# Improving the global applicability of the RUSLE model – Adjustment of the topographical and rainfall erosivity factors 3

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### 10 Abstract

11 Large uncertainties exist in estimated rates and the extent of soil erosion by surface runoff on a global scale. This limits our understanding of the global impact that soil erosion might have on 12 agriculture and climate. The Revised Universal Soil Loss Equation (RUSLE) model is due to its 13 simple structure and empirical basis, a frequently used tool in estimating average annual soil 14 15 erosion rates at regional to global scales. However, large spatial scale applications often rely on coarse data input, which is not compatible with the local scale on which the model is 16 17 parameterized. Our study aims at providing the first steps in improving the global applicability of the RUSLE model in order to derive more accurate global soil erosion rates. 18

We adjusted the topographical and rainfall erosivity factors of the RUSLE model and compared the resulting erosion rates to extensive empirical databases from the USA and Europe. By scaling the slope according to the fractal method to adjust the topographical factor, we managed to improve the topographical detail in a coarse resolution global digital elevation model.

Applying the linear multiple regression method to adjust rainfall erosivity for various climate zones, resulted in values that compared well to high resolution erosivity data for different regions. However, this method needs to be extended to tropical climates, for which erosivity is biased due to the lack of high resolution erosivity data.

After applying the adjusted and the unadjusted versions of the RUSLE model on a global scale 27 we find that the adjusted version shows a global higher mean erosion rate and more variability in 28 the erosion rates. Comparison to empirical datasets of the USA and Europe shows that the 29 adjusted RUSLE model is able to decrease the very high erosion rates in hilly regions that are 30 observed in the unadjusted RUSLE model results. Although there are still some regional 31 32 differences with the empirical databases, the results indicate that the methods used here seem to be a promising tool in improving the applicability of the RUSLE model on a coarse resolution on 33 global scale. 34

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### 36 1 Introduction

37 For the last centuries to millennia soil erosion by surface runoff is being accelerated globally due to human activities, such as deforestation and agricultural practices (Bork and Lang, 2003). 38 Accelerated soil erosion is a process that triggers land degradation in the form of nutrient loss, a 39 decrease in the effective root depth, water imbalance in the root zone and finally also 40 productivity reduction (Yang *et al.*, 2003). It is widely recognized that soil erosion has been a 41 major threat to sustainable agriculture and food production across the globe since the start of 42 agricultural activities (UNCCD, 2012, Walling, 2009). These effects of soil erosion are currently 43 exacerbated by the global population growth and climatic changes. Organizations such as the 44 United Nations Convention to Combat Desertification (UNCCD) try to address this problem by 45 stating a new goal for Rio +20 of zero land degradation (UNCCD, 2012). 46

Another aspect underpinning the relevance of soil erosion on the global scale is the effect of 47 erosion on global nutrient cycles. Recently, the biogeochemical components of Earth System 48 49 Models (ESMs) became increasingly important in predicting the global future climate (Thornton et al., 2007, Goll et al., 2012). Not only the global carbon cycle but also other nutrient cycles 50 51 such as the nitrogen and phosphorous cycles cannot be neglected in ESMs anymore (Goll et 52 al.,2012, Gruber and Galloway, 2008, Reich et al., 2006). Soil erosion may have a significant impact on these biogeochemical cycles through lateral fluxes of sediment, but the impact on the 53 global scale is still largely unknown. For example, Quinton et al. (2010) showed that erosion can 54 55 significantly alter the nutrient and carbon cycling and result in lateral fluxes of nutrients that are similar in magnitude as fluxes induced by fertilizer application and crop removal. Regnier et al. 56

(2013) looked at the effect of human induced lateral fluxes of carbon from land to ocean and
concluded that human perturbations, which include soil erosion, may have enhanced the carbon
export from soils to inland waters.

60 In general, the effect of soil erosion on the global carbon cycle has received considerable attention after the pioneering work of Stallard (1998), who proposed that global soil erosion can 61 result in sequestration of carbon by soils. After his work, the effect of soil erosion on the carbon 62 cycle has been studied extensively, but there remains a large uncertainty in the effect of soil 63 64 erosion on the carbon cycle. For example, several recent global assessments of the influence of soil erosion on the carbon cycle indicate a large uncertainty with a range from a source of 0.37 to 65 1 Pg C year<sup>-1</sup> to a net uptake or sink of 0.56 to 1 Pg C year<sup>-1</sup> (van Oost *et al.*, 2007). Thus, in 66 order to better constrain the global carbon budget and to identify optimal management strategies 67 for land use, it is essential to have accurate estimates of soil erosion and its variability on a 68 69 global scale.

70 Currently, there exists a large uncertainty in the global soil erosion rates as can be seen from recent studies that show rates between 20 and 200 Pg year<sup>-1</sup> (Doetterl *et al.*, 2012). This indicates 71 72 that modelling soil erosion on a global scale is still a difficult task due to the very high spatial 73 and temporal variability of soil erosion. Different approaches were previously applied to estimate 74 soil erosion on a large or global scale. Most of these approaches are based on extrapolated data from agricultural plots, sediment yield or extrapolated river sediment estimates (Milliman and 75 76 Syvitski, 1992, Stallard, 1998, Lal, 2003, Hooke, 2000, Pimentel et al., 1995, Wilkinson and 77 McElroy, 2007).

An alternative approach is based on the use of soil erosion models, in order to be able to predict 78 79 soil erosion rates for the past and future. One of the most applied models to estimate soil erosion on a large spatial scale is the semi-empirical/process-based Revised Universal Soil Loss 80 Equation (RUSLE) model (Renard et al., 1997). This model stems from the original Universal 81 82 Soil Loss Equation (USLE) model developed by USDA (USA Department of Agriculture), which is based on a large set of experiments on soil loss due to water erosion from agricultural 83 plots in the United States (USA). These experiments covered a large variety of agricultural 84 practices, soil types and climatic conditions, making it a potentially suitable tool on a regional to 85 86 global scale. The RUSLE model predicts the average annual soil erosion rates by rainfall and is

formulated as a product of a rainfall erosivity factor (R), a slope steepness factor (S), a slope 87 length factor (L), a soil erodibility factor (K), a land cover factor (C) and a support practice factor 88 (P). The RUSLE model was first applied on a global scale by Yang et al. (2003) and Ito (2007) 89 for estimating the global soil erosion potential. Various limitations were observed when applying 90 this model on global scale. Firstly, the model is originally developed to be applicable on the 91 92 agricultural plot scale. This makes the model incompatible with the coarse spatial scale of global datasets on soil erosion influencing factors such as precipitation, elevation, land-use and soil 93 94 characteristics. Secondly, the RUSLE and USLE models were parameterized for environmental 95 conditions of the United States (USA), and are thus not directly applicable to other areas in the world. Thirdly, only sheet and rill erosion are considered. Finally, the RUSLE model does not 96 contain sediment deposition and sediment transport terms, which are closely linked to soil 97 98 erosion.

However, the RUSLE model is to our knowledge one of the few erosion models that has the
potential to be applied on a global scale due to its simple structure and empirical basis.
Therefore, it is of key importance to address the above mentioned limitations first.

102 To address the first two limitations, Van Oost et al. (2007) presented in their work a modified 103 version of the USLE model for application on agricultural areas on global scale. They based their model on large-scale experimental soil erosion data from the USA (National Resource Inventory, 104 NRI database, USDA, 2000) and Europe, by deriving reference factors for soil erosion on 105 106 agricultural land, and for certain USLE parameters. They also introduced a procedure to scale 107 slope, which is an important parameter in the topographical factors S and L of the USLE/RUSLE model. In this scaling procedure slope was scaled from the GTOPO30 1km resolution digital 108 elevation model (USGS, 1996) to the coarser resolution of the erosion model. This method was 109 based on high resolution OS Ordnance (10 m resolution) and SRTM data on elevation (90 m 110 resolution, International Centre for Tropical Agriculture, CIAT) for England and Wales. 111

Doetterl *et al.* (2012) showed that together with the *S* factor, the rainfall erosivity or *R* factor explain up to 75 % of the erosion variability across agricultural areas at the large watershed scale. These factors represent the triggers for soil erosion by providing energy for soil to erode. They can also be seen as the natural components of the RUSLE model, as they include very little or no modification by human activities (Angulo-Martínez *et al.*, 2009) apart from indirect effects on precipitation and extreme events due to anthropogenic climate change. In this way they represent the natural environmental constraints to soil erosion that are important to capture before the effect of human activities on soil erosion through land use change can be investigated.

Previous studies on global soil erosion calculated the global R factor based on the total annual precipitation (Renard and Freimund, 1994). This method is different from the method presented in the original RUSLE model (Renard *et al.*, 1997), which is mainly based on 30 minute precipitation intensity. The reason for the method of Renard and Freimund is the lack of high resolution precipitation intensity on a global scale. However, high resolution precipitation intensity is an important explaining parameter of the R factor and therefore, the applicability of the method of Renard and Freimund is limited.

127 The overall objective of our study is to extend the applicability of the RUSLE model to a coarse 128 resolution at global scale, in order to make the model compatible with ESMs. This would enable future studies on the effects of soil erosion for the past, current and future climate. To this end, 129 we develop generally applicable methods that improve the estimation of slope and climatic 130 factors from coarse resolution global datasets. These methods should not only be applicable 131 132 across agricultural areas as in the studies of Van Oost et al. (2007) and Doetterl et al. (2012), but 133 also across non-agricultural areas. We adjust the S factor to the coarse resolution of the global scale based on the scaling of slope according to the fractal method. The adjustment of the R134 factor to the global scale is based on globally applicable regression equations. We derived these 135 regression equations for different climate zones based on parameters for precipitation, elevation 136 137 and the simple precipitation intensity. This approach is validated using several high resolution datasets on the R factor. Finally, the effects of these adjustments of both factors on global soil 138 erosion rates are investigated separately and tested against independent estimates of soil erosion 139 from high resolution and high precision datasets of Europe and the USA. 140

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### 142 **2.** Adjustment of the topographical factor

### 143 **2.1 Scaling slope according to the fractal method**

144 The topographical factors of RUSLE are the slope steepness factor (*S*) and a slope length factor145 (*L*). The S factor is generally computed by the continuous function of Nearing (1997):

146 
$$S=1.5+\frac{17}{1+e^{(2.3-6.1*\sin\theta)}}$$
 (1)

147 And the *L* factor is computed according to Renard *et al.* (1997):

148 
$$L = \left(\frac{l}{22.13}\right)^m$$
 (2)

149 where: 
$$m = \frac{F}{1+F}$$
 and  $F = \frac{(\sin \theta / 0.0896)}{(3^* (\sin \theta)^{0.8} + 0.56)}$  (3)

150 in which  $\theta$  is the slope and *l* is the slope length in meters.

151 As seen in the equations 1 to 3, slope is a crucial parameter and thus an accurate estimation is essential in deriving accurate estimates of the L and S factors and soil erosion rates. For an 152 accurate estimation of the slope, input elevation data from digital elevation models (DEMs) 153 should capture the detailed spatial variability in elevation. However, global DEMs are often too 154 coarse to capture the detailed topography because of the surface smoothening effect. To account 155 156 for this problem it is assumed that topography is fractal. Following Klinkenberg and Goodchild (1992) and Zhang et al. (1999), slope can be expressed as a function of the spatial scale by 157 applying the variogram equation. The variogram equation is used to approximate the fractal 158 dimension of topography and is expressed as follows: 159

160 
$$(Z_p - Z_q)^2 = k d_{pq}^{4-2D}$$
 (4)

161 so that:

162 
$$\frac{|Z_p - Z_q|}{d_{pq}} = \alpha d_{pq}^{1-D}$$
 (5)

where  $Z_p$  and  $Z_q$  are the elevations at points p and q,  $d_{pq}$  is the distance between p and q, k is a constant,  $\alpha = k^{0.5}$ , and D is the fractal dimension. Because the left side of Eq. (5) represents the slope, it can be assumed that the slope ( $\theta$ ) is related to the spatial scale or the grid size (d) in:

$$166 \quad \theta = \alpha \, d^{1-D} \tag{6}$$

167 This result implies that by calculating the fractal properties (D and  $\alpha$ ) Eq. (6) can be used to 168 calculate slope at any specified d. The local fractal dimension (D) describes the roughness of the 169 topography while the local value of  $\alpha$  is related to the concept of lacunarity, which is a measure 170 of the size of "gaps" (valleys and plains) in the topography (Zhang *et al.*, 2002). To estimate the 171 spatial variations of D and  $\alpha$ , Zhang *et al.* (1999) proposed to relate these parameters to the standard deviation of elevation. Hereby it is assumed that the standard deviation of elevation does not change much with the DEM resolution. *D* is then calculated as a function of the standard deviation ( $\sigma$ ) in a 3 x 3 pixels moving window, as proposed by Zhang *et al.* (1999):

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$$D=1.13589+0.08452 \ln \sigma$$
 (7)

To estimate  $\alpha$  we used the modified approach by Pradhan *et al.* (2006). They derived  $\alpha$  directly from the steepest slope in a 3 x 3 pixels moving window, called  $\alpha_{steepest}$  in the following. Having obtained  $\alpha_{steepest}$  and *D* from a grid at a given resolution, the scaled slope ( $\theta_{scaled}$ ) for a target grid resolution ( $d_{scaled}$ ) is obtained by:

$$180 \quad \theta_{scaled} = \alpha_{steepest} d_{scaled}^{1-D} \tag{8}$$

Pradhan *et al.* (2006) also showed that in their case study the ideal target resolution for downscaling slope was 150 m. This is due to the breakdown of the unifractal concept at very fine scales, which was shown to happen at a scale of 50 m. Altogether, this fractal method shows that a high resolution slope can be obtained from a low resolution DEM as is needed by the RUSLE model.

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### 187 2.2 Application of the fractal method on global scale

In this study, we investigate the performance of the fractal method on a global scale using different global DEMs as a starting point. The target resolution of downscaling is put to 150 m (about 5 arc-second) according to Pradhan *et al.* (2006). It should be noted that the spatial scale on which the original RUSLE and USLE models are operating, is usually between 10 and 100 m, which indicates that the 150 m target resolution may be still too coarse for a correct representation of slope. The DEMs that are used here are given in Table 1.

As reported in previous studies (Zhang *et al.*, 1999, Chang and Tsai, 1991, Zhang and Montgomery, 1994), the average slope decreases with decreasing DEM resolution. This confirms the expectation of loss of detail in topography at lower DEM resolutions. A large difference is found between the unscaled global average slope from the 5 arc-minute and the 30 arc-second DEMs, which is in the order of 0.017 m m<sup>-1</sup> or 74 % (Table 2). After applying the fractal method, the scaled slopes at 150 m target resolution from all DEMs all increased significantly

compared to the unscaled slopes (Fig. 1). However, there is still a difference of about 0.05 m m<sup>-1</sup> 200 or 8.5 % between the scaled slopes from the 5 arc-minute and the 30 arc-second DEMs (Table 201 202 2). This difference can be attributed to several factors. One factor could be the underlying assumption that the standard deviation of elevation ( $\sigma$ ) is independent of the DEM resolution. 203 Although  $\sigma$  does not change much when considering different resolutions, there is still a general 204 205 decrease in mean global  $\sigma$  when going from the 5 arc-minute to the 30 arc-second DEM (Table 2). Due to the dependence of the fractal dimension (D) on  $\sigma$  (Zhang et al., 1999), a decrease of  $\sigma$ 206 207 leads to a decrease in D and therefore an increase in the scaled slope. Other factors that could 208 play a role here are the dependence of  $\alpha_{steepest}$  on the steepest slope, and the breakdown of the 209 fractal method at certain scales and in certain environments. Zhang et al. (1999) mentioned that the scaling properties of slope are affected in very coarse resolution DEMs if  $\sigma$  changes 210 considerably. On the other hand, Pradhan et al. (2006) mentioned the breakdown of the fractal 211 method at very fine scales. This can indicate that the 150 m target resolution is not appropriate 212 for some topographically complex regions in the world or, as addressed by Zhang et al. (1999), 213 214 the DEMs used in this study are too coarse to scale down the slope to 150 m accurately for these 215 regions.

After applying the fractal method on a 30 arc-second resolution DEM, the scaled slope shows a clear increase in detail, while the unscaled slope shows a strong smoothening effect (Fig. 2A and 2B). It is found that after scaling the slope values range from 0 to 85 degrees and are less than 2 degrees in 80 % of the area. In contrast, all slope values are less than 45 degrees and range between 0 and 2 degrees in 89 % of this area when slope is computed directly from the 30 arcsecond DEM.

The scaled slope from the 30 arc-second DEM will be used in this study to estimate the globalsoil erosion rates by the RUSLE model.

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### 225 3. Adjustment of the rainfall erosivity factor

### **3.1 The approach by Renard and Freimund (1994)**

Rainfall erosivity (*R* factor) is described by Hudson (1971) and Wischmeier and Smith (1978) as
the result of the transfer of kinetic energy of raindrops to the soil surface. This causes a

detachment of soil and the downslope transport of the soil particles, depending on the amount of energy, rainfall intensity, soil type and cover, topography and management (Da Silva, 2004). The original method of calculating erosivity is described by Wischmeier and Smith (1978) and Renard *et al.* (1997) as:

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$$R = \frac{1}{n} * \sum_{j=1}^{n} \sum_{k=1}^{m_j} (EI_{30})_k$$
(9)

where *n* is the number of years of records,  $m_j$  is the number of storms of a given year *j*, and  $EI_{30}$ is the rainfall erosivity index of a storm *k*. The event's rainfall erosivity index  $EI_{30}$  (MJ mm ha<sup>-1</sup> hour<sup>-1</sup>) is defined as:

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$$EI_{30} = I_{30} * \sum_{r=1}^{m} e_r v_r$$
 (10)

where  $e_r$  and  $v_r$  are, respectively, the unit rainfall energy (MJ ha<sup>-1</sup> mm<sup>-1</sup>) and the rainfall depth (mm) during a time period *r*, and  $I_{30}$  is the maximum rainfall intensity during a time period of 30 minutes (mm hour<sup>-1</sup>). The unit rainfall energy,  $e_r$ , is calculated for each time period as:

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$$e_r = 0.29*(1-0.72*e^{-0.05*i_r})$$
 (11)

where  $i_r$  is the rainfall intensity during the time period (mm hour<sup>-1</sup>).

The information needed to calculate the R factor according to the method of Wischmeier and 243 Smith (1978) is difficult to obtain on a large spatial scale or in remote areas. Therefore, different 244 245 studies have been done on deriving regression equations for the R factor (Angulo-Martinez et al., 2009, Meusburger et al., 2012, Goovaerts, 1999, Diodato and Bellocchi, 2010). Most of these 246 studies, however, concentrate on a specific area and can therefore not be implemented on the 247 global scale. Studies on global soil erosion estimation by the RUSLE model or a modified 248 249 version of it (Doetterl et al., 2012, van Oost et al., 2007, Montgomery, 2007, Yang et al., 2003) have all used the method of Renard and Freimund (1994). Renard and Freimund related the R 250 251 factor to the total annual precipitation based on erosivity data available for 155 stations in the 252 USA, shown in the following equations:

253 
$$R=0.0483*P^{1.61}$$
,  $P \le 850 \text{ mm}$ 

254  $R=587.8-1.219*P+0.004105*P^2$ , P > 850 mm (12)

To test how this method performs globally, we calculated the *R* factor according to the method of Renard and Freimund (Eq. 12) first. Here we used the 0.25 degree resolution annual precipitation data from the Global Precipitation Climatology Center (GPCC) product (Table 1). Then, we selected three regions to validate the resulting *R* values and their variability: the USA (EPA, 2001), Switzerland (Meusburger *et al.*, 2011), and the Ebro basin in Spain (Angulo-Martinez *et al.*, 2009). For these regions high resolution erosivity data are available obtained from pluviographic data from local meteorological stations across the whole region.

262 Figure 3 shows that the R values computed with the Renard and Freimund method strongly 263 overestimate R when compared to the high resolution R data of the selected regions. For the USA the *R* factor of Renard and Freimund shows an overall overestimation for western USA and for a 264 large part of eastern USA when compared to the high resolution R (Table 7 and Fig. 3A). 265 Especially a strong overestimation is seen for the north-west coast of the USA. This region is 266 267 known to have complex rainfall patterns due to the presence of mountains and high local precipitation intensities with frequent snow fall (Cooper, 2011). It should be noted that the USA 268 269 is not a completely suited case study for testing the R values computed with the Renard and Freimund method, as this method is based on climate data from stations in the USA. The 270 271 available high resolution or observed data on the R factor from Switzerland and the Ebro basin are better suited for an independent validation. 272

For Switzerland, which has a complex precipitation variability influenced by the relief of the Alps (Meusburger *et al.*, 2012), the *R* factor of Renard and Freimund shows a strong overall overestimation when compared to the high resolution *R* values (Table 7 and Fig. 3B). For the Ebro basin located in Spain, the observed *R* data were available for the period 1997-2006 from Angulo-Martinez *et al.*, 2009. Also here the method of Renard and Freimund overestimates the *R* factor and is not able to reproduce the high spatial variability of the *R* data (Table 7 and Fig. 3C).

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### **3.2** The linear multiple regression approach using environmental factors

To better represent the *R* factor on a global scale, the *R* estimation was based on the updated Köppen-Geiger climate classification (Table 3 and Fig. 4). The Köppen-Geiger climate classification is a global climate classification and is based on the vegetation distribution connected to annual cycles of precipitation and temperature (Lohmann *et al.*, 1993). The reason for this approach is that this classification system includes annual cycles of precipitation and is thus indirectly related to precipitation intensity. Based on this, it is possible to derive regression equations for the R factor that are applicable for each individual climate zone of the classification. This provides a basis to calculate the R factor with coarse resolution data on a global scale.

As a basis for deriving the regression equations for the *R* factor we used high resolution *R* maps of the USA from EPA (2001). The USA covers most of the world's climate zones and is also the largest region with available high resolution *R* data. Linear multiple regression was used to adjust *R*:

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$$\log(R_i) = \beta_0 + \sum_{j=1}^n \beta_{i_j} * \log(X_{i_j}) + \varepsilon_i$$
, for  $i = 1, 2, ..., n$  (13)

where *X* is the independent explanatory variable, *j* is the number of explanatory variables,  $\beta$  is a constant and  $\varepsilon$  is the residual.

The regression operates on one or more of the following parameters  $(X_i)$ : total annual 297 precipitation (GPCC 0.25 degree product), mean elevation (ETOPO 5 DEM), and the simple 298 precipitation intensity index, SDII. It should be mentioned that the SDII was only available on a 299 300 very coarse resolution of 2.5 degree resolution for certain regions on earth, such as parts of Europe and the USA. The SDII is calculated as the daily precipitation amount on wet days (>= 1301 mm) in a certain time period divided by the number of wet days in that period. Previous studies 302 303 that performed regression of R showed that precipitation and elevation were in most cases the only explanatory variables (Meusburger et al., 2012, Mikhailova et al., 1997, Goovaerts, 1999, 304 305 Diodato and Bellocchi, 2010, Angulo-Martinez et al., 2009). Here, we added to the regression the SDII as it is a simple representation of precipitation intensity, which is an important 306 explaining variable of the R factor. The precipitation and SDII datasets were rescaled to a 5 arc-307 minute resolution (corresponding to 0.0833 degree resolution) to match the Köppen-Geiger 308 309 climate classification data that was available at the resolution of 6 arc-minute (corresponding to 310 0.1 degree).

Furthermore, high resolution erosivity data from Switzerland (Meusburger *et al.*, 2011) and annual precipitation from the GPCC 0.5 degree product were used to derive the regression equations for the *R* factor for the polar (E) climate zones. These climate zones are not present in the USA. For the rest of the climate zones that are not present in the USA it was difficult to

obtain high resolution erosivity data. Therefore, we maintained the method of Renard and 315 Freimund for those climate zones to calculate erosivity. Also, we kept the R factor of the Renard 316 317 and Freimund method if no clear improvement of the R factor was found when using the new regression equations for a specific climate zone. Here, we mainly used the  $r^2$  combined with the 318 residual standard error to evaluate if the new regression equations showed a clear improvement 319 in the R factor. The Renard and Freimund R factors where kept for the hot arid climate zone 320 (BWh) and the temperate climate zone with a hot summer (Csa) in the USA. These are just two 321 climate zones out of the 17 evaluated ones, which show that the Renard and Freimun method 322 performs as good as or slightly better than the regression method. All datasets for deriving the R323 factor are described in Table 1. 324

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### 326 **3.3** Application of the linear multiple regression method on a global scale

Tables 4 and 5 show the resulting regression equations for climate zones for which we found 327 initially a low correlation between the R values calculated by the method of Renard and 328 Freimund and the high resolution R values from EPA (2001) and Meusburger *et al.* (2011). 329 Figure 5 shows for each addressed climate zone how the method of Renard and Freimund and 330 the new regression equations compare to the high resolution R of the USA. For the cold climate 331 zones with a dry summer (Ds) the new regression equations show only a slight improvement as 332 compared to the method of Renard and Freimund. Also for the polar climate zones (E) the new 333 regression equations still show a significant bias. However, they perform much better compared 334 to the method of Renard and Freimund. For most of the addressed climate zones the simple 335 precipitation intensity index (SDII) explains a large part of the variability in the R factor. The 336 elevation plays a smaller role here. Elevation can be an important explaining variable in regions 337 338 with a high elevation variability, which then affects the precipitation intensity.

From Table 4 and Table 6 it can be concluded that the *R* factor in climate zones without a dry season (f), can be easily explained by the total annual precipitation and the SDII. Dry climate zones, especially dry summer climate zones showed a weaker correlation. This is most probably due to the fact that the SDII is too coarse to explain the variability in the low precipitation intensity in the summer. It is also interesting to see that even though the SDII was derived from a very coarse resolution dataset, it turned out to be still important for deriving more accurate *R*values.

We also show for each addressed climate zone a comparison of the newly computed average R346 347 factor with the average high resolution R factor, and the uncertainty range (Table 6). The uncertainty range was computed by taking into account the standard deviation of each of the 348 parameters in the regression equations. As mentioned before, the polar climate zones (E) showed 349 the largest uncertainty range. The new regression equations significantly improved the R values 350 351 and spatial variability in the western USA, and lead to an average R factor that was closer to the 352 data mean (Table 7 and Fig. 6A). Although the new regression equations show a bias for the polar climate zones (E) (the minimum and maximum R values are not captured), the resulting 353 mean R values for Switzerland show a strong improvement (Table 7 and Fig. 6B). 354

355 Furthermore, the variability in the estimated R factor compares well with the variability of the high resolution R factor. It should be noted that Switzerland is not an independent case study for 356 357 the polar climate zones (E), as the high resolution R values from this case study were used in our regression analysis. However, the Ebro basin case study confirms the strong improvement for the 358 359 polar climate zones (E) (Fig. 6C). As the high resolution R values of the USA and Switzerland 360 were used to derive the regression equations, the third case study, the Ebro basin in Spain, provided an important independent validation. For the Ebro basin, the new regression equations 361 362 not only improve the overall mean but also capture the minimum R values better. This resulted in an improved representation of the *R* variability (Table 7 and Fig. 6C). In Fig. 6C, however, there 363 364 is a clear pattern separation in the newly computed R values, which is due to the fact that the SDII data are not available for part of the Ebro basin. As mentioned before, SDII is an important 365 explaining parameter in the regression equations for most of the addressed climate zones. 366

Figure 7A shows the global patterns of the estimated *R* factor from the method of Renard and Freimund and the new regression equations. Figure 7B shows a difference plot between the estimated *R* factor with the method of Renard and Freimund and the *R* factor estimated with the new regression equations. The new regression equations significantly reduced the *R* values in most regions. However, the tropical regions still show unrealistic high *R* values (maximum *R* values go up to  $1 * 10^5$  MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>). This is because the *R* factor was not adjusted for the tropical climate zones due to the lack of high resolution *R* data. Oliveira *et al.* (2013) found for the *R* factor in Brazil that the maximum *R* values for the tropical climate zones reach 22,452 MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>. We find *R* values in Brazil that exceed this maximum *R* value found by Oliveira *et al.* (2013).

377 Finally, it should be noted that the purpose of the adjusting methods for the S and R factors in this study is to capture more accurately the large scale mean erosion rates rather than the 378 extremes. Therefore, even though the new regression equations are still not accurate enough for 379 certain climate zones, it is important that the average R factor is represented well. The approach 380 381 for adjusting the R factor also showed that although there is no high temporal resolution 382 precipitation intensity data available on a global scale, the R factor can still be represented well for most climate zones on a large spatial scale. This can be done by using other parameters, such 383 as elevation, and especially a representative of precipitation intensity, such as the SDII. The SDII 384 played an important role here as it improved the estimation of the R factor significantly, even 385 386 though data was only available at a very low resolution as compared to the other datasets of 387 precipitation, elevation and climate zone classification.

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### **Global application of the adjusted RUSLE model**

### **4.1** Computation of the soil erodibility and land cover factors

391 In the following we demonstrate the consequences of the new parameterizations of the S and R392 factors for global soil erosion rates. First, we compute the other individual RUSLE factors, soil 393 erodibility (K) and crop cover (C). Estimations of the K factor we based on soil data from the gridded 30 arc-second Global Soil Dataset for use in Earth System Models (GSCE). GSCE is 394 395 based on the Harmonized World Soil database (HWSD) and various other regional and national soil databases (Shangguan et al., 2014). We used the method of Torri et al. (1997) to estimate the 396 K factor, and gave volcanic soils a K factor of 0.08 t ha h ha<sup>-1</sup> MJ<sup>-1</sup> mm<sup>-1</sup>. This because these soil 397 types are usually very vulnerable to soil erosion, and the observed K values are beyond the range 398 399 predicted by the method of Torri et al. (1997) (van der Knijff et al., 1999). To account for the 400 effect of stoniness on soil erosion we used a combination of the methods by Cerdan et al. (2010) and Doetterl et al. (2012), who based their methods on the original method of Poesen et al. 401 (1994). For non-agricultural areas we used the method of Cerdan et al. (2010), where they 402 403 reduced the total erosion by 30 % for areas with a gravel percentage larger or equal to 30 %. For

agricultural and grassland areas we used the method of Doetterl *et al.* (2012), where erosion was
reduced by 80 % in areas where the gravel percentage exceeded 12 %.

406 We calculated the C factor according to the method of De Jong et al. (1998), using 0.25 degree 407 Normalized Difference Vegetation Index (NDVI) and land use data for the year 2002. An important limitation of this method is the fact that in winter the C factor is estimated too high 408 (van der Knijff et al., 1999). This is because the method does not include the effects of mulch, 409 decaying biomass and other surface cover reducing soil erosion. To prevent the C factor of being 410 411 too high, maximum C values for forest and grassland of 0.01 and 0.05 for pasture were used. 412 Doetterl et al. (2012) showed that the slope length (L) and support practice (P) factors do not contribute significantly to the variation in soil erosion at the continental scale to global scale, 413 when compared to the contribution of the other RUSLE factors (S, R and C). However, this does 414 not mean that their influence on erosion should be ignored completely. They may play an 415 416 important role in local variation of erosion rates. In our erosion calculations we do not include 417 these factors, because we have too little or no data on these factors on a global scale. Including 418 them in the calculations would only add an additional large uncertainty to the erosion rates. This would make it more difficult to judge the improvements we made to the S and R factors. 419

420

# 421 **4.2** Computation of global soil erosion rates and comparison to empirical 422 databases

We applied the RUSLE model with the settings mentioned in the previous paragraph on a 5 arcminute resolution on global scale for the present time period (see time resolutions of datasets in Table 1). We calculated global soil erosion rates with four different versions of the RUSLE model: (a) the unadjusted RUSLE, (b) RUSLE with only an adjusted *S* factor, (c) RUSLE with only an adjusted *R* factor and (d) the adjusted RUSLE (all adjustments included).

We found a global average soil erosion rate for the adjusted RUSLE of 6.5 t ha<sup>-1</sup> year<sup>-1</sup> (Fig. 8A). When including the uncertainty arising from applying the linear multiple regression method, the mean global soil erosion rate differs between 5.3 and 15 t ha<sup>-1</sup> year<sup>-1</sup>. Furthermore, the RUSLE version with only an adjusted *S* factor shows the highest average global soil erosion rate, while the lowest rate is found for the RUSLE version with only the adjusted *R* factor (Table 8). Figure 8C shows the difference between the erosion rates of the S adjusted RUSLE and the unadjusted

RUSLE versions. The erosion rates are in general increased here, and mostly pronounced in 434 mountainous regions. This feature is 'dampened' when adjusting the R factor. The difference 435 436 between the R adjusted RUSLE and unadjusted RUSLE versions (Fig. 8D) shows that the 437 erosion rates are overall decreased in regions where the adjustments are made. When combining both adjustments of the RUSLE model in the fully adjusted RUSLE version and subtract the 438 unadjusted RUSLE erosion rates (Fig. 8B), erosion rates are slightly decreased in areas where the 439 R factor is adjusted. However, for the tropics there an increase in erosion rates is found in the 440 fully adjusted RUSLE due to the lack of adjusting the R factor there. This indicates that these 441 two factors balance each other, and that it is important to have a correct representation of all the 442 RUSLE factors on a global scale in order to predict reliable erosion rates. 443

In this study the *K* and *C* factors are not tested and adjusted for a coarse resolution at global scale and thus validation with existing empirical databases on soil erosion is not fully justified. However, to test if the global erosion rates are in an acceptable range, they are compared to erosion estimates from the NRI database for the USA, and erosion estimates from the study of Cerdan *et al.* (2010) for Europe. These are to our knowledge the only large scale high resolution empirical databases on soil erosion.

450 The NRI database contains USLE erosion estimates for the year 1997, which are available at the Hydrologic Unit 4<sup>th</sup> Code (HUC4) watershed level. We aggregated the resulting erosion rates 451 from the adjusted and unadjusted RUSLE models to the HUC4 watershed level. The results show 452 453 that the average erosion rates from the adjusted RUSLE model come closer to that of the NRI 454 database (Table 9 and Fig. 9A). However, the maximum average HUC4 soil erosion rate from 455 the adjusted RUSLE is somewhat higher compared to the NRI database. From these results we can conclude that the erosion rates of the adjusted RUSLE fall in the range of observed values, 456 457 but that there are still some local overestimations. Some of these overestimations can be found in 458 south west of the USA where the adjusted RUSLE shows a slightly worse performance 459 compared to the unadjusted RUSLE. The R factor in this region was not changed as it was already estimated well by the method of Renard and Freimund, however, the S factor increased 460 461 due to the hilly terrain. Without adjusting the other RUSLE factors (K and C), this resulted in an overall increase in soil erosion rates. This indicates that the other RUSLE factors may play an 462 463 important role in this region. Furthermore, we see that along the west coast of the USA the 464 erosion values are not much improved with the adjusted RUSLE model. This is mainly because some climate zones such as the temperate climate zone with a dry and warm summer (Csb)
prevail in this region, for which the *R* factor is still difficult to estimate in a correct way (Table
467 4).

468 For Europe, Cerdan et al. (2010) used an extensive database of measured erosion rates on plots under natural rainfall. They extrapolated measured erosion rates to whole Europe (European 469 Union area) and adjusted them with a topographic correction. This correction was based on the L 470 and S factors of the RUSLE model. They also applied a correction to account for soil stoniness. 471 472 For comparison, the soil erosion rates from Cerdan et al. (2010) and the RUSLE estimates in our 473 study are aggregated at country level. The performance of the adjusted RUSLE model was not as 474 good for Europe as compared to the USA. This is not surprising as the RUSLE model is based on soil erosion data of the USA. However, also on the European scale the adjusted RUSLE model 475 476 performed better than the unadjusted RUSLE model (Table 9 and Fig. 9B). Especially the large 477 erosion rates in the south of Europe as observed in the results of the unadjusted RUSLE model 478 are less extreme in the adjusted RUSLE model. Still, the overall average erosion rate for Europe 479 is overestimated by approximately two times (Table 9).

480 The biases in erosion rates as seen for the south west of the USA and south Europe can be 481 attributed to several factors. As mentioned before, the other RUSLE factors (K and C) and the way they interact with the R and S factors are not adjusted to the coarse resolution at global 482 483 scale. We found no clear signal for which land cover types the adjusted RUSLE performs better 484 or worse. In general, we can see that the adjusted RUSLE model still overestimates erosion rates 485 for most land cover types. A short analysis for Europe showed that the largest biases are found 486 for shrubs, and the least for grassland. However, a more explicit analysis is needed to find out how we can improve the contribution of land cover and land use to erosion rates in the RUSLE 487 model. Explicitly including the interaction between the C and R factor on a monthly timescale 488 489 could be crucial. This is very important for example in areas with agriculture, and areas with a 490 strong seasonal character. Another aspect related to improving the C factor is looking at the location of land use in a certain grid cell. If the land use in a grid cell is located on steep slopes 491 492 the resulting erosion in that grid cell would be higher than when it would be located in the flatter areas. In this study, however, only mean fractions of land cover and the NDVI are used for each 493 494 grid cell. This can lead to possible biases in the resulting erosion rates.

495 Furthermore, land management is not accounted for in this study, which could introduce an important systematic bias in the soil erosion rates for especially agricultural areas. Land 496 497 management is represented by the P factor in the original USLE, however, it is partly also incorporated in the C factor for agricultural land use through plant residues, cover crops and 498 tillage. A limitation of the NDVI approach to estimate the C factor lies therefore in the inability 499 500 to estimate this land management effect. Applying this method also limits the interaction between the R and C factors on a monthly to seasonally scale, because this interaction is partly 501 502 based on land management.

503 Furthermore, uncertainties in the coarse resolution land cover/land use, soil and precipitation datasets that are not accounted for, can lead to the model biases. Also, better adjustment of the R504 factor for climate zones such as the polar climates (E) could help improving the overall results. 505 Some biases in the erosion rates can also be attributed to the fact that stepped relief, where flat 506 507 plateaus are separated by steep slopes, are not well captured by the 150 m target resolution used 508 in the fractal method to scale slope. In this way erosion would be overestimated in these areas. 509 Finally, errors and limitations in the observational datasets can also contribute to the differences between model and observations. The study of Cerdan et al. (2010) on Europe for example, used 510 extrapolation of local erosion data to larger areas that could introduce some biases. Also, the 511 underlying studies on measured erosion rates used different erosion measuring techniques that 512 513 can be linked to different observational errors.

514

### 515 **5 Conclusions**

516 In this study we introduced specific methods to adjust the topographical and rainfall erosivity 517 factors to improve the application of the RUSLE model on global scale, using coarse resolution 518 input data.

519 Our results show that the fractal method by Zhang *et al.* (1999) and Pradhan *et al.* (2006) can be 520 applied on coarse resolution DEMs to improve the resulting slope. Although the slope 521 representation improved after applying this method, the results still show a slight dependence on 522 the original grid resolution. This is attributable to several factors such as the underlying 523 assumption that the standard deviation of elevation ( $\sigma$ ) is independent of the DEM resolution, 524 and to the breakdown of the fractal method at certain scales. 525 We compared the rainfall erosivity calculated by the method of Renard and Freimund to available high resolution or observed erosivity data of the USA, Switzerland and the Ebro basin. 526 527 We find that this method results in overall significant biases in erosivity. Therefore, we implemented a linear multiple regression method to adjust erosivity for climate zones of the 528 Köppen-Geiger climate classification system in the USA. Using precipitation, elevation and the 529 simple precipitation intensity index as explaining parameters, the resulting adjusted erosivity 530 compares much better to the observed erosivity data for the USA, Switzerland and the Ebro 531 532 basin. Not only the mean values but also the spatial variability in erosivity is improved. It was surprising to notice that using the rather coarse resolution simple precipitation intensity index in 533 the regression analysis made it possible to explain much of the variability in erosivity. This, once 534 more, underpins the importance of precipitation intensity in erosivity estimation. 535

After calculating the newly adjusted erosivity on global scale, it is apparent that the tropical climate zones, for which erosivity was not adjusted, show strong overestimations in some areas. This shows that adjusting erosivity for the tropical climate zones should be the next step. The challenge is to find enough reliable long term and high resolution erosivity data for those regions.

541 To investigate how the adjusted topographical and rainfall erosivity factors affect the global soil erosion rates, we applied the adjusted RUSLE model on global scale. We found an average 542 global soil erosion rate of 6.5 t ha<sup>-1</sup> year<sup>-1</sup>. It is, however, difficult to provide accurate uncertainty 543 estimates to these global erosion rates, and to provide a good validation with observations. This 544 545 is due to lack of high resolution data on other individual RUSLE factors such as the land cover, 546 soil erodibility, slope length and support practice. These RUSLE factors are therefore not adjusted for application on a coarse resolution on global scale. We argue that it is important to 547 focus on adjusting the other RUSLE factors, for an improved application of the RUSLE model 548 549 on global scale. The next step would be to better capture the anthropogenic contribution to global 550 soil erosion. This can be done by adjusting first of all the land cover factor to a coarse resolution application, and focus on the interaction of this factor with rainfall erosivity on a monthly to 551 seasonal basis. This is important, because the land cover factor has strong interactions with the 552 rainfall erosivity factor, and includes the effect of human activities on erosion through 553 554 agricultural activities and land management.

555 To test if the soil erosion rates from the adjusted RUSLE model are in a realistic range, we compared the results to the USLE erosion estimates for the USA from the NRI database, and the 556 557 erosion estimates for Europe from the study of Cerdan et al. (2010). The adjusted RUSLE soil erosion rates, which we aggregated to the watershed level, show a better comparison with the 558 NRI USLE estimates than the unadjusted RUSLE erosion rates. For Europe the comparison of 559 560 the adjusted RUSLE soil erosion rates to the study of Cerdan et al. (2010) were not as good as for the USA. This is not surprising due to the fact that the parameterizations of the RUSLE 561 model are based on soil erosion data of the USA. However, also for Europe, the adjusted RUSLE 562 model performs better than the unadjusted RUSLE model. 563

We find overestimations by the adjusted RUSLE model for hilly regions along the west coast of the USA, and for south of Europe. We argue that besides for reasons mentioned before, these biases are due to the fact that the topographical detail may not be enough in some regions to capture the true variability in soil erosion effects by topography. Also, erosivity could not be adjusted for some climate zones that are not present in the USA or Switzerland, and needs to be further improved for climate zones such as the polar climate zones.

We conclude that even though there is still much improvement of the RUSLE model possible with respect to topography and erosivity, the methods proposed in this study seem to be promising tools for improving the global applicability of the model. A globally applicable version of the RUSLE model, together with data on environmental factors from Earth System Models (ESMs), can provide the possibility for future studies to estimate accurate soil erosion rates for the past, current and future time periods.

576

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# Table 1. List of datasets used in this study

Category	Dataset	Source	Spatial	Tempo	ral-	Variables
			resolution	period		
DEM	GTOPO Elevation Model	USGS, 1996, Gesch et al.,	30 arc-seconds			elevation
		1999				
	ETOPO1 Elevation	Amante and Eakins, 2009	1 arc-minute			elevation
	Model					
	ETOPO2 Elevation	US Department of	2 arc-minute			elevation
	Model	Commerce and NOAA,				
		2001				
	ETOPO5 Elevation	National Geophysical Data	5 arc-minute			elevation
	Model	Center/NESDIS/NOAA,				
		1995				
Climate	GPCC 0.5 degree dataset	Schneider et al., 2011	0.5 degrees	Years	1989-	total yearly
				2010		precipitation
	GPCC 0.25 degree	Meyer-Christoffer et al.,	0.25 degrees	years	1951-	total yearly

	dataset	2011		2000	precipitation
	GHCNDEX dataset	CLIMDEX (Donat et al.,	2.5 degrees	years 1951-	simple precipitation
		2013)		present	intensity index (SDII)
	Köppen-Geiger dataset	Peel et al., 2007	5 arc-minute		Köppen-Geiger
					climate classifications
Soil	Global Soil Dataset for	Shangguan et al., 2014	30 arc-seconds		sand, silt and clay
	use in Earth System				fractions, organic
	Models (GSCE)				matter %, gravel %
	Harmonized World Soil	Nachtergaele et al., 2012	30 arc-seconds		volcanic soils
	Database (HWSD)				
	version 1.2				
Land-cover	GIMMS dataset	ISLSCP II (Tucker et al.,	0.25 degrees	year 2002	Normalized difference
		2005, Hall et al., 2006			vegetation index
					(NDVI)
Land-use	MODIS dataset	ISLSCP II (Friedl et al.,	0.25 degrees	year 2002	Land use fractions
		2010, Hall et al., 2006)			

Table 2. Fractal parameters and the resulting mean global slopes before and after applying the fractal method on the different DEMs; Increase of slope means the increase of the average global slope of a DEM after applying the fractal method; difference after scaling  $-\frac{\theta_{scaled}(DEM) - \theta_{scaled}(GTOPO_{30})}{\theta_{scaled}(GTOPO_{30})} + 100$ ; difference before accling  $-\frac{\theta_{scaled}(DEM) - \theta_{scaled}(GTOPO_{30})}{\theta_{scaled}(GTOPO_{30})} + 100$ ;

		standard deviation of		mean				difference after	difference before
DEM	resolution	elevation	mean D	$\alpha_{steepest}$	$\theta$	$ heta_{scaled}$	Increase of $\theta$	scaling	scaling
	arc-minute	m			m m-1	m m-1	%	%	%
GTOPO30	0.5	570	1.32	0.99	0.023	0.059	61	0	0
ETOPO1	1	530	1.35	1.08	0.016	0.057	71.9	-3.4	-30.4
ETOPO2	2	549	1.37	1.17	0.011	0.055	80	-6.8	-52.2
ETOPO5	5	562	1.42	1.25	0.006	0.054	88.9	-8.5	-73.9

 $=\frac{\theta_{scaled(DEM)} - \theta_{scaled(GTOPO30)}}{\theta_{scaled(GTOPO30)}} * 100; \text{ difference before scaling} = \frac{\theta_{(DEM)} - \theta_{(GTOPO30)}}{\theta_{(GTOPO30)}} * 100$ 

1st	2nd	3rd	Descri	ption		Criteria*
Α			Tropic	al		T <sub>cold</sub> >=18
	f		-	Rainforest		P <sub>dry</sub> >=60
						Not (Af) & P <sub>dry</sub> >=100-
	m		-	Monsoon		MAP/25
	W		-	Savannah		Not (Af) & P <sub>dry</sub> <100–MAP/25
В			Arid			MAP<10×P <sub>threshold</sub>
	W		-	Desert		$MAP < 5 \times P_{threshold}$
	S		-	Steppe		MAP>=5×P <sub>threshold</sub>
		h		<ul> <li>Hot</li> </ul>		MAT>=18
		k		<ul> <li>Cold</li> </ul>		MAT<18
С			Tempe	erate		$T_{hot}$ 10&0< $T_{cold}$ <18
	S		-	Dry Summer		P <sub>sdry</sub> <40&P <sub>sdry</sub> <p<sub>wwet/3</p<sub>
	w		-	Dry Winter		P <sub>wdry</sub> <p<sub>swet/10</p<sub>
	f		-	Without dry sea	son	Not (Cs) or (Cw)
		а		•	Hot Summer	T <sub>hot</sub> >=22
		b		•	Warm Summer	Not (a) & T <sub>mon10</sub> >=4
		С		•	Cold Summer	Not (a or b) & 1<=T <sub>mon10</sub> <4
D			Cold			$T_{hot}$ >10& $T_{cold}$ <=0
	S		-	Dry Summer		P <sub>sdry</sub> <40&P <sub>sdry</sub> <p<sub>wwet/3</p<sub>
	w		-	Dry Winter		P <sub>wdry</sub> <p<sub>swet/10</p<sub>
	f		-	Without dry sea	son	Not (Ds) or (Dw)
		а		•	Hot Summer	T <sub>hot</sub> >=22
		а		•	Warm Summer	Not (a) & T <sub>mon10</sub> >=4
		с		•	Cold Summer	Not (a, b or d)
		d		•	Very Cold Winter	Not (a or b) & T <sub>cold</sub> <=-38
E			Polar			T <sub>hot</sub> <10
	Т		-	Tundra		T <sub>hot</sub> >0
	F		-	Frost		T <sub>hot</sub> <-0

Table 3. Description of Köppen climate symbols and defining criteria (from Peel et al., 2007).

\* MAP = mean annual precipitation, MAT = mean annual temperature,  $T_{hot}$  = temperature of the hottest month,  $T_{cold}$  = temperature of the coldest month,  $T_{mon10}$  = number of months where the temperature is above 10,  $P_{dry}$  = precipitation of the driest month,  $P_{sdry}$  = precipitation of the driest month in summer,  $P_{wdry}$  = precipitation of the driest month in winter,  $P_{swet}$  = precipitation of the wettest month in summer,  $P_{wwet}$  = precipitation of the wettest month in winter,  $P_{threshold}$  = varies according to the following rules (if 70% of MAP occurs in winter then  $P_{threshold}$  = 2 x MAT, if 70% of MAP occurs in summer then  $P_{threshold}$  = 2 x MAT + 28, otherwise  $P_{threshold}$  = 2 x MAT + 14). Summer (winter) is defined as the warmer (cooler) six month period of ONDJFM and AMJJAS.

Table 4. Linear multiple regression equations for different climate zones, relating high resolution R factor from the USA with one or more significant parameters: annual total mean precipitation, P (mm), mean elevation, z (m), and the simple precipitation intensity index, *SDII* (mm/day).

Climate	Explaining	Regression function - optimal	$R^2$	Residual standard error
zone	parameters			
BWk	P, SDII	$R = 0.809 * P^{0.957} + 0.000189 * SDII^{6.285}$		
BSh	P, SDII	$\log R = -7.72 + 1.595 * \log P + 2.068 * \log SD11$	0.97	0.22
BSk	P, SDII, Z	$\log R = 0.0793 + 0.887 * \log P + 1.892 * \log SD11 - 0.429 * \log Z$	0.89	0.35
Csb	Р	$R = 98.35 + 0.000355 * P^{1.987}$		0.16
Cfa	P, SDII, Z	$\log R = 0.524 + 0.462 * \log P + 1.97 * \log SDII - 0.106 * \log Z$	0.89	0.11
Cfb	P, SDII	$\log R = 4.853 + 0.676 * \log P + 3.34 * \log SD11$	0.97	0.21
Dsa	Z, SDII	$\log R = 8.602 - 0.963 * \log SD11 - 0.247 * \log Z$	0.51	0.05
Dsb	Р	$\log R = 2.166 + 0.494 * \log P$	0.45	0.25
Dsc	SDII	$\log R = 6.236 - 0.869 * \log SD11$	0.51	0.02
Dwa	Р	$\log R = -0.572 + 1.238 * \log P$	0.99	0.02
Dwb	P, SDII	$\log R = -1.7 + 0.788 * \log P + 1.824 * \log SD11$	0.98	0.02
Dfa	P, SDII	$\log R = -1.99 + 0.737 * \log P + 2.033 * \log SD11$	0.9	0.16
Dfb	P, SDII, Z	$\log R = -0.5 + 0.266 * \log P + 3.1 * \log SD11 - 0.131 * \log Z$	0.89	0.32
Dfc	SDII	$\log R = -1.259 + 3.862 * \log SD11$	0.91	0.23
ET	Р	$\log R = -3.945 + 1.54 * \log P$	0.14	0.42

EF+EFH	Р	$\log R = 16.39 - 1.286 * \log P$	0.6	0.13
ETH	P, SDII	$\log R = 21.44 + 1.293 * \log P - 10.579 * \log SDII$	0.52	0.53

Table 5. Linear multiple regression equations for different climate zones for regions that have no data on the simple precipitation intensity index, *SDII* (mm/day). The regression equations relate high resolution erosivity from the USA with the annual total mean precipitation, P (mm), and/or the mean elevation, z (m).

Climate zone	Optimal regression function	$\mathbf{R}^2$	Residual
	(when SDII is not available)		standard error
BWk	Method Renard & Freimund (1994)		
BSh	$\log R = -8.164 + 2.455 * \log P$	0.86	0.5
BSk	$\log R = 5.52 + 1.33 * \log P - 0.977 * \log Z$	0.76	0.52
Cfa	$\log R = 3.378 + 0.852 * \log P - 0.191 * \log Z$	0.57	0.23
Cfb	$\log R = 5.267 + 0.839 * \log P - 0.635 * \log Z$	0.81	0.5
Dsa	$\log R = 7.49 - 0.0512 * \log P - 0.272 * \log Z$	0.48	0.06
Dsc	$\log R = 4.416 - 0.0594 * \log P$	0.015	0.03
Dwb	$\log R = 1.882 + 0.819 * \log P$	0.81	0.08
Dfa	$\log R = -2.396 + 1.5 * \log P$	0.65	0.29
Dfb	$\log R = 1.96 + 1.084 * \log P - 0.34 * \log Z$	0.74	0.48
Dfc	$\log R = -3.263 + 1.576 * \log P$	0.56	0.49
ETH	$\log R = -10.66 + 2.43 * \log P$	0.4	0.59

	observed	Renard &	adjusted	
		Freimund	method	
		method		Adjusted method
climate	<i>R</i> mean	R mean	R mean	uncertainty range
BWk	284	533	291	158-495
BSh	2168	1356	2207	1723-2828
BSk	876	884	885	749-1046
Csb	192	1136	192	133-292
Cfa	5550	5607	5437	4830-6123
Cfb	1984	5359	1971	1431-2715
Dsa	172	445	171	86-340
Dsb	175	896	168	151-187
Dsc	115	374	115	91-145
Dwa	1549	1444	1551	1280-1879
Dwb	1220	1418	1214	1057-1395
Dfa	2572	2983	2582	2346-2843
Dfb	1101	1798	1124	922-1371
Dfc	483	701	483	423-552
ET	1352	6257	1249	23-68088
EF+EFH				
	1468	5469	1450	16-132001
ETH	945	5580	832	0-6314918

Table 6. Mean high resolution *R* values (MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>) from the USA and Switzerland and mean modelled *R* values with uncertainty range for each addressed climate zone

Table 7. Statistics of the comparison of high resolution R values (MJ mm ha <sup>-1</sup> h <sup>-1</sup> year <sup>-1</sup> ) from three regions to estimated R values	
from the Renard and Freimund method and the new regression equations	

	Observed			Estimated – R	enard & Frei	imund			Estimated – 1	nultiple linear	regression		
	Range	Mean	Standard deviation	Range	Mean	Standard deviation	Correlation coefficient	Rank correlation coefficient	Range	Mean	Standard deviation	Correlation coefficient	Rank correlation coefficient
Switzerland	121-6500	1204	833	2335-10131	5798	1654	0.51	0.42	225-2572	1256	472	0.49	0.3
the USA (aggregated huc4)	105-4963	1271	1174	57-15183	1870	2088	0.51	0.68	60-15808	1691	2188	0.58	0.83
Ebro basin	40 - 4500	891	622	747 - 5910	1529	846	-	-	167 - 4993	836	701	-	-

		25th	50th	75th paraantila	00th managentile
	mean	percentile	percentile	75th percentile	90th percentile
RUSLE unadjusted	4.5	0.2	0.7	2.4	7.5
RUSLE adjusted with S	9.8	0.3	1.0	3.8	13.5
RUSLE adjusted with R	3.2	0.1	0.5	1.7	5.7
RUSLE adjusted with S & R	6.5	0.1	0.7	2.7	9.6

Table 8. Comparison of the global erosion rates (t ha<sup>-1</sup> year<sup>-1</sup>) and percentiles between different versions of the RUSLE model

Table 9. Statistics of the observed and modelled erosion rates from the unadjusted and adjusted versions of the RUSLE for the USA and Europe (t  $ha^{-1} year^{-1}$ )

		Observa	tions		Adjusted RUSLE				Unadjusted RUSLE			
Region	Source											
				Standard			Standard		Standard			
		Range	Mean	deviation	Range	Mean	deviation	Range	Mean	deviation		
Europe (Aggregation country level) no small countries	Cerdan <i>et</i> <i>al.</i> , 2010	0.1-2.6	0.9	0.7	0.1-7	2.3	2.1	0-14	2.8	3.6		
the USA (Aggregation HUC4 level)	NRI database	0-11	1.6	2.1	0.2-13	1.6	1.9	0-14	1.4	1.8		

Figure 1. Global average unscaled slope estimated from different coarse resolution digital elevation models (DEMs) as function of their resolution (blue); and global average scaled slope from the same DEMs as function of their resolution (red).

Figure 2. (A) A global map of the scaled slope derived from the 30 arc-second DEM using a target resolution of 150m; (B) A global map showing the difference between the unscaled and scaled slopes (in degrees), where blue colours show an underestimation by the unscaled slope when compared to the scaled slope and reddish colours show and overestimation.

Figure 3. Spatial difference plots showing the difference between the high resolution R values and R values calculated with the method of Renard and Freimund for (A) the USA, (B) Switzerland and (C) the Ebro basin in Spain; In (A) and (B) the blue colours show an underestimation of the calculated R factor when compared to the high resolution R values, while the red colours show an overestimation; the Ebro basin serves here as an independent validation set and it has two graphs, (C1) a spatial plot of erosivity according to Renard and Freimund, and (C2) the high resolution R values from Angulo-Martinez *et al.* (2009); All values in the graphs are in MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>.

Figure 4. The Köppen-Geiger climate classification global map at a resolution of 5 arc-minute (Peel *et al.*, 2007).

Figure 5. Comparison of high resolution R factor data and predicted R values from (1) the Renard and Freimund method and (2) the new regression equations, for various climate zones;

the red line is the 1 tot 1 line, and does not appear in some graphs because predicted *R* values are overestimated.

Figure 6. Spatial difference plots showing the difference between the high resolution R values and R values calculated with the new regression equations for (A) the USA, (B) Switzerland and (C) the Ebro basin in Spain; In (A) and (B) the blue colours show an underestimation of the calculated R values when compared to the high resolution R values, while the red colours show an overestimation; the Ebro basin serves here as an independent validation set and it has two graphs, (C1) a spatial plot of the R factor according to the new regression equations, and (C2) the high resolution R values from Angulo-Martinez et al. (2009); All values in the graphs are in MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>.

Figure 7. (A) Global distribution of the new modelled *R* values according to the new regression equations; and (B) a difference map between *R* values calculated according to the method of Renard and Freimund and the new modelled *R* values (MJ mm ha<sup>-1</sup> h<sup>-1</sup> year<sup>-1</sup>), where blue colours indicate lower *R* values by Renard and Freimund compared to the new modelled *R* values, while redish colours indicate higher *R* values; map resolution is 5 arc-minute.

Figure 8. (A) Global yearly averaged erosion rates according to the fully adjusted RUSLE model; (B) a difference map between the fully adjusted and unadjusted RUSLE model; (C) a difference map between the adjusted S RUSLE and the unadjusted RUSLE model; (D) a difference map between the adjusted R RUSLE and the unadjusted RUSLE model; in figures B,C and D the reddish colors show an overestimation of by the adjusted RUSLE model and

yellow to bluish colors show an underestimation; resolution of all maps is 5 arc-minute and all units are in t ha<sup>-1</sup> year<sup>-1</sup>.

Figure 9. (A) Difference plots between soil erosion estimates from the NRI database for the USA and estimates of (A1) the unadjusted RUSLE model, and of (A2) the adjusted RUSLE model; all aggregated at HUC4 watershed level; (B) Difference plots between soil erosion estimates from the database of Cerdan *et al.* (2010) for Europe and estimates of (B1) the unadjusted RUSLE model and of (B2) the adjusted RUSLE model; all aggregated at country level; reddish colors represent an overestimation (t ha<sup>-1</sup> year<sup>-1</sup>) while the bluish represent and underestimation (t ha<sup>-1</sup> year<sup>-1</sup>) compared to the erosion values from the databases.

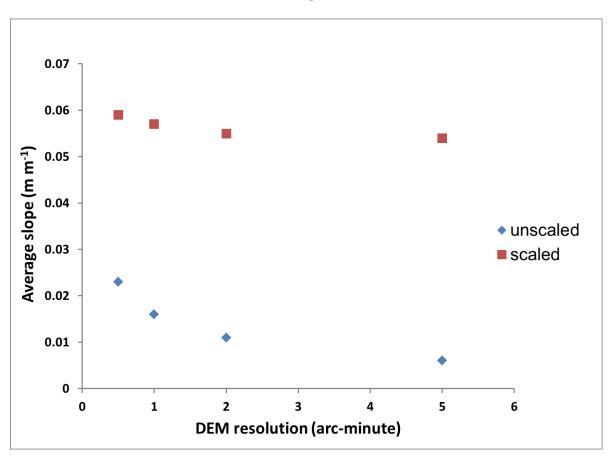
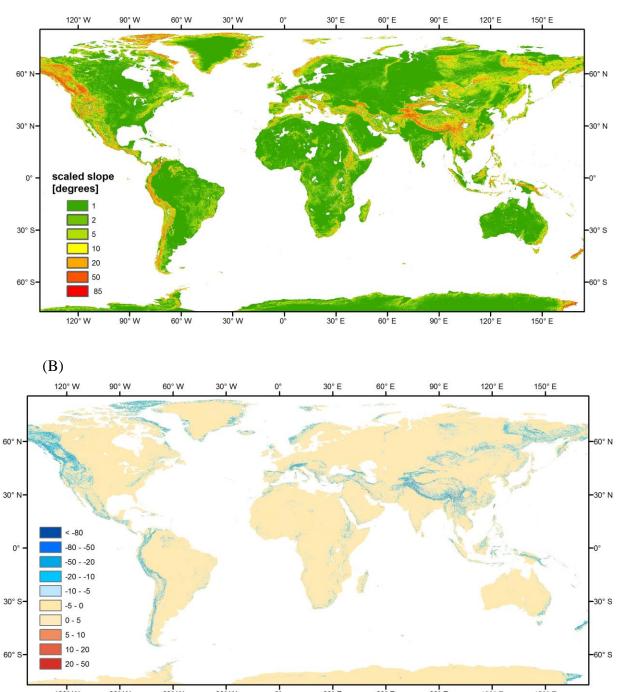


Figure 1

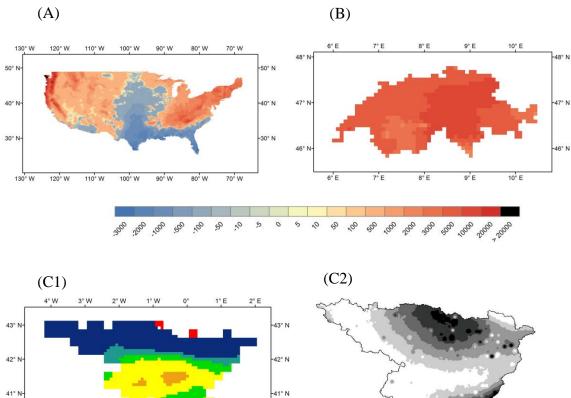


(A)



120° W 90° W 60° W 30° W 0° 30° E 60° E 90° E 120° E 150° E







40° N-

80°,00°, 120°, 120° 150° 800





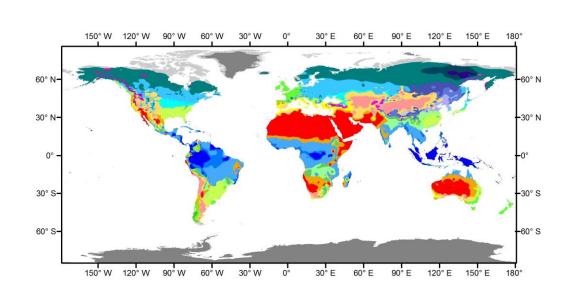
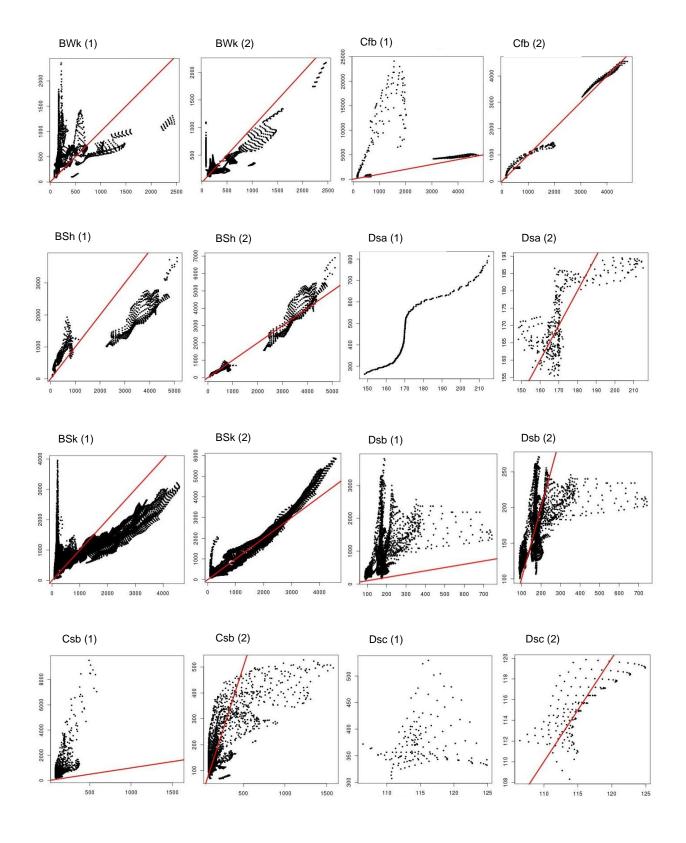
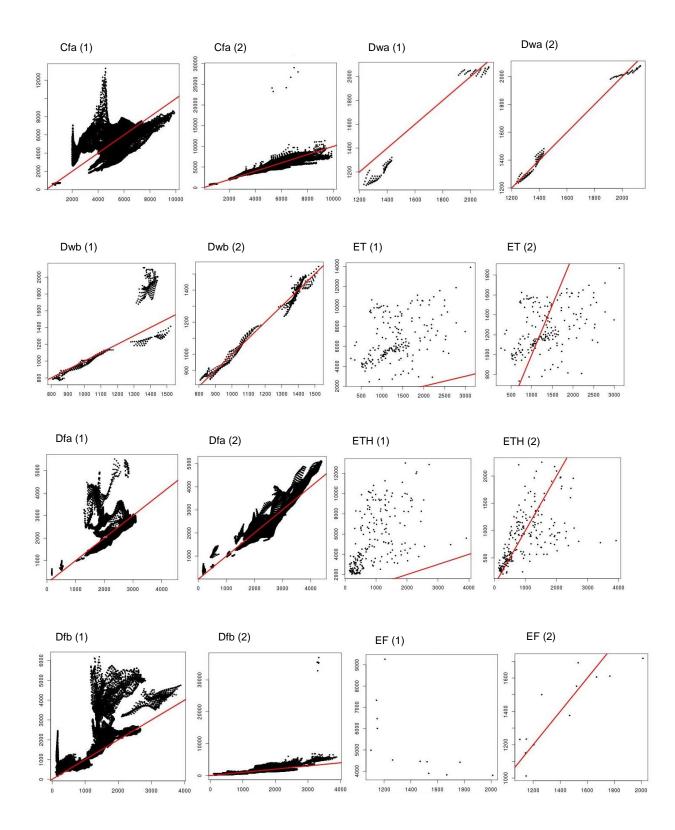
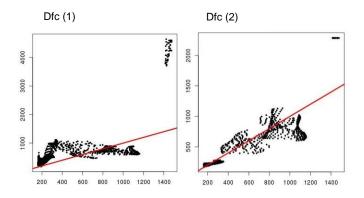


Figure 5

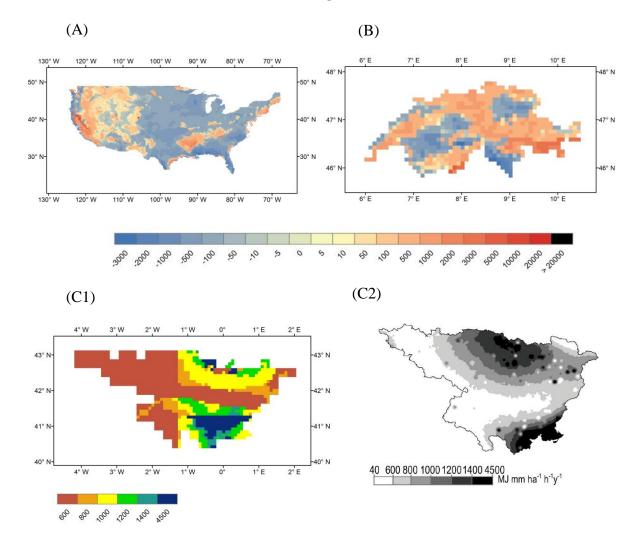


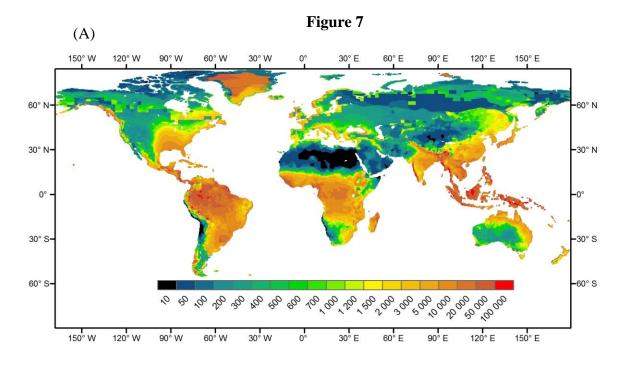
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## Figure 6





(B)

