

Author's Response to all comments:

Response to Anonymous Referee #1

We would first like to thank the anonymous referee for his or her constructive comments. In this response we will try to answer all the comments and the indicated changes will be applied in the revised manuscript below.

Comment 1: Table 3, description of Koppen climate symbols, may not be required. I think giving a reference (e.g., Peel et al., 2007) or minimal description (cf Table 6) is adequate, because this is a classic system.

Reply: We agree that there may be overlap between tables 3 and 6, due to the climate zone descriptions. We therefore will remove the descriptions of the climate zones in table 6 and will leave table 3 for the overall overview. We agree that the Koeppen-Geiger climate classification system is a classical system. However, as the classification system is the basis for our approach of adjusting erosivity, we think we should provide the descriptions of the climate zones for a better readability of the paper.

Comment 2: In Tables 4 and 5, can you add units for variables (e.g., P and z)?

Reply: We included the units.

Response to Anonymous Referee #3

We would first like to thank the anonymous referee for his or her constructive comments. In this response we will try to answer all the comments and the indicated changes will be applied in the revised manuscript below.

Comment 1: In section 3.3 it would be helpful to actually state the climate zones rather than use the letters as many people may not be up-to-date with the classification system. For example, rather than state the "For the Ds climate zones", the "f climate zones", or the E climate zones", state the cold climates (D) or the climates without dry seasons etc. This I believe would improve the readability and uptake of this particular section. This comment applies throughout the text where climates are mentioned (for example the Csb climate on line 453, or E zones line 485).

Reply: We agree that this would add clarity, and will state the climate zones explicitly in the text.

Comment 2: Specifically for the paragraph from Lines 468-493. First, it is stated that (line 469) that the other RUSLE factors (K and C) and the way they interact with each other are not adjusted the global scale. I would suggest that what is probably most important is the interaction of C and R and possibly even a recommendation for future models would be a monthly time step combining C and R at the global scale. This interaction is far more important than K and C and would be fundamental to improving the incorporation of the C factor in global models with improved R factor data. Second, the manuscript states that (Line 481) land management is not accounted for in the study. Often land management in RUSLE research is incorporated through the cover factor, particularly for different agricultural land uses. Maybe this is a limitation of the NDVI approach. These limitations are related but they are presented as being separate. I do think this section requires some work to be a bit more consistent with the research on the C factor and the importance of timing the C factor with the R factor in future applications.

Reply: These suggestions are very good, and we include these in the text. We edit the above mentioned sections and the conclusions with regard to the importance of adjusting the C factor and the role of land management.

Minor and minor editorial comments are all addressed in the revised manuscript (see below).

Comments from the editor are also addressed. We tried to shorten the sentences and make the text in general better readable. The figures are adjusted according to the suggestions of the editor.

1 **REVISED MANUSCRIPT**

2

3 **Improving the global applicability of the RUSLE model –**
4 **Adjustment of the topographical and rainfall erosivity factors**

5

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11

12 **Abstract**

13 Large uncertainties exist in estimated rates and the extent of soil erosion by surface runoff on a
14 global scale, ~~and t~~ This limits our understanding of the global impact that soil erosion might have
15 on agriculture and climate. The Revised Universal Soil Loss Equation (RUSLE) model ~~is~~, due to
16 its simple structure and empirical basis, ~~is a~~ frequently used tool in estimating average annual
17 soil erosion rates at regional to global scales. However, large spatial scale applications often rely
18 on coarse data input, which is not compatible with the local scale ~~at-on~~ which the model is
19 parameterized. ~~This Our~~ study ~~aimed aims~~ at providing the first steps in improving the global
20 applicability of the RUSLE model in order to derive more accurate global soil erosion rates.

21 We adjusted the topographical and rainfall erosivity factors of the RUSLE model and compared
22 the resulting ~~soil~~ erosion rates to extensive empirical databases ~~on soil erosion~~ from the USA and
23 Europe. ~~Adjusting the topographical factor required~~ By scaling ~~of the~~ slope according to the
24 fractal method ~~to adjust the topographical factor, which resulted in~~ we managed to improve ~~the~~
25 topographical detail in a coarse resolution global digital elevation model.

Comment [VN1]:

Minor editorial comment [2]: Reviewer #3: The sentence with the required scaling of slope is a bit awkward. Although it is not necessary the authors may want to enhance this important sentence of their abstract for improved readability

Reply: We edited to sentence to improve the readability

26 Applying the linear multiple regression method to adjust rainfall erosivity for various climate
27 zones, resulted in values that compared well to high resolution erosivity data for different
28 regions. However, this method needs to be extended to tropical climates, for which erosivity is
29 biased due to the lack of high resolution erosivity data.

30 After applying the adjusted and the unadjusted versions of the RUSLE model on a global scale
31 we find that the adjusted ~~RUSLE model not only~~version shows a global higher mean ~~soil~~ erosion
32 rate ~~but also~~and more variability in ~~the soil erosion~~the erosion rates. Comparison to empirical
33 datasets of the USA and Europe shows that the adjusted RUSLE model is able to decrease the
34 very high erosion rates in hilly regions that are observed in the unadjusted RUSLE model results.
35 Although there are still some regional differences with the empirical databases, the results
36 indicate that the methods used here seem to be a promising tool in improving the applicability of
37 the RUSLE model on a coarse resolution on global scale.

38

39 1 Introduction

40 For the last centuries to millennia soil erosion by surface runoff is being accelerated globally due
41 to human activities, such as deforestation and agricultural practices (Bork and Lang, 2003).
42 Accelerated soil erosion is a process that triggers land degradation in the form of nutrient loss, a
43 decrease in the effective root depth, water imbalance in the root zone and finally also
44 productivity reduction (Yang et al., 2003). It is widely recognized that soil erosion ~~is~~ has been a
45 major threat to sustainable agriculture and food production across the globe ~~since the start of~~
46 ~~agricultural activities (UNCCD, 2012, Walling, 2009)~~for many decades. These effects of soil
47 erosion are currently exacerbated by the global population growth and climatic changes.
48 Organizations such as the United Nations Convention to Combat Desertification (UNCCD) try to
49 address this problem by stating a new goal for Rio +20 of zero land degradation (UNCCD,
50 2012).

51 Another aspect underpinning the relevance of soil erosion on the global scale is the effect of ~~soil~~
52 erosion on ~~the~~ global nutrient cycles. Recently, the biogeochemical components of Earth System
53 Models (ESMs) became increasingly important in predicting the global future climate (Thornton
54 et al., 2007; Goll et al., 2012). Not only the global carbon cycle but also other nutrient cycles
55 such as the nitrogen (~~N~~) and phosphorous (~~P~~) cycles cannot be neglected in ESMs anymore (Goll

Comment [VN2]:

Minor comment [1]: Reviewer #3: The authors state that it is widely recognized that soil erosion is a major threat to sustainable agriculture though they do not provide a references – further the sentence is awkward with the many decades is seemingly attached at the end. Is “the decades” a reference to the past or the future (and hence why references may help with this statement).

Reply: We adjusted the sentence and proved some references

56 | et al., 2012; Gruber and Galloway, 2008; Reich et al., 2006). Soil erosion may have a significant
57 | impact on these nutrient-biogeochemical cycles through lateral fluxes of sediment, but the impact
58 | on the global scale is still largely unknown. For example, Quinton et al. (2010) showed that
59 | erosion can significantly alter the nutrient and carbon cycling, and result in lateral fluxes of
60 | nutrients that are similar in magnitude as fluxes induced by fertilizer application and crop
61 | removal. Regnier et al. (2013) looked at the effect of human induced lateral fluxes of carbon
62 | from land to ocean and concluded that human perturbations, which include soil erosion, may
63 | have enhanced the carbon export from soils to inland waters.

64 | In general, the effect of soil erosion on the global carbon cycle has received considerable
65 | attention after the pioneering work of Stallard (1998), who proposed that global soil erosion can
66 | result in sequestration of carbon by soils. After his work, the effect of soil erosion on the carbon
67 | cycle has been studied extensively, but there remains a large uncertainty in the effect of soil
68 | erosion on the carbon cycle. For example, several recent global assessments of the influence of
69 | soil erosion on the carbon cycle indicate a large uncertainty with a range from a source of 0.37 to
70 | 1 Pg C year⁻¹ to a net uptake or sink of 0.56 to 1 Pg C year⁻¹ (van Oost et al., 2007). Thus, in
71 | order to better constrain the global carbon budget and to identify optimal management strategies
72 | for land use, it is essential to have accurate estimates of soil erosion and its variability on a
73 | global scale.

74 | Currently, ~~however~~, there exists a large uncertainty in the global soil erosion rates as can be seen
75 | from recent studies that show rates between 20 and 200 Pg year⁻¹ (Doetterl et al., 2012). This
76 | indicates that modelling soil erosion on a global scale is still a difficult task due to the very high
77 | spatial and temporal variability of soil erosion. Different approaches were previously applied to
78 | estimate soil erosion on a large or global scale. Most of these approaches are based on
79 | extrapolated data from agricultural plots, sediment yield or extrapolated river sediment estimates
80 | (Milliman and Syvitski, 1992, Stallard, 1998, Lal, 2003, Hooke, 2000, Pimentel et al., 1995,
81 | Wilkinson and McElroy, 2007).

82 | An alternative approach is based on the use of soil erosion models, in order to be able to predict
83 | also past and future soil erosion rates. One of the most applied models to estimate soil erosion on
84 | a large spatial scale is the semi-empirical/process-based Revised Universal Soil Loss Equation
85 | (RUSLE) model (Renard et al., 1997). This model stems from the original Universal Soil Loss

86 Equation (USLE) model developed by USDA (USA Department of Agriculture), which is based
87 on a large set of experiments on soil loss due to water erosion from agricultural plots in the
88 United States (USA). These experiments covered a large variety of agricultural practices, soil
89 types and climatic conditions, making it a potentially suitable tool on a regional to global scale.
90 The RUSLE model predicts the average annual soil erosion rates by rainfall and is formulated as
91 a product of a rainfall erosivity factor (R), a slope steepness factor (S), a slope length factor (L), a
92 soil erodibility factor (K), a ~~crop-land~~ cover factor (C) and a support practice factor (P). The
93 RUSLE model was first applied on a global scale by Yang et al. (2003) and Ito (2007) for
94 estimating the global soil erosion potential. ~~and~~ Various limitations ~~were observed~~
95 ~~to~~when applying ~~the~~this RUSLE model on ~~the~~ global scale. Firstly, the model is originally
96 developed to be applicable on the agricultural plot scale. ~~This makes the model, which is not~~
97 ~~in~~compatible with the coarse spatial scale of global datasets on soil erosion influencing factors
98 such as precipitation, elevation, land-use and soil characteristics. Secondly, the RUSLE and
99 USLE models were parameterized for environmental conditions of the United States (USA), and
100 are thus not directly applicable to other areas in the world. Thirdly, only sheet and rill erosion are
101 considered. ~~and~~ Finally, the RUSLE model does not contain sediment deposition and sediment
102 transport terms, which are closely linked to soil erosion.

103 ~~However,~~ the RUSLE model is to our knowledge one of the few erosion models that has the
104 potential to be applied on a global scale due to its simple structure and empirical basis.
105 Therefore, it is of key importance to address the above mentioned limitations first.

106 To address the first two limitations, Van Oost et al. (2007) presented in their work a modified
107 version of the USLE model for application on agricultural areas on a global scale. They based
108 their model on large-scale experimental soil erosion data from the USA (National Resource
109 Inventory, NRI database, USDA, 2000) and Europe, by deriving reference factors for soil
110 erosion on agricultural land and for certain RUSLE parameters. They also introduced a
111 procedure to scale slope, which is an important parameter in the topographical factors S and L of
112 the USLE/RUSLE model. In this scaling procedure slope was scaled from the GTOPO30 1km
113 resolution digital elevation model (USGS, 1996) to the coarser resolution of the erosion model.
114 This method was based on high resolution OS Ordnance (10m resolution) and SRTM data on
115 elevation (90m resolution, International Centre for Tropical Agriculture (CIAT), 2004) for
116 England and Wales.

117 Doetterl et al. (2012) showed that together with the *S* factor, the rainfall erosivity or *R* factor
118 explain up to 75 % of the erosion variability across agricultural areas at the large watershed
119 scale. ~~These, as these~~ factors represent the triggers for soil erosion by providing energy for soil to
120 erode. They ~~*S* and *R* factors~~ can also be seen as the natural components of the RUSLE model, as
121 they ~~have include~~ very little or no modification by human activities (Angulo-Martínez et al.,
122 2009) apart from indirect effects on precipitation and extreme events due to anthropogenic
123 climate change ~~that are included in the *R* factor~~. In this way they represent the natural
124 environmental constraints to soil erosion that are important to capture before the effect of human
125 activities on soil erosion through land use change can be investigated.

126 Previous studies on global soil erosion ~~estimated-calculated~~ the global *R* factor based on the total
127 annual precipitation (Renard and Freimund, 1994). ~~This method is different from the method~~
128 ~~presented in the original RUSLE model (Renard et al., 1997), which is mainly based on 30~~
129 ~~minute precipitation intensity. The reason for the method of Renard and Freimund is due to~~ the
130 lack of high resolution precipitation intensity on a global scale. However, high resolution
131 precipitation intensity is an important explaining parameter of the *R* factor and therefore, the
132 applicability of ~~this-the~~ method ~~of Renard and Freimund~~ is limited.

133 The overall objective of ~~this-our~~ study is to extend the applicability of the RUSLE model to a
134 coarse resolution at ~~a~~ global scale, in order to ~~make the model compatible with ESMs. This~~
135 ~~would~~ enable future studies on the effects of soil erosion for the past, current and future climate.

136 To this end, we develop generally applicable methods that improve the estimation of slope and
137 climatic factors from coarse resolution global datasets. These methods should not only be
138 applicable across agricultural areas as in the studies of Van Oost et al. (2007) and Doetterl et al.
139 (2012), but also across non-agricultural areas. We adjust the *S* factor to the coarse resolution of
140 the global scale based on the scaling of slope according to the fractal method. The adjustment of
141 the *R* factor to the global scale is based on globally applicable regression equations. ~~We derived~~
142 ~~these regression equations~~ for different climate zones ~~that include~~ ~~based on~~ parameters for
143 precipitation, elevation and the simple precipitation intensity. This approach is validated using
144 several high resolution datasets on the *R* factor. Finally, the effects of these adjustments of both
145 factors on global soil erosion rates are investigated separately and tested against independent
146 estimates of soil erosion from high resolution and high precision datasets of Europe and the
147 USA.

148

149 2. Adjustment of the topographical factor

150 2.1 Scaling slope according to the fractal method

151 The topographical factors of RUSLE are the slope steepness factor (S) and a slope length factor
152 (L). The S factor is generally computed by the continuous function of Nearing (1997):

$$153 S = 1.5 + \frac{17}{1 + e^{(2.3 - 6.1 * \sin \theta)}} \quad (1)$$

154 And the L factor is computed according to Renard et al. (1997):

$$155 L = \left(\frac{l}{22.13} \right)^m \quad (2)$$

$$156 \text{ where: } m = \frac{F}{1+F} \text{ and } F = \frac{(\sin \theta / 0.0896)}{(3 * (\sin \theta)^{0.8} + 0.56)} \quad (3)$$

157 in which θ is the slope and l is the slope length in meters.

158 As seen in the equations ~~of the L and S factors 1-3~~, slope is a crucial parameter and thus an
159 accurate estimation is essential in deriving accurate estimates of the L and S factors ~~and finally~~
160 ~~also the~~ soil erosion rates. For an accurate estimation of the slope, ~~the~~ input elevation data from
161 digital elevation models (DEMs) should capture the detailed spatial variability in elevation.
162 However, global DEMs are often too coarse to capture the detailed topography because of the
163 surface smoothing effect. To account for this problem it is assumed that topography is fractal.
164 Following Klinkenberg and Goodchild (1992) and Zhang et al. (1999), slope can be expressed as
165 a function of the spatial scale by applying the variogram equation. The variogram equation is
166 used to approximate the fractal dimension of topography and is expressed as follows:

$$167 (Z_p - Z_q)^2 = k d_{pq}^{4-2D} \quad (4)$$

168 so that:

$$169 \frac{|Z_p - Z_q|}{d_{pq}} = \alpha d_{pq}^{1-D} \quad (5)$$

170 where Z_p and Z_q are the elevations at points p and q , d_{pq} is the distance between p and q , k is a
171 constant, $\alpha = k^{0.5}$, and D is the fractal dimension. Because the left side of Eq. (5) represents the
172 slope, it can be assumed that the slope (θ) is related to the spatial scale or the grid size (d) in:

173 $\theta = \alpha d^{1-D}$ (6)

174 This result implies that by calculating the fractal properties (D and α) Eq. (6) can be used to
175 calculate slope at any ~~specified scale d specified d~~ . The local fractal dimension (D) describes the
176 roughness of the topography while the local value of α is related to the concept of lacunarity,
177 which is a measure of the size of “gaps” (valleys and plains) in the topography (Zhang et al.,
178 2002). To estimate the spatial variations of ~~the fractal dimension D and the fractal coefficient α~~ ,
179 Zhang et al. (1999) proposed to relate these parameters to the standard deviation of elevation.
180 Hereby it is assumed that the standard deviation of elevation does not change much with the
181 DEM resolution. D is then calculated as a function of the standard deviation (σ) in a 3 x 3 pixels
182 moving window as proposed by Zhang et al. (1999):

183 $D = 1.13589 + 0.08452 \ln \sigma$ (7)

184 To estimate α we used the modified approach by Pradhan et al. (2006), ~~who They~~ derived α
185 directly from the steepest slope in a 3 x 3 pixels moving window, called $\alpha_{steepest}$ in the following.
186 Having obtained $\alpha_{steepest}$ and D from a grid at a given resolution, the scaled slope (θ_{scaled}) for a
187 target grid resolution (d_{scaled}) is obtained by:

188 $\theta_{scaled} = \alpha_{steepest} d_{scaled}^{1-D}$ (8)

189 Pradhan et al. (2006) also showed that in their case study the ideal target resolution for
190 downscaling slope was 150_m. This is due to the breakdown of the unifractal concept at very fine
191 scales, which ~~they was showed shown~~ to happen at a scale of 50_m. Altogether, this fractal
192 method shows that a high resolution slope can be obtained from a low resolution DEM as is
193 needed by the RUSLE model.

194

195 2.2 Application of the fractal method on global scale

196 In this study, we investigate the performance of the fractal method on a global scale using
197 different global DEMs as a starting point. The target resolution of downscaling is put to 150m
198 (about 5 arc-second) according to Pradhan et al. (2006). It should be noted that the original
199 spatial scale ~~that on which~~ the original RUSLE and USLE models are operating, ~~on~~ is usually

200 | between 10 and 100_m, which indicates that the 150_m target resolution may be still too coarse
201 | for a correct representation of slope. The DEMs that are used here are given in Table 1.

202 | As reported in previous studies (Zhang et al., 1999; Chang and Tsai, 1991; Zhang and
203 | Montgomery, 1994), the average slope decreases with decreasing DEM resolution. This confirms
204 | the expectation of loss of detail in topography at lower DEM resolutions. A large difference is
205 | found between the unscaled global average slope ~~of from~~ the 5 arc-minute and the 30 arc-second
206 | DEMs, which is in the order of 0.017 m m⁻¹ or 74 % (Table 2). After applying the fractal
207 | method, the scaled slopes ~~at 150 m target resolution of from all the~~ DEMs ~~at 150 m target~~
208 | ~~resolution are all~~ increased significantly compared to the unscaled slopes (Fig. 1). However,
209 | there is still a difference of about 0.05 m m⁻¹ or 8.5 % between the scaled slopes ~~of from~~ the 5
210 | arc-minute and the 30 arc-second DEMs (Table 2). This difference can be attributed to several
211 | factors. One factor could be the underlying assumption that the standard deviation of elevation
212 | (σ) is independent of the DEM resolution. Although σ does not change much when considering
213 | different resolutions, there is still a general decrease in mean global σ when going from the 5 arc-
214 | minute to the 30 arc-second DEM (Table 2). Due to the dependence of the fractal dimension (D)
215 | on σ (Zhang et al., 1999), a decrease of σ leads to a decrease in D and therefore an increase in the
216 | scaled slope. Other factors that could play a role here are the dependence of $\alpha_{steepest}$ on the
217 | steepest slope, and the breakdown of the fractal method at certain scales and in certain
218 | environments. Zhang et al. (1999) mentioned that the scaling properties of slope are affected in
219 | very coarse resolution DEMs if σ changes considerably. On the other hand, Pradhan et al. (2006)
220 | mentioned the breakdown of the fractal method at very fine scales. This can indicate that the 150
221 | m target resolution is not appropriate for some topographically complex regions in the world
222 | ~~when downscaling from the DEMs used in this study. Or based on the limitation of the fractal~~
223 | ~~method or~~, as addressed by Zhang et al. (1999), the DEMs used in this study are too coarse to
224 | scale down the slope to 150_m accurately ~~for these regions~~.

225 | After applying the fractal method on a 30 arc-second resolution DEM, the scaled slope shows a
226 | clear increase in detail, while the unscaled slope shows a strong smoothing effect (Fig. 2A and
227 | 2B). It is found that after scaling the slope values range from 0 to 85 degrees and are less than 2
228 | degrees in 80_% of the area. In contrast, all slope values are less than 45 degrees and range

229 | between 0 and 2 degrees in 89% of this area when slope is computed directly from the 30 arc-
230 second DEM.

231 The scaled slope from the 30 arc-second DEM will be used in this study to estimate the global
232 soil erosion rates by the RUSLE model.

233

234 **3. Adjustment of the rainfall erosivity factor**

235 **3.1 The approach by Renard and Freimund (1994)**

236 Rainfall erosivity (R factor) is described by Hudson (1971) and Wischmeier and Smith (1978) as
237 | the result of the transfer of the kinetic energy of raindrops to the soil surface. This causes a
238 | detachment of soil and the downslope transport of the soil particles, depending on the amount of
239 energy, rainfall intensity, soil type and cover, topography and management (Da Silva, 2004). The
240 original method of calculating erosivity is described by Wischmeier and Smith (1978) and
241 Renard et al. (1997) as:

$$242 \quad R = \frac{1}{n} * \sum_{j=1}^n \sum_{k=1}^{m_j} (EI_{30})_k \quad (9)$$

243 where n is the number of years of records, m_j is the number of storms of a given year j , and EI_{30}
244 is the rainfall erosivity index of a storm k . The event's rainfall erosivity index EI_{30} (MJ mm ha^{-1}
245 | hour^{-1}) is defined as:

$$246 \quad EI_{30} = I_{30} * \sum_{r=1}^m e_r v_r \quad (10)$$

247 where e_r and v_r are, respectively, the unit rainfall energy ($\text{MJ ha}^{-1} \text{mm}^{-1}$) and the rainfall depth
248 (mm) during a time period r , and I_{30} is the maximum rainfall intensity during a time period of 30
249 | minutes (mm hour^{-1}). The unit rainfall energy, e_r , is calculated for each time period as:

$$250 \quad e_r = 0.29 * (1 - 0.72 * e^{-0.05 * i_r}) \quad (11)$$

251 | where i_r is the rainfall intensity during the time period (mm hour^{-1}).

252 The information needed to calculate the R factor according to the method of Wischmeier and
253 Smith (1978) is difficult to obtain on a large spatial scale or in remote areas. Therefore, different
254 studies have been done on deriving regression equations for the R factor (Angulo-Martinez et al.,
255 2009, Meusburger et al., 2012, Goovaerts, 1999, Diodato and Bellocchi, 2010). Most of these

256 studies, however, concentrate on a specific area and can therefore not be implemented on the
257 global scale. Studies on global soil erosion estimation by the RUSLE model or a modified
258 version of it (Doetterl et al., 2012, van Oost et al., 2007, Montgomery ~~et al.~~, 2007, Yang et al.,
259 2003) have all used the method of Renard and Freimund (1994). Renard and Freimund related
260 the R factor to the total annual precipitation based on erosivity data available for 155 stations in
261 the USA, shown in the following equations:

$$262 \quad R=0.0483*P^{1.61}, \quad P \leq 850 \text{ mm}$$

$$263 \quad R=587.8-1.219*P+0.004105*P^2, \quad P > 850 \text{ mm} \quad (12)$$

264 To test how this method performs globally, ~~first we calculated~~ the R factor ~~was calculated in this~~
265 ~~study~~ according to the method of Renard and Freimund (Eq. 12) ~~first. Here we used using~~ the
266 0.25 degree resolution annual precipitation data from the [Global Precipitation Climatology](#)
267 [Center \(GPCC\)](#) product (Table 1). Then, ~~we selected~~ three regions ~~were selected~~ to validate the
268 resulting R values and their variability: the USA (EPA, 2001), Switzerland (Meusburger et al.,
269 2011), and the Ebro basin in Spain (Angulo-Martinez et al., 2009). For these regions high
270 resolution erosivity data are available obtained from pluviographic data from local
271 meteorological stations across the whole region.

272 Figure 3 shows that the R values computed with the Renard and Freimund method strongly
273 overestimate R when compared to the high resolution R data of the selected regions. For the USA
274 the R factor of Renard and Freimund shows an overall overestimation for western USA and for a
275 large part of eastern USA when compared to the high resolution R (Table 7 and Fig. 3A).
276 Especially a strong overestimation is seen for the north-west coast of the USA. This region is
277 known to have complex rainfall patterns due to the presence of mountains and high local
278 precipitation intensities with frequent snow fall (Cooper, 2011). It should be noted that the USA
279 is not a completely suited case study for testing the R values computed with the Renard and
280 Freimund method, as this method is based on [climate](#) data from stations in the USA. The
281 available high resolution ~~or observed~~ data on the R factor from Switzerland and the Ebro basin
282 are better suited for an independent validation.

283 For Switzerland, which has a complex precipitation variability influenced by the relief of the
284 Alps (Meusburger et al., 2012), the R factor of Renard and Freimund shows a strong overall
285 overestimation when compared to the ~~observed or~~ high resolution R values (Table 7 and Fig.

286 3B). For the Ebro basin located in Spain, the observed R data were available for the period 1997-
287 2006 from Angulo-Martinez et al., 2009. Also here the method of Renard and Freimund
288 overestimates the R factor and is not able to ~~model-reproduce~~ the high spatial variability of the R
289 data (Table 7 and Fig. 3C).

290

291 3.2 The linear multiple regression approach using environmental factors

292 To better represent the R factor on a global scale, the R estimation was based on the updated
293 Köppen-Geiger climate classification (Table 3 and Fig. 4). The Köppen-Geiger climate
294 classification is a global~~ly~~ climate classification and is based on the vegetation distribution
295 connected to annual cycles of precipitation and temperature (Lohmann et al., 1993). The reason
296 for this approach is that this classification system includes annual cycles of precipitation and is
297 thus indirectly related to precipitation intensity. Based on this, it is possible to derive regression
298 equations for the R factor that are applicable for each individual climate zone of the
299 classification. This provides a basis to calculate the R factor with coarse resolution data on a
300 global~~ly~~ scale.

301 As a basis for deriving the regression equations for the R factor ~~we used for most climate zones~~
302 ~~the~~ high resolution R maps of the USA from EPA (2001) ~~were used~~. The USA covers most of the
303 world's climate zones and is also the largest region with available high resolution R data. Linear
304 multiple regression was used to adjust R :

$$305 \log(R_i) = \beta_0 + \sum_{j=1}^n \beta_{i_j} * \log(X_{i_j}) + \varepsilon_i, \text{ for } i = 1, 2, \dots, n \quad (13)$$

306 where X is the independent explanatory variable, j is the number of explanatory variables, β is a
307 constant, and ε is the residual.

308 The regression operates on one or more of the following parameters (X_j): total annual
309 precipitation (GPCC 0.25 degree product), mean elevation (ETOPO 5 DEM), and the simple
310 precipitation intensity index, SDII. It should be mentioned that the SDII was only available on a
311 very coarse resolution of 2.5 degree resolution for certain regions on earth, such as parts of
312 Europe and the USA. The SDII is calculated as the daily precipitation amount on wet days (≥ 1
313 mm) in a certain time period divided by the number of wet days in that period. Previous studies
314 that performed regression of R showed that precipitation and elevation were in most cases the

315 only explanatory variables (Meusburger et al., 2012, Mikhailova et al., 1997, Goovaerts, 1999,
316 Diodato and Bellocchi, 2010, Angulo-Martinez et al., 2009). Here, we added to the regression
317 the SDII ~~is added~~ as it is a simple representation of precipitation intensity, which is an important
318 explaining variable of *R* factor. The precipitation and SDII datasets were rescaled to a 5 arc-
319 minute resolution (corresponding to 0.0833 degree resolution) to match the Köppen-Geiger
320 climate classification data that was available at the resolution of 6 arc-minute (corresponding to
321 0.1 degree). Furthermore, high resolution erosivity data from Switzerland (Meusburger et al.,
322 2011) and annual precipitation from the GPCP 0.5 degree product were used to derive the
323 regression equations for *R* factor for the polar (E) climate ~~zones, which~~ These climate zones are
324 not present in the USA. For the rest of the climate zones that were not present in the USA it was
325 difficult to obtain high resolution erosivity data. Therefore, we maintained the method of Renard
326 and Freimund for those climate zones ~~the method of Renard and Freimund was maintained~~ to
327 calculate erosivity. Also, we kept the *R* factor of the Renard and Freimund method if no clear
328 improvement of the *R* factor ~~was~~ found when using the new regression equations for a specific
329 climate zone, ~~the *R* factor of Renard and Freimund is kept~~. Here, we mainly used the r^2 combined
330 with the residual standard error to evaluate if the new regression equations showed a clear
331 improvement in the *R* factor. ~~From the climate zones where high resolution erosivity data was~~
332 ~~available, the Renard and Freimund *R* factors were kept for~~ the hot arid climate zone (BWh)
333 and the temperate climate zone with a hot summer (Csa) in the USA ~~the BWh and Csa climate~~
334 ~~zones~~. These are just two climate zones out of the 17 evaluated ones, which shows that ~~the~~
335 ~~regression method performs better than~~ the ~~old Renard and Freimund method~~ performs as good
336 as or slightly better than the regression method ~~in most cases~~. All datasets for deriving the *R*
337 factor are described in Table 1.

338

339 3.3 Application of the linear multiple regression method on a global scale

340 Tables 4 and 5 show the resulting regression equations for climate zones for which we found
341 initially a low correlation was found between the *R* values calculated by the method of Renard
342 and Freimund and the high resolution ~~or observed~~ *R* values from ~~the maps of~~ EPA (2001) and
343 Meusburger et al. (2011). Figure 5 shows for each addressed climate zone how the method of
344 Renard and Freimund and the new regression equations compare to the observed high resolution

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Comment [VN3]:

Minor comment [2]: Reviewer #3: It states "previous studies that performed regression" though no citations are listed. Please provide some citations.

Reply: We added some citations

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345 *R* of the USA. ~~For the cold climate zones with a dry summer (Ds) climate zones~~ the new
346 regression equations showed only a slight improvement as compared to the method of Renard
347 and Freimund. Also for the polar climate zones (E) ~~climate zones~~ the new regression equations
348 still showed a significant bias. However, they performed much better compared to the method of
349 Renard and Freimund. For most of the addressed climate zones the simple precipitation intensity
350 index (SDII) ~~explained~~ explains a large part of the variability in the *R* factor. The elevation
351 ~~played~~ plays a smaller role here. Elevation can be an important explaining variable in regions
352 with a high elevation variability, which then affects the precipitation intensity.

353 ~~Furthermore, from~~ Table 4 and Table 6 it can be concluded that the *R* factor in climate zones
354 without a dry season (f) ~~climate zones, which have no dry season,~~ can be easily explained by the
355 total annual precipitation and the SDII. Dry climate zones, especially dry summer climate zones
356 showed a weaker correlation, which is most probably due to the fact that the SDII is too coarse to
357 explain the variability in the low precipitation intensity in the summer. It is also interesting to see
358 that even though the SDII was derived from a very coarse resolution dataset, it turned out to be
359 still important for deriving more accurate *R* values.

360 ~~Furthermore, Table 6~~ We also show showed for each addressed climate zone a comparison of the
361 newly computed average *R* factor with the average observed high resolution *R* factor, and the
362 uncertainty range (Table 6). The uncertainty range was computed by taking into account the
363 standard deviation of each of the parameters in the regression equations. As mentioned before,
364 the polar climate zones (E) ~~climate zones~~ showed the largest uncertainty range. The new
365 regression equations significantly improved the *R* values and spatial variability in the western
366 USA, and lead to a mean average *R* factor that was closer to the data mean (Table 7 and Fig.
367 6A). Although the new regression equations showed a bias for the ~~E climate zones~~ polar climate
368 zones (E) (the minimum and maximum *R* values were are not captured), the resulting mean
369 average *R* values for Switzerland showed a strong improvement (Table 7 and Fig. 6B).

370 Furthermore, the variability in the estimated *R* factor ~~compared~~ compares well with the
371 variability of the observed high resolution *R*. It should be noted that Switzerland is not an
372 independent case study anymore for the ~~E climate zones~~ polar climate zones (E), as the high
373 resolution *R* values from this case study were used in our regression analysis. However, the Ebro
374 basin case study confirms ~~that~~ the strong improvement for the ~~E climate zones~~ polar climate

Comment [VN4]:

Comment [1]: Reviewer #3: In section 3.3 it would be helpful to actually state the climate zones rather than use the letters as many people may not be up-to-date with the classification system. For example, rather than state the "For the Ds climate zones", the "f climate zones", or the E climate zones", state the cold climates (D) or the climates without dry seasons etc. This I believe would improve the readability and uptake of this particular section. This comment applies throughout the text where climates are mentioned (for example the Csb climate on line 453, or E zones line 485).

Reply: We agree that this would add clarity, and will state the climate zones explicitly on the text

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375 | ~~zones (E) that also occur here is significant~~ (Fig. 6C). As the ~~observed-high resolution~~ *R* values
376 | of the USA and Switzerland were used to derive the regression equations, the third case study,
377 | the Ebro basin in Spain, provided an important independent validation. For the Ebro basin, the
378 | new regression equations not only ~~improved-improve~~ the overall mean but also captured the
379 | minimum *R* values better. ~~This resulted, resulting~~ in an improved representation of the *R*
380 | variability (Table 7 and Fig. 6C). In Fig. 6C, however, there ~~was-is~~ a clear pattern separation in
381 | the newly computed *R* values, which ~~was-is~~ due to the fact that the SDII data were not available
382 | for part of the Ebro basin. As mentioned before, SDII is an important explaining parameter in the
383 | regression equations for most of the addressed climate zones.

384 | Figure 7A ~~showed-shows~~ the global patterns of the estimated *R* factor from ~~respectively~~ the
385 | method of Renard and Freimund and the new regression equations. Figure 7B ~~showed-shows~~ a
386 | difference plot between the estimated *R* factor with the method of Renard and Freimund and the
387 | *R* factor estimated with the new regression equations. The new regression equations significantly
388 | reduced the *R* values in most regions. However, the tropical regions still showed unrealistic high
389 | *R* values (maximum *R* values go up to $1 * 10^5$ MJ mm ha⁻¹ h⁻¹ year⁻¹). This is because the *R*
390 | factor was not adjusted for the tropical climate zones due to the lack of high resolution *R* data.
391 | Oliveira et al. (2013) found for the *R* factor in Brazil that the maximum *R* values for the tropical
392 | climate zones reach 22,452 MJ mm ha⁻¹ h⁻¹ year⁻¹. ~~We find *R* values in Brazil that exceed this~~
393 | ~~maximum *R* value found by Oliveira et al. (2013).~~

394 | Finally, it should be noted that the purpose of the adjusting methods ~~for the *S* and *R* factors~~ in
395 | this study is to capture more accurately the large scale mean erosion rates rather than the
396 | extremes. Therefore, even though the new regression equations are still not accurate enough for
397 | certain climate zones, it is important that the ~~mean-average~~ *R* factor is represented well. The
398 | approach for adjusting the *R* factor also showed that ~~even-although~~ there is no high temporal
399 | resolution precipitation intensity data available on a global scale, the *R* factor can still be
400 | represented well for most climate zones on a large spatial scale. ~~This can be done~~ by using other
401 | parameters, such as elevation, and especially a representative of precipitation intensity, such as
402 | the SDII. The SDII played an important role here as it improved the estimation of the *R* factor
403 | significantly, even though data was only available at a very low resolution as compared to the
404 | other datasets of precipitation, elevation and climate zone classification.

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406 4 Global application of the adjusted RUSLE model

407 4.1 Computation of the soil erodibility and ~~crop-land~~ cover factors

408 In the following we demonstrate the consequences of the new parameterizations of the S and R
409 factors for global soil erosion rates ~~are demonstrated~~. First, we compute the other individual
410 RUSLE factors, soil erodibility (K) and ~~crop-land~~ cover (C) ~~needed to be computed~~. Estimations
411 of the K factor ~~were~~ based on soil data from the gridded 30 arc-second Global Soil Dataset for
412 use in Earth System Models (GSCE). GSCE is based on the Harmonized World Soil database
413 (HWSD) and various other regional and national soil databases (Shangguan et al., 2014). We
414 used ~~the~~ method of Torri et al. (1997) ~~was then used~~ to estimate the K factor, and gave
415 Volcanic soils ~~were given~~ a K factor of $0.08 \text{ t ha h ha}^{-1} \text{ MJ}^{-1} \text{ mm}^{-1}$. This because, ~~as~~ these soil
416 types are usually very vulnerable ~~for to~~ soil erosion, and the observed K values are beyond the
417 range predicted by the method of Torri et al. (1997) (van der Knijff et al., 1999). To account for
418 the effect of stoniness on soil erosion we used a combination of the methods ~~used~~ by Cerdan et
419 al. (2010) and Doetterl et al. (2012) ~~was applied~~, who based their methods on the original
420 method of Poesen et al. (1994). For non-agricultural areas we used the method of Cerdan et al.
421 (2010), ~~was used~~ where they reduced the total erosion by 30 % for areas with a gravel percentage
422 larger or equal to 30 %. For agricultural and grassland areas we used the method of Doetterl et al.
423 (2012) was used, where erosion was reduced by 80 % in areas where the gravel percentage
424 exceeded 12 %.

425 We calculated ~~the~~ C factor ~~was calculated~~ according to the method of De Jong et al. (1998),
426 using 0.25 degree Normalized Difference Vegetation Index (NDVI) and land use data for the
427 year 2002. An important limitation of this method is the fact that in winter the C factor is
428 estimated too large-high (van der Knijff et al., 1999). This is because the ~~equation-method~~ does
429 not include the effects of mulch, decaying biomass and other surface cover reducing soil erosion.
430 To prevent the C factor of being too largehigh, maximum C values for forest and grassland of
431 0.01 and 0.05 for pasture were used. Doetterl et al. (2012) showed that the slope length (L) and
432 support practice (P) factors do not contribute significantly to the variation in soil erosion at the
433 continental scale to global scale, when compared to the contribution of the other RUSLE factors
434 (S , R and C). However, this does not mean that their influence on erosion should be ignored

435 completely. They may play an important role in local variation of erosion rates. In our erosion
436 calculations we do not include these factors, because we have too little ~~to or~~ no data on these
437 factors on a global scale. Including them in the calculations would only add an additional large
438 uncertainty to the erosion rates. ~~This, which~~ would make it more difficult to judge the
439 improvements we made to the *S* and *R* factors.

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441 4.2 Computation of global soil erosion rates and comparison to empirical 442 databases

443 ~~We applied~~ The RUSLE model with the settings mentioned in the previous paragraph ~~is applied~~
444 on a 5 arc-minute resolution on a global scale for the present time period (see time resolutions of
445 datasets in Table 1). ~~We calculated~~ Global soil erosion rates ~~are calculated with~~ for four
446 different versions of the RUSLE model: (a) the unadjusted RUSLE, (b) RUSLE with only an
447 adjusted *S* factor, (c) RUSLE with only an adjusted *R* factor and (d) the adjusted RUSLE (all
448 adjustments included).

449 ~~We found~~ The global mean soil erosion rate for the adjusted RUSLE ~~is found to be of~~ 6.57 t ha⁻¹
450 year⁻¹ (Fig. 8A). When including the uncertainty arising from applying the linear multiple
451 regression method, the ~~mean-average~~ global soil erosion rate differs between 5.36 and 158 t ha⁻¹
452 year⁻¹. Furthermore, the RUSLE version with only an adjusted *S* factor shows the highest mean
453 global soil erosion rate, while the lowest rate is found for the RUSLE version with only the
454 adjusted *R* factor (Table 8). ~~Figure 8C shows~~ From the global map showing the difference
455 between the erosion rates of the *S* adjusted RUSLE and the unadjusted RUSLE versions, ~~(Fig.~~
456 ~~8C) one can see that~~ The erosion rates are in general increased here, and mostly pronounced in
457 mountainous regions. This feature is 'dampened' ~~by when~~ adjusting the *R* factor. ~~Looking at the~~
458 ~~global map showing the~~ The difference between the *R* adjusted RUSLE and unadjusted RUSLE
459 versions (Fig. 8D); ~~one can see~~ shows that the erosion rates are overall decreased in regions
460 where the adjustments are made. When combining both adjustments of the RUSLE model in the
461 fully adjusted RUSLE version and subtract the unadjusted RUSLE erosion rates (Fig. 8B), ~~one~~
462 ~~can see that the~~ erosion rates are slightly decreased in areas where the *R* factor is adjusted.
463 However, ~~in for~~ the tropics ~~for example there is~~ an increase in erosion rates is found by in the
464 fully adjusted RUSLE due to the lack of adjusting the *R* factor there. This indicates that these

465 two factors balance each other, and that it is important to have a correct representation of all the
466 | ~~RUSLE factors on a~~ global scale in order to predict reliable erosion rates.

467 In this study the *K* and *C* factors are not tested and adjusted for a coarse resolution at ~~the~~ global
468 | scale, and thus validation with existing empirical databases on soil erosion is not fully justified.

469 However, to test if the global erosion rates are in an acceptable range, they are compared to
470 | erosion estimates from the NRI database for the USA, and erosion estimates from the study of
471 | Cerdan et al. (2010) for Europe. These are to our knowledge the only large scale high resolution
472 | empirical databases on soil erosion.

473 The NRI database contains USLE erosion estimates for the year 1997, which are available at the

474 | Hydrologic Unit 4th Code (HUC4) watershed level. ~~After aggregating~~We aggregated the
475 | resulting erosion rates from the adjusted and unadjusted RUSLE models to the HUC4 watershed
476 | level. ~~The results showed~~ that the mean-average erosion rates from the adjusted RUSLE model

477 | come closer to that of the NRI database (Table 9 and Fig. 9A). However, the maximum ~~observed~~
478 | mean-average HUC4 soil erosion rate from the adjusted RUSLE ~~was twice as~~ somewhat
479 | high~~er~~ as compared to the NRI database. ~~This maximum is observed in the hilly and relatively~~
480 | ~~wet region on the west coast of the USA.~~ From these results we can conclude that the erosion

481 | rates of the adjusted RUSLE fall in the range of observed values, but that there are still some
482 | local overestimations. ~~For example~~Some of these overestimations can be found in, the north
483 | south west of the USA where the adjusted RUSLE shows a slightly worse performance

484 | compared to the unadjusted RUSLE. ~~in the adjusted model most probably because in this region~~
485 | ~~the estimation of~~ The R factor in this region was not changed as it was already estimated well
486 | by the method of Renard and Freimund, however, could not be improved, while the *S* factor ~~is~~

487 | increased due to the hilly terrain. Without adjusting the other RUSLE factors (*K* and *C*), ~~This~~
488 | ~~gives~~ resulted in an overall increase in soil erosion rates. This indicates that the other RUSLE

489 | factors may play an important role in this region. Furthermore, we see that along the west coast
490 | of the USA the erosion values are not much improved with the adjusted RUSLE model. This is
491 | mainly because ~~In this region of the USA,~~ some climate zones such as the temperate climate

492 | zone with a dry and warm summer (Csb) climate prevail in this regions, for which the *R* factor is
493 | still difficult to estimate in a correct way (Table 4). ~~So for this climate there are some outliers in~~
494 | ~~the R factor in this specific region.~~

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495 For Europe, Cerdan et al. (2010) used an extensive database of measured erosion rates on plots
496 under natural rainfall. They extrapolated measured erosion rates to the whole Europe (European
497 Union area) and adjusted them with a topographic correction. ~~This correction is~~ based on the *L*
498 and *S* factors of the RUSLE model. ~~They also applied, and~~ a correction to account for soil
499 stoniness. For comparison, the soil erosion rates from Cerdan et al. (2010) and the RUSLE
500 estimates in our study are aggregated at country level. The performance of the adjusted RUSLE
501 model was not as good for Europe as compared to the USA. ~~This, which~~ is not surprising ~~due to~~
502 ~~the fact that~~ as the RUSLE model is based on soil erosion data of the USA. However, also on the
503 European scale the adjusted RUSLE model performed better than the unadjusted RUSLE model
504 (Table 9 and Fig. 9B). Especially the large erosion rates in the south of Europe as observed in the
505 results of the unadjusted RUSLE model, are less extreme ~~for-in~~ the adjusted RUSLE model
506 ~~results~~. Still, the overall ~~mean-average~~ erosion rate for Europe ~~was-is~~ overestimated by
507 approximately two times (Table 9).

508 These biases in erosion rates as seen for the south west of the USA and south Europe can be
509 attributed to several factors. ~~As mentioned before~~ Firstly, the other RUSLE factors (*K* and *C*) and
510 ~~the way they interact with each other~~ the *R* and *S* factors are not adjusted to the coarse resolution
511 ~~of the~~ at global scale. ~~From figures 8, which provide global erosion rates, We found~~ no clear
512 signal ~~can be found~~ for which land cover types the adjusted RUSLE performs worse or better. In
513 general, we can see that the adjusted RUSLE model still overestimates erosion rates for most
514 land cover types. A short analysis for Europe showed that the largest biases are found for shrubs,
515 and the least for grassland. However, a more explicit analysis is needed here to find out how we
516 can improve the contribution of land cover and land use to erosion rates in the RUSLE model.
517 Explicitly including the interaction between the *C* and *R* factor on a monthly timescale could be
518 crucial. This is very important for example in areas with agriculture and areas with a strong
519 seasonal character. For example Another aspect related to improving the *C* factor is looking at the
520 location of land use in a certain grid cell. ~~could make a difference in the resulting erosion rates.~~
521 If the land use in a grid cell is located on steep slopes the resulting erosion in that grid cell would
522 be higher than when it would be located in the flatter areas. In this study, however, only mean
523 fractions of land cover and the NDVI are used for each grid cell. ~~This, which~~ can lead to possible
524 biases in the resulting erosion rates.

Comment [VN5]:

Comment [2]: Reviewer #3: Specifically for the paragraph from Lines 468-493. First, it is stated that (line 469) that the other RUSLE factors (*K* and *C*) and the way they interact with each other are not adjusted the global scale. I would suggest that what is probably most important is the interaction of *C* and *R* and possibly even a recommendation for future models would be a monthly time step combining *C* and *R* at the global scale. This interaction is far more important than *K* and *C* and would be fundamental to improving the incorporation of the *C* factor in global models with improved *R* factor data.

Reply: This is a very good suggestion, and we include this in the text

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525 ~~Secondly~~Furthermore, land management is not accounted for in this study, which could
526 introduce an important systematic bias in the soil erosion rates for especially agricultural areas.

527 ~~Land management is represented by the P factor in the original USLE. however, it is partly also~~
528 ~~incorporated in the C factor for agricultural land use through plant residues, cover crops and~~
529 ~~tillage. A limitation of the NDVI approach to estimate the C factor lies therefore in the inability~~
530 ~~to estimate this land management effect. Applying this method also limits the interaction~~
531 ~~between the R and C factors on a monthly to seasonally scale, because this interaction is partly~~
532 ~~based on land management.~~

533 Furthermore, uncertainties in the coarse resolution land cover/land use, soil and precipitation
534 datasets that are not accounted for, can lead to the model biases. Also, better adjustment of the R
535 factor for climate zones such as the ~~E-climate zones~~polar climate zones (E_p) could help
536 improving the overall results. Some biases in the erosion rates can also be attributed to the fact
537 that stepped relief, where flat plateaus are separated by steep slopes, are not well captured by the
538 150_m target resolution used in the fractal method to scale slope. In this way erosion would be
539 overestimated in these areas. Finally, errors and limitations in the observational datasets can also
540 contribute to the differences between model and observations. The study of Cerdan et al. (2010)
541 on Europe for example, used extrapolation of local erosion data to larger areas that could
542 introduce some biases. Also, the underlying studies on measured erosion rates used different
543 erosion measuring techniques that can be linked to different observational errors.

544

545 5 Conclusions

546 In this study we introduced specific methods to adjust the topographical and rainfall erosivity
547 factors to improve the application of the RUSLE model on a global scale, using coarse resolution
548 input data.

549 Our results show that the fractal method by Zhang et al. (1999) and Pradhan et al. (2006) can be
550 applied on coarse resolution DEMs to improve the resulting slope. Although the slope
551 representation improved after applying this method, the results still show a slight dependence on
552 the original grid resolution. This is attributable to several factors, such as the underlying
553 assumption that the standard deviation of elevation (σ) is independent of the DEM resolution,
554 and to the breakdown of the fractal method at certain scales.

Comment [VN6]:

Comment [2]: Reviewer #3: Second, the manuscript states that (Line 481) land management is not accounted for in the study. Often land management in RUSLE research is incorporated through the cover factor, particularly for different agricultural land uses. Maybe this is a limitation of the NDVI approach. These limitations are related but they are presented as being separate. I do think this section requires some work to be a bit more consistent with the research on the C factor and the importance of timing the C factor with the R factor in future applications.

Reply: We edit this section and the conclusions with regard to the importance of adjusting the C factor and the role of land management.

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555 We compared the rainfall erosivity calculated by the method of Renard and Freimund to
556 available high resolution or observed erosivity data of the USA, Switzerland and the Ebro basin.
557 ~~We find that this method results in and showed~~ overall significant biases in erosivity. Therefore,
558 ~~We~~ implemented a linear multiple regression method to adjust erosivity for climate zones of
559 the Köppen-Geiger climate classification system in the USA, ~~that showed a bias in erosivity~~
560 ~~calculated with the method of Renard and Freimund~~. Using precipitation, elevation and the
561 simple precipitation intensity index as explaining parameters, the resulting adjusted erosivity
562 compares much better to the observed erosivity data for the USA, Switzerland and the Ebro
563 basin. Not only the mean values but also the spatial variability in erosivity is improved. It was
564 surprising to notice that using the rather coarse resolution simple precipitation intensity index in
565 the regression analysis made it possible to explain much of the variability in erosivity. This, once
566 more, underpins the importance of precipitation intensity in erosivity estimation.

567 After calculating the newly adjusted erosivity on a global scale, it is apparent that the tropical
568 climate zones, for which erosivity was not adjusted, show strong overestimations in some areas,
569 ~~when compared to estimated erosivity from previous studies~~. This shows that adjusting erosivity
570 for the tropical climate zones should be the next step. The challenge is to find enough reliable
571 long term and high resolution erosivity data for those regions.

572 To investigate how the adjusted topographical and rainfall erosivity factors affect the global soil
573 erosion rates, we applied the adjusted RUSLE model on a global scale, ~~and estimate~~ We found an
574 mean-average global soil erosion rate of 6.57 t ha⁻¹ year⁻¹. It is, however, difficult to provide
575 accurate uncertainty estimates to these global erosion rates, ~~of this study~~ and to provide a good
576 validation with observations. This is, due to lack of high resolution data on other individual
577 RUSLE factors such as the land cover, soil erodibility, slope length and support practice. These
578 RUSLE factors, ~~together with the crop cover factor, which includes the effects of land use~~, are
579 therefore not adjusted for application on a coarse resolution on global scale. We argue that it is
580 important to focus on adjusting the other RUSLE factors, for an improved application of the
581 RUSLE model on global scale. The next step would be to better capture the anthropogenic
582 contribution to global soil erosion. This can be done by adjusting first of all the land cover factor
583 to a coarse resolution application, and focus on the interaction of this factor with rainfall
584 erosivity on a monthly to seasonal basis. This is important, because the land cover factor has

585 strong interactions with the rainfall erosivity factor, and includes the effect of human activities
586 on erosion through agricultural activities and land management.

587 To test if the soil erosion rates from the adjusted RUSLE model are in a realistic range, we
588 compared the results to the USLE erosion estimates for the USA from the NRI database, and the
589 erosion estimates for Europe from the study of Cerdan et al. (2010). The adjusted RUSLE soil
590 erosion rates, which we aggregated to the HUC4 watershed level, show a better comparison with
591 the NRI USLE estimates ~~for the USA than~~ the unadjusted RUSLE erosion rates. For Europe the
592 comparison of the adjusted RUSLE soil erosion rates to the study of Cerdan et al. (2010) were
593 not as good as for the USA. This is not surprising due to the fact that the parameterizations of the
594 RUSLE model are based on soil erosion data of the USA. However, also for Europe, the adjusted
595 RUSLE model performs better than the unadjusted RUSLE model.

596 We find ~~strong~~ overestimations by the adjusted RUSLE model for hilly regions ~~in~~ along the west
597 coast of the USA, and for south of Europe. We argue that besides for reasons mentioned before,
598 these biases are due to the fact that the topographical detail may not be enough in some regions
599 to capture the true variability in soil erosion effects by topography. Also, erosivity could not be
600 adjusted for some climate zones that are not present in the USA or Switzerland, and needs to be
601 further improved for climate zones such as the polar climate zones.

602 We conclude that even though there is still much improvement of the RUSLE model possible
603 with respect to topography and erosivity, the methods proposed in this study seem to be
604 promising tools for improving the global applicability of the ~~RUSLE~~ model. A globally
605 applicable version of the RUSLE model, together with data on environmental factors from Earth
606 System Models (ESMs), can provide the possibility for future studies to estimate accurate soil
607 erosion rates for the past, current and future time periods.

608

609 **Acknowledgements**

610

611 We like to thank the anonymous reviewers for their useful comments. The article processing 554
612 charges for this open-access publication have been covered by the Max Planck Society. J.
613 Pongratz was supported by the German Research Foundation's Emmy Noether Program (PO
614 1751/1-1).

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Table 1. List of datasets used in this study

Category	Dataset	Source	Spatial resolution	Temporal-period	Variables
DEM	GTOPO Elevation Model	USGS, 1996, Gesch et al., 1999	30 arc-seconds		elevation
	ETOPO1 Elevation Model	Amante and Eakins, 2009	1 arc-minute		elevation
	ETOPO2 Elevation Model	US Department of Commerce and NOAA, 2001	2 arc-minute		elevation
	ETOPO5 Elevation Model	National Geophysical Data Center/NESDIS/NOAA, 1995	5 arc-minute		elevation
Climate	GPCC 0.5 degree dataset	Schneider et al., 2011	0.5 degrees	Years 1989-2010	total yearly precipitation
	GPCC 0.25 degree	Meyer-Christoffer et al.,	0.25 degrees	years 1951-	total yearly

	dataset	2011		2000	precipitation
	GHCNDEX dataset	CLIMDEX (Donat et al., 2013)	2.5 degrees	years 1951-present	simple precipitation intensity index (SDII)
	Köppen-Geiger dataset	Peel et al., 2007	5 arc-minute		Köppen-Geiger climate classifications
Soil	Global Soil Dataset for use in Earth System Models (GSCE)	Shangguan et al., 2014	30 arc-seconds		sand, silt and clay fractions, organic matter %, gravel %
	Harmonized World Soil Database (HWSD) version 1.2	Nachtergaele et al., 2012	30 arc-seconds		volcanic soils
Land-cover	GIMMS dataset	ISLSCP II (Tucker et al., 2005, Hall <i>et al.</i> , 2006)	0.25 degrees	year 2002	Normalized difference vegetation index (NDVI)
Land-use	MODIS dataset	ISLSCP II (Friedl et al., 2010, Hall <i>et al.</i> , 2006)	0.25 degrees	year 2002	Land use fractions

Table 2. Fractal parameters and the resulting mean global slopes before and after applying the fractal method on the different DEMs; Increase of slope means the increase of the average global slope of a DEM after applying the fractal method; difference after scaling = $\frac{\theta_{scaled(DEM)} - \theta_{scaled(GTOPO30)}}{\theta_{scaled(GTOPO30)}} * 100$; difference before scaling = $\frac{\theta_{(DEM)} - \theta_{(GTOPO30)}}{\theta_{(GTOPO30)}} * 100$

DEM	resolution arc-minute	standard deviation of elevation m	mean D	mean $\alpha_{steepest}$	θ m m-1	θ_{scaled} m m-1	Increase of θ %	difference after scaling %	difference before scaling %
GTOPO30	0.5	570	1.32	0.99	0.023	0.059	61	0	0
ETOPO1	1	530	1.35	1.08	0.016	0.057	71.9	-3.4	-30.4
ETOPO2	2	549	1.37	1.17	0.011	0.055	80	-6.8	-52.2
ETOPO5	5	562	1.42	1.25	0.006	0.054	88.9	-8.5	-73.9

Table 3. Description of Köppen climate symbols and defining criteria (from Peel et al., 2007).

1st	2nd	3rd	Description	Criteria*
A			Tropical	$T_{cold} \geq 18$
	f		- Rainforest	$P_{dry} \geq 60$ Not (Af) & $P_{dry} \geq 100 - MAP/25$
	m		- Monsoon	MAP/25
	w		- Savannah	Not (Af) & $P_{dry} < 100 - MAP/25$
B			Arid	$MAP < 10 \times P_{threshold}$
	W		- Desert	$MAP < 5 \times P_{threshold}$
	S		- Steppe	$MAP \geq 5 \times P_{threshold}$
		h	▪ Hot	$MAT \geq 18$
		k	▪ Cold	$MAT < 18$
C			Temperate	$T_{hot} > 10 \& 0 < T_{cold} < 18$
	s		- Dry Summer	$P_{sdry} < 40 \& P_{sdry} < P_{wwet}/3$
	w		- Dry Winter	$P_{wdry} < P_{swet}/10$
	f		- Without dry season	Not (Cs) or (Cw)
		a	▪ Hot Summer	$T_{hot} \geq 22$
		b	▪ Warm Summer	Not (a) & $T_{mon10} \geq 4$
	c	▪ Cold Summer	Not (a or b) & $1 \leq T_{mon10} < 4$	
D			Cold	$T_{hot} > 10 \& T_{cold} \leq 0$
	s		- Dry Summer	$P_{sdry} < 40 \& P_{sdry} < P_{wwet}/3$
	w		- Dry Winter	$P_{wdry} < P_{swet}/10$
	f		- Without dry season	Not (Ds) or (Dw)
		a	▪ Hot Summer	$T_{hot} \geq 22$
		a	▪ Warm Summer	Not (a) & $T_{mon10} \geq 4$
		c	▪ Cold Summer	Not (a, b or d)
		d	▪ Very Cold Winter	Not (a or b) & $T_{cold} \leq -38$
E			Polar	$T_{hot} < 10$
	T		- Tundra	$T_{hot} > 0$
	F		- Frost	$T_{hot} < -0$

Comment [VN7]:

Comment [1]: Reviewer #1: description of Köppen climate symbols, may not be required. I think giving a reference (e.g., Peel et al., 2007) or minimal description (cf Table 6) is adequate, because this is a classic system.

Reply: We agree that there may be overlap between tables 3 and 6, due to the climate zone descriptions. We therefore will remove the descriptions of the climate zones in table 6 and will leave table 3 for the overall overview. We agree that the Köppen-Geiger climate classification system is a classical system. However, as the classification system is the basis for our approach of adjusting erosivity, we think we should provide the descriptions of the climate zones for a better readability of the paper.

* MAP = mean annual precipitation, MAT = mean annual temperature, T_{hot} = temperature of the hottest month, T_{cold} = temperature of the coldest month, T_{mon10} = number of months where the temperature is above 10, P_{dry} = precipitation of the driest month, P_{sdry} = precipitation of the driest month in summer, P_{wdry} = precipitation of the driest month in winter, P_{swet} = precipitation of the wettest month in summer, P_{wwet} = precipitation of the wettest month in winter, $P_{threshold}$ = varies according to the following rules (if 70% of MAP occurs in winter then $P_{threshold} = 2 \times MAT$, if 70% of MAP occurs in summer then $P_{threshold} = 2 \times MAT + 28$, otherwise $P_{threshold} = 2 \times MAT + 14$). Summer (winter) is defined as the warmer (cooler) six month period of ONDJFM and AMJJAS.

Table 4. Linear multiple regression equations for different climate zones, relating high resolution erosivity from the USA with one or more significant parameters: annual total mean precipitation, P (mm), mean elevation, Z (m), and the simple precipitation intensity index, $SDII$ (mm/day).

Climate zone	Explaining parameters	Regression function - optimal	R^2	Residual standard error
BWk	P, SDII	$R = 0.809 * P^{0.957} + 0.000189 * SDII^{6.285}$		
BSh	P, SDII	$\log R = -7.72 + 1.595 * \log P + 2.068 * \log SDII$	0.97	0.22
BSk	P, SDII, Z	$\log R = 0.0793 + 0.887 * \log P + 1.892 * \log SDII - 0.429 * \log Z$	0.89	0.35
Csb	P	$R = 98.35 + 0.000355 * P^{1.987}$		0.16
Cfa	P, SDII, Z	$\log R = 0.524 + 0.462 * \log P + 1.97 * \log SDII - 0.106 * \log Z$	0.89	0.11
Cfb	P, SDII	$\log R = 4.853 + 0.676 * \log P + 3.34 * \log SDII$	0.97	0.21
Dsa	Z, SDII	$\log R = 8.602 - 0.963 * \log SDII - 0.247 * \log Z$	0.51	0.05
Dsb	P	$\log R = 2.166 + 0.494 * \log P$	0.45	0.25
Dsc	SDII	$\log R = 6.236 - 0.869 * \log SDII$	0.51	0.02
Dwa	P	$\log R = -0.572 + 1.238 * \log P$	0.99	0.02
Dwb	P, SDII	$\log R = -1.7 + 0.788 * \log P + 1.824 * \log SDII$	0.98	0.02
Dfa	P, SDII	$\log R = -1.99 + 0.737 * \log P + 2.033 * \log SDII$	0.9	0.16
Dfb	P, SDII, Z	$\log R = -0.5 + 0.266 * \log P + 3.1 * \log SDII - 0.131 * \log Z$	0.89	0.32
Dfc	SDII	$\log R = -1.259 + 3.862 * \log SDII$	0.91	0.23
ET	P	$\log R = -3.945 + 1.54 * \log P$	0.14	0.42

Comment [VN8]:

Comment [2]: Reviewer #1: In Tables 4 and 5, can you add units for variables (e.g., P and z)?

Reply: Units are added

EF+EFH	P	$\log R = 16.39 - 1.286 * \log P$	0.6	0.13
ETH	P, SDII	$\log R = 21.44 + 1.293 * \log P - 10.579 * \log SDII$	0.52	0.53

Table 5. Linear multiple regression equations for different climate zones for regions that have no data on the simple precipitation intensity index, $(SDII)$ (mm/day). The regression equations relate high resolution erosivity from the USA with the annual total mean precipitation, (P) (mm), and/or the mean elevation, (z) (m).

Climate zone	Optimal regression function (when SDII is not available)	R ²	Residual standard error
BWk	Method Renard & Freimund (1994)		
BSh	$\log R = -8.164 + 2.455 * \log P$	0.86	0.5
BSk	$\log R = 5.52 + 1.33 * \log P - 0.977 * \log Z$	0.76	0.52
Cfa	$\log R = 3.378 + 0.852 * \log P - 0.191 * \log Z$	0.57	0.23
Cfb	$\log R = 5.267 + 0.839 * \log P - 0.635 * \log Z$	0.81	0.5
Dsa	$\log R = 7.49 - 0.0512 * \log P - 0.272 * \log Z$	0.48	0.06
Dsc	$\log R = 4.416 - 0.0594 * \log P$	0.015	0.03
Dwb	$\log R = 1.882 + 0.819 * \log P$	0.81	0.08
Dfa	$\log R = -2.396 + 1.5 * \log P$	0.65	0.29
Dfb	$\log R = 1.96 + 1.084 * \log P - 0.34 * \log Z$	0.74	0.48
Dfc	$\log R = -3.263 + 1.576 * \log P$	0.56	0.49
ETH	$\log R = -10.66 + 2.43 * \log P$	0.4	0.59

Table 6. Mean high resolution R values ($\text{MJ mm ha}^{-1} \text{h}^{-1} \text{year}^{-1}$) from the USA and Switzerland and mean modelled R values with uncertainty range for each addressed climate zone

climate	description	observed R mean	old <u>Renard</u> & <u>Freimund</u> method R mean	adjusted method R mean	Adjusted method uncertainty range
BWk	arid, desert, cold	284	533	291	158-495
BSh	arid, steppe, hot	2168	1356	2207	1723-2828
BSk	arid, steppe, cold	876	884	885	749-1046
Csb	temperate, dry warm summer	192	1136	192	133-292
Cfa	temperate, without dry season, hot summer	5550	5607	5437	4830-6123
Cfb	temperate, without dry season, warm summer	1984	5359	1971	1431-2715
Dsa	cold, dry hot summer	172	445	171	86-340
Dsb	cold, dry warm summer	175	896	168	151-187
Dsc	cold, dry cold summer	115	374	115	91-145
Dwa	cold, dry winter, hot summer	1549	1444	1551	1280-1879
Dwb	cold, dry winter, warm summer	1220	1418	1214	1057-1395
Dfa	cold, without dry season, hot summer	2572	2983	2582	2346-2843
Dfb	cold, without dry season, warm summer	1101	1798	1124	922-1371
Dfc	cold, without dry season, cold summer	483	701	483	423-552
ET	polar, tundra	1352	6257	1249	23-68088
EF+EFH	polar, frost + polar, frost, high elevation	1468	5469	1450	16-132001
ETH	polar, tundra, high elevation	945	5580	832	0-6314918

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Table 7. Statistics of the comparison of high resolution ~~erosivity~~ *R* values ($\text{MJ mm ha}^{-1} \text{h}^{-1} \text{year}^{-1}$) from three regions to estimated ~~erosivity~~ *R* values from the Renard and Freimund method and the new regression equations

	Observed			Estimated – Renard & Freimund				Estimated – multiple linear regression					
	Range	Mean	Standard deviation	Range	Mean	Standard deviation	Correlation coefficient	Rank correlation coefficient	Range	Mean	Standard deviation	Correlation coefficient	Rank correlation coefficient
Switzerland	121-6500	1204	833	2335-10131	5798	1654	0.51	0.42	225-2572	1256	472	0.49	0.3
the USA (aggregated huc4)	105-4963	1271	1174	57-15183	1870	2088	0.51	0.68	60-15808	1691	2188	0.58	0.83
Ebro basin	40 - 4500	891	622	747 - 5910	1529	846	-	-	167 - 4993	836	701	-	-

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Table 8. Comparison of the global erosion rates ($\text{t ha}^{-1} \text{ year}^{-1}$) and percentiles between different versions of the RUSLE model

Comment [VN9]: Due to a bug we found in the model related to the calculation of the K factor, the values of this table are slightly changed. This also affects slightly table 9 and figures 8 and 9.

	mean	25th percentile	50th percentile	75th percentile	90th percentile
RUSLE unadjusted	5.14.5	0.2	0.78	2.48	8.67.5
RUSLE adjusted with S	11.19.8	0.3	1.02	3.84.3	15.713.5
RUSLE adjusted with R	3.63.2	0.1	0.56	1.79	6.35.7
RUSLE adjusted with S & R	7.36.5	0.12	0.78	2.73	10.99.6

Table 9. Statistics of the high resolution or observed and modelled erosion rates from the unadjusted and adjusted versions of the RUSLE for the USA and Europe ($\text{t ha}^{-1} \text{ year}^{-1}$)

Region	Source	Observations			Adjusted RUSLE			Unadjusted RUSLE		
		Range	Mean	Standard deviation	Range	Mean	Standard deviation	Range	Mean	Standard deviation
Europe (Aggregation country level) no small countries	Cerdan et al., 2010	0.1-2.6	0.9	0.7	0.1-7	2.3	2.1	0-14	2.8	3.6
the USA (Aggregation HUC4 level)	NRI database	0-11	1.67	2.1	0.2- 1324	1.67	1.92.5	0-14	1.49	2.31.8

Figure 1. Global average unscaled slope estimated from different coarse resolution digital elevation models (DEMs) as function of their resolution (blue); and global average scaled slope from the same DEMs as function of their resolution (red).

Comment [VN10]:

Minor editorial comment [13]: Reviewer #3: Does it need a figure title along with the description in the figure caption?

Reply: We removed the figure title and made the x and y-axis consistent

Figure 2. (A) A global map of the scaled slope derived from the 30 arc-second DEM using a target resolution of 150m; (B) A global map showing the difference between the unscaled and scaled slopes (in degrees), where blue colours show an underestimation by the unscaled slope when compared to the scaled slope and reddish colours show an overestimation.

Figure 3. Spatial difference plots showing the difference between the high resolution R values and R values calculated with the method of Renard and Freimund for (A) the USA, (B) Switzerland and (C) the Ebro basin in Spain; In (A) and (B) the blue colours show an underestimation of the calculated R factor when compared to the high resolution R values, while the red colours show an overestimation; the Ebro basin serves here as an independent validation set and it has two graphs, (C1) a spatial plot of erosivity according to Renard and Freimund, and (C2) the high resolution R values from Angulo-Martinez et al. (2009); All values in the graphs are in $\text{MJ mm ha}^{-1} \text{ h}^{-1} \text{ year}^{-1}$.

Figure 4. The Köppen-Geiger climate classification global map ~~with~~ at a resolution of 5 arc-minute (Peel et al., 2007).

Figure 5. Comparison of high resolution R factor data and predicted R values from (1) the Renard and Freimund method and (2) the new regression equations, for various climate zones;

the red line is the 1 to 1 line, and does not appear in some graphs because predicted R values are overestimated.

Figure 6. Spatial difference plots showing the difference between the high resolution R values and R values calculated with the new regression equations for (A) the USA, (B) Switzerland and (C) the Ebro basin in Spain; In (A) and (B) the blue colours show an underestimation of the calculated R values when compared to the high resolution R values, while the red colours show an overestimation; the Ebro basin serves here as an independent validation set and it has two graphs, (C1) a spatial plot of the R factor according to the new regression equations, and (C2) the high resolution R values from Angulo-Martinez et al. (2009); All values in the graphs are in MJ mm ha⁻¹ h⁻¹ year⁻¹.

Figure 7. (A) Global distribution of the new modelled R values according to the new regression equations; and (B) a difference map between R values calculated according to the method of Renard and Freimund and the new modelled R values (MJ mm ha⁻¹ h⁻¹ year⁻¹), where blue colours indicate lower R values by Renard and Freimund compared to the new modelled R values, while reddish colours indicate higher R values; map resolution is 5 arc-minute.

Figure 8. (A) Global yearly averaged erosion rates according to the fully adjusted RUSLE model; (B) a difference map between the fully adjusted and unadjusted RUSLE model; (C) a difference map between the adjusted S RUSLE and the unadjusted RUSLE model; (D) a difference map between the adjusted R RUSLE and the unadjusted RUSLE model; in figures B,C and D the reddish colors show an overestimation of by the adjusted RUSLE model and

yellow to bluish colors show an underestimation; resolution of all maps is 5 arc-minute and all units are in $\text{t ha}^{-1} \text{year}^{-1}$.

Figure 9. (A) Difference plots between soil erosion estimates from the NRI database for the USA and estimates of (A1) the unadjusted RUSLE model, and of (A2) the adjusted RUSLE model; all aggregated at HUC4 watershed level; (B) Difference plots between soil erosion estimates from the database of Cerdan et al. (2010) for Europe and estimates of (B1) the unadjusted RUSLE model and of (B2) the adjusted RUSLE model; all aggregated at country level; reddish colors represent an overestimation ($\text{t ha}^{-1} \text{year}^{-1}$) while the bluish represent and underestimation ($\text{t ha}^{-1} \text{year}^{-1}$) compared to the erosion values from the databases.

Comment [VN11]: The colors and representation of these plots are slightly changed compared to the previous manuscript