1 Vertical resolution dependence of gravity wave momentum

2 flux simulated by an atmospheric general circulation model

3 S. Watanabe¹, K. Sato², Y. Kawatani¹, and M. Takahashi³

- 4 [1]{Japan Agency for Marine-Earth Science and Technology, Yokohama, Japan}
- 5 [2]{Department of Earth and Planetary Science, Graduate School of Science, The University
- 6 of Tokyo, Tokyo, Japan}
- 7 [3]{Atmosphere and Ocean Research Institute, The University of Tokyo, Kashiwa, Japan}
- 8
- 9 Correspondence to: S. Watanabe (wnabe@jamstec.go.jp)
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1 Abstract

2 The dependence of the gravity wave spectra of energy and momentum flux on the horizontal 3 resolution and time step of atmospheric general circulation models (AGCMs) has been 4 thoroughly investigated in the past. In contrast, much less attention has been given to the 5 dependence of these gravity wave parameters on models' vertical resolutions. The present study demonstrates the dependence of gravity wave momentum flux (GWMF) in the 6 7 stratosphere and mesosphere on the model's vertical resolution, which is evaluated using an AGCM with a horizontal resolution of about 0.56°. We performed a series of sensitivity test 8 9 simulations changing only the model's vertical resolution above a height of 8 km, and found a 10 global reduction of GWMF with increasing vertical resolution. Inertial gravity waves with short vertical wavelengths simulated at higher vertical resolutions might play an important 11 role in determining GWMF in the summertime stratosphere. The sensitivity test simulation 12 also demonstrated the importance of model's vertical resolution on representing realistic 13 14 behaviors of gravity waves near their critical level. 15

1 **1 Introduction**

2 Due to recent advancements in high-performance computing, simulations of the global 3 atmosphere with sub-kilometer horizontal resolutions have been achieved, allowing 4 convective systems to be resolved (Miyamoto et al., 2013). Considering the global 5 momentum budget in such ultra high-resolution atmospheric models, explicitly resolved 6 gravity waves (GWs) undoubtedly play important roles (Alexander et al., 2010).

7 The dependence of the GW spectra of energy and momentum flux on the horizontal resolution 8 and time step of atmospheric general circulation models (AGCMs) has been studied in 9 considerable depth. Using comprehensive atmospheric general circulation models, Koshyk 10 and Hamilton (2001) and Hamilton et al. (2008) demonstrated the dependence of the 11 horizontal wavenumber spectra of GW energy on the horizontal resolution of the AGCM. Shutts and Vosper (2011) evaluated the dependence of GW energy on the horizontal 12 13 resolution and time step of state-of-the-art numerical weather prediction models. These 14 pioneering works have served as useful guidance to other modeling disciplines.

15 In contrast, much less attention has been given to the dependence of the GW parameters on the vertical resolution of the AGCM. At present, only a few AGCMs have achieved sub-16 17 kilometer vertical resolution coverage throughout the middle atmosphere, which is believed to 18 be crucial for accurately reproducing GW-related processes such as generation, propagation, 19 dissipation, and mixing. Among such high-vertical-resolution AGCMs, the model developed 20 for the KANTO project had the highest vertical resolution of 300 m, which was actually 21 determined based on an expert judgment rather than a sensitivity test approach (Watanabe et al., 2008). The main purpose of the present study is to clarify the dependence of GW 22 23 momentum flux on the vertical resolution of the model, with the aim of elucidating the optimum vertical resolution. 24

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26 2 Model and experimental design

The model used in the present study was JAGUAR (Japanese Atmospheric General circulation model for Upper Atmosphere Research) (Watanabe and Miyahara, 2009). The vertical domain of this model extends from the Earth's surface to a height of about 150 km, although the present study focused on just the first 80 km. The horizontal resolution was set to 0.56°, which is the same as that used by Watanabe et al. (2008) and Watanabe and Miyahara

(2009). This horizontal resolution allows the model to resolve GWs with horizontal 1 2 wavelengths larger than ~ 190 km. Considering the fact that the GWs observed in the mesosphere and lower thermosphere frequently include components with horizontal 3 4 wavelengths in the order of 10 km, the present model did not cover the full range of GW 5 spectra. Note, however, that a series of studies has suggested that the model qualitatively reproduces the seasonal and interannual variations of large-scale thermal and wind structures, 6 7 behaviors of explicitly resolved GWs and vertically fine structures of the extratropical 8 tropopause layer (Watanabe et al., 2008, 2009; Tomikawa et al., 2008, 2012; Kawatani et al., 9 2010a & b; Sato et al., 2009, 2012; Miyazaki et al., 2010a & b).

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11 In the present study, we performed a series of sensitivity test simulations changing only the 12 model's vertical resolution above 8 km. Vertical resolutions of dz = 200 m, 300 m, 400 m, 500 m, and 1000 m were used (Figure A1). The vertical resolution below 8 km remained 13 14 unchanged. (Changing the vertical resolution in the lower troposphere is known to have 15 significant effects on the behaviors of physical parameterizations such as cumulus convection 16 and boundary layer processes, but these are not addressed in the present study.) The vertical 17 resolutions used in the KANTO project and the previous JAGUAR study were 300 and 500 m, 18 respectively. The main focus in this study was GW momentum flux at northern summer mid-19 latitudes, where the short-term variability of planetary-scale and synoptic-scale waves is 20 relatively small. This condition is important because it is preferable for GW source 21 distribution (e.g., diabatic heating and jet-front systems) in the troposphere to be similar in 22 each run, to a qualitative degree at the very least.

23 Due to the limited computational resources available for this study, we only performed a 24 short-term deterministic forecast-type experiment starting from virtually the same initial 25 condition as in the original (control) simulation. The original initial condition at 00:00 UT on 26 June 21 was taken from a run using dz = 500 m, which had been spun-up for several years and 27 well reproduced large-scale thermal and wind structures in the middle atmosphere. That initial 28 condition was vertically interpolated into the dz = 200 m, 300 m, 400 m, and 1000 m runs, 29 each of which was performed for the week of June 21-27. The time step was set to 30 s in 30 every run.

Meteorological fields, e.g., winds, temperatures, and precipitations, were output every 30 min as 30-min averages, and GW components were extracted using a high-pass filter based on the spherical harmonics with a cut-off horizontal wavelength of about 950 km, i.e., wavelengths shorter than 950 km were extracted (Watanabe et al., 2008). GW momentum flux is referred to as GWMF hereafter for simplicity. This paper focuses on the net vertical flux of eastward momentum associated with the GW components, because it is of primary importance in the momentum budget in the middle atmosphere.

6 Both the chaotic behavior of the fluid system and the difference in the vertical resolution 7 resulted in different evolutions of the synoptic motions and GW distributions. However, as 8 will be shown later, the differences in the simulated GWMF in the middle atmosphere caused 9 by the vertical resolution were significant. Since the simulated GW field requires only a few 10 days for initial spin-up, i.e., to generate, propagate, and fill the stratosphere (Hamilton et al., 11 2008; Shutts and Vosper, 2011) the present work mainly focused on the period of June 24-26, 12 during which the synoptic systems in all five runs held a morphological resemblance to each 13 other. Because the vertical interpolation used in the preparation of initial conditions disturbed the original dynamical state, spurious GWs appeared during the initial spin-up, though we 14 15 found them to be negligible during the analysis period.

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17 3 Results

18 **3.1** Strong dependence of GW momentum flux

19 Figure 1a compares vertical profiles of the GWMF for northern summer mid-latitude, which 20 were simulated using the five different vertical resolutions. Positive values suggest the dominance of the GWs propagating upward and eastward against background easterly winds 21 22 prevailing in the summertime stratosphere and mesosphere (e.g., Watanabe, 2008; Sato et al, 2009). It was quite surprising to find that the GWMF substantially decreases with increasing 23 24 vertical resolution throughout the stratosphere and mesosphere. In other words, a coarse 25 vertical resolution leads to a significant overestimation of the GWMF. This characteristic is opposite to that for horizontal resolution; a coarse horizontal resolution causes an 26 27 underestimation of the GWMF, which results in a cold pole problem in the wintertime 28 stratosphere (Hamilton et al., 1999). In these particular simulations, the dependence of the GWMF on the model's vertical resolution seems to start converging between dz = 300 m and 29 30 dz = 200 m. In the following sections, we discuss possible causes of this strong vertical 31 resolution dependence.

1 3.2 Critical level filtering

2 Figure 1b shows similar vertical profiles to Figure 1a but for the zonal mean zonal wind. The 3 wind profiles are almost identical to each other below 30 hPa, which implies that critical level 4 filtering of GWs propagating upward due to background large-scale flows in the troposphere 5 and lower stratosphere does not explain the differences in the GWMF. The difference in the 6 zonal mean zonal wind above the 30 hPa level rather reflects the difference in the GWMF, 7 that is, the larger GWMF in the coarser vertical resolution runs generally gives larger GW 8 forcing in the upper stratosphere and mesosphere, decelerating large-scale winds through 9 wave-mean flow interactions.

10 **3.3** Effects of particular GW events

11 It is necessary to determine whether the present vertical resolution dependence of the GWMF 12 originates from particularly severe GW events. The upper panels of Figure 2 compare longitude-height distributions of the net eastward GWMF for dz = 1000 m and 200 m. It is 13 14 revealed that the longitudinal distributions of large-scale zonal winds below the 30 hPa level 15 are qualitatively similar to each other. Meanwhile, the GWMF in the dz = 1000 m run is generally larger than that in the dz = 200 m run. The GWMF is large not only near active 16 17 source regions, $(100-160^{\circ} \text{ E and } 60-150^{\circ} \text{ W})$, but also near relatively calm regions (±45° from 18 0° E and near the date line).

19 The lower panels of Figure 2 show the time evolution of the GWMF at the 30 hPa level, along with contours of strong precipitation. Strong GW events with large positive GWMF (e.g., 20 21 $100-160^{\circ}$ E) are repeatedly observed in the east of strong precipitation regions (e.g., $100-120^{\circ}$ 22 E), suggesting that the GWMF is likely associated with convectively generated high 23 frequency GWs, which can penetrate westerly winds in the tropospheric subtropical jet (see 24 the contours of the background zonal winds in the upper panels). Overall, it can be concluded 25 that the vertical resolution dependence of the GWMF shown in Figure 1 is not caused by any 26 particular GW events, but is likely caused by systematic differences related to GW behaviors.

27 3.4 Effects of thin GWs

Sato et al. (1999) reported existence of a spectral peak of GWs near the inertial frequency in
the global lower stratosphere of a high-resolution (about 1° horizontal resolution) aqua-planet
AGCM experiment, which was later confirmed by observational evidence (Sato and Yoshiki,

1 2008). Such GWs have the lowest intrinsic frequency among vertically propagating GWs and 2 generally have short vertical wavelengths (e.g., less than 2-3 km). Therefore, a coarse vertical 3 resolution systematically reduces their number. Here, there is the apparent contradiction that 4 the GWMF *decreases* in runs with higher vertical resolutions, in which thin GWs can be 5 resolved.

6 Figure 3 shows close-up views of instantaneous longitude-height GW distributions (horizontal 7 wind divergence components). In the dz = 200 m run, thin GWs ($\lambda_z = 1-3$ km) which are 8 likely emitted by convective heating at around 140° E propagate upward and westward 9 against the tropospheric westerly jet. Qualitatively, these low-frequency GWs generated 10 within the sub-tropical jet reach their own critical levels near the zero-wind contours below a 11 50 hPa level, and do not directly affect the GWMF observed above the 30 hPa level.

12 As expected, the thin GWs ($\lambda_z = 1-3$ km) in the lower stratosphere are absent in the dz = 1000m run. Instead, GWs with $\lambda_z > 4-5$ km are dominant everywhere, and the amplitude of the 13 14 GWs seen above the 30 hPa level is obviously larger than those in the dz = 200 m run. These 15 circumstances may imply the existence of suppression effects of the thin GWs in the dz = 20016 m run, which effectively suppress the high-frequency GWs with longer vertical wavelengths. 17 One possible candidate of the suppression mechanisms is the turbulent diffusion, which is 18 sometime induced by wave saturation of thin GWs. It is really hard to see but green lines in 19 Figure 3 indicate regions of Ri < 0.25, where parameterized turbulent mixing occurs in the 20 model. The GWs with longer vertical wavelength encountering the turbulent layer would be suppressed due to vertical redistribution of wave momentum. Another suppression 21 22 mechanism might be a discontinuous vertical profiles of the buoyancy frequency, which 23 causes the partial reflection of GWs (e.g., Sato et al. 2012). More statistical investigation are necessary to clarify the roles of thin GWs in the high-vertical resolution models. 24

25 **3.5** Orographic GWs in the winter hemisphere

We have mainly focused on the non-orographic GWs appearing in the northern summer midlatitudes. Here we briefly investigate a case for orographic GWs in the southern winter midlatitudes. Figure 4 shows a similar longitude-height GW distributions to Figure 3, but over the Andes. Westerly winds over the surface orography excite deep GWs, and their phase structures resemble to each other below about 100 hPa. Above 100 hPa of the dz = 200 m run, the vertical wavelength of orographic GWs substantially decreases with height and the GWs

1 disappear below about 30 hPa. This behavior suggests occurrences of Doppler shifting and 2 dissipation near the critical level associated with vertical variations of the background winds. A weak wind layer is observed at 20-50 hPa downwind of the mountain, implying effects of 3 wave-mean flow interactions associated with the orographic GWs. On the other hand, the 4 5 orographic GWs in the dz = 1000 m run are not allowed to be shortened beyond the 2 km limit, and propagate higher than those seen in the dz = 200 m run. The temporary and regional 6 7 average of GWMF during this particular orographic GW event in the dz = 200 m run was 8 smaller than that in the dz = 1000 m run throughout the troposphere and stratosphere (not 9 shown). Although such dependence is similar to the northern summer mid-latitudes, longer 10 simulations and careful examinations are needed since mountain waves have large 11 intermittency, having just one case during the present one week simulation.

12 **3.6 Latitudinal variations**

Figure 5 compares meridional distributions of the zonal mean zonal winds and GWMF, which were simulated in the dz = 1000 m and dz = 200 m simulations. At almost all latitudes, the magnitude of GWMF decreases with increasing vertical resolution, which in turn alters the zonal mean wind structures through changes in GW forcing. Longer simulations are required to obtain climatological views of the GWMF distributions and background wind structures, and those dependence on the model's vertical resolution.

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20 4 Concluding remarks

21 In order to investigate the vertical resolution dependence of the GWMF in a comprehensive AGCM which explicitly resolves a portion of the GW spectra ($\lambda_h > 190$ km), a series of 22 23 sensitivity test simulations was performed changing only the model's vertical resolution (dz =24 200 m, 300 m, 400 m, 500 m, and 1,000 m). The simulated GWMF in the stratosphere and 25 mesosphere of northern summertime mid-latitude showed a strong dependence on the model's vertical resolution. The GWMF was systematically overestimated with decreasing vertical 26 27 resolution; it was confirmed that this overestimation did not stem from any particular GW 28 events. The existence of low-frequency thin ($\lambda_z = 1-3$ km) GWs in the lower stratosphere 29 might cause the vertical resolution dependence of the GWMF. On the other hand, the case 30 study for the deep orographic GWs in the southern wintertime mid-latitude showed the 31 importance of vertical resolution on appropriate representation of wave phase tilting and dissipation near the critical level. The comparison for the meridional distribution of GWMF simulated with different vertical resolution confirmed that the GWMF in the middle atmosphere decreased with increasing vertical resolution at all latitudes. Further discussions and investigations are required to obtain plausible mechanisms that explain the causality of the present findings.

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7 Author contribution

S. W. developed the model code. S. W. and K. S. designed the experiments, and S.W. carried
them out. S.W. prepared the manuscript with contributions from all co-authors.

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Figure 1. (a) Vertical profiles of the zonal mean net upward flux of the eastward momentum associated with the gravity wave component ($\lambda_h < 950$ km) for each vertical resolution. (b) Similar to (a) but for the zonal mean eastward winds. Averages over 35° N– 40° N from 00:00 UT June 23 to 00:00 UT June 27 are shown.



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Figure 2. Upper panels: Longitude-height distribution of net upward flux of the eastward momentum associated with the gravity wave component ($\lambda_h < 950$ km) in the dz = 1000 m run (a) and dz = 200 m run (b). The contours show low-pass filtered (> 1000 km) eastward winds with an interval of 15 ms⁻¹. Averages over 35° N–40° N from 00:00 UT June 24 to 00:00 UT June 27 are shown. Lower panels: Hovmöller diagrams of the eastward gravity wave momentum flux (color) and the background large-scale eastward winds (black contours with an interval of 5 ms⁻¹) at 30 hPa. Red contours show precipitation rate of 2 mm h⁻¹.



Figure 3. Instantaneous longitude-height distribution of the unfiltered divergence component
of the horizontal winds (color), the low-pass filtered (> 1000 km) eastward winds (black
contours with an interval of 15 ms⁻¹) and the moist diabatic heating rate of 0.1 K h⁻¹ (purple
contours) at 37.5° N, 00:00 UT June 24. Note that the longitudinal coverage is different from
Figure 2.



Figure 4. Instantaneous longitude-height distribution of the unfiltered divergence component
of the horizontal winds (color), the low-pass filtered (> 1000 km) eastward winds (black
contours with an interval of 10 ms⁻¹) at 30° S, 06:00 UT June 27.



Figure 5. The zonal mean eastward winds (contours) and net upward flux of the eastward momentum associated with the gravity wave component ($\lambda_h < 950$ km) in the dz = 1000 m (a) and dz = 200 m (b) simulations. Averages from 00:00 UT June 23 to 00:00 UT June 27 are shown. The color shading with momentum flux larger than $\pm 3 \times 10^{-3}$ Pa are omitted. The latitude box of 35° N-40° N is indicated, which we mainly focus in the present study.



Figure A1. Standard vertical layer distribution for each vertical resolution. Note that a hybrid
sigma-pressure coordinate system was actually used in the model, and a scale height of 7 km

4 was used to calculate the log-pressure standard levels shown in this figure.