Dear editor and reviewer,

We thank you for your highly valuable comments. It is our great honor to receive such a careful edit. We have carefully incorporated the referee's comments and suggestions. The point-to-point responses are as follows.

Responses to the comments of Prof. David Webb:

(1) "The standard of English is poor."

[Response]:

Thanks to Prof. Webb for carefully editing our manuscript. Following his suggestions, we have revised the whole paper thoroughly. Almost every sentence of the manuscript has been revised and we learned a lot by following his edit.

In addition, the paper is professionally proof-read for grammatical errors and poor sentence structures. We believe the current version is substantially improved and hope it is suitable for publication.

(2) "There is a lot of repetition and redundant text."

[Response]:

Agreed and now corrected. We removed redundant sentences and reorganized most paragraphs for a more concise presentation. For example, in our previous draft, we repetitively described the optimization of chasing method in Section 4.1(B) and last paragraph of Section 4.1. Following Prof. Webb's suggestions, we now split Section 4.1 into two parts. The first part describes the standard computer improvements and the second describes the optimizations special to the GPU, including the local memory blocking optimization of the chasing method.

(3) The technical description is slanted too much towards computer specialists - who should not need to be told anyway.

[Response]:

We agree and now have shortened the implementation details of communication optimizations (Section 4.2) and I/O optimizations (Section 4.3), as well as the verification of accuracy, which are too much towards the computer specialists. In addition, we have placed the related projects in a table to clearly show their speedups in Section 1 and have added a diagram illustrating the GPU memory architecture in Section 3. With the audience in mind, we further revised large numbers of sentences describing the GPU architecture and the POM.gpu, and tried to make every computer term clear and simple.

We really appreciate your great effort and highly valuable comments. We hope our revised manuscript will be more suitable for the publication of GMD.

Best wishes,

Xiaomeng Huang

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gpuPOM1POM.gpu-v1.0: a GPU-based Princeton Ocean Model

Shizhen Xu¹, Xiaomeng Huang¹, Lie-Yauw Oey^{2,3}, Fanghua Xu¹, Haohuan Fu¹, Yan Zhang¹, and Guangwen Yang¹

¹ Ministry of Education Key Laboratory for Earth System Modeling, Center for Earth System Science, Tsinghua University, 100084, and Joint Center for Global Change Studies, Beijing, 100875, China.

² Institute of Hydrological & Oceanic Sciences, National Central University, Jhongli, Taiwan.
 ³ Program in Atmospheric & Oceanic Sciences, Princeton University, Princeton, New Jersey, USA.

Correspondence to: Xiaomeng Huang (hxm@tsinghua.edu.cn)

Abstract. Rapid advances in the performance of the graphics processing unit (GPU) have made the GPU a compelling solution for a series of scientific applications Graphics Processing Units (GPUs) is an attractive solution in many scientific applications due to its high performance. However, most existing GPU acceleration works for climate models are doing partial code porting for

- 5 certain hot spots, and can only achieve limited speedup for the entire model. In this work, we take conversions of climate models use GPUs for only a few computationally intensive regions. In the present study, we redesign the mpiPOM (a parallel version of the Princeton Ocean Model) as our starting point, design and implement a GPU-based Princeton Ocean Model. By carefully considering the architectural features of the state-of-the-art GPU devices, we rewrite the full mpiPOM model
- 10 from the original Fortran version into with GPUs. Specifically, we first convert the model from its original Fortran form to a new Compute Unified Device Architecture C (CUDA-C) version. We take several accelerating methods to further improve the performance of gpuPOM, including optimizing memory access in a single GPU, overlapping communication and boundary operations among multiple-code, then we optimise the code on each of the GPUs, the communications between
- 15 the GPUs, and overlapping input/output (the I/O) between the hybrid Central Processing Unit (CPU)and the GPU. Our experimental results indicate between the GPUs and the Central Processing Units (CPUs). We show that the performance of the gpuPOM new model on a workstation containing 4 GPUs is comparable to that on a powerful cluster with 408 CPU cores standard CPU cores, and it reduces the energy consumption by a factor of 6.8times.

20 1 Introduction

High-resolution atmospheric, oceanic and *for climate modeling remains a climate modelling remain* significant scientific and engineering challenge challenges because of the enormous computing, com-

Model Name	Model Description	Porting Modules to GPU	Speedup
WRF	Weather research and forecasting	WSM5 microphysics	8_
WRF-Chem	WRF chemical	Chemical kinetics kernel	<u>8.5</u>
POP	Parallel ocean program	Loop structures	2.2
COSMO	Consortium for small-scale modelling	Dynamical core	22.7
NIM	Non-hydrostatic icosahedral model	Dynamical core	34
ASUCA	Non-hydrostatic weather model	Dynamical core & physical	<u>80</u>

Table 1. Existing GPU porting work in climate fields. The speedups are normalized to one CPU core.

munication, and storage requirements - With involved. Due to the rapid development of computer architecture, in particular the development of multi-core and many-core techniqueshardware, the com-

- 25 puting power that can be applied to scientific problems has increased exponentially in recent decades. Some parallel computing techniquesParallel computing methods, such as the Message Passing Interface (MPI, Gropp et al. (1999)) and Open Multi-Processing (OpenMP, Chapman et al. (2008)) have been widely used to support the parallelization of numerous-climate models. Moreover, as modern massive supercomputers become more and more heterogeneous because of the increasing number of
- 30 different accelerating However, supercomputers are becoming increasingly heterogeneous involving devices such as the GPU , the Intel many integrated core and the Intel Many Integrated Core (Intel MIC) and reconfigurable computing based on field programmable gate array (FPGA), and new approaches are required to more effectively utilize the emerging novel architecture, communication and input/output (I/O) to achieve order-of-magnitude acceleration required for climate models. new
- 35 <u>hardware</u>.

In recent years, a number of scientific codes have been ported to the GPU - Different levels of speedup were achieved as shown in Table 1. Most existing GPU acceleration codes for climate models using GPUs. Michalakes and Vachharajani (2008) accelerated a computationally intensive microphysics process of the are only operating on certain hot spots of the program, leaving a

- 40 significant portion of the program still running on CPUs. The speed of some subroutines reported in the Weather Research and Forecast (WRF) model with a speedup of nearly 25x; but the entire WRF model is sped up by (Michalakes and Vachharajani, 2008) and WRF-Chem(Linford et al., 2009) is improved by a factor of approximately 8 whereas the whole model achieves limited speedup because of partial porting. The speed of POP (Zhenya et al., 2010) is improved by a factor of only 1.23x.
- 45 Shimokawabe et al. (2010) fully accelerated the ASUCA model a non-hydrostatic weather model on 528 Nvidia Tesla GT200 GPUs and achieved a speedup of 80x. Linford et al. (2009) accelerated a computationally intensive chemical kinetics kernel from the WRF model with Chemistry on an Nvidia Tesla C1060 and achieved a speedup of 8x. Leutwyler et al. (2014) accelerated a full huge operational weather forecasting model COSMO and achieved 2.8X speedup for its dynamic core.
- 50 Carpenter et al. (2013) accelerated the spectral element dynamical core of the Community Earth

System Model (CESM) using the GPU by 3x. Govett et al. (2010) ported the dynamics portion of the Non-hydrostatic Icosahedral (NIM) model to the GPU and achieved a speedup of 34x.Zhenya et al. (2010) adopted 2.2 because the model only accelerated a number of loop structures using the OpenACC Application Programming Interface (OpenACC API), which used simple compiler directives to accelerate some

55 hot-spot functions, to accelerate the parallel ocean program (POP) by 2.2x.

Most existing GPU acceleration projects for climate models are only working on certain hot spots of the program, leaving a significant part of the program still running on CPUs. Therefore, there are usually frequent data exchange between CPUs and GPUs, which significantly reduces the overall performance. The speed of COSMO(Leutwyler et al., 2014), NIM(Govett et al., 2010) and

60 ASUCA(Shimokawabe et al., 2010) are greatly improved by multiple GPUs. We believe that the elaborate optimization of the memory access of each GPU and the communication between GPUs can further accelerate these models.

The objective of our study is was to shorten the high computation time of high-resolution ocean models by parallelizing their the Princeton Ocean Model (POM) by parallelizing its existing model

- 65 structures using the GPU. Taking the parallel version of the Princeton Ocean Model (mpiPOM)as an example, we demonstrate how to parallelize code an ocean model to make it run efficiently on a so that it runs efficiently on GPU architecture. Using the state-of-the-art GPU architecture, we We first convert the mpiPOM from its original Fortran version into a new Compute Unified Device Architecture C (CUDA-C) version, POM.gpu-v1.0. CUDA-C is the dominant programming language
- 70 for GPUs. We call the new version gpuPOM1.0. Then, we design and implement several optimizing methods: (i) computation optimization in a single GPU; (ii) communication optimization among multiple GPUs, and (iii) I/O optimization between a hybrid GPU and CPU.

In terms of computing, we concentrate on memory access optimization and making better use of caches in GPU memory hierarchy. We improve memory usage by using read-only data cache,

75 local memory blocking, loop fusion, function fusion and that disables error-correcting code memory (Error Checking Correction, ECC memory). The experimental results demonstrate that high memory access optimization can achieve a speedup of approximately 100x when comparing a single GPU against a single CPU core.

In terms of communication, we concentrate on the overlapping between the inner-region computation and the outer-region communication and update. With the GPUDirect communication technology, multiple GPUsin one node can communicate directly and bypass the CPU. In addition, with the fine-grained control of the CUDA streams and its priority, inner-region computation can be executed concurrently with outer-region communication and updating.

In terms of I/O, we choose to split the MPI communicator into computation and then optimise 85 the code on each of the GPUs, the communications between the GPUs, and the I/O processes. One individual computation process and one individual I/O process are attached to one GPU. The computation process is responsible for launching kernels on the GPU and the I/O process is responsible for data copy back from the GPU and to write on disk. The computing process and the I/O process execute concurrently.between GPUs and the CPUs to further improve the performance of POM.gpu.

90

To understand the accuracy, performance and scalability of the gpuPOM, we build a customized POM.gpu code, we customized a workstation with four GPU-Nvidia K20X devices inside. The experimental GPUs. The results show that the performance of the gpuPOM-POM.gpu running on this workstation is comparable to that on a powerful cluster with 408 standard CPU cores.

- 95 The This paper is organized as follows. In Section 2, we review the mpiPOM model. In Section 3, we briefly introduce the GPU computing model. In Section 4, we present detailed techniques about computation optimization in a single GPU, communication optimization among multiple GPUs, and I/O optimization between a hybrid GPU and CPU. We provide the corresponding experimental results about the detailed optimization techniques. In Section 5, we report on the correctness, per-
- 100 formance and scalability in Section 5 of the model. We present the code availability in Section 6 and conclude our work in Section 7.

2 The mpiPOM

The mpiPOM is a parallel version of the Princeton Ocean Model (POM) that is based on MPIPOM. It retains most of the physics package of the original POM (Blumberg and Mellor, 1983, 1987; Oey

- 105 et al., 1985a, b, c; Oey and Chen, 1992a, b), but includes also and includes satellite and drifter assimilation schemes from the Princeton Regional Ocean Forecast System (Oey, 2005; Lin et al., 2006; Yin and Oey, 2007), as well as more recently advanced features such as wind-wave induced Stokes drift, stokes drift and wave-enhanced mixingand Localized Ensemble Transform Kalman Filter (Oey et al., 2013; Xu et al., 2014). The POM
- 110 code was reorganized and MPI the parallel MPI version was implemented by Jordi and Wang (2012) using a two-dimensional data decomposition of the horizontal domainwith a halo of ghost cells. The MPI is a standard library for message passing and it is widely used to develop parallel programs. The POM is a powerful ocean model that has been used in a wide range of applications: circulation and mixing processes in rivers, estuaries, shelf and slope, shelves, slopes, lakes, semi-enclosed seas and
- open and global oceans. It is also at the core of various real-time ocean and hurricane forecasting systems, for examples: Japan e.g., the Japanese coastal ocean and Kuroshio (Isobe et al., 2012); Adiratic current (Miyazawa et al., 2009; Isobe et al., 2012; Varlamov et al., 2015); the Adriatic Sea Forecasting System (Zavatarelli and Pinardi, 2003); the Mediterranean Sea forecasting system (Korres et al., 2007); the GFDL Hurricane Prediction system (Kurihara et al., 1995, 1998), the US' Hur-
- 120 ricane Forecasting System (Gopalakrishnan et al., 2010, 2011) and the Advanced Taiwan Ocean Prediction system (Oey et al., 2013). Additionally, the model has been used to study various geophysical fluid dynamical processes (e.g. Allen and Newberger, 1996; Newberger and Allen, 2007a, b; Kagimoto and Yamagata, 1997; Guo et

Allen and Newberger, 1996; Newberger and Allen, 2007a, b; Kagimoto and Yamagata, 1997; Guo et al., 2006; Oey et al., 2003; Za For a more complete list, please visit the POM website (http://www.ccpo.odu.edu/POMWEB).

- 125 The mpiPOM experiment that is used in this paper is one of the two two that were designed and tested by Professor Oey and students; the codes and results are freely available at the FTP site (ftp://profs.princeton.edu/leo/mpipom/atop/tests/). The reader can see refer to Chapter 3 of the Lecture Notes lecture notes (Oey, 2014) for more detail. The test case is a dam-break problem in which warm and cold waters are initially separated in the middle of a zonally periodic chan-
- 130 nel $\frac{200 \text{km} \times 50 \text{km} \times 50 \text{m}}{(200 \text{km} \times 50 \text{km} \times 50 \text{m})}$ on an f-plane, with walls at the northern and southern boundaries. Geostrophic adjustment then ensues and baroclinic instability waves amplify and develop into finite-amplitude eddies in 10~20 days. The horizontal grid sizes are 1 km and there are 50 vertical sigma levels. Although the problem is a test case, the code is the full mpiPOM version that is used in the ATOP forecasting system.
- 135 The model solves the primitive equation under hydrostatic and boussinesq Boussinesq approximations. In the horizontal, spatial derivatives are computed either using centered-space centred-space differencing or Smolarkiewicz's positive definite advection transport algorithm (Smolarkiewicz, 1984) on a staggered Arakawa C-grid; both schemes have been tested, but the latter is reported here. In the vertical, the mpiPOM supports terrain-following sigma coordinates and a fourth-order scheme
- 140 option to reduce the internal pressure-gradient errors (Berntsen and Oey, 2010). The mpiPOM uses the time-splitting technique to separate the vertically integrated equations (external mode) from the vertical structure equations (internal mode). The external mode calculation is responsible for updating the surface elevation and the vertically averaged velocities. The internal mode calculation results in updates for updates the velocity, temperature and salinity, as well as the turbulence quantities.
- 145 The three-dimensional internal mode and the two-dimensional external mode are both integrated explicitly using a second-order leapfrog scheme. These two modules are the most computationally intensive kernels of the mpiPOM model.

3 GPU programming model overview

- In this section, we describe the basic GPU architecture in a programmer's perspective and focus on
 how to harness the power of the GPU with NVIDIA's Compute Unified Device Architecture(CUDA)
 , a programming model and computing platform that makes GPU program elegant and simple The
 main computational problem of the mpiPOM is memory bandwidth limited. To confirm this issue, we
 use the runtime performance API tool to estimate the floating point operation count and the memory
 access instruction count, as in Browne et al. (2000). The results reveal that the computational intensity,
- 155 defined as floating point operations per byte transferred to or from memory, of the mpiPOM is approximately 1:3.3, whereas the computational intensity provided by a modern high-performance CPU (an Intel SandyBridge E5-2670) is 7.5:1. Many large arrays are mostly pulled from main

memory and there is poor data reuse in the mpiPOM. In addition, there are no obvious hot spot functions in the mpiPOM, and even the most time-consuming subroutine occupies only 20% of

160 the total execution time. Therefore, porting a handful of subroutines to the GPU is not helpful in improving the model efficiency. This explains why we must port the entire program from the CPU to the GPU.

In the GPU hardware design, there are numerous-

3 GPU computing model overview

- 165 Modern GPUs employ a stream-processing model with parallelism. Each GPU contains a number of stream multiprocessors (SMs)grouped by large numbers of CUDA cores. As an example, the . In this work, we carried out the conversion using four Nvidia's K20X GPU we used has GPUs. Each K20X GPU contains 14 SMs and each SM has 192 CUDA cores for single precision operation. One K20X GPU can achieve 3.93TFlops single precision processors and 64 additional processors for
- 170 double precision. Although the computational capability of each processor is low, one GPU with thousands of processors can greatly boost the performance compared to the CPU. In computing, FLOPS (FLoating-point Operations Per Second) is a measure of computer performance. The theoretical peak performance with single-precision floating point and 250GBof each K20X GPU is 3.93 teraFLOPS (TFLOPS, one trillion floating-point operations per second) for the single precision
- 175 floating-point calculations. In contrast, a single Intel SandyBridge E5-2670 CPU is only capable of 0.384 TFLOPS.

Each pair of GPUs shares 6 Gigabytes (GB) of memory, with the interface having a potential bandwidth of 250 GB/smemory bandwidth. Figure 3 illustrates the memory hierarchy of the K20X GPU. Each SM has its own execution units (CUDA cores, load/store units, special function units),

- 180 warp-schedulers, and various possesses some types of fast on-chip faster memories such as registersmemory such as register, L1 cache/, shared memory and texture cache. Various on-chip caches provides more opportunities to implement memory optimizations on GPU platform. Each SM owns 64K 32 bit registers which are the fastest memory in the GPU memory hierarchyread-only data cache. In GPUs, the register is the fastest memory, of which the size is 256 Kilobytes (KB) for each SM. The shared
- 185 memory and the L1 cache share a 64KB on-chip fast memory and can be configured with artificial options such use the common 64 KB space which can be partitioned as 16/48KB48 KB, 32/32KB 32 KB or 48/16 KB. In addition, there are The 48 KB read-only data cache which add the feature for read-only data in global memory to be loaded through the same cache. is useful for holding frequently used values that remain unchanged during each stage of the processing.
- 190 There are three common methods to port a program from CPU to GPU widely used methods for porting a program to GPUs. The first method uses drop-in libraries provided by CUDA to replace the existing code, such as the work implemented by as in Siewertsen et al. (2012). The second method



Figure 1. The hierarchy of stream, kernel, block, warp and thread.

uses simple OpenACC directive as hints in the original CPU code , such as the work implemented by as in Zhenya et al. (2010). The last method , is the most complex but also the most effective,

195 rewrites the whole program with ; it involves rewriting the entire program using low level CUDA subroutines.

In CUDA , a kernel is a

In CUDA terminology, a kernel is a single section of code or subroutine running on the GPU. Each kernel launch consists of a large number of threads and these The underlying code in a kernel

- 200 is split into a series of threads each of which deals with different data. These threads are grouped into equal size blocks which thread blocks that can be executed independently. Each A thread block is further divided into warps , which consist as basic scheduled units. A warp consists of 32 consecutive threads . Threads in a warp that execute the same instruction simultaneouslyand can be scheduled as a whole unit. Kernel function. Each kernel and data transfer commands command in CUDA has
- 205 an optional parameter "stream ID". If "stream ID" is declared "stream ID". If the "stream ID" is set in code, commands belonging to different streams can be executed concurrently. It is usually used to alleviate the kernel launch overhead of subsequent independent kernelsA stream in CUDA is a sequence of commands executed in order. Different streams can execute concurrently with different priorities. Figure 1 illustrates the hierarchy of these terms.
- 210 At present, there are two CUDA platforms to support CUDA compilers are available for C and Fortranrespectively, which are CUDA-C and CUDA-Fortran. Although CUDA-Fortran compiler

has been available since 2009 and that can bring about less modification to would involve less modification of the mpiPOM code, we still choose chose CUDA-C at the gpuPOM1to convert the POM.gpu-v1.0 because of the following reasons: 1) CUDA-C is free of chargewhile CUDA-Fortran

- 215 for one workstation costs more than \$1000.; 2) Previous work (Henderson et al., 2011) show that , during the porting of Nondydrostatic Icosahedral Model(NIM), the commercial previous work (Henderson et al., 2011) has shown that the CUDA-Fortran compiler does did not perform as well as the manually converted CUDA-C version in some kernels. for some of the kernels during the porting of NIM; 3) The the read-only data cache utilization is not supported in by CUDA-Fortran,
- 220 which is the key optimization of Section 4.1(A). 4.1.2; and 4) We have already had a lot of previous experiences for deep optimizations we have many previous optimisation experiences with CUDA-C.

4 Full GPU acceleration of the mpiPOM

Figure 2 illustrates the flowchart of the gpuPOM.is a flowchart illustrating the structure of POM.gpu. The main difference between mpiPOM and gpuPOM the mpiPOM and the POM.gpu is that the

- 225 CPU in gpuPOM the POM.gpu is only responsible for the initializing work and the outputting and the output work. The gpuPOM begins with POM.gpu begins by initializing the relevant arrays on the CPU host and then copies data from the CPU host CPU to the GPU. The GPU does all the computations, including the external mode, the internal mode, and their interactions. In the 2D external mode loop, the depth-averaged velocity UA, VA and sea surface height are calculated.
- 230 In the 3D internal model loop, the fields such as velocities (U, V), temperature (T), salinity (S), and various turbulence variables are time-stepped forward, then performs all of the model computations. Outputs such as velocity and sea surface height, are copied back to the CPU host and and are then written to the disk at a user-specified time interval.

In our implementation, the 3D arrays of variables are stored sequentially in the order of x, y, 235 z and the 2D arrays are stored in the order of x, y, which is the same as the original code. The vertical diffusion is solved by the tridiagonal solver (the Thomas Algorithm) which is calculated sequentially in the z direction. For simplicity, the grid is divided along x and y directions (2D block decomposition) in all kernel functions. Each GPU thread specifies a (x,y) point in the horizontal

direction and performs all the calculations from surface to bottom. The thread blocks are divided

- 240 as (32,4). In the x direction, the block number should be a multiple of 32 threads to perform coalesced memory access within a warp. In the y direction, we tested many thread numbers, such as 4 and 8, and obtained similar performances. We finally choose 4 because we attempt to obtain more blocks to distribute the workload among stream multiprocessors (SM) more uniformly, and also to obtain enough occupancy (Volkov, 2010). Occupancy is the percentage of threads active per
- 245 multiprocessor the following sections, we introduce the optimizations of the POM.gpu by computation, communication and I/O aspects individually.

For the individual GPUs, we concentrate on memory access optimization by making better use of caches in the GPU memory hierarchy. This involves using read-only data cache, local memory blocking, loop fusion, function fusion, and disabling error-correcting code memory. The test results

250 demonstrate that a single GPU can run the model almost one hundred times faster than a single CPU core.

In the following sections, we introduce the general optimizations of the gpuPOM in a single GPU and the special optimizations of the gpuPOM following the state-of-the-art GPU architecture. Then, we present the design of communications for various processes and multiple GPUs within a node.

255 Finally, we describe the design of terms of communication, we overlapped the sending of boundary data between the GPUs with the main computation. Data is also sent directly between the GPUs, bypassing the CPU.

In terms of I/O, we launched extra MPI processes on the main CPU to output the data. These MPI processes are divided into two categories, the computation processes and the I/O processes. The

260 computation processes are responsible for launching kernels into GPUs and the I/O overlapping for hybrid CPU and GPU architecture. processes are responsible for copying data back from the GPUs and for writing to disks. The computation processes and the I/O processes can execute simultaneously to save output time.

4.1 Computational optimizations in a single GPU

- 265 Managing the significant performance difference between off-chip global memory and on-chip fast memory is the primary concern of a GPU programmer. for GPU computing. The ratio of bandwidth between global memory and shared memory is approximately 1:10. Therefore, data reuse in on-chip cache always needs to be seriously considered. As shown on the right side of Fig. 3, we propose five key optimizations to fully utilize the faster on-chip memory of two classes of optimization,
- 270 including the standard optimization of fusion and the GPU and describe the relationships between the GPUmemory hierarchy and each special optimization of the GPU, to better utilize the fast registers and caches.

4.1.1 Standard optimizations of fusion

Fusion optimization in the following.POM.gpu code includes loop fusion and function fusion. The
 loop fusion merges several loops into one loop and the function fusion merges several subroutines into one subroutine.

(A) Read-only data cache utilization. Effective use of the new 48KB directly-access and Loop fusion is an effective method to store scalar variables in registers for data reuse. As shown in Fig. 4, if the variable drhox(k, j, i) is read several times in multiple loops, we can fuse these loops into

280 one. Therefore, *drhox(k, j, i)* will first be read from the global memory and then repeatedly read from a register. For instance, for the *profg* kernel optimized with loop fusion, the device memory



Figure 2. gpuPOM-POM.gpu flowchart

transactions decrease by 57%, and the running speed of this kernel is improved by 28.6%. The loop fusion optimization can also be applied in a number of mpiPOM subroutines.

Similar to loop fusion, we can also merge functions in which the same arrays are accessed. For
example, the *advv* and *advu* functions in the mpiPOM code are used to calculate the advection terms in horizontal directions, respectively. After merging them into one subroutine, the redundant memory access is avoided. The function fusion can also be applied in which one function is called several times to calculate different tracers. The *proft* function in the mpiPOM code is called twice – one for temperature and one for salinity. Their computing formulas are similar and some common



Figure 3. The memory hierarchy of the K20X GPU and the relationships with each optimizations optimization

```
/*********
                                                       *****
*There exist two loops.
                                                       *These loops can be fused into one
*drhox is visited twice in these loops.
                                                       *to reduce global memory access.
for (k = 1; k < nz-1; k++){
                                                      for (k = 1; k < nz-1; k++)
  drhox[k][j][i] = drhox[k-1][j][i] + A[k][j][i];
                                                        drhox[k][j][i] = drhox[k-1][j][i] + A[k][j][i];
                                                        drhox[k-1][j][i] = drhox[k-1][j][i] * B[k-1][j][i];
}
for (k = 0; k< nz-1; k++){
  drhox[k][j][i] = drhox[k][j][i] * B[k][j][i];
                                                      drhox[k-1][j][i] = drhox[k-1][j][i] * B[k-1][j][i];
}
```

(a)Original CUDA-C code

(b)Optimized CUDA-C code

Figure 4. A simple example of loop fusion.

arrays are accessed. After function fusion, the running speed of the *proft* kernel is improved by 28.8%.

4.1.2 Special optimizations of the GPU

Our special optimizations mainly focus on the improved utilization of the read-only data cache in the K20X GPUcan improve the performance of memory intensive kernels. This feature will

295 be automatically enabled and utilized and the L1 cache on the GPU. It is useful to alleviate the bottleneck of memory bandwidth that is limited by using these fast on-chip caches.

There is a 48KB read-only data cache in the K20X GPU. We can automatically use this as long as eertain conditions are met. We the read-only condition is met. In the POM.gpu, we simply add "const __restrict__" qualifiers to " qualifiers into the parameter pointers in gpuPOM to explicitly

300 allocate the read-only data cache for our program. The "LDG.E" instruction will then appear in the disassembling code, and Nvidia Visual Profiler(NVVP) software will show that the read-only data cache is actually being utilized.

to explicitly direct the compiler to implement the optimization. As an example, consider the calculations of advection and the horizontal diffusion terms. Because mpiPOM adopts the Arakawa

- 305 C-grid, in the horizontal plane, updating the temperature(T) requires the velocity of longitude(u), the update of T(i, j, k) requires the value of u(i, j, k), u(i + 1, j, k), v(i, j, k) and v(i, j + 1, k), in addition to the value of velocity of latitude(v) and the horizontal kinematic viscosity, (*aam*, from four neighboring) on the neighbouring grid points. In one time step, the arrays of kernel, the u and v must be arrays are accessed twice, and the *aam* array must be is accessed four times. Therefore it
- 310 is natural to use the After using read-only data cache to improve the data localityof gpuPOM. This optimization improves the performance of this part, the running speed of this kernel is improved by 18.8%.

(B) Local memory blocking. Cache blocking is a common method to improve data reuse in parallel computing To reuse the data in each thread, we use local memory blocking to pull the data

315 from global memory to the L1 cache. In this method, a small subset of a dataset is loaded into the fast on-chip faster memory (e.g., the L1/L2 cache in the GPU and the CPU) and memory and then the small data block is repeatedly accessed by the program. It is helpful to reduce This method is helpful in reducing the need to access the off-chip with high latency memory(e.g., global memory on the GPU). Because regular global memory access cannot be cached in L1 cache for K20X GPU,

320 the method used here is to pull the data from local memory to the L1 cache.

For the subroutines about . In the subroutines of the vertical diffusion and source/sink terms, the chasing method is used to solve a tridiagonal matrix along the vertical direction for each grid point individually. As shown in Algorithm ??, the 3D temporary arrays in the original code, such as *ce*, *gg*, that store Each thread only accesses its own tiles of row transformation coefficientsare

- 325 streamed from memory. However, these arrays are too large to reside in the cache entirely; code efficiency is therefore decreased. We find that each thread performs a column calculation from surface to bottom and there is no communication. Thus, we declare 1D. As shown in Fig. 5, the arrays ee_new,gg_new in local memory to replace the original 3D global arrays. Their size is equal to the level of ocean, nz 1, which is typically a very small value.
- 330 In the chasing method, these local arrays are accessed twice within one thread, one from the surface (k = 0 to the bottom (k = nz 1) and another from the bottom (k = nz 1 to the surface (k = 0). After blocking the vertical direction arrays in local memory, the L1 cache is fully utilized although some of them may be spilled to global memory. The performance of the subroutines

```
/*****
/*********
                                                           *Each thread pulls its own tile of ee,gg to
*3D arrays ee and gg represent row transformation
                                                           *1D new arrays ee_new, gg_new(local memory).
*coefficients of the chasing method.
                                                           *There two new arrays can be cached in L1 for reuse.
              ********
                                                           for (k = 1; k < nz-2; k++)
                                                          for (k = 1; k < nz-2; k++)
  ee[k][j][i] = ee[k-1][j][i]*A[k][j][i];
                                                            ee_new[k] = ee_new[k-1]*A[k][j][i];
 gg[k][j][i] = ee[k-1][j][i]*gg[k-1][j][i] - B[k][j][i];
                                                            gg_new[k] = ee_new[k-1]*gg[k-1] - B[k][j][i];
for (k = nz-3; k \ge 0; k++)
                                                          for (k = nz-3; k \ge 0; k++)
 uf[k][j][i] = (ee[k][j][i]*uf[k+1][j][i]+gg[k]) * C[k][j][i];
                                                           uf[k][j][i] = (ee_new[k]*uf[k+1]+gg_new[k])*C[k][j][i];
```

(a)Original CUDA-C code

(b)Optimized CUDA-C code

Figure 5. A simple example of local memory blocking.

about vertical diffusion and source/sink terms and the running speed of these subroutines is improved
by 35.3% when using the local memory blocking technique.

A simple example of local memory blocking

- 340 north-south(y), vertical(z), i.e., i, j, k ordering. 2D arrays are stored in i, j ordering. The vertical diffusion is solved using a tridiagonal solver which is calculated sequentially in the z direction. For simplicity, in our kernel functions the grid is divided along x and y. Each GPU thread then specifies an (x, y) point in the horizontal direction and performs all of the calculations from the surface to the bottom. The thread blocks are divided as 32×4 subdomains in the x-y plane. In the x direction, the
- 345 block number must be a multiple of 32 threads to perform consecutive and aligned memory access within a warp (NVIDIA, 2015). In the *y* direction, we tested many thread numbers, such as 4 and 8, and obtained similar performances. We ultimately choose 4 because this value produced more blocks and allowed us to distribute the workload more uniformly amongst the SMs. In addition, 128(=1; k < nz-2; k++){ eekji= eek-1ji*Akji; ggkji= eek-1ji*ggk-1ji-Bkji; } for (k = nz-3; k</p>
- 355 In GPU computing, one is free to choose which arrays will be stored in an on-chip cache. Our experience involves putting the data along the horizontal direction into the read-only cache to reuse

among threads, and putting the data along with vertical direction into the local memory for reuse within one thread.

(C) Loop fusion. Loop fusion is an effective method to store scalar variables in registers for data reuse. Registers are the fastest memory in the GPU memory hierarchy. For example, as shown in Algorithm ??, if the variable *drhox(k, j, i)* must be read several times in multiple loops, we can fuse these loops into one. Therefore, the *drhox(k, j, i)* will be read from the global memory the first time and then repeatedly read from a register. This method can also be applied in a number of the mpiPOM subroutines.

365 Take the kernel *profq* as an example. After rewriting part of source code with loop fusion, the device memory transactions decrease by 57%, while the registers used per thread increase from 46 to 72, as reported in NVVP. Although the occupancy achieved decrease from 61.1% to 42.7%, the performance of this kernel is improved by 28.6%.

A simple example of loop fusion

- (D) Function fusion. Because we can fuse the loops in which the same arrays are accessed, we can also fuse functions in which similar formulas are calculated and the same arrays are accessed. For example, the *advv* and *advu* functions of the mpiPOM calculate advection in longitude and latitude, respectively, and they can be fused into one subroutine. This optimization benefits from the elimination of the redundancy calculations.
- This optimization is also useful for the situation in which one function is called several times
 to calculate different tracers. For example, Furthermore, we improve the *proft* functions of the mpiPOM is called twice once for temperature and once for salinity. Their computing formulas are similar and certain common arrays are accessed; these functions were modified to calculate temperature and salinity simultaneously. The method of Function fusion improves the performance of these functions by 28.8%.
- 385 (E)ECC-off and GPU boost. Because ECC memory consumes some amount of memory bandwidth, we can improve the GPU-global memory bandwidth by disabling the error checking and memory correcting features. Also, the memory bandwidth that can be achieved is improved by Error Checking and memory Correcting(ECC-off), as well as enhancing the clock of SM core. In our implementation, we overclock the default clock of K20X GPUfrom 732 MHz to 784 MHz. The methods of ECC-off
- 390 and GPU booston the GPU(GPU boost). This method improves the performance of the whole application POM.gpu by 13.8%.

4.1.3 Results of the computational optimizations

We divide all the gpuPOM subroutines into different of the POM.gpu subroutines into three categories based on their different computational patterns. As shown in Table 2, in gpuPOM the

395 POM.gpu, we deploy different optimizations in different categories to achieve improved performance these categories to improve the performance of POM.gpu; these categories are now described described as follows.

(1) Category 1: Advection and horizontal diffusion (advadv)

- This category has 6 subroutines, and calculates the advectionand, horizontal diffusion and in the ease of velocity, the the pressure gradient and Coriolis terms . Here in the case of velocity. Here, it is possible to reuse data among adjacent threads, and the subroutines therefore benefit from using the read-only data cacheand shared-memory. Also, At the same time, the variables are calculated in different loops of one function or in different functions , so such that the loop fusion and function fusion optimizations apply are applied to this part as well.
- 405 (2) Category 2: vertical diffusion (verver)

This category has 4 subroutines, and calculates the vertical diffusion. In this part, the chasing method is used in the tridiagonal solver in the k-direction. The main feature is that data is reused the data are accessed twice within one thread, while data is accessed once from k = 0 to k = nz - 1 and once from k = nz - 1 to k = 0 once from the surface to the bottom and again from the bottom to the

410 <u>surface</u>. The subroutines are significantly sped up after grouping the k-direction variable in <u>the</u> local memories.

(3) Category 3: vorticity (vort), baroclinic(barovort), baroclinicity (baro), continuity equation (contcont) and equation of state (state state)

This category is less time consuming than the two categories <u>described</u> above, but it also bene-415 fits from our optimizations. Because there exists data reuse with adjacent data exists reuse among threads, the use of a read-only data cache improves <u>efficiency</u>. For vortdata locality. For the *vort* <u>subroutine</u>, there is data reuse within one thread, and <u>thus the loop</u> fusion improves the <u>efficiency</u><u>data</u> <u>locality</u>.

The main bottleneck of the mpiPOM is memory-bound problem. To confirm this issue, we use the 420 Performance API(Browne et al., 2000) to estimate floating point operation count and the memory access(store/load) instruction count. Results reveal that the computational intensity(flops/byte) of the mpiPOM is around 1:3.3, while the computational intensity provided by SandyBridge E5-2670 CPUs is 7.5:1, and large arrays are mostly streamed from memory and shows little locality. According to the roofline model(Williams et al., 2009), the whole mpiPOM is mainly memory-bounded. In

425 addition, the mpiPOM suffers from a flat profiling results, with even the most time-consuming subroutine just occupying 20% of the total execution time. Namely, there are no obvious hot spot functions in the mpiPOM and porting a handful of subroutines to GPU is not helpful to improve the model efficiency. That is the reason that we need to port the whole program from CPU to GPU.

Subroutines	A-Loop fusion	B-Function fusion	C-Read-only data cache	D-Local memory	E-ECC-off & GPU boost	Speedup
Adv & Hor diff	\checkmark	\checkmark	\checkmark		\checkmark	2.05X
Ver diff	\checkmark	\checkmark		\checkmark	\checkmark	2.82X
Baroclinic Baroclinicity	\checkmark		\checkmark		\checkmark	2.08X
Continuity equequation	\checkmark		-1		\checkmark	1.39X
Vorticity	\checkmark		\checkmark		\checkmark	3.19X
State equequation	\checkmark		\checkmark		\checkmark	1.35X

Table 2. Different subroutines adopt different optimizations in gpuPOM the POM.gpu

To alleviate the memory bound problem, an optimization method that is frequently used is cache blocking. It is usually cache beneficial to use vertical index as the innermost array index(z,x,y ordering). For the mpiPOM with 962 × 722 × 51 test case, one array has 962 × 722 × 4bytes= 2.6MBytes in the x-y plane, while one CPU has a 32KB per-core L1 cache, 256KB per-core L2 cache and 20MB shared L3 caches. Take the chasing method in vertical diffusion terms as an extreme case. If x,y,z ordering is used, in terms of calculation along z-axis, each x-y plane is blocked in L3 cache for

- 435 reuse. When traversing backwards along z, the data needed are all evicted. If z,x,y ordering is used, in terms of calculation along z-axis, each k column data is blocked in L1 cache for reuse. When traversing backwards along z, the data remains valid in L1 cache. Unfortunately, the mpiPOM uses east-west index as the innermost array index. However, for gpuPOM, z,x,y ordering has to be avoided to satisfy GPU memory coalescing, which is also demonstrated in Shimokawabe et al. (2010). We
- 440 make east-west (x) as innermost index(x,y,z ordering). A big difference for memory optimizations between GPU and CPU is that, in GPU, programmers can artificially choose which array to store in cache. Moreover, GPU provides various on-chip caches, such as L1/L2 cache, shared memory, texture cache. Thus, according to how the arrays are used, we can put different arrays in different caches. In the gpuPOM, we have explored a better data placement on different caches for different
- 445 terms, besides conventional cache blocking optimizations.

4.2 Communication optimizations among multiple GPUs

In this section, we present the optimizing strategies used to harness the computing power of for multiple GPUs. With multiple GPUs, the computing domain is divided into smaller blocks than with a single GPU. The performance of GPU computing is faster and the memory requirement for

450 each GPU is reduced. To utilize multiple GPUs, an effective domain decomposition method and communication method should be employed. We split the domain along the *x*-In the mpiPOM, the entire domain is split along the horizontal directions and *y* directions (2-D decomposition) and assign each MPI process for is responsible for the model's computation of one subdomain, following



Figure 6. Data decomposition in gpuPOM the POM.gpu

Jordi and Wang (2012). ThenIn the POM.gpu, we attach the one MPI process to one GPU and send

- 455 messages from one GPU to another. move the complete computation to the GPU. The MPI process is in charge of the computation within each subdomain and of the data transfer between the GPU and main memory. The data transfer between subdomains is handled by the GPUs directly. Shimokawabe et al. (2010) and Yang et al. (2013) proposed some-fine-grained overlapping methods of GPU computation and CPU communication to improve the simulation computing performance. An important
- 460 common issue issue in their work is that the communications between multiple GPUs explicitly require the participation of the CPU. In our current work, we hope to implement the communication to simply bypass the CPU to fully employ in implementing the communication to fully exploit the capability of the GPUGPUs.

State-of-the-art At present, two MPI libraries, such as OpenMPI and MVAPICH2, have announced

- 465 their support for MPI communication directly from GPU memory, which is known provided support for the direct communication from the GPU to the main memory. This capability is referred as CUDA-aware MPI. We tried-attempted to use MVAPICH2 to implement direct communication among multiple GPUsat first. However, we found that the boundary operation and MPI inter-domain communication occupied nearly 1518% of the total runtimeafter GPU porting.
- 470 To Instead, to fully overlap the boundary operations and MPI communications with computation, we adopt the data decomposition method shown in Fig. 6. The data region is decomposed into three partsregions: the inner partregion, the outer part, and the halo part. The outer part includes east/west/north/south part, and the halo part also includes east/west/north/south halos to exchange



Figure 7. The workflow of multiple streams on the GPU. The "inner/east/west/north/south <u>part" region</u>" and "Halo<u>"</u>" refer to <u>the</u> computation and update of <u>the</u> corresponding <u>partregion</u>. "Comm.<u>"</u>" refers to <u>the</u> communication between processes, which implies synchronization.

data with neighbors. In CUDA, a stream is a sequence of commands that execute in order; different
streams can also execute concurrently with different priorities. In region, and a halo region which
exchanges data with its neighbours. In our design, the inner partregion, which is the most timeconsuming part with the largest workload is allocated to "stream 1 in which to execute". The east/west
outer part region is allocated to "stream 2" and the north/south outer part region is allocated to stream
3. "stream 3". In the east/west outer partregion, the width is set to 32 to ensure coalesced consecutive

480 and aligned memory access in a warpto improve performance. The halo part is . All of the halo regions are also allocated to stream 2. "stream 2".

The workflow of multiple streams on the GPU is shown in Fig. 7. The east/west/north/south parts are normal regions are common kernel functions that can run in parallel with the inner part region through different streams. The communication operations between domains are implemented by

- 485 *cudaMemepyAsyne*, which is an asynchronous CUDA memory copyfunction. The corresponding synchronization operation operations between the CPU and the GPU or among the MPI processes are implemented with *cudaStreamSynchronize* function and *MPI_barrier* by a synchronization CUDA function and a MPI barrier function. To hide overlap the subsequent communication by the inner part, with the inner region, "stream 2and" and "stream 3" for the outer part-region have higher
- 490 priority to preempt in preempting the computing resource from "stream 1" at any time.

Current CUDA-aware MPI implementation such as MVAPICH2 is not suitable for the "Comm." part in Fig. 6. We found the two-sided MPI functions *MPI_Send* and *MPI_Recv* will block the current stream so that the concurrency pipeline is broken. The probable cause is synchronous *cudaMemcpy* function is called in the current implementation of *MPI_Send* and *MPI_Recv*,

495 according to Potluri et al. (2012). Moreover, the implementation of non-contiguous MPI datatype for communication between GPUs is not efficient enough for the gpuPOM. The computation time of many kernels is about a few hundred microseconds to a few milliseconds while MPI latency for our message size is about the same, which means the outer part update and communication can not be fully overlapped.

- 500 From CUDA 4.1, the Inter-Process Communication (IPC) feature has been introduced to facilitate direct data copy among multiple GPU buffers that are allocated by different processes. The IPC is implemented by creating and exchanging memory handles among processes and obtaining the device buffer pointers of others. This feature has been utilised in CUDA-aware MPI libraries to optimise communications within a node. Therefore, we decided to implement the communication among
- 505 multiple GPUs by calling the low-level IPC functions and asynchronous CUDA memory copy functions directly, instead of using high-level CUDA-aware MPI functions. Our communication optimizations among multiple GPUs are mainly implemented with the following two optimizations.

First, we put the phases of creating, exchanging and opening relevant memory handles into the

- 510 initialization phase of the gpuPOM, which is executed only once. This method can remove the overhead of IPC memory handle operations during each MPI communication operation. The *cudaMemepyAsyne* function with the corresponding device buffer pointers of neighbor processes replaces the original MPI functions.
- Second, we take full consideration of the architecture of our platform in which 4 GPUs are connected with two I/O Hubs (IOHs). As illustrated in Fig. ??, there are two Intel SandyBridge CPUs that connect two GPUs. Both the CPUs are themselves connected through Intel QuickPath Interconnect (QPI). Notation ① means that the communications between GPUs are connected with the same IOH support Peer-to-Peer (P2P) access. Notation ② represents the communications in which P2P access is not supported. If MPI0 (context on GPU-0) sends data to MPI2 (context
- 520 on GPU-2), rank 0 must switch its context to GPU-2 temporally and opens the corresponding memory handles to obtain the device buffer pointers of rank 2. For those GPUs that do not support P2P access between one another, we must switch context to the same GPU before opening the corresponding memory handles. We then call regular *cudaMemepyAsync* functions to fulfill data communications. For communications between GPUs on the same IOH, the switching context is
- 525 not necessary. Although the function cudaMemepyAsync is used in the communication of both ① and ②, the NVVP software shows that ① does a device-to-device memory copy that bypasses the CPU, whereas ② does a device-to-host and a host-to-device memory copy that involves the CPU. The 2-D decomposition introduced in Fig. ?? is an example to demonstrate Based on this workflow, the inter-domain communication is overlapped with the computation. The experimental results show
- 530 that our design can easily extend to 8 or more GPUs within one noderemove the communication overhead taken by MVAPICH2.

Communications pattern among multiple GPUs in one node

4.3 I/O optimizations between hybrid GPU the GPUs and CPU the CPUs

The time consumed for I/O in the original mpiPOM is not significant because the output frequency 535 is relatively low. However, after we fully accelerate the model by GPU, the I/O overhead, which is



Figure 8. One computing process and one I/O process both set their contexts on the same GPU. During the data copy phase, the computing process remains idle and the I/O process will copy data from the GPU to the CPU host through the *cudaMemcpy* function.

it accounts for approximately 30% of the total runtime, cannot be ignored. As described in Sec. 4.2, each MPI process sets its context on one GPU and is responsible for launching kernel functions on this GPU, and the CPU is used to collect and output data. In fact, in most climate models, including the mpiPOM, the. The computing phase and the I/O phase run alternately. In a sense, the computing

540 phase and the I/O phase are serial, which means that the GPU will remain idle until the CPU finishes the I/O operations. Huang et al. (2014) designed a fast Motivated by previous work on I/O library for climate models and provided automatic overlapping of I/O and computing. Motivated by their work, we design a method so that computations on overlapping (Huang et al., 2014), we designed a similar method following computations on a GPU and I/O operations on CPU can a CPU to run in 545 parallel.

Because MPI processes are blocked during the output phase and cannot launch kernels to GPUs, we choose In the POM.gpu, we chose to launch more MPI processes. We divide all the MPI processes The MPI processes are divided into computing processes and I/O processes with different MPI communicators. The computing processes are responsible for launching kernel functions as usual, and

the I/O processes are responsible for output. One I/O process attaches to one computing process and 550 these two processes set their contexts on one single GPUthrough cudaSetDevice function. The total number of MPI processes are twice the size they were before. the same GPU.

Since Because the I/O processes must fetch data from the GPU, where the data are allocated by the computing processes, communication is necessary between them. Here, we again utilize the feature

- 555 of CUDA IPC, as introduced in Sec. 4.2. Through CUDA IPC, the The I/O processes obtain the device buffer pointers from the computing processes during the initialization phase. When there is a need to output data writing history files, the computing processes are blocked and kept remain idle for a short time while, waiting for I/O processes to fetch data. Then, the computing processes continue their computation, and the I/O processes complete their output in the background, as illustrated in
- Fig. 8. This method can be further optimized by placing the archive data into a set-aside buffer and 560 carry on the main calculation. However, the method requires more memory, which is not abundant in current K20X GPUs.

The advantage of this method is that it overlaps the I/O on the CPU with <u>computation the model</u> <u>calculation</u> on the GPU. In <u>the</u> serial I/O, the <u>GPU</u> computing processes are blocked while data

- 565 are brought to the host sent to the CPU and written to disk. In the overlapping I/O, the computing processes only wait for the data to be brought sent to the host. In addition, the The bandwidth of data brought to the host through the PCI-express bus is approximately 6 GBpsGB/s, but the output bandwidth to the disk is approximately 100 MBpsMB/s, as determined by the speed of the disk. Therefore, the overlapping method significantly accelerates the entire application.
- 570 The 3 cases when a subroutine is broken into small kernels.

Note that there are more than 50 kernel functions in the current version of gpuPOM. The main reason that we have a large number of kernels in gpuPOM is that there exist numerous subroutines in mpiPOM. Since we port the entire model one subroutine by one subroutine, which is a convenient way to debug the gpuPOM and to guarantee its bit-by-bit identical results to mpiPOM, we need to

- 575 write a large number of GPU kernels. Further more, we break several subroutines of mpiPOM into several GPU kernels of gpuPOM in 3 cases: when subroutine B is invoked in subroutine A(illustrated in Fig. ??(a)), when a MPI function call is invoked in subroutine A(illustrated in Fig. ??(b)), and when interior array is first written by one thread and later read by adjacent threads, in the mean while caching this array in shared memory makes no sense(illustrated in Fig. ??(c)). Although function
- 580 fusion has been done as described in Section 4.1 (D), aggressive function fusion to make use of data locality between functions is a promising optimization(Wahib and Maruyama, 2014). But, a redesign of the code structure of mpiPOM is needed and it is a part of our future work.

5 Experiments

In this section, we first describe the specification of our platform and comparison methods used methodology to validate the correctness of the gpuPOM.POM.gpu. Furthermore, we present the performance and scalability of the gpuPOM on the GPU platform in comparison POM.gpu comparied with the mpiPOMon the CPU platform.

5.1 Platform Setup

- The GPU platform used in our experiments is a super workstation computer POM.gpu runs in a workstation consisting of two CPUs and 4 GPUs, as illustrated in Fig. ??. four GPUs. The CPUs are 2.6 GHz 8-core Intel E5-2670 (architecture code-named SandyBridge), which can turbo to 3.0 GHz when all 8 cores are utilized. The peak single-precision performance of the Intel SandyBridge CPU is 384 GFlops and the peak memory bandwidth is 51.2 GBps. The SandyBridge E5-2670. The GPUs are Nvidia Telsa Tesla K20X, equipped with 2,688 GPU-cores and 6 GB GDDR5 fast
- 595 on-board memory. The peak single-precision performance of K20X GPU is 3.95 TFlops and the peak memory bandwidth is 250 GBps. Therefore, the aggregated performance provided with 4 GPUs can

reach 16 TFlops and 1 TBps memory bandwidth, which is sufficient to execute the general simulation research for regional ocean models thus far. The . The operating system is RedHat Enterprise Linux 6.3 x86_64. The programs on this platform <u>All programs</u> are complied with Intel compiler v14.0.1,

600 <u>CUDA 5.5 Toolkit</u>, Intel MPI Library v4.1.3 and CUDA 5.5 Toolkit. For the purposes of MVAPICH2 v1.9.

For comparison, the CPU platform used in our experiments is mpiPOM runs on the Tansuo100 supercomputer cluster at Tsinghua University , which consists consisting of 740 nodes, each of which has. Each node is equipped with two 2.93 GHz 6-core Intel Xeon X5670 processors CPUs

- and 32 GB of memory. The nodes are connected through an Infiniband network, which provides a maximum bandwidth of 40 Gbps. The node infiniband network. The operating system is Red-Hat Enterprise Linux 5.5 x86_64. All the programs Programs on this platform are compiled with Intel compiler v11.1, and the MPI environment is and Intel MPI v4.0.2. The Original mpiPOM code is benchmarked with its initial compiler flags(compiled with its original compiler flags, i.e.,
- 610 "-O3 -precise) and also with the same Intel compiler. We also use the GPUDirect technology within MVAPICH2 v1.9 to test the communication effects among multiple GPUs, and compare the results with our implementation. -fp-model precise".

5.2 The test case and the verification of accuracy

The "dam break" "dam break" simulation (Oey, 2014) is conducted to verify the correctness and test the performance and the scalability of the gpuPOM.POM.gpu. It is a baroclinic instability problem which that simulates flows produced by horizontal temperature gradients. The model domain is configured as a straight channel with a uniform depth of 50 m. Periodic boundary conditions are used in the east-west direction, and the channel is closed in the north and south. Its horizontal resolution is $\frac{1km \times 1km}{1}$. To test large computational grid, the 1km×1km. The domain size of this test case

- 620 is increased to 962 × 722 horizontal grid points and 51 vertical sigma levels, which is limited by the capacity of on-board one GPU's memory. Initially, the temperature in the southern half of the channel is 15°C and 25°C in the northern half. The salinity is fixed at 35 psu. The fluid is then allowed to adjust. In the first 3-5 days, geostrophic adjustments occurs. Then, an unstable wave develops due to baroclinic instability. Eventually, eddies are generated. Figure 9 shows the sea-
- 625 surface height (SSH), sea-surface temperature (SST), and currents after 39 days. The development of a gravity wave is manifest. Noticeably, The gravity wave is confined in the middle of the channel by Rossby radius deformation. scales of the frontal wave and eddies are determined by the Rossby radius of deformation. This dam break case uses a single-precision format.

To verify the accuracy, we check the binary output files output from the original mpiPOM and 630 the gpuPOM. This testing method is also used in the GPU-porting of ROMs (Mak et al., 2011). As introduced in Whitehead and Fit-Florea (2011), the same inputs will give identical results for individual IEEE-754 operations except in a few special cases. These cases can be classified into





Figure 9. The model results after 39 days of simulation. For the <u>up top</u> figure, <u>eolor the colour</u> shading is the <u>Sea Surface Height sea-surface height (SSH). Vectors</u>, and vectors are ocean <u>currentcurrents</u>. For the <u>low</u> bottom figure, <u>eolor the colour</u> shading is the <u>Sea Surface Temperature sea surface temperature</u> (SST). Several warm and cold eddies are generated in the middle of the domain where the SST gradient is largest. Noticeably, the gravity wave is confined in the middle of the channel ; their scales are determined by the Rossby radius of deformation.

three categories: different operations orders, different instructions and different implementations of math libraries. For the first in our study, the parallelization of the mpiPOM does not change the order of each floating point operation and we benefit from this. For the second case in our study, the GPUs

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have fused multiply-add (FMA) instruction while the CPU does not in our CPU platform.Because this instruction might cause a difference in the numerical results, we disable FMA instructions with the "-fmad=false" compiler flag for the GPUs. For the third case in our study, the value of exponent used in the GPU has a maximum of 2 rounding errors NVIDIA (2014). Fortunately, in the execution

640 path of our dam break simulation, the power of the exponent functions remains unchanged over the entire simulation. Therefore, we accomplish this function on the CPU during the initialization phase and copy the results to the GPU for later data reuse. The experimental of the mpiPOM and the POM.gpu, as in Mak et al. (2011). The test results demonstrate that the output variables regarding variables velocity, temperature, salinity and sea surface height are all identical.

645 5.3 Model Performance

To understand the advantages of the optimizing methods introduced optimizations in Sec. 4, we test the dam break case with different experiments. The current dam break case uses single-precision format. The conducted different tests. The metrics of seconds per simulation day , which is the walltime it requires to obtain 24 hours in the simulation, is measured and used are measured to compare the model performance.

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In the first experiment

5.3.1 Single GPU performance

In our first test, we compare the gpuPOM with the mpiPOM on different hardware platforms, including K20X GPU, the Intel Westmere 6-cores performance of the mpiPOM using two different

- 655 <u>CPUs, the Intel X5670 CPU (6 cores)</u> and the Intel SandyBridge E5-2670 CPU (8 cores), with that obtained from the POM.gpu using one single GPU. Fig. 10 shows that one K20X GPU can compete with approximately 55 Intel SandyBridge CPU cores or E5-2670 CPU cores to 95 Intel Westmere CPU cores . Obtaining such a speedup on a pure CPU platform is reasonable. Taking the SandyBridge CPU platform as an example, the theoretical memory bandwidth of one 8-core
- 660 X5670 CPU cores in the simulation. From the parameters of the Intel E5-2670 CPU is 51.2 GBps, and the peak single-precision floating point performance is 384 GFlops with all 8 cores turbo to 3.0 GHz. However, for and Nvidia K20X GPU, the memory bandwidth and peak single-precision floating point performance are 250 GBps and 3.95 TFlops, respectively. The approximate we find that, the ratio of memory bandwidth between one SandyBridge CPU and one K20X GPU is 1 :
- 665 5, and and the ratio of floating points performance between one SandyBridge CPU and one K20X GPU is are approximately 1:10. Namely, 5 and 1:10, respectively. This means, if an application is strictly memory bound, one K20X bandwidth limited, one GPU can compete with 5 SandyBridge CPUs. In addition, CPUs; if an application is strictly computing boundcomputation limited, it can compete with 10 SandyBridge CPUs. As CPUs. Since the mpiPOM is memory bound, according to
- 670 the memory bandwidth ratio between the CPU and the GPU, our gpuPOM bandwidth limited, the

<u>POM.gpu</u> should provide equivalent performance to 5x8 = 40 CPU cores. Combining our careful memory optimizations, our final design achieves another performance boost of 25%, and one GPU provides similar performance to more than 50 Intel 8-core SandyBridge the mpiPOM running on up to $5 \times 8 = 40$ CPU cores. Compared with Intel Westmere 6-cores CPU, our results provide similar

675 performance to more than 95 CPU cores. Our procedure attempts to optimize memory access and we can further increase this number to 55.

The performance API tool (PAPI) shows that the performance of the gpuPOM on single K20X is 107.3Gflops in single-precision for the 962*722*51 grid size. The low performance in Gflops reflects the memory-bound problem in climate models. Previous work such as time skewing (McCalpin and Wonnacott (1999); Wonnacott (2)

680 can make a stencil computation compute bound by making use of data locality between different time-steps. However, for real-world climate models including mpiPOM, the code is usually tens to hundreds of thousands lines and analyzing the dependency manually is tough. Designing an automated tool to further analyze and optimize the mpiPOM and the gpuPOM is a part of our future work.



Figure 10. Performance comparison with different hardware platforms

685 5.3.2 Multiple GPUs performance

In the second experiment, we test the test, we compare our communication overlapping method used in the gpuPOM and compare it with the MVAPICH2. In the current MVAPICH2, the communication and boundary operations are not overlapping with computing. Library. Fig. 11 shows presents the weak scaling performance of the gpuPOM on multiple GPUs. To maximize performance, where the

690 grid size for each GPU is set to kept at $962 \times 722 \times 51$. When using 4 GPUs with the implementation of are used with MVAPICH2, approximately 18% of the total runtime is consumed in executing the by inter-domain communication and boundary operations. This overhead does not exist in can be greatly reduced by our communication overlapping method. Fig. 11 shows that it spends almost the same time when using different GPUs because the communication and boundary operations are almost fully overlapped with the inner part of the computation.

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Figure 11. The weak scaling test between our communication overlapping method and the MVAPICH2 subroutines.

In the third experiment, we test the efficiency of the gpuPOM on multiple GPUs. Table 3 shows the strong scaling result of the gpuPOM on multiple GPUs. We test, we fix the global grid size at $962 \times 722 \times 51$ and increase the amount of GPUs gradually. The results show, and measure the strong scaling performance of POM.gpu. Table 3 shows that the strong scaling efficiency is 99% on

- 2 GPUs and 92% on 4 GPUs. A smaller subdomain will decrease When more GPUs are used, the size of each subdomain becomes smaller. This decreases the performance of the gpuPOM POM gpu in two aspects. First, communication time can easily the communication overhead may exceed the computation time in the inner part and cannot be overlapped. As the subdomain size decreases, the inner part computation time decreases, but the communication time will not decrease because latency
- 705 is the dominant factor of the inner region as the size of each subdomain decreases. As a result, the overlapping method in Section 4.2 are not effective. Second, the latency of kernel launching and overhead of implicit synchronization after kernel execution will not decrease. There are a series of smallthere are many "small" kernels in the gpuPOM, and the execution time is close to launching latency and synchronization overhead. When the subdomain size decreases, the impact of these
- 710 delays expandsPOM.gpu code, in which the calculation is simple and less time consuming. With fewer inner region computations, the overhead of kernel launching and implicit synchronization with kernel execution must be counted.

Table 3. The strong scaling result of gpuPOMPOM.gpu

Number of GPUs	1-GPU	2-GPUs	4-GPUs
Time(s)	97.2	48.7	26.3
Efficiency	1.00 - <u>100%</u>	0.99-<u>99</u>%	0.92-92%

5.3.3 I/O performance

In the fourth experiment, we test the performance of the test, we compare our I/O overlapping method and compare it with the default with the parallel NetCDF (PnetCDF) method and NO-I/Omethod. NO-I/O means that all I/O operations are disabled in the program and that the time measured is the pure computing time. We simulated the experiment This simulation is run for 20 daysand output , and the history files daily in the netCDF format. The variables included in the output netCDF files are 2-dimensional arrays of size 722 × 482 and 3-dimensional arrays of size 722 × 482 × 51.

- 720 The are output daily. The final history files in NetCDF format are approximately 12 GB. Fig. 12 shows that the I/O overlapping method outperforms the default PnetCDF method. For 1 GPU and 2 GPUs, the overall runtime decreases from1694/from 1694/1142 seconds to 1239/688 seconds, which is close to the NO-I/Omethod. The small difference between our design and. The extra overhead of our method compared with NO-I/O is that involves the computing processes must that need to
- 725 be blocked until the I/O processes bring obtain data from the GPU. For the case of GPUs. When running with 4 GPUs, the output time is longer than computational time because the latter is fast and the I/O time is relatively large such that exceeds the computation time. Then, the I/O phase cannot fully overlap with the computing be fully overlapped with the model computation phase. The overall runtime equals the sum of the computation time and the non-overlapped I/O time.

730 5.3.4 Comparison with a cluster

In the last experiment, we test different workloads with the gpuPOM and compare the results with the mpiPOM on test, we compare the performance of POM.gpu on a workstation containing 4 GPUs with that on the *Tansuo*100 platform. The available global grid size are choosen from the three cluster. Three different high-resolution sets grids (Grid-1: $962 \times 722 \times 51$, Grid-2: $1922 \times 722 \times 51$,

- 735 Grid-3: 1922×1442×51) are used. Fig. 13 shows that our workstation with 4 GPUs is comparable to a powerful cluster with 408 standard CPU cores (= 34 nodes * 12 cores/node) for the simulation of mpiPOM. Since the Thermal Design Power(TDP) in the simulation. Because the thermal design power of one X5670 CPU (6-cores) is 95W-is 95 W and that of one K20X GPU is 235W, it means using 4 GPUs brings 6.8 times less energy consumption compared with 408 CPU cores. Small
- 740 subdomains will decrease the performance of the gpuPOM as discussed in the strong scaling test, but it may greatly benefit the mpiPOM on the CPU. The last level cache of one SandyBridge CPU in



Figure 12. I/O Test test for gpuPOM the POM.gpu

our platform is 20 MB, whereas that of K20X GPU is only 1.5 MB. As the subdomain size for 235 W, we reduce the energy consumption by a factor of 6.8. Theoretically, as the subdomain of each MPI process decreases becomes smaller, the cache hit ratio will increase on a pure CPU platform,

- 745 which can surely improve the performance especially for the memory-bound of the mpiPOM code will increase. This will greatly alleviate the memory bandwidth-limited problem. However, for in the simulation on 408 standard CPU cores, the MPI communication time-may occupy more than 40% of the total execution time. With the number of cores increasing When scaling to over 450 cores, the mpiPOM simulation may instead become slower, the execution time may increase instead, as shown
- 750 in Fig. 13. As a result, our GPU solution has an overwhelming Therefore, for high-resolution ocean modelling, our POM.gpu has a clear advantage compared to the CPU because the communication overhead is less expensive and overlapped original mpiPOM.

6 Code availability availability

The gpuPOM used to simulate the regional ocean dynamic and physical process releases with the

755 <u>The POM.gpu</u> version 1.0 series, which is freely available at . Note that the testing script "is available at https://github.com/hxmhuang/POM.gpu. To reproduce the test case in Section 5, the script "run_exp002.sh" can be downloaded "is provided to compile and execute the codes, and to reproduce the test case.POM.gpu code.



Figure 13. Four GPUs performance Performance test of four GPUs compared with *Tansuo*100 clusters(Intel Westmere CPUs)cluster

7 Conclusions and future work

- 760 In this paper, we provide develop POM.gpu, a full GPU accelerated solution of POM. Unlike partial solution based on the mpiPOM. Unlike previous GPU porting, such as WRF and ROMs, the gpuPOM does all the the POM.gpu code distributes the model computations on the GPU. The main contribution of our work includes a better use of state-of-the-art GPU architecture, particularly regarding the memory subsystem, a new design of a communication and boundary operations overlapping
- 765 approach and a new design of an Our main contributions include: optimizing the code on each of the GPUs, the communications between GPUs, and the I/O overlapping approach. With the process between the GPUs and the CPUs. Using a workstation with 4 GPUs, we achieve over 400x speedup against a single CPU core, and provide equivalent performance to the performance of a power-ful CPU cluster with more than 400 coresand reduce 408 standard CPU cores. Our model also
- 770 reduces the energy consumption by a factor of 6.8times. This work provides . It is a cost-effective and efficient ways in ocean modeling. energy-efficient strategy for high-resolution ocean modelling. We have described the method and tests in details and, with the availability of the POM.gpu code, our experiences may hopefully be useful to developers and designers of other general circulation models.
- 775 In our current POM.gpu, we design a large number of kernel functions because we port the entire mpiPOM one subroutine at a time. This was done to simplify the debugging of POM.gpu and to check that the results are consistent with the mpiPOM. In our future work, we will adjust the code structure of POM.gpu and adopt aggressive function fusion to further improve the performance.

Previous studies proposed to take advantage of data locality between time steps by time skewing

- 780 (McCalpin and Wonnacott, 1999; Wonnacott, 2000), thus transforming the problem of memory bandwidth into the problem of computation. However, the real-world ocean models, including the mpiPOM, often involve hundreds of thousands lines of code, and analysing the data dependency and applying time skewing in such a context are challenging and difficult. We leave that to the next-generation POM.gpu.
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