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# Path-integral method for the source apportionment of photochemical pollutants

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The goal of source apportionment is to determine, quantitatively, how much different emission sources contribute to a given pollutant concentration. Source apportionment is thus a useful tool in developing efficient strategies to meet air quality standards by identifying the most important sources. If emissions are involved in only linear processes between where they are emitted and where they impact a receptor location, the concentration of the pollutant at the receptor is the sum of independent contributions from the individual emission sources. For example, one can define a tracer for each source of primary, unreactive particulate matter (PM) in an air quality model such that the sum of the tracer concentrations is the total primary PM concentration and the tracer concentrations form the source apportionment. However, if a secondary pollutant is formed by nonlinear chemical reactions, source apportionment is more complicated and, indeed, there is no unique apportionment.

Reflecting this non-uniqueness, a number of approaches have been developed for source apportionment of secondary pollutants. The simplest approach is source removal or the brute force method. Simulations with and without a particular source are compared, and the changes in predicted concentrations are assigned to emissions from that source (Marmur et al., 2006; Tong and Mauzerall, 2008; Wang et al., 2009; Zhang et al., 2014). A related approach is the factor-separation method, which for M sources involves analysis of a set of  $2^M$  simulations (Stein and Alpert, 1993; Tao et al., 2005). Each simulation includes emissions from a different source or a different combination of sources. Pollutant concentrations are assigned not just to sources but to interactions among sources.

Another approach involves the use of reactive tracers for individual chemical species, sources, and/or geographic regions (Yarwood et al., 1996; Dunker et al., 2002b; Mysliwiec and Kleeman, 2002; Wagstrom et al., 2008; Wang et al., 2009; Kwok et al., 2013). However, various chemical assumptions (beyond those in the chemical mechanism) are needed to track production of the secondary pollutant in nonlinear reactions. In

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addition, the source contributions are often restricted to be positive even if some primary pollutants can inhibit formation of the secondary pollutant. Assignment methods trace through all the reaction pathways from products back to parent reactants (Bowman and Seinfeld, 1994; Bowman, 2005). These methods also require extra chemical 5 assumptions for reactions in which a product results from multiple reactants. Lastly, local sensitivity coefficients have been used to apportion ozone (O<sub>3</sub>) and PM (Dunker et al., 2002b; Cohan et al., 2005; Koo et al., 2009). This approach involves constructing a Taylor series representation of the concentration as a function of source emissions and extrapolating the representation to zero emissions.

This work presents a new approach for source apportionment called the Path-Integral Method (PIM). The PIM provides a new, direct mathematical connection between sensitivity analysis and source apportionment and a connection between source apportionment and emission-control strategies. In contrast to reactive-tracer and assignment methods, the PIM does not require additional chemical assumptions. An important advantage of the PIM is its ability to allocate to sources a concentration increment, i.e., the difference between two simulations (base and background cases). If the anthropogenic increment is allocated to sources, the PIM requires that the base-case concentration minus the sum of the anthropogenic source contributions equals the background concentration. Other methods do not have this requirement, and thus may over- or underallocate the anthropogenic increment to the anthropogenic sources and also allocate a concentration to the background sources that is not the concentration from a simulation with only background sources included.

The PIM is applied here to allocate the anthropogenic increments of O<sub>3</sub> and other species using a 2-cell configuration of the Comprehensive Air Quality Model with Extensions (CAMx) (ENVIRON, 2013). Another application of the PIM using a detailed, 3-D CAMx configuration for the eastern US will be reported elsewhere.

#### **Equations**

The PIM is based on an exact mathematical equation that is in itself not new. However, the application of the equation to source apportionment is new. For this work, the 5 equation (Kaplan, 1959) takes the form

$$\Delta c_i(\mathbf{x},t) = c_i^1(\mathbf{x},t;\mathbf{\Lambda}=1) - c_i^0(\mathbf{x},t;\mathbf{\Lambda}=0) = \sum_{m=1}^M \int_P \frac{\partial c_i(\mathbf{x},t;\mathbf{\Lambda})}{\partial \lambda_m} \, \mathrm{d}\lambda_m \tag{1}$$

The  $c_i^1$  is the concentration of species i in the base case, with all emissions present, and  $c_i^0$  is the concentration in the background case, with M emission sources removed.  $\Lambda$  is the array of the parameters  $\lambda_m$  that scale the emissions of the M sources. If all  $\lambda_m = 0$  ( $\Lambda = 0$ ), the emissions are those of the background case, and if all  $\lambda_m = 1$ ( $\Lambda$  = 1), the emissions are those of the base case. The  $\partial c_i/\partial \lambda_m$  are the first-order sensitivities of  $c_i$  with respect to the scaling parameters. The integrals on the right side of Eq. (1) are taken over a curve or path P in M-dimensional space leading from the emissions in the background case to those in the base case. The  $\Delta c_i$  is the difference between the concentrations in the base and background cases at the same spatial location x and time t.

Although the focus here is on emissions, Eq. (1) can also include parameters that scale the initial and boundary concentrations. Furthermore, if the background case has all emissions and initial and boundary concentrations set to zero, then  $c_i^0 = 0$  and  $\Delta c_i$  is the total concentration. Thus, the PIM can allocate the total concentration in a simulation as well as concentration differences between simulations.

The contribution of source m to  $\Delta c_i$ ,  $S_{im}$ , is defined to be

$$S_{im}(\mathbf{x},t;P) = \int_{P} \frac{\partial c_{i}(\mathbf{x},t;\mathbf{\Lambda})}{\partial \lambda_{m}} \,\mathrm{d}\lambda_{m} \tag{2}$$

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The source contributions depend on the path P from the point  $\Lambda=0$  to the point  $\Lambda=1$ . Because there are an infinite number of paths between these two points, there are an infinite number of sets of source contributions, one set corresponding to each path. Viewed in the direction of integration, from  $\Lambda=0$  to  $\Lambda=1$ , emissions are added into the background case until the base case is reached. Viewed in the opposite direction, emissions are controlled from the base case until the background case is reached. Thus, each path P represents a possible emission-control scenario, and the contribution of a given source to the change in concentration  $\Delta c_i$  depends on the control scenario.

The path P can be described via a path variable u. Then,  $\Lambda = \Lambda(u)$ , such that as u varies from 0 to 1, each  $\lambda_m$  varies along P from 0 to 1. However, u may not equal the normalized distance along P, denoted by s, and s can be useful in designing the numerical integration procedure because it is easier to understand the distribution of the integration points using s. The absolute distance D is related to u by

$$D(u) = \int_{0}^{u} \left[ \sum_{m=1}^{M} \left( \frac{\mathrm{d}\lambda_{m}}{\mathrm{d}u} \right)^{2} \right]^{1/2} \mathrm{d}u$$
 (3)

Then, s(u) = D(u)/D(1). Using s, the source contribution becomes

$$S_{im}(\mathbf{x},t;P) = \int_{0}^{1} \frac{\partial c_{i}(\mathbf{x},t;\mathbf{\Lambda})}{\partial \lambda_{m}} \bigg|_{\mathbf{\Lambda} = \mathbf{\Lambda}(s)} \frac{d\lambda_{m}}{ds} ds$$
 (4)

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The sensitivity in Eq. (4) is evaluated along the specific path defined by  $\Lambda(s)$ . Also, though the emissions are reduced along the path and the concentrations are determined in a simulation with the reduced emissions, the sensitivity of  $c_i$  is to  $\lambda_m$ , which scales the full emissions in the base case, not the reduced emissions. The decoupled direct method (DDM) provides an accurate, efficient means for calculating the sensitivities (Dunker, 1981, 1984; Yang et al., 1997). The DDM has been implemented in current 3-D models for the formation of  $O_3$  and particulate matter (Dunker et al., 2002a; Cohan et al., 2005; Napelenok et al., 2006; Koo et al., 2007).

The simplest and shortest integration path, termed the diagonal path, is defined by  $\lambda_m = u$ , all m. This is a straight line from  $\Lambda = 0$  to  $\Lambda = 1$  along which the emissions from all sources are reduced or grown by the common factor u. If there are two sources, Fig. 1 displays the diagonal path, Path 1, and two other possible paths. Path 2 is defined by the equations:

$$\lambda_1(u) = u^3 \tag{6}$$

$$\lambda_2(u) = \sin\left(\pi \frac{u}{2}\right) \tag{7}$$

Beginning at the base case, point B, emissions from source 1 are reduced much more rapidly than those from source 2 along Path 2. As the first 80 % of the emissions from source 1 are reduced, only 20 % of the emissions from source 2 are reduced. Then the remaining 80 % of the emissions from source 2 are reduced as the remaining 20 % of the emissions from source 1 are reduced, down to the background case, point b. Path 3 is the opposite of Path 2, obtained by interchanging the definitions of  $\lambda_1$  and  $\lambda_2$  in

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The Gaussian numerical integration formulas have maximum precision (Isaacson and Keller, 1966). This means that for a given number of points at which the integrand is evaluated, n, the formulas give an exact integration of all polynomials of degree 0 up to 2n - 1, the maximum degree possible using n points. Thus, the Gaussian formulas should minimize the number of points at which the integrand in Eq. (4) must be evaluated to achieve a given accuracy. This is useful because the major computational effort in the PIM is determining the sensitivities at multiple points along the path P. The Gauss—Legendre formula is one version of Gaussian integration suited to integration of a function f(z) over a finite interval:

$$\int_{a}^{b} f(z) dz \cong \frac{b-a}{2} \sum_{k=1}^{n} w(\xi_k) f\left(\frac{b-a}{2} \xi_k + \frac{b+a}{2}\right)$$
(8)

$$z = \frac{b-a}{2}\xi + \frac{b+a}{2} \tag{9}$$

The  $\xi_k$  are the zeroes of the Legendre polynomials, and the  $w(\xi_k)$  are weights determined to give the formula the maximum precision. The  $\xi_k$  and  $w(\xi_k)$  are readily available (efunda, 2014).

#### 2.2 Special cases

One special case is successive zero-out (SZO) of the sources. In SZO, the emissions from one source are reduced to zero while leaving all other emissions unchanged, then the emissions from a second source are reduced to zero, etc. until the background case is reached. This is a path along the edges of the hypercube in  $\Lambda$ -space. In Fig. 1, one path would be B-b2-b and the other, B-b1-b. Along the segment B to b2 of the former path, the sensitivities are nonzero, but d $\lambda_2$  = 0. Therefore, the only contribution to  $\Delta c_i$  9086

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in Eq. (1) is that for source 1, and this contribution equals  $c_i^B - c_i^{b2}$ . Similarly, along the segment from b2 to b,  $\mathrm{d}\lambda_1 = 0$ , the only contribution to  $\Delta c_i$  is that for source 2, and the contribution equals  $c_i^{b2} - c_i^b$ . Thus, a SZO path is a special case of PIM in which no calculation or integration of sensitivities is required, only a series of simulations to obtain the concentrations at the corners of the hypercube. Calculation and integration of the sensitivities is necessary if two or more sources are controlled simultaneously, and the path is then interior to the hypercube.

Another special case involves expanding the sensitivities in a Taylor series in the  $\lambda_m$  at  $\Lambda = 1$  (base case). If there are two sources and the Taylor series through first order in  $\lambda_m$  is integrated along the diagonal path, then (see Supplement (SI))

$$S_{i1}(\text{diag}) = \frac{\partial c_i}{\partial \lambda_1} \bigg|_{\Lambda=1} - \frac{1}{2} \frac{\partial^2 c_i}{\partial \lambda_1^2} \bigg|_{\Lambda=1} - \frac{1}{2} \frac{\partial^2 c_i}{\partial \lambda_1 \partial \lambda_2} \bigg|_{\Lambda=1}$$
 (10)

$$S_{i2}(\text{diag}) = \frac{\partial c_i}{\partial \lambda_2} \bigg|_{\Lambda=1} - \frac{1}{2} \frac{\partial^2 c_i}{\partial \lambda_2^2} \bigg|_{\Lambda=1} - \frac{1}{2} \frac{\partial^2 c_i}{\partial \lambda_1 \partial \lambda_2} \bigg|_{\Lambda=1}$$
(11)

The cross term  $(-\partial^2 c_i/\partial \lambda_1 \partial \lambda_2)$  is split evenly between  $S_{i1}$  and  $S_{i2}$ . If the integration is done instead on the path B-b1-b in Fig. 1, the full cross term is assigned to  $S_{i1}$  and is absent entirely from  $S_{i2}$ . Similarly, if the integration is along the path B-b2-b, the full cross term is assigned to  $S_{i2}$  and is absent from  $S_{i1}$ . Thus, the source contributions are the same for these 3 paths except for the location of the cross term. Cohan et al. (2005) expanded  $c_i$  in a second-order Taylor series about  $\Lambda = 1$  and used it to develop source apportionments that are the same as Eqs. (10) and (11) except that they did not assign the cross term to the individual sources. The PIM shows that the cross term can be assigned to sources based on the emission-control path.

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The dependence of the source contributions on path has an analogy in thermodynamics. For example, in the case of a single-component gas, the energy E is a function of the state variables: temperature T, and volume V. The change in E between two states of the system,  $\Delta E$ , depends only on the initial and final values of T and V. However, when  $\Delta E$  is split into contributions from the heat exchange with the surroundings  $(\int_P dq)$  and the pressure (p)-related work  $(\int_P p dV)$  in the equation  $\Delta E = \int_P dq - \int_P p dV$ , the heat exchange and work depend on the path P from the initial to final states of the system. Thus, the concentrations  $c_i$  from an air quality simulation may be regarded as analogous to E and the emissions, initial and boundary concentrations, meteorology and chemical mechanism as analogous to E and E0. The E1 between two simulations differing only in emissions can be allocated to sources, but this allocation is analogous to heat exchange and work and depends on the path along which the emissions are changed.

### 3 Model and inputs

Time-dependent inputs were developed for CAMx, v6.00, configured with 2 cells in a vertical column. The lower cell varied diurnally in height from  $100 \rightarrow 300 \rightarrow 100\,\mathrm{m}$  and the upper cell varied in height such that the top of the column was  $1500\,\mathrm{m}$ . Diurnally varying emissions were introduced at the bottom boundary. The simulations were run for 3 days, 20–22 June, beginning with clean initial concentrations in both cells. There was no transport into the cells via the lateral or top boundaries. The latitude was that of Los Angeles and Atlanta. The Carbon Bond 6 (CB6) chemical mechanism represented the gas-phase chemistry (Yarwood et al., 2012). The effect of the inputs is that cleaner air from the upper cell is entrained into the lower cell during the morning as the lower cell grows in height. Then, in the evening, the lower cell shrinks in height and leaves pollutants aloft in the upper cell. Consequently, there is carry-over of pollutants from

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day to day affecting the chemistry in the lower cell. Additional details of the simulations are in Table S1 (SI).

The emissions were developed from the national totals in the 2008 U.S. National Emission Inventory, version 3 (U.S. EPA, 2013b) with several adjustments. Emissions from wildfires and prescribed fires were excluded because these vary greatly from year to year and were unusually high in 2008. Also, to represent summer conditions, emissions from residential wood combustion were excluded. Further, emissions of NO from lightning were added (Koo et al., 2010). The emissions were segregated into biogenic (plus lightning) emissions and 5 major source categories of anthropogenic emissions: fuel combustion, industrial sources, on-road vehicles, non-road vehicles, and other emissions. Vegetation and soil emissions and their speciation are from BEIS3.14 (Pierce et al., 1998). Anthropogenic emissions of volatile organic compounds (VOC's) from a major source category were allocated to CB6 species using speciation profiles from SPECIATE 4.3 for 1 or 2 sub-categories of sources comprising a significant fraction of the VOC emissions (Simon et al., 2010; U.S. EPA, 2013a). The annual emissions of VOC species, NO<sub>x</sub> (= NO + NO<sub>2</sub>), CO, and HONO for each source category were allocated to hours of a Wednesday in June using temporal profiles (U.S. EPA, 2013c). On a national scale, the biogenic VOC emissions are large compared to the anthropogenic VOC emissions, but this is not the case in urban areas. To represent better an urban area the anthropogenic emissions were weighted by a factor of 5 and the biogenic emissions by a factor of 1. A summary of the resulting daily emission rates for all source categories is given in Table 1, and the complete set of emission rates is in Table S2.

The model and inputs are not intended to be a detailed representation of a specific urban area but rather to provide a useful platform for testing the PIM, specifically different integration formulas and the dependence of the source contributions on paths.

The concentrations of  $O_3$  and formaldehyde (FORM) in the background simulation (biogenic emissions only), the base simulation (both the biogenic and anthropogenic emissions) and the difference between the simulations (anthropogenic increment) are shown in Fig. 2. Similar plots for  $NO_2$  and  $HNO_3$  are in Fig. S1. The peak  $O_3$  concentration remains relatively constant over the 3 days in the background simulation (47–52 ppb) but increases steadily in the base simulation (from 75 ppb on day 1 to 151 ppb on day 3) due to the additional anthropogenic emissions on days 2 and 3 and the carryover of pollutants in the upper cell. Both  $O_3$  and FORM have sizeable concentrations in the background case whereas  $NO_2$  and  $HNO_3$  have very low concentrations due to the low biogenic  $NO_x$  emissions. The  $O_3$  increment is negative at the beginning of day 1 due to the titration of  $O_3$  by the anthropogenic NO emissions. The  $VOC/NO_x$  ratio in the base case increases from 5–7 on day 1 to 9–20 ppbC ppb<sup>-1</sup> on day 3. Overall, the simulations provide a wide range of conditions for testing the PIM.

# 4.1 Accuracy of the numerical integration

The  $O_3$ , FORM,  $NO_2$ , and  $HNO_3$  increments were allocated to the 5 anthropogenic source categories and to the 4 species or groups of species emitted by each source category: VOC, CO,  $NO_x$ , and HONO. Thus, a total of M=20 sensitivities were calculated and integrated in the PIM. Source apportionments were determined for 3 emission-control paths: diagonal (Diag); VOC first (VOCF);  $NO_x$  first (NOxF). Along the Diag path, the scaling parameters  $\lambda_m^{VOC} = \lambda_m^{CO} = \lambda_m^{NO_x} = \lambda_m^{HONO} = u$ , for each source category  $m=1,\ldots,5$ . Thus, the sources and emission species are treated equivalently. The VOCF path emphasizes initial control of VOC and CO emissions followed by later control of  $NO_x$  and HONO emissions, as defined by  $\lambda_m^{VOC} = \lambda_m^{CO} = u^3$  and  $\lambda_m^{NO_x} = \lambda_m^{HONO} = \sin(\pi u/2)$ ,  $m=1,\ldots,5$ . The NOxF path has the reverse assignments of  $u^3$  and  $\sin(\pi u/2)$ . Viewing  $\lambda_m^{VOC}$ ,  $\lambda_m^{CO}$  as analogous to  $\lambda_1$  in Fig. 1 and  $\lambda_m^{NO_x}$ ,  $\lambda_m^{HONO}$ 

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The Gauss-Legendre formula was tested for accuracy using different numbers of integration points and different integration variables. One set of tests, labeled GLns, <sub>5</sub> used the distance s as the integration variable and n integration points. Another set of tests, labeled GLnr, used a transformation of the variable s to  $r = s^{1/2}$ . Equation (4) then becomes

$$S_{im}(\mathbf{x},t;P) = 2 \int_{0}^{1} \frac{\partial c_{i}(\mathbf{x},t;\mathbf{\Lambda})}{\partial \lambda_{m}} \left| \sum_{\mathbf{\Lambda} = \mathbf{\Lambda}(s[r])} \frac{d\lambda_{m}}{ds} \right|_{s(r)} r dr$$
(12)

Because the background case contains no anthropogenic emissions, O<sub>3</sub> formation is strongly limited by the availability of NO<sub>x</sub>. As a consequence, the sensitivity of O<sub>3</sub> with respect to any  $\lambda_m$  that scales NO<sub>x</sub> emissions is very large near  $\Lambda = 0$ , but the sensitivity decreases very rapidly as  $NO_{x}$  emissions are added. The transformation to r has two potentially beneficial effects for the source apportionment of O<sub>3</sub>. First, the points for the numerical integration are chosen for the variable r. When transformed back to the variable s, the points for s are closer to  $\Lambda = 0$  than if s were the integration variable, giving more resolution where the sensitivity is changing most rapidly. Second, the factor r in Eq. (12) reduces the magnitude of the integrand near  $r = s = \lambda_m = 0$ , and makes the integrand identically 0 at r = 0. This can yield an integrand that is easier to integrate. Finally, as a simple alternative, the source contributions were calculated by the trapezoidal rule using the 2 points at  $\Lambda = 0$  and 1 (labeled TR2).

The sum of the source contributions on the 3 paths was compared to the anthropogenic concentration increment (right- vs. left-hand sides of Eq. 1) to determine the accuracy of the formulas. Table 2 gives the mean absolute error and mean bias of the formulas for O<sub>3</sub> and FORM, and Table S3 gives the error and bias for NO<sub>2</sub> and  $HNO_3$ . For comparison, the mean absolute values of the increments  $\Delta O_3$ ,  $\Delta FORM$ , ΔNO<sub>2</sub>, and ΔHNO<sub>3</sub> are 34.9, 1.52, 7.67, and 16.0 ppb, respectively. Though they use

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the same number of points, there is a large reduction in error and bias from TR2 to GL2s or GL2r, indicating the significant advantage of the GL formulas. As the number of points included in the GLns or GLnr formulas increases, the error decreases for  $O_3$ , FORM, and  $NO_2$  and generally the bias as well. There are some exceptions to this trend for  $HNO_3$ , but these occur for cases where the error and bias are already quite low (average error < 4% of the average increment). For  $O_3$  and the Diag path, the GLnr formula gives more accurate results than the GLns formula for 2 or 3 points and essentially the same accuracy for 4 points. For FORM, the GLnr formula is always more accurate than the GLns formula. The GLnr formula is usually less accurate than the GLns formula for  $NO_2$  and  $HNO_3$  and for  $O_3$  with the NOxF and VOCF paths.

Table 2 also shows that the accuracy of a formula is lower for the VOCF path than the other paths when using the same number of points. This difference can be understood by examining the integrand in Eq. (4). Figure 3 displays the integrands for allocating  $\Delta O_3$  to sources at the time of peak  $O_3$  on day 3, when it is most difficult to obtain good agreement between the sum of the source contributions and  $\Delta O_3$ . Along the Diag and NOxF paths, the integrands have a constant curvature, either positive (Diag) or negative (NOxF), and the integrands are mainly positive, with only small negative values near s=1. However, along the VOCF path, 4 of the integrands have positive curvature from s=0 to  $s=\sim0.5$  and then negative curvature for the remainder of the path. Also, the integrands vary over a wider range along the VOCF path than the other paths. Further, the integrands for on-road vehicles and fuel combustion are both positive and negative, resulting in the cancellation of contributions to the integrals from different sections of the path. The change in curvature, wider range of variation and especially the cancellation of contributions require more points on the VOCF path to obtain an accurate integration.

Overall, the GL3r formula for the Diag path and the GL4s formula for the other paths give quite accurate results and were used to calculate the source apportionments in Sect. 4.2. Figure S2 gives a comparison of the sum of the source contributions vs.  $\Delta O_3$ ,

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ΔFORM, ΔNO<sub>2</sub>, and ΔHNO<sub>3</sub> at each hour of the simulation. The plots show again that the largest errors occur for the VOCF path.

#### Source apportionments

Figure 4 presents the apportionment of ΔO<sub>3</sub> to the 5 source categories and 4 emission species using the Diag path. The VOC contributions are always positive, and the largest contributions are from industrial sources and on-road and non-road vehicles. The NO<sub>x</sub> contributions are small and primarily negative on day 1, when the atmospheric  $VOC/NO_x < 7.5 \text{ ppbC ppb}^{-1}$  in the base case. Under these conditions,  $NO_x$ emissions tend to inhibit O<sub>3</sub> formation, and hence the contributions are negative. On day 2, however, the NO<sub>x</sub> contributions become positive and then increase from day 2 to day 3. The total of the NO<sub>v</sub> contributions from all sources at 42 h is essentially the same as the total VOC contribution, and at 66 h, the total NO<sub>v</sub> contribution is twice the total VOC contribution. The increasing importance of the  $NO_x$  contributions is due to the increasing VOC/NO<sub>x</sub>, which is 10-20 ppbC ppb<sup>-1</sup> after 36 h, resulting in NO<sub>x</sub>-limited 15 O<sub>3</sub> formation.

Other methods for source apportionment assign O<sub>3</sub> only to VOC and NO<sub>x</sub> emissions and thereby likely include any contributions of CO and HONO emissions with the VOC and NO<sub>x</sub> emissions, respectively. However, the PIM can separate the contributions of all emission species. Figure 4 shows that the CO contributions from on-road and non-road vehicles are not negligible compared to the VOC contributions of these sources. For onroad vehicles, the CO contributions are generally 20-45% of the VOC contributions, and for non-road vehicles, 10-30%. HONO emissions are assigned only to on-road and non-road vehicles and are small (0.8 % of NO<sub>v</sub>, Table 1). For both of these sources, their HONO emissions contribute < 0.35 ppb to the  $\Delta O_3$ .

Figure 5 displays the source contributions to  $\Delta O_3$  obtained with the 3 paths. (The contributions of all emission species from a source are combined together.) Results for the Diag and NOxF path are similar. For these paths, on-road vehicles have the largest

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and non-road vehicles the second-largest contributions during most of the simulation, and the "other" category contributes < 3 ppb to  $\Delta O_3$ . However, industrial sources are more important than fuel combustion for the Diag path and the reverse is true for the NOxF path. The source contributions to ΔHNO<sub>3</sub> for the VOCF path are distinctly differ-5 ent. Over most of the simulation, the ranking of the contributions is industrial sources > non-road vehicles > on-road vehicles, the opposite of the Diag path. Also, fuel combustion has a negative contribution over the entire simulation and the other category has a larger contribution (up to 6.5 ppb) than for the Diag and NOxF paths.

The different results for the VOCF path can be explained by the fact that the NO, emissions are controlled last on this path or, in terms of the integration, essentially only NO<sub>x</sub> emissions are added near s = 0. The sensitivity of O<sub>3</sub> to these emissions is large and positive near s = 0 (Fig. 3) because the VOC/NO<sub>x</sub> ratio is high in the background case. However, the VOC/NO<sub>x</sub> ratio decreases rapidly as s increases along the VOCF path, the sensitivity to NO<sub>v</sub> emissions becomes negative, and O<sub>3</sub> formation becomes VOC-limited for most of the path. Thus, fuel combustion has a negative source contribution because its emissions are mostly NO<sub>x</sub>, and industrial sources have the largest positive contribution because they have the largest VOC emissions. Also, nonroad vehicles have a larger contribution than on-road vehicles because both sources have a similar magnitude of VOC emissions but on-road vehicles have 82 % more NO, emissions, which suppress O<sub>3</sub> formation on the VOC-limited section of the path.

The source contributions to ΔFORM for the 3 paths are also in Fig. 5. For the Diag path, the relative importance of the sources on days 2 and 3 is the same for ΔFORM as for  $\Delta O_3$ , and this is also true for the NOxF path. For the VOCF path, the on-road and non-road vehicles contribute more to  $\Delta$ FORM than the industrial sources, but the reverse is true for the contributions of these sources to ΔO<sub>3</sub>. The on-road and non-road vehicles have the largest contributions to ΔFORM on each path because these sources have the largest primary FORM emissions and the largest emissions of olefins, which are important precursors to secondary FORM from oxidation reactions (Table S2).

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Figure S3 contains the apportionment of  $\Delta NO_2$  and  $\Delta HNO_3$  to sources. The source contributions to  $\Delta NO_2$  for the Diag and NOxF paths are quite similar; those for the VOCF path differ in that the contributions of the industrial sources and other category are primarily negative after 18 h. The source contributions to  $\Delta HNO_3$  for the Diag and NOxF paths are again quite similar, and the ranking of the sources in importance is the same as the ranking of their  $NO_x$  emissions. The source contributions for the VOCF path are similar to those for the other paths except that the contributions of non-road vehicles and fuel combustion are reversed in importance. The reversal is likely due to the much larger VOC emissions from non-road vehicles, which would enhance the oxidation of  $NO_x$  on the VOC-limited part of the path.

#### 5 Conclusions

As shown in Sect. 4, the PIM can allocate the difference in concentration between two simulations to emission sources. Consequently, the PIM ensures that the anthropogenic increments to  $O_3$  and the other species are neither over- nor under-allocated to the anthropogenic sources (within the accuracy of the numerical integration). Another advantage is that the PIM is based on an exact mathematical relationship that is independent of the chemistry or model and does not require added relationships or approximations. The PIM allows source contributions to be either positive or negative. If the secondary pollutant formation is inhibited by emissions of some species, source, or geographic area, the sensitivity to these emissions will be negative for at least some values of the scaling parameter  $\lambda_m$ , and the integral in Eq. (2) may be negative.

Once a model has been modified to calculate the first-order sensitivities, the PIM requires only very simple post-processing of model results, specifically, calculating a linear combination of sensitivities from different simulations. This can be readily done with existing post-processing packages such as the Package for Visualization of Environmental data (PAVE) or the Visualization Environment for Rich Data Interpretation (VERDI) (Univ. of North Carolina, 2004, 2014). The PIM is not focused on just one

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species, e.g.,  $O_3$ . The calculations needed to allocate  $\Delta c_j$  for species i also generate all the information needed to allocate  $\Delta c_j$  for any other species j predicted by the model, and there is minimal additional effort needed to allocate  $\Delta c_j$  for the second and subsequent species. Finally, the PIM highlights the importance of the background simulation. For a simulation with anthropogenic emissions included to be useful in designing emission controls, there is an implicit assumption that a simulation without the anthropogenic emissions gives concentrations consistent with estimates for clean air. The concentrations in the background simulation can be determined by an actual simulation or by subtracting the source contributions from the base-case concentrations.

In principle, there is an infinite number of source apportionments available from the PIM. However, each source apportionment is linked to an emission-control strategy. If a control strategy is defined along with the timing of the controls, the number of source apportionments is reduced to just one.

The major disadvantage of the PIM is that it requires more computational effort than other methods because the sensitivities must be determined at several emission levels between the base and background simulations. This disadvantage is mitigated, to some degree, because the additional simulations provide information on how concentrations and sensitivities will change along the emission-control path.

The PIM has been applied in this work to a simplified configuration of CAMx that includes the nonlinear chemistry but not transport or dispersion. However, transport and dispersion do not involve nonlinear interactions among the species. Because the nonlinear dependence of the sensitivities on the integration variable (Fig. 3) is driven by the nonlinear chemistry and a full 3-D configuration should not have any other sources of nonlinearity, the number of integration points required for PIM for a 3-D configuration should be similar to the number required for the simplified configuration (3 or 4).

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Application of the PIM to the special case involving the Taylor series expansion, input data and emissions for the model simulations, accuracy in allocating ΔNO<sub>2</sub> and ΔHNO<sub>3</sub> to sources using different integration formulas, comparison of the sum of the source contributions to the anthropogenic increment at each hour, and source contributions to  $\Delta NO_2$  and  $\Delta HNO_3$ .

The Supplement related to this article is available online at doi:10.5194/gmdd-7-9079-2014-supplement.

#### References

- Bowman, F. M.: A multi-parent assignment method for analyzing atmospheric chemistry mechanisms, Atmos. Environ., 39, 2519-2533, 2005.
  - Bowman, F. M. and Seinfeld, J. H.: Ozone productivity of atmospheric organics, J. Geophys. Res., 99, 5309-5324, 1994.
  - Cohan, D. S., Hakami, A., Hu, Y., and Russell, A. G.: Nonlinear response of ozone to emissions: source apportionment and sensitivity analysis, Environ. Sci. Technol., 39, 6739-6748, 2005.
  - Dunker, A. M.: Efficient calculation of sensitivity coefficients for complex atmospheric models, Atmos. Environ., 15, 1155-1161, 1981.
  - Dunker, A. M.: The decoupled direct method for calculating sensitivity coefficients in chemical kinetics, J. Chem. Phys., 81, 2385-2393, 1984.
- Dunker, A. M., Yarwood, G., Ortmann, J. P., and Wilson, G. M.: The decoupled direct method for sensitivity analysis in a three-dimensional air quality model- implementation, accuracy, and efficiency, Environ. Sci. Technol., 36, 2965-2976, 2002a.
  - Dunker, A. M., Yarwood, G., Ortmann, J. P., and Wilson, G. M.: Comparison of source apportionment and source sensitivity of ozone in a three-dimensional air quality model, Environ. Sci. Technol., 36, 2593-2964, 2002b.
  - efunda: available at: http://www.efunda.com/math/num integration/findgausslegendre.cfm (last access: 29 January 2014), 2014.

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- ENVIRON: Comprehensive Air Quality Model with Extensions, available at: http://www.CAMx.com (last access: 15 May 2013), 2013.
- Isaacson, E. and Keller, H. B.: Analysis of Numerical Methods, John Wiley, New York, 1966.
- Kaplan, W.: Advanced Calculus, Addison-Wesley, Reading, Massachusetts, 1959.
- Koo, B., Dunker, A. M., and Yarwood, G.: Implementing the decoupled direct method for sensitivity analysis in a particulate matter air quality model, Environ. Sci. Technol., 41, 2847–2854, 2007.
  - Koo, B., Wilson, G. M., Morris, R. E., Dunker, A. M., and Yarwood, G.: Comparison of source apportionment and sensitivity analysis in a particulate matter air quality model, Environ. Sci. Technol., 43, 6669–6675, 2009.
  - Koo, B., Chien, C.-J., Tonnesen, G., Morris, R., Johnson, J., Sakulyanontvittaya, T., Piyachaturawat, P., and Yarwood, G.: Natural emissions for regional modeling of background ozone and particulate matter and impacts on emissions control strategies, Atmos. Environ., 44, 2372–2382, 2010.
  - Kwok, R. H. F., Napelenok, S. L., and Baker, K. R.: Implementation and evaluation of PM<sub>2.5</sub> source contribution analysis in a photochemical model, Atmos. Environ., 80, 398–407, 2013.
  - Marmur, A., Park, S.-K., Mulholland, J. A., Tolbert, P. E., and Russell, A. G.: Source apportionment of PM<sub>2.5</sub> in the southeastern United States using receptor and emissions-based models: conceptual differences and implications for time-series health studies, Atmos. Environ., 40, 2533–2551, 2006.
  - Mysliwiec, M. J. and Kleeman, M. J.: Source apportionment of secondary airborne particulate matter in a polluted atmosphere, Environ. Sci. Technol., 36, 5376–5384, 2002.
  - Napelenok, S. L., Cohan, D. S., Hu, Y., and Russell, A. G.: Decoupled direct 3D sensitivity analysis for particulate matter (DDM-3D/PM), Atmos. Environ., 40, 6112–6121, 2006.
- Pierce, T., Geron, C., Bender, L., Dennis, R., Tonnesen, G., and Guenther, A.: Influence of increased isoprene emissions on regional ozone modeling, J. Geophys. Res., 103, 25611– 25629, 1998.
  - Simon, H., Beck, L., Bhave, P. V., Divita, F., Hsu, Y., Luecken, D., Mobley, J. D., Pouliot, G. A., Reff, A., Sarwar, G., and Strum, M.: The development and uses of EPA's SPECIATE database, Atmospheric Pollution Research, 1, 196–206, 2010.
  - Stein, U. and Alpert, P.: Factor separation in numerical simulations, J. Atmos. Sci., 50, 2107–2115, 1993.

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- Tao, Z., Larson, S. M., Williams, A., Caughey, M., and Wuebbles, D. J.: Area, mobile, and point source contributions to ground level ozone: a summer simulation across the continental USA, Atmos. Environ., 39, 1869–1877, 2005.
- Tong, D. Q. and Mauzerall, D. L.: Summertime state-level source-receptor relationships between nitrogen oxides emissions and surface ozone concentrations over the continental United States, Environ. Sci. Technol., 42, 7976–7984, 2008.
- University of North Carolina, Package for Analysis and Visualization of Environmental Data, version 2.3, available at: http://www.ie.unc.edu/cempd/EDSS/pave\_doc/EntirePaveManual. html, (last access: 17 November 2014), 2004.
- University of North Carolina, Visualization Environment for Rich Data Interpretation, version 1.5, available at: https://www.cmascenter.org/verdi/, (last access: 17 November 2014), 2014.
  - U.S. EPA: Carbon Bond and SAPRC Speciation Profiles, available at: http://www.cmascenter.org/download/data.cfm (last access: 19 November 2013), 2013a.
- U.S. EPA: 2008 National Emissions Inventory, Version 3, Technical Support Document, September 2013-Draft, available at: http://www.epa.gov/ttn/chief/net/2008inventory.html, (last access: 20 November 2013), 2013b.
- U.S. EPA: CAIR Platform Data, available at: http://www.epa.gov/ttn/chief/emch/temporal/index. html (last access: 24 December 2013), 2013c.
- Wagstrom, K. M., Pandis, S. N., Yarwood, G., Wilson, G. M., and Morris, R. E.: Development and application of a computationally efficient particulate matter apportionment algorithm in a three-dimensional chemical transport model, Atmos. Environ., 42, 5650–5659, 2008.
- Wang, H., Jacob, D. J., LeSager, P., Streets, D. G., Park, R. J., Gilliland, A. B., and van Donkelaar, A.: Surface ozone background in the United States: Canadian and Mexican pollution influences, Atmos. Environ., 43, 1310–1319, 2009.
- Wang, Z. S., Chien, C. J., and Tonnesen, G. S.: Development of a tagged species source apportionment algorithm to characterize three-dimensional transport and transformation of precursors and secondary pollutants, J. Geophys. Res., 114, D21206, doi:10.1029/2008JD010846, 2009.
  - Yang, Y.-J., Wilkinson, J. G., and Russell, A. G.: Fast, direct sensitivity analysis of multidimensional photochemical models, Environ. Sci. Technol., 31, 2859–2868, 1997.
  - Yarwood, G., Morris, R. E., Yocke, M. A., Hogo, H., and Chico, T.: Development of a methodology for source apportionment of ozone concentration estimates from a photochemical grid

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model, in: Proceedings of the 89th Annual Meeting of the Air & Waste Management Association, Air and Waste Management Association, Pittsburgh, PA, Paper 96-TA23A.06, 1996. Yarwood, G., Gookyoung, H., Carter, W. P. L., and Whitten, G. Z.: Environmental Chamber Experiments to Evaluate NO<sub>x</sub> Sinks and Recycling in Atmospheric Chemical Mechanisms, Texas Air Quality Research Program Project 10-042, University of Texas, Austin, 2012.

Zhang, Y., Wang, W., Wu, S.-Y., Wang, K., Minoura, H., and Wang, Z.: Impacts of updated emission inventories on source apportionment of fine particle and ozone over the southeastern US, Atmos. Environ., 88, 133–154, 2014.

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**Table 1.** Summary of daily emission rates used in the base-case simulation.

Species	Emission Rate (molday <sup>-1</sup> km <sup>-2</sup> )						
	Biogenic Sources <sup>a</sup>	Fuel Combustion	Industrial Sources	On-road Vehicles	Non-road Vehicles	Other Sources	
NO	13.5	77.4	19.7	132.9	73.2	1.9	
NO <sub>2</sub>	0.00	8.60	2.19	13.59	7.48	0.21	
НОЙО	0.00	0.00	0.00	1.18	0.65	0.00	
CO	35.9	51.8	58.2	1158.4	683.0	57.0	
VOC	166.8	6.1	244.3	129.9	115.1	59.3	
$VOC/NO_x^b$	29.8	0.09	16.6	1.4	2.4	31.8	

a Includes lightning.

<sup>&</sup>lt;sup>b</sup>  $NO_x = NO + NO_2$ .  $VOC/NO_x$  units are mole C (mole  $NO_x$ )<sup>-1</sup>.

**Table 2.** Average error and bias for different numerical integration formulas. The sum of the source contributions calculated using the formula is compared to the anthropogenic increment of  $O_3$  or FORM.

Path	Formula <sup>a</sup>	Mean Absolute	Mean Bias <sup>b</sup>				
		Error <sup>b</sup> (ppb)	(ppb)				
O <sub>3</sub> Increment							
Diag	TR2	65.93	65.93				
Diag	GL2s	7.38	-7.36				
Diag	GL2r	5.95	5.71				
Diag	GL3s	3.32	-3.30				
Diag	GL3r	1.64	-1.49				
Diag	GL4s	1.51	-1.50				
Diag	GL4r	1.54	-1.49				
NOxF	GL3s	2.20	2.15				
NOxF	GL3r	7.73	-7.67				
NOxF	GL4s	1.57	-1.54				
VOCF	GL3s	7.56	-7.32				
VOCF	GL3r	10.46	9.62				
VOCF	GL4s	4.68	-4.63				
FORM Increment							
Diag	TR2	2.45	2.45				
Diag	GL2s	0.21	-0.20				
Diag	GL2r	0.19	0.19				
Diag	GL3s	0.12	-0.12				
Diag	GL3r	0.04	0.02				
Diag	GL4s	0.05	-0.04				
Diag	GL4r	0.03	-0.02				
NOxF	GL3s	0.11	-0.10				
NOxF	GL3r	0.08	-0.01				
NOxF	GL4s	0.08	0.08				
VOCF	GL3s	0.30	-0.30				
VOCF	GL3r	0.17	0.11				
VOCF	GL4s	0.09	-0.08				

 $<sup>^{\</sup>rm a}$  TR2 = trapezoidal rule, 2 points. GLnx = Gauss—Legendre formula using n points and x as the integration variable.

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<sup>&</sup>lt;sup>b</sup> Hourly average over the 3 day simulation.





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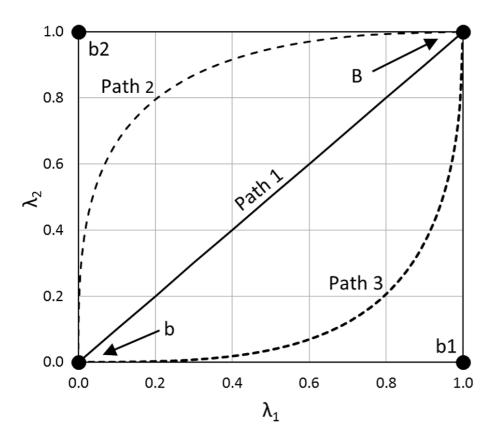


Figure 1. Three possible integration paths when the concentration difference between the base (point B) and background (point b) cases is allocated to two sources with emissions scaled by  $\lambda_1$ and  $\lambda_2$ . Path 1: equal control of emissions from both sources (diagonal path). Path 2: emphasis on control of emissions from source 1 first followed by control of emissions from source 2. Path 3: opposite of Path 2. Points b1 and b2 have the emissions from the background case plus source 1 and source 2, respectively.

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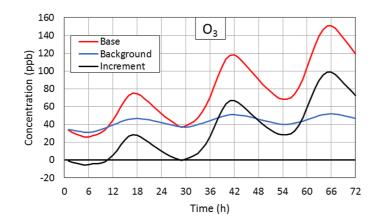
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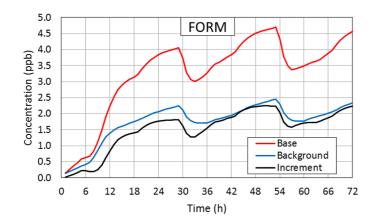


Figure 2. Results from the 2-cell model simulations. Ozone and formaldehyde concentrations for the base case and the background case and the difference between them (anthropogenic increment).



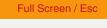
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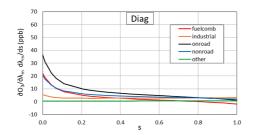
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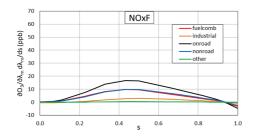


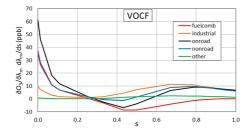


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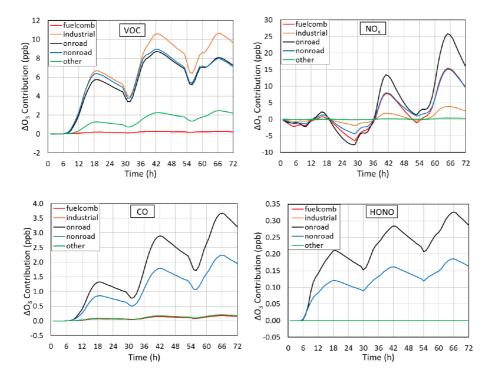








**Figure 3.** Dependence of the integrands for allocating  $O_3$  to sources on the distance s along the Diag, NOxF and VOCF paths. The integrand (Eq. 4) is calculated at the time of peak O<sub>3</sub> on day 3 (66 h).



**Figure 4.** Contributions of sources and VOC,  $NO_x$ , CO, and HONO emissions to the anthropogenic  $O_3$  increment. Results are for the Diag path.

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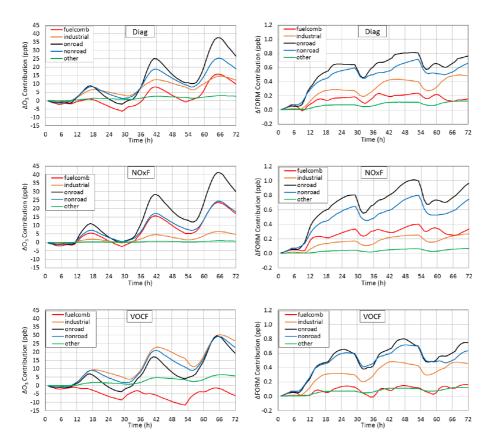
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**Figure 5.** Apportionment of the anthropogenic  $O_3$  increment (left) and the FORM increment (right) to sources using the Diag, NOxF, and VOCF emission-control paths.

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