

# 1 Implementation and comparison of a suite of heat stress 2 metrics within the Community Land Model version 4.5

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## 11 12 **Abstract**

13 We implement and analyse 13 different metrics (4 moist thermodynamic quantities and 9 heat  
14 stress metrics) in the Community Land Model (CLM4.5), the land surface component of the  
15 Community Earth System Model (CESM). We call these routines the HumanIndexMod. We  
16 limit the algorithms of the HumanIndexMod to meteorological inputs of temperature,  
17 moisture, and pressure for their calculation. All metrics assume no direct sunlight exposure.  
18 The goal of this project is to implement a common framework for calculating operationally  
19 used heat stress metrics, in climate models, offline output, and locally sourced weather  
20 datasets, with the intent that the HumanIndexMod may be used with the broadest of  
21 applications. The thermodynamic quantities use the latest accurate and efficient algorithms  
22 available, which in turn are used as inputs to the heat stress metrics. There are three  
23 advantages of adding these metrics to CLM4.5 1) improved moist thermodynamic quantities,  
24 2) quantifying heat stress in every available environment within CLM4.5, and 3) these metrics  
25 may be used with human, animal, and industrial applications.

26 We demonstrate the capabilities of the HumanIndexMod in a default configuration simulation  
27 using CLM4.5. We output 4x daily temporal resolution globally. We show that the  
28 advantage of implementing these routines into CLM4.5 is capturing the nonlinearity of the  
29 covariation of temperature and moisture conditions. For example, we show that there are

1 systematic biases of up to 1.5°C between monthly and  $\pm 0.5^\circ\text{C}$  between 4x daily offline  
2 calculations and the online instantaneous calculation, respectively. Additionally, we show  
3 that the differences between an inaccurate wet bulb calculation and the improved wet bulb  
4 calculation are  $\pm 1.5^\circ\text{C}$ . These differences are important due to human responses to heat stress  
5 being non-linear. Furthermore, we show heat stress has unique regional characteristics.  
6 Some metrics have a strong dependency on regionally extreme moisture, while others have a  
7 strong dependency on regionally extreme temperature.

8

## 9 **1 Introduction**

10 Heat related conditions are the number one cause of death from natural disaster in the United  
11 States; more than tornadoes, flooding, and hurricanes combined (NOAA Watch, 2014). Short-  
12 term duration (hours) of exposure to heat while working may increase the incidence of heat  
13 exhaustion and heat stroke (Liang et al., 2011). However, long-term exposure (heat waves or  
14 seasonally high heat), even without working, may drastically increase morbidity and mortality  
15 (Kjellstrom et al., 2009). Although there is high uncertainty in the number of deaths, the 2003  
16 European heat wave killed 40,000 people during a couple weeks in August (Garcia-Herrera et  
17 al., 2010), and tens of thousands more altogether for the entire summer (Robine et al., 2008).  
18 The 2010 Russian heat wave, the worst recorded heat wave, killed 55,000 people over the  
19 midsummer (Barriopedro et al., 2011).

20 A growing literature is concerned with the frequency and duration of heat waves (Seneviratne  
21 et al., 2012 and references therein). One study concluded that intensification of 500-hPa  
22 height anomalies will produce more severe heat waves over Europe and North America in the  
23 future (Meehl and Tebaldi, 2004). Another study shows that even with including the global  
24 warming ‘hiatus’, there is an increasing occurrence of extreme temperatures (Seneviratne et  
25 al., 2014). Multiple studies associate lack of precipitation and/or low soil moisture to  
26 contributing to high temperatures (Fischer et al., 2007; Mueller and Seneviratne, 2012;  
27 Miralles et al., 2014).

28 Regarding humans, however, temperature differences are not the primary method for heat  
29 dissipation. Evaporation of sweat is crucial to maintaining homeostasis, and none of the  
30 before mentioned studies incorporate atmospheric moisture to measure heat stress. Many  
31 diagnostic and prognostic methods were developed to diagnose heat stress (over a 100 year  
32 history, Table 1), such as the Wet Bulb Globe Temperature (WBGT), the Discomfort Index

1 (DI), or Heat Index (HI), and policy makers have decided to incorporate these indices in  
2 weather warning systems (Epstein and Moran, 2006; Parsons, 2006; Parsons, 2013; Rothfus,  
3 1990; Fiala et al., 2011).

4 There are a limited number of studies validating, exploring, or using heat stress metrics on a  
5 global scale (Kjellstrom et al., 2009b; Hyatt et al., 2010; Sherwood and Huber, 2010; Fischer  
6 and Schar, 2010; Fischer et al., 2012; Fischer and Knutti, 2012; Willett and Sherwood, 2012;  
7 Dunne et al., 2013; Kjellstrom et al., 2013; Oleson et al., 2013). Algorithms for measuring  
8 heat stress and labor capacity are based upon sub-daily rates of exposure to heat stress  
9 (Parsons, 2006). Most of these studies do not capture the diurnal cycle of heat stress  
10 (Kjellstrom et al., 2009b; Hyatt et al., 2010; Fischer and Schar, 2010; Fischer and Knutti,  
11 2012; Willett and Sherwood, 2012; Dunne et al., 2013; Kjellstrom et al., 2013), thus not  
12 representing both nighttime highs, and daytime extremes. Only one study includes solar  
13 radiation as a component in heat stress (Kjellstrom et al., 2013). Different metrics are used  
14 between each study, and only one study attempts to compare more than two metrics (Oleson,  
15 et al., 2013b).

16 Various forms of moist thermodynamic calculations (Buck, 1981; Davies-Jones, 2008; Stull,  
17 2011) and heat stress metrics are criticized for their inaccuracies (Budd, 2008; Alfano et al.,  
18 2010; Davies-Jones, 2008). Buck (1981) moist thermodynamic calculations are not as  
19 accurate as Bolton (1980), yet are used in a recent study (Kjellstrom et al., 2013). Wet bulb  
20 temperature calculations are different between multiple studies (Hyatt et al., 2010; Sherwood  
21 and Huber, 2010; Dunne et al., 2013; Kjellstrom et al., 2013; Oleson et al., 2013). Hyatt et al.  
22 (2010) and Kjellstrom et al. (2013) use natural wet bulb temperature—a calculation, that due  
23 to non-linear components of its equation, may have multiple steady state solutions (Alfano et  
24 al., 2010). Oleson et al. (2013b) uses a recent formulation of wet bulb temperature that is  
25 limited in effective range of input temperatures (Stull, 2011) (we go into further detail on this  
26 equation in section 2). Sherwood and Huber (2010) and Dunne et al. (2013) both use Davies-  
27 Jones (2008) as their source paper for their calculation of wet bulb temperature. However,  
28 Sherwood and Huber's (2010) wet bulb temperature calculations use Bolton's (1980)  
29 equivalent potential temperature Eq. (38), rather than the more accurate Eq. (39) (Bolton,  
30 1980; Davies-Jones, 2008; Davies-Jones, 2009). Furthermore, their calculation is only valid  
31 for wet bulb temperatures above 10°C. Dunne et al. (2013), on the other hand, uses wet bulb  
32 potential temperature Eq. (3.4) in Davies-Jones (2008), yet the recommended equations for

1 wet bulb potential temperature are Eq. (3.5-3.7, and 3.8) (Davies-Jones, 2008) for the  
2 temperature ranges used in their paper. Dunne et al. (2013) also uses Bolton's (1980)  
3 equivalent potential temperature Eq. (40), rather than the more accurate Eq. (39) (Bolton,  
4 1980). Additionally, Dunne et al. (2013) uses a variation of WBGT that is heavily criticized,  
5 the indoorWBGT (Budd, 2008).

6 Occasionally, results using heat stress limits are misinterpreted. One study confuses wet bulb  
7 temperature thresholds with dry bulb temperature thresholds (Benestad, 2011). This has  
8 misleading consequences as their results do not include moisture metrics, yet the author cites  
9 Sherwood and Huber (2010)'s wet bulb threshold (35°C) as the threshold value for their  
10 temperature analysis. The wet bulb temperature at 35°C is a theoretical limit where humans  
11 would die from heat stress after 6 hours of exposure. Benestad (2011)'s misapplication  
12 implies that most humans should die every year, because a great portion of the world reaches  
13 temperatures of 35°C for more than a 6 hour period.

14 Our goal here is to improve the situation by creating a module that calculates a large suite of  
15 metrics, using the most accurate and efficient algorithms available, that may be used with as  
16 many applications as possible: climate models, offline archive data, model validation studies,  
17 and weather station datasets. We call this module the HumanIndexMod. The module  
18 calculates 4 moist thermodynamic quantities and 9 heat stress metrics. These heat stress  
19 metrics are in operational use worldwide, and cover a wide range of assumptions.

20 As an example of numerous applications, we implement the HumanIndexMod into the  
21 Community Land Model (CLM4.5), a component model of the Community Earth System  
22 Model (CESM), maintained by the National Center for Atmospheric Research (NCAR)  
23 (Hurrell et al., 2013). The metrics are directly calculated at the sub-grid scale, capturing heat  
24 stress in every environment: urban, lakes, vegetation, and bare ground. We show examples of  
25 the advantages of calculating these metrics at the model time step as compared to lower  
26 temporal resolution, and the importance of using accurate moist thermodynamic calculations.  
27 We also show that having all metrics calculated at the same time allows for comparison of  
28 metrics between each other, and allows for unique analysis of conditional distributions of the  
29 inputs. Finally, we show that the metrics may also be used as model diagnostics.

30 The outline of the paper is as follows: section 2 (Heat stress modeling) focuses on the  
31 development, calculation, and use of these 13 metrics. Section 3 (Methods) describes the  
32 implementation and model setup. Section 4 (Results) presents the results of a model

1 simulation using these metrics. Section 5 (Discussion) discusses the implications of the  
2 research, and section 6 (Summary) presents the conclusions of the paper.

3

## 4 **2 Heat stress modeling**

### 5 **2.1 Background**

6 The primary focus of this paper is on atmospheric variable based heat stress metrics that we  
7 introduce into the HumanIndexMod. The models for determining heat stress for humans vary  
8 greatly; ranging from simple indices to complex prognostic physiology modelling (Table 1).  
9 Prognostic thermal models are beyond the scope of this paper, as they require more than  
10 atmospheric inputs. Additionally, metrics that include radiation and wind (with one  
11 exception, Apparent Temperature) are also beyond the scope of this paper. Each index that  
12 we chose uses a combination of atmospheric variables: temperature ( $T$ ), humidity ( $Q$ ), and  
13 pressure ( $P$ ). We chose these metrics because they are in operational use globally by  
14 industry, governments, and weather services. Furthermore, these metrics may be applied to  
15 the broadest range of uses: climate and weather forecasting models, archive datasets, and local  
16 weather stations.

17 Sections 2.2-2.4 describe the metrics that we have chosen to implement in the  
18 HumanIndexMod (see variables defined in Table 2). Most of the metrics have units of  
19 temperature, which may be misleading. The metrics have temperature scales for comparative  
20 purposes only, as the metrics are an index, not a true thermodynamic quantity. We break  
21 these metrics into three categories, based upon design philosophies: comfort, physiological  
22 response, and empirical fit. Comfort based algorithms are a quantification of behavioural or  
23 ‘feels like’ reactions to heat in both animals and humans. Physiological indices quantify the  
24 physical response mechanisms within a human or animal, such as changes in heart rate or core  
25 temperatures. The empirical indices quantify relationships between weather conditions and a  
26 non-physical or comfort related attribute. For example, an empirical algorithm’s result may  
27 determine how much work may be completed per hour per weather condition.

### 28 **2.2 Comfort algorithms**

29 We use Apparent Temperature, Heat Index, Humidex, and Temperature Humidity Index for  
30 Comfort to account for comfort level. These metrics were either tailored to the global

1 locations where they were developed, or streamlined for ease of use from physiology models.  
2 The underlying philosophical approach to deriving comfort metrics is representing behavioral  
3 reactions to levels of comfort (Masterson and Richardson, 1979; Steadman, 1979a). The goal  
4 of these equations of comfort is to match the levels of discomfort to appropriate warnings for  
5 laborers (Gagge et al., 1972) and livestock (Renaudeau et al., 2012). Discomfort in humans  
6 sets in much earlier than physiological responses, i.e. the human body provides an early  
7 warning to the mind that continuing the activity may lead to disastrous consequences. For  
8 example, when heat exhaustion sets in, the body is sweating profusely, and often there are  
9 symptoms of dizziness. However, the actual core temperature for heat exhaustion is defined  
10 at 38.5°C, which is considerably lower than heat stroke (42°C). We describe the 4 comfort  
11 based algorithms below.

12 Apparent Temperature (AT) was developed using a combination of wind, radiation, and heat  
13 transfer to measure thermal comfort and thermal responses in humans (Steadman, 1994). AT  
14 is used by the Australian Bureau of Meteorology, and was developed for climates in Australia  
15 (ABM, 2014). The metric is an approximation of a prognostic thermal model of human  
16 comfort (Steadman 1979a,b; Steadman, 1984).

$$17 \quad AT = T_c + \frac{3.3e_{RH}}{1000} - 0.7u_{10m} - 4 \quad (1)$$

$$18 \quad e_{RH} = \left(\frac{RH}{100}\right)e_{sPa} \quad (2)$$

19 where the vapor pressure ( $e_{RH}$ ) is in Pascals and is calculated from the relative humidity ( $RH$   
20 in %), and saturated vapor pressure ( $e_{sPa}$ , also in Pascals). We use this notation because  $e_s$   
21 (Table 2) is in millibars. These variable names are the explicit names of the variables in the  
22 HumanIndexMod. AT uses the wind velocity (m/s) measured at the 10m height ( $u_{10m}$ ). Air  
23 temperature ( $T_c$ ) and AT are in units of degrees Celsius. AT is the only metric in the  
24 HumanIndexMod that includes an explicit calculation for wind velocity; the other metrics  
25 assume a reference wind. We included this metric due to a previously used legacy version  
26 within CLM4.5 (Oleson et al., 2013b). An assumption made by AT is that the subject is  
27 outside, but not exposed to direct sunlight. AT has no explicit thresholds; rather, the index  
28 shows an amplification of temperatures. Previous work, however, has used temperature  
29 percentiles to describe AT (Oleson et al., 2013b).

1 Heat Index (HI) was developed using a similar process as AT. The United States National  
2 Weather Service (NWS) required a heat stress early warning system, and the index was  
3 created as a polynomial fit to Steadman's (1979a) comfort model (Rothfusz, 1990).

$$4 \quad HI =$$
$$5 \quad -42.379 + 2.04901523T_F + 10.14333127RH + -0.22475541T_F RH + -6.83783 \times$$
$$6 \quad 10^{-3}T_F^2 + -5.481717 \times 10^{-2}RH^2 + 1.22874 \times 10^{-3}T_F^2 RH + 8.5282 \times 10^{-4}T_F RH^2 +$$
$$7 \quad -1.99 \times 10^{-6}T_F^2 RH^2 \quad (3)$$

8 Here, air temperature ( $T_F$ ) and HI are in Fahrenheit. HI has a number of assumptions. The  
9 equation assumes a walking person in shorts and T-shirt, who is male and weighs ~147lbs  
10 (Rothfusz, 1990). Additionally, this subject is not in direct sunlight. As with AT, HI  
11 represents a 'feels like' temperature, based upon levels of discomfort. HI uses a scale for  
12 determining heat stress: 27-32°C is caution, 33-39°C is extreme caution, 40-51°C is danger,  
13 and  $\geq 52^\circ\text{C}$  is extreme danger.

14 Humidex (HUMIDEX) was developed for the Meteorological Service of Canada, and  
15 describes the 'feels like' temperature for humans (Masterson and Richardson, 1979). The  
16 original equation used dew point temperature, rather than specific humidity. The equation  
17 was modified to use vapor pressure, instead:

$$18 \quad HUMIDEX = T_c + \frac{5}{9} \left( \frac{e_{RH}}{100} - 10 \right) \quad (4)$$

19 HUMIDEX is unitless because the authors recognized that the index is a measure of heat load.  
20 The index has a series of thresholds: 30 is some discomfort, 46 is dangerous, and 54 is  
21 imminent heat stroke (Masterson and Richardson, 1979).

22 The Temperature Humidity Index for Comfort (THIC) is a modification of the Temperature  
23 Humidity Index (THI) (Ingram, 1965). Comfort was quantified for livestock through THIC  
24 (NWSCR, 1976). We use the original calibration, which is for pigs (Ingram, 1965). The  
25 index is unitless:

$$26 \quad THIC = 0.72T_w + 0.72T_c + 40.6 \quad (5)$$

27 where wet bulb temperature ( $T_w$ ) is in units of Celsius. The index is used to describe  
28 behavioral changes in large animals due to discomfort (seeking shade, submerging in mud,  
29 etc.). The index is in active use by the livestock industry for local heat stress and future  
30 climate considerations (Lucas et al., 2000; Renaudeau et al., 2012). The index describes

1 qualitative threat levels for animals: 75 is alert, 79-83 is dangerous, and 84+ is very  
2 dangerous. There are different approaches to the development of THIC, including  
3 considerations of physiology of large animals.

#### 4 **2.3 Physiology algorithms**

5 Numerous metrics are based upon direct physiological responses within humans and animals;  
6 however, almost all of them are complicated algorithms (e.g. Moran et al., 2001; Berglund  
7 and Yokota, 2005; Gribox et al., 2008; Maloney and Forbes, 2011; Havenith et al., 2011;  
8 Gonzalez et al., 2012; Chan et al., 2012). Most metrics require radiation measurements, or  
9 heart rates, and/or even sweat rates. The available metrics that are calibrated for  
10 physiological responses using only meteorological inputs, though, are limited, such as the  
11 Temperature Humidity Index for Physiology (THIP; Ingram, 1965):

$$12 \quad THIP = 0.63T_w + 1.17T_c + 32 \quad (6)$$

13 THIP and THIC are modifications of the Temperature Humidity Index (THI). Additionally,  
14 THIC and THIP have applications beyond heat stress. THIP and THIC threshold levels are  
15 computed from both indoor and outdoor atmospheric variables. The differences between  
16 outdoor and indoor values are used to evaluate evaporative cooling mechanisms, e.g. swamp  
17 coolers (Gates et al., 1991a,b).

#### 18 **2.4 Empirical algorithms**

19 The last category of metrics are derived from first principle thermo-physiology models, or  
20 changes in worker productivity, etc., and then reduced by empirical fit. The first metric we  
21 present is widely used modification of an industry labor standard, the Simplified Wet Bulb  
22 Globe Temperature (sWBGT):

$$23 \quad sWBGT = 0.56T_c + \frac{0.393e_{RH}}{100} + 3.94 \quad (7)$$

24 sWBGT was designed for estimating heat stress in sports medicine, adopted by the Australian  
25 Bureau of Meteorology, and is acknowledged that its accuracy of representing the original  
26 labor industry index may be questionable (ABOM, 2010; ACSM, 1984; ACSM, 1987). We  
27 chose, however, to implement sWBGT due to its wide use. sWBGT is unitless, and its threat  
28 levels are: 26.7-29.3 is green or be alert, 29.4-31.0 is yellow or caution, 31.1-32.1 is red or  
29 potentially dangerous, and  $\geq 32.2$  is black or dangerous conditions (US Army, 2003).



1 Discomfort Index (DI) was developed in the 1950s as a calibration for air conditioners  
 2 (Thom, 1959). It was adapted by the Israeli Defense Force as a decision making tool  
 3 regarding heat stress (Epstein and Moran, 2006). DI requires  $T_w$  and  $T_C$ . The computation of  
 4  $T_w$  in the past was computationally expensive, and the DI equations often used  
 5 approximations (e.g., Oleson et al., 2013b):

$$6 \quad T_{wS} = T_C \arctan(0.151977\sqrt{RH + 8.313659}) + \arctan(T_C + RH) - \arctan(RH -$$

$$7 \quad 1.676331) + 0.00391838RH^{3/2}\arctan(0.023101RH) - 4.68035 \quad (8)$$

8 where  $T_{wS}$  is the wet bulb temperature in Celsius (Stull, 2011). Stull's function has limited  
 9 range of effective accuracy.

$$10 \quad \begin{matrix} -20 < T_C < 50 \\ -2.27T_C + 27.7 < RH < 99 \end{matrix} \quad (9)$$

11 We compute DI with both  $T_{wS}$  and  $T_w$  calculated using our implementation of Davies-Jones  
 12 (2008) (Eq. A.22). We keep the legacy version (Stull, 2011) for comparative purposes. DI is  
 13 calculated from these inputs:

$$14 \quad DI = 0.5T_w + 0.5T_C \quad (10)$$

15 where the DI is unitless and the values are an indicator of threats to the populations: 21-24 is  
 16 <50% of population in discomfort, 24-27 >50% of population in discomfort, 27-29 most of  
 17 the population in discomfort, 29-32 severe stress, and >32 is state of emergency (Giles et al.,  
 18 1990).

19 The last index we present is a measurement of the capacity of evaporative cooling  
 20 mechanisms. Often, these are referred to as swamp coolers. Large-scale swamp coolers  
 21 generally work by spraying a 'mist' into the air, or blowing air through a wet mesh. This mist  
 22 then comes in contact with the skin, and subsequently evaporated, thus cooling down the  
 23 subject. In dry environments, they can be an effective mass cooling mechanism.  
 24 Unfortunately, swamp coolers raise the local humidity considerably, reducing the  
 25 effectiveness of direct evaporation from the skin. Swamp coolers are measured by their  
 26 efficiency:

$$27 \quad \eta = \frac{T_c - T_t}{T_c - T_w} 100\% \quad (11)$$

28 where  $\eta$  (%) is the efficiency, and  $T_t$  is the target temperature for the room to be cooled  
 29 towards in Celsius (Koca et al., 1991). Rearranging Eq. (11) and solving for  $T_t$ :

$$1 \quad T_t = T_c - \frac{\eta}{100}(T_c - T_w) \quad (12)$$

2 where  $T_t$  is now the predicted temperature based upon environmental variables. The  
3 maximum efficiency of typical swamp coolers is 80%, and a typical value of a sub-standard  
4 mechanism is 65% (Koca et al., 1991). Thus, we calculate  $T_t$  with two different efficiencies:  
5 SWMP80, for  $\eta$  at 80%, and SWMP65 for  $\eta$  at 65%. With the mist-injected air cooled to  $T_t$ ,  
6  $T_t$  is approximately equal to a new local  $T_w$ . Humid environments or environments that are  
7 hot and have an above average  $RH$  relative to their normally high  $T$ , severely limit the cooling  
8 potential of swamp coolers. The livestock industry uses evaporative cooling mechanisms for  
9 cooling, and often in conjunction with THIP and THIC, as mentioned previously (Gates et al.,  
10 1991a,b). Due to their low cost, swamp coolers are used throughout the world as a method of  
11 cooling buildings and houses. No one has implemented SWMP65 and SWMP80 in global  
12 models, and we believe that this will provide many uses to industry by its inclusion in  
13 CLM4.5. Table 2 shows what metrics are discussed in this paper.

14

### 15 **3 Methods**

16 Our approach is to choose a subset of heat stress metrics that are in common use operationally  
17 by governments and/or used extensively in prior climate modeling studies (Table 3). We do  
18 this in order to provide a framework to allow comparisons of metrics across studies, and we  
19 designate the algorithms the HumanIndexMod. Section 3.1 describes CLM4.5. Section 3.2  
20 discusses the implementation of the HumanIndexMod into CLM4.5. Section 3.3 describes  
21 our simulation setup that we use to demonstrate the capabilities of the HumanIndexMod. The  
22 simulation is for showcasing the HumanIndexMod, not as an experiment for describing real  
23 climate or climate change. Section 3.4 describes a unique application method for analyzing  
24 heat stress.

#### 25 **3.1 The structure of Community Land Model version 4.5**

26 We use CLM version 4.5, which was released in June, 2013 (Oleson et al., 2013a). Boundary  
27 conditions for CLM4.5 consist of land cover and atmospheric weather conditions. Each grid  
28 cell in CLM4.5 can include vegetation, lakes, wetlands, glacier, and urban. There are new  
29 parameterizations and models for snow cover, lakes, crops, a new biogeochemical cycles  
30 model, and new urban classifications (Oleson et al., 2013a). The urban biome, a single-layer

1 canyon model, is designed to represent the ‘heat island’, where temperatures are amplified by  
2 urban environments (Oleson et al., 2008a,b; Oleson et al., 2010a,b,c). The ‘heat island’ effect  
3 can increase the likelihood of complications from human heat stress (Oleson, 2012).

### 5 **3.2 HumanIndexMod design and implementation**

6 There are two philosophical aspects to the design of the HumanIndexMod. 1) Accurate and  
7 efficient moist thermodynamic algorithms, and 2) a modular format to increase use through  
8 both narrowly focused applications and up to broad based studies. The module is in an open  
9 source format, and is incorporated into the CLM4.5 developer branch (the module itself is  
10 available from the corresponding author’s website). The modular format encourages adapting  
11 the code to specific needs; whether that focus is on moist thermodynamics or heat stress. The  
12 inclusion of heat stress metrics covering comfort, physiology, and empirical philosophies  
13 encourages the use of HumanIndexMod for many applications.

14 We directly implemented the code into the CLM4.5 architecture through seven modules.  
15 Four of these modules—BareGroundFluxesMod, CanopyFluxesMod, SlakeFluxesMod, and  
16 UrbanMod—call the HumanIndexMod. The HumanIndexMod is calculated for every surface  
17 type in CLM4.5. The design of CLM4.5 allows the urban and rural components, where the  
18 rural component represents the natural vegetation surface, to be archived separately for  
19 intercomparison. The HumanIndexMod uses the 2-meter calculations of water vapor,  
20 temperature, and pressure, as well as 10-meter winds. Three other modules are modified with  
21 the implementation process. These modules—clmtype, clmtypeInitMod, and histFldsMod—  
22 are used for initializing memory and outputting variable history files.

23 Moist thermodynamic water vapor quantities in CLM4.5 are calculated within QSatMod. We  
24 use the outputs from QSatMod as the inputs to the HumanIndexMod. Within the  
25 HumanIndexMod, we created a subroutine, QSat\_2, which has all the same functionalities as  
26 QSatMod. This subroutine uses the August-Roche-Magnus (ARM) equation (Eq. A.13),  
27 rather than the Flatau et al. (1992) polynomial equations for vapor pressure in QSatMod. The  
28 log derivative of ARM (Eq. A.15) is a critical component of the calculation of  $T_w$ , and is not  
29 available in QSatMod. Additionally, QSat\_2 calculates  $f(\theta_E)$  (Eq. A.18) with respect to the  
30 input temperature, and the subsequent derivatives. These are required to calculate  $T_w$  (Eq.  
31 A.22) using Davies-Jones (2008), and cannot be accomplished using QSatMod. We show

1 acceptable differences between the Stull version of wet bulb temperature ( $T_{ws}$ ) calculated  
2 using both QSatMod and QSat\_2 (Fig. 1a). The new subroutines improve CLM4.5 by  
3 calculating previously unused thermodynamic quantities. Additionally, these routines are  
4 useful moist thermodynamic routines for other datasets for researchers to use, thus expanding  
5 the capacity of the HumanIndexMod.

6 We implement specific thermodynamic routines developed by Davies-Jones (2008) to  
7 accurately calculate  $T_w$  (see Appendix A). Equation (A.4) is the most accurate and efficient  
8  $\theta_E$  calculation available (Bolton, 1980; Davies-Jones, 2009). Calculating Eq. (A.4) required  
9 implementing  $T_L$  and  $\theta_{DL}$  (Eq. A.2 and A.3, respectively) into the HumanIndexMod.  $T$ ,  $P$ , and  
10  $Q$  from CLM4.5 are used to calculate  $\theta_E$  and  $T_E$  (Eq. A.5).  $T_E$ , a quantity used in a previous  
11 heat stress study (Fischer and Knutti, 2012), is an input into QSat\_2 for calculating the initial  
12 guess of  $T_w$ , and subsequently followed by the accelerated Newton-Raphson method (Eq. A.9-  
13 A.22). We found it advantageous to split the heat stress quantities into their own subroutines,  
14 allowing the user to choose what quantities to be calculated. The minimum requirements to  
15 execute the entire module are  $T$  (K),  $P$  (Pa),  $RH$  (%),  $Q$  (g/kg),  $e$  (Pa), and  $u_{10m}$  (m/s). Table 4  
16 shows the subroutines, input requirements, and outputs in HumanIndexMod.

### 17 **3.3 CLM4.5 experimental setup**

18 CLM4.5 may be executed independently of the other models in CESM, called an I-Compset.  
19 To do so, CLM4.5 requires atmospheric boundary conditions. We use the default dataset for  
20 CLM4.5—CRUNCEP. CRUNCEP is the NCEP/NCAR reanalysis product (Kalnay et al.,  
21 1996) corrected and downscaled by the Climatic Research Unit (CRU) gridded observations  
22 dataset from the University of East Anglia (Mitchell and Jones, 2005). The time period is 4x  
23 daily from 1901-2010, and is on a regular grid of  $\sim 0.5^\circ \times 0.5^\circ$ . The combination of CRU and  
24 NCEP products was to correct for biases in the reanalysis product, and improve overall  
25 resolution (Casado et al., 2013). To drive CLM4.5 we used surface solar radiation, surface  
26 precipitation rate, temperature, specific humidity, zonal and meridional winds, and surface  
27 pressure.

28 Our simulation has the carbon and nitrogen cycling on (biogeophysics ‘CN’). The simulation  
29 was initialized at year 1850, on a finite volume grid of  $1^\circ \times 1^\circ$ , using boundary conditions  
30 provided from NCAR (Sam Levis, personal communication). The simulation spun up while

1 cycling 3 times over CRUNCEP 1901-1920 forcings. Once completed, our experiment used  
 2 the spun up land conditions, and ran the entirety of 1901-2010.

### 3 **3.4 Heat stress indices analysis**

4 An open question is what drives extreme high heat stress events, which are, by definition, rare  
 5 events. For example, we cannot determine from the mean climate state or from theory, in a  
 6 warm and humid climate, if abnormally high temperature, abnormally high moisture, or a  
 7 combination of the two, caused a heat stress event. This is a question of the covariance of  
 8 perturbations of temperature and humidity, not a statement of mean conditions, and there is no  
 9 theory to explain these situations. For example, we may apply Reynolds averaging to the  
 10 NWS Heat Index equation (Eq. 3):

$$\begin{aligned}
 11 \quad HI &= a + \overline{bT} + \overline{cRH} + \overline{dTRH} + \overline{eT^2} + \overline{fRH^2} + \overline{gT^2RH} + \overline{hTRH^2} + \overline{iT^2RH^2} + \\
 12 \quad &\left[ \overline{dRH'T'} + \overline{eT'^2} + \overline{fRH'^2} + \overline{gT'^2RH'} + \overline{hT'RH'^2} + \overline{iT'^2RH'^2} \right] \quad (13)
 \end{aligned}$$

13 where  $a$ ,  $b$ ,  $c$ ,  $d$ ,  $e$ ,  $f$ ,  $g$ ,  $h$ , and  $i$  are constants in the polynomial.  $RH$  and  $T$  are relative  
 14 humidity and temperature, respectively. We are not concerned with the terms outside the  
 15 brackets, as they are the means. The terms within the bracket are representative of turbulent  
 16 effects on the Heat Index, which we are discussing. It is these turbulent states where a GCM  
 17 is able to determine these individual factors, by calculating the heat stress metrics and  
 18 thermodynamic quantities at every model time step. Furthermore, each heat stress metric has  
 19 different assumptions (such as body size, or physical fitness, etc.) that weigh temperature and  
 20 humidity differently. A high heat stress event indicated by one metric does not necessarily  
 21 transfer onto another metric.

22 Thus, we outputted 4x daily averages of the heat stress metrics and the corresponding surface  
 23 pressure ( $P$ ), 2-meter temperature ( $T$ ), 10-meter winds ( $u_{10m}$ ), and 2-meter humidity ( $Q$ )  
 24 fields. We computed statistics for the time series (mean, variance, exceedance, etc.). We  
 25 focus primarily on the 99<sup>th</sup> percentiles (hottest 1606 six hour intervals, ~402 days), but also  
 26 show some of the robust features with the 75<sup>th</sup> (hottest 40,150 six hour intervals, ~10,038  
 27 days) and 95<sup>th</sup> percentiles (hottest 8030 six hour intervals, ~2008 days).

28 Every 6-hour period that exceeds the percentiles was located within the time series, and we  
 29 calculated the conditional distributions. For example, the 99<sup>th</sup> percentile exceedance of HI  
 30 isolated the top 1606 hottest time steps for each grid cell. After isolating these time steps, we

1 use this distribution as a mask to isolate all other quantities (e.g., temperature and humidity),  
2 allowing cross comparison between all metrics and HI. The goal is to develop an analysis  
3 technique comparing all covariances of the metrics within CLM4.5.

4 After the conditional distributions are calculated, we, again, compute the statistical dispersion  
5 (mean, variance, exceedance, etc.) of the percentiles. We display this analysis with maps in  
6 two ways. 1) We show the exceedance value of a metric, and 2) we show  $T$ - $Q$  regime plots of  
7 that same metric. We calculate the  $T$ - $Q$  regimes through expected rank values (Fig. 2). This  
8 required a series of steps. 1) We take the conditional distribution of  $T$  and  $Q$  that represent  
9 exceedance percentile of the source heat stress or moist thermodynamic metric. 2) We take  
10 the expected value (median) of the conditional distributions of  $T$  and  $Q$  and determine what  
11 percentile they come from in their respective time series. 3) We condition these values on  
12 each other to create the expected rank values (Fig. 2).

13

## 14 **4 Results**

15 We present a snap shot of the many metrics calculated. First, we present results of our  
16 evaluation the improved moist thermodynamic calculations and the implementation these  
17 metrics into CLM4.5 (Fig. 1). Second, we show an example of the possible global  
18 applications for these metrics (Fig. 3-6). This approach characterizes heat stress within  
19 CLM4.5 in response to one observation reanalysis product, the CRUNCEP.

### 20 **4.1 Evaluation of improved moist thermodynamic quantities**

21 We present a series of box and whisker plots demonstrating the value added of implementing  
22 1) accurate and efficient moist thermodynamic quantities, and 2) online calculation of the heat  
23 stress metrics is an improvement over calculating these metrics using monthly or 4x daily  
24 model output (Fig. 1). Figure 1a shows the difference in the Stull (2011) wet bulb  
25 temperature calculated using the saturated vapor pressure from Davies-Jones (2008) (QSat\_2)  
26 and Flatau et al. (1992) (QSatMod). The differences are minimal. However, our point is that  
27 the Davies-Jones (2008) method for wet bulb temperature is preferred. We show the  
28 difference between wet bulb temperatures using Stull (2011) calculated with QSat\_2, and  
29 Davies-Jones (2008) (which requires QSat\_2) (Fig. 1b). Differences are greater than 1K  
30 between Stull (2011) and Davies-Jones (2008) methods, and they are temperature dependent  
31 (Fig. 1b). Lastly, we show the difference between calculating Davies-Jones (2008)  $T_w$  using

1 monthly and 4x daily averaged model data versus the model instantaneous calculations (Fig.  
2 1c and 1d, respectively). Using model-averaged data instead of the instantaneous data  
3 systematically overestimates  $T_w$  by more than 1K for monthly and 0.5K for 4x daily output.

#### 4 **4.2 Exceedance values and regime maps**

5 We show exceedance and  $T$ - $Q$  regime maps for the 75<sup>th</sup> and 95<sup>th</sup> percentiles of 3 metrics, and  
6 99<sup>th</sup> percentiles of 6 metrics. The maps show spatial patterns of heat stress and  
7 characteristics. Equatorial and monsoonal regions show moderate levels of heat stress in the  
8 75<sup>th</sup> percentile (Fig. 3a-c). sWBGT shows values exceeding minimum metric warning levels  
9 (e.g. China, Northern Africa), whereas HI does not have necessarily the same warning. The  
10 95<sup>th</sup> percentile shows that moderate levels of heat stress have expanded into higher latitudes  
11 (Fig. 4a-c). At equatorial and monsoonal regions, heat stress labor reductions should be in  
12 effect as it is not safe to work outside, and in some cases (West Africa, the Arabian Peninsula,  
13 and the Himalayan Wall), no work at all. At the 99<sup>th</sup> percentile, severe heat stress is  
14 experienced in the monsoonal regions (Fig. 5a-c). These maxima correlate with maxima in  $T_w$   
15 (Fig. 5c).

16 The  $T$ - $Q$  regime maps show that partitioning of heat stress into  $T$  and  $Q$  begins in regional  
17 locations at the 75<sup>th</sup> percentile (Fig. 3d-f). The partitioning occurs in low latitudes, and is not  
18 consistent between metrics. At the 95<sup>th</sup> percentile, the partitioning expands into higher  
19 latitudes, however, many areas (continental interiors) remain equally dependent on  $T$  and  $Q$   
20 (Fig. 4d-f).  $T_w$  is largely driven by extreme moisture (Fig. 4f) and in some locations  
21 (monsoonal Africa, Indian sub-continent, and equatorial South America) very extreme  
22 moisture. HI is driven by  $T$  (Fig. 4e), and sWBGT is mixed between extreme  $Q$  and extreme  
23  $T$  (Fig. 4d). All three metrics agree with  $T$  in the Western United States and Middle East. At  
24 the 99<sup>th</sup> percentile, HI, although dominated by  $T$  worldwide, shows sign reversals in very  
25 small locations (Fig. 5e). Extreme  $Q$  expands for  $T_w$ , and all of the low latitudes experience  
26 moisture dependence except for Western United States and Middle East (Fig. 5f). sWBGT  
27 has some reversal of  $T$  to  $Q$  dominated heat stress (Western Africa).  $Q$  largely expands  
28 worldwide. In all instances, except for HI, high latitudes are equally dependent on  $Q$  and  $T$   
29 for heat stress.

30 Our final maps show SWMP65, SWMP80, and  $\theta_E$  at the 99<sup>th</sup> percentile. Maxima for  $\theta_E$  are  
31 spatially the same as  $T_w$  (Fig. 5c and 6c). Additionally,  $\theta_E$  partitions towards  $Q$ , just as  $T_w$

1 shows (Fig. 5f and 6f). Spatial patterns between SWMP65 and HI are similar (Fig. 5b and  
2 6a), and their regime maps show similar partitioning toward  $T$  globally, except for select  
3 locations of strong monsoonal locations that show  $Q$  dependency (Fig. 5e and 6d). Lastly,  
4 SWMP80 and sWBGTT share similar spatial patterns (Fig. 5a and 6b). As with the other  
5 paired metrics, their  $T$ - $Q$  regime maps share the same characteristics (Fig. 5d and 6e). Low  
6 latitudes show strong  $Q$  dependence, and higher latitudes switch to a  $T$  dependence.

7

## 8 **5 Discussion**

9 We designed the HumanIndexMod to calculate diagnostic heat stress and moist  
10 thermodynamics systematically. There are many approaches to evaluating heat stress.  
11 Monthly and seasonal temperature and moisture averages were used for general applications  
12 (Dunne et al., 2013), however these averages overestimate the potential severity of heat stress  
13 (Fig. 1c,d). Even using daily or sub-daily averages (Kjellstrom et al., 2009b; Hyatt et al.,  
14 2010; Fischer and Schar, 2010; Fischer and Knutti, 2012; Willett and Sherwood, 2012;  
15 Kjellstrom et al., 2013) potentially overestimates heat stress. This is due to the non-linear  
16 covariance of  $T$  and  $Q$ , and averages miss these extremes. Ultimately, capturing the diurnal  
17 cycle is crucial for quantifying heat stress extremes (Oleson et al., 2013b). Heat stress related  
18 illness is exacerbated by high heat stress nights as well as daytimes. To accurately calculate  
19 these extremes, one needs either high temporal resolution data, or directly computing them at  
20 each time step within climate models. We discuss the results from the implementation  
21 separately: moist thermodynamics and heat stress.

### 22 **5.1 Moist thermodynamics**

23 The spatial distributions of high heat stress are robust between CLM model versions (Oleson  
24 et al., 2011; Fischer et al., 2012; Oleson et al., 2013b). Due to the conservation of energy and  
25 entropy, calculating moist thermodynamic variables shows that climate models and reanalysis  
26 fall along constant lines of  $T_E$  (Eq. A.5), even out to the 99<sup>th</sup> percentile of daily values  
27 (Fischer and Knutti, 2012). The spread between models is small as compared to the spread in  
28  $T$ , thus using heat stress metrics in Earth system modeling may reduce the uncertainties of  
29 climate change (Fischer and Knutti, 2012).

30 Previous modeling studies have demonstrated that urban equatorial regions transition to a  
31 nearly permanent high heat stress environment when considering global warming (Fischer et



1 al., 2012; Oleson et al., 2013b). The convective regions are areas with the highest heat stress  
2 maximums and are often near coastal locations. Many of these metropolitan areas are in  
3 monsoonal regions, which have strong yearly moisture variability, yet the partitioning of heat  
4 stress is towards  $Q$ , not  $T$ , in these regions (Fig. 5d-f and 6d-f). Heat stress in both equatorial  
5 and monsoonal regions is expected to increase dramatically when considering global warming  
6 (Kjellstrom et al., 2009b; Fischer and Knutti, 2012; Dunne et al., 2013; Oleson et al., 2013b).  
7 Accurate moist thermodynamic calculations from the HumanIndexMod will aid future  
8 characterizations of heat stress.

## 9 **5.2 Heat stress**

10 We show that there are two regimes of heat stress globally in agreement between metrics in  
11 the CRUNCEP CLM4.5 simulation,  $T$  (Western United States and Middle East) and  $Q$   
12 (monsoonal regions). Western United States and Middle East regions consistently have  
13 higher temperatures and lower humidities than the monsoonal areas. However, we show that  
14 maximum heat stress is partitioned between  $T$  and  $Q$  globally. Characterizing arid regions  
15 versus non-arid regions may require different heat stress metrics (e.g. Oleson et al., 2013b,  
16 specifically the comparison between Phoenix and Houston). The HumanIndexMod provides  
17 this capability.

18 The assumptions/calibrations that derived the heat stress metrics in the HumanIndexMod are  
19 another avenue of research that may be explored using a global model. For example, the  
20 original equation that sWBGT was derived from was calibrated using US Marine Corps  
21 Marines during basic training (Minard et al., 1957), who are in top physical condition. HI  
22 was calibrated for an ‘average’ American male (Steadman, 1979a; Rothfus, 1990).  
23 Calculating these heat stress metrics, and the many others in the HumanIndexMod, at every  
24 time step within climate models were previously intractable due to insufficient data storage  
25 capabilities for high temporal resolution variables. We show that SWMP65 and SWMP80  
26 diverge in their values (Fig. 6a,b and 6d,e). Yet, SWMP80 and sWBGT are similar in spatial  
27 patterns and regimes, while HI and SWMP65 have similar patterns and regimes. What links  
28 SWMP65 and SWMP80 together is  $T_w$ . Swamp coolers are evaporators, and as their  
29 efficiency approaches 100%, their solutions approach  $T_w$ . Figures 5 and 6 are similar to a  
30 circuit resistor, or stomatal resistance (Oke, 1987), which is measure of efficiency. The  
31 ‘average’ person (HI) may be acting as a stronger resistor to evaporation than one that is  
32 acclimatized (sWBGT). The HumanIndexMod may explore the effects of acclimatization,

1 and its impact on efficiency of evaporative cooling through climate modeling. This type of  
2 research may ultimately reduce the number metrics required for computing heat stress.

3 Exposure to high moist temperatures, ultimately, threatens humans physically, and long-term  
4 exposure may lead to death. Extreme moist temperatures are projected to increase in the  
5 future, and potentially may reach deadly extremes, permanently in some regions (Sherwood  
6 and Huber, 2010). Heat stress indices have the ability to diagnose instantaneous exposure.  
7 Diagnostic models, however, cannot measure or evaluate the potential impacts of long-term  
8 exposure to heat stress accurately. Prognostic thermal physiological models can be used to  
9 predict the complexities of heat stress on humans.

10 Prognostic thermal physiology considers wind, ambient temperature, and moisture from the  
11 environment, as well as internal processes, such as blood flow and sweat. There are  
12 numerous different forms of prognostic models (Table 1). Some of them are quite  
13 complicated, using hundreds of grid cells to represent all parts of the body (Fiala et al., 1999).  
14 Less complicated models represent the human body as a single cylinder with multiple layers  
15 (Kraning and Gonzalez, 1997). Neither computational method is currently coupled to Earth  
16 system models, and this is a significant gap in determining future heat stress impacts that the  
17 HumanIndexMod may not be able to fulfill. To make progress towards representing the  
18 effects of heat stress on the human body prognostically, we recommend, as a first step,  
19 incorporating mean radiant temperature of humans. Radiation is a major component of  
20 human energy balance, and implementing this also allows incorporating more accurate  
21 diagnostics, such as Wet Bulb Globe Temperature (Minard et al., 1957) and the Universal  
22 Thermal Climate Index (Havenith et al., 2012).

23

## 24 **6 Summary**

25 We present the HumanIndexMod that calculates 9 heat stress metrics and 4 moist  
26 thermodynamical quantities. The moist thermodynamic variables use the latest accurate and  
27 efficient algorithms available. The heat stress metrics cover three developmental  
28 philosophies: comfort, physiological, and empirically based algorithms. The code is  
29 designed, with minimal effort, to be implemented into general circulation, land surface, and  
30 weather forecasting models. Additionally, this code may be used with archived data formats  
31 and local weather stations.

1 Furthermore, we have implemented the HumanIndexMod into the latest public release version  
2 of CLM4.5. Archival is flexible, as the user may choose to turn on high frequency output,  
3 and the default is monthly averages. Additionally, monthly urban and rural output of the  
4 metrics is default. We show that the module may be used to explore new avenues of research:  
5 characterization of human heat stress, model diagnostics, and intercomparisons of heat stress  
6 metrics. Our results show that there are two regimes of heat stress, extreme moisture and  
7 extreme temperature, yet all of the most extreme heat stress events are tied to maximum  
8 moisture.

9 Our approach has limitations. None of the metrics in the HumanIndexMod include the effects  
10 of solar and thermal radiation. Radiation is a non-negligible component of heat stress. As a  
11 consequence, the heat stress metrics presented always assume that the subject is not in direct  
12 solar exposure. Additionally, the indices represent a diagnostic environment for heat stress.  
13 These metrics do not incorporate prognostic components or complex physiology of the human  
14 thermal system.

15 Overall, the HumanIndexMod provides a systematic way for implementing an aspect of  
16 thermo-animal physiology into an Earth system modeling framework. Incorporating the  
17 HumanIndexMod into a variety of different models would provide a baseline for model-  
18 model comparisons of heat stress, such as the Coupled Model Intercomparison Project  
19 (CMIP) (Taylor et al., 2012) and other collaborative modeling frameworks. We encourage  
20 researchers to incorporate the HumanIndexMod within their research environments.

21

## 22 **Code Accessibility**

23 We will make the HumanIndexMod available at the University of New Hampshire Data  
24 Discover Center New Hampshire Climate section. The NSF-funded New Hampshire  
25 EPSCoR Ecosystem and Society Project manage this data archive. Additionally, we will  
26 upload the HumanIndexMod to Data.gov, a free repository for data, metrics, and results for  
27 public use. The United States Government manages this repository.

28

## 29 **Appendix A: Moist Thermodynamics**

30 Davies-Jones (2008) shows multiple methods of computing  $T_w$ , and we implemented the most  
31 accurate equations, described below. We introduce terminology to describe the Davies-Jones

1 (2008) calculation. All temperature subscripts that are capitalized are in Kelvin, while lower  
 2 case are in Celsius.  $\kappa_d$  is the Poisson constant for dry air (0.2854), and  $\lambda$  is the inverse  
 3 (3.504). Many of the following equations are scaled using non-dimensional pressure (also  
 4 known as the Exner function),  $\pi$ :

$$5 \quad \pi = (p/p_0)^{1/\lambda} \quad (\text{A.1})$$

6 where  $p$  is the pressure (mb), and  $p_0$  is a reference pressure (1000mb).

7 To define  $T_w$  (the wet bulb temperature), we solve for the equivalent potential temperature,  $\theta_E$ .  
 8 Determining  $\theta_E$  is a three-step process. First, we solve for the lifting condensation  
 9 temperature ( $T_L$ ):

$$10 \quad T_L = \frac{1}{\frac{1}{T-55} - \frac{\ln(RH/100)}{2840}} + 55 \quad (\text{A.2})$$

11 where  $T$  is the parcel temperature (Kelvin). For example, we use the 2 m air temperature in  
 12 CLM4.5.  $RH$  (%) is taken at the same height as  $T$ .  $T_L$  (Eq. A.2), from Eq. (22) Bolton (1980),  
 13 is the temperature at which a parcel that is lifted, following a dry adiabatic lapse rate, begins  
 14 to condense. Second, as the air rises further, the parcel now follows a moist potential  
 15 temperature,  $\theta_{DL}$ :

$$16 \quad \theta_{DL} = T \left( \frac{p_0}{p-e} \right)^{\kappa_d} \left( \frac{T}{T_L} \right)^{0.00028r} \quad (\text{A.3})$$

17 where  $e$  is the parcel vapor pressure (mb) (using CLM4.5, this is the 2 m vapor pressure), and  
 18  $r$  is the mixing ratio (g/kg) (this is converted from the 2 m height  $Q$  to  $r$  in CLM4.5). Third,  
 19 the parcel is raised to a great height where all latent heat is transferred to the air parcel, and  
 20 the water is rained out, giving the solution to  $\theta_E$ . There are many methods for representing  
 21 this process. The analytical solution (Holton, 1972) is computationally prohibitive in  
 22 atmospheric and land surface models. There are various approximations of different aspects  
 23 of potential and saturated temperatures to calculate  $\theta_E$  (Betts and Dugan, 1973; Simpson,  
 24 1978), however, many of them have large errors. These errors are compared in Bolton  
 25 (1980), and Eq. (39) (Bolton's formulation) is up to an order of magnitude more accurate:

$$26 \quad \theta_E = \theta_{DL} \exp \left[ \left( \frac{3.036}{T_L} - 0.001788 \right) r (1 + 0.000448r) \right] \quad (\text{A.4})$$

27 Equivalent temperature,  $T_E$ , is  $\theta_E$  scaled by  $\pi$ :

$$28 \quad T_E = \theta_E \pi \quad (\text{A.5})$$

1 The initial guess for  $T_w$  is based upon regions where the second order derivative of  $\theta_E$  reaches  
 2 a linear relationship with variations in  $T_w$  and  $\lambda$ . Two coefficients are derived (Davies-Jones,  
 3 2008):

$$4 \quad k1 = -38.5\pi^2 + 137.81\pi - 53.737 \quad (\text{A.6})$$

$$5 \quad k2 = -4.392\pi^2 + 56.831\pi - 0.384 \quad (\text{A.7})$$

6 The initial guess of  $T_w$  for coldest temperatures:

$$7 \quad T_w = T_E - C - \frac{Ar_s(T_E, \pi)}{1 + Ar_s(T_E, \pi) \frac{\partial \ln(e_s)}{\partial T_E}} \quad (\text{A.8})$$

8 where  $C$  is freezing temperature,  $A$  is a constant (2675), and  $r_s$  is the saturated mixing ratio.

9 The evaluation of errors at a various pressures necessitated that Davies-Jones develop a  
 10 regression line on colder regions of the initial guess:

$$11 \quad \left(\frac{C}{T_E}\right)^\lambda > D(\pi); D = \left(0.1859 \frac{p}{p_0} + 0.6512\right)^{-1} \quad (\text{A.9})$$

12 where  $D$  is calculating transition points between quadratic fits to the second order derivatives  
 13 of  $\theta_E$ .  $T_w$  for all other temperature regimes is governed by:

$$14 \quad T_w = k1(\pi) - 1.21cold - 1.45hot - (k2(\pi) - 1.21cold) \left(\frac{C}{T_E}\right)^\lambda + \left(\frac{0.58}{\left(\frac{C}{T_E}\right)^\lambda}\right)hot$$

15 (A.10)

$$16 \quad cold \left\{ \begin{array}{l} = 0: 1 \leq \left(\frac{C}{T_E}\right)^\lambda \leq D(\pi) \\ = 1 \end{array} \right. \quad (\text{A.11})$$

$$17 \quad hot \left\{ \begin{array}{l} = 1: T_E > 355.15 \\ = 0 \end{array} \right. \quad (\text{A.12})$$

18 where the combination of equations' initial guesses are valid from 1050mb down to 100mb.  
 19 Following the initial guess, up to two iterations using the Newton-Raphson method are  
 20 required to reach the true wet bulb temperature. Using  $T_w$ , saturation vapor pressure is solved  
 21 by the August-Roche-Magnus formulation of the Clausius-Clayperon equation (Bolton, 1980;  
 22 Lawrence, 2005):

$$23 \quad e_s(T_w) = 6.112 \exp\left(\frac{a(T_w - C)}{T_w - C + b}\right) \quad (\text{A.13})$$

24 where  $e_s$  is in mb,  $a$  and  $b$  are constants. The saturation mixing ratio,  $r_s$ , is dependent on  $e_s$ :

$$1 \quad r_s(T_W) = \frac{\varepsilon e_s(T_W)}{(p_0 \pi^\lambda - e_s(T_W))} \quad (\text{A.14})$$

2 where  $\varepsilon$  is a constant ( $\sim 0.622$ ). Following Davies-Jones, we use the derivative of ARM  
3 equation for calculating the derivative of  $r_s$ :

$$4 \quad \frac{\partial \ln(e_s)}{\partial T_W} = \frac{ab}{(T_W - c + b)^2} \quad (\text{A.15})$$

$$5 \quad \frac{\partial e_s}{\partial T_W} = e_s \frac{\partial \ln(e_s)}{\partial T_W} \quad (\text{A.16})$$

$$6 \quad \left( \frac{\partial r_s}{\partial T_W} \right)_\pi = \frac{\varepsilon p}{(p - e_s(T_W))^2} \frac{\partial e_s}{\partial T_W} \quad (\text{A.17})$$

7 Now, we return to  $\theta_E$ , and substitute  $T_W$  for  $T_L$ :

$$8 \quad f(T_W; \pi) = \left( C/T_W \right)^\lambda \left[ 1 - \frac{e_s}{p_0 \pi^\lambda} \right]^{\kappa_d \lambda} \exp(-\lambda G(T_W; \pi)) \quad (\text{A.18})$$

9 where:

$$10 \quad G(T_W; \pi) = \left( \frac{3036}{T_W} - 1.78 \right) [r_s(T_W; \pi) + 0.448 r_s^2(T_W; \pi)] \quad (\text{A.19})$$

11 The derivative of the function Eq. (A.18) is required for the Newton-Raphson method:

$$12 \quad f'(T_W; \pi) = -\lambda \left[ \frac{1}{T_W} + \frac{\kappa_d}{(p - e_s(T_W))} \frac{\partial e_s}{\partial T_W} + \left( \frac{\partial G}{\partial T_W} \right)_\pi \right] \quad (\text{A.20})$$

13 where the derivative of  $G(T_W; \pi)$ :

$$14 \quad \left( \frac{\partial G}{\partial T_W} \right)_\pi = -\frac{3036(r_s(T_W) + 0.448 r_s^2(T_W))}{T_W^2} \left( \frac{3036}{T_W} - 1.78 \right) \left( 1 + 2(0.448 r_s(T_W)) \right) \left( \frac{\partial r_s}{\partial T_W} \right)_\pi \quad (\text{A.21})$$

15 and, due to the linear relationship of the second order derivative of Eq. (A.18), we may  
16 accelerate the Newton-Raphson method using the initially calculated  $T_W$  and  $T_E$ :

$$17 \quad T_W = T_W - \frac{f(T_W; \pi) - (C/T_E)^\lambda}{f'(T_W; \pi)} \quad (\text{A.22})$$

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1 Table 1. Heat stress diagnostics and prognostic models.

Metric	Type	Ref.
Wet Bulb Temperature	Temperature	Haldane (1905)
Effective Temperature	Index	Houghton and Yaglou (1923)
Equivalent Temperature	Temperature	Dufton (1929)
Heat Stress Index	Index	Belding and Hatch (1955)
Wet Bulb Globe Temperature	Index	Yaglou and Minard (1957)
Discomfort Index	Index	Thom (1959)
Temperature Humidity Index	Index	Ingram (1965)
Temp. Regulation in Man	Prognostic	Stolwijk and Hardy (1966)
Physiological Mathematical Model	Prognostic	Wyndham and Atkins (1968)
Solar Heat in Man	Index	Breckenridge and Goldman (1971)
Mathematical Model Temperature in Man	Prognostic	Stolwijk (1971)
New Effective Temperature	Index	Gagge (1972)
Humidex	Index	Masterson and Richardson (1979)
Sultriness Index	Index	Steadman (1979a)
Mathematical Model Thermal Regulation	Prognostic	Stolwijk (1980)
Apparent Temperature	Index	Steadman (1984)
Heat Index	Index	Rothfus (1990)
Computer Based Thermal Response	Prognostic	Haslam and Parsons (1994)
SCENARIO	Prognostic	Kraning and Gonzalez (1997)

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Computer Model Human Thermo-Regulation	Prognostic	Fiala et al. (1999); Fiala et al. (2001)
PET	Index	Höppe (1999)
Environmental Stress Index	Index	Moran et al. (2001)
SCENARIO Monte Carlo	Prognostic	Gonzalez (2004)
Generalized Transient Thermal Model	Prognostic	Khan et al. (2004)
ISO 7243 WBGT	Index	Parsons (2006)
IDCA	Prognostic	Yokota et al. (2008)
Physiological Equivalent Temperature	Index	Jendritzky et al. (2009)
UTCI	Index	Fiala et al. (2010)
UTCI-Fiala Model	Index-Prognostic	Fiala et al. (2011)
Index of Equivalent Temperature	Index	Liang et al. (2011)

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1

1 Table 2. Moist temperature variables and heat stress metrics.

Metric	Variable	Equation #
Temperature (Kelvin)	$T$	N/A
Temperature (Celsius)	$T_C$	N/A
Temperature (Fahrenheit)	$T_F$	N/A
Pressure	$P$	N/A
Relative humidity	$RH$	N/A
Specific humidity	$Q$	N/A
10 m Winds	$u_{10m}$	N/A
Vapor Pressure (mb)	$e_{RH}$	2
Vapor Pressure (Pa)	$e_{sPa}$	N/A
Saturated vapor pressure (mb)	$e_s$	A.13
Derivative saturated vapor pressure	$de_s/dT$	A.16
Log derivative saturated vapor pressure	$d(\ln(e_s))/dT$	A.15
Mixing ratio	$r_s$	A.14
Derivative mixing ratio	$dr_s/dT$	A.17
Function of equivalent potential temperature	$f(\theta_E)$	A.18
Derivative of function of equivalent potential temperature	$f'(\theta_E)$	A.20
Wet Bulb Temperature	$T_w$	A.22
Wet Bulb Temperature, Stull	$T_{wS}$	8-9
Lifting condensation	$T_L$	A.2

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temperature		
Moist potential temperature	$\theta_{DL}$	A.3
Equivalent potential temperature	$\theta_E$	A.4
Equivalent temperature	$T_E$	A.5
Heat Index	$HI$	3
Apparent Temperature	$AT$	1
Humidex	$HUMIDEX$	4
Simplified WBGT	$sWBGT$	7
Discomfort Index	$DI$	10
Temperature Humidity Index for Comfort	$THIC$	5
Temperature Humidity Index for Physiology	$THIP$	6
Swamp cooler efficiency 65%	$SWMP65$	11
Swamp cooler efficiency 80%	$SWMP80$	11

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1 Table 3. List of previous heat stress studies. Studies using datasets, reanalysis, and/or model  
 2 output that range from ~1900 until ~2010 are labeled ‘Modern’ and from ~2005 to ~2100 are  
 3 labeled Future. Some studies do not analyze heat stress quantitatively (Assessment).

Location	Metric	Time	Model	Ref.
Mediterranean Sea	<i>HI</i>	Modern and Future	RegCM3	Diffenbaugh et al. (2007)
Delhi	<i>WBGT</i>	Modern	NOAA	Kjellstrom et al. (2009a)
World	<i>sWBGT</i>	Future	HadCM3	Kjellstrom et al. (2009b)
World Cities	<i>WBGT, T</i>	Modern and Future	NOAA/Various Models	Kjellstrom et al. (2009c)
Global	<i>PET variation</i>	Future	ECHAM4	Jendritzky and Tinz (2009)
Global	$T_w$	Modern and Future	CCSM3/ERA Interim	Sherwood and Huber (2010)
Europe	<i>HI, HUMIDEX</i>	Future	ENSEMBLES	Fischer and Schar (2010)
Global	<i>indoorWBGT</i>	Modern and Future	NOAA	Hyatt et al. (2010)
Global	—	Modern	Assessment	Nilsson and Kjellstrom (2010)
Southern Brazil	<i>UTCI</i>	Modern	Direct Measurement	Bröde et al. (2012)
Global	<i>sWBGT</i>	Modern and Future	CLM4	Fischer et al. (2012)
Global	<i>sWBGT</i>	Modern and Future	HadCRUH/ISD-NCDC	Willett and Sherwood

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Global	<i>T</i>	Modern	Various Datasets	(2012) SREX IPCC
Western India	<i>WBGT, T</i>	Modern	Direct Measurement	(2012) Nag et al. (2013)
California Farms	—	Modern	Assessment	Stoecklin- Marois et al. (2013)
Thailand	—	Modern	Assessment	Tawatsupa et al. (2013)
Nepal	<i>sWBGT, HI, HUMIDEX</i>	Modern	Direct Measurement	Pradhan et al. (2013)
South East Asia	<i>WBGT</i>	Modern and Future	GSOD/CRU/BC M2	Kjellstrom et al. (2013)
Quebec	<i>T</i>	Future	Assessment	Adam-Poupart et al. (2013)
Global	<i>indoorWBGT</i>	Modern and Future	ESM2M/NCEP- NCAR	Dunne et al. (2013)
United States	<i>sWBGT, DI, HI, HUMIDEX, AT</i>	Modern and Future	CLM4/CLMU/W RF	Oleson et al. (2013b)

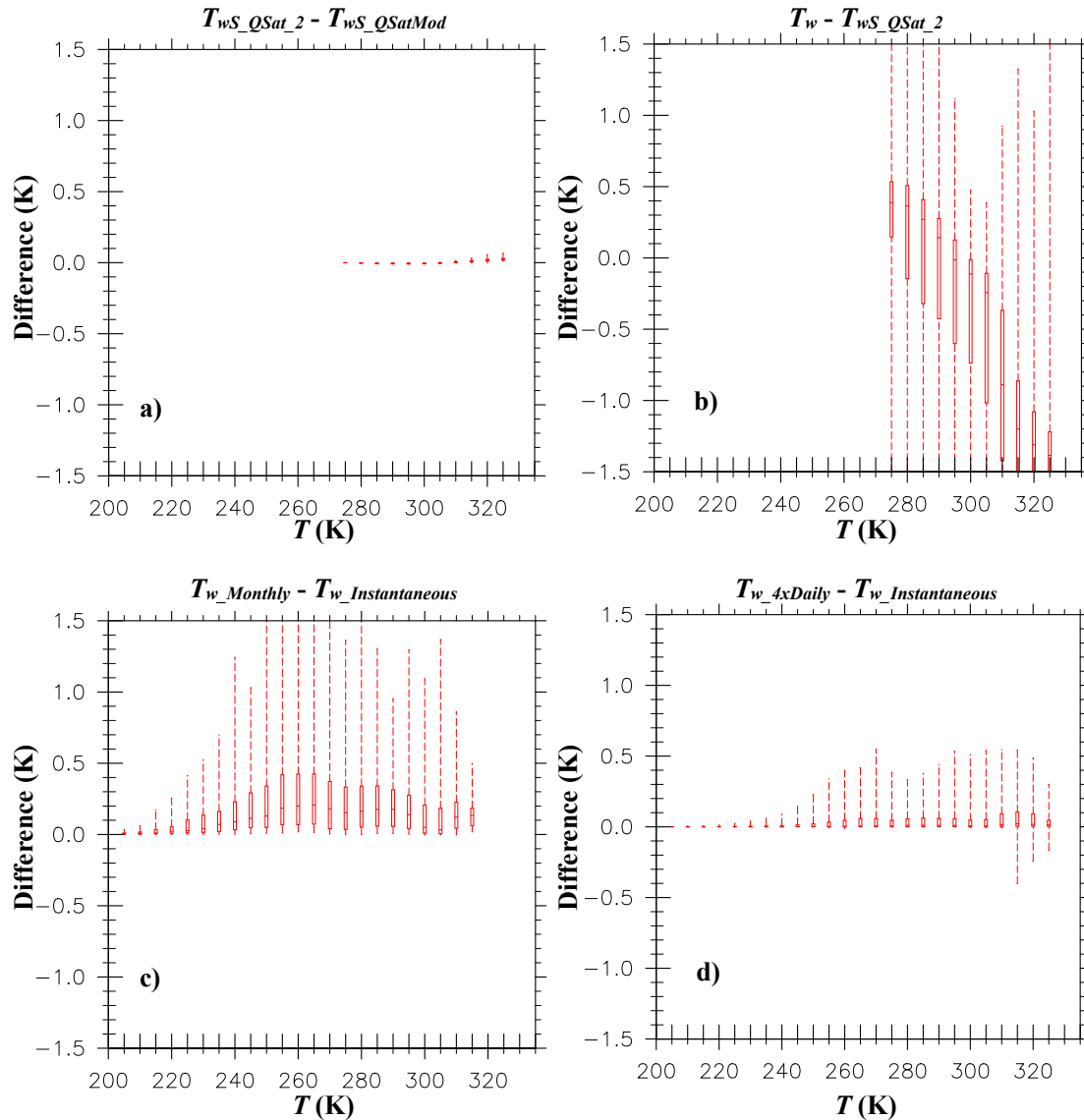
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1 Table 4. The HumanIndexMod: subroutine names, required inputs, and variables calculated.

Name	Subroutine	Input	Calculates
Moist Thermodynamics	<i>Wet_Bulb</i>	$T, e_{RH}, P, RH, Q$	$T_E, \theta_E, T_w$
Wet Bulb Temperature, Stull	<i>Wet_BulbS</i>	$T_C, RH$	$T_{wS}$
Heat Index	<i>HeatIndex</i>	$T_C, RH$	$HI$
Apparent Temperature	<i>AppTemp</i>	$T_C, e_{RH}, Wind$	$AT$
Simplified WBGT	<i>swbgt</i>	$T_C, e_{RH}$	$sWBGT$
Humidex	<i>hmdex</i>	$T_C, e_{RH}$	$HUMIDEX$
Discomfort Index	<i>dis_coi</i>	$T_C, T_w$	$DI$
Discomfort Index w/Stull	<i>dis_coiS</i>	$T_C, T_{wS}$	$DI$
Temperature Humidity Index	<i>THIndex</i>	$T_C, T_w$	$THIC, THIP$
Swamp Cooler Efficiency	<i>SwampCoolEff</i>	$T_C, T_w$	$SWMP65, SWMP80$
Kelvin to Celsius	<i>KtoC</i>	$T$	$T_C$
Vapor Pressure	<i>VaporPres</i>	$RH, e_s$	$e_{RH}$
Saturated Vapor Pressure	<i>QSat_2</i>	$T, P$	$e_s, de_s/dT, d(\ln(e_s))/dT, r_s, dr_s/dT, f(\theta_E), f'(\theta_E)$

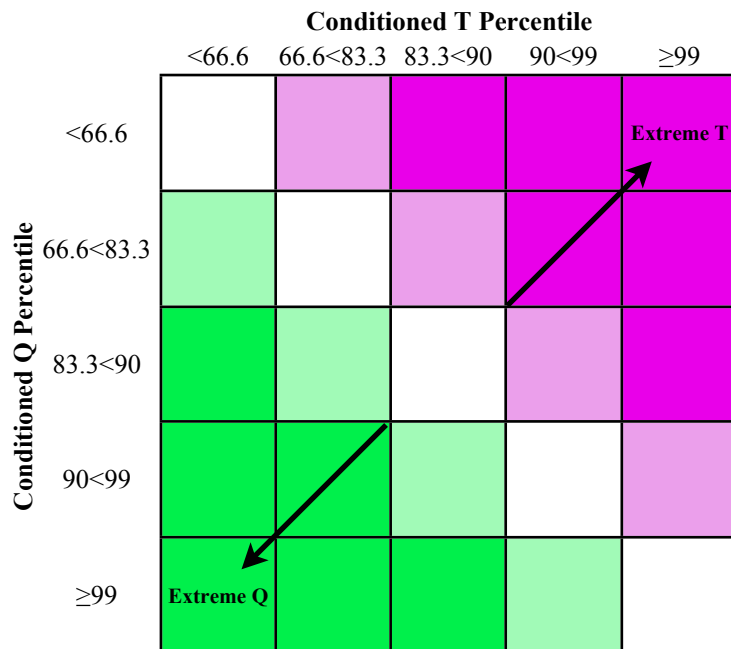
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## Wet Bulb Evaluation



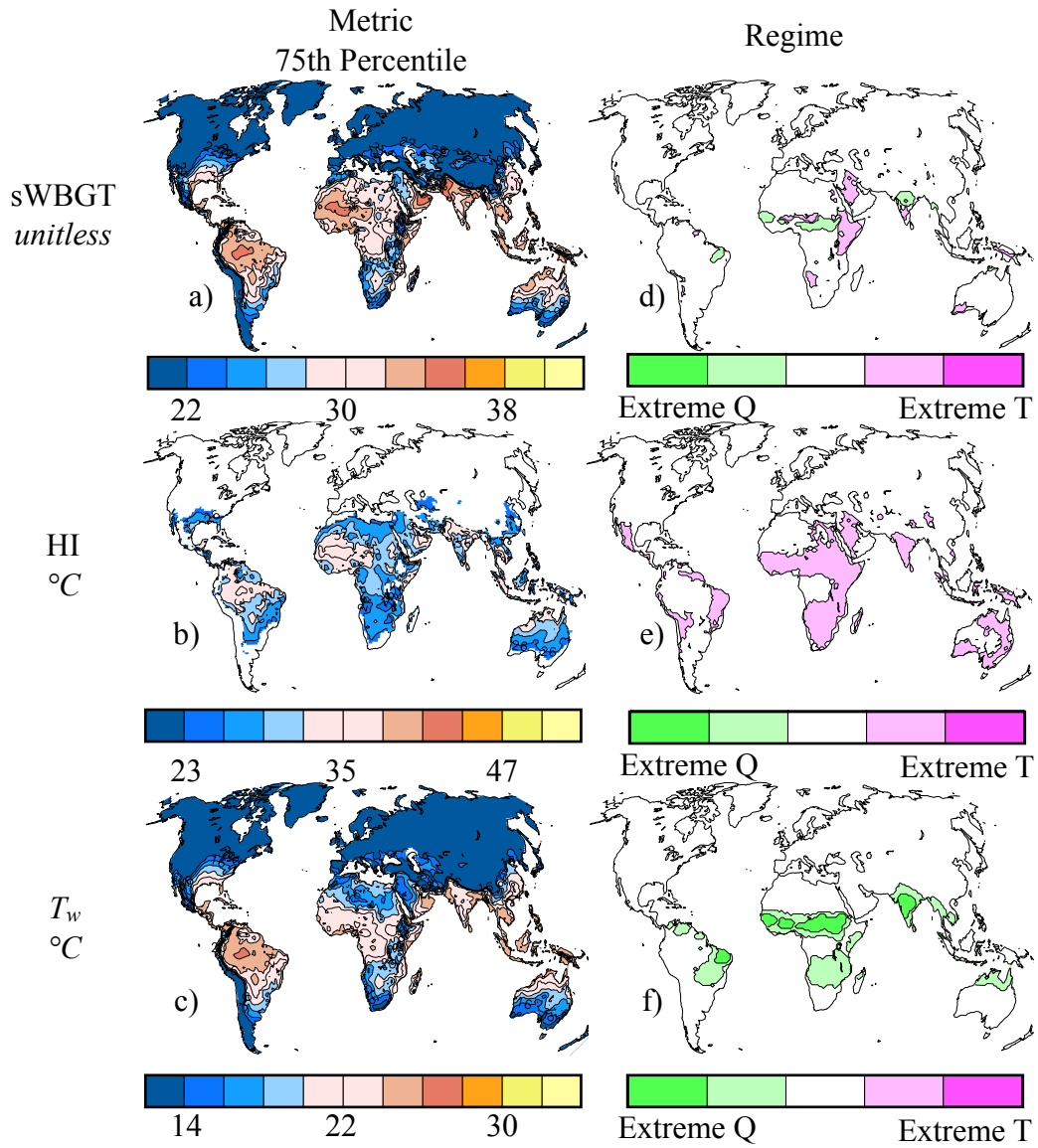
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2 Figure 1. Evaluation of wet bulb temperatures. The boxes represent the 90% confidence  
 3 interval. The upper and lower tails represent the 100% confidence interval. The horizontal  
 4 line in each box is the median value. a) difference between  $T_{ws}$  using QSat\_2 saturated vapor  
 5 pressure and QSatMod saturated vapor pressure over the valid range for  $T_{ws}$ . b) difference  
 6 between  $T_w$  (Davies-Jones, 2008) and  $T_{ws}$  (Stull, 2011) (both using QSat\_2 saturated vapor  
 7 pressure calculation) over the valid range for  $T_{ws}$ . c) is the difference between using model  
 8 monthly averaged input fields and model instantaneous fields to calculate monthly  $T_w$ . d)  
 9 difference between using model 4x Daily averaged input fields and model instantaneous fields  
 10 to calculate 4x Daily  $T_w$ . For a), b), and d) the inputs of  $T$ ,  $P$ , and  $Q$  are derived from model  
 11 4x Daily fields from the years 2001-2010. For c) the inputs of  $T$ ,  $P$ , and  $Q$  are derived from  
 12 model Monthly fields from the years 2001-2010.

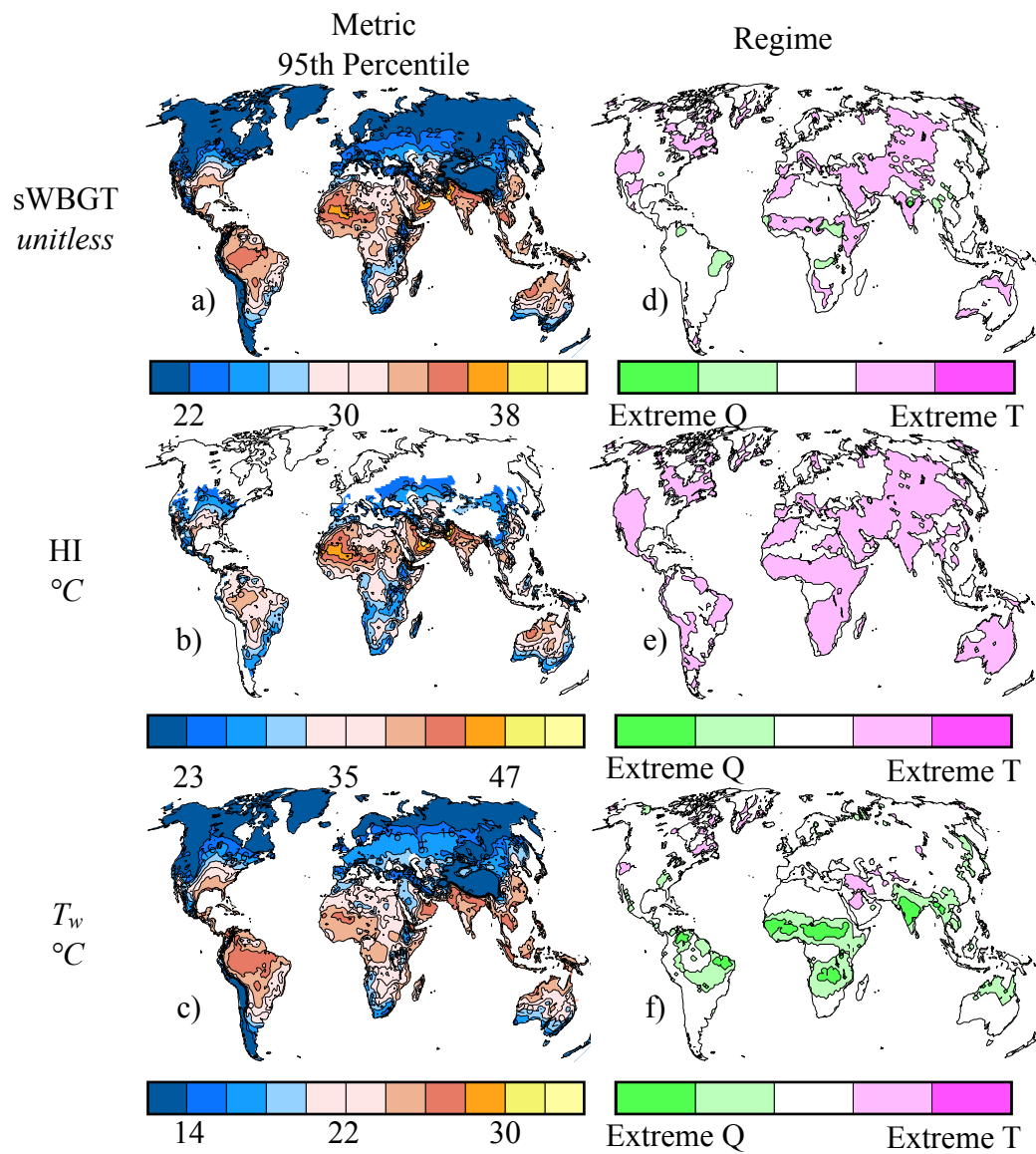


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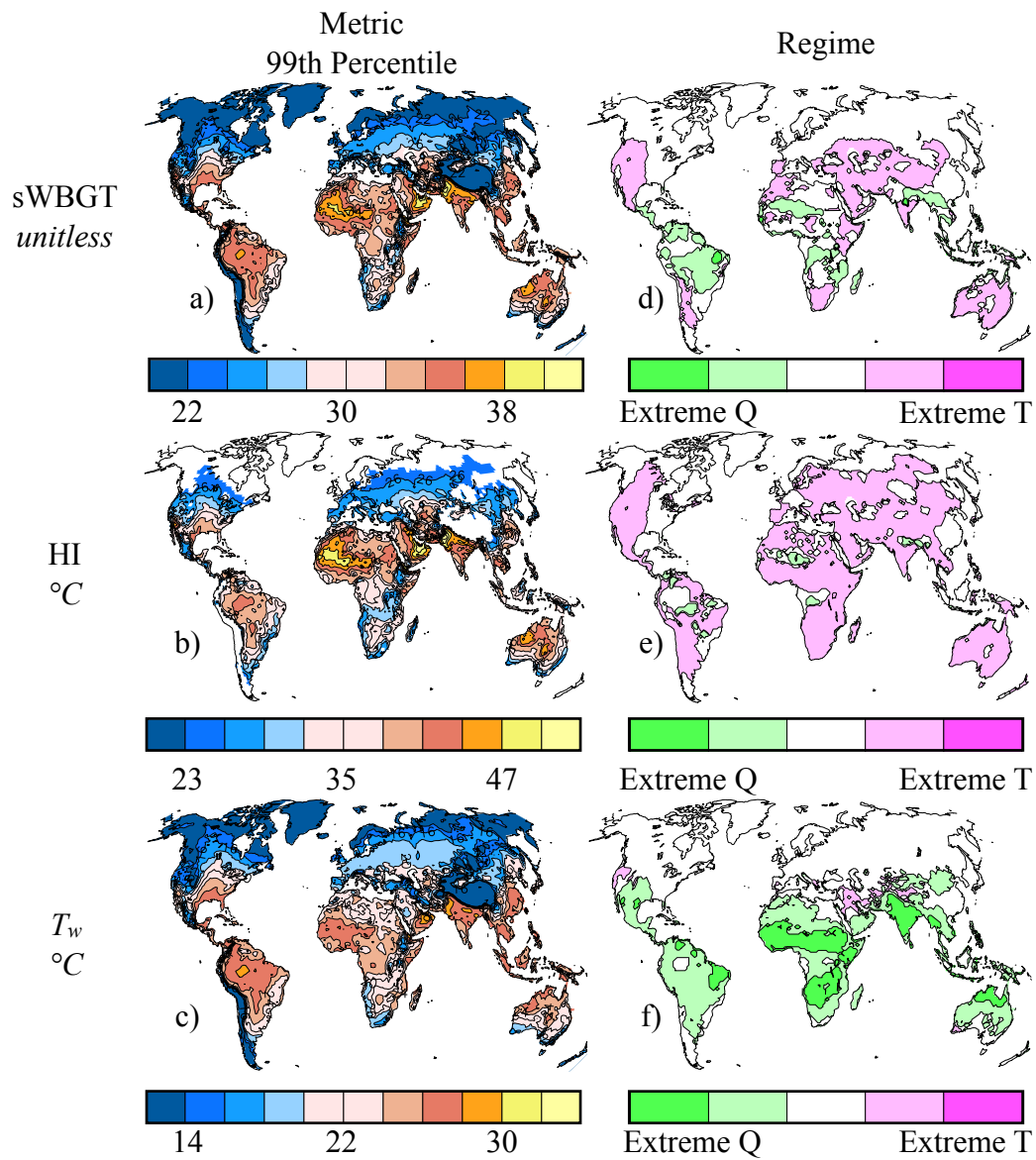
2 Figure 2. Expected value ranking.  $T$  and  $Q$  conditioned upon exceedance value of a heat  
 3 stress or moist thermodynamic metric. The  $T$  and  $Q$  values are compared to their respective  
 4 time series as a percentile. These  $T$  and  $Q$  percentiles are binned and are compared to each  
 5 other. Extreme  $Q$  are greens and extreme  $T$  are magentas.



1  
 2 Figure 3. 75th percentile exceedance value of 3 metrics for a) sWBGT, b) HI, and c)  $T_w$  (left).  
 3 Expected rank value  $T$ - $Q$  regime maps d), e), and f) (right) conditioned by a), b) and c),  
 4 respectively. Rank values for d)-f) are described in Figure 2.

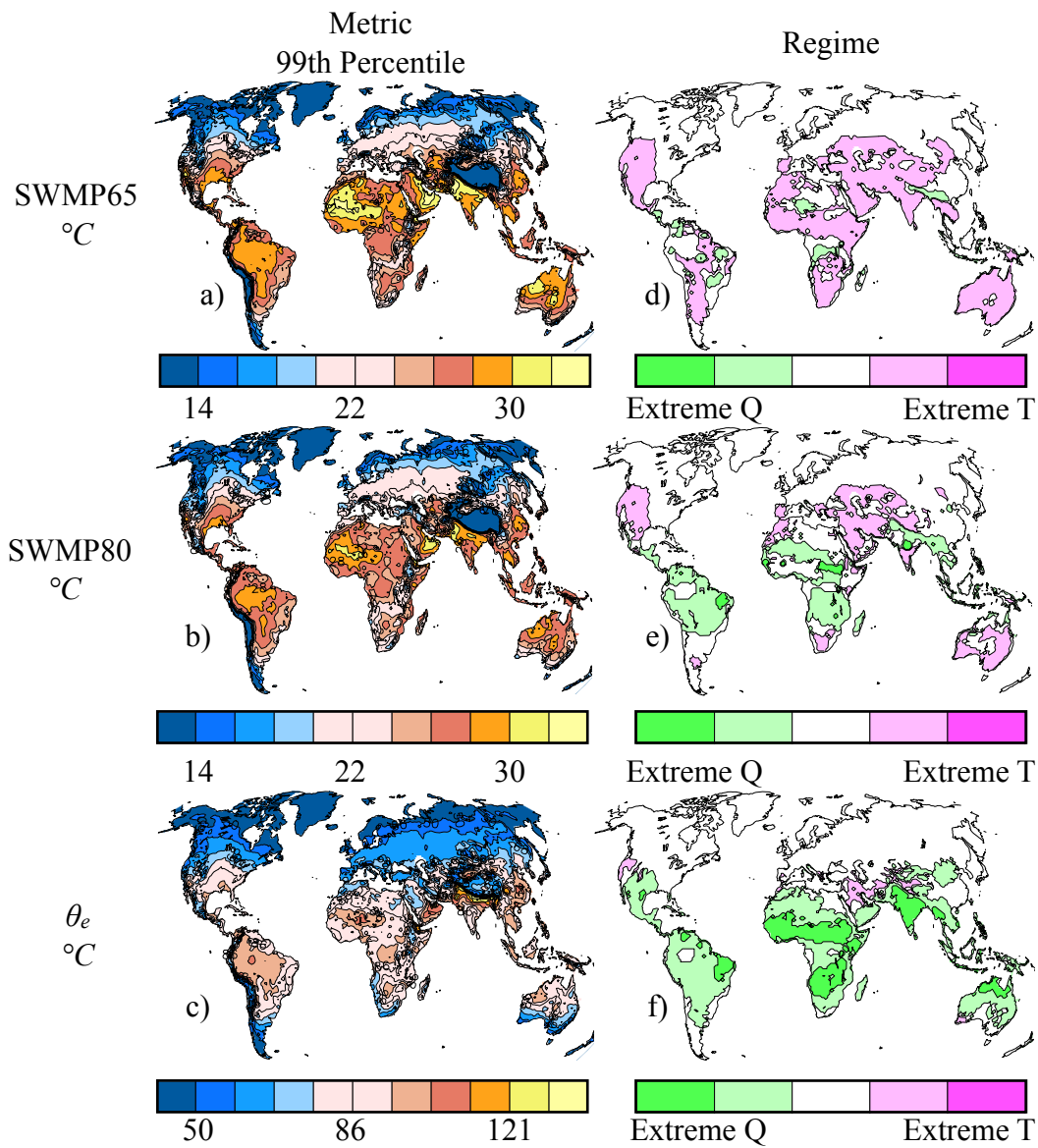


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 2 Figure 4. 95th percentile exceedance value of 3 metrics for a) sWBGT, b) HI, and c)  $T_w$  (left).  
 3 Expected rank value  $T$ - $Q$  regime maps d), e), and f) (right) conditioned by a), b) and c),  
 4 respectively. Rank values for d)-f) are described in Figure 2.



1  
 2 Figure 5. 99th percentile exceedance value of 3 metrics for a) sWBGT, b) HI, and c)  $T_w$  (left).  
 3 Expected rank value  $T$ - $Q$  regime maps d), e), and f) (right) conditioned by a), b) and c),  
 4 respectively. Rank values for d)-f) are described in Figure 2.





1  
 2 Figure 6. 99th percentile exceedance value of 3 metrics for a) SWMP65, b) SWMP80, and c)  
 3  $\theta_E$  (left). Expected rank value  $T$ - $Q$  regime maps d), e), and f) (right) conditioned by a), b) and  
 4 c), respectively. Rank values for d)-f) are described in Figure 2.