term on the right-hand side of Eq. (40) converts the activity
- 21 coefficient  $\ln \gamma_s^{(x)}$  (infinitely diluted reference state on the mole fraction basis) to the activity
- 22 coefficient on molality basis and infinitely diluted (in water) reference state. One can derive
- 23 this term based on convention-independence of the chemical potentials
- 24  $\left(\mu_i^{(m)}(p,T,n_j) = \mu_i^{(x)}(p,T,n_j)\right)$  and the definitions of the chosen reference states (Zuend et
- 25 al., 2008).
- 26 The extension of database by the combination of AIOMFAC and modified LIFAC makes

Gelöscht: 3

Gelöscht: 5

Gelöscht: 40

Gelöscht: 1

- SPACCIM a versatile tool to study the influence of the treatment of <u>solution</u> non-ideality on multiphase aerosol chemistry. SpactMod is highly flexible to extension and further inclusion
- 3 of organic functional groups and ions, whenever the required data become available. During
- 4 the implementation of the code, the activity coefficients responsible for LR and SR
- 5 contribution terms are computed for all the ions (either cation or anion) included in the
- 6 considered chemical system. For those species, where the interaction parameters are not
- 7 available to compute MR contribution terms; they are prescribed as unity (i.e.,  $\gamma_i^{MR,(x),\infty} = 1$ )
- 8 due to the lack of extensive database.

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#### 3 Model evaluation and applications

- 10 In this section we will examine the model extensions described above. Especially, the activity
- 11 coefficient module SpactMod is evaluated and compared with literature data. The reliability
- 12 of the extended SPACCIM code is shown in the last subsection. Furthermore, the deviation of
- 13 the activity coefficients from ideality and, consequently, the impact on the chemical behavior
- 14 are demonstrated for a test scenario. A more detailed analysis of the impact of the non-ideality
- approach on the multiphase will be published in a separate paper.

#### 3.1 Evaluation of the activity coefficient module

- 17 Considerable effort has been devoted by several authors (see e.g., Raatikainen and Laaksonen
- 18 (2005); Tong et al. (2008); Zuend et al. (2008)) to compare different established activity
- 19 coefficient models that could be potentially suitable for modeling of hygroscopic properties of
- 20 organic-electrolyte particles as well as the prediction of activity coefficients of aqueous
- 21 species. The investigations summarized here were aimed to evaluate the robustness of the
- 22 implemented module SpactMod and to check the reproducibility towards original model
- 23 results. However, the interaction parameters in the applied models were fitted against
- 24 measurements. Hence, this comparison can be considered as indirect comparison with
- 25 measurements. Furthermore, results are also compared with direct also water activity
- measurements and the AIM model (Aerosol Inorganic Model) of Clegg et al. (1998b, 1998a).
- 27 The model comparisons cover a scale, ranging from very simple to complex simulations.
- 28 Initially, the comparison is performed for selected binary aqueous electrolyte solutions, then
- 29 aqueous organic solutions, followed by mixtures of aqueous organic-electrolyte solutions.
- 30 However, here we present the results of selected examples only.

#### 3.1.1 Comparison between activity coefficient models for inorganic systems

Naturally, the reproducibility of the original AIOMFAC results in Zuend et al. (2008) was 3 verified in a first step. Note that the graphs of the newly implemented module SpactMod 4 depicted in Figs. 5 and 6 correspond to the original results given in Zuend et al. (2008). Fig. 5 5 shows the comparison between calculated water activities predicted by the selected four 6 models and experimental data. The differences for the electrolyte mixture of NaCl + NH<sub>4</sub>NO<sub>3</sub> 7 are in good agreement up to moderate salt concentrations  $(x_w \ge 0.5)$ . The values for high 8 concentrations  $(x_w \le 0.4)$  indicate the formation of a solid salt (or hydrate), when the solution 9 becomes supersaturated as well as the deliquescent point of the particular salt. The models do not reproduce this, since the formation of solids was not incorporated in the present model 10 calculations. As can be seen from Figs. 5 and 6, the modeled water activities agree well with 11 12 each other at low concentrations. Contrary at high salt concentrations, mod. LIFAC strongly 13 deviates from SpactMod as shown in Fig. 5, by a steep increase in  $a_w$  and in Fig. 6 by an 14 increase followed by a sharp decrease, as shown by Zuend et al. (2008). Note that the 15 Ca(NO<sub>3</sub>)<sub>2</sub> parameterization of mod. LIFAC (see Fig. 6) results only from water activity data of bulk measurements as the approach of Ming and Russell (2002) model, behaves similar to 16 17 SpactMod at medium concentrations and proceed to formation of solids. The interaction 18 coefficients of AIOMFAC applied in SpactMod were fitted from vapor-liquid as well as 19 liquid-liquid equilibrium data, salt solubilities and electromotive force measurements 20 covering also high solution concentrations and ternary mixtures (Zuend et al., 2008). Hence, 21 the slope of the curve enables much better descriptions and predictions up to high 22 concentrations, even very low water concentration available and at high ionic strength. It is noted that Ca(NO<sub>3</sub>)<sub>2</sub> is not available in the AIM, thus Fig. 6 includes only results of the other 23 24 activity coefficient approaches.

25 Apart from the predicted water activities, the calculated mean activity coefficients also have

differences with each other. Therefore, a comparison of mean activity coefficients is 26

presented additionally in Fig. 6. The mean activity coefficient ( $\gamma_{\pm}$ ) is related to single ion-27

28 activity coefficients by

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$$\gamma_{\pm} = (\gamma_{+}^{V_{+}} \cdot \gamma_{-}^{V_{-}})^{1/(V_{+} + V_{-})}$$
 (41)

30 where  $\gamma_+$  and  $\gamma_-$  are the activity coefficients of a cation and anion, respectively.  $V_+$  and  $V_-$  are

the corresponding stoichiometric coefficients. The mean activity coefficients predicted by 31

Gelöscht: 2

Gelöscht: but is described here

- 1 AIOMFAC and the approach of Ming and Russell (2002) show a similar curve shape with
- 2 5 % of difference. In contrast, mod. LIFAC shows a different behavior especially for water
- 3 fractions later than 0.8.

#### 4 3.1.2 Verification of SpactMod for organic-electrolyte mixtures

- 5 In this section, the performance of different activity coefficient models is evaluated by
- 6 comparing calculated and measured water activities of mixtures of electrolyte and organic
- 7 system. For all water activity calculations, the organic acids are treated as non-dissociating
- 8 solutes, and a single liquid phase is assumed with no solid phases present. All calculations are
- 9 performed at atmospheric pressure (1 atm) and at 298 K.
- 10 Fig. 7 shows the comparison of experimental data with predicted water activities using
- 11 different UNIFAC parameterizations. Here, the parameters for the original UNIFAC are
- 12 | adopted from Hansen et al. (1991). Furthermore, a revised set of fitted UNIFAC parameters
- 13 given by Peng et al. (2001) for the interactions of functional groups OH, H<sub>2</sub>O and COOH is
- 14 used for the comparison. As depicted in Fig. 7, the original UNIFAC and Ming and Russell
- 15 (2002) exhibit similar behavior for all water fractions. Moreover, SpactMod and the version
- of Peng et al. (2001) have deviations that are usually less than 50% of the deviations with the
- 17 original UNIFAC. Furthermore, the original UNIFAC exhibits much bigger deviations than
- the UNIFAC version of Peng et al. (2001) and SpactMod. The last two models show a similar
- behavior and a good agreement with the measurements. In difference to the Peng approach,
- 20 | SpactMod take into account dynamic hydration numbers (see Eq. (37) and (39)), which is in
- 21 consistency with the computation of the combinatorial term in AIOMFAC.
- 22 Fig. 8 shows the comparison of mean ionic activity coefficients of binary electrolyte mixtures.
- As can be seen from the plot, good results were obtained by SpactMod based on mod. LIFAC
- 24 parameterization. Mod.LIFAC shows better results compared to LIFAC due to the improved
- 25 reference state calculation of ions in the SR part. Due to the normalization of ions, SpactMod
- 26 gives better agreement compared to original LIFAC for these binary electrolytes.
- 27 Fig. 9 shows the comparison between predicted water activities from different activity
- 28 coefficient models for the mixture of  $(NH_4)_2SO_4 + Glycerol + H_2O$  [(2:1:1) mole ratio]. As
- 29 expected, SpactMod accurately reproduces the results from the original AIOMFAC. All the
- 30 models behave similarly up to moderate concentrations ( $x_w = 0.6$ ). As in Fig. 6, at lower water
- activity, mod. LIFAC and LIFAC strongly deviate from SpactMod. As argued earlier, LIFAC

Gelöscht: Hanson and Ravishankara (1993)

Gelöscht: 8

Gelöscht: at the deliquescent phase

and mod. LIFAC are able to predict vapor liquid equilibria and liquid liquid equilibria but cannot describe the deviations from ideality at high concentrations. A steep increase of  $a_w$  shown in Fig. 9 have to be rated as artefacts of the LIFAC and mod. LIFAC parameterization.

Fig. 10 shows the comparison between experimental and predicted water activities for the mixture of (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> + Ethanol + Acetic acid [(2:1:1) mole ratio]. All the models strongly agree with the measurements at high relative humidities or at low and moderate salt concentrations  $(x_w \approx 0.8)$ . However at the deliquescent phase  $(x_w \approx 0.6)$ , the mod. LIFAC and Ming and Russell (2002) model strongly deviate from SpactMod. These differences for lower water fractions are mainly caused by the different treatment of ion ↔ organic interactions included in the models. It can be seen from Fig. 10 that the strange behavior does not appear for the pure organic and pure electrolyte mixture predictions. The MR interaction term in the model is responsible for this atypical shape in the predictions. Moreover, Raatikainen and Laaksonen (2005) argued that, in the MR part, the logarithms of activity coefficients are calculated as sums of terms, which are proportional to the fitting parameters, ion molalities and ionic strength. Because these terms have quite large numerical values, and a small change in the interaction parameters or molality can cause a very big change to activity coefficients. The MR part and modification of SR part given in SpactMod could be the main reason, since this model can predict the water activities at high salt concentrations as well. Consequently, as can be seen from Fig. 10, mod. LIFAC have an increase followed by a sharp decrease, features that have to be rated as artifacts of the mod. LIFAC parameterization, whereas the Ming and Russell (2002) model has also a strong increase after the water fraction is about  $(x_m \approx 0.3)$ . As mentioned earlier, these artifacts indicate the formation of a solid salt (or hydrate), when the solution becomes supersaturated, since the formation of solids was not enabled in the model calculations.

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However, the consideration here is only a limited set of mixtures of organic-electrolyte compounds. Hence, the presented results should be viewed as a first assessment. The scarcity of experimental data for mixtures of atmospheric relevance remains a limitation for testing activity coefficient models. When experimental data become available in the future, the models can be validated against measurements, while comparing the water activity and species activity coefficients against water fraction  $x_w$ . All in all, despite the difficulties in determining the ion  $\leftrightarrow$  organic mixture parameters, it should be noted that the ion  $\leftrightarrow$  organic

Gelöscht: 8

Gelöscht: (Ming and Russell, 2002)

Gelöscht: 8

Gelöscht: 8

Gelöscht: Fig. 9 shows the comparison of mean ionic activity coefficients of binary electrolyte mixtures. As can be seen good results were obtained by SpactMod based on mod. LIFAC parameterization. The reliable prediction of activity coefficients with improved reference state calculation, the mod. LIFAC produced better results compare to LIFAC. Due to the normalization of ions SpactMod gives better accuracy compare with original LIFAC for these binary electrolytes ... [11]

- 1 interaction parameters have improved the model performance, a fact which was already noted
- 2 in previous studies (Clegg and Seinfeld, 2006b, a; Clegg et al., 2001; Tong et al., 2008)

#### 3.2 Sensitivity studies on the importance of the different interactions

- 4 Tong et al. (2008) studied the importance of inclusion of a treatment of ion ↔ organic
- 5 interactions and states that these interactions would substantially improve the performance of
- 6 the coupled models over that of the decoupled models. It has been concluded that, decoupled
- 7 approaches, such as those in CSB (Clegg et al., 2001), ADDEM (Topping et al., 2005a, b),
- 8 performs well, and in some cases better than the coupled models (Ming and Russell, 2002;
- 9 Erdakos et al., 2006a, b). Additionally in such cases, the ion ↔ organic terms do not
- 10 necessarily lead to improved model predictions. At the same time, models are prerequisite,
- 11 composed of an aqueous electrolyte term, an (aqueous) organic term, and an organic  $\leftrightarrow$ ion
- 12 mixing term in order to treat the organic-inorganic mixtures. In contrast to the study of Tong
- 13 et al. (2008), the present study aims at the evaluation of the importance of different interaction
  - terms in the model approach Eq. (24) for the computation of water activities and the activity
- 15 coefficients.

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3

- 16 Intermolecular forces or interactions are essential in the deliquesced particle phase, where
- 17 high solute concentrations and low water fractions are available. They are important because
- 18 they are responsible for many of the physical properties of solids, liquids, and gases.
- 19 Moreover, these interaction forces become significant at the molecular range of about
- 20 1 nanometer or less, but are much weaker than the forces associated with chemical bonding.
- 21 The characteristic contribution of different interaction forces from the model development
- 22 | point of view in the solution can be computed using Eq. (24). Utilizing this conceptual idea in
- 23 the computation of activity coefficients, here we address the question, which intermolecular
- 24 | forces of attraction are important and need be considered for the treatment of solution non-
- ideality for organic-electrolyte mixtures. In order to answer this question, the SpactMod is
- 26 used for sensitivity studies. Overall, the studies have revealed that middle-range (MR)
- 27 interactions are important to compute the total activity coefficients.
- 28 Fig. 11 shows the contribution of different interaction forces in the solution for the mixture of
- 29 NaCl + (NH<sub>4</sub>)<sub>2</sub> SO<sub>4</sub> + Ethanol + Malonic acid [1:1:1:1 (mole ratio)] as an example. However,
- 30 the deviations regarding the different interactions depend on the considered mixture. As can
- 31 be seen in Fig. 9, the water activity strongly deviates in absence of MR interaction forces,

Gelöscht: 5

Gelöscht: 5

1 mainly caused from ion  $\leftrightarrow$  ion, ion  $\leftrightarrow$  dipole and ion  $\leftrightarrow$  induced dipole forces. Thus, the MR 2 interactions were found important. Similar to the findings of Tong et al. (2008), it is expected 3 that ion \( \lor \) organic interactions be of most importance in solutions with high solute 4 concentrations, for which inclusion of ion ↔ organic parameters would be beneficial. 5 However, the absence of each interaction terms can be seen in Fig. 11. The short-range 6 interactions also influence in the total contribution of computation of water activity, where the 7 deviations are about 10%. In the case of considered the MR and SR interactions, the 8 deviations are about 25%. It should be noted that the ion ↔ organic interactions are the 9 dominant interaction forces in the solution, however the further interaction forces need to be 10 considered. The deviations from the total contribution of interaction forces is significant in all ranges of relative humidity as well as in the full range of concentration. Nevertheless, the 11 12 deviations are increasing from lower salt/acid concentration to higher. During the low 13 salt/acid concentration ( $x_w \approx 0.9$ ) the contribution of the considered interactions were found 14 similar.

#### 3.3 First application of the advanced SPACCIM model

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16 To demonstrate the functioning of the whole advanced SPACCIM model framework including the newly considered activity coefficient module SpactMod and a complex 17 multiphase aerosol chemistry mechanism, first air parcel simulations have been performed 18 19 with a simple model scenario. In the two following subsections, the applied model scenario 20 and chemical mechanism is briefly outlined, and subsequently selected model results are presented. However, it is noted that the presented simulations are not aimed at the detailed 21 22 examination of non-ideal solution effects on multiphase chemical processes. The detailed 23 investigation of this complex issue will be given in a companion paper (Rusumdar et al., 24 2015).

#### 3.3.1 Model scenario and chemical mechanism

26 In the applied meteorological scenario, an air parcel moves along a predefined 3-hour model 27 trajectory that involves three cloud passages and non-cloud periods in which the aerosol 28 particles are deliquesced. Simulations were performed with and without consideration of non-29 ideal solutions. Furthermore, the simulations have been performed with two different relative 30 humidity levels (90 % r.h. and 70% r.h.) during the non-cloud periods. In total, simulations have been performed for four cases: with and without consideration of non-ideal solutions and 31

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- both with a 90% and 70% relative humidity level during the non-cloud periods, respectively.
- 2 For the modeling, mono-disperse aerosol particles with a radius of 200 nm and a number
- 3 concentration of 1.0·10<sup>+8</sup> cm<sup>-3</sup> were used.
- 4 For the test simulations, a complex multiphase chemistry mechanism has been applied. The
- 5 applied mechanism consists of the gas phase mechanism RACM-MIM2ext (Tilgner and
- 6 Herrmann, 2010) and an extended version of the aqueous phase mechanism CAPRAM2.4
- 7 (CAPRAM2.4 + organicExt). The employed aqueous phase mechanism consists of the
- 8 CAPRAM2.4 mechanism (Ervens et al., 2003) combined with the reduced organic extension
- 9 of CAPRAM3.0i-red (Deguillaume et al., 2010) along with the condensed oxidation scheme
- of malonic acid and succinic acid based on the CAPRAM3.0i-red (see Deguillaume et al.
- 11 (2010) for further details). Thus, the aqueous phase mechanism contains a detailed oxidation
- scheme of inorganic as well as organic compounds with 204 species and 477 reactions. In the
- 13 considered organic reaction scheme describes the chemistry of organic compounds with up to
- 4 carbon atoms and different functional groups. All model simulations have been performed
- 15 for continental remote environmental conditions (see Ervens et al. (2003) for further details).

#### 16 3.3.2 Model results

17 Modeled activity coefficients of key inorganic ions

Fig. 12 depicts the time evolution of the activity coefficients of main inorganic ions and key

- 19 transition metal ions (TMIs) modeled for the two different relative humidity cases. The plots
- 20 show, expectedly, a strong dependency on the microphysical conditions. During cloud
- 21 conditions, the modeled activity coefficients are almost equal to unity for the depicted ions.
- 22 The in-cloud activity coefficients of ions with charge state 3+ deviate a bit more from the one
- 23 than less charged ions. Under concentrated deliquesced particle conditions, the activity
- 24 coefficients of ions are much lower and show a strong dependence on the relative humidity
- 25 level. In the 90% r.h. case, the activity coefficients of singly charged ions are in the range of
- 26 0.6-0.7, whereas the modeled coefficients for the doubly and triply charged ions are 0.3-0.35
- 27 and 0.1, respectively. Additionally, Fig. 12 reveals that the deviations from ideal behavior
- 28 strongly depend on the species regarded but mainly on the charge state. The comparison with
- 29 the 70% r.h. case shows clearly that the activity coefficients do not change linearly with
- 30 relative humidity. This fact is caused by a non-linear change of activity coefficients in terms
- 31 of the molality due to the different types of interactions in the solution. From Fig. 10 it can be

**Gelöscht:** For the two cases without treatment of non-ideal effects, the aqueous phase chemistry is treated as ideal.

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- 1 seen that the activity coefficients of singly or doubly charged ions are significantly lowered in
- 2 the 70% r.h. case compared to the 90% r.h. case. However, no substantial decrease is
- 3 simulated for triply charged ions such as Fe<sup>3+</sup>, which are still in the range of 0.1. Interestingly,
- 4 the activity coefficient of H<sup>+</sup> show only a drop of 0.1 between the two cases, while the activity
- 5 coefficients of other singly charged ions are lowered by approximately 0.2.
- 6 In total, the simulated activity coefficients of inorganic ions with values below 1 implicate
- 7 that the mass fluxes of chemical processes in deliquesced particles involving those ions are
- 8 most likely decreased leading thus to a different chemical regime than present under ideal
- 9 cloud conditions. For example, the huge differences in the activity coefficients of the TMIs
- 10 can lead to substantial differences in the redox cycling.

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Modeled activity coefficients of important organic compounds

13 | Fig. 13, illustrates the modeled time evolution of the activity coefficients of important organic

14 carbonyl compounds and organic acids (both free acid and anions) for the two different

relative humidity cases. For organic carbonyl compounds, the depiction reveals quite uneven

pattern. For hydrated glyoxal and glycolaldehyde, the predicted activity coefficient are larger

than 1 in both model cases. In contrast, activity coefficients below 1 are predicted for the

other unhydrated organic carbonyls and the hydrated formaldehyde. As shown for the organic

ions, there is a strong dependence of the non-ideal behavior on the species and their specific

forms (i.e., functional groups included) as well as additionally the relative humidity

21 conditions. For the hydrated glyoxal and glycolaldehyde with more than 3 OH functionalities

22 included, activity coefficient values of about 1.2 and 1.6, respectively, are modeled in the

90% r.h. case. Many times higher activity coefficients are calculated for the 70% r.h. case.

24 The predicted activity coefficients of the organic acid anions behave similarly to the inorganic

ions. Differences can be observed for the 2 free acids plotted in Fig. 13. While the activity

coefficient of formic and acetic acid corresponds mainly to the present supersaturation of 0.9

27 in the 90% r.h. case, the activity coefficient of acetic acid are higher during the more

28 concentrated case at 70% r.h. This behavior is caused by the additional methyl group. In

summary, the predicted activity coefficients of organic compounds imply that the chemical

processing of organics can be either increased or decreased under deliquesced particle

conditions depending on the particular compound.

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Gelöscht: 1

Gelöscht: 1

Gelöscht: organic

2 Modeled acidity

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3 The modeled pH-values for the four different simulations are plotted in Fig. 14. The pH 4 values simulated with and without consideration of non-ideal solution effects reveal no 5 difference during the cloud periods but substantial deviations during the non-cloud periods. 6 During the cloud periods under almost ideal conditions, an decrease of the pH value is 7 modeled due to occurring acidifying reactions such as the S(IV) to S(VI) conversion. The acidification is strongest during the first cloud passage and lower during the two following 8 9 clouds. From the two plots, it can be seen that the difference between the ideal and non-ideal 10 case is somewhat larger for the 70% case. On average, the pH values of the simulations considering solution non-ideality are -0.27 and -0.44 pH units lower under 90% r.h. and 11 12 70% r.h. conditions, respectively. This, lower acidity in the non-ideal case is able to affect 13 both aqueous phase chemical reactions (i.e., acid catalyzed reactions) and all dissociations. 14 Further implications of this difference for the chemical processing are not discussed here, but 15 outlined in a companion paper (Rusumdar et al., 2015).

Overall, the performed simulations demonstrated that the further developed SPACCIM model performs well and the simulation results emphasize the consideration of solution non-ideality

in multiphase chemistry models especially for an adequate description of the chemical aerosol

processing in deliguesced portioles

19 processing in deliquesced particles.

4 Summary

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30 31 In the present work, a robust and comprehensive model framework is developed and implemented in order to treat the aqueous phase chemistry considering non-ideal solution effects in the context of the multiphase model SPACCIM. The implemented group-contribution concept enables the reliable estimation of activity coefficients for organic-inorganic mixtures composed of various ions and functional groups. Treatment of solution non-ideality for mixed-solvent systems requires a careful combination of standard-state properties with activity coefficient models. This was achieved in practice by ensuring the correct representation of Gibbs excess energy by three contributions to the excess Gibbs energy. Surface tension depreciation due to the organic compounds is effectively accounted and included in the model framework. Interaction parameters accounts for various

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**Gelöscht:** including the considered non-ideality approach

1 contributions of interactions. Mixed organic-inorganic systems from the literature are 2 critically assessed and a new database is created. For all tested types of systems and data, the 3 designed model SpactMod has been shown to reproduce both the original model results and experimental results with good accuracy. Sensitivity studies have shown that the inclusion of 4 5 middle-range interaction contributions is necessary. This inclusion enhances the robustness of 6 the model. The current developed framework is open to extension to further organic 7 functional groups, and ions, when thermodynamic data on such systems become available. Indeed, compound specific parameter, such as charge, organic functional groups and 8 9 interaction parameters, required for the activity coefficient model as well as chemical reaction 10 data are read from input files. The interaction parameters will be easily incorporate and the database can flexibly updated. Besides, the computer code will facilitate the changes and 11 future inclusions. The implemented numerical schemes merely give good computational 12 efficiency. Due to the limitations regarding the lack of experimental data, and the ability to 13 treat the organic-electrolyte mixtures of atmospheric relevance at various complexities, 14 15 predictions are improved considerably while using extended interaction parameters. In future, the database will be extended with new parameters of recent studies ((Zuend et al., 2011; 16 17 Mohs and Gmehling, 2013; Ganbavale et al., 2015) within this activity coefficient module. 18 First test simulations with the advanced SPACCIM model have demonstrated the applicability 19 of SpactMod within the model framework. Furthermore, the simulations emphasize that the 20 treatment of solution non-ideality is mandatory for modeling multiphase chemistry processes 21 in deliquesced particles. For important ions, the model runs have shown activity coefficients 22 <1 and a strong dependency on the charge state as well as on the microphysical conditions. 23 Thus, the model results implicate that the chemical processing of ions in deliquesced particles is potentially lowered and different to a chemical regime present under ideal cloud conditions. 24 25 For organic compounds, the modeled activity coefficients the activity coefficients are both 26 lower and higher than unity suggesting that the chemical processing of organics can be either 27 increased or decreased under deliquesced particle conditions depending on the particular 28 species. The complexity of consideration of non-ideal solutions and its influence on 29 multiphase chemistry is investigated in detail in a companion paper (Rusumdar et al., 2015).

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#### 1 Appendix A: SPACCIM's activity coefficient module

#### 2 A.1 Middle-range contribution-model extension

- 3 The activity coefficients responsible for the MR interaction forces are obtained by
- 4 differentiating the Eq. (30) with respect to the number of moles of solvent main groups,
- 5 cations, and anions respectively. Thus, expressions for a specific cation  $c^*$  on a mole fraction
- 6 basis can be written as:

$$\ln \gamma_{c^{*}}^{MR,(x),\infty} = \frac{1}{M_{av}} \sum_{k} B_{k,c^{*}}(I) x_{k}^{'} + \frac{z_{c^{*}}^{2}}{2M_{av}} \sum_{k} \sum_{i} B_{k,i}^{'}(I) x_{k}^{'} m_{i} + \sum_{a} B_{c^{*},a}(I) m_{a}$$

$$+ \frac{z_{c^{*}}^{2}}{2} \sum_{c} \sum_{a} B_{c,a}^{'}(I) m_{c} m_{a} + \sum_{a} C_{c^{*},a}(I) m_{a} \sum_{i} m_{i} |z_{i}|$$

$$+ \sum_{c} \sum_{a} \left[ C_{c,a}(I) |z_{c^{*}}| + C_{c,a}^{'}(I) \frac{z_{c^{*}}^{2}}{2} \sum_{i} m_{i} |z_{i}| \right] m_{c} m_{a}$$

$$+ \sum_{c} R_{c^{*},c} m_{c} + \sum_{c} \sum_{a} Q_{c,c^{*},a} m_{c} m_{a}$$
(A1)

8 For a better understanding, Eq. (A1) can be divided into different terms:

9 
$$\ln \gamma_i^{MR} = T_i^{solvent} + T_i^{ion-solvent} + T_i^{ion} + T_i^{ion-ion} + T_i^{ternary}$$
 (A2)

10 with

11 
$$T_i^{solvent} = \frac{1}{M} \sum_k B_{k,c^*}(I) x_k',$$
 (A3)

12 
$$T_i^{solvent} = \frac{1}{M_{ov}} \sum_k B_{k,c*}(I) x_k',$$
 (A4)

13 
$$T_i^{ion} = \sum_a B_{c^*,a}(I) m_a + \sum_c R_{c^*,c} m_c + \sum_a C_{c^*,a}(I) m_a \sum_i m_i |z_i|,$$
 (A5)

$$T_{i}^{ion-ion} = \frac{z_{c^*}^2}{2} \sum_{c} \sum_{a} B_{c,a}^{\dagger}(I) m_{c} m_{a} + \sum_{c} \sum_{a} \left[ C_{c,a}(I) |z_{c^*}| + C_{c,a}^{\dagger}(I) \frac{z_{c^*}^2}{2} \sum_{i} m_{i} |z_{i}| \right] m_{c} m_{a}$$
(A6)

$$T_i^{ternary} = \sum \sum Q_{c,c^*,a} m_c m_a. \tag{A7}$$

al. (2008) to improve the treatment of systems at high ionic strength.

4

3

- 5 As mentioned in Sect. 3, the activity coefficient module SpactMod is substantially based on
- AIOMFAC (Zuend et al., 2008). But it has been extended by including the new interaction 6
- 7 parameters for the species shown in Fig. 4, based on mod. LIFAC (Kiepe et al., 2006). A
- 8 sufficient evaluation was performed using the actual experimental database, which has been
- 9 significantly enlarged within the last years (see Raatikainen and Laaksonen (2005); Tong et
- 10 al. (2008)).

11

- The general concentration dependence of the interaction parameters can be written as 12
- 13 analogous to Eq. (31):

14

15 
$$B_{i,j} = b_{i,j} + c_{i,j} \exp(a_1 \sqrt{I})$$
 (A8)

- 16 where,  $b_{i,j}$ ,  $c_{i,j}$  and  $a_1$  are adjustable interaction parameters. However, according to
- mod. LIFAC (Kiepe et al., 2006), the second virial coefficient  $B_{i,j}$  is the interaction 17
- coefficient between the species i and j. The relations of the ion  $\leftrightarrow$  ion interaction parameter 18
- 19  $B_{c,a}$  and ion  $\leftrightarrow$  solvent group interaction parameter  $B_{k,ion}$  to the ionic strength are described
- 20 by Kiepe et al. (2006).

21

22 
$$B_{c,a} = b_{c,a} + c_{c,a} \exp(-\sqrt{I} + 0.125I),$$
 (A9)

23 
$$B_{k,i} = b_{k,i} + c_{k,i} \exp(-1.2\sqrt{I} + 0.25I)$$
. (A10)

- 24 The equation for interaction parameters shown in the two versions (Eqs. 31 - 32 A9 and
- 25 A10) was compared and the final model equations are derived. As a result, Eq. (A9) can be
- 26 written as similar to Eq. (32):

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Gelöscht: 2

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$$B_{c,a}(I) = b_{c,a} + c_{c,a} \exp\left(-\left(1.0 - 0.125\sqrt{I}\right)\sqrt{I}\right)$$
 (A11)

- 2 Based on this, while using the similar model equations, the database was utilized with the ion
- $3 \leftrightarrow \text{ion interaction parameters as:}$

4 
$$b_{c,a}^{(1)} = b_{c,a}, b_{c,a}^{(2)} = c_{c,a}, b_{c,a}^{(3)} = (1.0 - 0.125\sqrt{I}).$$
 (A12)

- 5 Since ion ↔ ion ↔ ion interaction parameters (ternary interactions) were not available with
- 6 mod. LIFAC, the interaction parameters for  $c_{c,a}^{(1)}$  and  $c_{c,a}^{(2)}$  were assigned to zero. Similar to ion
- 8 parameters were also modified. Compared to Eq. (31) and Eq. (A10), the parameters are
- 9 assigned as

10 
$$b_{k,i}^{(1)} = b_{k,i}, \ b_{k,i}^{(2)} = c_{k,i}, \ b_{k,i}^{(3)} = (1.2 - 0.125\sqrt{I}).$$
 (A13)

- 11 Afterwards without altering the model equations given in AIOMFAC, computation of activity
- 12 coefficients for all species is performed. Even, the ternary and quaternary interactions were
- 13 also assigned to zero during the computation of activity coefficients for solvent groups.
- Hence, the model equations reduced to original model equations as described in Kiepe et al.
- 15 (2006) and Yan et al. (1999). Similarly, for the ions, the ternary interactions (Eq. (A6)) are
- not considered to compute the activity coefficients, which are not explicitly described in the
- 17 original AIOMFAC. So this term is equal to zero, and hence the Eq. (3.19) and Eq. (3.20)
  - given in Zuend et al. (2008) lead to the original model equations (see Eq. (12) in Kiepe et al.
- 19 (2006)). The chemical species included in the multiphase mechanism are categorized by
- 20 different classes in the input files. While using these input files, this algorithm performs a
- search, and gathers the information, whether the computation of interaction parameters needs
- 22 to perform according to AIOMFAC or the modified equations specified according to Kiepe et
- 23 <u>al. (2006)</u>. Thus, the adjustable interaction parameters are used to compute and finally utilized
- by the activity coefficients responsible for MR interactions.

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Table A1: MR Parameters  $b_{k,i}^{(1)}$  and  $b_{k,i}^{(2)}$  between solvents and ions (AIOMFAC- Black/ mod. LIFAC- Red)

Ion	Group	$b_{k,i}^{(1)}$	$b_{k,i}^{(2)}$	Ion	Group	$b_{k,i}^{(1)}$	$b_{k,i}^{(2)}$
		(kg mol <sup>-1</sup> )	(kg mol <sup>-1</sup> )			(kg mol <sup>-1</sup> )	(kg mol <sup>-1</sup> )
Na <sup>+</sup>	CH <sub>n</sub>	0.124972	- 0.031880	Na <sup>+</sup>	ОН	0.080254	0.002201
$K^{+}$	$CH_n$	0.121449	0.015499	$K^{+}$	ОН	0.065219	-0.170779
$\mathrm{NH_4}^+$	$CH_n$	0.103096	-0.001083	$\mathrm{NH_4}^+$	ОН	0.039373	0.001083
$Ca^{2+}$	$CH_n$	0.000019	-0.060807	Ca <sup>2+</sup>	ОН	0.839628	-0.765776
$Mg^{2+}$	$CH_n$	- 0.34610	-0.44995	$\mathrm{Mg}^{2^+}$	ОН	0.281980	0.07617
$Zn^{2+}$	$CH_n$	- 0.10163	- 0.06578	$Zn^{2+}$	ОН	0.036480	0.02249
Cl <sup>-</sup>	$CH_n$	0.014974	0.142574	Cl <sup>-</sup>	ОН	-0.042460	-0.128063
$NO_3^-$	$CH_n$	0.018368	0.669086	$NO_3^-$	ОН	-0.128216	-0.962408
SO <sub>4</sub> <sup>2-</sup>	$CH_n$	0.101044	-0.070253	SO <sub>4</sub> <sup>2-</sup>	ОН	-0.164709	0.574638

Ι-	$CH_n$	0.01206	- 0.02777	Ι-	ОН	-0.04479	0.04151
				F -	ОН	0.15233	-0.04145
				CH <sub>3</sub> COO <sup>-</sup>	ОН	0.02672	-0.02117
Na <sup>+</sup>	$H_2O$	0.00331	-0.00143	$Na^+$	CH₃OH	0.16617	0.03928
$K^{+}$	$H_2O$	0.00258	- 0.00088	$K^{+}$	CH <sub>3</sub> OH	0.10797	0.19164
$\mathrm{NH_4}^+$	$H_2O$	0.00088	0.00288	$\mathrm{NH_4}^+$	CH <sub>3</sub> OH	0.20529	- 0.10550
$Ca^{2+}$	$H_2O$	0.01105	0.00641	Ca <sup>2+</sup>	CH <sub>3</sub> OH	0.37818	0.00247
$Mg^{2+}$	$H_2O$	0.00050	0.01163	$Cu^{2+}$	CH <sub>3</sub> OH	0.00789	- 0.06944
$Cu^{2+}$	$H_2O$	- 0.00571	- 0.00760	$Zn^{2+}$	CH <sub>3</sub> OH	0.16775	- 0.44229
$Zn^{2+}$	$H_2O$	- 0.01848	0.00001				
Cl <sup>-</sup>	$H_2O$	-0.00128	- 0.00020	Cl <sup>-</sup>	CH <sub>3</sub> OH	- 0.03352	0.00242
$NO_3^-$	$H_2O$	0.03228	- 0.00083	$NO_3^{-1}$	CH₃OH	- 0.07716	- 0.00669
SO <sub>4</sub> <sup>2-</sup>	$H_2O$	0.02278	0.00271	Br <sup>-</sup>	CH₃OH	- 0.00944	- 0.06080
Br <sup>-</sup>	$H_2O$	- 0.00247	- 0.00008	Ι-	CH <sub>3</sub> OH	- 0.02090	- 0.14894

$NO_2^{-}$	H <sub>2</sub> O	0.00549	- 0.00565	F -	CH <sub>3</sub> OH	0.07436	- 0.04388
Ι.	$H_2O$	-0.00537	0.00018	CH <sub>3</sub> COO	CH <sub>3</sub> OH	0.00046	0.01249
F -	$H_2O$	0.00652	0.00132				
CH <sub>3</sub> COO	$H_2O$	0.01918	0.00230				
Na <sup>+</sup>	CH <sub>2</sub> CO	-0.21019	0.94813				
K <sup>+</sup>	CH <sub>2</sub> CO	-0.44195	1.10287				
Cl <sup>-</sup>	CH <sub>2</sub> CO	0.54064	-0.62981				
Br <sup>-</sup>	CH <sub>2</sub> CO	0.48898	-0.96778				
I -	CH <sub>2</sub> CO	0.08245	0.03292				
CH <sub>3</sub> COO	CH <sub>2</sub> CO	0.26560	-0.93032				

Table A2: Mod. LIFAC Binary cation-anion MR interaction parameters

Cation	Anion	$b_{c,a}^{(1)}$	$b_{c,a}^{(2)}$
Na <sup>+</sup>	F-	-0.00694	-0.08166
$Na^+$	I-	0.27922	-0.13430
$Na^+$	$NO_3^-$	0.04425	-0.41980
Na <sup>+</sup>	CH₃COO⁻	0.25018	0.31363
$K^{+}$	F <sup>-</sup>	0.18434	-0.28912
$K^{+}$	I-	0.12860	0.02379
$K^{+}$	$NO_3^-$	-0.06095	-0.67019
K <sup>+</sup>	CH₃COO⁻	0.27327	0.45129
$\mathrm{Mg}^{^{+}}$	Cl-	0.45150	1.19298
$Mg^+$	Br-	0.59615	1.37619
$Mg^+$	I-	0.76336	1.58654
$Mg^+$	$NO_3^-$	0.28427	1.72405
$Mg^+$	$SO_4^{2-}$	0.53597	1.03876
Ca <sup>+</sup>	Br-	0.60948	0.30140
Ca <sup>+</sup>	I-	0.59261	1.46632
Ca <sup>+</sup>	$SO_4^{2-}$	-15.8421	-0.00212
Cu <sup>2+</sup>	Cl-	0.21233	0.11695

Cu <sup>2+</sup>	NO <sub>3</sub>	0.45706	-0.41585
$Cu^{2+}$	$SO_4^{2-}$	1.24148	-5.86466
$Zn^{2+}$	Cl-	0.04463	0.43088

Table A3: AIOMFAC Binary cation ↔ anion MR interaction parameters.

Cation	Anion	$b_{c,a}^{(1)}$	$b_{c,a}^{(2)}$	$b_{c,a}^{(3)}$	$c_{c,a}^{(1)}$	$c_{c,a}^{(2)}$
		$[kg \ mol^{-1}]$	$[kg \ mol^{-1}]$	$[kg^{1/2}mol^{-1/2}]$		$[kg^{1/2}mol^{-1/2}]$
$H^+$	Cl <sup>-</sup>	0.182003	0.243340	0.8	0.033319	0.504672
$H^{+}$	Br	0.120325	0.444859	0.8	0.080767	0.596776
$H^{+}$	$NO_3$	0.210638	0.122694	0.8	-0.101736	1.676420
$H^{+}$	$SO_4^{2-}$	0.097108	-0.004307	1.0	0.140598	0.632246
$H^{+}$	HSO <sub>4</sub>	0.313812	-4.895466	1.0	-0.358419	0.807667
Li <sup>+</sup>	Cl <sup>-</sup>	0.106555	0.206370	0.8	0.053239	0.535548
Li <sup>+</sup>	Br	0.106384	0.316480	0.8	0.057602	0.464658
Li <sup>+</sup>	$NO_3$	0.076313	0.300550	0.8	0.046701	0.664928
Li <sup>+</sup>	$SO_4^{2-}$	0.114470	0.035401	0.8	-0.263258	1.316967
Na <sup>+</sup>	Cl <sup>-</sup>	0.053741	0.079771	0.8	0.024553	0.562981
Na <sup>+</sup>	Br	0.180807	0.273114	0.8	-0.506578	2.209050
Na <sup>+</sup>	$NO_3$	0.001164	-0.102546	0.410453	0.002535	0.512657
Na <sup>+</sup>	SO <sub>4</sub> <sup>2-</sup>	0.001891	-0.424184	0.8	-0.223851	1.053620
Na <sup>+</sup>	HSO <sub>4</sub>	0.021990	0.001863	0.8	0.019921	0.619816

1	$\overline{K}^+$	Cl <sup>-</sup>	0.016561	-0.002752	0.8	0.020833	0.670530
	$K^{+}$	Br <sup>-</sup>	0.033688	0.060882	0.8	0.015293	0.565063
	$K^{+}$	$NO_3$	0.000025	-0.413172	0.357227	-0.000455	0.342244
	$K^{+}$	$SO_4^{2-}$	0.004079	-0.869936	0.8	-0.092240	0.918743
	$\mathrm{NH_4}^+$	Cl	0.001520	0.049074	0.116801	0.011112	0.653256
	$\mathrm{NH_4}^+$	Br	0.002498	0.081512	0.143621	0.013795	0.728984
	$\mathrm{NH_4}^+$	$NO_3$	-0.000057	-0.171746	0.260000	0.005510	0.529762
	$\mathrm{NH_4}^+$	$SO_4^{2-}$	0.000373	-0.906075	0.545109	-0.000379	0.354206
	$\mathrm{NH_4}^+$	HSO <sub>4</sub>	0.009054	0.214405	0.228956	0.017298	0.820465
	$\mathrm{Mg}^{2^{+}}$	Cl	0.195909	0.332387	0.8	0.072063	0.397920
	$\mathrm{Mg}^{2^{+}}$	$NO_3$	0.430671	0.767242	0.8	-0.511836	1.440940

-3.425876

0.866923

0.203681

0.8

0.8

0.8

-0.738561

0.072063

-0.075452

0.864380

0.365747

1.210906

 $Mg^{2+}$ 

 $Ca^{2+}$ 

 $Ca^{2+}$ 

2 3

 $SO_4^{2-}$ 

Cl

 $NO_3$ 

0.122364

0.104920

0.163282

Table A4: UNIFAC interaction parameter (E-AIM). Values from Peng et al. (2001) are presented in red.

Organics	CHn	ОН	CH <sub>3</sub> OH	H <sub>2</sub> O	CH <sub>2</sub> CO	СНО	CCOO	НСОО	CH <sub>2</sub> O	СООН
CH <sub>n</sub>	0.0	986.5	697.2	1318.0	476.4	677.0	232.1	507.00	251.5	663.5
ОН	156.4	0.0	-137.1	276.4	84	-203.60	101.1	267.80	28.06	224.39
СН <sub>3</sub> ОН	16.51	249.1	0.0	-181.0	23.39	306.4	-10.72	179.70	-128.60	-202
H <sub>2</sub> O	-89.71	-153.0	289.6	0.0	-195.4	-116.0	72.870	233.87	540.5	-69.29
CH <sub>2</sub> CO	26.76	164.5	108.7	472.5	0.0	-37.36	-213.7	-190.40	-103.60	669.4
СНО	505.7	529.00	-340.2	480.80	128.0	0.0	-110.3	766.00	304.1	497.5
CCOO	114.8	245.40	249.63	200.0	372.2	185.10	0.0	-241.80	-235.7	660.2
НСОО	329.30	139.40	227.80	124.63	385.40	-236.50	1167.0	0.0	-234.00	-268.1
CH <sub>2</sub> O	83.36	237.7	238.40	-314.7	191.10	-7.838	461.3	457.30	0.0	664.00
СООН	315.3	-103.03	339.80	-145.88	-297.8	-165.50	-256.3	193.90	-338.5	0.0

Table A5: UNIFAC Relative Vander Waals group volume  $(R_k)$  and surface area  $(Q_k)$  parameters for solvent groups.

No	Family Name	Main Group	Subgroup	$R_t$	Qt
1	Alkane	$CH_n (n=0,1,2,3)$	CH3	0.9011	0.848
			CH2	0.6744	0.540
			СН	0.4469	0.228
			C	0.2195	0.00
2	Alcohol	ОН	ОН	1.0000	1.20
3	Water	$H_2O$	$H_2O$	0.9200	1.400
4	Methanol	CH <sub>3</sub> OH	CH <sub>3</sub> OH	1.4311	1.432
5	Carbonyl	CH <sub>2</sub> CO	CH <sub>3</sub> CO	1.6724	1.488
			$CH_2CO$	1.4457	1.180
6	Aldehyde	СНО	СНО	0.9980	0.948
7	Acetate	CCOO	CH <sub>3</sub> COO	1.9031	1.728
			CH <sub>2</sub> COO	1.6764	1.420
8	Formate	HCOO	HCOO	1.2420	1.188
9	Ether		$CH_3O$	1.1450	1.088
		$CH_2O$	$CH_2O$	0.9183	0.780
			CH-O	0.6908	0.468
10	Carboxylic acid	СООН	COOH	1.3013	1.224
			НСООН	1.5280	1.532

Table A6: Relative van der Waals subgroup volume ( $R_t^H$ ) and surface area ( $Q_t^H$ ) parameters for cations and anions considering dynamic hydration. Values from AIOMFAC and mod. LIFAC are presented in black and red, respectively.

Ion	ADHN a,b	$R_{t}$	$Q_{t}$	$R^{H c}$	$O_{\cdot}^{H}$ c	Reference
$H^{+}$	1.93	0.0	0.0	1.78	2.70	Zuend et al. (2008)
$Na^+$	0.22	0.18	0.18	0.38	0.62	Zuend et al. (2008)
$K^{+}$	0.00	0.44	0.58	0.440	0.58	Zuend et al. (2008)
$\mathrm{NH_4}^+$	0.00	0.69	0.78	0.69	0.78	Zuend et al. (2008)
$\mathrm{Mg}^{2+}$	5.85	0.06	0.16	5.44	8.35	Zuend et al. (2008)
$Ca^{2+}$	2.10	0.31	0.46	2.24	3.40	Zuend et al. (2008)
$\mathrm{Fe}^{2+}$	0.00	0.90	0.84	0.901	0.84	d
Cu <sup>2+</sup>	0.00	0.13	0.26	0.13	0.26	Kiepe et al. (2006)
$\mathrm{Mn}^{2+}$	0.00	0.90	0.84	0.901	0.84	d
$Zn^{2+}$	2.18	0.12	0.24	2.12	3.29	Kiepe et al (2006)
Cl <sup>-</sup>	0.00	0.99	0.99	0.99	0.99	Zuend et al. (2008)
Br	0.00	1.25	1.16	1.25	1.16	Zuend et al. (2008)
$NO_3^-$	0.00	0.95	0.97	0.95	0.97	Zuend et al. (2008)
HSO <sub>4</sub>	0.00	1.65	1.40	1.65	1.40	Zuend et al. (2008)
$SO_4^{2-}$	1.83	1.66	1.40	3.34	3.96	Zuend et al. (2008)
OH-	2.80	1.16	1.27	3.74	5.196	Kiepe et al. (2006)

$CO_3^{2-}$	0.00	2.06	2.25	2.06	2.26	Kiepe et al. (2006)
$NO_2^-$	0.00	1.52	1.68	1.52	1.6	Kiepe et al. (2006)
Γ	0.00	1.55	1.34	1.55	1.34	Kiepe et al. (2006)
F <sup>-</sup>	5.02	0.29	0.44	4.92	7.45	Kiepe et al. (2006)
HCOO-	0.00	0.901	0.84	0.901	0.84	d
CH <sub>3</sub> COO	0.00	1.74	1.04	1.74	1.0437	Kiepe et al. (2006)
HOOCCH <sub>2</sub> COO	0.00	0.901	0.84	0.901	0.84	d
HOOCC <sub>2</sub> H <sub>4</sub> COO	0.00	0.901	0.84	0.901	0.84	d
HCO <sub>3</sub> -	0.00	0.901	0.84	0.901	0.84	d
CHOCOO-	0.00	0.901	0.84	0.901	0.84	d

The apparent dynamic hydration numbers (ADHN) at 303.15 K and 0.1 M take from Kiriukhin and Collins (2002).

Values of ADHN = 0 are assigned to the ions for which the data is unavailable.

c calculated using Eq. (34) and (35), respectively.

<sup>&</sup>lt;sup>d</sup> ADHN data is not available

## 1 Appendix B: List of symbols, indices and acronyms

# 2 Table B1. List and description of symbols and indices.

Symbol/Index	Description
$a_i$	Activity of species i
$a_{_{A}}$	Activity of compound A
$a_i^k$	Activity of species $i$ in the $k^{th}$ particle/cloud droplet class
$a_w$	Water activity
$a_w^k$	Water activity in the $k^{th}$ particle/cloud droplet class
${ m A}_{(aq)}$	Compound A in the aqueous phase
$A_{(g)}$	Compound A in the gas phase
A	Debye-Hückel parameter
b	Debye-Hückel parameter
$B_{c,a}(I)$	Ionic strength dependent binary interaction coefficient between cations and anions
$b_{k,i}^{(1)}, b_{k,i}^{(2)}, b_{c,a}^{(1)}, b_{c,a}^{(2)}, c_{c,a}^{(1)}, c_{c,a}^{(2)}$	Fitted parameters (AIOMFAC)
$B_{k,i}(I)$	Ionic strength dependent binary interaction coefficient between solvent main groups and ions
c*	Specific cation
$C_{c,a}(I)$	Interaction coefficient between cation $\leftrightarrow$ anion pairs with respect to the total charge concentration
$c^G$	Vector of the concentrations of the gas phase species
$c_i$	Mass concentration of an aqueous phase species i
$c_{i,k}^s$	Saturation vapor mole concentration
$c^G_{i^*}$	<i>i</i> ** <sup>th</sup> gas phase chemical species
$\mathbf{c}^{\mathbf{k}}$	Vector of all concentrations
$c_i^k$	$i^{th}$ aqueous phase chemical species in the $k^{th}$ particle/cloud droplet class
$C_{sol}$	Solute concentration
$c^k_{sol}$	Solute concentration in the $k^{th}$ particle class
$D_i^G$	Gas diffusion coefficient
$F(c_l^1,\ldots,c_l^M)$	Mass transfer between different droplet classes by microphysical processes
$G^{ex}_{LR}$	Long-range (LR) electrostatic interactions contributing to excess Gibbs free energy
$G^{ex}_{MR}$	Middle-range (MR) electrostatic interactions contributing to excess Gibbs free energy
$G^{ex}_{\mathit{SR}}$	Short-range (SR) electrostatic interactions contributing to excess Gibbs free energy
$G^{ex}(p,T,n_j)$	Excess Gibbs energy

Symbol/Index	Description
$\overline{H_i}$	Dimensionless Henry's law constant of species i
$i,i^*$	Species index
I	Identity matrix
I	Ionic strength
j	Species index
J	Approximation of the Jacobian
$k=1,\ldots,M$	Particle/cloud droplet class index
$k_t^{ki}$	Mass transfer coefficient of species $i$ into the $k^{th}$ particle/cloud droplet class
$K_{eq}$	Equilibrium constant
$K_i^H$	Henry's law constant of species i
L	Liquid water content
$L_k$	Liquid water content of the $k^{th}$ droplet class inside the box volume
$m_{\scriptscriptstyle A}$	Molality of compound A
$M_{c}$	Molar mass of carbon
$m_i$	Molality of an aqueous phase species i
$m_i^k$	Molality of dissolved gas phase species $i$ in particle class $k$
$m_{j}$	Molality of the <i>j</i> <sup>th</sup> species
$mol_{sol_i}^k$	Moles of soluble material of the $i^{th}$ species in the the $k^{th}$ particle/droplet class
$M_{sol}$	Mean molar mass of solute
$M_{s}$	Molar mass of solvent s
$mol_w^k$	Molar water fraction
$N_{\scriptscriptstyle A}$	Number of aqueous phase species
$n_a$	Moles of anions
$N_{\scriptscriptstyle t}^{\scriptscriptstyle ADH}$	Dynamic hydration numbers
$n_c n_{c'}$	Moles of cations
$n_{cb}$	Number of carbon atoms
$N_G$	Number of gas phase species
$n_{j}$	Number of moles of component j
p	Total pressure
$p_{i,k}^s$	Saturation vapor pressure of gas phase species $i$ over a particle in size bin $k$
$p_{_{\scriptscriptstyle W}}$	Equilibrium partial pressure of water over the solution droplet
$p_w^o$	Equilibrium water vapor pressure over a flat surface of pure water
$Q_{c,c',a}(I)$	Ternary interaction coefficient involving two different cations
$q_i / r_i$	Surface area / volume of component i

Symbol/Index	Description
$r_{\!\scriptscriptstyle A}$	Reaction rate
$r_{drop}(m)$	Mean wet droplet radius
$r_k$	Droplet radius of the $k^{th}$ particle/cloud droplet class
R	Universal gas constant
$R_{c,c'}(I)$	Binary interaction coefficient involving two different cations
RH	Ambient relative humidity
$R_l^A$	Aqueous phase chemical reaction terms of species <i>l</i> (chemical production and degradation fluxes)
$R_{l^*}^G$	Gas phase chemical reaction terms of species $l^*$ (chemical production and degradation fluxes)
$R_t / Q_t$	Relative van der Waals subgroup volume/surface area parameters
$R_t^H / Q_t^H$	Hydrated group volume and surface area parameters
$R_w / Q_w$	$R_t / Q_t$ values of the water molecule
T(K)	Temperature
$X_w$	Mole fraction of water
$\mathcal{X}_i$	Mole fraction of component <i>i</i>
$Z_i$	Number of elementary charges of ion i
$\{a_i\}$	Thermodynamic activity of species i
$\{A\}$ etc.	Individual thermodynamic activities
$\left\{A_{(aq)}\right\} = m_A \gamma_A$	Activity of an un-dissociated compound
$\left\{A_{(g)}\right\}$	Activity of a gas over a particle surface
$\left\{A_{(s)}\right\} = m_s$	Activity of a solid
$\left\{A^{+}\right\} = m_{A^{+}} \gamma_{A^{+}}$	Activity of an ion in solution
$\left[C^{k} ight]$	Concentration of WSOC (Water Soluble Organic Carbon) in particle class $k$
$\left\{H_2O_{(aq)}\right\} = a_w$	Activity of liquid water in a particle
$lpha_{_i}$	Mass accommodation coefficient of the i <sup>th</sup> species
β	Parameter of the integration method
$\gamma_{\scriptscriptstyle A}$	Activity coefficient of compound A
$\gamma_i$	Molality based activity coefficient of species i
$\gamma_w$	Molality based water activity coefficient
${m \gamma}_j^k$	Activity coefficient of the $j^{th}$ species in the $k^{th}$ particle/droplet class
$\gamma_{\pm}$	Mean activity coefficient
$\gamma_+/\gamma$	Activity coefficients of a cation and anion
$oldsymbol{arepsilon}_{w}$	Static permittivity

Symbol/Index	Description
$\kappa_{_{l}}$	Prefactor of the Henry term (solubility index)
$\lambda_i (= \pm 1)$	Factor +1 for products and -1 for reactants
$\mu$	Time dependent entrainment/detrainment rate
$\mu_i^{(m)}(p,T,n_j)/\mu_i^{(x)}(p,T,n_j)$	Chemical potentials
$V_i$	Molecular speed of gas phase species i
$v_w$	Partial molar volume of water
$ ho_{\scriptscriptstyle w}$	Density
$\sigma_{_w}$	Surface tension of pure water
$\sigma_{\scriptscriptstyle w,s}$	Droplet solution surface tension
$\ln \gamma_i^{SR}$	Short-range activity coefficient $\gamma_j$ of a molecular component $j$ (can be solute
-	or solvent)
$\ln \gamma_i^{SR,(x),\infty}$	Unsymmetrical normalized activity coefficient

## 3 Table B2. List and description of acronyms.

Acronym	Description
ADCHAM	Aerosol Dynamics, gas- and particle-phase chemistry model for laboratory CHAMber studies
ADDEM	Aerosol Diameter Dependent Equilibrium Model
AIM	Aerosol Inorganic Model
GFEMN	Gibbs free energy minimization model
AIOMFAC	Aerosol Inorganic-Organic Mixtures Functional groups Activity Coefficients
BDF	Backward differential formula
CAPRAM	Chemical Aqueous Phase RAdical Mechanism
CSB	Clegg-Seinfeld-Brimblecombe model
E-AIM	Extended Aerosol Inorganic Model 3rd Equilibrium Simplified Aerosol Model (EQSAM3)
EQSAM3	
EQUISOLV II	EQUIlibrium SOLVer version 2 Thermodynamic equilibrium aerosol model (= "equilibrium" in Greek)
ISORROPIA	
ISORROPIA II	Thermodynamic equilibrium aerosol model version 2
LR	Long-range
MADM	Multicomponent Aerosol Dynamics Model
MARS-A	Model for an Aerosol Reacting System - version A

Acronym	Description
MESA	Multicomponent Equilibrium Solver for Aerosols
mod. LIFAC	Modified Liquid Functional Activity Coefficient Model
MOSAIC	MOdel for Simulating Aerosol Interactions and Chemistry
MR	Middle-range
ODE	Ordinary differential equation
SPACCIM	Spectral Aerosol Cloud Chemistry Interaction Model
SpactMod	SPACCIM activity coefficient module
SR	Short-range
TMIs	Transition Metal Ions
UHAERO	Inorganic atmospheric aerosol phase equilibrium model (UHAERO)
UNIFAC	UNIversal Functional-group Activity Coefficients
WSOC	Water Soluble Organic Carbon

2 3 |

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7 8

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# 1 Tables:

35

2 Table 1. Description of activities implemented in SPACCIM.

Activities	Description
Activity of a gas over a particle surface	$\left\{A_{(g)}\right\} = p_{A,s}$
Activity of an un-dissociated compound	$\left\{A_{(aq)}\right\} = m_A \gamma_A$
Activity of an ion in solution	$\left\{A^{+}\right\} = m_{A^{+}} \gamma_{A^{+}}$
Activity of liquid water in a particle	$\left\{H_2 O_{(aq)}\right\} = a_w$
Activity of a solid	$\{A_{(s)}\}=m_{s}$ , i. e., $\gamma_{s}=1$

Gelöscht: Seitenumbruch

# Figures:

Fig. 1: Schematic of the model coupling strategy and its implementation considering the treatment of solution non-ideality and surface tension effects in SPACCIM.

Fig. 2: Scheme of activity coefficients and surface tension used in the microphysics and multiphase chemistry models.

Fig. 3: Sparse structure of Jacobian and two droplet classes [adapted from Wolke et al. (2005)].

Fig. 4: Scheme of the currently used interactions in the MR and SR part. Parameters for ion  $\leftrightarrow$  ion and ion  $\leftrightarrow$  organic main group interactions are all incorporated in the MR part and set to zero in the SR (UNIFAC) part.

Fig. 5: Comparison with measurements of aqueous electrolyte solutions (symbols) and corresponding calculations of the models <u>E-AIM/AIM III</u> (Clegg et al., 1998b), mod. LIFAC (Kiepe et al., 2006), Ming and Russell (Ming and Russell, 2002) and <u>SpactMod</u> at 298 K for the salt NaCl + NH<sub>4</sub>NO<sub>3</sub> at a molar salt mixing ratio of (3:1). Note that <u>SpactMod reproduces</u> the results of <u>AIOMFAC</u> (Zuend et al., 2008) due to the same parameters applied.

Fig. 6: Intercomparison between selected models for Ca(NO<sub>3</sub>)<sub>2</sub> salt: Water activities (solid lines) and mean activity coefficients (dashed lines). Again, SpactMod reproduces AIOMFAC.

Fig. 7: Comparison between experimental and calculated water activities  $(a_w)$  in aqueous citric acid solutions as a function of water fraction  $(x_w)$  at 298.15K. Experimental data are taken from Maffia and Meirelles (2001).

Fig. 8: Comparison between experimental (symbols) and calculated mean activity coefficients (solid lines) of binary salt mixtures as a function of molality (mol kg<sup>-1</sup>) at 298 K.

Experimental data are taken from Hamer and Wu (1972).

Fig. 9: Comparison of modeled water activities for the aqueous solution composed of organic-electrolyte mixture:  $(NH_4)_2SO_4 + Glycerol + H_2O$  [(2:1:1) mole ratio]. The SpactMod results are in agreement with AIOMFAC.

Fig. 10: Comparison between measured and modeled water activities for the aqueous solution composed of organic-electrolyte mixture: (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> + Ethanol + Acetic acid [(2:1:1) mole ratio].

Fig. 11: Importance of different interactions in the aqueous solution composed of NaCl +  $(NH_4)_2SO_4$  + Ethanol + Malonic acid [1:1:1:1 (mole ratio)].

Fig. 12: Modeled activity coefficients of main inorganic particle phase constituents (top) and important transition metal ions (TMIs, down) as the function of the simulation time for the two different relative humidity cases (left: 90% r.h., right: 70% r.h.). The blue bars mark the in-cloud time periods during the simulation time.

 Gelöscht: AIOMFAC (Zuend et al., 2008)

#### [2] verschoben (Einfügung)

[3] nach unten verschoben: Comparison between measured and modeled water activities for the aqueous solution composed of organic-electrolyte mixture: (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> + Ethanol + Acetic acid [(2:1:1) mole ratio].

### Feldfunktion geändert

## [3] verschoben (Einfügung)

**Gelöscht:** Comparison between measured and modeled water activities for the aqueous solution composed of organic-electrolyte mixture: (NH<sub>a</sub>)<sub>2</sub>SO<sub>4</sub> + Ethanol + Acetic acid [(2:1:1) mole ratio].

[2] nach oben verschoben: Comparison between experimental (symbols) and calculated mean activity coefficients (solid lines) of binary salt mixtures as a function of molality (mol kg <sup>-1</sup>) at 298 K. Experimental data from Hammer and Wu (1972).

**Gelöscht:** Comparison of modeled water activities for the aqueous solution composed of organicelectrolyte mixture: (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> + Glycerol + H<sub>2</sub>O [(2:1:1) mole ratio].

Gelöscht: 9

Gelöscht: 0

Fig. 13: Modeled activity coefficients of organic carbonyl compounds (top) and organic acids/anions (TMIs, down) as the function of the simulation time for the two different relative humidity cases (left: 90% r.h., right: 70% r.h.). The blue bars mark the in-cloud time periods during the simulation time.

Fig. 14: Modeled pH values as the function of the simulation time for the two different relative humidity cases (left: 90% r.h., right: 70% r.h.) considering ideal (red line) and

Fig. 14; Modeled pH values as the function of the simulation time for the two different relative humidity cases (left: 90% r.h., right: 70% r.h.) considering ideal (red line) and non-ideal (blue line) solutions, respectively. The blue bars mark the in-cloud time periods during the simulation time.

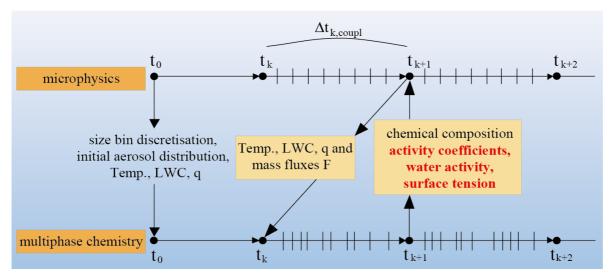
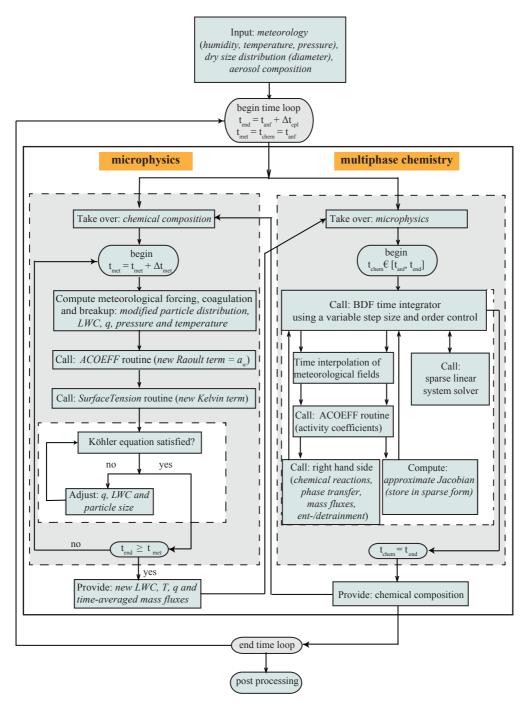


Fig. 1



<sup>1</sup> Fig. 2

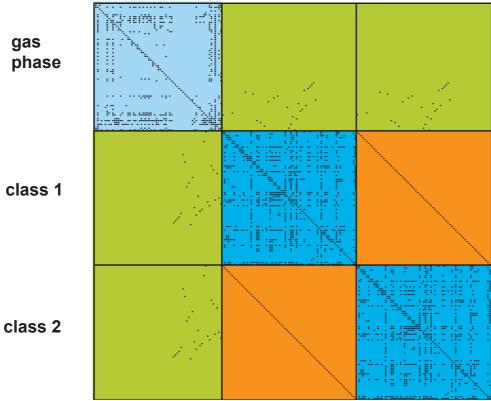


Fig. 3

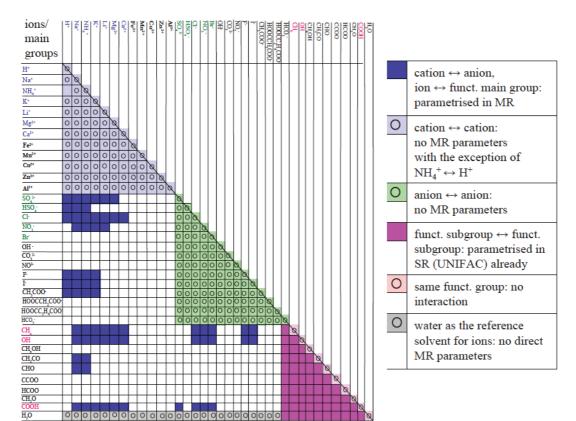


Fig. 4

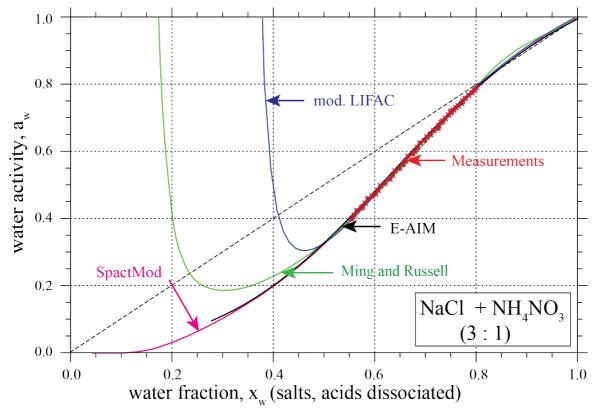


Fig. 5

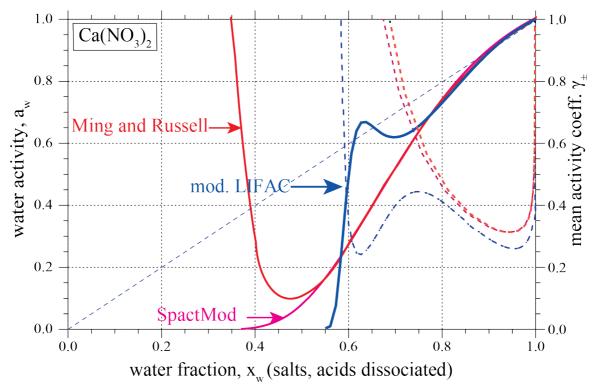


Fig. 6:

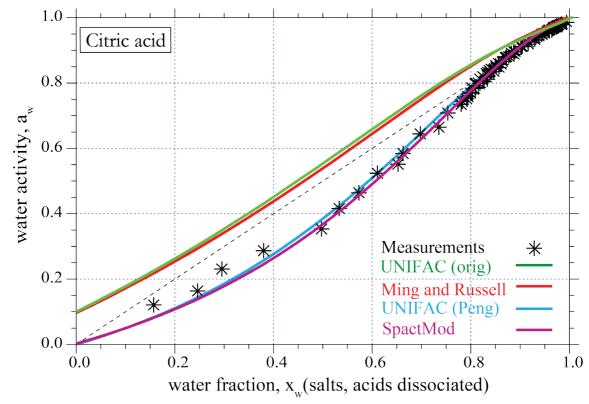


Fig. 7

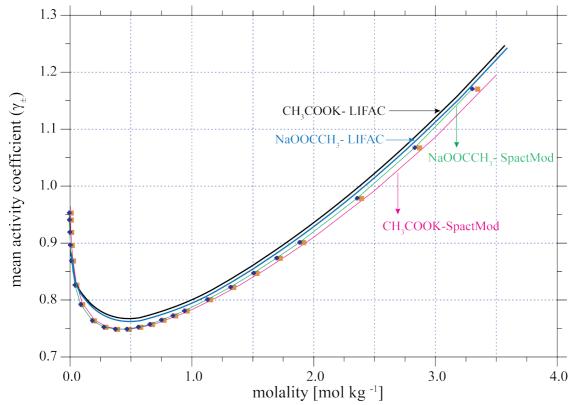


Fig. 8

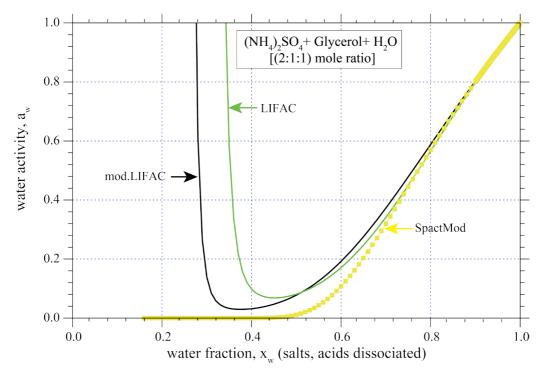


Fig. 9

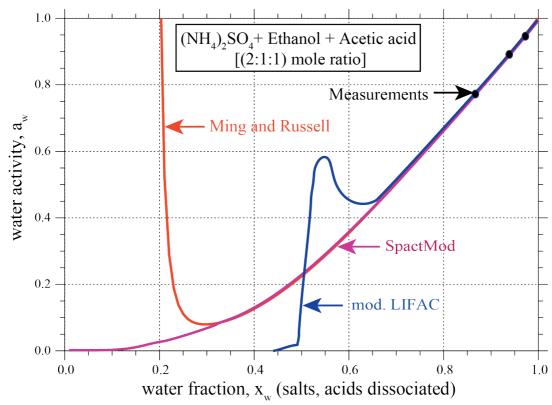


Fig. 10

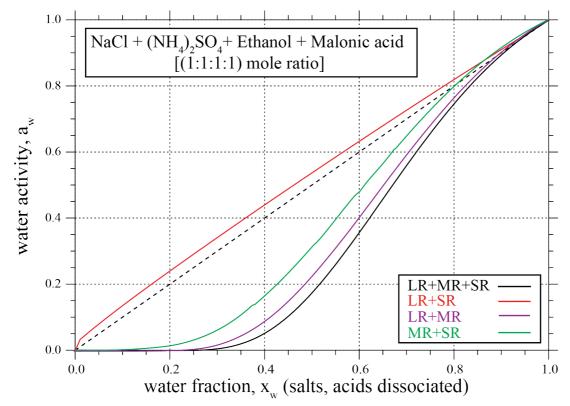


Fig. 11

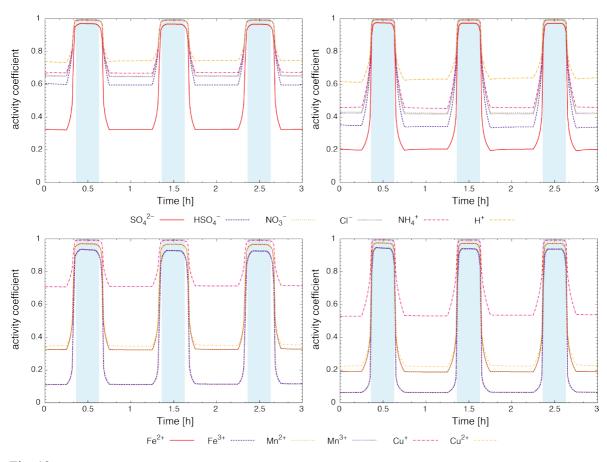


Fig. 12

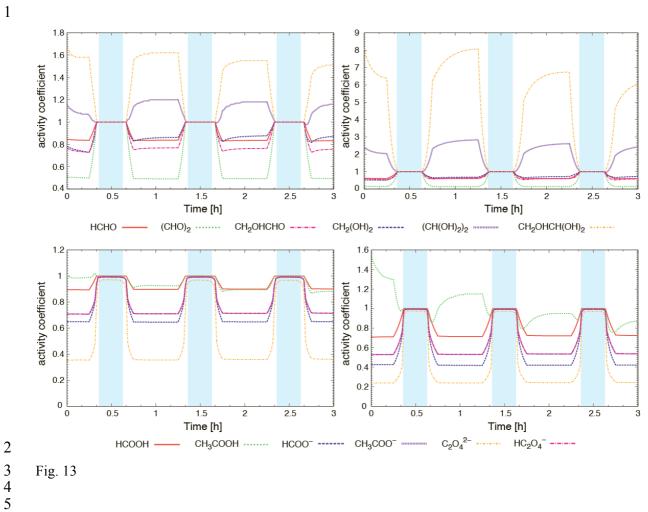


Fig. 13

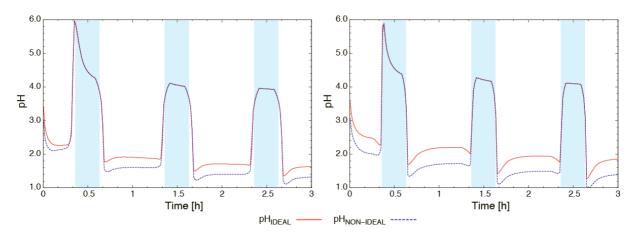


Fig. 14