We thank both of the referees, as well as the editor Andrew Yool, for their close reading of the manuscript, and their thoughtful, constructive comments.

Reviewer comments are in bold, and are followed by our response, and then by changes and/or additions to the text.

At the end of the responses, we provide the marked-up version showing the differences between the first and revised submissions.

Anonymous Referee #1

-Page 10147, line 19: Consider rewording "has the potential to transform" to something more definite as we're already seeing impacts of climate change on temperature distribution (e.g., Pinksy et al. 2013 Science, Walsh et al. 2015 PLoS ONE).

We have changed the sentence as follows:

<u>Original</u>

Anthropogenic climate change, on the other hand, has the potential to transform the ocean temperature distribution and thereby alter marine ecosystems by affecting elements of ocean circulation that drive nutrient dynamics and primary production (Doney et al., 2012).

Revised

Anthropogenic climate change, on the other hand, is already altering nutrient dynamics and primary production through its effects on ocean temperature and circulation (Doney et al., 2012), with demonstrated consequences on the distributions of several fish populations (Pinsky et al, 2013; Walsh et al., 2015).

-Page 10150, lines 24 – 26: Consider stating that these three groups are independent "species groups" and that fish don't grow into the next larger size spectrum. In other words, "small" consists of fish that remain small

throughout their life history and not the juveniles of "medium" and "large". This becomes clear later in the paper, but it would eliminate confusion by clarifying early on.

We have changed the sentence as follows:

<u>Original</u>

We consider three populations of fish at every grid point, and so resolve three biomass spectra. These populations, which we refer to as groups, represent small, medium, and large fish, and allow a very crude representation of biodiversity (Andersen and Beyer, 2006; Maury and Poggiale, 2013).

Revised

We consider three independent populations of fish at every grid point, and so resolve three biomass spectra. These populations, which we refer to as groups, are defined by their asymptotic sizes as small, medium, and large fish, which allows for a very crude representation of biodiversity (Andersen and Beyer, 2006; Maury and Poggiale, 2013). There is no growth from one group to another; in other words, the small group consists of fish that remain small throughout their life history, such as anchovies and sardines, and so are distinct from the juveniles of the medium and large groups.

-Page 10152, first paragraph: I have trouble seeing where this paragraph is going. Is it providing support for making biomass a function of net primary production? Please clarify.

The goal of this paragraph is to place BOATS in the context of existing global fisheries modeling studies, and to provide a brief literature review of related work that employs the MVF model. We have revised the first to sentence of the paragraph to clarify this.

<u>Original</u>

BOATS continues on from the earlier work of Ryther (1969), who estimated global fish production and harvest based on NPP and simple trophic scaling relationships.

Revised

BOATS continues in a tradition of studies that model the global fishery by applying ecological principles to spatiallyresolved environmental properties. This line of research can be traced to the work of Ryther (1969), who estimated the potential global fish production and harvest based on NPP and simple trophic scaling relationships.

-Section 2.1: Why is the time increment per second? This seems quite fast.

We use seconds as our time unit since it is the standard unit used in climate models (although it does lead to some unwieldy numbers - with no effect on the results).

-Page 10154, lines 11 - 13: What specifically prevents a buildup of biomass at the largest sizes in each spectrum? Also, would fishing mortality come into this mortality term, or would it be an additional term in eq. (1)? You don't need to go into detail about how fishing mortality is included, but it would be helpful just to note where it enters.

First part of question:

As mass approaches the asymptotic size, fish growth declines to zero, while mortality does not. This, together with the assumption that the allocation of input energy to growth, as opposed to reproduction, is strictly decreasing with increasing mass (equations 17 and 23), will prevent a buildup of biomass at the largest sizes in each group.

Second part of question, concerning harvest mortality:

The mortality due to harvest would be represented by another loss term in equation 1. However, since harvest is often assumed to be proportional to biomass, as in the BOATS framework, one could interpret the mortality Lambda_k(m) as being the sum of 2 terms, one for natural mortality and another for harvest mortality.

We have added a sentence to line 13 to describe how harvest mortality would be introduced into equation 1:

New sentence

Although we do not consider harvest mortality in this paper, in the full BOATS model (described by Carozza et al., (2016), in review) it is represented by another loss term on the right hand side of equation (1).

-Section 2.5: I'm unclear whether phytoplankton size structure influences fish size structure. How would a shift towards smaller or larger phytoplankton impact the fish spectra?

We represent phytoplankton size structure through a single representative phytoplankton mass (equation 25). This is set by the large fraction of phytoplankton production, which we calculate using the empirical relationship of Dunne et al. (2005). The only way to change the phytoplankton structure is therefore through a change in temperature or net primary production. The impacts of such changes are described in figure 5B for the intercept and in figure 5C for the slope.

The approach just described would also integrate the other impacts that a change in NPP or T would have on the system (such as through the allometric growth rate or mortality rate). An alternative approach to address this question would be to only change the representative mass, ignoring the other impacts of T and NPP.

A shift to smaller (larger) phytoplankton would result in a downward (upward) shift of the fish production spectrum, but would not affect the mass dependence of the fish production spectrum. We can explain this again using equation (25). First we can rewrite equation (25) as

 $pi(m,t) = Pi_psi(t) * m_psi(t)^{-tau} * m^{-tau - 1},$

where $m_{psi}(t)$ is the representative mass of phytoplankton. tau is equal to log10(trophic efficiency)/log10(predator to prey mass ratio), and so is negative because the trophic efficiency is < 1 and the predator to prey mass ratio is > 1. -tau is therefore positive, and so we have m_{psi} to the power of a positive exponent. Therefore, a shift to smaller (larger) phytoplankton would result in a shift downward (upward) of the entire fish production spectrum; that is, a reduction (increase) in the total fish production, without changes in its partitioning to different fish sizes.

This will influence the growth rate, since the shift in the fish production distribution will alter where the von Bertalanffy limit determines growth (equation 11). Moreover, the fish size structure also depends on the mortality. It would require further simulation to fully understand the details of a change in only the representative phytoplankton size. That said, as a very simple example of such a simulation, we have run the model to equilibrium with the same NPP and T values but have increased the large phytoplankton mass (parameter m_L in equation 15) by a factor of 10. The left panel consists of time series of biomass by group and equilibrium spectra for larger m_L, whereas the right panel is for a smaller m_L). At a qualitative level, there is a negligible change in the structure of the biomass spectra, but a clear positive shift in the intercepts.



-Section 2.6, final two paragraphs: I have a hard time with the lack of predation- dependent mortality, especially in a model that aims to investigate fisheries. It doesn't sound like the model is able to capture top-down impacts. For example, if there's a heavy removal of larger sizes (say, though fishing) would smaller sizes increase in

abundance as a result of reduced predation? Maybe this is captured through the mechanism discussed on page 10158, lines 1 - 4? Also, the final sentence of this section seems to contradict the rest of the paragraph. Please clarify the example you're giving with a bit more detail.

The model does not capture top-down impacts. This is explicitly stated in the last paragraph on page 10165 of the manuscript. Top-down impacts are complex processes that are poorly constrained by data and difficult to implement in a manner that is both realistic and sufficiently general to be applied at the global scale. In the simplifying spirit of the model, we decided not to include them the current version, although we certainly hope to explore them in future. In the scenario proposed by the Reviewer, if there is a strong removal of large sizes in a given group, there is no impact on the mortality of any other fish.

The mechanism discussed in Lines 1-4 on page 10158 would not capture top-down impacts. Those lines indicate that the energy input from primary production to an individual fish would increase under harvest (or another form of removal), and so that the growth rate from primary production would be higher. We have revised these sentences to clarify this.

Original Lines 1-4 on page 10158

Since we assume that the NPP that is transferred up through the trophic web is uniformly input to all individuals in a given mass class, if the biomass in a mass class falls (due to harvesting for example) then the number of individuals has fallen. This implies that more fish production is input to each individual, and so ξ_{Pk} increases.

Revised

Since we assume that the NPP that is transferred up through the trophic web is uniformly input to all individuals in a given mass class, if the biomass in a mass class falls due to a removal (such as harvesting, for example) then this is equivalent to a decrease in the number of individuals in that mass class. This implies that more fish production would input to each individual, and so in such a scenario ξ_{Pk} would increase.

To further clarify this point, we have added to the final sentence of section 2.3.

Original

When biomass is low enough that this equation holds, NPP no longer influences the input energy, and fish will grow at their maximum physiological rate.

Revised

When biomass is low enough that this equation holds, NPP no longer influences the input energy, fish will grow at their maximum physiological rate, and any unused energy available to fish production is assumed to be transferred to unresolved parts of the ecosystem.

Concerning the final sentence of section 2.6, we have revised the final paragraph as follows:

Original

At the same time, since the abundance of predators does not feature in the prey mortality rate, we cannot resolve topdown trophic cascades (Andersen and Pedersen, 2010; Hessen and Kaartvedt, 2014). Since, at present, the scarcity of data prevents a formal verification of theorized trophic cascades in the open ocean, we feel this is a necessary simplifying assumption that we will further explore in the future. Through the growth formulation described in Eq. (1), however, changes in biomass due to harvesting, for example, are carried up through the trophic web.

Revised

Since the prey mortality rate does not depend on the predator biomass, we do not resolve top-down trophic cascades (Andersen and Pedersen, 2010; Hessen and Kaartvedt, 2014). At present, a scarcity of data hinders a formal verification of generalized trophic cascades in the open ocean, which would be desirable for the formulation of their impact within the BOATS framework. However, we do represent bottom-up <u>effects</u> through the growth formulation described in Eq. (1), since a change in biomass in one size class is carried upward through the trophic web as fish grow to larger mass classes.

-Page 10169, lines 2 - 29 and page 10170, lines 1 - 4: Consider condensing these paragraphs considerably. I don't think it's necessary to delve this far into the details of satellite estimates of NPP in this paper. After all, as you state, you could force the model with some other source. It seems sufficient to treat discussion of your NPP input as you do your discussion of temperature input.

We have made substantial changes to section 2.8. As suggested, we have removed many of the details of how NPP is estimated from satellite observations.

Revised section 2.8

The ecological model requires temperature and NPP information <u>as forcing input</u> to calculate the time evolution of biomass (Eq. 1). These <u>variables</u> can be provided by an ocean general circulation model <u>that includes</u> a lower trophic level model. Here, <u>we instead use</u> observational estimates, which would be expected to provide a more realistic simulation.

For temperature, we use the World Ocean Atlas 2005 (Locarnini et al., 2006), which brings together multiple sources of in

situ quality-controlled temperature interpolated to monthly climatologies on a $1^{\circ} \times 1^{\circ}$ grid. We discuss our usage of temperature in Sect. 2.2, and as discussed above, use the average water temperature from the upper 75 m of the water column to force temperature-dependent rates.

For NPP, we take the average of three satellite-based estimates (Behrenfeld and Falkowski, 1997; Carr et al., 2006; Marra et al., 2007) to capture some of the variability that exists in different NPP models (Saba et al., 2011). We note that satellite-based estimates suffer from a range of shortcomings, including lack of productivity sources other than phytoplankton (e.g. seagrass and corals), and biases in coastal regions and estuaries (Saba et al., 2011; Smyth, 2005). Although overall minor, these uncertainties will carry through to the modeled biomass and harvest.

-Page 10173, line 11: Your definition of the intercept here is different from that on page 10172, line 1. Is this intentional? If so, why use two different definitions?

We did not intend to use two different definitions. Since the lower boundary of the resolved biomass spectra are 10 g, this is the mass at which the intercept is defined, and that which we use for the simulations and figures. However, for the idealized continuous spectrum described in equation (30), our objective is to point out what sets the part of the curve that is not dependent on the mass of the organism, and since the actual value of the intercept assumed does not affect this, we propose the following change.

Original lines 1-3 of page 10172

On the other hand, the intercept of the spectrum (in logarithmic space, when m = 1) depends on a variety of parameters such as the NPP and trophic efficiency, as well as the natural mortality rate and the representative phytoplankton mass.

Revised lines 1-3 of page 10172

On the other hand, the intercept of the spectrum (in logarithmic space, when $m = m_0 = 10$ g in our case) depends on a variety of parameters such as the NPP and trophic efficiency, as well as the natural mortality rate and the representative phytoplankton mass.

-Page 10174, lines 1 – 3: The sentence beginning, "Overall. . ." is a nice summary of the influences of NPP and temperature on the biomass spectra.

Thank you.

Technical Corrections

-Throughout the paper equations are mentioned out of order. I can see why this is done in some cases, but if it's possible to address it would aid the reader. It's not critical, though.

Throughout the manuscript, we preferred to introduce the equations in logical rather than chronological order to facilitate the description and explanation of the different model components. Where appropriate, we added section numbers to the equation numbers when referring to equations that have not been introduced yet in the text.

-Page 10146, line 19: I think this should read, "determine how they change...", not "determine how the change".

We have made the change as suggested.

-Page 10149, final sentence: Fragment, but would be fixed by removing the word "which".

We removed the word "which".

-Page 10154, line 4: The closing parenthesis is missing before the period.

We corrected the error.

-Page 10154, line 13 and page 10164, line 22: Consider replacing "old age" with "senescence".

We have made the changes as suggested.

-Page 10155, lines 17 – 18: Consider omitting "more than" for tone.

We have made the changes as suggested.

-Page 10162, lines 7 – 9: I don't think Blanchard et al. (2009) model the dynamics of the phytoplankton spectrum, but rather assume constant conditions.

We have removed this reference to Blanchard et al. (2009).

-Page 10163, lines 24 – 25: Please state how carbon is converted to wet weight, either here in the text or in Table 1.

mmolC_2_wetB = (12*gC_2_wetB)/1000; % [wetB / mmolC]

Original lines 22-25 of page 10163

Since the model is forced with NPP data, we run the model in units of mmolC, and then convert biomass and harvest to grams of wet biomass (gwB) for analysis and presentation by assuming a constant conversion rate.

Revised

The model is forced with observations of NPP, and so we run the model in units of mmolC. For analysis and presentation, we convert to grams of wet biomass (gwB) by assuming that there are 12 gC per molC, and that there are 10 gwB for every g of dry carbon (Jennings et al., 2008).

-Page 10168, final sentence: Consider replacing "ocean general circulation model including a lower trophic level model" with "earth system model".

See response above to changes in section 2.8.

-Page 10174, line 17: Insert "such as" before "for use in. . .".

We have made the change as suggested.

-Page 19175, line 2: Convert "10 cm" to mass to be consistent with the body of the paper. This could be a parenthetical after the length if it's desirable to have both measures.

We have made the change as suggested.

Moreover, we have added the asymptotic masses used to section 2.10, and have made sure the units are consistent with the values used in table 1.

-Figure 5c: Are groups 1, 2, and 3 the same as small, medium, large in the other figures? If so, please change the legend for consistency.

We have made the change as suggested, and refer to the groups as small, medium, and large throughout.

-This is a somewhat picky suggestion, but blue-green-red color scheme could be hard for color-blind folks to distinguish. An easy solution would be solid, dashed, and dotted lines, differently shaded lines, or some combination thereof.

We have made the change as suggested for all of the relevant figures (2, 4, and 5c). Total curves are in grey, whereas group curves are in black as suggested, with solid, dashed, and dot-dash curves for the small, medium, and large groups, respectively.

Anonymous Referee #2

I want to point out just a few places where I think the simplifying assumptions may break down somewhat; not necessarily for the authors to change their approach, but to indicate that these are important assumptions that should be further explored at some point.

Firstly, the input of all NPP as a potentially exploitable resource for commercial fish species seems excessive. A substantial fraction is taken up by the many other non-commercial organisms inhabiting the oceans, for example, by export flux that goes to mesopelagics, by marine mammals, by the millions of non-commercially fished marine species. Although this is moderated somewhat when growth is constrained by allometry instead of productivity, it would make sense to have some fraction of NPP go to other groups and not be available to modelled organisms. This fraction could be a parameter, and may improve fit to data.

We assume that all NPP is transferred to commercial fish. Although difficult to constrain, we considered alternate fractions of NPP available to commercial fish (25, 50, and 75%, not shown or described in the manuscript). In those simulations, we found that globally integrated unharvested biomass, harvested biomass, and peak harvest were linear with the fraction of NPP available. From this we took that including the NPP fraction available as a parameter in the Monte Carlo analysis would not allow us to exploit another mode of variability, and so opted to not include it as a parameter.

Nevertheless, we recognize that as new approaches to estimating this parameter become available, it will be constructive to include it in future sensitivity analyses. We have revised the second paragraph on page 10157 to address these concerns.

Revised paragraph 2 p.10157

We assume that all NPP is transferred to the three commercial fish groups, and further assume that each group has access to one third of the total production. Group fish production is written as the fraction allocated to group k, $\phi_{\Pi,k'}$ multiplied by the fish production $\Pi(m,t)$. Although these are strong assumptions, we feel that they are necessary and commensurate with the simple three-group representation of the ecosystem and the scarcity of appropriate data constraints. We have examined alternative fractions of NPP transferred to the commercial groups (not shown) and find that the unharvested and harvested biomass are approximately linear with the fraction $\phi_{\Pi,k'}$. For this reason, we did not include it as a parameter when constraining the model (see Sect. 3, table 1, and Carozza et al., 2016).

<u>Groups are independent of one another, except in that they all receive a part of NPP.</u> Ecologically, this implies equal resource partitioning of NPP to each group, both when they are at the larval stage (through recruitment) and as juveniles and adults (through growth) (Chesson, 2000). This can be thought of as each group occupying an ecological niche that remains stable over time, and implies that excess NPP, which would result from growth-rate limitation of biomass advection, is not available to other potentially commercial groups, but rather supplied to non-commercial species. Non-commercial species could include, among others, unharvested mesopelagic fish, planktonic invertebrates such as cnidarians and fish, and benthic invertebrates such as amphipods and nematodes. By assuming that a fixed portion of NPP goes to each commercial group, all groups are assured to coexist stably.

As it stands, the model is likely biased in that for low productivity systems, most of the NPP will be taken up by commercial species (since NPP will be a strong constraint), whereas in high productivity systems, a much larger fraction will go to other groups (since NPP constraints will be relaxed and allometry play a stronger role). The authors might want to consider any effects this will have on their results.

We note this bias on line 15 of p 10159. However, since this could also cause a bias in harvest, we will note its effect on the results in the companion paper, since such a mechanism could help to explain a bias in harvest.

New sentence at line 15 of p10159

For low productivity systems, the model could overestimate biomass since a larger fraction of primary production will be transferred to commercial species. However, in high productivity systems, the allometric limit is more likely to set growth rates and so a larger fraction will be transferred to the non-commercial groups. That said, the potential for, and the magnitude of, such a feature will depend on the particular values of the growth rates at the site in question (equation 11).

Additionally, does the fact that this model can be (is) applied to the open ocean, where depths may be great, mean that there is also an issue in deeper regions, because the export productivity going to demersal and benthic organisms will be much lower (i.e. decrease exponentially), and so the 1/3 sharing for each group also be biased?

As above, and now noted in the manuscript, the 1/3 sharing for each group is a strong assumption. Our groups are defined based on asymptotic size, and so given that at a deeper site less primary production will be delivered to benthic species, and that benthics are predominantly small and medium, then we could be overestimating benthic biomass in the open ocean.

We recognize that other variables, such as depth or the front probability index (Woodson and Litvin, PNAS, 2015, 112(6), 1710–1715), could provide for informative and alternative ways to represent important first-order processes. Although we have not included depth in this version of the model, we plan to consider it, as well as other variables, in future model development.

Secondly, having natural mortality be independent of predator biomass seems restrictive in terms of situations where it will be an appropriate assumption. For example, if all top predators are fished out, then (if I understand correctly), the mortality rate will not change, even though there are no uber-predators. Although the authors acknowledge this, their justifications ('without necessarily losing realism', and - to paraphrase - suggesting that 'lack of data is sufficient to assume that trophic cascades in the ocean do not happen and thus this simplification is OK') seems like a stretch. I would recommend not suggesting that this is 'realistic' (which it is not), but a necessary simplification which may lead to problems with certain biomass spectra. It might also be something worth exploring in the future.

Anonymous Referee #1 made a similar comment above and we have addressed both sets of concerns in the modifications described for the comment above.

Thirdly, no dispersal. On P10150 I15-17 'we effectively ignore nonlocal movements over spatial scales > 100x100km'. Whether this is an issue presumably depends upon the time-step of the model relative to the spatial scale. Here it is 15 days (1/2 month). For a fast region of the ocean (e.g. gulf stream, assume 6km/h, 144km/day, potentially 2160km/15 days), or even a moderate one, it does appear as if advection could move species through many grid cells and thus play a role. This should be included as a caveat, rather than saying 'we expect it to have a negligible impact on our results'. Also note that grid cells are much smaller at high latitudes on a 1 degree grid.

We have changed the paragraph.

Original lines 12-23 p10150

These are complex processes whose role in determining fish biomass are difficult to quantitatively evaluate at the global scale given present knowledge (Watson et al., 2014). For the moment, in BOATS we assume that fish are present where

there is NPP to provide food. Given that the model grid points are $1^{\circ} \times 1^{\circ}$, we only effectively ignore nonlocal movements that occur over spatial scales that are larger than approximately 100 km × 100 km. However, movement induced by ocean circulation and fish behavior could be easily implemented in the future, with existing advection and diffusion algorithms (Faugeras and Maury, 2005; Watson et al., 2014). Although the location at which NPP, zooplankton (secondary) production, and fish production take place are different due to the movement of plankton by currents, we expect this to have a negligible impact on our results given our relatively coarse (approximately 100 km) spatial resolution.

Revised

These are complex processes that have been shown to play a role in determining fish biomass distributions (Watson et al., 2014). In BOATS we assume that fish are present where there is NPP to provide food. Given that the model grid cells are $1^{\circ} \times 1^{\circ}$, we only effectively ignore nonlocal movements that occur over spatial scales that are larger than

approximately 100 km × 100 km. This could bias our results in parts of the ocean where the advection of fish biomass is strong, such as in the Gulf Stream, relative to the time step and spatial grid scale. This is especially true for larvae, but would likely pose less of a problem for larger fish since they swim faster than even strong oceanic currents. Due to the movement of plankton by currents, a bias could also result from the difference in the locations at which plankton and fish production occur. We expect this to have a <u>small</u> impact on our results given our relatively coarse spatial resolution. Movement induced by ocean circulation and fish behavior could be implemented in the future, with existing advection and diffusion algorithms (Faugeras and Maury, 2005; Watson et al., 2014).

I also think the Watson et al. paper is mis-cited here; rather than saying 'These are complex processes whose role in determining fish biomass are difficult to quantitatively evaluate at the global scale given present knowledge', the last line of the Watson abstract is 'These results highlight the importance of considering movement in global-scale ecological models!'

We addressed this concern in the response to the previous question.

Other comments:

Conversion between abundance and biomass: I don't buy that the conversion between abundance and biomass (e.g. 10153 I14-16) would not influence model dynamics. In an ideal setting (i.e. a continuous spectrum), then I think this would be the case. But here, where there are 50 mass bins, this discretization will prevent conservation of mass and abundance. If the model was run with a fixed total amount of NPP input, and all pools of biomass resulting from this measured (including respired, detritus etc), I do not think this total would remain constant, as it would in a continuous setting. This is because of fishes 'jumping' between the mid-points of size bins, i.e. the growth rate may only be enough to just about take them into the next size bin, but they are automatically inserted at its geometric mean, representing an instantaneous accumulation of biomass not resulting from NPP. This is simply a computational artefact, but it will clearly affect both biomass and, therefore, abundance. So while true in the limit, I don't think that this model will actually give the same results when run as abundance or biomass.

We have revised lines 14-16 on p. 10153:

Original

Regardless, since the abundance *n* and biomass *f* spectra are related by f(m, t) = n(m, t)m, using one form over the other does not influence the model dynamics.

<u>Revised</u>

Regardless, since the abundance *n* and biomass *f* spectra are related by f(m,t) = n(m,t)m, in the continuous case, using one form over the other does not influence the model dynamics. We note that, in the numerical implementation of the model, there will be a small difference between the two since we use the geometric mean to represent a discretized range of masses (section 2.10). Hence, as fish grow they jump from one geometric mean to next, which may result in an accumulation of biomass.

I find the notation a little cumbersome; why not drop the mass and time dependencies (where possible) as per Appendix A? It would make it easier to read.

We have removed the mass and time dependencies in numbered equations, when the general variables are used (i.e., not a particular value of mass or time). However, in the text, we keep the mass or time dependence since that is where we describe the equations and find it useful to the reader. We will also keep the dependencies in table 2.

I was wondering where the details of parameter estimation were to be found; there is only a brief reference on p10171. This makes it hard to judge how effective the model fitting process is. Could a line or two be added to give more details (e.g. is this a Bayesian approach? If so, are flat priors being used? How many MC runs are used?

We have reorganized the two paragraphs that introduce section 3.

Revised

Here we describe the behaviour of the fish ecology model, and make use of a simplified version of the model as a reference point and initial biomass condition. We consider two model grid points that correspond to individual patches of ocean at a cold-water site in the East Bering Sea (EBS) LME ($64\circ N$, $165\circ W$) and a warm-water site in the Benguela Current (BC) LME site ($20\circ S$, $12\circ E$), and describe the resulting biomass spectra and other model variables. We discuss the results from a sensitivity test that considers the role of NPP (ranging from 50 to 2000 mg C m–2 d–1) and temperature (ranging from –2 to $30\circ C$) on biomass. For these simulations, we use a 15-day timestep and constant forcing of annually-averaged NPP and temperature.

We do not use these sites for a thorough data-based model validation, which is difficult at this time due to a lack of suitable fish biomass data. The parameter values used here are taken from an extensive data-model comparison that employs the global implementation of the model, and is fully described in the companion paper (Carozza et al., 2015). In that study, we take a Monte Carlo approach with over 10,000 parameter sets to find parameter combinations that best fit observed harvest at the LME-scale, considering the full range of the uncertain parameter space for the 13 most important parameters. Of these 13 parameters, 2 are economic, with the remaining 11 ecological parameters being identified with a dagger symbol in table 1. Beyond the validation to harvest at the LME-scale in the companion paper (Carozza et al., 2015), more specific validation could be done in the future with suitable datasets when they become available (that is, size aggregated, regional-scale, species-comprehensive biomass assessments).

I would really like to see how precisely biomass spectra fit to data (slopes of -1.0 to -1.2 on p10173). There is nothing in the figure, and in the text it just says that 'they are consistent with published values', though maybe not at lower temperatures.. It would be good to get the mean values (and the confidence around that, from the MC simulations) into both the text and the figure, for comparisons sake.

We feel that such an analysis is difficult to justify given the current limitations in observations of size spectra, and so would be beyond the scope of the current work. We are currently completing another manuscript, which employs global harvest data to further examine the uncertainty in the Monte Carlo simulations that we developed (in the companion paper).

The numerical methods (Appendix C, particularly C1) are really important and should be moved to the main text (Section 3), or at least the key points, so that all details of the model (timestep, grid cell size, numerical approach used, mass bin structure) are in one place. Details of the model mass bin approach (number of bins, bin boundaries) are not numerical methods, they are model structure details like the timestep or cell size.

We have moved Appendix C: Numerical Methods to become a new section 2.10, and have moved Appendix C1: Group and Mass Class Structure to become a new section 2.9.

We have made a few adjustments throughout the text to reflect that these are now sections and not appendices, and made minor changes to the first paragraph of 2.10.

Minor editorial comments

P10148 I5-6: '... not always coupled directly with predictive models of fishing activity'. It would be good to see a reference or two for this.

We have revised this sentence and added references:

Original lines 5-6 P10148:

In addition, spatially-resolved models of fish production are not always coupled directly with predictive models of fishing activity.

Revised

In recent years, generalized, spatially-resolved models of the marine ecosystem applicable to the global domain have been developed, but most are not directly coupled with predictive models of fishing activity (Jennings et al., 2008; Lefort et al., 2014, Watson et al., 2014).

P10148 I10-11 'aims to represent the global community of marine organisms'. This is incorrect; all noncommercial species (millions!), marine mammals etc etc are left out. Please rephrase to more carefully delineate the boundaries.

We have revised the sentence on lines 9-13 of P10148.

Original

The ecological module of the BiOeconomic mArine Trophic Size-spectrum model (BOATS) aims to represent the global community of marine organisms as a suite of "super-organism" populations that grow, reproduce, and die, taking into account their dependence on local environmental variables in the framework of a two-dimensional grid of the global ocean.

Revised

The ecological module of the BiOeconomic mArine Trophic Size-spectrum model (BOATS) aims to represent commercial organisms as a <u>set of super-organism populations (that we refer to as groups)</u> that grow, reproduce, and die, taking into account their dependence on local environmental variables in the framework of a two-dimensional grid of the global ocean.

P10148 I11 'a suite of super-organism populations' – not quite sure what is being referred to here. Is it the three size classes?

See revision to previous question.

P10148 I18-19: 'which requires arbitrarily defining under-constrained feeding relationships' seems a little strong, given that the present model is arbitrarily defining many things (e.g. size bins). As mentioned previously, I don't think the authors need be so defensive.

We have removed this clause.

Revised lines 18-19 P10148.

Instead of attempting to model such species-level characteristics, we rely on the simple principle that the overall growth of organisms within a community depends on the availability of energy from net primary production, relative to the total consumption of energy by the metabolic activity of the community.

P10151 I12-14: But there is a strong difference in how they will experience the total primary productivity input, particularly in deeper cells.

We addressed this concern in the question above concerning depth.

P10156 Eqn 5: The notation here is confusing – why not use the same symbol for formation of biomass (whether reproductive or somatic), instead of the same symbol for energetic input and somatic biomass?

We now use the symbol γ to represent formation of somatic (γ_S) and reproductive (γ_R) biomass.

Original equation 5

$$\xi_{I,k}(m,t) = \gamma_k(m,t) + \xi_{R,k}(m,t),$$

Revised equation 5

 $\xi_{I,k}(m,t) = \gamma_{S,k}(m,t) + \gamma_{R,k}(m,t),$

P10157 I8: Is there any evidence for equal partitioning of NPP among size classes? If not, this should be stated as a (fairly strong) assumption.

The revisions that we made to paragraph 2 on page 10157 that we presented above address this question.

P10170 I15-20: It would be useful to know bottom-depth at these sites.

We addressed this concern in the question above concerning depth.

P10174 I21: 'often unconstrainable ecological processes' – again this seems overly harsh, and not necessarily accurate.

We have changed this sentence.

Original line 21

We apply empirical relationships to simplify complex and often unconstrainable ecological processes when possible.

Revised

When possible, we apply empirical relationships to simplify complex ecological processes that are difficult to constrain.

P10175 I8: 'Reasonably realistic' would be more appropriate.

We have made the change as suggested, and have made this change to the abstract as well.

Table 2: By variables, do you mean fitted parameters? I'm just trying to get a sense of how many parameters are actually estimated in the model – it would be good to have this value in the text somewhere as well, because right now it is just stated that there are fewer parameters than comparable models, without saying how many there actually are.

Variables refers to quantities that change in mass or time.

13 parameters are estimated in the Monte Carlo procedure described in the companion paper. 11 of these parameters are ecological, and 2 are economic. We have added this information to the introduction to section 3 (see response above). Moreover, in the section 3 introduction (changes described above), as well as in the caption to table 1, we note that the dagger symbol represents a fitted parameter, which was omitted in the manuscript.

I found Fig 1 a little unintuitive – is there a clearer way of presenting this?

We have added to the figure caption.

<u>Original</u>

Figure 1. Schematic diagram of the main modules, components, and processes of the eco- logical module of BOATS. Solid arrows represent fluxes of biomass, whereas dashed arrows represent dependencies. Arched lines identify model components or extend a process over mass classes or groups.

Revised

Figure 1. Schematic diagram of the main modules, components, and processes of the ecological module of BOATS. Net primary production (NPP) and temperature (T) force the model and are used to calculate the fish production spectrum, by assuming a transfer of energy from phytoplankton to successive sizes of fish that depends on the trophic efficiency and the predator to prey mass ratio. From fish production, we calculate the size-dependent growth rate of biomass in three independent groups that represent small, medium, and large commercial fish. Mortality rates are calculated as a function of size and asymptotic size, and also depend on temperature. Adult fish, the largest sizes in each spectrum, allocate energy to reproduction, of which a fraction is returned to the smallest mass class of the corresponding spectrum, representing recruitment of juveniles.

Fig 5. 'Note that the spectral slope does not depend on NPP' please clarify for those just looking at the figures; also needs a clearer title for panel C.

We have changed the sentence mentioned to:

In (c), since the slopes of the biomass spectra do not depend on NPP, the slopes are lines that depend only on temperature.

We have changed the Panel (b) title to: Intercept of total biomass spectra

We have changed the Panel (c) title to: Slope of nonreproducing biomass spectra

Other corrections

We have added a sentence to line 13 of page 10148 to better place the BOATS model relative to other global models:

New sentence

The approach is structurally-simpler than that of Christensen et al. (2015), and bears similarity with that of Jennings and Collingwood (2015), but unlike these models the BOATS ecological model explicitly treats life history and reproduction, similar to Maury et al. (2007).

*Please note that we have made further minor clarifications to improve readability as well as a few corrections. The difference file in pdf format shows these changes.

Topical Editor Report

Topical Editor Decision: Publish subject to technical corrections (01 Apr 2016) by Andrew Yool

Comments to the Author:

Thank you for your responses to the referees and your revised manuscript. I have now reviewed these and am pleased to report that I am satisfied that you have addressed the referees' concerns.

That said, one of the issues raised by Referee 2, namely their concern about all of the NPP going to the modelled commercial species, could be dealt with more convincingly. While the fraction reaching the modelled groups is perhaps not well-known, it is at least known that it's not the 100% assumed here. As the referee remarks, the plethora of non-commercial species, as well as export to the deep ocean, represent a sink for NPP that BOATS overlooks. My interpretation of your response to this point is that since your main results scale linearly with the fraction assumed, you exclude this parameter from your analysis in order to simplify it. This is sort of fine as far as it goes (i.e. a sensible short-cut for model world), but as the referee notes, does it not perhaps overlook commercial fish biomass as a data constraint? That is, if you choose different values, you will have more / less biomass and will conform to reality more / less. Perhaps, however, there is insufficient data to do so (you do also note "the scarcity of appropriate data constraints").

In passing, the concluding sentence in this section ("By assuming that ...") is something of a non-sequitur to the preceding sentence.

Anyway, assuming that my interpretation above is accurate, I think it would be helpful for the text to more clearly note that this assumption is made purely to facilitate analysis rather than being what you actually think the fraction is. And on the data constraint point, perhaps noting the uncertainty range of biomasses might convince readers not to get overly concerned about this assumption.

If this final point can be cleared up, I see no problem in accepting this manuscript. Thanks again for your efforts, and for dealing so completely and clearly with the referee concerns.

Response

We have made numerous changes to the two paragraphs in question.

Original Paragraphs

We assume that all NPP is transferred to the three commercial fish groups, and further 315 assume that each group has access to one third of the total production. Group fish pro- duction is written as the fraction allocated to group k, $\phi_{\Pi,k}$, multiplied by the fish production $\Pi(m,t)$. Although these are strong assumptions, we feel that they are necessary and commensurate with the simple three-group representation of the ecosystem and the scarcity of appropriate data constraints. We have examined alternative fractions of NPP transferred to the commercial groups (not shown) and find that the unharvested and harvested biomass are approximately linear with the fraction $\phi_{\Pi,k}$. For this reason, we did not include it as a parameter when constraining the model (see Sect. 3, Table 1, and Carozza et al. (2016)).

Groups are independent of one another, except in that they all receive a part of NPP. Ecologically, this implies equal resource partitioning of NPP to each group, both when they 325 are at the larval stage (through recruitment) and as juveniles and adults (through growth) (Chesson, 2000). This can be thought of as each group occupying an ecological niche that remains stable over time, and implies that excess NPP, which would result from growth-rate limitation, is not

available to other potentially commercial groups, but rather supplied to non- commercial species. Non-commercial species could include, among others, unharvested 330 mesopelagic fish, planktonic invertebrates such as cnidarians, and benthic invertebrates such as amphipods and nematodes. By assuming that a fixed portion of NPP goes to each commercial group, all groups are assured to coexist stably.

Revised Paragraphs

We define $\phi_{\Pi \Psi,C}$ as the fraction of NPP that is potentially available to the sum of all com- 20 mercial fish groups. In the present work, we assume that $\phi_{\Pi \Psi,C}$ is equal to 1, and therefore omit it from the equations. This simplifying assumption implies that the entire global ecosystem of animals larger than 10 g would have consisted of potentially commercial species prior to fish harvesting (including bycatch). Obviously this is incorrect, in that the existence of non-commercial animals larger than 10 g requires that $\phi_{\Pi \Psi,C} < 1$ in the real world. How- 25 ever, given the weak observational constraints on biomasses of non-commercial animal species at the large scale, and the fact that the species composition of all marine ecosys- tems has been heavily altered by human activity, it is very difficult to estimate the true value of $\phi_{\Pi \Psi,C}$. Despite this difficulty, sensitivity tests revealed that biomass and harvest in the model are approximately linear with $\phi_{\Pi \Psi,C}$ (not shown). Since we constrain the parameters in BOATS by comparing linear correlations of modelled and observed harvest (see Sect. 3, Table 1, and Carozza et al. (2016)), and given the linearity of modelled harvest vs. $\phi_{\Pi \Psi,C}$, the value of $\phi_{\Pi \Psi,C}$ would have a negligible effect on the spatial correlation criterion used for the optimized parameter choices. Nevertheless, it should be pointed out that using alternate values of $\phi_{\Pi \Psi,C}$ would change the predicted biomass and harvest, all else being equal.

We further assume that each of the three fish groups has access to an equal fraction of the available primary production, $\phi_{\Pi \Psi,C}/3$. By assuming that constant portions of the avail- able photosynthetic energy are available to each of the commercial fish groups, all groups are assured to coexist stably. Ecologically, our assumption implies equal resource parti- tioning to each group, both when they are at the larval stage (through recruitment) and as juveniles and adults (through growth) (Chesson, 2000). This can be thought of as reflecting a separate ecological niche for each group that remains stable over time, and implies that excess NPP, which would result from growth-rate limitation of one group, is not available to other potentially commercial groups, but rather supplied to non-commercial species. Non- commercial species could include, among others, unharvested mesopelagic fish, planktonic invertebrates such as cnidarians, and benthic

invertebrates such as amphipods and nematodes. Although this and the previous assumption are not strictly accurate representations of the marine ecosystem, we feel that they are commensurate with the simple three-group representation of the ecosystem and the scarcity of appropriate data constraints, and could be improved in future work.

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The ecological module of BOATS-1.0: a bioenergetically-constrained model of marine upper trophic levels suitable for studies of fisheries and ocean biogeochemistry

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Abstract

Environmental change and the exploitation of marine resources have had profound impacts on marine communities, with potential implications for ocean biogeochemistry and food security. In order to study such global-scale problems, it is helpful to have computationally

- ⁵ efficient numerical models that predict the first-order features of fish biomass production as a function of the environment, based on empirical and mechanistic understandings of marine ecosystems. Here we describe the ecological module of the BiOeconomic mArine Trophic Size-spectrum (BOATS) model, which takes an Earth-system approach to modeling fish biomass at the global scale. The ecological model is designed to be used on an Earth
- System model grid, and determines size spectra of fish biomass by explicitly resolving life history as a function of local temperature and net primary production. Biomass production is limited by the availability of photosynthetic energy to upper trophic levels, following empirical trophic efficiency scalings, and by well-established empirical temperature-dependent growth rates. Natural mortality is calculated using an empirical size-based relationship,
- ¹⁵ while reproduction and recruitment depend on both the food availability to larvae from net primary production and the production of eggs by mature adult fish. We describe predicted biomass spectra and compare them to observations, and conduct a sensitivity study to determine how the they change as a function of net primary production and temperature. The model relies on a limited number of parameters compared to similar modeling efforts,
- ²⁰ while retaining <u>reasonably</u> realistic representations of biological and ecological processes, and is computationally efficient, allowing extensive parameter-space analyses even when implemented globally. As such, it enables the exploration of the linkages between ocean biogeochemistry, climate, and upper trophic levels at the global scale, as well as a representation of fish biomass for idealized studies of fisheries.

1 Introduction

Humans have harvested fish and marine resources since prehistoric times, but due to the development of modern fish capture technologies since the end of the Second World War, and to a strong increase in demand arising from increasing population,

- ⁵ global wild harvest increased at an unprecedented rate following 1945. This strong appetite for marine resources has had important impacts on marine ecosystems. A significant fraction of fisheries are overexploited, and estimates of the fraction of collapses range from 7–13 to 25% of all fisheries (Mullon et al., 2005; Branch et al., 2011). Large finfish biomass is thought to be significantly depleted relative to its preharvest
- state (Myers and Worm, 2003), numerous species of finfish and invertebrates have witnessed range reductions (local extinctions) (McCauley et al., 2015), and an index of marine finfish biomass indicates an aggregate loss of 38% over many species (Hutchings et al., 2010). Despite increasing harvesting effort (Watson et al., 2013b), annual wild harvest appears to have peaked globally in the early 1990s at approximately 90
- (Watson et al., 2004; Pauly, 2007; FAO, 2014) at an annual rate that has been recently estimated at 130 million tonnes (Mt) (Watson et al., 2004; Pauly, 2007; FAO, 2014) and not changed substantially since per year (Pauly and Zeller, 2016), since which time it appears to have declined. As older coastal fisheries have become increasingly depleted (Jackson, 2001), harvest has extended to more taxa as well as further from the coast and deeper in the water column (Norse et al., 2012; Watson and Morato, 2013).
- Anthropogenic climate change, on the other hand, has the potential to transform the ocean temperature distribution and thereby alter marine ecosystems by affecting elements of ocean circulation that drive is already altering nutrient dynamics and primary production (Doney et al., 2012)through its effects on ocean temperature
- and circulation (Doney et al., 2012), with demonstrated consequences on the distributions of several fish populations (Pinsky et al., 2013; Walsh et al., 2015). Global climate models suggest that increased surface water stratification due to warming could decrease nutrient upwelling and so reduce net primary production

(Steinacher et al., 2010; Bopp et al., 2013) (Sarmiento et al., 2004; Steinacher et al., 2010; Bopp Warming can also directly influence fish biomass by affecting physiological rates that influence growth, mortality, reproduction, recruitment, and migration (Brander, 2010; Sumaila et al., 2011). Despite progress in identifying important mechanisms of biomass change, important uncertainties remain in constraining the overall impact and the spatial distribution of change in net primary production (Taucher and Oschlies, 2011) and fish biomass, with current analyses pointing toward heterogeneous spatial change in fish production and harvest potential (Cheung et al., 2010; Barange et al., 2014; Lefort et al., 2014).

Research in fisheries and fisheries economics often focusses on particular species, regions, and markets. In addition, recent years, generalized, spatially-resolved models of fish production are not always coupled directly the marine ecosystem applicable to the global domain have been developed, but most are not directly coupled with predictive models of fishing activity (Jennings et al., 2008; Lefort et al., 2014; Watson et al., 2014). Our intention is to follow an alternative approach, by modeling model fisheries and eco-

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- nomic harvesting as parts of a an integrated system that is bioenergetically constrained, 15 and based on fundamental physical, ecological, and economic principles. The ecological module of the BiOeconomic mArine Trophic Size-spectrum model (BOATS) aims to represent the global community of marine commercial organisms as a suite of set of super-organism "populations that populations (that we refer to as groups) that grow,
- reproduce, and die, taking into account their dependence on local environmental vari-20 ables in the framework of a -two-dimensional grid of the global ocean. The approach is structurally simpler than that of Christensen et al. (2015), and bears similarity with that of Jennings and Collingridge (2015), but unlike these models the BOATS ecological model explicitly treats life history and reproduction, similar to Maury et al. (2007).
- The true ecological structure of marine communities is very complex, and includes many 25 species-level ecological dynamics that are not understood at a useful mechanistic predictive level. A typical oceanic food web consists of dozens or more of interacting species, whose sizes span several orders of magnitude and whose lifetimes range from days to decades. Instead of attempting to model such species-level characteristics, which requires arbitrarily

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defining under-constrained feeding relationships, we make the simplifying assumption we rely on the simple principle that the overall growth of organisms within a -community depends on the availability of energy from net primary production, relative to the total consumption of energy by the metabolic activity of the community. Since one of our primary goals is to predict fishery harvest through coupling with an economic model, we define our community as including all commercially-harvested organisms, including pelagic, demersal, and benthic species, both finfish and invertebrates (see discussion of size-based groups in

the next section), referring to all as "fish" for simplicity.

- In this paper, we describe the ecological module of the BOATS model. In a companion paper (Carozza et al., 2016), the ecological module is coupled to an economic harvesting module and extended to a two-dimensional global grid, in order to explore the spatial distribution of harvest results in the model parameter space, and to explore parameter as well as the parameter uncertainty. Here, we present in detail the equilibrium biomass at two ocean sites using a single set of parameter values, and conduct a sensitivity study to illustrate how
- the model biomass and the size structure of marine communities depend on net primary production and temperature.

2 Fish ecology model

5

The ecological module of BOATS uses the McKendrick–von Foerster (MVF) model (McKendrick, 1926; von Foerster, 1959), a widely-used continuous-time model for an ageor size-structured population, to represent the evolution of biomass. Populations of fish biomass (all of the organisms in a group) are organized continuously by size and are described by a continuous biomass distribution that we refer to as a biomass spectrum. Fish begin in the smallest size class and grow over time into adjacent (larger) size classes. In each size class, fish biomass evolves in time as the biomass growth less the natural mortality.

Biomass growth is determined by the net primary production that is transferred to fish from phytoplankton at the base of the food web, and is limited by but cannot exceed the

empirical maximum physiological fish growth rates that depend on the individual fish mass and temperature. As such, the local net primary production supports a maximum possible production rate of fish biomass. If actual production within the resolved fish spectra falls below this, due to a shortfall in the availability of biomass that can grow larger, the surplus

- net primary production is assumed to be taken up outside the resolved fish spectra, by non-commercial species (e.g. non-commercial invertebrates). The natural mortality in each mass class represents biomass losses due to predation, by organisms both within and outside of the community, as well as other natural causes. The mortality formulation depends on an empirical relationship that considers the individual mass of the fish, the asymptotic
- mass of the fish (the maximum theoretical mass), and the temperature. The addition of new biomass into the smallest mass class, referred to as recruitment, which is determined as a function of the net primary production and the production and survival of eggs.

BOATS is designed with the global ocean in mind, yet for ease of reading we present it for a single patch of the ocean, or in other words, for a single grid point on a twodimensional grid. By then applying BOATS to each oceanic grid cell independently, we 15 represent fish biomass and harvest on a two-dimensional global grid. We force biomass using two-dimensional grids of vertically-integrated net primary production (NPP) and vertically-averaged temperature derived from satellite ocean color and direct temperature measurements, respectively (Sect. 2.8). At each grid point, we therefore simulate biomass spectra that are independent of the adjacent grid points. Hence, we do not 20 take active or passive movement of fish, larvae, or eggs between adjacent grid points into account. These are complex processes whose that have been shown to play a role in determining fish biomass are difficult to quantitatively evaluate at the global scale given present knowledge (Watson et al., 2014). For the moment, in BOATSdistributions (Watson et al., 2014). In BOATS, we assume that fish are present where there is NPP 25 to provide food. Given that the model grid points cells are $1^{\circ} \times 1^{\circ}$, we only effectively ignore nonlocal movements that occur over spatial scales that are larger than approximately 100 km × 100 km. However, movement induced by ocean circulation and fish behavior

could be easily implemented in the future, with existing advection and diffusion algorithms

(Faugeras and Maury, 2005; Watson et al., 2014). Although the location at which NPP, zooplankton (secondary) production, and fish production take place are different due This could bias our results in parts of the ocean where the advection of fish biomass is strong relative to the time step and spatial grid scale, such as in the Gulf Stream. This is especially

- true for larvae, but would likely pose less of a problem for larger fish since they swim faster than strong oceanic currents. Due to the movement of plankton by currents, we a bias could also result from the difference in the locations at which plankton and fish production occur. We expect this to have a <u>negligible small</u> impact on our results given our relatively coarse (approximately 100) spatial resolution. Movement induced by ocean circulation and
- ¹⁰ fish behavior could be implemented in the future, with existing advection and diffusion algorithms (Faugeras and Maury, 2005; Watson et al., 2014).

We consider three In the current implementation of the model, we consider three independent populations of fish at every grid point, and so resolve three biomass spectra. These populations, which we refer to as groups, represent are defined by their asymptotic

- sizes as small, medium, and large fish, and allow a which allows for a very crude representation of biodiversity (Andersen and Beyer, 2006; Maury and Poggiale, 2013). There is no growth from one group to another; in other words, the small group consists of fish that remain small throughout their life history, such as anchovies and sardines, and so are distinct from the juveniles of the medium and large groups. The asymptotic mass, the
- mass at which all energy is allocated to reproduction and therefore the mass at which growth stops, characterizes each group. We employ groups since they allow us to make use of well-studied growth and mortality characteristics of fish of different asymptotic size (Andersen and Beyer, 2006; Maury and Poggiale, 2013). We work with a finite number of groups as opposed to a continuum (as in Andersen and Beyer, 2006; Maury and Pog-
- giale, 2013), to directly compare our harvest results to the Sea Around Us Project (SAUP) harvest database (Watson et al., 2004; Pauly, 2007), using the three asymptotic masses (Appendix ??Sect. 2.9) from the functional group definitions of the SAUP harvest database. Our group formulation combines functional groups (pelagic, demersal, and benthic, for example). Such an assumption may not be appropriate for particular aspects of benthic

ecosystems, which have been shown to require more than a representation of size structure to adequately represent core ecosystem features (Duplisea et al., 2002; Blanchard et al., 2009). Nevertheless, for our global-scale model, we feel justified in using such a group formulation since Friedland et al. (2012) found little difference in how the biogeochemical attributes and harvest of pelagic and demersal fisheries reacted to primary production and trophic transfer efficiencies. Alternative group formulations remain a promising avenue of research in global fisheries modeling, one that could be pursued in future work (Blanchard et al., 2009; Maury, 2010).

Although we use the classical MVF model, we implement empirical relationships whenever possible to determine fundamental rates such as growth and mortality, since our goal is to represent fish biomass at the global scale, while limiting the model complexity and number of parameters. As opposed to determining both growth and mortality from explicit predation, as in Maury et al. (2007), Blanchard et al. (2009), Hartvig et al. (2011), and Maury and Poggiale (2013), NPP and the size distribution of phytoplankton set growth rates

- ¹⁵ for all mass classes of fish through a trophic transfer of energy from phytoplankton to fish. To guarantee that growth rates do not exceed realistic values, a von Bertalanffy growth formulation that is based on field observations acts as an upper limit to the growth rate (von Bertalanffy, 1949; Hartvig et al., 2011; Andersen and Beyer, 2013). Mortality is based on an empirical parameterization that depends on mass and asymptotic mass, but also on the
- constant allometric growth rate in the empirical limit (Gislason et al., 2010; Charnov et al., 2012).

BOATS continues on from the earlier in a tradition of studies that model the global fishery by applying ecological principles to spatially-resolved environmental properties. This line of research can be traced to the work of Ryther (1969), who estimated the potential global

fish production and harvest based on NPP and simple trophic scaling relationships. More recently, Pauly and Christensen (1995); Chassot et al. (2010); Watson et al. (2013a), and Rosenberg et al. (2014) examined the sustainability of global harvest by considering the NPP required to generate present harvest levels, given simple macroecological assumptions. Others have examined global or basin-scale problems concerning fish biomass using

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models based on the MVF model. APECOSM (the Apex Predators ECOSystem Model, Maury, 2010) was used to study tuna dynamics in the Indian Ocean (Dueri et al., 2012), as well as the impact of climate change on biomass and the spatial distribution of pelagic fish at the global scale (Lefort et al., 2014). Moreover, Blanchard et al. (2009, 2012) considered the impact of future environmental change in Large Marine Ecosystems (LMEs) and Exclusive Economic Zones, while Woodworth-Jefcoats et al. (2012) examined the impact of climate change in three regions of the Pacific Ocean.

2.1 Biomass evolution: the McKendrick-von Foerster (MVF) model

The MVF model, a first-order advection-reaction partial differential equation, was first presented by McKendrick (1926) for use in epidemiology, but was later more formally derived for use in the study of cellular systems by von Foerster (1959). Since it provides a natural framework for representing aspects of size dependency and fish life history, and generates biomass spectra that resemble those found in the field (Sheldon et al., 1972; Blueweiss et al., 1978; Brown et al., 2004; Marquet et al., 2005; White et al., 2007), the MVF model has seen a wide variety of applications in marine ecosystems and fisheries. Ecosystem models that have applied the MVF approach to large-scale fisheries studies generally make use of the classical size-structured equation, but differ in the formulations used to calculate

growth, mortality, and reproduction, and differ in the structural organisation of fish groups.
Although the MVF model can be expressed by a variety of variables, it is usually presented in terms of the number of fish (the abundance) that evolve in time as a function of the fish age. As an alternative to age, size (measured as length or mass) is also used as an organizing variable, since it can be more descriptive than age for certain applications. Since fish growth (von Bertalanffy, 1949; Andersen and Beyer, 2013), natural mortality (Pauly, 1980; Gislason et al., 2010; Charnov et al., 2012), and harvest (Rochet et al., 2011)

are generally size-dependent, we employ size in lieu of age. Moreover, we describe size in terms of mass as opposed to length, although there is a strong relationship between fish mass and length (Froese et al., 2013). The MVF model uses a spectral framework to describe fish populations; that is, it describes the biomass of fish of mass m at time t by a continuous spectrum f(m,t) such that the fish biomass in the mass interval [m, m + dm] is f(m,t) dm. Although abundance is typically used in applications of the MVF model, and has been used in marine ecosystem

- ⁵ applications, see for example Andersen and Beyer (2006); Blanchard et al. (2009), or Datta et al. (2010), we use biomass to compare our results more directly with the harvest data that we use to evaluate BOATS. Regardless, since the abundance *n* and biomass *f* spectra are related by f(m,t) = n(m,t)m, f(m,t) = n(m,t)m, in the continuous case, using one form over the other does not influence the model dynamics. We note that, in the numerical
- implementation of the model, there will be a small difference between the two since we use the geometric mean to represent a discretized range of masses (Sect. 2.9). Hence, as fish grow they jump from one geometric mean to next, which may result in an accumulation of biomass.

Fish biomass evolves in time as

¹⁵
$$\frac{\partial}{\partial t}f_k(m,t) = -\underbrace{\frac{\partial}{\partial m}\gamma_{S,k}(m,t)f_k(m,t)}_{1} + \underbrace{\frac{\gamma_{S,k}(m,t)f_k(m,t)}{m}}_{2} - \underbrace{\underbrace{\Lambda_k(m,t)f_k(m,t)}_{3}}_{3}$$

$$f_k(m,t=0) = f_{k,m,0}$$
 (2)

$$f_k(m_0,t)\gamma_{\underline{k}\underline{S},\underline{k}}(m_0,t) = R_k(m_0,t),$$

where $f_k(m,t)$ is the biomass spectrum in grams of wet fish biomass (gwB) per square meter of ocean surface per unit of the mass class (gwB m⁻² g⁻¹), for an individual fish of mass m, at time t, belonging to group k. In Appendix A, we derive the biomass form of the MVF model used in Eq. (1). From the definition of the biomass spectrum above, we have that the cumulative biomass at time t of individuals of mass ranging from 0 to m is the integral $F_k(m,t) = \int_0^m f_k(m',t) dm'$. In this paper, spectral variables such as the biomass spectra $f_k(m,t)$ are written in lower case, whereas cumulative variables that are integrated over size are written in upper case. Discussion Paper L

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(1)

(3)
Fish biomass is controlled by growth, mortality, reproduction, and recruitment (note that we present harvest in the companion paper, (Carozza et al., 2016)). Term 1 on the right hand side of Eq. (1) represents the <u>somatic</u> growth in fish biomass that occurs at a rate $\gamma_k(m,t) \cdot \gamma_{S,k}(m,t) (g s^{-1})$. This term results from fish growing from one interval of mass, which in the discrete case is called a mass class, into the adjacent mass class (for example from a class of 1 to 2 kg to a class of 2 to 3 kg). Since the MVF model is founded on the conservation of numbers of fish (Appendix A), term 2 represents the biomass growth

- accumulation that occurs from fish growing in size. Term 3 of Eq. (1) represents the natural mortality $\Lambda_k(m)f_k(m,t)$ (gwB m⁻² g⁻¹ s⁻¹), or all non-harvesting sources of fish mortality, which includes losses to predation as well as non-predation losses such as parasitism and disease, old agesenescence, and starvation (Pauly, 1980; Brown et al., 2004). Although we do not consider harvest mortality in this paper, in the full BOATS model (described by Carozza et al. (2016), in review) it is represented by another loss term on the right hand side of equation Eq. (1). The growth rate $\gamma_k(m,t) \gamma_{S,k}(m,t)$ (Eq. 22) and the mortality rate $\Lambda_k(m)$ (Eq. 26) depend on both mass and temperature.
- Since the time evolution equation of the MVF model is a first-order partial differential equation, to guarantee that it is well-posed, we must we specify an initial condition (Eq. 2) and a boundary condition (Eq. 3). The initial condition, or the fish biomass spectrum at the starting time $f_{k,m,0}$, is discussed in Sect. 3.1. The boundary condition, which is defined at the lower mass boundary m_0 , determines the flux of biomass that is added to the biomass spectrum at the initial size class, and depends on the energy allocated to reproductive biomass, the recruitment, and the NPP. This term is detailed in Sect. 2.4 and summarized in Eq. (29). A schematic of the ecological module of BOATS, with the main model components and processes, is presented in Fig. 1.

25 2.2 Temperature dependence

Organismal body temperature is a fundamental driver of physiological processes since it strongly controls rates of metabolic activity and therefore strongly influences growth, mortality, and reproduction rates (Boltzmann, 1872; ?; Brown et al., 2004)(Brown et al., 2004).

(4)

To model temperature dependence, which we represent by the function a(T), we apply the van't Hoff–Arrhenius equation

$$a(T) = \exp\left[rac{\omega_a}{k_B}\left(rac{1}{T_{\mathsf{r}}}-rac{1}{T}
ight)
ight],$$

where T_r (K) is the reference temperature of the process in question (growth or mortality, for example), k_B (eV K⁻¹) the Boltzmann constant, and ω_a (eV) the activation energy of metabolism. Although there is at present no mechanistic derivation of the relationship between metabolic rate and temperature at the level of an entire organism, we interpret the exponential temperature dependence of Eq. (4) as an empirical parameterization of this complex relationship with strong observational constraints (Clarke, 2003, 2004; Marquet et al., 2005; Vandermeer, 2006).

For all temperature-dependent rates, we use the average water temperature from the upper 75 m of the water column (Jennings et al., 2008), since it is representative of an average mixed layer depth and so identifies the average temperature at which photosynthesis takes place (Dunne et al., 2005), and since it is representative of the depths at which many

- fish live and are harvested (Morato et al., 2006; Watson and Morato, 2013). We further assume that fish adopt exactly the water temperature. Given that the greater majority of marine organisms are ectotherms, we feel that this is a <u>more than</u> reasonable assumption. Taking the average of the upper 75 m of the water column could create biases in regions with strong vertical temperature gradients, since different components of the ecosystem
- ²⁰ could live at substantially different temperatures, or in regions that are dominated by bottom dwellers in regions deeper than 75 m. However, given that many commercial fish spend significant time near the surface, but actively travel throughout the water column, we feel that this depth is an appropriate first approximation of the average temperature felt by the community. Note that the temperature we apply is generally not appropriate accurate for
- mesopelagic ecosystems, which could make up a large part of marine biomass (Irigoien et al., 2014), but since the majority of these ecosystems are not commercial have not been commercially exploited, they are not included in our modeled community.

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(6)

2.3 Energy allocation to growth

Fish growth rates are key mass-dependent quantities that characterize each fish group and are limited by the energy available to consumers, and, ultimately, by the photosynthetic primary production. We assume that there is a constant energetic content of biomass (Krohn

- et al., 1997; Maury et al., 2007), and so treat biomass and energy as equivalents. We envision that energy is supplied to a fish of mass *m* by the transfer of biomass through the food web by means of predation. This Following macroecological theory, this complex process is parameterized by assuming that a fraction of the energy from NPP is transferred up through the food web to become fish biomass production, depending on the average trophic effi-
- ¹⁰ ciency, the average predator to prey mass ratio, and the phytoplankton size (Ernest et al., 2003; Brown et al., 2004) (Eq. 8). Individual fish then allocate this energy input to either somatic growth (that is, the formation of additional biomass, which we from here on refer to simply as growth $\gamma_k(m,t)\gamma_{S,k}(m,t)$, gs^{-1}) or to formation of reproductive biomass $\xi_{R,k}(m,t)\gamma_{R,k}(m,t)$ (gs^{-1}), and so we have that
- 15 $\xi_{I,k}(m,t) = \gamma_k(m,t)_{S,k} + \xi_{\gamma_{R,k}}(m,t),$

where $\xi_{I,k}(m,t)$ is the input of energy to a fish at time t in group k. We rearrange to write the growth rate as

 $\gamma_k(m,t)_{\underline{S},\underline{k}} = \xi_{I,k}(m,t) - \underline{\xi}\gamma_{R,k}(m,t).$

It is important to recognize that the individual fish growth rate cannot exceed a biologically-determined maximum rate, no matter how much food is available. This aspect of fish growth is based on empirical observations and allometric arguments, and founded on the work of von Bertalanffy (1938, 1949, 1957) and expanded upon by many others including Paloheimo and Dickie (1965), West et al. (2001), and Lester et al. (2004). To take this growth rate limitation into account, we assume that the realized input energy $\xi_{I,k}(m,t)$ cannot exceed that supplied by NPP through the trophic scaling, or that determined by

(7)

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empirical growth limits, and so have that the energy input is

 $\xi_{I,k}(m,t) = \min[\xi_{P,k}(m,t),\xi_{\mathsf{VB},k}(m,t)],$

where $\xi_{P,k}$ $\xi_{P,k}(m,t)$ is the energy input to fish from NPP as transferred through the food web, and $\xi_{VB,k}$ $\xi_{VB,k}(m,t)$ is that input from a purely empirical allometric framework follow-

ing von Bertalanffy (1949). Essentially, $\xi_{VB,k} \xi_{VB,k}(m,t)$ describes the maximum growth rate of fish in the case that food is extremely abundant.

We partition NPP equally among three fish groups, and so the group fish production is the fraction allocated to group k, $\phi_{\pi,k}$, multiplied by the fish production $\Pi(m,t)$. Groups are independent of one another, except in that they all receive a part of NPP. Ecologically, this

- ¹⁰ We define $\phi_{\Pi_{\Psi},C}$ as the fraction of NPP that is potentially available to the sum of all commercial fish groups. In the present work, we assume that $\phi_{\Pi_{\Psi},C}$ is equal to 1, and therefore omit it from the equations. This simplifying assumption implies that the entire global ecosystem of animals larger than 10 g would have consisted of potentially commercial species prior to fish harvesting (including bycatch). Obviously this is incorrect,
- ¹⁵ in that the existence of non-commercial animals larger than 10 g requires that $\phi_{\Pi_{\Psi},C} < 1$ in the real world. However, given the weak observational constraints on biomasses of non-commercial animal species at the large scale, and the fact that the species composition of all marine ecosystems has been heavily altered by human activity, it is very difficult to estimate the true value of $\phi_{\Pi_{\Psi},C}$. Despite this difficulty, sensitivity tests revealed that
- ²⁰ biomass and harvest in the model are approximately linear with $\phi_{\Pi_{\Psi},C}$ (not shown). Since we constrain the parameters in BOATS by comparing linear correlations of modelled and observed harvest (see Sect. 3, Table 1, and Carozza et al. (2016)), and given the linearity of modelled harvest vs. $\phi_{\Pi_{\Psi},C}$, the value of $\phi_{\Pi_{\Psi},C}$ would have a negligible effect on the spatial correlation criterion used for the optimized parameter choices. Nevertheless, it
- ²⁵ should be pointed out that using alternate values of $\phi_{\Pi_{\Psi},C}$ would change the predicted biomass and harvest, all else being equal.

We further assume that each of the three fish groups has access to an equal fraction of the available primary production, $\phi_{\Pi_{\Psi},C}/3$. By assuming that constant portions of the

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available photosynthetic energy are available to each of the commercial fish groups, all groups are assured to coexist stably. Ecologically, our assumption implies equal resource partitioning of NPP to each group, both when they are at the larval stage (through recruitment) and as juveniles and adults (through growth) (Chesson, 2000). This can be thought

- ⁵ of as each group occupying an ecological niche reflecting a separate ecological niche for each group that remains stable over time, and implies that excess NPP, which would result from growth-rate limitation of biomass advectionone group, is not available to other potentially commercial groups, but rather supplied to non-commercial species. Non-commercial species could include, among others, unharvested mesopelagic fish, planktonic inverte-
- ¹⁰ brates such as cnidariansand fish, and benthic invertebrates such as amphipods and nematodes. By assuming that a fixed portion of NPP goes to each commercial group, all groups are assured to coexist stably Although this and the previous assumption are not strictly accurate representations of the marine ecosystem, we feel that they are commensurate with the simple three-group representation of the ecosystem and the scarcity of appropriate
- data constraints, and could be improved in future work.

Each individual fish receives an equal part of the fish production that is input to its mass class, which we here identify as an infinitesimal mass interval of width dm. The Where $\phi_{C,k}$ is the fraction of $\phi_{\Pi_{\Psi},C}$ that is available to group k, and $\pi(m,t)$ the fish production distribution, the individual fish production is therefore the fish production in the mass interval $\phi_{\pi,k}\pi(m,t)dm - \phi_{C,k}\pi(m,t)dm$ divided by the number of individuals in the mass class $n_k(m,t)dm$ (Eq. 8). Since the abundance spectrum $n_k(m,t)$ is equal by definition to $f_k(m,t)/m$, the primary-production-based input of energy to each individual fish is

$$\xi_{P,k}(\underline{m,t}) = \frac{\phi_{\pi,k}\pi(m,t)\,\mathrm{d}m}{n_k(m,t)\,\mathrm{d}m} \frac{\phi_{C,k}\pi\,\mathrm{d}m}{n_k\,\mathrm{d}m} = \frac{\phi_{\pi,k}\pi(m,t)m}{f_k(m,t)} \frac{\phi_{C,k}\pi m}{f_k(m,t)}.$$
(8)

Since we assume that the NPP that is transferred up through the trophic web is uniformly input to all individuals in a -given mass class, if the biomass in a -mass class falls (due to harvesting due to a removal (such as harvesting, for example) then this is equivalent to a decrease in the number of individuals has fallen in that mass class. This implies that

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more fish production is would input to each individual, and so in such a scenario $\xi_{P,k}$ increases would increase. This input of energy depends on the biomass (also referred to as density-dependence) and the fish production. The fish production term depends on temperature through the representative mass of phytoplankton $m_{\psi}(t)$ (Eq. 25), which is a function of the temperature-dependent large fraction of phytoplankton $\Phi_{I}(t)$ (Dunne et al., 2005).

In conditions that are not limited by food availability, the standard von Bertalanffy (somatic) growth rate equation is

$$\gamma_{\mathsf{VB},k}(m) = Am^b - k_a m - k_r m,$$

5

where the Am^b term represents the energy input from food intake after assimilation and standard metabolism, and k_am and k_rm represent the energy used in activity and reproduction, respectively (von Bertalanffy, 1949; Paloheimo and Dickie, 1965; Chen et al., 1992; Andersen and Beyer, 2013). The allometric growth rate (not to be confused with the growth rate γ_k somatic growth rate $\gamma_{S,k}$), which we write as $A = A_0 a_A(T)$, is the growth constant A_0 (g^{1-b} s⁻¹) modulated by the van't Hoff–Arrhenius temperature dependence for growth 15 $a_A(T)$ (Eq. 4).

The energy input we wish to resolve is that for both growth and reproduction, and so we add the reproduction term $k_r m$ to both sides of Eq. (9) to find the energy input to be

 $\xi_{\mathsf{VB},k}(m) = Am^b - k_a m. \tag{10}$

Although the interpretation of the terms in Eq. (10) do not exactly correspond to von Bertalanffy's original interpretation of a balance between anabolic growth and catabolic decay, we refer to this equation as the von Bertalanffy energy input $\xi_{\text{VB},k}$. We consider different values of the activation energy of metabolism for growth $\omega_{a,A}$ and mortality $\omega_{a,\lambda}$ (Eq. 4), which result in different temperature dependence curves $a_A(T)$ and $a_\lambda(T)$. The parameter b (unitless) is the allometric scaling constant, and k_a (s⁻¹) is the mass specific investment in

²⁵ activity. We follow Andersen and Beyer (2013) and define a new constant $\epsilon_a = k_a/(k_a + k_r)$, which when combined with the idea that there is zero growth at the asymptotic mass $m_{\infty,k}$

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(13)

(Munro and Pauly, 1983; Chen et al., 1992; Andersen and Beyer, 2013), allows us to express the mass specific investment in activity as $k_a = A\epsilon_a m_{\infty,k}^{b-1}$. At each group's asymptotic mass, we therefore have that $\xi_{\text{VB},k}(m_{\infty,k}) = A(1-\epsilon_a)m_{\infty,k}^b$.

Equation (7) for the input of energy to growth and reproduction is therefore

the minimum of a term that depends on biomass and one that does not. Applying the definition of the fish production spectra that we introduce in the next section (Eq. 24), we have a change in growth regime when f_k is such that

$$f_k(\underline{m,t}) < \frac{\phi_{\pi,k} \Pi_{\psi}(t)}{m_{\psi}(t)} \frac{\phi_{C,k} \Pi_{\psi}}{m_{\psi}} \frac{m^{\tau}}{Am^b - k_a m}.$$
(12)

¹⁰ When biomass is low enough that this equation holds, NPP no longer influences the input energy, and fish will grow at their maximum physiological rate., and any unused energy available to fish production is assumed to be transferred to unresolved parts of the ecosystem. For low productivity systems, the model could overestimate biomass since a larger fraction of primary production will be transferred to commercial species. However, in high productivity systems, the allometric limit is more likely to set growth rates and so a larger fraction will be transferred to the non-commercial groups. That said, the potential for, and the magnitude of, such a feature will depend on the particular values of the growth

.

rates at the site in question (Eq. 11).

2.4 Energy allocation to reproduction

We assume that the energy allocated to reproduction $\xi_{R,k}(m,t) \gamma_{R,k}(m,t)$ is proportional to the total input energy $\xi_{I,k}(m,t)$ such that

 $\underline{\xi}\underline{\gamma}_{R,k}(m,t) = \Phi_k(m)\xi_{I,k}(m,t),$

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where $\Phi_k(m)$ is the mass-dependent fraction of input energy that is allocated to reproduction. From Eq. (6), we write the growth rate as

$$\gamma_{\underline{k}}(\underline{m},\underline{t})_{\underline{S},\underline{k}} = \left(1 - \Phi_{\underline{k}}(\underline{m})\right) \xi_{I,\underline{k}}(\underline{m},\underline{t}).$$
(14)

We now derive an expression for $\Phi_k(m)$. Following Hartvig et al. (2011), we assume that the allocation to reproduction is proportional to mass (Blueweiss et al., 1978; West et al., 2001; Lester et al., 2004; Andersen and Beyer, 2013), and that it also scales with a sizedependent rate $s_k(m)$ that defines the size-structure of the transition to maturity (Eq. 23). This gives us

$$\underline{\xi}\gamma_{R,k}(m,t) = k_r^{\max} s_k(m)m,\tag{15}$$

where k_r^{max} is a normalizing constant. Combined with Eq. (13), we have that

15

$$\underline{\xi}\underline{\gamma}_{R,k}(\underline{m,t}) = \Phi_k(\underline{m})\overline{\xi}_{I,k}(\underline{m,t}) = k_r^{\max}s_k(\underline{m})\underline{m},$$
(16)

where $\overline{\xi}_{I,k}$ is a representative input energy that we employ to guarantee that the allocation to reproduction does not change with biomass. For the representative input energy, we take the maximum possible value; that is, the von Bertalanffy input energy described in Eq. (10), and so have that $\overline{\xi}_{I,k} = \xi_{\text{VB},k}$. We therefore determine $\Phi_k(m)$ for the energy input regime that is not limited by fish production, and find that

$$\Phi_{k}(\underline{m}) = \frac{k_{r}^{\max} s_{k}(m)m}{\xi_{\mathsf{VB},k}(m,t)} \frac{k_{r}^{\max} s_{k}m}{\xi_{\mathsf{VB},k}}.$$
(17)

We determine k_r^{max} by applying the definition of the asymptotic mass, namely that it is the mass at which energy is only allocated to reproduction and so $\Phi_k(m_{\infty,k}) = 1$. This gives

20
$$\Phi_k(m_{\infty,k}) = \frac{k_r^{\max} s_k(m_{\infty,k}) m_{\infty,k}}{\xi_{\mathsf{VB},k}(m_{\infty,k},t)} = 1,$$
(18)

and so we have that

$$k_r^{\max} = \frac{\xi_{\mathsf{VB},k}(m_{\infty,k},t)}{s_k(m_{\infty,k})m_{\infty,k}}.$$
(19)

We replace this value of k_r^{max} into Eq. (17) to find that

$$\Phi_{k}(\underline{m}) = \frac{s_{k}(m)}{\underline{s_{k}(m_{\infty,k})}} \frac{s_{k}}{\underline{s_{k}(m_{\infty,k})}} \frac{m}{m_{\infty,k}} \frac{\xi_{\mathsf{VB},k}(m_{\infty,k},t)}{\underline{\xi_{\mathsf{VB},k}(m,t)}} \frac{\xi_{\mathsf{VB},k}(m_{\infty,k},t)}{\underline{\xi_{\mathsf{VB},k}(m,t)}}.$$
(20)

⁵ Applying Eq. (10) for $\xi_{VB,k}$, and noting that $s_k(m_{\infty,k})$ is essentially equal to 1, we find that

$$\Phi_k(\underline{m}) = s_k(\underline{m}) \frac{1 - \epsilon_a}{(m/m_{\infty,k})^{b-1} - \epsilon_a}.$$
(21)

Bringing this development together with Eq. (14), the individual fish growth rate is

$$\gamma_{\underline{k}}(\underline{m,t})_{\underline{S,k}} = \left(1 - s_{\underline{k}}(\underline{m}) \frac{1 - \epsilon_{a}}{(m/m_{\infty,k})^{b-1} - \epsilon_{a}}\right) \min\left[\frac{\phi_{\pi,k}\pi(\underline{m,t})m}{f_{\underline{k}}(\underline{m,t})} \frac{\phi_{C,k}\pi m}{f_{\underline{k}}}, Am^{b} - k_{a}m\right].$$
(22)

As in Hartvig et al. (2011), we assume that the mass structure of the allocation of energy to reproduction $s_k(m)$ is a sharply transitioning function that shifts from near zero to near one around the mass of maturity $m_{\alpha,k}$. Based on Beverton (1992) and Charnov et al. (2012), we further assume that the mass of maturity is proportional to the asymptotic mass $m_{\infty,k}$ such that $m_{\alpha,k} = \eta m_{\infty,k}$ (Table 1). Although other functional forms are plausible, $s_k(m)$ must have a transition in mass that is proportional to $m_{\infty,k}$ (or to the maturity mass) (Hartvig et al., 2011), and so we use the functional form used by Hartvig et al. (2011),

$$s_k(\underline{m}) = \left[1 + \left(\frac{m}{m_{\alpha,k}}\right)^{-c_s}\right]^{-1},\tag{23}$$

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where the parameter c_s determines how quickly the transition from zero to one takes place (Fig. 2). For reference, we calculate the reproduction allocation mass scale, the range over which the majority of the change in reproduction allocation takes place, as the inverse of the derivative evaluated at the maturity mass, $\left(\frac{ds_k}{dm}\Big|_{m=m_{\alpha,k}}\right)^{-1}$, which we find to be $\frac{4m_{\alpha,k}}{c_s}$.

5 2.5 Fish production spectrum

25

We model the biomass production of fish by assuming that both phytoplankton and fish production are part of the same energetic production spectrum (Sheldon et al., 1972; Ernest et al., 2003; Brown et al., 2004). Unlike in the approaches of Maury et al. (2007); Blanchard et al. (2009), Maury et al. (2007) and Hartvig et al. (2011), among others, we do not model the growth and decay dynamics of phytoplankton biomass. Instead, we represent fish production over a spectrum of individual fish masses, $\pi(m,t)$ (mmol C m⁻² g⁻¹ s⁻¹). Following Brown et al. (2004) and Jennings et al. (2008), we base this formulation on (1) the NPP $\Pi_{\psi}(t)$ (mmol C m⁻² s⁻¹) (Sect. 2.8), (2) the representative size at which NPP takes place $m_{\psi} m_{\psi}(t)$ (g) (Jennings et al., 2008), and (3) the trophic

scaling exponent τ that indicates how efficiently energy is transferred through the trophic web, where τ depends on the trophic efficiency α and the predator to prey mass ratio β , and is equal to $\log(\alpha)/\log(\beta)$ (Brown et al., 2004). The fish production spectrum follows

$$\pi(\underline{m,t}) = \frac{\Pi_{\psi}(t)}{\underline{m_{\psi}(t)}} \frac{\Pi_{\psi}}{\underline{m_{\psi}}} \left(\frac{\underline{m}}{\underline{m_{\psi}(t)}} \frac{\underline{m}}{\underline{m_{\psi}}} \right)^{\tau-1}.$$
(24)

As in Brown et al. (2004), we assume that α and β , and hence τ , are constant. From the expression for fish production detailed in Eq. (24), we determine the individual fish growth rate using Eq. (22).

Although variability in the trophic scaling τ , that could depend on environmental or ecosystem characteristics, is potentially of significant importance, we take here the simple assumption that the trophic scaling is globally constant, as other authors have (Brown et al., 2004; Jennings et al., 2008). We note that, using a large database of individual prev

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eaten by individual predators, Barnes et al. (2010) found that the predator to prey mass ratio increases with predator mass. Given that we apply an average value of β , and assuming that all else remains equal, the work of Barnes et al. (2010) implies that we would underestimate β for large *m* and overestimate β for small *m*, and so (by Eq. 24) we under-

- ⁵ estimate π_k for large *m* and overestimate π_k for small *m*. Essentially, a mass-dependent β would tend to decrease the steepness of biomass spectra relative to what is shown here. It is also commonly assumed that the trophic efficiency α is constant (Brown et al., 2004; Jennings et al., 2008; Tremblay-Boyer et al., 2011). Based on acoustic biomass estimates and modelling work, Irigoien et al. (2014) suggests that trophic efficiency can instead be
- ¹⁰ significantly different in low and high productivity regions, at different levels in the food web (from phytoplankton to mesozooplankton and from mesozooplankton to fish) and that it can also depend on environmental parameters such as temperature (through its influence on organismal metabolic rates) and water clarity (which affects visual predation). Quantifying variability in τ is an important target for future work.
- ¹⁵ The production spectrum is the product of two terms. The first is the initial value determined at the representative phytoplankton mass $m_{\psi}m_{\psi}(t)$, which corresponds to the NPP normalized by the representative phytoplankton size. The fish production spectrum then follows a power law dependence in m with a scaling exponent of $\tau - 1$. This mass scaling represents larger phytoplankton (larger $m_{\psi}m_{\psi}(t)$) being trophically closer to fish than
- ²⁰ smaller phytoplankton, thereby permitting more energy to be transferred from phytoplankton to fish (Ryther, 1969). The power law dependence that we use is based on Kooijmann (2000) and Brown et al. (2004). Since the The model is forced with NPP data, observations of NPP, and so we run the model in units of mmol C, and then convert biomass and harvest . For analysis and presentation, we convert to grams of wet biomass (gwB) for analysis and
- presentation by assuming a constant conversion rate by assuming that there are 12 g C per mol C, and that there are 10 gwB for every g of dry carbon (Jennings et al., 2008).

Phytoplankton mass ranges over several orders of magnitude (Jennings et al., 2008). We take a simple approach and express the spectrum of phytoplankton as a single representative mass at which NPP takes place. Due to the wide range of phytoplankton mass, we

calculate the representative mass as

$$m_{\psi}(\underline{t}) = m_{\mathsf{L}}^{\Phi_{\mathsf{L}}(t)} m_{\mathsf{S}}^{1-\Phi_{\mathsf{L}}(t)},$$

and so take the geometric mean of the mass of a typical large, m_L , and a typical small, m_S , phytoplankton, weighted by the fraction of production due to large or small phytoplankton, $\Phi_L(t)$ and $1 - \Phi_L(t)$, respectively. We calculate this fraction using the phytoplankton size structure model of Dunne et al. (2005), which resolves small and large phytoplankton and

- structure model of Dunne et al. (2005), which resolves small and large phytoplankton and assumes that small zooplankton are able to successfully prey upon increasing production of small phytoplankton, but that large zooplankton are unable to do so as effectively for large phytoplankton production. Dunne et al. (2005) propose an empirical relationship for
- ¹⁰ the large fraction of NPP $\Phi_L(t)$ in terms of temperature $T_C(t)$ (°C) and the NPP, the Eppley factor $e^{k_E T_C(t)}$ where k_E (°C⁻¹) is the Eppley temperature constant for phytoplankton growth, and Π^* (mmol C m⁻³ d⁻¹) the productivity normalized to a temperature of 0 °C. The Dunne et al. (2005) model resolves a high fraction of the variability in phytoplankton community structure (Agawin et al., 2000), and provides a mechanism to explain how the fraction of large phytoplankton biomass increases with increasing phytoplankton biomass. Although we use this particular formulation for the large fraction in Eq. (25), future work could examine

alternatives (Denman and Pena, 2002).

2.6 Natural mortality

The natural mortality term represents all forms of natural (non-fishing) mortality. It mainly consists of predation, but also includes non-predatory sources of mortality such as parasitism, disease, and old age senescence (Pauly, 1980). This term is of first-order importance in determining energy flows in marine food webs, and so also in determining biomass. In pursuing our principle of using empirical parameterizations to represent complex processes that are incompletely understood, we follow the work of Gislason et al. (2010) and

(25)

Charnov et al. (2012) and take the mortality rate to be

$$\Lambda_k(\underline{m}) = \lambda m^{-h} m_{\infty,k}^{h+b-1},$$

where $\lambda = e^{\zeta_1}(A_0/3)a_\lambda(T)$ (see Appendix B for a full derivation of this form). ζ_1 is a parameter estimated from mortality data (Gislason et al., 2010), $A_0 (g^{1-b} s^{-1})$ is the growth constant from Eq. (10), and $a_\lambda(T)$ is the van't Hoff–Arrhenius exponential for mortality as described in Eq. (4). Charnov et al. (2012) provided a mechanistic underpinning for Eq. (26) by calculating the optimal number of daughters per reproducing female over that female's lifetime. Unlike other empirical mortality rate frameworks, such as that of Savage et al. (2004), the mass dependence m^{-h} does not depend on the allometric growth scaling *b*, and so the mass dependence of the mortality rate is not determined by internal biological parameters, but by predation and competition (Charnov et al., 2012). The losses due to natural mortality, term 3 in Eq. (1), are linearly proportional to biomass as in Gislason et al. (2010), and in keeping with the classical MVF model.

It is important to highlight the fact that unlike some other models, we do not adopt an explicit representation of predation-dependent mortality (Maury et al., 2007; Blanchard et al., 2009; Hartvig et al., 2011). The mortality rate only depends on the organism mass, asymptotic mass, and temperature, and is linear in biomass. This choice is motivated by the wide range of predator-prey mass ratios in marine ecosystems (Barnes et al., 2010), and the complexity and non-stationarity of food web relationships. In applying this parameteriza-

- tion, we avoid the complication of choosing a difficult-to-constrain prey selectivity function, and benefit from applying mortality rates that are directly founded in observed rates. Without necessarily losing realism, this parameterization simplifies the complicated dynamics that result from more sophisticated prey selectivity formulations (Andersen and Pedersen, 2010).
- At the same time, since the abundance of predators does not feature in the Since the prey mortality rate , we cannot does not depend on the predator biomass, we do not resolve top-down trophic cascades (Andersen and Pedersen, 2010; Hessen and Kaartvedt, 2014). Since, at present, the At present, a scarcity of data prevents a hinders a formal

(26)

verification of theorized generalized trophic cascades in the open ocean, we feel this is a reasonable simplifying assumption. Through which would be desirable for the formulation of their impact within the BOATS framework. However, we do represent bottom-up effects through the growth formulation described in Eq. (1), however, changes in biomass due to harvesting, for example, are carried up since a change in biomass in one size class is

harvesting, for example, are carried up since a change in biomass in one size class i carried upward through the trophic web as fish grow to larger mass classes.

2.7 From reproduction to recruitment

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Fish reproduction and recruitment comprise a set of complex ecological processes that result in new fish biomass entering a fishery (Myers, 2002). This first involves fish allocating energy to reproduction and releasing eggs and sperm during spawning. Fertilized eggs must then survive predation until they hatch to become larvae, when they must again survive predation until they grow into juveniles (Dahlberg, 1979; McGurk, 1986; Myers, 2001).

- The end of the juvenile stage is generally defined as when fish reach sexual maturity or when they begin interacting with other adult members of the fishery (Kendall et al., 1984).
- ¹⁵ The definition of a recruit is more nuanced since it generally depends on the fishery in question and can be based on a particular size or age, the size or age of sexual maturity, or the size or age at which fish can be caught (Myers, 2002). For the model, we refer to recruitment as the flux of new biomass into the lower boundary mass (m_0) of each group.
- Recruitment is driven by biomass-dependent (density-dependent) processes, such as predation and disease, as well as by biomass-independent (density-independent) processes such as environmental change. These processes strongly and nonlinearly affect mortality throughout the egg, larval, and juvenile stages (Dahlberg, 1979; McGurk, 1986; Myers, 2002). To model the number of recruits that result from a given spawning stock of biomass, one must make assumptions on the nature of these processes. The widely-used
- stock-recruitment models of Ricker (1954); Schaefer (1954), and Beverton and Holt (1957), and the generalization of these models by Deriso (1980) and Schnute (1985), make such assumptions and operate in terms of the spawning stock biomass; that is, the biomass that is of reproductive age.

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We model recruitment by considering both the NPP and the production and survival of eggs by adult fish. Our formulation is based on the Beverton-Holt stock recruitment relationship (which employs a Holling Type 2 functional form, Holling, 1959), as used by Beverton and Holt (1957) and Andersen and Beyer (2013), with NPP setting the upper limit and the half-saturation constant (Eq. 29). This form allows for an approximately linear decrease to zero recruitment as the spawning stock biomass goes to zero, but sets an upper limit that depends on the NPP when the spawning stock biomass is large, in order to represent the role of food availability in determining larval survival.

5

The flux of biomass out of a mass class is the growth rate multiplied by the biomass in that mass class (Eq. 1). Since the recruitment is also a flux of biomass (one that occurs at the lower mass boundary), to define it in terms of NPP $R_{P,k}(m_0,t)$ (gwB m⁻² s⁻¹), we apply Eq. (8) and find that

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 (gwB m⁻² s⁻¹), we apply Eq. (8) and find that
$$R_{P,k}(m_0,t) = \gamma_{P,k}(m_0,t)f_k(m_0,t) = \frac{\phi_{\pi,k}\pi(m_0,t)m_0}{f_k(m_0,t)} \frac{\phi_{C,k}\pi(m_0,t)m_0}{f_k(m_0,t)} f_k(m_0,t) = \phi_{\pi,k}c_k\pi(m_0,t)$$
(27)
where m_0 is the lower bound of the smallest mass class, and π is the fish production spectrum from Eq. (24). Alternatively, the recruitment from the production and survival of eggs to recruits, $R_{e,k}(m_0,t)$ (gwB m⁻² s⁻¹), depends on the energy allocated to reproduction, $\xi_{R,k}(t) \gamma_{R,k}(t)$ (Eq. 13), by all n_k individuals over all mass classes, which we write as

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$$R_{e,k}(m_0,t) = \phi_{\mathsf{f}} s_{\mathsf{e}} \frac{m_0}{m_e} \int_{m_0}^{m_{\infty,k}} \underline{\xi} \gamma_{R,k}(\underline{m,t}) n_k(\underline{m,t}) \mathrm{d}m.$$
(28)

The model biomass includes both males and females, which are assumed to mature at the same mass (Beverton, 1992). As in other model studies (Maury et al., 2007; Andersen 20 and Pedersen, 2010; Andersen and Beyer, 2013), males and females of reproductive age continually reproduce, yet only the female contribution is counted in the flux into the smallest

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mass class, since the male contribution to a fertilized egg is negligible compared to that of the female. Hence, when the integral part of Eq. (28) is multiplied by the fraction of females, ϕ_f , we have the biomass of eggs produced. Dividing by the mass of an egg m_e therefore gives the number of eggs produced, which when multiplied by the survival fraction s_e , expressing the probability that an egg becomes a recruit, gives the number of recruits. From the number of recruits produced per unit time, we multiply by the mass of a recruit, m_0 , to determine the biomass flux of recruits.

Applying the same form as the stock-recruitment model developed by Beverton and Holt (1957) (see Andersen and Beyer, 2013) we take the overall recruitment $R_k(m_0,t)$ ₁₀ (gwB m⁻² s⁻¹) to be

$$R_k(m_0,t) = R_{P,k}(m_0,t) \frac{R_{e,k}(m_0,t)}{R_{P,k}(m_0,t) + R_{e,k}(m_0,t)}.$$
(29)

Following Andersen and Beyer (2013), we take the half-saturation constant (the value of $R_{e,k}(m_0,t)$ at which the overall recruitment is one half of the maximum recruitment allowed by productivity) to be $R_{P,k}(m_0,t)$. Figure 3 shows how the overall recruitment $R_k(m_0,t)$ ¹⁵ changes as a function of $R_{P,k}(m_0,t)$ and $R_{e,k}(m_0,t)$. As is the case for a Holling Type 2 functional form, as biomass and therefore also the egg- and survival-based recruitment $R_{e,k}(m_0,t)$ increases, the overall recruitment saturates toward the primary production-based limit $R_{P,k}(m_0,t)$. This indicates that for sites with high biomass, NPP limits recruitment. At the other extreme, when $R_{e,k}(m_0,t)$ is small relative to $R_{P,k}(m_0,t)$, the recruitment is approximately linear in $R_{e,k}(m_0,t)$ and so has a weak dependence on $R_{P,k}(m_0,t)$ such that at low biomass the egg production and survival limits recruitment. A summary of

Tables 1 and 2 detail the fish model parameters and variablesis shown in Tables 1 and 2, respectively. The group and mass class structure, and the numerical discretization of the continuous biomass spectrainto mass classes and related assumptions, are presented in Appendix **??**.Sect. 2.9 and Sect. 2.10, respectively.

25

2.8 Environmental forcing: temperature and net primary production

The ecological model requires temperature and NPP information as forcing input to calculate the time evolution of biomass (Eq. 1). These variables can be provided by an ocean general circulation model including a that includes a lower trophic level model. Herewe

- ⁵ take the alternative approach of using observational estimates for the input, we instead use observational estimates, which would be expected to provide a -more realistic simulation. For temperature, we use the World Ocean Atlas 2005 (WOA05) (Locarnini et al., 2006). The WOA05 (Locarnini et al., 2006), which brings together multiple sources of in situ qualitycontrolled temperature data averaged and interpolated to monthly climatologies on a $1^{\circ} \times 1^{\circ}$ arid. We discuss our usage of temperatures in Sect. 2.2
- ¹⁰ grid. We discuss our usage of temperature in Sect. 2.2.

, and as discussed above, use the average water temperature from the upper 75 m of the water column to force temperature-dependent rates. For NPP, we use data products that take satellite measurements of ocean reflectance to estimate chlorophyll a, and that then apply models to estimate NPP. An empirical algorithm first estimates

- the in situ chlorophyll *a* concentration ()from in situ remote sensing reflectance (O'Reily et al., 2000). Large datasets of such in situ data have been developed for this purpose (for example, 2853 in situ observations described in O'Reily et al., 2000). The chlorophyll *a* concentration is fit to take the average of three satellite-based estimates (Behrenfeld and Falkowski, 1997; Carr et al., 2006; Marra et al., 2007) to capture some of
- the variability that exists in different NPP models (Saba et al., 2011). We note that satellite-based estimates suffer from a range of shortcomings, including lack of productivity sources other than phytoplankton (e.g. seagrass and corals), and biases in coastal regions and estuaries (Smyth, 2005; Saba et al., 2011). Although overall minor, these uncertainties will carry through to the modeled biomass and harvest.

25 2.9 Group and mass class structure

Fish span several orders of magnitude in mass, and we therefore discretize the mass spectra into logarithmic mass classes. In order to directly compare our results with the

(30)

Sea Around Us Project (SAUP) harvest database (Watson et al., 2004; Pauly, 2007), we consider three fish groups each with a different asymptotic mass. We first convert the maximum lengths used in the SAUP (30 cm for the small group, 90 cm for medium group, and up to our maximum resolved length for the large group) to asymptotic length assuming

- that the maximum length is 95% of the reflectance using a polynomial function of the maximum of the ratios of certain green to blue and green to green wavelengths. With this resulting polynomial equation for chlorophyll *a* concentration, satellite observations of reflectance (after correcting for the influence of the atmosphere) are used to predict the chlorophyll *a* concentration at global scales. With knowledge of chlorophyll, asymptotic
- ¹⁰ length (Taylor, 1958; Froese and Pauly, 2014), and then apply a length–weight relationship of the form $m = \delta_1 l^{\delta_2}$ (Froese et al., 2013) to calculate the asymptotic mass. This results in asymptotic masses of 0.3 kg, 8.5 kg, and 100 kg for the small, medium, and large groups, respectively.

Although the asymptotic masses differ, all three groups have the same mass class structure, with lower and upper bounds of $m_0 = 10$ g and further information on the photosynthetically-available radiation, sea surface temperature, and mixed-layer depth, models are applied to estimate the column-integrated NPP (Saba et al., 2011) $m_{u_{c}} =$ 100 kg, respectively. Since the ocean color estimates assume that color is due strictly to phytoplankton, we only resolve ecosystems where phytoplankton is the fundamental energy

- ²⁰ resource. This does not pose a problem since non-phytoplankton primary production, such as that from seagrasses and corals, makes up only a small fraction of the total oceanic primary production (Duarte and Chiscano, 1999; Crossland et al., 1991). groups have different asymptotic masses $m_{k,\infty}$, there are therefore fewer resolved mass classes for groups with smaller asymptotic mass. We define the mass classes by dividing the mass
- spectrum into N_M classes with lower bounds $m_{i,L}$ such that

$$m_{i,L} = m_0 \left(\frac{m_u}{m_0}\right)^{\frac{i-1}{N_M}},$$

(31)

where *i* is the index of the mass class that ranges from 1 to N_M . Based on this definition, we describe a mass class as an interval $I_i = [m_{i,L}, m_{i+1,L}]$ of length $\Delta m_i = m_{i+1,L} - m_{i,L}$ $(i = 1, ..., N_M)$. We divide the spectrum into 50 mass classes ($N_M = 50$). Although we use fewer mass classes than some other studies (Maury et al., 2007; Hartvig et al., 2011), we have tested higher temporal and spatial resolutions and find that our interpretations would not be influenced by our choice of temporal or spatial resolution.

Despite the use of large datasets of in situ observations, measurements do not represent all ocean basins appropriately (Claustre, 2003), and chlorophyll *a* estimates are left with a large relative error that ranges from less than 35% over much of the open ocean

to high uncertainty in high chlorophyll regions (Moore et al., 2009). Coastal and river outflow estimates of chlorophyll *a* and NPP are generally overestimated because of the presence of colored dissolved organic matter and suspended particulate matter, since these constituents can be misinterpreted as chlorophyll (Saba et al., 2011; Smyth, 2005). In models that use NPP to determine fish growth and reproduction, such as ours, these uncertainties carry through to the modeled biomass and harvest.

For this study, we use observations collected from the Sea-viewing Wide Field of View Sensor (SeaWiFS) (McClain et al., 2004). As described above, BOATS is forced with monthly climatologies of column-integrated net primary production. Instead of using a particular NPP model, we take the average of three models (Behrenfeld and Falkowski, 1997; Carr et al., 2006; Marra et al., 2007). Using the average isa simple though effective way of capturing some of the uncertainty and bias that exists in different sets of NPP model assumptions When we calculate and present mass-dependent quantities, we consider a mass m_i that represents the average or central value of its class. For this, we apply the geometric mean of the lower and upper bounds of a mass class, which we calculate as

 $\underline{m_i = (m_{i,L}m_{i+1,L})^{1/2}},$

since the upper bound of a mass class is the same as the lower bound of the adjacent class.

2.10 Numerical methods

The biological part of our model is a system of three nonlinear first-order (in mass) partial differential equations that describe the evolution of the biomass spectra of three fish groups. Each equation is forced with the same net primary production and temperature information,

and the equations do not interact with one another. Here, we use the standard notation of a subscript *i* to describe a mass cell, and a superscript *n* to describe a temporal cell. The notation *k*, as in the main text, refers to a fish group. For example, $f_{k,i}^{n+1}$ represents the biomass spectral value *f* of group *k*, at mass class *i* at time n+1.

Since the McKendrick von-Foerster model is an advective equation in biomass, as is true of advective equations, transport errors are a concern (Press et al., 1992). To limit such errors, and because growth is always defined to be positive (or zero), we apply an upwind scheme (Maury et al., 2007; Hartvig et al., 2011). This numerical scheme uses only biomass information that is upwind of the cell of interest; that is, it only uses biomass information at cells *i* and i - 1 to integrate and determine the biomass at cell *i* at the next

timestep. We use a forward difference scheme for the temporal rate of change, and explicitly calculate the growth (γ) and mortality (Λ) rates; that is, we use the current temporal state of biomass $f_{k,i}^n$ to update the biomass, as opposed to using the future biomass state $f_{k,i}^{n+1}$ as in an implicit scheme, and integrate biomass as

$$f_{k,i}^{n+1} = f_{k,i}^{n} + \left[-\left(\frac{\gamma_{k,i}^{n} f_{k,i}^{n} - \gamma_{k,i-1}^{n} f_{k,i-1}^{n}}{\Delta m_{i}}\right) + \frac{\gamma_{k,i}^{n} f_{k,i}^{n}}{m_{i}} - \Lambda_{k,i}^{n} f_{k,i}^{n}\right] \Delta t.$$
(32)

²⁰ The model is stable and converges as we decrease Δt .

3 Results and discussion

Here we describe the behaviour of the fish ecology model, and make use of a -simplified version of the model as a -reference point and initial biomass condition. We consider two model grid points that correspond to individual patches of ocean at a -cold-water site in the East

Bering Sea (EBS) LME (64° N, 165° W) and a –warm-water site in the Benguela Current (BC) LME site (20° S,12° E), and describe the resulting biomass spectra and other model variables. However, we do not use these sites for a thorough data-based model validation, which is difficult at this time due to a lack of suitable fish biomass data. Beyond the validation

to harvest at the LME-scale in the companion paper (Carozza et al., 2016), more specific validation could be done in the future with suitable datasets when they become available (that is, size aggregated, regional-scale, species-comprehensive biomass assessments).

We then We discuss the results from a -sensitivity test that considers the role of NPP (ranging from 50 to 2000 mg C m⁻² d⁻¹) and temperature (ranging from −2 to 30 °C) on biomass. For these simulations, we use a 15 day 15 day timestep and constant forcing of annually-averaged NPP and temperature.

We do not use these sites for a thorough data-based model validation, which is difficult at this time due to a lack of suitable fish biomass data. The parameter values used here are taken from an extensive data-model comparison using that employs the global im-

- plementation of the model, in which a and is fully described in the companion paper (Carozza et al., 2016). In that study, we take a Monte Carlo approach is used with over 10,000 parameter sets to find parameter combinations that best fit observed harvests within the harvest at the LME-scale, considering the full range of the uncertain parameter space for the 13 most important parameters. Of these 13 parameters, 2 are economic,
- with the remaining 11 ecological parameters being identified with a dagger symbol in Table 1. Beyond the validation to harvest at the LME-scale in the companion paper, more specific validation could be done in the future with suitable datasets when they become available (that is, size aggregated, regional-scale, as described in the companion paper (Carozza et al., 2016species-comprehensive biomass assessments).

25 3.1 Initial biomass state

To begin our results and analysis section, we make a series of simplifying assumptions in order to derive an analytical biomass spectrum $f_{k,m,0}$, which we use as a reference point for evaluating aspects of the full model. Since this analytical biomass state is a reason-

able approximation of the full model, we also use it as an initial biomass condition for our simulations. Beginning with the evolution of biomass in Eq. (1), we assume that the input energy expressed in Eq. (7) is solely controlled by NPP, so that $\xi_{I,k}(m,t) = \xi_{P,k}(m,t) = \phi_{\pi,k}\pi(m,t)m/f_k(m,t)\xi_{I,k}(m,t) = \xi_{P,k}(m,t) = \phi_{C,k}\pi(m,t)m/f_k(m,t)\xi_{L,k}(m,t) = \xi_{P,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)\xi_{L,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)\xi_{L,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)g_{L,k}(m,t) = \xi_{P,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)g_{L,k}(m,t) = \xi_{P,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)g_{L,k}(m,t) = \xi_{P,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)g_{L,k}(m,t)g_{L,k}(m,t) = \xi_{P,k}(m,t)m/f_k(m,t)g_{L,k}$ that there is no allocation of energy to reproduction, SO that and $\Phi_k(m) = 0.$ These assumptions growth of two result in rate а $\gamma_k(m,t) = \phi_{\pi,k}\pi(m,t)m/f_k(m,t)\gamma_{S,k}(m,t) = \phi_{C,k}\pi(m,t)m/f_k(m,t), \text{ which allows us}$ to calculate the equilibrium biomass spectrum ($\frac{\partial}{\partial t}f_k(m,t)=0$) in terms of the fish production spectrum (Eq. 24) and the mortality rate (Eq. 26). We consider constant forcing and so 10 apply the annual average NPP $\overline{\Pi}_{\psi}$ and temperature (which are contained in the mortality rate λ and representative phytoplankton mass m_{ψ} terms), and find that the equilibrium biomass spectrum of each each group is

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$$f_{k,m,0} = \frac{\phi_{\pi,k} \overline{\Pi}_{\psi} (1-\tau)}{\lambda m_{\psi}^{\tau} m_{\infty,k}^{h+b-1}} \frac{\phi_{C,k} \overline{\Pi}_{\psi} (1-\tau)}{\lambda m_{\psi}^{\tau} m_{\infty,k}^{h+b-1}} m^{\tau+h-1}.$$
(33)

As expected from the MVF model, biomass follows a power law spectrum with respect to 15 mass. Given that the power law scaling exponent is $\tau + h - 1$, biomass scales as a function of the trophic and mortality scalings, which we assume are constant. On the other hand, the intercept of the spectrum (in logarithmic space, when $m = 1m = m_0 = 10$ g) depends on a variety of parameters such as the NPP and trophic efficiency, as well as the natural mortality rate and the representative phytoplankton mass. Unlike the mass scaling, the 20 intercept is also group dependent through the fraction of primary production allocated to each group and the asymptotic mass.

Biomass equilibrium 3.2

As in other studies, we use features of the modeled biomass spectra, shown in Fig. 4, to interpret the model results. Work on marine ecosystems indicates that biomass spectra, 25

when plotted in log-log space, are approximately linear over most of the size range and have slopes that range from -1.0 to -1.2 (Blueweiss et al., 1978; Brown et al., 2004; Marguet et al., 2005; White et al., 2007). Ignoring harvest, group biomass spectra generally decrease with size, except at the maturity mass at which energy begins to be allocated to reproduction (Fig. 2), where there is a decrease in the growth rate and so an accumulation 5 of biomass that may result in a local maximum or a local decrease of the spectrum slope (Andersen and Beyer, 2013). As expected from Eq. (33), the group intercepts differ, but by little since in our formulation the only difference arises from the weak asymptotic mass dependence $m_{\infty,k}^{h+b-1}$ in the mortality term. Biomass is larger at the cold-water site, despite

it having a lower NPP (Fig. 5). In particular, large group biomass is larger at the cold-water 10 site, which is consistent with the findings of Watson et al. (2014).

There is a nonlinear decrease in biomass at larger mass classes (Fig. 4). The shape of the biomass spectra are determined from the growth and mortality rates. Since the growth rate consists of NPP and allometric regimes (Eq. 22), and the mortality rate of a single

regime (Eq. 26), any changes in the shape of the biomass spectra are determined by the 15 growth rate. We generally find that the NPP regime (Eq. 8) limits energy input in smaller mass classes, whereas the allometric regime (Eq. 10) plays the limiting role in the largest mass classes.

Sensitivity tests 3.3

- Total biomass (Fig. 5a) increases monotonically for increasing NPP, yet decreases 20 monotonically for increasing temperature. Increasing temperature not only reduces the primary-production-based growth rate $\gamma_{\rm P}$ by reducing the representative phytoplankton size (Eq. 24), it also significantly drives up the mortality rate, generating a clear pattern of reduced biomass. Under the allometric regime of growth (Eq. 10), higher temperature implies
- a greater growth rate, which on its own results in an increase in biomass (not shown). How-25 ever, this feature is more than counterbalanced by the mortality rate increase, which results in an overall lower biomass for higher temperature.

We calculate the total biomass spectrum as the sum of the biomass of each mass class over all groups. We use the biomass value at the first mass class to define the intercept, and calculate the slopes based on the non-reproducing nonreproducing parts of the spectra (the mass classes that are smaller than the maturity mass $m_{\alpha,k}$) since this is generally the

- ⁵ linear part of the spectra (Maury and Poggiale, 2013), using linear regression on the logtransformed data (Xiao et al., 2011). The spectral intercept (Fig. 5b) depends on both NPP and temperature, monotonically increasing with increasing NPP, but nonlinearly changing in temperature due to the multiple sources of temperature dependence in the intercept (Eq. 33). The biomass slope does not depend on NPP (Fig. 5c), as indicated in Eq. (33),
- and the resulting total slope values (black-grey curve in Fig. 5c), given the parameters used in this single realization of the model, are consistent with published values from marine ecosystems that range from -1.0 to -1.2 (Blueweiss et al., 1978; Brown et al., 2004; Marquet et al., 2005; White et al., 2007). ThoughHowever, we find flatter slopes for lower temperatures, to values as low as -0.9. This implies that our model would result in gener-
- ally higher biomass than if the slope of the spectra fell between -1 and -1.2. Equation (33) also indicates that the slope is not a function of temperature. That equation applies for the small group (blue curve in Fig. 5c) over all temperatures, and for the medium group at low temperatures. However, when the input energy is determined by the von Bertalanffy limit, as is the case for high temperatures in the medium group and all temperatures for
 the large group, a rise in temperature steepens the biomass slope. Overall, NPP only influored applies to a prostra by chifting the intercent whereas temperature beth chifts the intercent and
- ences spectra by shifting the intercept, whereas temperature both shifts the intercept and changes the slopes of biomass spectra when the input energy is set by the von Bertalanffy limit.

The model illustrates hypothetical inferences, based on the macroecological theory it uses, that would be interesting to check against realityneed to be compared to suitable observations. Further validation of the model at specific locations and at the size-class level of detail remains a challenge because of the scarcity of suitable datasets. To further validate BOATS and comparable models, we require size-class-resolved observations at the ecosystem level, at a high enough resolution to detect variations in spectral properties, and

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at a sufficient number of sites so as to detect bulk variations due to different temperature and NPP. This type of detail at the ecosystem level is not available even in current stock assessment databases, and it should be considered an important target for future data syntheses.

5 4 Conclusions

10

We have described a new marine upper trophic level model for use in gridded, global ocean models. The model as described here is used as the ecological module of the BOATS model, designed to study the global fishery. In a companion paper, we discuss the economic module of the BOATS model and complete the model evaluation by comparing harvest simulations to global harvest observations. The approach could be readily adapted to other purposes, such as for use in studies of ocean biogeochemistry or ecology.

The model uses NPP and temperature to represent the first-order features of fish biomass using fundamental marine biogeochemical and ecological concepts. We When possible, we apply empirical relationships with mechanistic underpinnings to simplify complex and often

- ¹⁵ unconstrainable ecological processes when possible cological processes that are difficult to constrain. Phytoplankton community structure is represented by the proportion of large phytoplankton. Fish growth rates are determined by a parameterized trophic transfer of energy from primary production, but limited by empirical allometric estimates. The natural mortality rate is based on an empirical relationship that depends on the individual and
- asymptotic mass, and reproduction depends on the NPP and the fish biomass of reproductive age. The resulting biomass spectra, as defined here, include all commercially-harvested organisms longer than approximately 10 cm (greater than 10 g).

We presented simulated biomass spectra at a warm- and a cold-water site, and performed a sensitivity test of the model forcing variables to examine key model variables. ²⁵ We find that the structure of modeled biomass spectra is broadly consistent with observations, and biomass slopes match observations over a wide range of NPP and temperature. Although the model employs a limited number of parameters compared to similar model-

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ing efforts, it retains reasonably realistic representations of biological and ecological processes, and is computationally efficient, which allows for extensive sensitivity studies and parameter-space analyses even when implemented globally. Due to its dynamical generality and conceptual simplicity, the ecological module of BOATS is well-suited for global-scale studies where the resolution of species or functional-groups is not necessary.

Appendix A: Biomass version of the McKendrick-von Foerster (MVF) model

The MVF model equation is an expression of the conservation of the number of fish (Kot, 2001), and in terms of abundance is written as

$$\frac{\partial}{\partial t}n(m,t) = -\frac{\partial}{\partial m}\gamma(m,t)n(m,t) - \Lambda(m,t)n(m,t),$$
(A1)

where $\gamma(m,t)$ is a characteristic velocity of growth (Kot, 2001), which we assume is equivalent to the individual growth rate $\frac{dm}{dt}$, and $\Lambda(m,t)$ is the instantaneous natural mortality rate. For ease of reading, we ignore the mass and time dependencies and write f = f(m, t), $\gamma = \gamma(m,t), \Lambda = \Lambda(m,t), \text{ and } n = n(m,t).$ The biomass spectrum f(m,t) is defined as n(m,t)m, and so n(m,t) = f(m,t)/m. Substituting this expression into Eq. (A1), we have that 15

$$\frac{\partial}{\partial t}(f/m) = -\frac{\partial}{\partial m}[\gamma(f/m)] - \Lambda(f/m), \tag{A2}$$

which simplifies to

5

$$\frac{1}{m}\frac{\partial f}{\partial t} = -\left[\frac{\partial}{\partial m}\left(\frac{f}{m}\right)\right]\gamma - \left[\frac{\partial\gamma}{\partial m}\right]\frac{f}{m} - \Lambda\frac{f}{m}.$$
(A3)

36

Multiplying through by m and simplifying, we find that

m

$${}_{20} \quad \frac{\partial f}{\partial t} = -\left[\frac{\partial f}{\partial m} - \frac{f}{m}\right]\gamma - \left[\frac{\partial \gamma}{\partial m}\right]f - \Lambda f \tag{A4}$$
$$= -\frac{\partial}{\partial m}[\gamma f] + \frac{\gamma f}{m} - \Lambda f. \tag{A5}$$

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This result is similar in structure to its abundance-based counterpart in Eq. (A1), aside from the extra term $\frac{\gamma f}{m} \frac{\gamma f}{m}$, which is equivalent to γn . This new term is a direct consequence of the conservation of the number of fish written in terms of biomass, and represents the increase in biomass that occurs as a given number of fish grow into a larger mass interval at the rate γ .

Appendix B: Derivation of natural mortality formulation

5

We apply the empirical model of natural mortality from Gislason et al. (2010) to derive Eq. (26). The natural mortality rate is model 2 of Table 1 from Gislason et al. (2010),

$$\operatorname{Ln}(\Lambda) = \zeta_1 + \zeta_2 \operatorname{Ln}(l) + \zeta_3 \operatorname{Ln}(l_{\infty}) + \operatorname{Ln}(K) - \frac{\zeta_4}{T}, \tag{B1}$$

¹⁰ where Λ is the natural mortality rate, l is the organism length, l_{∞} is the asymptotic organism length, K is the von Bertalanffy growth parameter that is equivalent to $\frac{A}{3}m_{\infty}^{b-1}$, and T is temperature. The variable $A = A_0 a_{\lambda}(T)$ is the growth constant A_0 scaled by the van't Hoff– Arrhenius exponential function for mortality, and b is the allometric scaling constant (Eq. 10). Gislason et al. (2010) found that the ζ_4 parameter was not statistically significant, and so we rewrite the natural mortality rate ignoring the temperature term as

$$\Lambda = e^{\zeta_1} l^{\zeta_2} l_{\infty}^{\zeta_3} K. \tag{B2}$$

We apply the length–weight relationship $l = (m/\delta_1)^{1/\delta_2}$ taking $\delta_2 = 3$ (Froese et al., 2013) to write the equation in terms of mass, and find that

$$\Lambda = e^{\zeta_1} \left(\frac{m}{\delta_1}\right)^{\zeta_2/3} \left(\frac{m_\infty}{\delta_1}\right)^{\zeta_3/3} \frac{A}{3} m_\infty^{b-1}.$$
(B3)

²⁰ Based on the statistical estimates of ζ_2 and ζ_3 made by Gislason et al. (2010), and as in Charnov et al. (2012), we assume that $\zeta_3 = -\zeta_2$. By then writing $-\zeta_2/3$ as *h* and cancelling

(B4)

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the δ_1 , we have that

$$\Lambda = \lambda(T)m^{-h}m_{\infty}^{h+b-1} \equiv \frac{e^{\zeta_1}A_0a_{\lambda}(T)}{3}m^{-h}m_{\infty}^{h+b-1}$$

Appendix C: Numerical methods

The biological part of our model is a system of three nonlinear first-order (in mass) partial

⁵ differential equations that describe the evolution of the biomass spectra of three fish groups. Each equation is forced with the same net primary production and temperature information, and the equations do not interact with one another. Here, we use the standard notation of a subscript *i* to describe a mass cell, and a superscript *n* to describe a temporal cell. The notation *k*, as in the main text, refers to a fish group. For example, $f_{k,i}^{n+1}$ represents the biomass spectral value *f* of group *k*, at mass class *i* at time n + 1.

Since the McKendrick von-Foerster model is an advective equation in biomass, as is true of advective equations, transport errors are a concern (Press et al., 1992). To limit such errors, and because growth is always defined to be positive (or zero), we apply an upwind scheme (Maury et al., 2007; Hartvig et al., 2011). This numerical scheme uses only

- ¹⁵ biomass information that is upwind of the cell of interest; that is, it only uses biomass information at cells *i* and *i* – 1 to integrate and determine the biomass at cell *i* at the next timestep. We use a forward difference scheme for the temporal rate of change, and explicitly calculate the growth (γ) and mortality (A) rates; that is, we use the current temporal state of biomass $f_{k,i}^n$ to update the biomass, as opposed to using the future biomass state $f_{k,i}^{n+1}$ as in an implicit achemic, and integrate biomass as
- ²⁰ in an implicit scheme, and integrate biomass as

$$f_{k,i}^{n+1} = f_{k,i}^{n} + \left[-\left(\frac{\gamma_{k,i}^{n} f_{k,i}^{n} - \gamma_{k,i-1}^{n} f_{k,i-1}^{n}}{\Delta m_{i}}\right) + \frac{\gamma_{k,i}^{n} f_{k,i}^{n}}{m_{i}} - \Lambda_{k,i}^{n} f_{k,i}^{n} \right] \Delta t$$

The model is stable and converges as we decrease Δt and Δm_i .

B1 Group and mass class structure

Fish span several orders of magnitude in mass. We therefore discretize the mass spectra into logarithmic mass classes. We consider three groups of fish with different asymptotic mass. We first convert maximum lengths used in the SAUP (30 for the small group, 90 for medium group, and up to our maximum resolved length for the large group) to asymptotic length assuming that the maximum length is 95% of the asymptotic length

asymptotic length assuming that the maximum length is 95% of the asymptotic length (Taylor, 1958; Froese and Pauly, 2014), and then use a length–weight relationship of the form $l = (m/\delta_1)^{1/\delta_2}$ (Froese et al., 2013) to calculate the asymptotic mass.

Although the asymptotic masses differ, all three groups have the same mass class structure, with lower and upper bounds of $m_0 = 10$ and $m_u = 100$, respectively. Since the groups have different asymptotic masses $m_{k,\infty}$, there are therefore fewer resolved mass classes for groups with smaller asymptotic mass. We define the mass classes by dividing the mass spectrum into N_M classes with lower bounds $m_{i,L}$ such that

$$m_{i,L} = m_0 \left(\frac{m_u}{m_0}\right)^{\frac{i-1}{N_M}},$$

where i is the index of the mass class that ranges from 1 to N_M . Based on this definition,

- we describe a mass class as an interval $I_i = [m_{i,L}, m_{i+1,L}]$ of length $\Delta m_i = m_{i+1,L} m_{i,L}$ ($i = 1, ..., N_M$). We divide the spectrum into 50 mass classes ($N_M = 50$). Although we use fewer mass classes than in other studies (Maury et al., 2007; Hartvig et al., 2011), we have tested higher temporal and spatial resolutions and find that our interpretations would not be influenced by our choice of temporal or spatial resolution.
- When we calculate and present mass-dependent quantities, we consider a mass m_i that represents the average or central value of its class. For this, we apply the geometric mean of the lower and upper bounds of a mass class, which we calculate as

 $\underline{m_i = (m_{i,L}m_{i+1,L})^{1/2}},$

since the upper bound of a mass class is the same as the lower bound of the adjacent class.

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Code availability

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BOATS was written in MATLAB version R2012a (MATLAB, 2012), and was also tested in version R2010b. The zero-dimensional version of BOATS (for a single patch of ocean, that is, a single site), which includes the model run script, required functions, and forcing data, is available for download at doi:10.5281/zenodo.27700.

Author contributions. D. A. Carozza designed the model in collaboration with D. Bianchi and E. D. Galbraith. D. A. Carozza and D. Bianchi developed the model code and D. A. Carozza performed the simulations and analysis. D. A. Carozza wrote the manuscript and prepared the figures and tables with comments from co-authors.

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References

- Agawin, N. S., Duarte, C. M., and Agusti, S.: Nutrient and temperature control of the contribution of picoplankton to phytoplankton biomass and production, Limnol. Oceanogr., 45, 591–600, doi:10.4319/lo.2000.45.3.0591, 2000.
- ²⁵ Andersen, K. H. and Beyer, J. E.: Asymptotic size determines species abundance in the marine size spectrum, Am. Nat., 168, 54–61, doi:10.1086/504849, 2006.
 - Andersen, K. H. and Beyer, J. E.: Size structure, not metabolic scaling rules, determines fisheries reference points, Fish Fish., 16, 1–22, doi:10.1111/faf.12042, 2013.

- Andersen, K. H. and Pedersen, M.: Damped trophic cascades driven by fishing in model marine ecosystems, P. Roy. Soc. B-Biol. Sci., 277, 795–802, doi:10.1098/rspb.2009.1512, 2010.
 Arrhenius, S. A.: Über die Reaktionsgeschwindigkeit bei der Inversion von Rohrzucker durch Säuren, Z. Phys. Chem., 4, 226–248, 1889.
- ⁵ Barange, M., Merino, G., Blanchard, J., Scholtens, J., Harle, J., Allison, E. H., Allen, J. I., Holt, J., and Jennings, S.: Impacts of climate change on marine ecosystem production in societies dependent on fisheries, Nature Climate Change, 4, 211–216, doi:10.1038/NCLIMATE2119, 2014.
 - Barnes, C., Maxwell, D., Reuman, D. C., and Jennings, S.: Global patterns in predator-prey size relationships reveal size dependency of trophic transfer efficiency, Ecology, 91, 222–232,
- ¹⁰ doi:10.1890/08-2061.1, 2010.
 - Behrenfeld, M. J. and Falkowski, P. G.: Photosynthetic rates derived from satellite-based chlorophyll concentration, Limnol. Oceanogr., 42, 1–20, doi:10.4319/lo.1997.42.1.0001, 1997.
 - Beverton, R. J. H.: Patterns of reproductive strategy parameters in some marine teleost fishes, J. Fish Biol., 41, 137–160, doi:10.1111/j.1095-8649.1992.tb03875.x, 1992.
- Beverton, R. J. H. and Holt, S. J.: On the Dynamics of Exploited Fish Populations, Springer Science+Business Media Inc., Dordrecht, 1957.
 - Bissinger, J. E., Montagnes, D. J., Sharples, J., and Atkinson, D.: Predicting marine phytoplankton maximum growth rates from temperature: Improving on the Eppley curve using quantile regression, Limnol. Oceanogr., 53, 487–493, doi:10.4319/lo.2008.53.2.0487, 2008.
- Blanchard, J. L., Jennings, S., Law, R., Castle, M. D., McCloghrie, P., Rochet, M.-J., and Benoît, E.: How does abundance scale with body size in coupled size-structured food webs?, J. Anim. Ecol., 78, 270–280, doi:10.1111/j.1365-2656.2008.01466.x, 2009.
 - Blanchard, J. L., Jennings, S., Holmes, R., Harle, J., Merino, G., Allen, J. I., Holt, J., Dulvy, N. K., and Barange, M.: Potential consequences of climate change for primary production and fish
- 25 production in large marine ecosystems, Philos. T. R. Soc. B-Biol. Sci., 367, 2979–2989, doi:10.1098/rstb.2012.0231, 2012.
 - Blueweiss, L., Fox, H., Kudzma, V., Nakashima, D., Peters, R., and Sams, S.: Relationships between body size and some life history parameters, Oecologia, 37, 257–272, doi:10.1007/BF00344996, 1978.
- Boltzmann, L.: Weitere Studien über das Wärmegleichgewicht unter Gasmolekülen, Sitzungsberichte der Mathematisch-Naturwissenschaftlichen Classe der Kaiserlichen Akademie der Wissenschaften Wien, 66, 275–370, 1872.

Discussion Paper

- Bopp, L., Resplandy, L., Orr, J. C., Doney, S. C., Dunne, J. P., Gehlen, M., Halloran, P., Heinze, C., Ilyina, T., Séférian, R., Tjiputra, J., and Vichi, M.: Multiple stressors of ocean ecosystems in the 21st century: projections with CMIP5 models, Biogeosciences, 10, 6225–6245, doi:10.5194/bg-10-6225-2013, 2013.
- ⁵ Branch, T. A., Jensen, O., Ricard, D., YE, Y., and Hilborn, R.: Contrasting global trends in marine fishery status obtained from catches and from stock assessments, Conserv. Biol., 25, 777–786, doi:10.1111/j.1523-1739.2011.01687.x, 2011.
 - Brander, K.: Impacts of climate change on fisheries, J. Marine Syst., 79, 389–402, doi:10.1016/j.jmarsys.2008.12.015, 2010.
- Brown, J., Gillooly, J., Allen, A., Savage, V., and West, G.: Toward a metabolic theory of ecology, Ecology, 85, 1771–1789, doi:10.1890/03-9000, 2004.
 - Carozza, D. A., Bianchi, D., and Galbraith, E. D.: BOATS: A bioenergetically-constrained coupled fisheries ecology and economics model for global studies of harvest and climate change, Fish and Fisheries, under review, 2015. 2016.
- ¹⁵ Carr, M.-E., Friedrichs, M. A. M., Schmeltz, M., Noguchi Aita, M., Antoine, D., Arrigo, K. R., Asanuma, I., Aumont, O., Barber, R., Behrenfeld, M., Bidigare, R., Buitenhuis, E. T., Campbell, J., Ciotti, A., Dierssen, H., Dowell, M., Dunne, J., Esaias, W., Gentili, B., Gregg, W., Groom, S., Hoepffner, N., Ishizaka, J., Kameda, T., Le Quéré, C., Lohrenz, S., Marra, J., Mélin, F., Moore, K., Morel, A., Reddy, T. E., Ryan, J., Scardi, M., Smyth, T., Turpie, K., Tilstone, G., Waters, K., and
- ²⁰ Yamanaka, Y.: A comparison of global estimates of marine primary production from ocean color, Deep-Sea Res. Pt. II, 53, 741–770, doi:10.1016/j.dsr2.2006.01.028, 2006.
 - Charnov, E. L., Gislason, H., and Pope, J. G.: Evolutionary assembly rules for fish life histories, Fish Fish., 14, 213–224, doi:10.1111/j.1467-2979.2012.00467.x, 2012.

Chassot, E., Bonhommeau, S., and Dulvy, N.: Global marine primary production constrains fisheries catches, Ecol. Lett., 13, 495–505, doi:10.1111/j.1461-0248.2010.01443.x, 2010.

Chen, Y., Jackson, D. A., and Harvey, H. H.: A comparison of von bertalanffy and polynomial functions in modelling fish growth data, Can. J. Fish. Aquat. Sci., 49, 1228–1235, doi:10.1139/f92-138, 1992.

25

30

Chesson, P.: Mechanisms of maintenance of species diversity, Annu. Rev. Ecol. Syst., 31, 343–366, doi:10.1146/annurev.ecolsys.31.1.343, 2000.

Cheung, W. W. L., Lam, V. W. Y., Sarmiento, J. L., Kearney, K., Watson, R., Zeller, D., and Pauly, D.: Large-scale redistribution of maximum fisheries catch potential in the global ocean under climate change, Glob. Change Biol., 16, 24–35, doi:10.1111/j.1365-2486.2009.01995.x, 2010.

42

Christensen, V., Coll, M., Buszowski, J., Cheung, W. W., L., Frölicher, T., Steenbeek, J., Stock, C., A., Watson, R., A., Walters, C., J.: The global ocean is an ecosystem: simulating marine life and fisheries, Global Ecology and Biogeography., 24, 5, 507–517, doi:10.1111/geb.12281, 2015.

- Clarke, A.: Costs and consequences of evolutionary temperature adaptation, Trends Ecol. Evol., 18, 573–581, doi:10.1016/j.tree.2003.08.007, 2003.
- Clarke, A.: Is there a universal temperature dependence of metabolism?, Funct. Ecol., 18, 252–256, doi:10.1111/j.0269-8463.2004.00842.x, 2004.

Claustre, H.: The many shades of ocean blue, Science, 302, 1514–1515, doi:10.1126/science.1092704, 2003.

- ¹⁰ Crossland, C. J., Hatcher, B. G., and Smith, S. V.: Role of coral reefs in global ocean production, Coral Reefs, 10, 55–64, doi:10.1007/BF00571824, 1991.
 - Cury, P. and Pauly, D.: Patterns and propensities in reproduction and growth of marine fishes, Ecol. Res., 15, 101–106, doi:10.1046/j.1440-1703.2000.00321.x, 2000.

Dahlberg, M. D.: A review of survival rates of fish eggs and larvae in relation to impact assessments,

¹⁵ Mar. Fish. Rev., 41, 1–12, 1979.

5

Datta, S., Delius, G. W., and Law, R.: A jump-growth model for predator–prey dynamics: derivation and application to marine ecosystems, B. Math. Biol., 72, 1361–1382, doi:10.1007/s11538-009-9496-5, 2010.

Denman, K. L. and Pena, M. A.: The response of two coupled one-dimensional mixed

layer/planktonic ecosystem models to climate change in the NE subarctic Pacific Ocean, Deep-Sea Res. Pt. II, 49, 5739–5757, doi:10.1016/S0967-0645(02)00212-6, 2002.

Deriso, R. B.: Harvesting strategies and parameter estimation for an age-structured model, Can. J. Fish. Aquat. Sci., 37, 268–282, doi:10.1139/f80-034, 1980.

Doney, S. C., Ruckelshaus, M., Emmett Duffy, J., Barry, J. P., Chan, F., English, C. A., Galindo, H. M.,

Grebmeier, J. M., Hollowed, A. B., Knowlton, N., Polovina, J., Rabalais, N. N., Sydeman, W. J., and Talley, L. D.: Climate change impacts on marine ecosystems, Annual Review of Marine Science, 4, 11–37, doi:10.1146/annurev-marine-041911-111611, 2012.

Duarte, C. M. and Alcaraz, M.: To produce many small or few large eggs: a size-independent reproductive tactic of fish, Oecologia, 80, 401–404, doi:10.1007/BF00379043, 1989.

³⁰ Duarte, C. M. and Chiscano, C. L.: Seagrass biomass and production: a reassessment, Aquat. Bot., 65, 159–174, doi:10.1016/S0304-3770(99)00038-8, 1999.

Dueri, S., Faugeras, B., and Maury, O.: Modelling the skipjack tuna dynamics in the Indian Ocean with APECOSM-E: Part 1. Model formulation, Ecol. Model., 245, 41–54, doi:10.1016/j.ecolmodel.2012.02.007, 2012.

Dunne, J., Armstrong, R., Gnanadesikan, A., and Sarmiento, J.: Empirical and mechanistic models

- for the particle export ratio, Global Biogeochem. Cy., 19, GB4026, doi:10.1029/2004GB002390, 2005.
 - Duplisea, D. E., Jennings, S., Warr, K. J., and Dinmore, T. A.: A size-based model of the impacts of bottom trawling on benthic community structure, Can. J. Fish. Aquat. Sci., 59, 1785–1795, doi:10.1139/F02-148, 2002.
- Ernest, S. K. M., Enquist, B. J., Brown, J. H., Charnov, E. L., Gillooly, J. F., Savage, V. M., White, E. P., Smith, F. A., Hadly, E. A., Haskell, J. P., Lyons, S. K., Maurer, B. A., Niklas, K. J., and Tiffney, B.: Thermodynamic and metabolic effects on the scaling of production and population energy use, Ecol. Lett., 6, 990–995, doi:10.1046/j.1461-0248.2003.00526.x, 2003.

FAO: The State of World Fisheries and Aquaculture: Opportunities and Challenges, Rome, Italy, 2014.

- Faugeras, B. and Maury, O.: A multi-region nonlinear age-size structured fish population model, Nonlinear Anal.-Real, 6, 447–460, 2005.
- Freedman, J. A. and Noakes, D. L. G.: Why are there no really big bony fishes? A point-of-view on maximum body size in teleosts and elasmobranchs, Rev. Fish Biol. Fisher., 12, 403–416,
- ²⁰ doi:10.1023/A:1025365210414, 2002.

15

Friedland, K. D., Stock, C., Drinkwater, K. F., Link, J. S., Leaf, R. T., Shank, B. V., Rose, J. M., Pilskaln, C. H., and Fogarty, M. J.: Pathways between Primary Production and Fisheries Yields of Large Marine Ecosystems, PLoS ONE, 7, e28945, doi:10.1371/journal.pone.0028945, 2012.

Froese, R. and Pauly, D.: Fishbase, World Wide Web electronic publication, available at: www. fishbase.org (last access: 31 July 2015), version (11/2014), 2014.

- Froese, R., Thorson, J. T., and Reyes Jr., R. B.: A Bayesian approach for estimating length-weight relationships in fishes, J. Appl. Ichthyol., 30, 78–85, doi:10.1111/jai.12299, 2013.
- Gislason, H., Daan, N., Rice, J. C., and Pope, J. G.: Size, growth, temperature and the natural mortality of marine fish, Fish Fish., 11, 149–158, doi:10.1111/j.1467-2979.2009.00350.x, 2010.
- Hartvig, M., Andersen, K. H., and Beyer, J. E.: Food web framework for size-structured populations, J. Theor. Biol., 272, 113–122, doi:10.1016/j.jtbi.2010.12.006, 2011.
 - Hessen, D. O. and Kaartvedt, S.: Top–down cascades in lakes and oceans: different perspectives but same story?, J. Plankton Res., 36, 914–924, doi:10.1093/plankt/fbu040, 2014.

44

- Holling, C. S.: Some characteristics of simple types of predation and parasitism, Can. Entomol., 91, 385–398, doi:10.4039/Ent91385-7, 1959.
- Hutchings, J. A., Minto, C., Ricard, D., Baum, J. K., and Jensen, O. P.: Trends in the abundance of marine fishes, Can. J. Fish. Aquat. Sci., 67, 1205–1210, doi:10.1139/F10-081, 2010.
- Irigoien, X., Klevjer, T. A., Røstad, A., Martinez, U., Boyra, G., Acuña, J. L., Bode, A., Echevarria, F., Gonzalez-Gordillo, J. I., Hernandez-Leon, S., Agusti, S., Aksnes, D. L., Duarte, C. M., and Kaartvedt, S.: Large mesopelagic fishes biomass and trophic efficiency in the open ocean, Nature Communications, 5, 3271, doi:10.1038/ncomms4271, 2014.
 - Jackson, J. B. C.: Historical overfishing and the recent collapse of coastal ecosystems, Science, 293, 629–637, doi:10.1126/science.1059199, 2001.
- Jennings, S., Mélin, F., Blanchard, J. L., Forster, R. M., Dulvy, N. K., and Wilson, R. W.: Global-scale predictions of community and ecosystem properties from simple ecological theory, P. Roy. Soc. B-Biol. Sci., 275, 1375–1383, doi:10.1098/rspb.2008.0192, 2008.

Jennings, S., Collingridge, K.: Predicting Consumer Biomass, Size-Structure, Production, Catch

- Potential, Responses to Fishing and Associated Uncertainties in the World's Marine Ecosystems, PLoS ONE, 10, 7, e0133794, doi:10.1371/journal.pone.0133794, 2015.
 - Kendall Jr., A. W., Alstrom, E. H., and Moser, H. G.: Early life history stages of fishes and their characters, in: Ontogeny and Systematics of Fishes, edited by: Moser, H. G., The American Society of Ichthyologists and Herpetologists, Lawrence, KS, USA, 11–22, 1984.
- Kooijmann, S. A. L. M.: Dynamic Energy Mass Budgets in Biological Systems, Cambridge University Press, Cambridge, doi:10.1017/CBO9780511565403, 2000.

Kot, M.: Elements of Mathematical Ecology, Cambridge University Press, Cambridge, 2001.

²⁵ 54, 113–121, doi:10.1139/f96-159, 1997.

10

Lefort, S., Aumont, O., Bopp, L., Arsouze, T., Gehlen, M., and Maury, O.: Spatial and body-size dependent response of marine pelagic communities to projected global climate change, Glob. Change Biol., 21, 154–164, doi:10.1111/gcb.12679, 2014.

Lester, N. P., Shuter, B. J., and Abrams, P. A.: Interpreting the von Bertalanffy model of so-

³⁰ matic growth in fishes: the cost of reproduction, P. Roy. Soc. B-Biol. Sci., 271, 1625–1631, doi:10.1098/rspb.2004.2778, 2004.

- Locarnini, R. A., Mishonov, A. V., Antonov, J. I., Boyer, T. P., Garcia, H. E., and Levitus, S. (eds.): World Ocean Atlas 2005, volume 1: Temperature, NOAA Atlas NESDIS 61, US Gov. Printing Office, Washington, DC, USA, 2006.
- Maranón, E.: Cell size as a key determinant of phytoplankton metabolism and community structure,
- 5 Annual Review of Marine Science, 7, 241–264, doi:10.1146/annurev-marine-010814-015955, 2015.
 - Marquet, P. A., Quiñones, R. A., Abades, S., Labra, F., Tognelli, M., Arim, M., and Rivadeneira, M.: Scaling and power-laws in ecological systems, J. Exp. Biol., 208, 1749–1769, 2005.
 - Marra, J., Trees, C. C., and O'Reilly, J. E.: Phytoplankton pigment absorption: a strong pre-
- dictor of primary productivity in the surface ocean, Deep-Sea Res. Pt. I, 54, 155–163, doi:10.1016/j.dsr.2006.12.001, 2007.
 - MATLAB: version 7.14.0.739 (R2012a), The MathWorks Inc., Natick, MA, 2012.
 - Maury, O.: An overview of APECOSM, a spatialized mass balanced "Apex Predators ECOSystem Model" to study physiologically structured tuna population dynamics in their ecosystem, Prog.
- Oceanogr., 84, 113–117, doi:10.1016/j.pocean.2009.09.013, 2010.
 Maury, O. and Poggiale, J.-C.: From individuals to populations to communities: a dynamic energy budget model of marine ecosystem size-spectrum including life history diversity, J. Theor. Biol., 324, 52–71, doi:10.1016/j.jtbi.2013.01.018, 2013.
 - Maury, O., Faugeras, B., Shin, Y.-J., Poggiale, J.-C., Ben Ari, T., and Marsac, F.: Modeling environ-
- ²⁰ mental effects on the size-structured energy flow through marine ecosystems. Part 1: The model, Prog. Oceanogr., 74, 479–499, doi:10.1016/j.pocean.2007.05.002, 2007.
 - McCauley, D. J., Pinsky, M. L., Palumbi, S. R., Estes, J. A., Joyce, F. H., and Warner, R. R.: Marine defaunation: animal loss in the global ocean, Science, 347, 1255641, doi:10.1126/science.1255641, 2015.
- McClain, C. R., Feldman, G. C., and Hooker, S. B.: An overview of the SeaWiFS project and strategies for producing a climate research quality global ocean bio-optical time series, Deep-Sea Res. Pt. II, 51, 5–42, doi:10.1016/j.dsr2.2003.11.001, 2004.
 - McGurk, M. D.: Natural mortality of marine pelagic fish eggs and larvae: role of spatial patchiness, Mar. Ecol.-Prog. Ser., 34, 227–242, 1986.
- ³⁰ McKendrick, A. G.: Applications of mathematics to medical problems, P. Edinburgh Math. Soc., 3, 98–130, 1926.
Discussion Paper

Moore, T. S., Campbell, J. W., and Dowell, M. D.: A class-based approach to characterizing and mapping the uncertainty of the MODIS ocean chlorophyll product, Remote Sens. Environ., 113, 2424–2430, doi:10.1016/j.rse.2009.07.016, 2009.

Morato, T., Watson, R., Pitcher, T. J., and Pauly, D.: Fishing down the deep, Fish Fish., 7, 24–34, doi:10.1111/j.1467-2979.2006.00205.x, 2006.

- Mullon, C., Freon, P., and Cury, P.: The dynamics of collapse in world fisheries, Fish Fish., 6, 111–120, doi:10.1111/j.1467-2979.2005.00181.x, 2005.
- Munro, J. L. and Pauly, D.: A simple method for comparing the growth of fishes and invertebrates, Fishbyte, 1, 5–6, 1983.
- Myers, R. A.: Stock and recruitment: generalizations about maximum reproductive rate, density dependence, and variability using meta-analytic approaches, ICES J. Mar. Sci., 58, 937–951, doi:10.1006/jmsc.2001.1109, 2001.
 - Myers, R. A.: Recruitment: understanding density-dependence in fish populations, Handbook of Fish Biology and Fisheries, 1, 123–148, 2002.
- ¹⁵ Myers, R. A. and Worm, B.: Rapid worldwide depletion of predatory fish communities, Nature, 423, 280–283, doi:10.1038/nature01610, 2003.
 - Norse, E. A., Brooke, S., Cheung, W. W., Clark, M. R., Ekeland, I., Froese, R., Gjerde, K. M., Haedrich, R. L., Heppell, S. S., Morato, T., Morgan, L. E., Pauly, D., Sumaila, R., and Watson, R.: Sustainability of deep-sea fisheries, Mar. Policy, 36, 307–320, doi:10.1016/j.marpol.2011.06.008, 2012.
- 20 2012.

5

- O'Reily, J. E., Maritorena, S., Siegel, D. A. et al.: Ocean color chlorophyll-a algorithms for Sea-WiFS, OC2 and OC4: Version 4, in: SeaWiFS Postlaunch Technical Report Series Volume 11, SeaWiFS Postlaunch Calibration and Validation Analyses, Part 3, edited by: Hooker, S. B. and Firestone, E. R., NASA Goddard Space Flights Center, Greenbelt, MD, pp. 9–23, 2000.
- Paloheimo, J. E. and Dickie, L. M.: Food and growth of fishes: I. A growth curve derived from experimental data, J. Fish. Res. Board Can., 22, 521–542, doi:10.1139/f65-048, 1965.
 - Pauly, D.: On the interrelationships between natural mortality, growth parameters, and mean environmental temperature in 175 fish stocks, ICES J. Mar. Sci., 39, 175–192, doi:10.1093/icesjms/39.2.175, 1980.
- Pauly, D.: The sea around us project: documenting and communicating global fisheries impacts on marine ecosystems, AMBIO, 36, 290–295, doi:10.1579/0044-7447(2007)36[290:TSAUPD]2.0.CO;2, 2007.

- Pauly, D. and Christensen, V.: Primary production required to sustain global fisheries, Nature, 374, 255–257, doi:10.1038/374255a0, 1995.
- Pauly, D. and Zeller, D.: Catch reconstructions reveal that global marine fisheries catches are higher than reported and declining, Nature Communications, 7, 10244, doi:10.1038/ncomms10244, 2016.
- Pinsky, M. L., Worm, B., Fogarty, M. J., Sarmiento, J. L., Levin, S. A.: Marine Taxa Track Local Climate Velocities, Science, 341, 1239–1242, doi:10.1126/science.1239352, 2013.
- Press, W. H., Teukolsky, S. A., Vetterling, W. T., and Flannery, B. P.: Numerical Recipes in C (2nd edn.): the Art of Scientific Computing, Cambridge University Press, New York, NY, USA, 1992.
- Pulkkinen, H., Mäntyniemi, S., and Chen, Y.: Maximum survival of eggs as the key parameter of stock-recruit meta-analysis: accounting for parameter and structural uncertainty, Can. J. Fish. Aquat. Sci., 70, 527–533, doi:10.1139/cjfas-2012-0268, 2013.
 - Ricker, W. E.: Stock and recruitment, J. Fish. Res. Board Can., 11, 559–623, doi:10.1139/f54-039, 1954.
- Rochet, M.-J., Collie, J. S., Jennings, S., and Hall, S. J.: Does selective fishing conserve community biodiversity? Predictions from a length-based multispecies model, J. Fish. Res. Board Can., 68, 469–486, doi:10.1139/F10-159, 2011.
 - Rosenberg, A., Fogarty, M., Cooper, A., Dickey-Collas, M., Fulton, E., Gutiérrez, N., Hyde, K., Kleisner, K., Kristiansen, T., Longo, C., Minte-Vera, C., Minto, C., Mosqueira, I., Chato Osio, G.,
- ²⁰ Ovando, D., Selig, E., Thorson, J., and Ye, Y.: Developing New Approaches to Global Stock Status Assessment and Fishery Production Potential of the Seas, FAO Fisheries and Aquaculture Circular No. 1086, FAO, Rome, Italy, 2014.

Ryther, J. H.: Photosynthesis and fish production in the sea, Science, 166, 72–76, doi:10.1126/science.166.3901.72, 1969.

- Saba, V. S., Friedrichs, M. A. M., Antoine, D., Armstrong, R. A., Asanuma, I., Behrenfeld, M. J., Ciotti, A. M., Dowell, M., Hoepffner, N., Hyde, K. J. W., Ishizaka, J., Kameda, T., Marra, J., Mélin, F., Morel, A., O'Reilly, J., Scardi, M., Smith Jr., W. O., Smyth, T. J., Tang, S., Uitz, J., Waters, K., and Westberry, T. K.: An evaluation of ocean color model estimates of marine primary productivity in coastal and pelagic regions across the globe, Biogeosciences, 8, 489–503, doi:10.5194/bg-8-
- 30 489-2011, 2011.

5

Sarmiento, J. L., Slater, R., Barber, R., Bopp, L., Doney, S. C., Hirst, A. C., Kleypas, J., Matear, R., Mikolajewicz, U., Monfray, P., Soldatov, V., Spall, S. A., Stouffer, R.:

Response of ocean ecosystems to climate warming, Global Biogeochemical Cycles, 18, 3, doi:10.1029/2003GB002134, 2004.

- Savage, V. M., Gillooly, J. F., Brown, J. H., West, G. B., and Charnov, E. L.: Effects of body size and temperature on population growth, Am. Nat., 163, 429–441, doi:10.1086/381872, 2004.
- Schaefer, M. B.: Some aspects of the dynamics of populations important to the management of the commercial marine fisheries, Bulletin of the Inter-American Tropical Tuna Commission, 1, 27–56, doi:10.1007/BF02464432, 1954.

Schnute, J.: A general theory for analysis of catch and effort data, Can. J. Fish. Aquat. Sci., 42, 414–429, doi:10.1139/f85-057, 1985.

¹⁰ Sheldon, R. W., Prakash, A., and Sutcliffe Jr., W.: The size distribution of particles in the ocean, Limnol. Oceanogr., 17, 327–340, doi:10.4319/lo.1997.42.1.0001, 1972.

Smyth, T. J.: Integration of radiative transfer into satellite models of ocean primary production, J. Geophys. Res., 110, C10014, doi:10.1029/2004JC002784, 2005.

Steinacher, M., Joos, F., Frölicher, T. L., Bopp, L., Cadule, P., Cocco, V., Doney, S. C., Gehlen, M.,

Lindsay, K., Moore, J. K., Schneider, B., and Segschneider, J.: Projected 21st century decrease in marine productivity: a multi-model analysis, Biogeosciences, 7, 979–1005, doi:10.5194/bg-7-979-2010, 2010.

Sumaila, U. R., Cheung, W. W. L., Lam, V. W. Y., Pauly, D., and Herrick, S.: Climate change impacts on the biophysics and economics of world fisheries, Nature Climate Change, 1, 449–456,

doi:10.1038/nclimate1301, 2011.

Taucher, J. and Oschlies, A.: Can we predict the direction of marine primary production change under global warming?, Geophys. Res. Lett., 38, L02603, doi:10.1029/2010GL045934, 2011.

Taylor, C. C.: Cod growth and temperature, ICES J. Mar. Sci., 23, 357–365, doi:10.1093/icesjms/23.3.366, 1958.

Tremblay-Boyer, L., Gascuel, D., Watson, R., Christensen, V., and Pauly, D.: Modelling the effects of fishing on the biomass of the world's oceans from 1950 to 2006, Mar. Ecol.-Prog. Ser., 442, 169–185, doi:10.3354/meps09375, 2011.

Vandermeer, J.: Metabolic theories in ecology, Trends Ecol. Evol., 21, 136–140, doi:10.1016/j.tree.2005.11.004, 2006.

von Bertalanffy, L.: A quantitative theory of organic growth (inquiries on growth laws. II), Hum. Biol., 10, 181–213, 1938.

von Bertalanffy, L.: Problems of organic growth, Nature, 163, 156–158, doi:10.1038/163156a0, 1949. von Bertalanffy, L.: Quantitative laws in metabolism and growth, Q. Rev. Biol., 32, 217–231, 1957.

- von Foerster, H.: Some remarks on changing populations, in: The Kinetics of Cellular Proliferation, edited by: Stohlman Jr., F., Grune and Stratton, New York, 1959.
- Walsh, H. J., Richardson, D. E., Marancik, K. E., Hare, J. A.: Long-Term Changes in the Distributions of Larval and Adult Fish in the Northeast U.S. Shelf Ecosystem, PLoS ONE, 10(9), e0137382, doi:10.1371/journal.pone.0137382, 2015.
- Watson, R. A. and Morato, T.: Fishing down the deep: accounting for within-species changes in depth of fishing, Fish. Res., 140, 63–65, doi:10.1016/j.fishres.2012.12.004, 2013.
- Watson, R., Kitchingman, A., and Gelchu, A.: Mapping global fisheries: sharpening our focus, Fish Fish., 5, 168–177, doi:10.1111/j.1467-2979.2004.00142.x, 2004.
- ¹⁰ Watson, R., Zeller, D., and Pauly, D.: Primary productivity demands of global fishing fleets, Fish Fish., 15, 231–241, doi:10.1111/faf.12013, 2013a.
 - Watson, R. A., Cheung, W. W. L., Anticamara, J. A., Sumaila, R. U., Zeller, D., and Pauly, D.: Global marine yield halved as fishing intensity redoubles, Fish Fish., 14, 493–503, doi:10.1111/j.1467-2979.2012.00483.x, 2013b.
- ¹⁵ Watson, J. R., Stock, C. A., and Sarmiento, J. L.: Exploring the role of movement in determining the global distribution of marine biomass using a coupled hydrodynamic – size-based ecosystem model, Prog. Oceanogr., doi:10.1016/j.pocean.2014.09.001, online first, 2014.
 - West, G. B., Brown, J. H., and Enquist, B. J.: A general model for ontogenetic growth, Nature, 413, 628–631, doi:10.1038/35098076, 2001.
- White, E. P., Ernest, S. K. M., Kerkhoff, A. J., and Enquist, B. J.: Relationships between body size and abundance in ecology, Trends Ecol. Evol., 22, 323–330, doi:10.1016/j.tree.2007.03.007, 2007.
 Woodworth-Jefcoats, P. A., Polovina, J. J., Dunne, J. P., and Blanchard, J. L.: Ecosystem size structure response to 21st century climate projection: large fish abundance decreases in the central North Pacific and increases in the California Current, Glob. Change Biol., 19, 724–733,
- ²⁵ doi:10.1111/gcb.12076, 2012.

5

Xiao, X., White, E. P., Hooten, M. B., and Durham, S. L.: On the use of log-transformation vs. nonlinear regression for analyzing biological power laws, Ecology, 92, 1887–1894, doi:10.1890/11-0538.1, 2011.

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Table 1. Ecological model parameters. Assumption (I) (Brown et al., 2004; Savage et al., 2004; Andersen and Beyer, 2013); assumption (II) value of slope sufficiently large to have abrupt increase in allocation of reproduction from 0 to 1; assumption (III) (Beverton, 1992; Charnov et al., 2012); assumption (IV) (Jennings et al., 2008; Barnes et al., 2010; Irigoien et al., 2014). β truncated since we only consider fish up to 100 kg; assumption (V) Equal partitioning of net primary production to each group; assumption (VI) (Dahlberg, 1979; Andersen and Pedersen, 2010; Pulkkinen et al., 2013). Assumption (VII) (Duarte and Alcaraz, 1989; Cury and Pauly, 2000; Freedman and Noakes, 2002; Maury et al., 2007). The [†] symbol in the first column identifies parameters that were considered in the tuning procedure of the companion paper (Carozza et al., 2016). $\partial F/\partial p$ is the rate of change of equilibrium biomass (calculated over the three groups) with respect to change in a parameter *p*.

Parameter	Name	Value [Range]	$\partial F/\partial p$	Unit	Equation	Reference
	Lower bound of smallest mass class	10	-	g	(2), (B1)	AppendixSect. 2.9
m_u	Upper bound of largest mass class	10 000	-	g	(B1)	AppendixSect. 2.9
N_M	Number of mass classes	50	-	-	(B1)	AppendixSect. 2.9
$m_{i,L}$	Mass at lower bound of mass class i	-	-	g	(B1)	AppendixSect. 2.9
m_i	Representative mass of a mass class i	-	-	g	(B1)	AppendixSect. 2.9
$m_{\infty,k}$	Asymptotic mass	(314 8500 0.3 8.5 100 000)	-	kg	-	AppendixSect. 2.9
T_{r}	Reference temperature for $a(T)$	10	-	°Ō	(4)	Andersen and Beyer (2013)
k_B	Boltzmann's constant	8.617×10 ⁻⁵	-	${ m eV}{ m K}^{-1}$	(4)	Boltzmann (1872)
$\dagger \omega_{a,A}$	Growth activation energy of metabolism	$0.3116~[0.45\pm0.09~]$	< 0	eV	(4)	Savage et al. (2004)
$\dagger \omega_{a,\lambda}$	Mortality activation energy of metabolism	$0.3756~[0.45\pm0.09~]$	< 0	eV	(4)	Savage et al. (2004)
† b	Allometric scaling exponent	$0.6787~[0.7\pm0.05~]$	< 0	Unitless	(10)	Assumption I
$^{\dagger}A_{0}$	Allometric growth constant	$3.6633[4.46\pm0.5]$	< 0	$g^{1-b} s^{-1}$	(10)	Andersen and Beyer (2013)
ϵ_a	Activity fraction	0.8	-	Unitless	(109),(9 10)	Andersen and Beyer (2013)
c_s	Slope parameter of $s_k(m)$	5	-	Unitless	(23)	Assumption II
η	Ratio of mature to asymptotic mass	$0.25~[0.25\pm0.075~]$	-	Unitless	(23)	Andersen and Beyer (2013) and III
$^{\dagger} \alpha$	Trophic efficiency	0.16 [0.1,0.16]	> 0	Unitless	(24)	Assumption IV
$^{\dagger}\beta$	Predator to prey mass ratio	7609 [850, 10 000]	> 0	Unitless	(24)	Assumption IV
au	Trophic scaling	-0.2047	-	Unitless	(24)	Assumption IV
m_{L}	Mass of large phytoplankton	$4 imes 10^{-6}$	-	g	(25)	Maranón (2015)
m_{S}	Mass of small phytoplankton	$4 imes 10^{-15}$	-	g	(25)	Maranón (2015)
$^{\dagger} k_{E}$	Eppley constant for phytoplankton growth	$0.0667 \ [0.0631 \pm 0.009 \]$	< 0	$^{\circ}C^{-1}$	-	Bissinger et al. (2008)
P^*	Characteristic nutrient concentration	1.9 ± 0.3	-	mmol C m $^{-3}$	-	Dunne et al. (2005)
† ∏*	NPP normalized to $T_{C} = 0^{\circ}C$ at P^{*}	$0.3135~[0.37\pm0.1~]$	< 0	mmol C m $^{-3}$ d $^{-1}$	-	Dunne et al. (2005)
† ζ1	Mortality constant	$0.2701~[0.55\pm0.57~]$	< 0	Unitless	(26)	Gislason et al. (2010)
$^{\dagger}h$	Allometric mortality scaling	$0.4641~[0.54\pm0.09~]$	< 0	Unitless	(26)	Gislason et al. (2010)
$\phi_{\rm f}$	Fraction of females	0.5	-	Unitless	(28)	Maury et al. (2007)
$\phi_{\pi,k}\phi_{\Pi \psi,C}$	Fraction of NPP to commercial fish groups	1	-	Unitless	-	Sect. 2.3
$\phi_{C,k}$	Fraction of $\phi_{\Box_{\Psi,C}}$ allocated to a group k	1/3	-	Unitless	(24)	Assumption V
† se	Egg to recruit survival fraction	0.0327 [10 ^{-3.5} , 0.5]	> 0	Unitless	(28)	Assumption VI
m_{e}	Egg mass	5.2×10 ⁻⁴	-	g	(28)	Assumption VII

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Symbol	Name	Unit	Equation
m	Size (mass) of fish	g	_
t	Time	S	_
T	Temperature	K or °C	_
f(m,t)	Fish biomass spectrum	$ m gwBm^{-2}g^{-1}$	(1)
F(m,t)	Cumulative fish biomass	$gwB m^{-2}$	_
$\gamma_k(m,t) \gamma_{S,k}(m,t)$	Individual fish growth rate	${ m gs^{-1}}$	(22)
$\Lambda(m) \Lambda_k(m,t)$	Natural mortality rate	s^{-1}	(1), (26)
a(T)	van't Hoff–Arrhenius temperature dependency	Unitless	(4)
$\xi_{I,k}(m,t)$	Total input energy to growth and reproduction	${ m gs}^{-1}$	(11)
$\xi_{R,k}(m,t) \gamma_{R,k}(m,t)$	Energy allocated to reproduction	${ m gs}^{-1}$	(13)
$\xi_{P,k}(m,t)$	Energy input from net primary production	${ m gs^{-1}}$	(8)
$\xi_{VB,k}(m,t)$	Energy input from allometric theory	${ m gs}^{-1}$	(10)
$\Pi(m,t)$	Fish production	$ m gwBm^{-2}s^{-1}$	(8)
$\pi(m,t)$	Fish production spectrum	${ m gwB}{ m m}^{-2}{ m g}^{-1}{ m s}^{-1}$	(8), (24)
$N_k(m,t)$	Cumulative group abundance	$\#{ m m}^{-2}$	(8), (A1)
$n_k(m,t)$	Group abundance spectrum	$\#{ m m}^{-2}{ m g}^{-1}$	(8), (A1)
k_a	Mass specific investment in activity	s^{-1}	(10)
$s_k(m)$	Mass structure of energy to reproduction $\Phi(m)$	Unitless	(23)
$\Phi_k(m)$	Fraction of input energy to reproduction	Unitless	(21)
$\Pi_{\psi}(t)$	Net primary production	mmol C m $^{-3}$ d $^{-1}$	(24)
$\overline{\Pi}_{\psi}$	Annual average net primary production	mmol C m $^{-3}$ d $^{-1}$	(33)
$m_{\psi}(t)$	Representative mass of phytoplankton	g	(24), (25)
$\Phi_{L}(t)$	Fraction of large phytoplankton production	Unitless	(25)
$R_P(m_0,t)$	Primary-production determined recruitment	$ m gwBm^{-2}s^{-1}$	(27)
$R_{e,k}(m_0,t)$	Egg production and survival determined recruitment	$ m gwBm^{-2}s^{-1}$	(28)
$R_k(m_0,t)$	Overall recruitment	$ m gwBm^{-2}s^{-1}$	(29)

Table 2. Ecological model variables.



Figure 1. Schematic diagram of the main modules, components, and processes of the ecological module of BOATS. Solid arrows represent fluxes Net primary production (NPP) and temperature (T) force the model and are used to calculate the fish production spectrum, by assuming a transfer of biomassenergy from phytoplankton to successive sizes of fish that depends on the trophic efficiency and the predator to prey mass ratio. From fish production, whereas dashed arrows we calculate the size-dependent growth rate of biomass in three independent groups that represent dependenciessmall, medium, and large commercial fish. Arched lines identify model components or extend Mortality rates are calculated as a process over function of size and asymptotic size, and also depend on temperature. Adult fish, the largest sizes in each spectrum, allocate energy to reproduction, of which a fraction is returned to the smallest mass classes or groups class of the corresponding spectrum, representing recruitment of juveniles.

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Figure 2. Mass dependence of reproduction by group. The mass scaling function $s_k(m)$ (thin lines, Eq. 23) determines the mass dependence of the allocation of energy to reproduction. $\Phi_k(m)$ (thick lines, Eq. 21) is the fraction of energy allocated to reproduction.



Figure 3. Recruitment flux. The recruitment flux of group k, $R_k(m_0,t)$ (gwB m⁻² yr⁻¹, Eq. 29) as a function of the recruitment based on the boundary flux of NPP $R_{P,k}(m_0,t)$ (gwB m⁻² yr⁻¹, Eq. 27), and the recruitment from production and survival of eggs $R_{e,k}(m_0,t)$ (gwB m⁻² yr⁻¹, Eq. 28).





Figure 4. Steady state biomass spectra at two sites. BlueBlack solid, greendashed, and red dash-dot curves represent the small, medium, and large groups group biomass, respectively, and whereas the black grey curves represent the total of the three groups. The model is forced at two sites with annual average net primary production (NPP) and temperature (T) with a timestep of 15 days. Simulations are for a (a) cold-water site in the East Bering Sea LME (64° N, 165° W) and a (b) warm-water site in the Benguela Current LME site (20° S, 12° E).

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Figure 5. Model sensitivity to net primary production (NPP) and temperature (*T*). (a) Total biomass in terms of NPP and *T*, (b) intercept of total fish spectrum in terms of NPP and *T*, and (c) group and total slope of the nonreproducing part of the fish biomass spectra. Note that In (c), since the spectral slope does slopes of the biomass spectra do not depend on NPP, the slopes are lines that depend only on temperature. Red and blue circles in (a) and (b) represent the NPP and *T* of the warm- and cold-water sites, respectively, used in Fig. 4. All total spectral intercepts and slopes are calculated by adding the biomass in each mass class over all three groups. The intercept is the spectral biomass of the first mass class, and the slope is calculated from the mass classes that are smaller than the maturity mass $m_{\alpha,k}$ (the non-reproducing nonreproducing mass classes).