

1           **Uncertainty in Lagrangian pollutant transport simulations due to**  
2                           **meteorological uncertainty at mesoscale**

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17 **Key Points:**

18 Ensemble spread of tracer concentrations from a Lagrangian particle dispersion model  
19 (FLEXPART-WRF) is presented.

20 Uncertainty of tracer concentrations at grid scale due only to meteorological uncertainty is 30-40%.

21 Uncertainty of tracer age due only to meteorological uncertainty is 15-20%.

22 No simple relationships are found between tracer spread and local physical parameters.

23

24 **Abstract**

25 Lagrangian particle dispersion models require meteorological fields as input. Uncertainty in the  
26 driving meteorology is one of the major uncertainties in the results. The propagation of uncertainty  
27 through the system is not simple, and has not been thoroughly explored. Here, we take an  
28 ensemble approach. Six different configurations of the Weather Research and Forecast (WRF)  
29 model drive otherwise identical simulations with FLEXPART-WRF for 49 days over eastern North  
30 America. The ensemble spreads of wind speed, mixing height, and tracer concentration are  
31 presented. Uncertainty of tracer concentrations due solely to meteorological uncertainty is 30-40%.  
32 Spatial and temporal averaging reduces the uncertainty marginally. Tracer age uncertainty due  
33 solely to meteorological uncertainty is 15-20%. These are lower bounds on the uncertainty,  
34 because a number of processes are not accounted for in the analysis.

35

36 **Index Terms:**

37 0345 Pollution: urban and regional

38 0368 Troposphere: constituent transport and chemistry

39 3307 Boundary layer processes

40 3355 Regional modeling

41 **Keywords:**

42 Lagrangian particle dispersion model (LPDM)

43 Uncertainty

44 FLEXPART

45 WRF

46 Tracer transport

47 Southeast U.S.

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49     **1. Introduction**

50 Lagrangian particle dispersion models (LPDMs) are commonly used to simulate transport of trace  
51 gasses and aerosols for air pollution studies, greenhouse gas tracking, determination of sources of  
52 radiative releases [Stohl *et al.*, 2012], and forecasting of volcanic impacts. Lagrangian models are  
53 efficient, flexible, and self-adjoint. The latter property means that simulations can be run backward  
54 in time to find the sources of species observed at a particular time and place, which can provide a  
55 very large gain in efficiency. Backward runs are used, among other uses, to invert measurements to  
56 find source emission strengths and locations [Brioude *et al.*, 2011; Brioude *et al.*, 2013b; Locatelli  
57 *et al.*, 2013] (and many others). LPDMs are used at scales ranging from global to mesoscale.

58 Uncertainty in LPDM results is difficult to assess. Many sources of uncertainty exist, among the  
59 most important being uncertainty in emissions and uncertainty in the driving meteorology.  
60 Lagrangian models require meteorological fields as input. These are usually provided by  
61 operational output or reanalysis from a numerical weather prediction model.. For global or large-  
62 scale simulations, output from global operational models or associated reanalyses is commonly  
63 used. Mesoscale simulations require more finely resolved input data (here we define mesoscale as  
64 intended to resolve features 10-100 kilometers in size). Many groups run their own mesoscale  
65 meteorological simulations. Assessing the uncertainties and biases in those simulations is itself  
66 difficult, since observations are sparse and themselves uncertain. Further, the propagation of errors  
67 from the meteorological fields through the LPDM is not trivial. Some aspects are obvious. For  
68 example, random errors in wind direction will broaden the plume from a small source. However,  
69 the limits of this kind of thinking become clear quite quickly when one considers a plume  
70 propagating in a spatially inhomogeneous and temporally changing atmosphere, in which the errors

71 also change in space and time. This is precisely the situation for which mesoscale simulations are  
72 needed.

73 In this paper we present LPDM (FLEXPART-WRF) [Brioude *et al.*, 2013a] simulations driven by a  
74 six-member ensemble of meteorological model runs. Other than the driving meteorology, the  
75 FLEXPART-WRF runs are identical. FLEXPART-WRF is run forward in time, transporting  
76 specified tracer emissions. We postulate that the ensemble spread of wind speed and of mixing  
77 height represent the uncertainty of the meteorological simulation. The spread of the tracer  
78 concentrations then represents the meteorological uncertainty as propagated through FLEXPART-  
79 WRF. However, such a small ensemble probably does not represent the full range of uncertainty.  
80 Biases due to errors in parts of the model common to all configurations will produce biases in the  
81 ensemble output that cannot be detected. We therefore attempt to interpret the results with suitable  
82 modesty. Many results are presented with one significant figure, or as ranges, to avoid unwarranted  
83 precision. We also note that the generality of the results is unknown. The region we cover is in the  
84 middle of a continent, with only modest terrain, and we only consider six weeks of one season. We  
85 use spatially distributed emissions; point sources might produce rather different results.

86 *Hegarty et al.* [2013] showed that differences between LPDMs are much smaller than differences  
87 between meteorological models, pointing out the fact that uncertainties most likely arise from the  
88 meteorological models when Lagrangian models are used. The propagation of uncertainty from  
89 meteorological fields through an LPDM was addressed by *Lin and Gerbig* [2005] for horizontal  
90 wind uncertainty, and by *Gerbig et al.* [2008] for uncertainty in vertical mixing. In both cases, they  
91 found that failing to account for meteorological uncertainty produced backward simulations with  
92 insufficient dispersion. They pointed out the importance of spatial correlation in the random errors.

93 All errors were assumed to be random, that is, biases were not addressed. Numerical uncertainties,  
94 especially those due to terrain, were addressed by *Brioude et al.* [2012]. Meteorological  
95 performance of a group of regional air quality models was evaluated by *Vautard et al.* [2012].  
96 Ensemble forecasts were used to evaluate ozone predictability in Texas by *Zhang et al.* [2007].  
97 *Locatelli et al.* [2013] used several different global meteorological and transport model pairs to  
98 evaluate uncertainty in methane inversions, finding large uncertainties at regional and smaller  
99 scales. Several recent studies [*Chevallier et al.*, 2010; *Houweling et al.*, 2010; *Kretschmer et al.*,  
100 2012; *Lauvaux and Davis*, 2014] used small numbers of models or configurations of one model to  
101 evaluate uncertainties in carbon dioxide (CO<sub>2</sub>) simulations. Of these, *Kretschmer et al.* [2012] and  
102 *Lauvaux and Davis* [2014] worked at mesoscale with WRF meteorology. They explored only the  
103 differences due to parameterization of vertical mixing.

104 The Southeast Nexus (SENEX) campaign (<http://www.esrl.noaa.gov/csd/projects/senex/>) was  
105 conducted in June and July 2013. The NOAA WP3 aircraft made 19 science flights (figure 1) from  
106 its base in Smyrna, TN (near Nashville). The aircraft carried a comprehensive package of gas-  
107 phase and aerosol chemistry instruments, as well as standard meteorological instruments.

108 After presenting the model configurations (section 2), we evaluate the ensemble and its members  
109 against specifically relevant observations (section 3). Then we present the ensemble spreads  
110 (section 4) followed by discussion and conclusions.

## 111 **2. Model configurations**

112 Six WRF configurations are used, as shown in table 1. They cover three axes of the configuration  
113 space, including two different initial and boundary condition datasets, two different planetary  
114 boundary layer parameterizations, and two different treatments of the soil variables. All are run on

115 a single 12 km horizontal grid covering most of the eastern half of North America (figure 1). The  
116 vertical grid has 60 levels with 19 below 1 km AGL and the lowest level at 16 m. We note that the  
117 goal is to produce several reasonable solutions, not to establish a single “best” configuration. All  
118 configurations use WRF version 3.5, RRTMG shortwave and longwave radiation, Eta  
119 microphysics, and the Noah land surface model with single-level urban canopy. The Grell 3D  
120 cumulus scheme was used, with shallow cumulus option on for runs with the MYNN PBL scheme  
121 and off for runs with the TEMF PBL. The model was initialized at 0000 UTC each day and run for  
122 30 hours. Except for the runs with cycled soil moisture and temperature, all initial and land  
123 boundary conditions were taken from the global analysis (GFS or ERA-Interim). To make a  
124 continuous output dataset, the first six hours of each daily run were discarded as spinup. Sea  
125 surface temperature was provided by the U.S. Navy GODAE high-resolution SST, (see  
126 [http://www.usgodae.org/ftp/outgoing/fnmoc/models/ghrsst/docs/ghrsst\\_doc.txt](http://www.usgodae.org/ftp/outgoing/fnmoc/models/ghrsst/docs/ghrsst_doc.txt)) updated every six  
127 hours and interpolated between updates. No observed data was directly assimilated into WRF, nor  
128 were the WRF runs nudged toward any analysis. Most of these configuration choices were the  
129 same as used for California in [Angevine *et al.*, 2012]. References for all WRF options can be  
130 found in [Skamarock *et al.*, 2008].

131 We used a version of the FLEXPART Lagrangian particle dispersion model [Stohl *et al.*, 2005]  
132 modified to use WRF output [Brioude *et al.*, 2013a]. FLEXPART-WRF uses the same grid spacing  
133 as in WRF. FLEXPART-WRF solves turbulent motion in a Lagrangian framework using first-order  
134 Langevin equations. The turbulent motion is stochastic and parameterized using the Hanna scheme.  
135 That scheme uses PBL height, Monin-Obukhov length, convective velocity scale, roughness length  
136 and friction velocity. The PBL height and friction velocity are read from the WRF output. The PBL  
137 height in WRF with the MYNN PBL scheme is calculated based on a TKE threshold. With the

138 TEMF PBL scheme, the PBL height is the level reached by an entraining thermal from the surface  
139 [*Angevine et al.*, 2010]. FLEXPART-WRF prescribes a turbulent profile based on the Hanna  
140 scheme [*Stohl et al.*, 2005], depending on convective, neutral or stable conditions. Horizontal and  
141 vertical turbulence are both calculated from the Hanna scheme. We used the WRF output with an  
142 output time interval of 30 minutes. The number of particles emitted per unit time in each grid  
143 square is proportional to the tracer emissions at that time and place in the inventory (described  
144 below). Runs begin at 0000 UTC 4 May 2010 and run until 0000 UTC 26 June 2010. Particles are  
145 retained until they leave the domain. Each particle carries a fixed quantity of tracer. The time of  
146 emission is carried with each particle. We used time-average wind out of WRF to reduce trajectory  
147 uncertainties [*Brioude et al.*, 2012] as time-average wind is more representative of the wind  
148 variability than instantaneous wind out of WRF. *Brioude et al.* [2012] have shown that this setup  
149 conserves the well mixed criterion in the PBL in FLEXPART-WRF. Above the PBL, a simple  
150 coefficient of diffusivity is used to simulate the horizontal turbulent motion in the free troposphere.  
151 Particles are not exchanged directly by turbulence between the PBL and the free troposphere but by  
152 horizontal displacement or by the resolved vertical displacement in the WRF wind.

153 We defined the FLEXPART-WRF output grid (which is independent of the transport calculation)  
154 with a 12 km grid spacing in both horizontal dimensions and 28 vertical layers, each 100 m thick.  
155 The horizontal grid corresponds to that used for the driving WRF simulations. Particles are  
156 grouped into six age classes on output, with maximum ages of 3, 6, 12, 24, 48, and 120 hours since  
157 emission.

158 Approximately 1.8 million particles were emitted each day of the simulation. No chemical  
159 transformation or deposition was simulated. The spatial and temporal pattern of emissions is that

160 of carbon monoxide (CO) specified according the U.S. EPA 2011 National Emission Inventory,  
161 version 1, available as of November 8, 2013  
162 (<http://www.epa.gov/ttn/chief/net/2011inventory.html#inventorydoc>). Gridded (4-km resolution),  
163 hourly emissions for a July average weekday in 2011 have been derived from this inventory, and  
164 are publically available at the WRF/Chem data site:  
165 [ftp://aftp.fsl.noaa.gov/divisions/taq/emissions\\_data\\_2011/](ftp://aftp.fsl.noaa.gov/divisions/taq/emissions_data_2011/). Specific details on the files and data-sets  
166 used for spatial and temporal partitioning are supplied in the readme.txt file at the data site.  
167 Because the map projection and domain used in the WRF and FLEXPART-WRF simulations is  
168 chosen to overlap with the U.S. EPA emissions grid, hourly emissions from the 4-km NEI  
169 inventory are simply combined together within the 12km grid resolution used here. Details of the  
170 emissions are not directly relevant here, since all runs use the same emissions and results are  
171 normalized. When comparing with observed CO, it must be kept in mind that there are a number of  
172 CO sources not accounted for in these simulations. These include biomass burning, class-3  
173 commercial marine vessels, and oxidation of methane and volatile organic compounds.

### 174 **3. Meteorological evaluation**

175 Here we present some evaluation of the performance of each of the WRF configurations. Our goal  
176 is to establish that each of the runs has reasonable and comparable performance and therefore that  
177 each is a suitable ensemble member. We do not intend to comprehensively evaluate each run in  
178 this context. Evaluation of specific processes such as vertical transport by clouds is reserved for  
179 future analyses.

180 Table 2 presents a statistical comparison of each model run to data from all 19 flights of the NOAA  
181 WP3 aircraft during SENEX. All data below 1000 m ASL are used, that is, data in the daytime

182 boundary layer and the nighttime residual layer. All the runs produce statistics in the range usually  
183 considered in the literature to be “good agreement.” While small differences may be statistically  
184 significant with such a large dataset, we do not consider the differences to be of practical  
185 significance. These data, and all WP3 data presented herein, are averaged to 120 s (approximately  
186 12 km) to match the model output grid. Calculations with 10 s data (not shown) produce very  
187 similar results.

188 Soil moisture is a key control on meteorological model performance [*Chen et al., 2007; Koster et*  
189 *al., 2010; Kumar et al., 2006; LeMone et al., 2008*] because it governs the partitioning of incoming  
190 solar radiation into sensible heat flux (heating the boundary layer) and latent heat flux (moistening  
191 the boundary layer). The six WRF runs use three different strategies to initialize soil moisture and  
192 temperature. The runs with GFS initial and boundary conditions (“G” runs) use the soil moisture  
193 directly from the GFS analysis at 0000 UTC each day, interpolated to the WRF grid. Runs with  
194 ERA-Interim (“E” runs) do the same with the ERA-Interim soil moisture. Cycled runs (“ExC”)  
195 start with the soil moisture from ERA-Interim at 0000 UTC on 28 May, and then run open loop.  
196 That is, the soil moisture for each day’s run is taken from the 24-hour forecast initialized the  
197 previous day. This approach was shown by *Angevine et al. [2014]* and *Di Giuseppe et al. [2011]* to  
198 improve results under some conditions, although the differences in these runs are small.

199 The Climate Reference Network (CRN) [*Diamond et al., 2013*] provides measurements of soil  
200 moisture at multiple levels at 28 sites within our model domain. The time series of modeled and  
201 observed soil moisture is shown in figure 2. The runs using GFS soil moisture directly are clearly  
202 too moist, and a strong tendency to dry down in the course of each day is visible. Runs with ERA-  
203 Interim start and stay close to the observations. Without cycling, these runs (EM and ET) are too

204 moist after day 170, and a diurnal cycle is visible, but smaller than with GFS. Run EMC stays  
205 closest to the observations through the period. Around day 160 run ETC falls below the  
206 observations and remains there until late in the period. In figure 3, the observations of daily  
207 maximum and minimum near-surface air temperature at the CRN sites are shown along with the  
208 simulations from each WRF run. All runs have a larger diurnal cycle than the observations. Some  
209 of the differences between runs can be traced to the soil moisture and shallow cloud treatment, but  
210 the details are outside the scope of this paper.

211 Cycling soil moisture is vulnerable to errors in modeled precipitation. Figure 4 shows the observed  
212 precipitation for the whole period from the NOAA Stage IV analysis  
213 (<http://data.eol.ucar.edu/codiac/dss/id=21.093>), a blend of gauge and radar measurements. The  
214 corresponding modeled precipitation is shown in figure 5, and the totals are in table 4. All of the  
215 WRF runs miss an area of precipitation in the north-central part of the domain (roughly 38-40N,  
216 87-89W) that occurs in late June, but otherwise the spatial patterns are similar. All runs  
217 underestimate the total precipitation except GM, which comes quite close despite the previously  
218 mentioned missing area.

#### 219 **4. Ensemble spreads and their relationships**

220 The ensemble spread of wind speed is shown in figure 6. The averages are taken over all 50 days  
221 and hours 1000-1200 UTC (denoted AM) and 1800-2000 UTC (denoted PM). Throughout the text,  
222 we discuss the “2/3” spread, that is, the difference between the fourth and second ranking values of  
223 the six models at each point. This corresponds to the common idea of uncertainty as a standard  
224 deviation [*Taylor*, 1997]. The choice is discussed further in the Discussion section below. Some  
225 tables also show the “full” spread (maximum minus minimum value). If the spread is not explicitly

226 qualified as “2/3” or “full”, the 2/3 spread is intended. In the figures, spreads are normalized by the  
227 mean value at that point from the six models, so a plotted value of 1 means that the spread is equal  
228 to the mean value. The level of approximately 200 m AGL is chosen to be relevant to both daytime  
229 and nighttime transport. Mean and median spreads are approximately 20%. This includes the  
230 narrow band at the domain edges where the spread is small, but the results are only slightly reduced  
231 thereby. Some geographic features are apparent, for example the Appalachian Mountains have  
232 larger spreads than surrounding lowlands both in the morning and especially at midday. The  
233 largest spreads are found in northern Florida, probably due to differences in thunderstorms between  
234 the WRF runs.

235 Mixing height is a key parameter in Lagrangian models. The ensemble spread of mixing height  
236 (also called PBL height here) is shown in figure 7. The mixing height as used within FLEXPART-  
237 WRF is shown, which is somewhat modified from the direct WRF output. In particular, a  
238 minimum height of 100 m is imposed upon input to FLEXPART-WRF. The early morning PBL  
239 heights (1000-1200 UTC) have large spreads in the eastern part of the domain and even larger in  
240 the western part. This is largely because the TEMF PBL scheme allows very low PBL heights as  
241 designed, while the MYNN PBL scheme diagnoses higher heights. Near the western edge of the  
242 domain, the three runs with TEMF PBL differ on the location and extent of high PBLs, which are  
243 not present in the MYNN runs at all. In the afternoon (1800-2000 UTC), PBL height spreads are  
244 moderate except over water. Most land areas have spreads around 20%. The large spreads over  
245 water arise from differences in the temperature and wind speed and direction. Overwater PBLs can  
246 be stable and therefore shallow in the afternoon, but not at the exact same times and places in the  
247 different runs. Mean PBL height spreads over the whole domain are 50% in the early morning and  
248 25% at midday.

249 The effects of mixing height and wind speed can be combined into a single quantity called  
250 “ventilation”, which roughly expresses the tendency of emissions to be diluted horizontally and  
251 vertically. The ventilation is simply the product of mixing height and wind speed, in this case at  
252 200 m AGL (figure 8). The ventilation spread maps inherit primary features from the wind speed  
253 (figure 6) and PBL height (figure 7) maps. In the early morning, the ventilation spread is moderate  
254 in the east and large in the west. At midday, the Appalachian Mountains stand out as areas of  
255 moderately large spread, with quite large values over the Great Lakes, Florida, and the Atlantic and  
256 Gulf Coasts. Mean ventilation spreads for the whole domain are 60% in the early morning and  
257 35% at midday.

258 Figure 9 shows the mean ensemble spread of tracer mixing ratio in the lowest FLEXPART-WRF  
259 level (0-100 m AGL). Points with small mean values ( $<10$  ppbv) are masked out. In the afternoon  
260 (lower panel) moderate spreads (roughly 30%) are present over most of the central part of the  
261 domain. Spreads are large near the Gulf Coast, Great Lakes, and offshore. Mean spread for the  
262 whole domain is 35% (Table 5). In the morning (upper panel), the area of moderate spreads is  
263 smaller but the spatial distribution of values is similar. Mean spreads are larger, roughly 40%.  
264 Some areas with large emissions, for example Atlanta, Georgia (approximate coordinates -84, 34),  
265 have relatively small spreads. Table 5 gives the means for several threshold values of mean mixing  
266 ratio, showing that areas with larger concentrations have slightly smaller spreads. Note that the  
267 tracer values do not include any background CO, so areas unaffected by emissions within the  
268 domain have zero mixing ratio. Absolute values of mean tracer concentration and spread are  
269 shown in the Supplemental Material. These are useful for checking the reasonableness of the  
270 results, but difficult to interpret in terms of uncertainty.

271 The near-surface layer is perhaps the most difficult layer for the models, so in figure 10 we show  
272 the tracer spread in the 400-500 m AGL layer. The afternoon pattern and mean values are similar  
273 to the 0-100 m layer, which makes sense because boundary layer turbulence couples these levels  
274 strongly during the day. In the early morning, normalized spreads are larger in the upper layer than  
275 near the surface, because the upper layer is decoupled from surface emissions.

276 The WP3 aircraft flights provide another perspective on the ensemble behavior of the CO tracer.  
277 Table 6 displays correlations between the measured CO and the tracer from each member and the  
278 ensemble mean. Biases and standard deviations are not shown because computing them requires  
279 strong assumptions about the emissions and background. In figure 11, a two-dimensional  
280 histogram shows the frequency of occurrence of tracer mixing ratio spread and mean age along the  
281 flight tracks for all points with CO measurements below 1000 m AGL. The peak of the spread  
282 histogram is at about 20% and 30 hours age, and the mean spread is 30% (median 21%). Although  
283 the diagram suggests a correlation between age and spread, its value is only 0.12 (Spearman).  
284 There are a number of points with short ages and large spreads, and a wide distribution of spread at  
285 any age. Fresh plumes near sources explain the large spreads at short ages. These plumes can be  
286 rather narrow and small differences in wind direction move them to slightly different locations. At  
287 longer ages, the spread distribution narrows because the air being sampled has circulated through  
288 the domain for several days, and differences in transport and mixing in specific locations have been  
289 smoothed out. The spread may be asymptotic to a value of 50-60% at long ages.

290 We might have expected that spread and mixing ratio would correlate inversely, plumes measured  
291 near sources having little time to be transported differently, but the lower panel of figure 11 shows  
292 no such correlation. Larger mixing ratios occur near sources, but different source strengths place

293 those occurrences at different places on the X-axis. In fact, the peak of the histogram occurs at  
294 small to moderate spread (10-20%) and small mixing ratio (~15 ppb).

295 Tracer age is another important product from the FLEXPART-WRF simulations, and its  
296 uncertainty should also be evaluated. Figure 12 shows two-dimensional histograms of age spread.  
297 The peak of the histogram is at moderate ages (25-35 hours) and spreads of 15-20%. Overall mean  
298 spread is 17% and its median is 13%. Age spread is not correlated with age or mixing ratio.

## 299 **5. Discussion**

300 A key question in working with an ensemble is whether it is reliable, that is, does the probability  
301 with which an event occurs in the ensemble correspond to the probability of that event in reality?  
302 For our application, we are interested in a simpler but related criterion, whether the spread of the  
303 ensemble is a good estimate of the uncertainty of the CO mixing ratio (above background) at a  
304 particular time and place. Uncertainty is often expressed by a standard deviation. One standard  
305 deviation each side of the mean covers 66% of a Gaussian distribution. For those times, places, and  
306 variables for which we have observations, we can compare the error (simulation-obs) with the  
307 ensemble spread. These relationships are tabulated in Table 7. Of the meteorological variables,  
308 potential temperature and water vapor from the aircraft show spreads somewhat larger than the  
309 standard deviation of the errors. Wind speed has approximately equal spread and error.  
310 Temperature at 2 m from the Climate Reference Network sites has errors twice the spread. The CO  
311 tracer error is sensitive to the choice of mean for normalization, since the observed mean (minus its  
312 minimum) is twice as large as the simulated mean. This is due largely to the neglect of non-  
313 anthropogenic sources in the simulations. The spread-error relationship is therefore not useful in  
314 this situation.

315 Rank histograms [Hamill, 2001] are a method to visualize the relationship between spread and  
316 error. Each measurement is ranked among the values from the ensemble members and the ranks  
317 are counted. The expectation is that an observation should fall with equal probability into each bin  
318 of a ranked ensemble if the ensemble is reliable. Therefore the histogram should be approximately  
319 flat, although caveats apply. In figure 13, the rank histograms for meteorological variables  
320 measured by the P3 are shown. The potential temperature histogram is fairly flat, indicating  
321 reasonable reliability. An excess of points in the leftmost bin indicates a small bias consistent with  
322 the values in table 2. A more significant bias to the right is found for water vapor. The wind speed  
323 spread may be somewhat too small as indicated by the U shape of the histogram. Figure 14 shows  
324 the rank histogram for 2m T at the CRN sites, for which the ensemble clearly has too little spread.

325 For our six-member ensemble, the standard deviation can be approximated as the range of the four  
326 inner members (leaving out the minimum and maximum). This quantity is tabulated as “2/3”  
327 spread in table 7, and shown in the preceding figures. It agrees better with the error (also defined  
328 as a standard deviation) than the full spread for potential temperature and water vapor. This is the  
329 reason we have used the 2/3 spread above and in our conclusions below. The 2/3 spread is clearly  
330 too small for 2m T at the CRN sites, for reasons we have not explored.

331 The ensemble spreads presented above represent, by our postulate, the uncertainty at a single point  
332 of a 12-km grid in a single realization. For the maps in figures 9 and 10, the spreads were  
333 computed with 3-hour averaging. The comparisons with WP3 data (table 6) include no temporal  
334 averaging. The uncertainty can be reduced by further averaging in space or time. The effect of  
335 averaging depends on the degree of independence of the samples. Figure 15 shows the behavior of  
336 the ensemble spread (uncertainty) with respect to spatial and temporal averaging. Results are

337 shown for individual hours (1100 UTC and 1900 UTC) and for 3-h averages, each spatially  
338 averaged over 1, 3, 5, 7, 9, and 19 grid points in each direction (1, 9, 25, 49, 81, and 361 points  
339 total). Averaging is done to each mixing ratio field before the spread is calculated. Points are also  
340 shown on the right axis for averaging over the entire spatial domain. Removing the three-hour  
341 averaging increases the spread by about 5%. Averaging over 3 points in each direction reduces the  
342 spread by about 5%. Further reductions come with increased averaging, but the gain is rather slow.  
343 Even averaging over 9 points in each direction only reduces the spread by 5-10%. The reduction is  
344 much slower than would be expected if we naively assumed that all points in the average or all  
345 points in each direction were independent, in which case averaging would reduce uncertainty by the  
346 inverse square root of the number of samples (green and red lines respectively). The spreads for 1-  
347 h and 3-h averaging converge as spatial averaging increases. The pattern of improvement with  
348 averaging is similar at the surface and in the 400-500 m layer. Averaging over the entire domain, a  
349 rather extreme procedure, reduces the spread to roughly 5%. This remnant spread is due to the fact  
350 that the tracer can leave the finite domain at different rates with different wind patterns.

351 The results we have presented (figures 6-10) show that patterns of ensemble spread of CO tracer  
352 are not simply related to patterns of wind speed, PBL height, or ventilation (their product). This  
353 result may appear surprising at first glance. However, we are dealing with a large area with  
354 moderately complex terrain, distributed sources, and complex meteorology. The LPDM simulates  
355 all of the complex patterns, including medium-range transport between regions and partial  
356 recirculation or stagnation of the tracer. There is some tendency toward larger spread of all  
357 variables in mountainous areas, at night, and over coastal waters (see for example [Ngan *et al.*,  
358 2012]).

359 Previous work of *Gerbig et al.* [2008] and *Lin and Gerbig* [2005] addressed uncertainty in  
360 meteorology driving an LPDM by adding a correlated random error, effectively increasing the  
361 diffusion terms in the transport equations. Our work shows that the uncertainty is highly variable  
362 in space and time, and it is not clear how one would account for this in an approach like theirs.  
363 Most likely, uncertainties from meteorological model runs cannot be fully addressed by correlated  
364 random errors, and an ensemble approach should be used instead.

## 365 **6. Conclusions**

366 We have presented ensemble spreads of tracer mixing ratio from the FLEXPART-WRF Lagrangian  
367 particle dispersion model driven by meteorological fields from six different configurations of WRF.  
368 The FLEXPART-WRF model and WRF model source codes are publicly available online.  
369 Interested parties can contact us to access the (large) amount of WRF and FLEXPART-WRF  
370 output used in this study.

371 The spreads of a passive tracer emitted according to all inventoried CO sources are 30-40% , for  
372 transport time of 5 days or less, whether they are taken over the whole domain at the surface or in  
373 the daytime boundary layer (table 5), or sampled by the aircraft (table 7). Excluding points with  
374 small tracer mixing ratios keeps the spreads near the smaller end of those ranges (table 7). Spatial  
375 or temporal averaging reduces the spreads, but rather slowly (figure 15).

376 We postulated that the tracer spread is a measure of uncertainty in the LPDM simulation due to  
377 meteorological uncertainty. This is verified by comparing spreads to errors in meteorological  
378 variables. Among meteorological variables compared with measurements on the aircraft, the  
379 ensemble is roughly reliable for potential temperature and water vapor, but has too little spread for

380 wind speed. For near-surface temperature at the CRN sites, the ensemble has significantly too little  
381 spread.

382 No member of a valid ensemble should be obviously bad or obviously superior. The direct  
383 comparisons with observations in tables 2 and 3 verify this. The best and worst performing  
384 members for one variable or platform are not the same as for others. It is also interesting to note  
385 that the ensemble mean is not obviously better than the best member for any particular variable.

386 We examined wind speed, boundary layer height, and ventilation looking for relationships between  
387 the spreads of these parameters and the tracer spread. No obvious relationships were found.  
388 Spreads of meteorological variables are largest where we would expect, in complex terrain, at  
389 night, and over coastal waters. Simple relationships among the uncertainties of meteorological  
390 parameters and the tracer uncertainty are missing because of terrain, partial recirculation, medium-  
391 range (order 100 km) transport, and long tracer lifetime. These are the reasons why an LPDM is  
392 needed in this and similar real mesoscale situations. We do not think that tracer spreads can be  
393 predicted from known error characteristics of the meteorological variables. We recommend that an  
394 ensemble approach like this one, or even more sophisticated, be used to assess the uncertainty of  
395 Lagrangian simulations.

396 Uncertainty in single LPDM simulations of passive tracers at mesoscale due solely to uncertainty in  
397 the meteorological forcing is 30-40% of the tracer mixing ratio. The uncertainty is somewhat less,  
398 perhaps as little as 20%, under particularly favorable conditions (strong, broad plumes sampled in  
399 daytime at moderate distance/time downwind of their sources). It is greater, as much as 60%,  
400 under less favorable conditions (weak or narrow plumes, undifferentiated background, or sampling

401 at night). Spatial averaging can reduce the uncertainty with loss of resolution. Uncertainty of  
402 simulated tracer age is 15-20%.

403

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483 **Tables**

484 Table 1: Names and primary definitions of the six WRF configurations to be discussed.

Name	Initialization	PBL scheme	Soil treatment	Cumulus
GM	GFS	MYNN2	Direct	Grell 3D with shallow
EM	ERA	MYNN2	Direct	Grell 3D with shallow
EMC	ERA	MYNN2	Cycled	Grell 3D with shallow
GT	GFS	TEMF	Direct	Grell 3D NO shallow
ET	ERA	TEMF	Direct	Grell 3D NO shallow
ETC	ERA	TEMF	Cycled	Grell 3D NO shallow

485

486 Table 2: Comparison statistics for all WP3 aircraft flights below 1000 m ASL. Model points are  
 487 extracted along the flight track every 10 s, linearly interpolated in space and time, and then  
 488 averaged to 120 s. Std.Dev. is the standard deviation of the differences, and r is the Spearman rank  
 489 correlation coefficient. Units are  $\text{m s}^{-1}$  for wind speed, K for potential temperature, and g/kg for  
 490 water vapor mixing ratio. Sign of bias is (model – measurement). Number of points is 2026.

WP3	GM	EM	EMC	GT	ET	ETC	Ensemble mean
Wind speed Mean bias	0.26	-0.14	-0.16	0.48	0.15	0.14	0.12
Std.Dev.	1.7	1.7	1.7	1.8	1.8	1.8	1.5
r	0.64	0.72	0.72	0.66	0.67	0.68	0.72
Potential temperature Mean bias	-0.30	0.07	0.16	-0.16	0.30	0.58	0.11
Std.Dev.	0.94	1.1	1.1	1.1	1.2	1.2	0.96
r	0.93	0.90	0.90	0.92	0.90	0.90	0.92
Water vapor mixing ratio Mean bias	-0.20	-0.73	-0.88	-0.76	-1.3	-1.6	-0.91
Std.Dev.	1.6	1.5	1.5	1.5	1.5	1.5	1.3
r	0.74	0.79	0.79	0.76	0.78	0.78	0.82

491

492 Table 3: Comparison statistics of near-surface (2 m) temperature for 28 Climate Reference  
 493 Network sites. Model results are from the nearest grid point to each site. Sign of biases is model-  
 494 measurement.

	GM	EM	EMC	GT	ET	ETC	Ensemble mean
Daily maximum bias	1.4	2.2	2.4	1.8	2.8	3.6	2.4
Daily maximum std. dev.	2.2	1.9	2.0	2.3	2.4	2.9	2.1
Daily maximum r	0.35	0.43	0.42	0.43	0.40	0.34	0.44
Daily maximum 2/3 spread							1.5
Daily minimum bias	-1.6	-0.86	-1.4	-2.0	-1.3	-2.1	-1.5
Daily minimum std. dev.	2.9	2.8	3.0	2.7	2.6	3.0	2.8
Daily	0.46	0.48	0.44	0.47	0.49	0.45	0.47

minimum r							
Daily minimum 2/3 spread							1.0
Daily mean bias	- 0.13	-0.54	-0.41	-0.13	0.48	0.47	0.27
Daily mean std. dev.	1.7	1.8	1.9	1.7	1.8	1.9	1.7
Daily mean r	0.54	0.46	0.44	0.52	0.43	0.39	0.48
Daily mean 2/3 spread							1.4

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498 Table 4: Precipitation totals in the portion of the domain shown in figures 3 and 4.

Stage IV	GM	EM	EMC	GT	ET	ETC
observed						
237	245	189	185	199	154	147

499  
500

501 Table 5: Mean normalized CO tracer spreads at two levels of the whole domain with varying  
 502 mixing ratio thresholds. Number of points is also shown. Grid size is 216\*236 so maximum  
 503 possible N = 50976.

Threshold (mean mixing ratio >)	10 ppb	20 ppb	30 ppb	40 ppb	50 ppb
0-100 m AGL AM 2/3	0.39	0.36	0.34	0.32	0.32
AM full	0.70	0.65	0.61	0.58	0.57
N	38354	29169	19822	13299	8568
PM 2/3	0.35	0.32	0.30	0.29	0.29
PM full	0.62	0.57	0.54	0.52	0.51
N	35856	22698	14238	7739	3487
400-500 m AGL AM 2/3	0.43	0.40	0.38	0.38	N too small
AM full	0.78	0.71	0.69	0.68	N too small
N	34248	18127	10383	1963	20
PM 2/3	0.35	0.32	0.30	0.30	0.29
PM full	0.61	0.56	0.53	0.52	0.51
N	34525	19240	10993	4045	1069

504  
505

506 Table 6: Comparison statistics of CO and CO tracer for all WP3 aircraft flights below 1000 m  
 507 ASL. Model points are extracted along the flight track every 10 s, linearly interpolated in space  
 508 and time, and then further averaged to 120 s.  $r$  is the Spearman rank correlation coefficient.  
 509 Number of samples is 1597.

510

	GM	EM	EMC	GT	ET	ETC	Ensemble mean
CO tracer mixing ratio $r$	0.62	0.61	0.61	0.59	0.59	0.59	0.62

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512

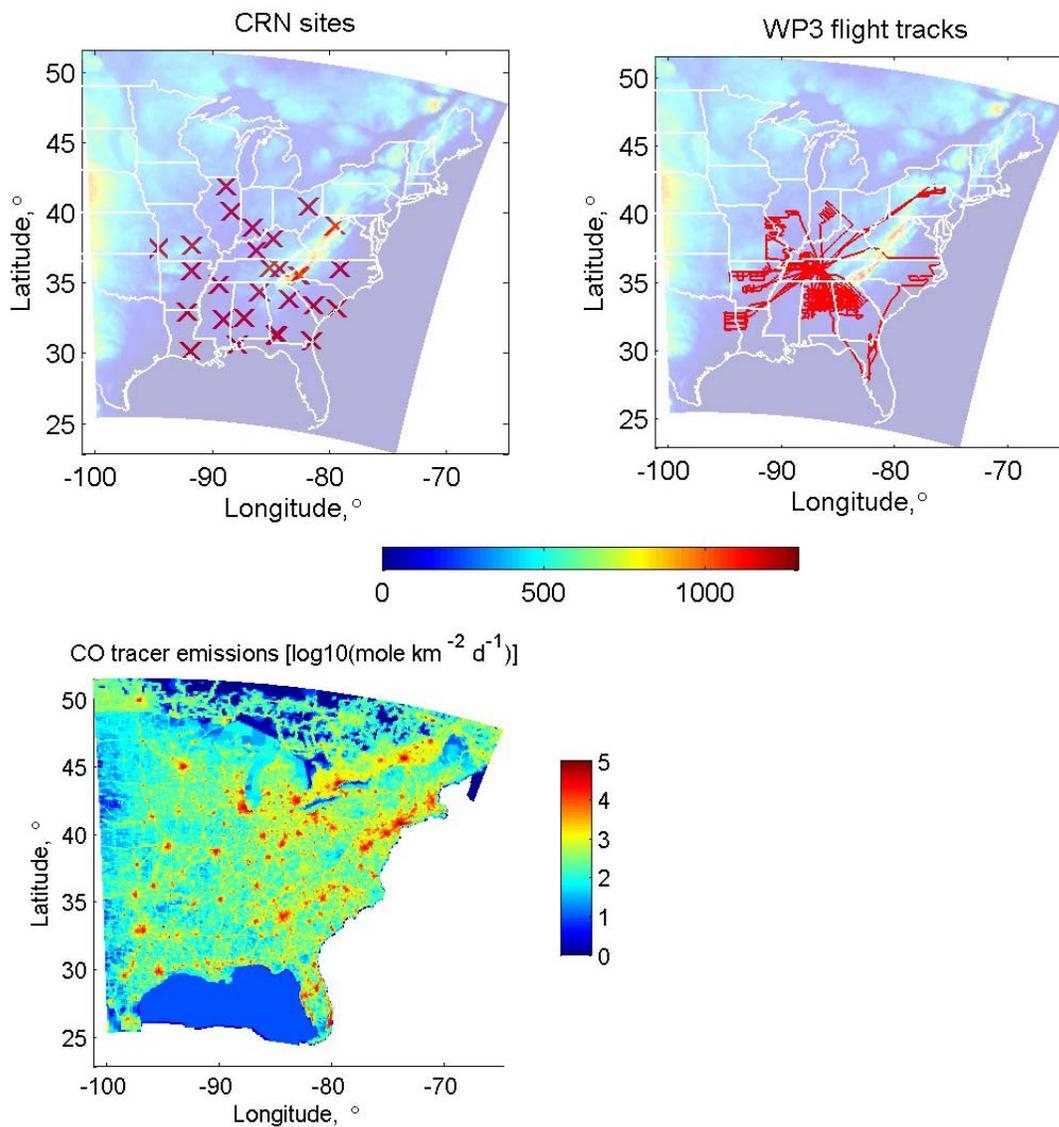
513 Table 7: Spread and standard deviation statistics for all WP3 aircraft flights below 1000 m ASL  
514 and for CRN 2m temperature. Model points are extracted along the flight track every 10 s, linearly  
515 interpolated in space and time, and then averaged over 120 s. CRN 2m temperature statistics are  
516 for all available hourly observations (N=33569). N=2026 for P3 meteorology, N=1597 for P3 CO.  
517 CO spreads and simulated CO standard deviation are normalized by the simulated ensemble mean.  
518 Observed CO standard deviation is normalized by the observed mean with minimum value  
519 subtracted to account for background. For simulated-observed standard deviation of CO, two  
520 values are shown, the smaller is normalized by the observed mean with minimum subtracted (71  
521 ppb) and the larger is normalized by the simulated mean (32 ppb).

522

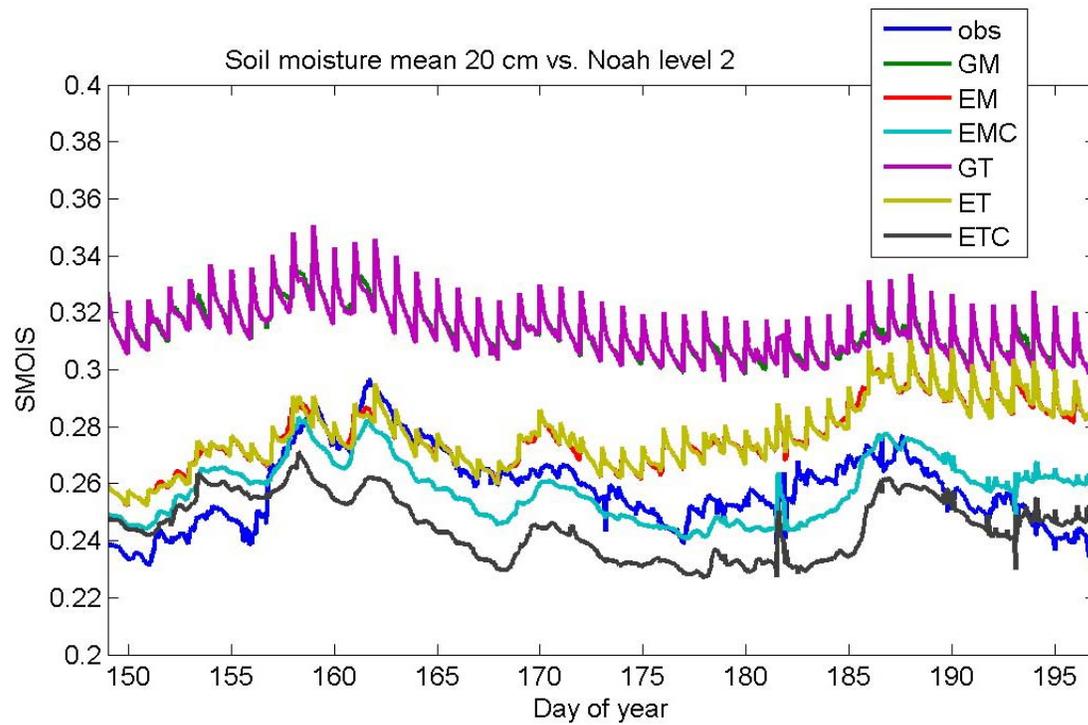
	Standard deviation of difference (simulated-observed)	Ensemble spread (full)	Ensemble spread (2/3)	Standard deviation observed	Standard deviation simulated ensemble mean
Potential temperature (P3) (K)	0.96	1.5	0.89	9.1	9.1
Water vapor mixing ratio (P3) (g/kg)	1.3	2.0	1.3	2.3	2.1
Wind speed (P3) (m/s)	1.5	1.9	1.3	2.2	2.3

2m T (CRN) (K)	4.7	2.4	1.5	4.5	4.9
CO tracer mixing ratio (normalized)	0.39 (0.87)	0.54	0.31	0.46	0.58

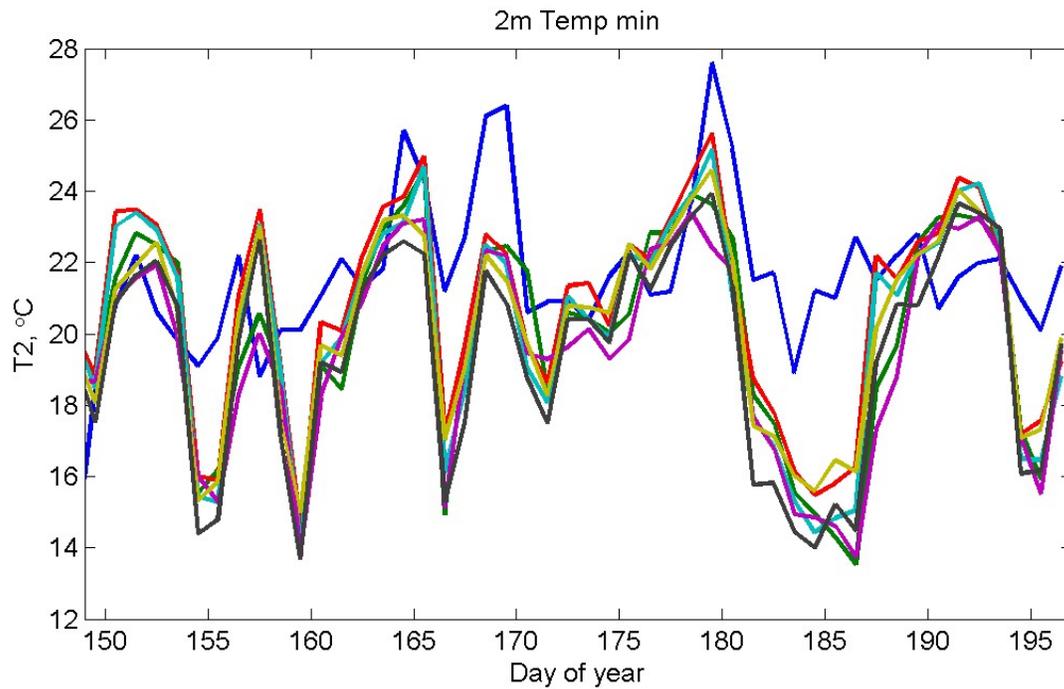
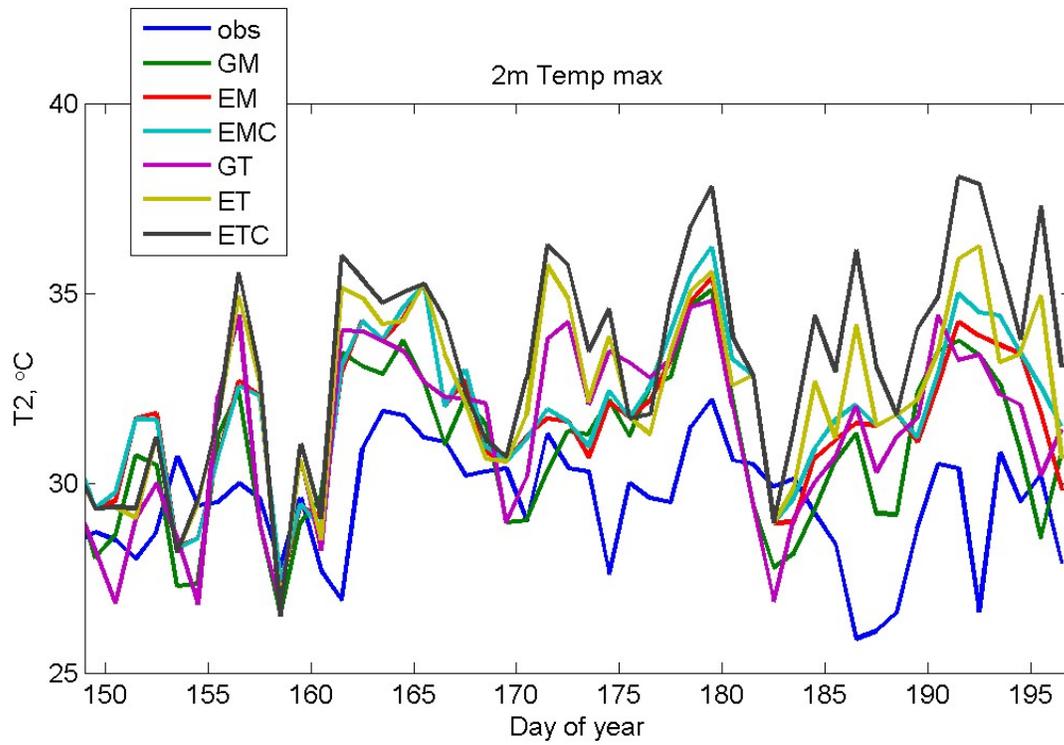
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524 Figure 1: Maps of the WRF domain with terrain height (m ASL) colored as background and  
 525 showing Climate Reference Network sites (upper left) and flight tracks of the NOAA WP3 (upper  
 526 right). Lower panel shows CO tracer emissions used in the FLEXPART-WRF runs.

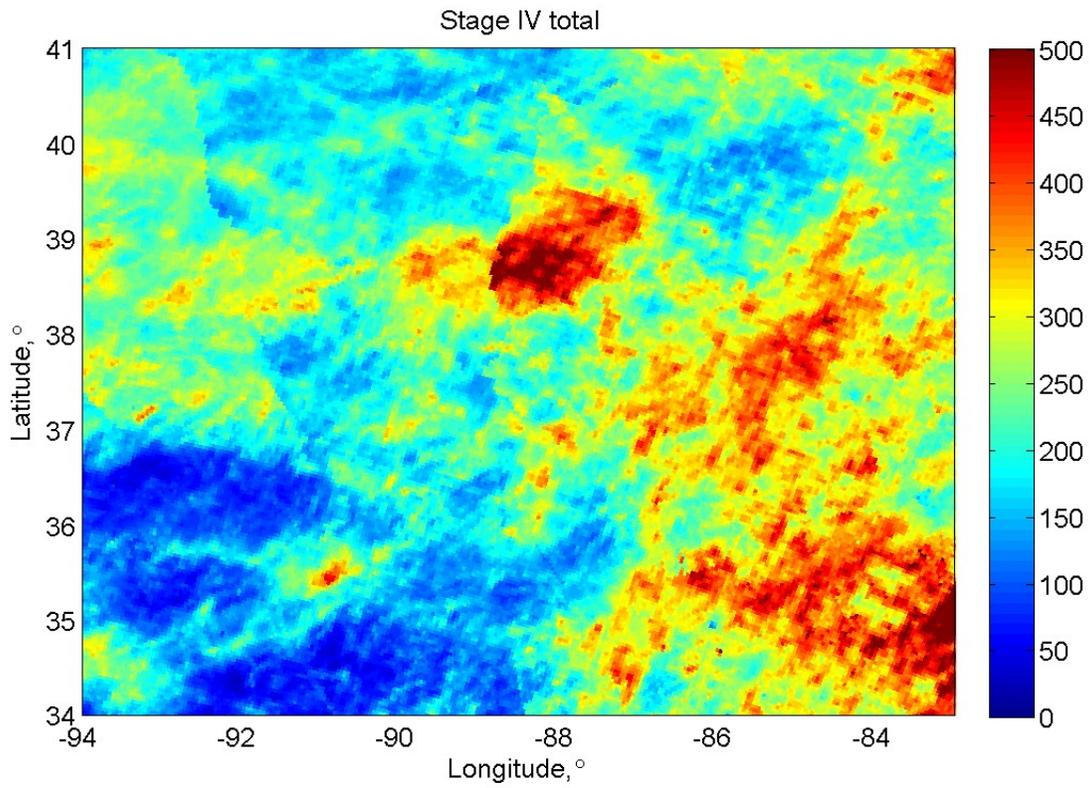


528  
 529 Figure 2: Soil moisture mean of 28 Climate Reference Network stations. Measurement at 20 cm  
 530 depth is compared to second model level (10-40 cm). Legend refers to table 1. Run GM is often  
 531 obscured by GT.  
 532



533 Figure 3: Daily maximum and minimum near-surface temperature averaged over 28 Climate  
 534 Reference Network sites.

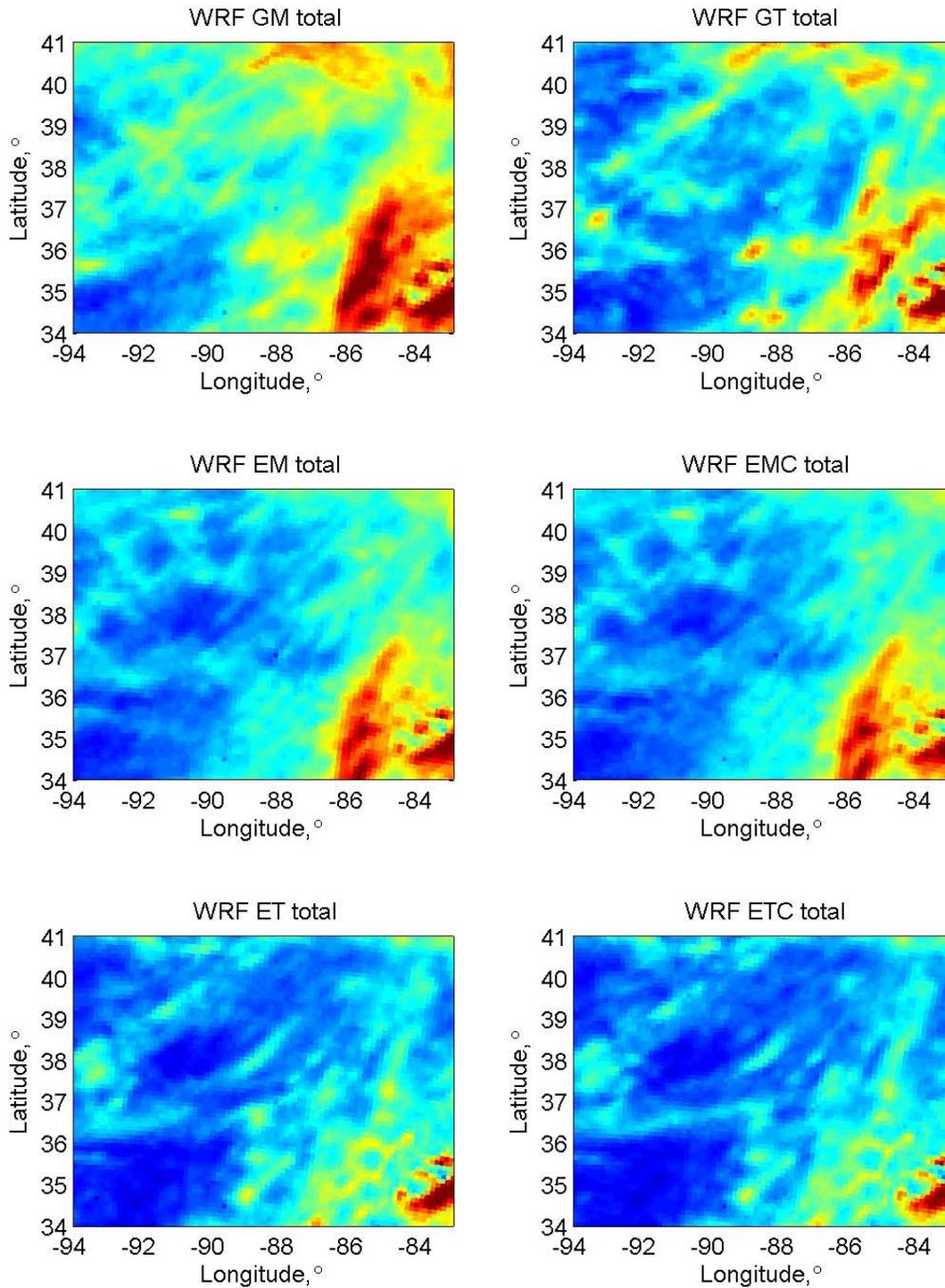
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536 Figure 4: Observed precipitation from the NOAA Stage IV product for 28 May – 15 July 2013

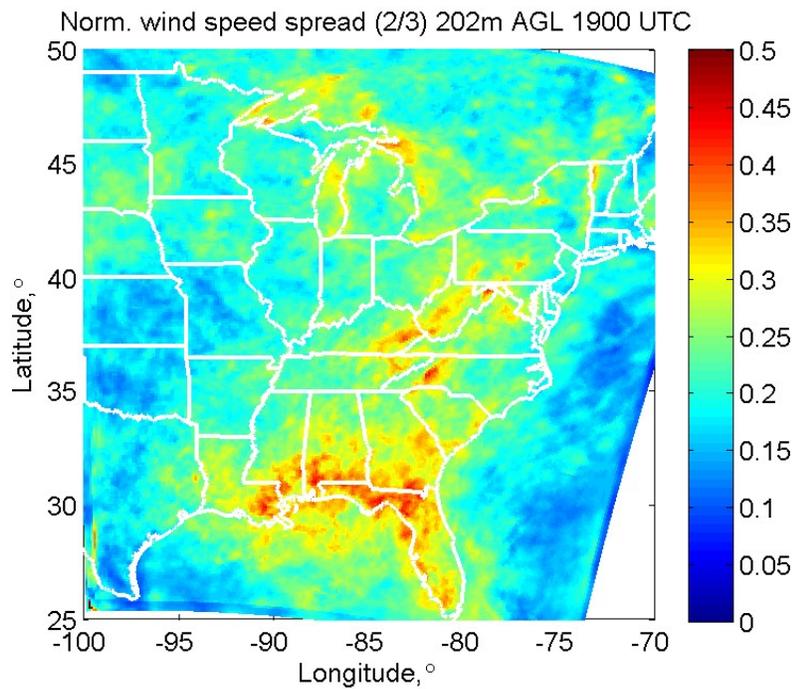
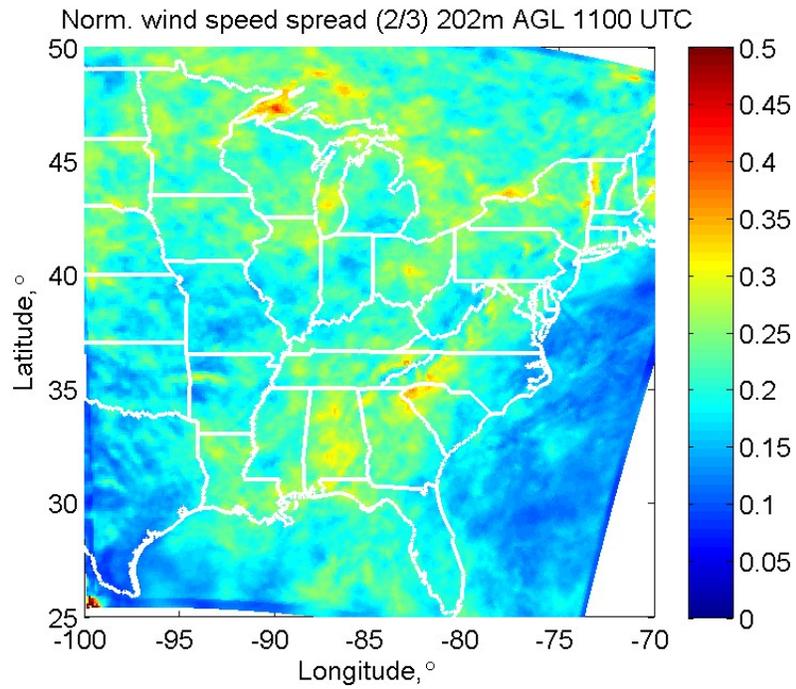
537 (mm). Edges of the domain are excluded for clarity.

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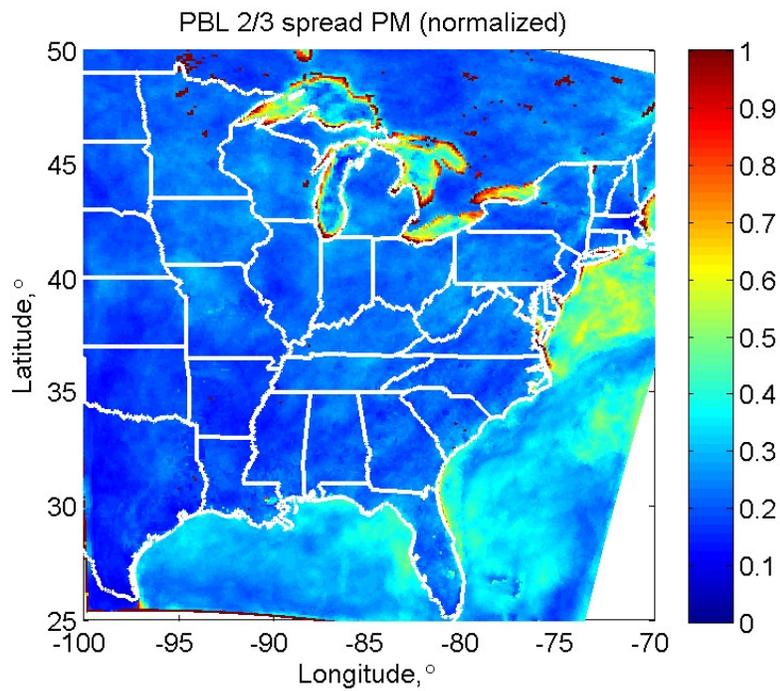
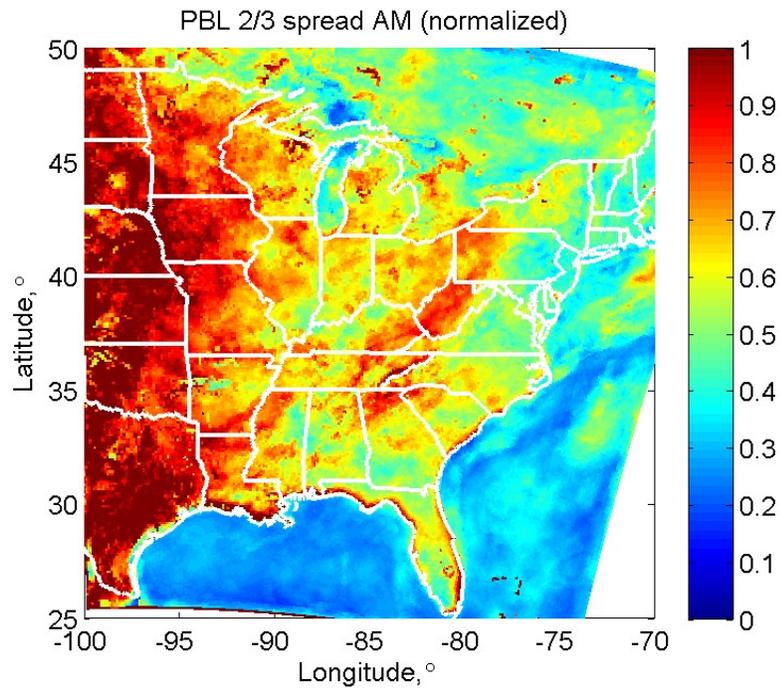


539 Figure 5: Total precipitation from each WRF run for 28 May – 15 July 2013. Color scale same as  
 540 figure 3.

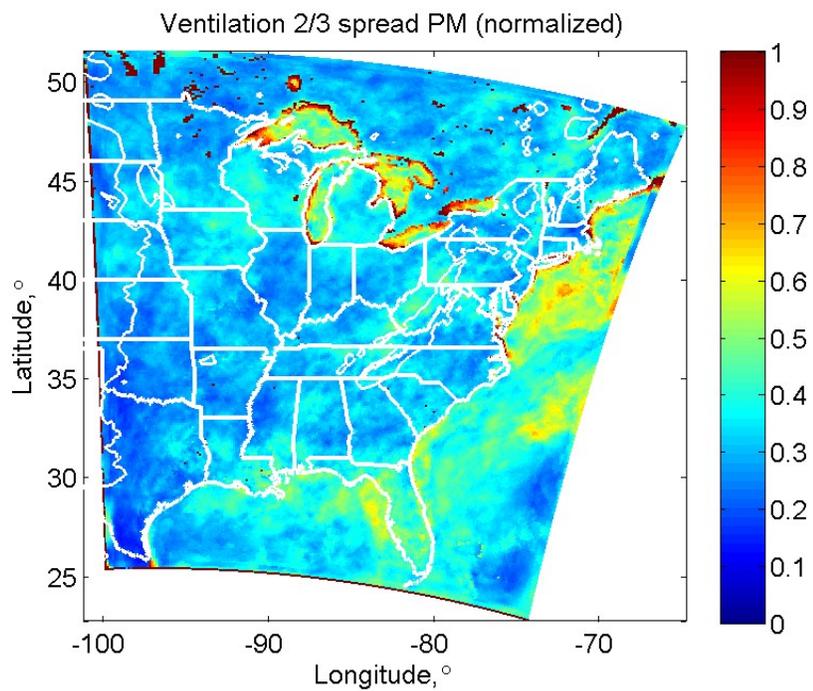
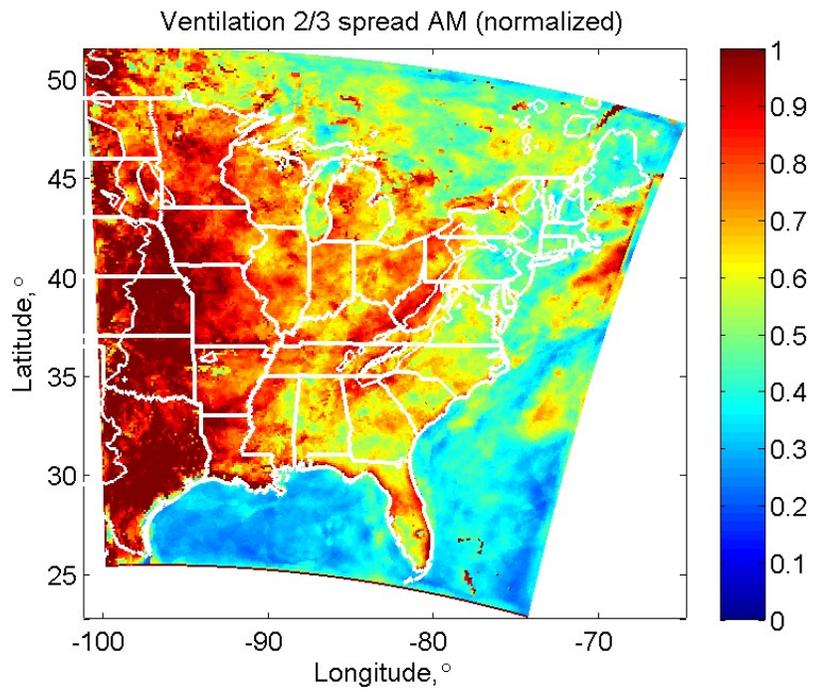
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542 Figure 6: Wind speed spread in early morning and midday from the WRF ensemble. Spread is  
 543 normalized by mean speed (therefore unitless) and averaged over all 49 days.

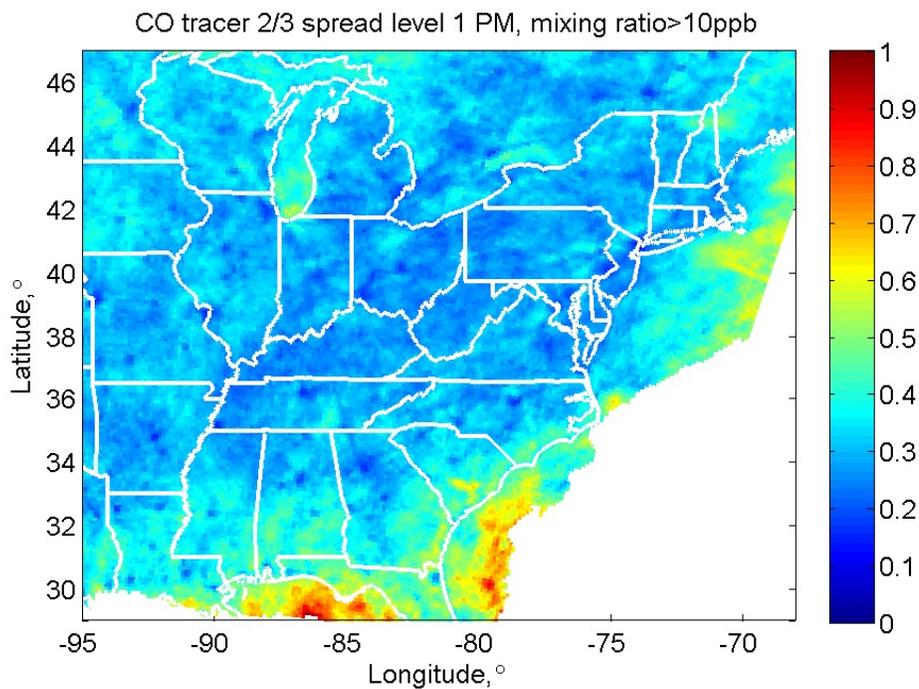
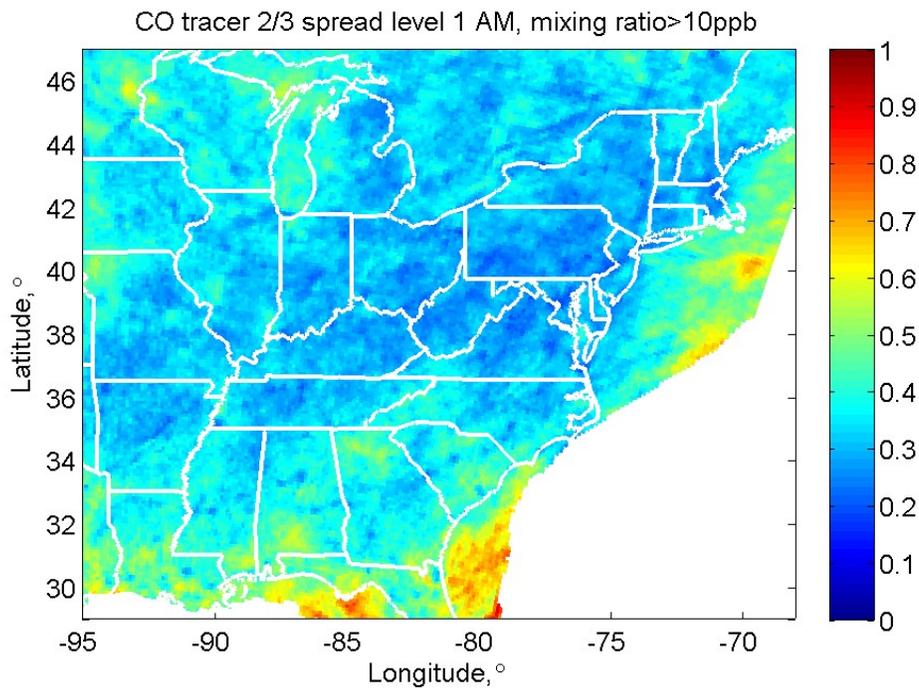


544 Figure 7: Spread of boundary layer height (mixing height) in the early morning and midday as  
 545 interpreted by FLEXPART-WRF from the WRF ensemble input. Spread is normalized by the  
 546 mean value.

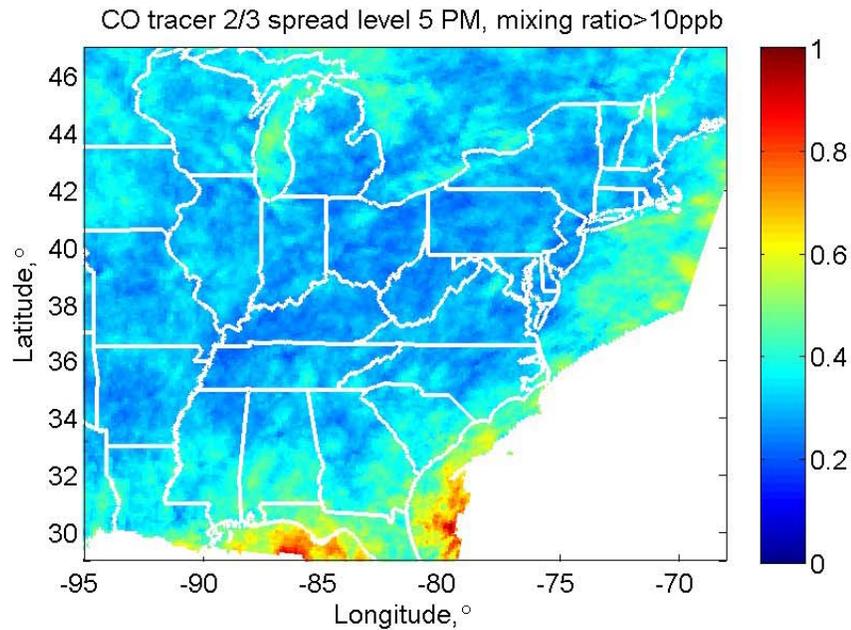
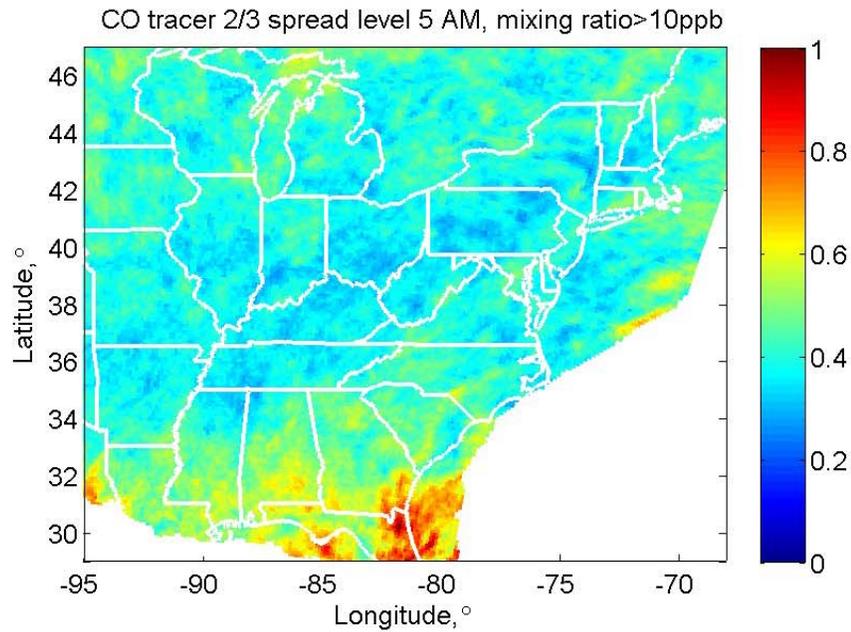


547 Figure 8: Spread of ventilation (PBL height \* wind speed) in the early morning and midday.

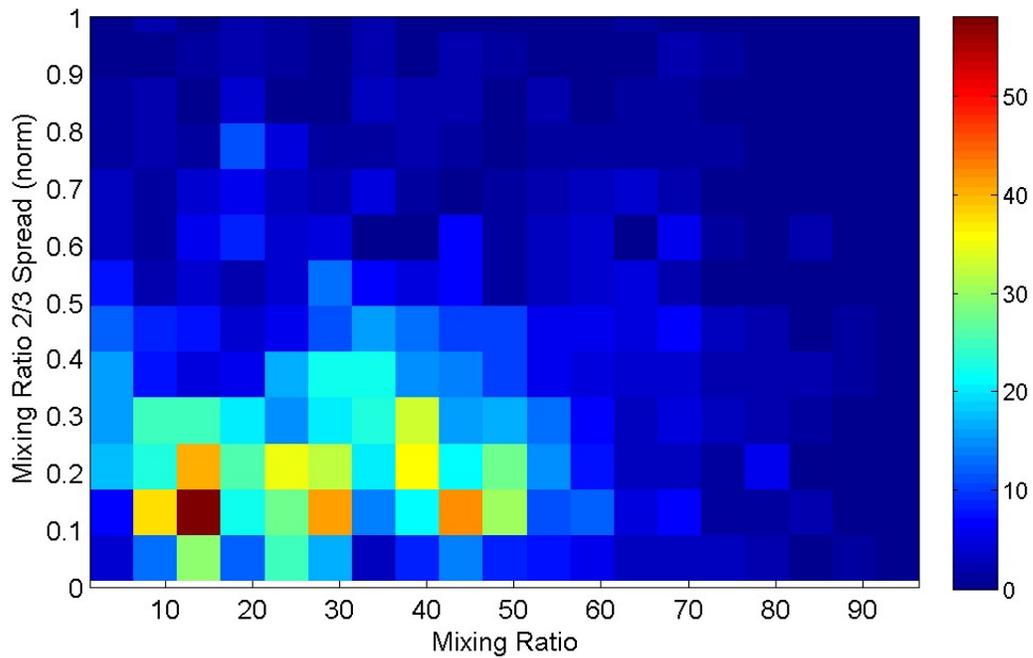
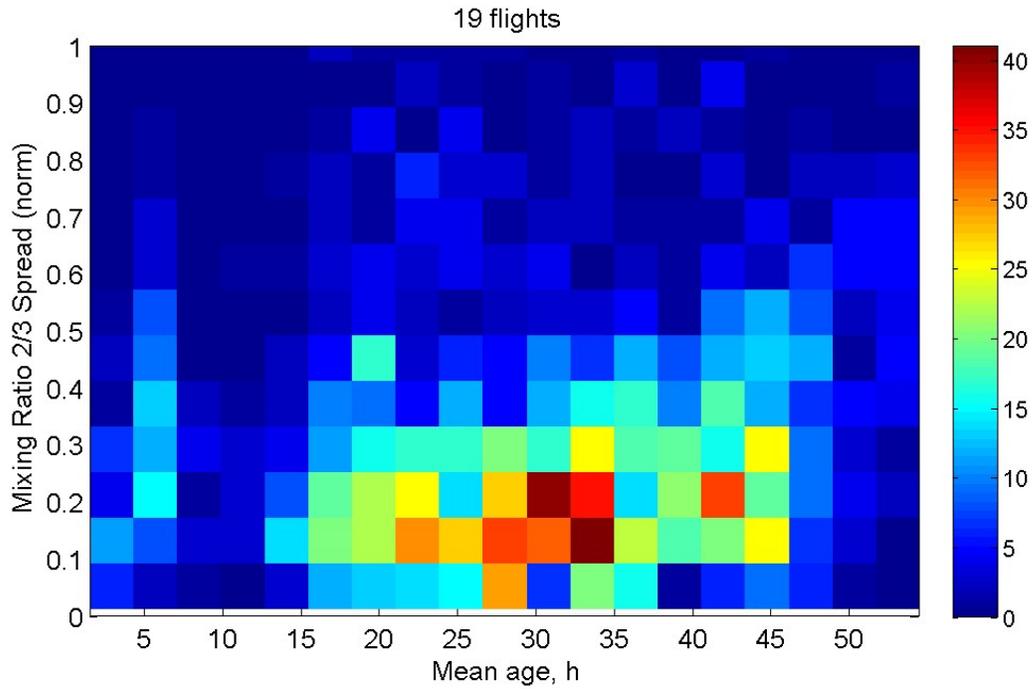
548 Spread is normalized by the mean value.



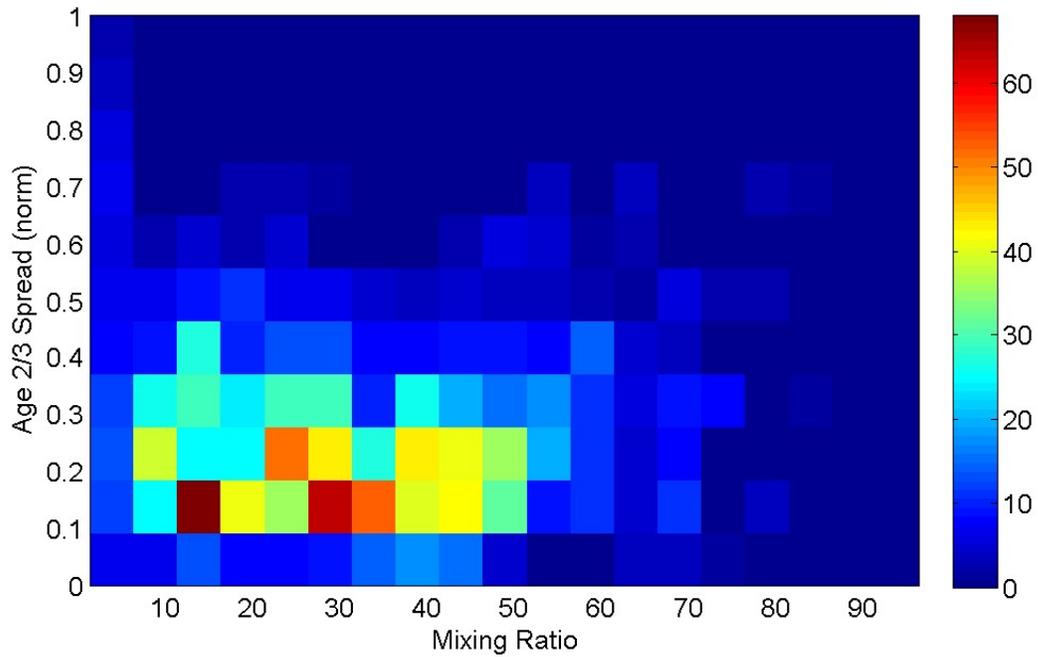
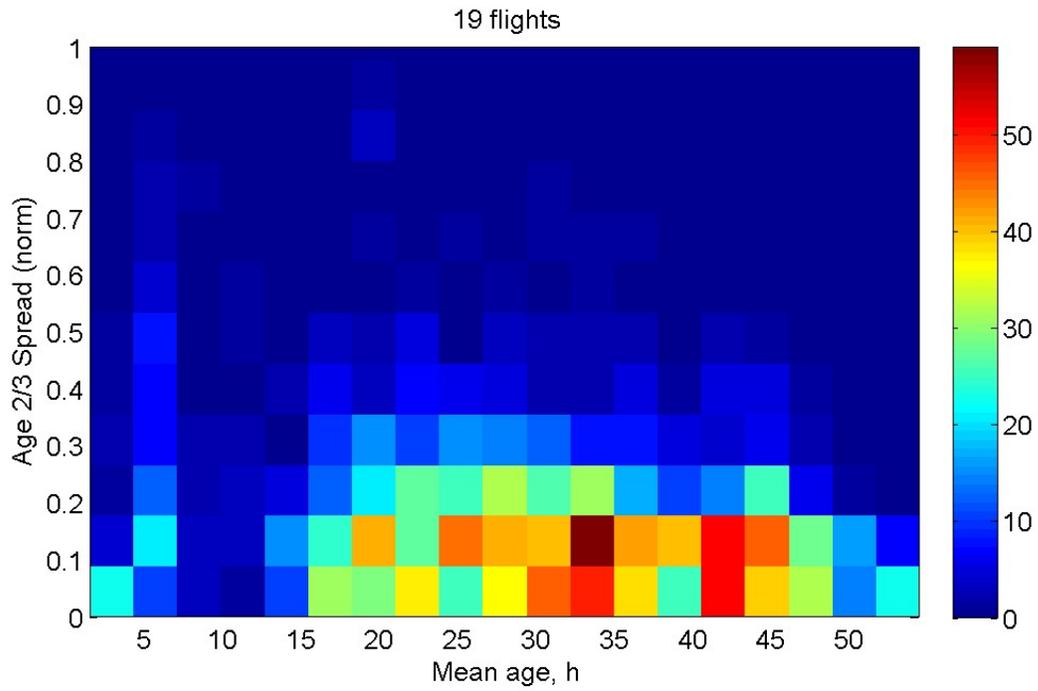
549 Figure 9: Mean ensemble spread of tracer mixing ratio at level 1 (0-100 m AGL). The averages  
 550 are taken over all 49 days and hours 0400-0600 LST (AM, top) and 1300-1500 LST (PM, bottom).  
 551 The spread is normalized by the mean mixing ratio at each point. Points with small mean values  
 552 (<10 ppbv) are masked out.



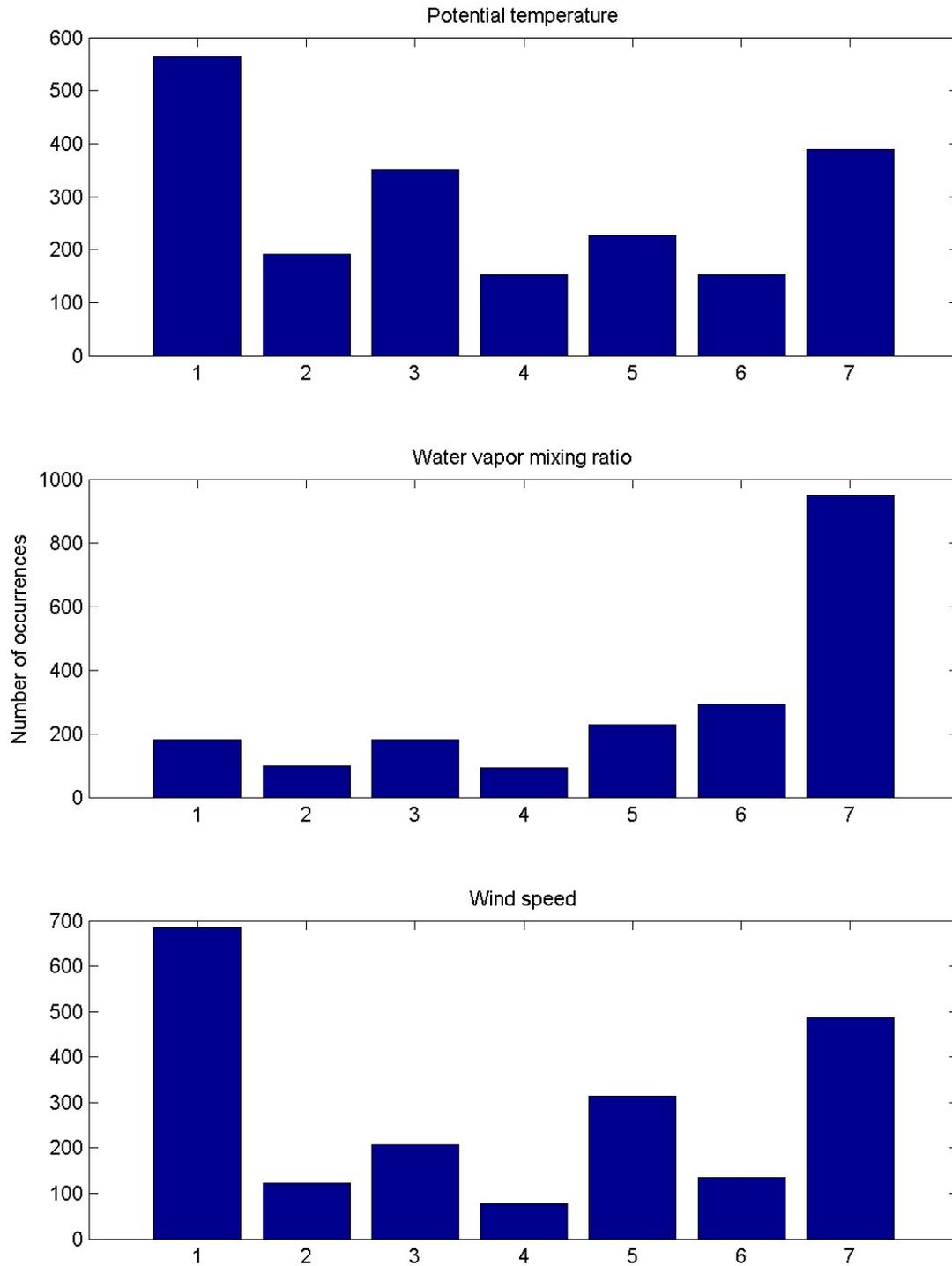
553 Figure 10: Mean ensemble spread of tracer mixing ratio at level 5 (400-500 m AGL). The  
 554 averages are taken over all 49 days and hours 0400-0600 LST (AM, top) and 1300-1500 LST (PM,  
 555 bottom). The spread is normalized by the mean mixing ratio at each point. Points with small mean  
 556 values (<10 ppbv) are masked out.



557 Figure 11: Frequency of occurrence of CO tracer spread along the P3 flight tracks vs. simulated  
 558 mean tracer age (top) and simulated mixing ratio (bottom) for all points with valid CO  
 559 measurements below 1000 m AGL.

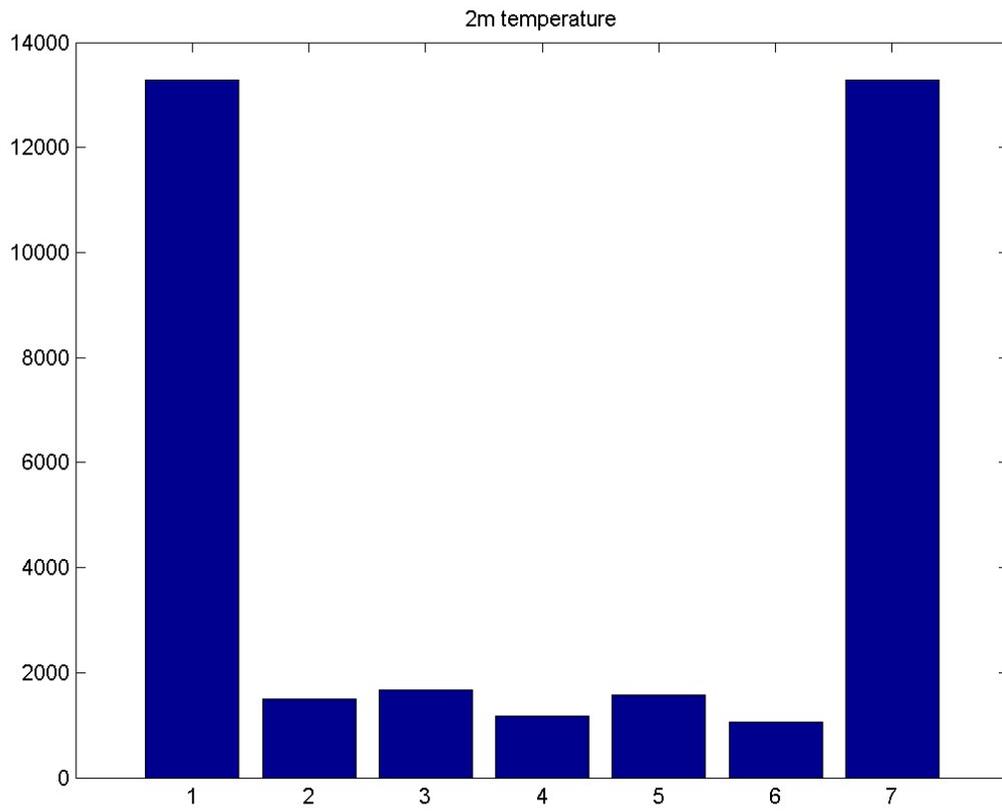


560 Figure 12: Frequency of occurrence of CO tracer age spread along the P3 flight tracks vs.  
 561 simulated mean tracer age (top) and simulated mixing ratio (bottom) for all points with valid CO  
 562 measurements below 1000 m AGL.



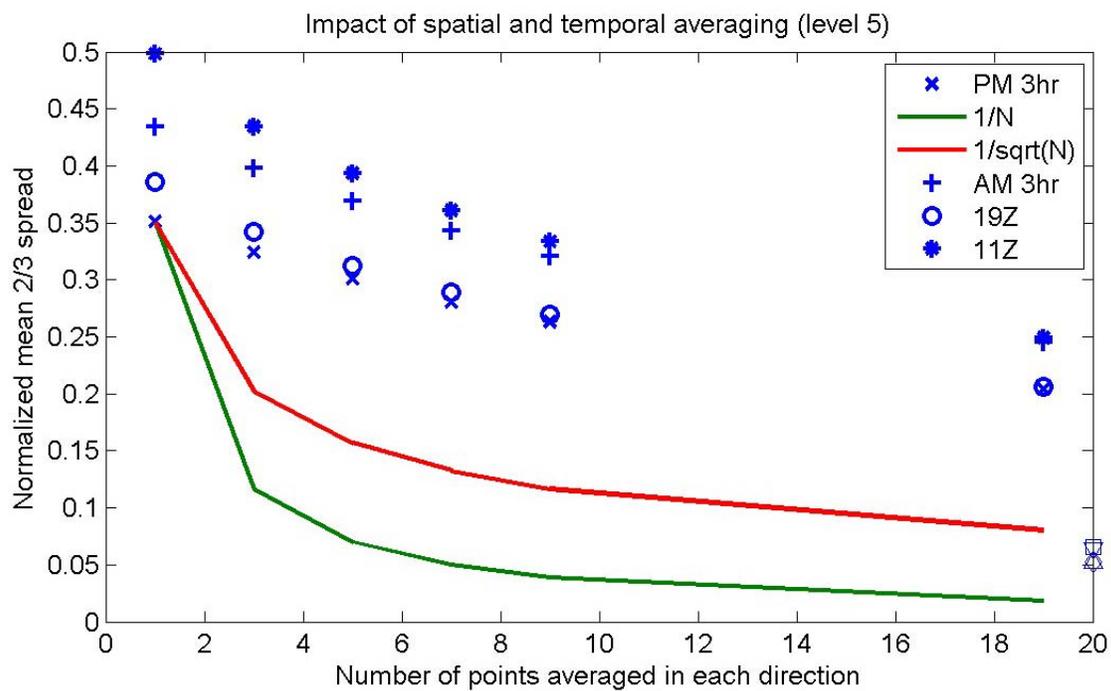
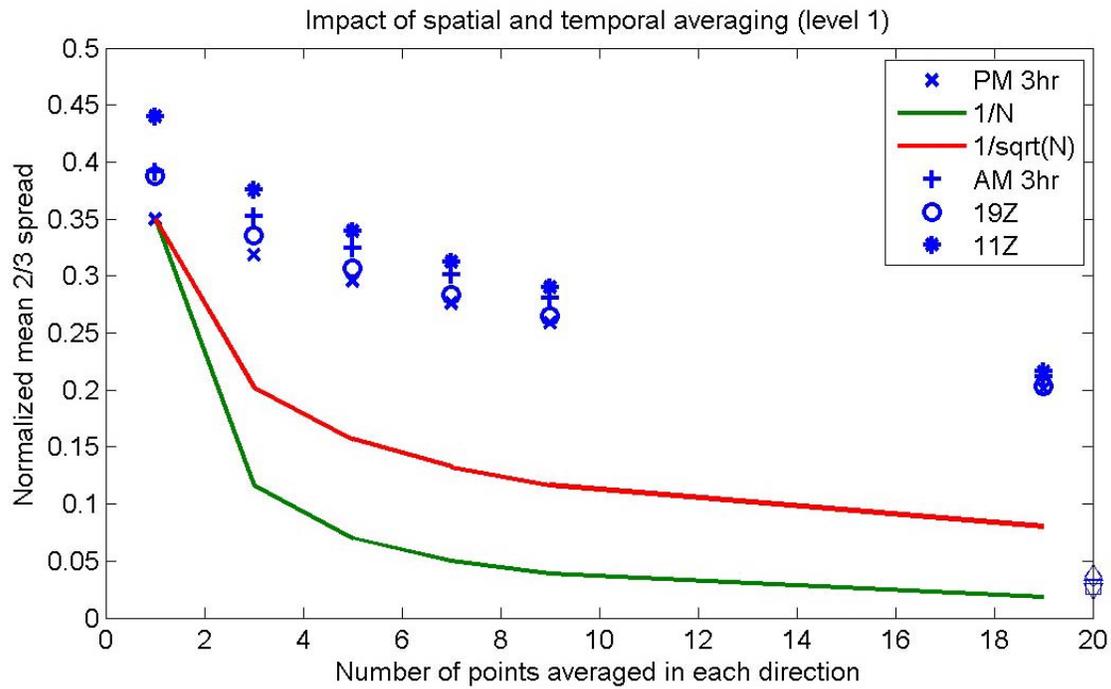
563 Figure 13: Rank histograms for all P3 flight data below 1000 m AGL for potential temperature,  
 564 water vapor mixing ratio, and wind speed (as labeled).

565



566 Figure 14: Rank histogram for all hourly near-surface temperature observations at 28 Climate  
567 Reference Network sites.

568



569 Figure 15: CO tracer spread as a function of averaging for surface (top) and 400-500 m AGL  
 570 (bottom). The points (+ and x) for AM and PM 3h averaging without spatial averaging are the  
 571 means shown in the figures and in the second column of table 5. Points on the right axis are for  
 572 averages over the entire domain (216x236 points).