1 Model-data fusion across ecosystems: from multi-site optimizations to

2 global simulations

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17 Abstract

This study uses a variational data assimilation framework to simultaneously constrain a global 18 19 ecosystem model with eddy covariance measurements of daily net ecosystem exchange (NEE) and 20 latent heat (LE) fluxes from a large number of sites grouped in seven plant functional types (PFTs). 21 It is an attempt to bridge the gap between the numerous site-specific parameter optimization works 22 found in the literature and the generic parameterization used by most land surface models within 23 each PFT. The present multi-site approach allows deriving PFT-generic sets of optimised 24 parameters enhancing the agreement between measured and simulated fluxes at most of the sites 25 considered, with performances often comparable to those of the corresponding site-specific 26 optimizations. Besides reducing the PFT-averaged model-data root-mean-square difference (RMSD) and the associated daily output uncertainty, the optimization improves the simulated CO₂ 27 28 balance at tropical and temperate forests sites. The major site-level NEE adjustments at the seasonal scale are: reduced amplitude in C3 grasslands and boreal forests, increased seasonality in temperate 29 30 evergreen forests, and better model-data phasing in temperate deciduous broadleaf forests. 31 Conversely, the poorer performances in tropical evergreen broadleaf forests points to deficiencies 32 regarding the modeling of phenology and soil water stress for this PFT. An evaluation with 33 data-oriented estimates of photosynthesis (GPP) and ecosystem respiration (Reco) rates indicates 34 distinctively improved simulations of both gross fluxes. The multi-site parameter sets are then

tested against CO₂ concentrations measured at 53 locations around the globe, showing significant adjustments of the modelled seasonality of atmospheric CO₂ concentration, whose relevance seems PFT-dependent, along with an improved interannual variability. Lastly, a global scale evaluation with remote sensing NDVI measurements indicates an improvement of the simulated seasonal variations of the foliar cover for all considered PFTs.

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1. Introduction

8 Land surface models (LSMs) have been tools of growing importance in the continuous effort to develop comprehensive Earth system models which help to understand the effects of 9 10 changes in land surface processes and land-use practices upon biogeochemical (carbon, water, 11 nutrients) and energy cycles, and more generally upon the Earth's climate (Cramer et al., 2001; 12 Friedlingstein et al., 2006; Sitch et al., 2008). With the goal of improving accuracy and realism, the 13 increasing amount and range of scale of the processes included in mechanistic LSMs result in a 14 growing number of parameters associated with the corresponding model equations (Pitman, 2003). 15 Some parameters are easily identified with a given physical process (and can sometimes be 16 measured); others are purely empirical and account for a variety of processes embodied in a few 17 equations, yet to be refined. In both cases, obvious computational and complexity limits have 18 traditionally led model developers to use broad classes of soil and vegetation types, for which 19 typical, generic parameter values are assigned (e.g., (Sellers et al., 1996)).

20 One difficulty is in scaling up the leaf- and plant-level measurements of physical parameters for 21 ecosystem-scale simulations (Jarvis, 1995; Bonan et al., 2012). Besides, the variety of species 22 within each of the 10 to 20 plant functional types (PFTs) typically used by most models makes the 23 choice of a representative parameter value critical, thus adding significant uncertainty to the model 24 outputs. In this context, parameter optimization methods have been increasingly used to calibrate 25 model parameters and reduce the associated uncertainty. The criterion is to minimize the misfit 26 between simulation outputs and observed data (Raupach et al., 2005). As for ecosystem models, 27 eddy covariance measurements provide direct, near-continuous, in situ observations of carbon 28 dioxide, water and energy exchanges between the canopy and the atmosphere (Baldocchi et al., 29 2001; Baldocchi, 2008). This measurement method has been applied across an extensive global 30 network (560 sites as of October 2013), spanning a wide range of ecosystems and climates 31 (http://fluxnet.ornl.gov/).

Over the last decade, numerous studies with various LSMs have used this available information to derive sets of parameters that significantly improve the model-data fit, with optimization approaches ranging from simple parameter adjustments to rigorous data assimilation frameworks (e.g., (Wang et al., 2001, 2007; Reichstein et al., 2003; Braswell et al., 2005; Knorr and Kattge,

2005; Santaren et al., 2007; Thum et al., 2008; Williams et al., 2009; Carvalhais et al., 2010; 1 Keenan et al., 2012)). However, most of these efforts have focused on model calibration at 2 individual sites. It often results in model parameters overly tuned to the specifics of a particular site 3 given the small spatial footprint of each flux tower (typically a few hectares). Only recently, some 4 5 studies started to assess through optimization the generic nature of model parameters within PFTs. The benefit of a set of parameters derived at one site was evaluated for simulations at a similar site 6 7 (Medvigy et al., 2009; Verbeeck et al., 2011) and over the surrounding region (Medvigy and Moorcroft, 2012), with encouraging results. In parallel, two independent efforts simultaneously 8 9 used data constraints from several sites to assess the degree of improvement of the simulated fluxes depending on the "generic criterion" used for the optimised parameters (Groenendijk et al., 2011; 10 11 Kuppel et al., 2012). The study of (Groenendijk et al., 2011), conducted at over a hundred locations 12 across several PFTs, found that the cross-site parameter variability after optimization explained the 13 poorer performances of grouping sites by PFT, while no such discrepancy appeared in (Kuppel et 14 al., 2012), a study however limited to temperate deciduous broadleaf forests.

15 Building on the optimization procedure developed by (Kuppel et al., 2012), the present work assesses the potential of the multi-site assimilation of carbon net ecosystem exchange (NEE) and 16 17 latent heat (LE) flux measurements in a process-based terrestrial ecosystem model (ORCHIDEE). The objective is to improve site-scale simulations of carbon and water fluxes at a large number of 18 19 flux towers sites, as well as global scale simulations of vegetation phenology and terrestrial carbon 20 balance. Specifically, we address the following questions: 1) for each of the seven PFTs considered 21 (out of 12 in ORCHIDEE, 5 being not covered by the measurements used here), can we find a 22 generic set of optimised parameters that enhance the model-data fit at all sites? 2) how well does the 23 multi-site approach compare to site-specific optimizations? 3) what are the main improvements 24 introduced by the optimization procedure from seasonal to annual time scales: daily error, model-data bias, seasonal cycle amplitude and/or phase? 4) which processes remain poorly captured 25 26 by the model after optimization? 5) have the eddy-covariance-constrained sets of multi-site 27 parameters a notable impact on global scale simulations?

28 Section 2 presents the ecosystem model, the data assimilation system, and the eddy covariance 29 measurements used in this study, as well the supplementary datasets and models. The results are 30 presented and discussed in Sect. 3, successively dealing with the model-data fit at the site level 31 (3.1), the comparison between multi- and single-site results (3.2), the uncertainties of modelled 32 NEE and LE (3.3). Then are evaluated the impact of the derived multi-site parameterization upon 33 the site-scale simulation of photosynthesis and ecosystem respiration rates (3.4), and at the global scale upon the simulated seasonality and interannual variability of atmospheric CO₂ concentration 34 35 (3.5.1) and finally upon the seasonality of vegetation activity (3.5.2).

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2. Materials & Methods

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2.1 Vegetation model and optimised parameters

5 The biogeochemical vegetation model used in this study is ORCHIDEE (Organizing Carbon 6 and Hydrology in Dynamic Ecosystems, (Krinner et al., 2005)). It calculates the water, energy and 7 carbon fluxes between the land surface and the atmosphere at a half-hourly time step. The exchange of carbon and water during photosynthesis and the energy balance are treated every 30 minutes, 8 9 while carbon allocation, autotrophic respiration, foliar onset and senescence, mortality and soil 10 organic matter decomposition are computed on a daily time step. The soil hydrology follows a 11 double-bucket scheme (Ducoudré et al., 1993) and its impact on stomatal conductance is described 12 in (Krinner et al., 2005). The reader is referred to previous publications for the standard equations 13 of ORCHIDEE (e.g., (Kuppel et al., 2012)). As in most biogeochemical models, the vegetation is 14 grouped into several PFTs, 12 in the case of ORCHIDEE, excluding bare soil. Except for the 15 modelled phenology (Botta et al., 2000), the equations governing the different processes are generic across PFTs, but with specific parameter values for each vegetation class. When used in "grid-point 16 mode" at a given site, we force the model with the corresponding half-hourly gap-filled 17 18 meteorological data measured at the flux towers. At the global scale, the global ERA-Interim 19 meteorology (Dee et al., 2011) is used as forcing and the model outputs are calculated at a 0.72 x 20 0.72 deg² resolution. In this case the global PFT map is computed at the spatial resolution of the forcing fields, from an original vegetation map available at 5km, which is derived from a 21 22 high-resolution IGBP AVHRR global land dataset (Eidenshink and Faundeen, 1994) and uses 94 23 ecosystem classes (Olson, 1994). Importantly, the modelled carbon pools are initially brought to 24 equilibrium before both site- and global-scale simulations by cycling the available meteorological 25 forcing over several centuries (spin up procedure), with the prior parameterization of the model. 26 This procedure ensures a net carbon flux close to zero over annual-to-decadal timescales.

27 Table 1 presents the PFT-generic parameters used in this study. As our emphasis is on adjusting the 28 carbon cycle, there are significantly more optimised parameters leveraging on photosynthesis and 29 respiration processes than, for instance, on the energy balance. We also included two additional 30 parameters to optimise the initial state of the model provided by the spin up procedure, which are 1) 31 a common multiplier of the initial carbon pool content, by default equal to one, and 2) the initial 32 leaf area index (LAI) of non-deciduous PFTs, by default taken from the spin up outputs. Both 33 parameters are considered as site-specific, since the soil organic carbon content is closely related to 34 the local land-use history, while the foliar cover of evergreen and herbaceous species directly relates 35 to vegetation history at the site level. One consequence is that they cannot be spatially extrapolated,

thus the global simulations performed for evaluation (see sect. 2.4) use the default value of these
last two parameters, i.e., using the initial carbon pool content and foliar cover provided by the spin
up procedure.

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5 2.2 Data assimilation system

6 The model parameters are optimised using the variational data assimilation method described in 7 (Kuppel et al., 2012). Assuming a Gaussian distribution for errors on the parameters, the model 8 outputs and the measured data, the optimised set of parameters corresponds to the minimization of 9 the following Bayesian cost function J(x) (Tarantola, 2005):

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$$J(x) = \frac{1}{2} \left[(y - H(x))^T R^{-1} (y - H(x)) + (x - x_b)^T P_{b^{-1}} (x - x_b) \right], \qquad (1)$$

11 12

which quantifies both the misfit between modelled and observed fluxes, and the misfit between a priori and optimised parameters. x is the vector of unknown parameters, x_b the vector of background (i.e., here, prior) parameter values, H(x) the model output, y the vector of observed fluxes, while P_b and **R** are the prior covariance matrices of parameter errors and observation errors, respectively.

17 The cost function is iteratively minimized with the gradient-based algorithm L-BFGS-B, which 18 allows prescribing boundaries for each variable to optimise (Byrd et al., 1995). At each iteration, the 19 gradient of the cost function $J(\mathbf{x})$ is computed with respect to all parameters, mostly using the 20 Tangent Linear (TL) model of ORCHIDEE generated with the automatic differentiator tool TAF (Transformation of Algorithms in Fortran, see (Giering et al., 2005)). Exceptions concern two 21 phenological parameters, $K_{\text{pheno,crit}}$ and c_{Tsenes} (see Table 1), where the threshold functions prevent the 22 23 use of a linear approximation. In these cases we use a finite-difference approach with prescribed 24 perturbation steps respectively equal to 4% and 2% of the allowed variation range. The recent work 25 of (Santaren et al., 2013) with the same ecosystem model highlighted the risk of converging 26 towards a local minimum within a site-specific variational optimization. In our case, preliminary 27 tests within three PFTs (tropical and temperate evergreen broadleaf forests, and temperate deciduous broadleaf forests) allowed us to verify that the convergence of our multi-site approach 28 29 barely depends on the choice of the first-guess values assigned to the optimised parameters. 30 However, such robustness is not guaranteed with the site-specific approach, and potential convergence issues are discussed in the results section. 31

32 Once the cost function reaches the minimum, the posterior parameter error variance/covariance 33 matrix P_a is explicitly calculated from the prior error covariance matrices (P_b and R) and the 1 Jacobian of the model H at the minimum of the cost function (H_{∞}), using the linearity assumption

- 2 (Tarantola, 2005):
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$$P_{a} = \left[H_{\omega^{T}}R^{-1}H_{\omega} + P_{b^{-1}}\right]^{-1}$$
(2)

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6 The prior parameter error covariance matrix \mathbf{P}_{b} is diagonal as prior uncertainties are supposed to be 7 uncorrelated between parameters. The prior standard deviation for each parameter is equal to 1/6 of 8 the range between lower and higher boundaries. The latter have been carefully specified following 9 the physical and empirical expertise of the ORCHIDEE modelers, based on literature reviews or 10 databases (such as TRY, (Kattge et al., 2011)).

In the prior observation error covariance matrix **R**, we include both the random error on the 11 12 measurements and the model error, the latter stemming from missing/inadequate process 13 representation in the structural equations of the ecosystem model. Although the measurements error 14 is known not to be constant (e.g. (Richardson et al., 2008)), a previous study using the ORCHIDEE 15 model suggested that the model component dominates the observation error budget (Kuppel et al., 16 2013). The variances in **R** are chosen constant at a given site for each type of data (NEE and LE), 17 equal to the mean square difference between the prior model and the observations. We also choose for simplicity to keep **R** diagonal, based on the rapid decline of the model error autocorrelation 18 19 beyond the first lag day (Kuppel et al., 2013).

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21 2.3 Assimilated eddy covariance flux data

We use the eddy covariance data provided by 78 flux towers of the FLUXNET global network 22 23 (Baldocchi, 2008), representative of seven of the 12 vegetated PFTs defined in the ORCHIDEE 24 model (supplementary Table S2). All the sites of a given dominant ecosystem are located in the 25 same geographical hemisphere, which makes seasonal analyses easier. These observations derive 26 from standard flux data processing methodologies (correction, gap-filling and partitioning) of the 27 La Thuile dataset (Papale, 2006). From the large amount of available site-years in this dataset, our 28 selection was driven by several requirements, the first of these being a minimum vegetation cover of 70% by the dominant PFT within each tower footprint, based on site-level information. Then 29 30 were discarded the sites where measurements show a significant disagreement with the prior 31 simulation outputs, as it suggests strong model structural deficiencies that make the parameter 32 optimization pointless. Lastly, we selected at each site the longest data segment of consecutive years 33 without gaps larger than a few weeks. Where measurements of the ground heat flux (G) were 34 available, the monthly energy balance was closed with a correction factor then

half-hourly-interpolated and applied to the latent heat (LE) and sensible heat (usually called H) 1 2 fluxes, according to the Bowen ratio technique (Twine et al., 2000). The half-hourly, gap-filled measured fluxes of net ecosystem exchange (NEE) and LE are then used to compute daily means. 3 We chose to assimilate daily-averaged observations and not half hourly measurements so as to focus 4 5 the optimization on time scales ranging from seasonal to annual variations, and to take advantage of the rapidly-decreasing autocorrelation of gap-filled half-hourly fluxes (Lasslop et al., 2008). In 6 7 order not to give too much weight to data estimated from gap-filling as compared to measured data, each daily observation error is inflated by a factor 1+0.5k, where k is the daily fraction of 8 9 half-hourly data estimated from gap-filling. We also checked that the gaps still remaining after the gap-filling were distributed evenly over the course of the day. The individual days with more than 10 11 20% of these "ultimate" gaps were not included in the assimilation.

The eddy covariance data are compared to the simulated fluxes in terms of RMSD and bias. In addition, for the six non-tropical PFTs we use a curve fitting procedure (composed of a polynome of degree 2 and four harmonics) to decompose the fluxes into their trends and mean seasonal cycles following (Thoning et al., 1989). The detrended smooth seasonal cycle is used to estimate the ratio between the average annual amplitude of the simulated and observed fluxes, as well as a model phase coefficient defined as

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$$C_{phase} = 1 - \frac{|e_{sim} - e_{obs}| + |b_{sim} - b_{obs}|}{e_{obs} - b_{obs}}$$
(3)

19 20

Here, b_i and e_i are respectively defined as the days when the detrended smooth curve crosses the zero line. In tropical evergreen broadleaf forests, the phase and amplitude diagnostics presented above are not applied, due to the lack of a marked seasonal cycle. Instead, the predictive power of the simulations is evaluated using the Nash-Sutcliffe model efficiency coefficient (Nash and Sutcliffe, 1970):

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$$NSE = 1 - \frac{\sum \left(F_{sim}^{t} - F_{obs}^{t}\right)^{2}}{\sum \left(F_{obs}^{t} - \overline{F_{obs}}\right)^{2}},$$
(4)

27 28

29 where F_i^t is the value of the simulated or observed flux at the time step *t*, and $\overline{F_{obs}}$ the mean 30 observed flux.

- 31
- 32 2.4 Evaluation tools

1 The model is evaluated at the sites using the two components of NEE: the gross primary 2 productivity (GPP) and the ecosystem respiration rate (R_{eco}), both estimated via the flux-partitioning 3 method described in (Reichstein et al., 2005). This method extrapolates nighttime measurement of NEE, representing nighttime Reco, into daytime Reco using a short-term-calibrated temperature 4 5 response function. GPP is then derived as the difference between R_{eco} and NEE. We acknowledge that GPP and R_{eco} are not fully independent data (with respect to the assimilated NEE) and are 6 essentially model-derived estimates somewhat conditional on our underlying assumptions, and it 7 will be kept in mind during the analysis. 8

9 Additionally, measurements of the Normalized Difference Vegetation Index (NDVI) made by the 10 MODIS instrument are used to evaluate the simulated phenology at the global scale. From 2000 to 11 2010, the calculated reflectances (from measured irradiances) have been corrected for atmospheric absorption and scattering (Vermote et al., 2002) and directional effects (Vermote et al., 2009) in 12 13 order to obtain a daily NDVI product with a 5-km spatial resolution. Observations contaminated 14 with snow cover were removed from the analysis using MODIS' quality filter, and we discarded 15 NDVI observations below 0.2 in order to minimize the impact of bare soil reflectance. Spatial averaging is used to match the ERA-Interim resolution (0.72° x 0.72°) used for the global scale 16 17 simulations. Because it is directly derived from surface reflectances, we preferred NDVI to other satellite products such as FAPAR or LAI, the latter requiring intermediate processing steps usually 18 19 involving radiative transfer models, and thus possibly adding uncertainty to the retrieved data 20 (Garrigues et al., 2008). Following (Maignan et al., 2011), we then calculate the Pearson correlation 21 factor between the times series of measured NDVI and the Fraction of Absorbed Photosynthetically Active Radiation (FAPAR) modelled by ORCHIDEE, at the weekly time scale during the period 22 23 2000-2010. FAPAR has been estimated from modelled LAI with a simple Beer's law:

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 $FAPAR = 1 - \exp(-0.5 \times LAI)$ (5)

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The link between simulations and measurements is made by spatially averaging the latter to reach the resolution of the vegetation model (i.e. that of the ERA-Interim forcing). For each of the seven PFTs considered, we restrict our correlation computation to the model boxes where the dominant PFT's cover fraction exceeds 50% and where both NDVI and FAPAR time-series exhibit a visible seasonal cycle (i.e. with a standard deviation larger than 0.04).

Lastly, the simulated global NEE fluxes are output at the daily timescale and spatially averaged from the ERA-Interim grid $(0.72^{\circ}x0.72^{\circ})$ to a $2.5^{\circ}x3.75^{\circ}$ resolution (latitude, longitude). The LMDz atmospheric transport model (Hourdin et al., 2006) was used at this resolution to convert these terrestrial fluxes into monthly atmospheric CO₂ concentrations, during the period 1989 to

2009. In order to complete the carbon balance at the planetary scale, we also transport the global 1 2 oceanic and fossil net carbon fluxes respectively taken from a climatology (Takahashi et al., 2009) and from the EDGAR database (http://edgar.jrc.ec.europa.eu). The contribution of biomass burning 3 is neglected, because re-growth of burnt vegetation is not accounted for in this version of 4 5 ORCHIDEE, and so are the evasion of CO2 from aquatic bodies and emissions from harvested wood and agricultural products. The transported fluxes are evaluated using 53 smoothed record of 6 7 atmospheric CO_2 concentrations (C_{CO2}) over the globe (supplementary Table S3) (GLOBALVIEW-CO2, 2013). As the optimization of the initial soil carbon content cannot be 8 spatially extrapolated for global simulations (see sect. 2.1), the modelled trend of C_{CO2} is not 9 evaluated. Rather, we focus on the seasonal analysis and use the curve-fitting procedures of 10 11 (Thoning et al., 1989) to extract the detrended seasonal signal of C_{CO2} . In addition, we identify the 12 contributions of 11 sub-continental regions to the simulated atmospheric CO_2 concentration at each 13 station by independently transporting the fluxes from each following area: boreal North America, 14 temperate North America, tropical America, South America, Europe, northern Africa, southern 15 Africa, boreal Asia, temperate Asia, tropical Asia, and Australia (e.g., Fig. 1 in (Gurney et al., 2003)). The simulated interannual variability of the C_{CO2} is evaluated using the model-data RMSD 16 17 of monthly anomaly, from the detrended smooth seasonal signal calculated above:

$$C_{CO2,anom} = C_{CO2,month} - \langle C_{CO2,month} \rangle_{allyears}, \qquad (6)$$

19 where $\langle C_{CO2,month} \rangle_{allyears}$ is the all-time average, for each month of the year.

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3 Results & discussion

3.1 Site-level simulation of carbon and water fluxes

24 Figure 1 shows the average corrections brought by the optimization to the modelled NEE fluxes 25 (with negative values meaning carbon uptake), grouped by dominant PFT (see acronyms in Table 1), in terms of RMSD and bias between simulations and measured data, also showing the 26 27 PFT-averaged mean seasonal cycles. The largest reductions of model-data RMSD are found in 28 temperate and boreal broadleaf forests (TempEBF, TempDBF and BorDBF), where the two 29 optimization scenarios (single- and multi-site) decrease the misfit by more than 25% compared with 30 the prior (unoptomized) model. In temperate needleleaf forests (TempENF) and C3 grasslands 31 (C3grass), the RMSD reduction exceeds 30% for single-site optimizations, but the corresponding multi-site sets of parameters reduce this value to less than 20%. The improvements are less 32 33 significant in tropical evergreen broadleaf forests (TropEBF) and boreal evergreen needleleaf 34 forests (BorENF), where the reductions of misfit is between 9 and 15%. Figure 1B shows that the

NEE is on average overestimated by the prior model for all PFTs. This feature is even more striking 1 in ecosystems which are marked sinks of carbon (according to the average measured carbon 2 3 balance, not shown), here tropical and temperate forests. This positive bias is an artifact from the model initialization procedure, which brings each simulated site to a near equilibrium (see sect. 4 5 2.1). It is significantly corrected by the optimization, notably via the scaling of the initial carbon pool content at each site (parameter K_{soilC} in Table 1), one consequence being a clear reduction of 6 7 the respiration during the winter of temperate and boreal ecosystems and grasslands sites in agreement with the measured data (Fig. 1C). 8

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10 Figure 2 shows that the simulation of the latent heat flux (LE) is overall less improved by the 11 optimizations than that of the net carbon flux, keeping however in mind the problem of energy balance closure discussed in sect. 2.3. The reduction of RMSD is the highest on average at 12 13 TempDBF sites with values 24% below the prior value, while decreases of 15 to 19% are found at TempEBF and BorENF sites. The effect of the optimization is the weakest on average at sites 14 15 located in TempENF and C3grass ecosystems. These weaker performances regarding LE flux indicate that the energy and water cycles in the ORCHIDEE model involve other relevant 16 17 parameters not optimised here, and possibly that the structural equations bear a significant error. Notably, we include in the optimization only one parameter that directly controls the soil 18 evaporation ($Z\theta_{\text{overheight}}$, see Table 1), and there is for example no constraint on the calculation of the 19 20 surface temperature, a key component of the energy balance.

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22 At the seasonal scale, Fig. 3A shows that large reductions (in relative value) of the simulated 23 mean seasonal NEE amplitude are found in boreal evergreen needleleaf and deciduous broadleaf 24 forests and C3 grasslands. The average correction is somewhat exaggerated in the two former cases 25 and relatively accurate in the latter case. Conversely, the seasonal NEE variations are consistently 26 amplified by the optimization in temperate evergreen needleleaf and broadleaf forests. However, the 27 averaged model-data phasing is only weakly modified for the five aforementioned PFTs, with the 28 exception of the site-specific improvements at TempENF and C3grass sites. Besides, considering 29 the mild correction of the model-data biases in BorENF, BorDBF and C3grass (Fig. 1B), one can 30 deduce that most of the reduction of RMSD discussed earlier is for these three PFTs due to an 31 improvement of the simulated NEE amplitude after the optimization.

In temperate deciduous broadleaf forests, the simulated pattern of NEE is chiefly improved via a better phased seasonal cycle, as shown by the increased phase score, which was already close to one before optimization. An earlier study at a similar set of sites of the same PFT showed that the optimization scheme tends to correct the overall prior model overestimation of the growing season length (Kuppel et al., 2012). On the other hand, the simulated seasonal amplitude of NEE is barely
changed after optimization, as the corrected flux overestimations in winter and summer tend to
cancel out, with a PFT-averaged seasonal amplitude remaining smaller than that of the observed
data (Figs. 1C and 3).

5 Regarding the latent heat flux, Fig. 3B shows that the optimization has generally a weaker effect on the simulated LE average phase and amplitude than in the case of NEE. In most cases the 6 7 correction brought by the optimization barely affects the modelled phase, but improves the seasonal amplitude. We notice that the LE seasonal cycle is most often flattened as compared to the prior 8 9 model in agreement with the observations, except for the inconsistent amplification at TempEBF sites and the over-reduction after the site-specific optimization in C3 grasslands. The weak phase 10 11 correction might be related to the soil evaporation component of the latent heat flux, on which the 12 optimization has a limited leverage as mentioned earlier in this section, while the transpiration rate 13 is tightly linked to GPP. It would also explain the generally lower phase coefficient in deciduous 14 ecosystems (Fig. 3), where soil evaporation is a potentially significant component of LE during leaf 15 onset and senescence.

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17 Besides, applying the Nash-Sutcliffe model efficiency coefficient (NSE, see Eq. 4) to all sites shows that TropEBF is the only PFT studied here where the PFT-averaged value of this metric 18 19 remains below zero after optimization for both fluxes, with NSE_{NEE} =[-2.77, -1.99, -1.83] and 20 NSE_{LE} =[-0.64, -0.35, -0.52] in prior, multi-site and site-specific cases, respectively (other PFT) 21 values not shown). It means that after optimization the model-data mean square error is still larger 22 than the variance of the observations, or, in other words, that the observed mean is on average a 23 better predictor than the model outputs. Figure 1 shows that for TropEBF the prior model simulates 24 an unobserved increase of NEE from sink to source around July, and the simultaneous decrease of 25 LE (Fig. 2) points towards an unrealistic simulated drought stress during this period of the year, the 26 driest at most sites of this PFT. The optimization barely corrects the NEE variations during the dry 27 season, although a more realistic LE flux is simulated after the multi-site optimization. An earlier 28 optimization study at a site of the same PFT highlighted the need for a much deeper soil water 29 reservoir along with a more linear root profile than that parameterized in the prior model, in order to 30 account for the ability of tropical evergreen forests to maintain high photosynthesis and 31 transpiration during the dry season (Verbeeck et al., 2011). Our multi-site parameterization of the 32 processes dealing with soil water availability goes in that direction, with values of soil water depth, 33 root profile and water stress coefficient respectively adjusted from 2 to 2.38 ± 0.065 m, from 0.8 to 34 0.72 ± 0.095 m⁻¹ and from 6 to 6.5 ± 1.06 (Table 1). These corrections from the prior parameterization remain however insufficient, as shown by the poorly realistic optimised seasonal 35

cycle of NEE in Fig. 1. On the other hand, (Verbeeck et al., 2011) also pointed at the structural 1 inconsistency in the standard ORCHIDEE model for tropical evergreen forests: the phenological 2 scheme notably neglects the leaf renewal at the transition between wet and dry season (Chave et al., 3 2010) and the hydric stress calculation ignores the role of groundwater (Miguez-Macho and Fan, 4 5 2012), while these mechanisms possibly explain the high subsequent photosynthesis and transpiration rates often observed (Weirdt et al., 2012). Concerning the LE flux, the optimization 6 brings somewhat limited, yet consistent changes, while the reduction of daily uncertainty is modest, 7 indicating a poor level of constraint by the observations used. It suggests either significant errors in 8 9 the model equations, or that relevant, poorly known parameters, have not been considered.

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3.2 Single-site versus multi-site

13 It can be noticed in Figs. 1, 2 and 3 that there is a general consistency across PFTs between RMSD reductions introduced by multi-site and site-specific optimizations, with some exceptions in 14 15 TempENF and most notably C3grass where the average site-specific RMSD reduction is twice as 16 large for NEE, while there is almost no average multi-site RMSD decrease for LE. Although the large number of sites selected for this last PFT and the associated inter-site variability calls for 17 18 prudence when considering average seasonal flux variations, it is worth noting that C3 grasslands are here the only PFT generically spanning such a diversity of climates. The reported discrepancy 19 20 might thus indicate a need for additional classes of C3 grasslands in the model, at least with a 21 climatic regionalization and ideally taking also into account pedologic conditions and management 22 practices.

23 More generally, one would expect better efficiency from a site-specific scheme than with a 24 multi-site approach, given that grouping sites with different characteristics introduces conflicting 25 constraints on the model equations, along with the fact that the RMSD is the criterion used in the 26 optimization procedure (as the prior covariance matrix in the cost function of Eq. (1) is chosen diagonal, see sect. 2.2). It is true most of the time, except notably for NEE in boreal deciduous 27 28 broadleaf forests and LE at TropEBF, TempEBF and BorENF sites where the multi-site 29 optimization results on average in larger RMSD decreases than the site-specific approach. In these 30 cases, Figs. 1 and 2 show that it stems from unchanged local RMSD after the site-specific 31 optimization at a few sites of these particular PFTs. As found by (Santaren et al., 2013), it may point 32 to a failure of the single-site inversion algorithm to converge towards the global minimum of the 33 cost function, possibly due to the presence of local minima. Our hypothesis is that the 34 corresponding multi-site cost functions avoid this pitfall because they are made more regular by the 35 larger amount of simultaneous constraints on the parameters, "smoothing out" some of the

problematic local minimums. Preliminary multi-site optimization tests, using a few tens of random starting points, support this hypothesis, and further investigations will be needed to evaluate if this behavior is valid for all PFTs. Indeed, we acknowledge some uncertainty regarding whether or not the optimised sets of parameters correspond to the very minimum of the cost function, as the efficiency of the variational optimization approach employed is conditional on a reasonable compliance with the linearity hypothesis.

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3.3 Site-scale uncertainty

9 In addition to improving the agreement between modelled and measured fluxes, the 10 optimization procedure is also useful to reduce the total uncertainty associated with the modelled 11 output variables at each site, defined as:

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 $\sigma_{total} = \sqrt{\sigma_{observations}^2 + \sigma_{parameters}^2}$ (7)

14

15 σ_{total} represents the summed contribution of two errors arising in the observation space: the 16 measurements error and the error of the equations of the model (see sect. 2.2). It is not directly 17 altered through parameter optimization, although the model component may in principle vary with 18 the parameter values. Following (Desroziers et al., 2005), σ_{total} is diagnosed at each site as the square 19 root of the covariance between the time series of prior and posterior flux residuals (model minus 20 observations). $\sigma_{\text{parameters}}$ is the parameter error contribution to the simulated fluxes, calculated at each 21 site, before optimization, as the average daily standard deviation of the projection in observation 22 space of the prior error covariance matrix P_b , using the model's Jacobian matrix H, based on the 23 definitions of sect 2.2. The same is done after optimization, respectively using P_a and H_{∞} .

Figure 4 reports the average value of for simulated daily NEE and LE, showing individual sites values and the corresponding PFT means as in Figs. 1 and 2. The reduction of the total NEE uncertainty varies from one PFT to another, ranging from 6% in tropical evergreen broadleaf forests to 33% in boreal evergreen needleleaf forests. As is reduced by 65 to 95% (not shown), we deduce from Eq. (7) that the weak relative decrease of indicates a dominance of the observation error in the total uncertainty budget. This is for example consistent with the reported inaccuracies in the model structure for TropEBF ecosystems discussed in the previous section.

Regarding the LE flux, the mild changes from prior to posterior uncertainty means that we might face a potentially large observation error component (model + measurements) –the latter being insensitive to parameter optimization, see sect. 2.3– and overall that little statistical information has been gained from the optimization of the selected water cycle parameters. Besides, one can notice that the posterior uncertainties are always slightly lower for multi-site optimization than with the site-specific approach, which is consistent with the fact that the number of assimilated data is larger in the former case than in the latter. Finally, we also found that the optimization suppresses at each site much of the temporal correlation of the flux error, which are large in the prior ORCHIDEE model (see for instance the time correlogram in the Fig. 1 of (Kuppel et al., 2013)). It results in a large decrease of the total yearly uncertainty from the prior model for all PFTs, by 77 to 86% and 43 to 80% for simulated NEE and LE flux, respectively (not shown).

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3.4 Simulated GPP and respiration

10 Figure 5 shows the mean seasonal cycle, averaged over each PFT, for the gross carbon fluxes: photosynthesis (GPP, Fig. 5A) and ecosystem respiration (Reco, Fig. 5B). The "observed" values are 11 estimates based on a partition of the measured NEE (see sect. 2.4). These gross carbon fluxes have 12 13 not been used as constraints in the optimization procedure, but are useful as indicators of the model 14 performance. One can first notice that the average increases of GPP at TropEBF and TempEBF sites 15 are responsible for the NEE decrease observed in Fig. 1. It is worth noting that the results reported 16 in Fig. 5 also confirm the inability of the model to simulate a sustained high photosynthesis rate 17 during the dry season at TropEBF sites (see Sect. 3.1), while this feature appears in the observations estimates. At TempENF sites, the remarkable adjustment of the NEE cycle primarily derives from a 18 19 reduced Reco at the peak of the growing season. Both GPP and Reco are consistently decreased in 20 boreal forests and C3 grasslands sites, although the reduction is still lower than what would be 21 needed to match the estimates. In addition, because the respiration rate is the sole reducing component in winter and because the photosynthesis rate is more largely decreased than R_{eco} during 22 23 the growing season, the net result is the reduction of the seasonal amplitude of NEE for these three 24 PFTs. Finally there is a large, yet insufficient, decrease of R_{eco} after the optimization in temperate 25 deciduous broadleaf forests, notably related to the scaling of the initial carbon pool content (sect 3.1 26 and (Kuppel et al., 2012)), while GPP is less drastically reduced, in close agreement with the 27 observations. This evaluation at each site with gross carbon fluxes shows that the optimization 28 procedure is able to provide a set of parameters which improves the simulation of both assimilation 29 and respiration processes in the ORCHIDEE model for six out of the seven PFTs considered here, 30 suggesting a partial distinction of both gross contributions from the constraint provided by the net 31 carbon flux.

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33 **3.5 Global-scale evaluation**

34 One of the objectives of assimilating flux data from a large number of sites, spanning a wide 35 range of ecosystems, is to identify generic sets of parameters that improve the simulation of carbon and water balance at the regional-to-global scale. Indeed, there is no guarantee that a set of parameters improving the simulations at an ensemble of individual sites sharing broadly common biogeochemical and biophysical characteristics, but with a limited spatial footprint, will also be beneficial for simulations at much larger scales. In this context, global simulations allow evaluation of how the constraint of eddy covariance data is propagated from one spatial scale to another, and how transferable the optimised parameterization is from grouped in situ optimizations to gridded simulations.

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3.5.1 Seasonality of atmospheric CO₂ concentrations

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11 Regarding the simulated mean seasonal cycle of atmospheric C_{CO2} , the optimised set of 12 parameters yields a median reduction of the model-data RMSD of 5.2%. Among the 53 samples 13 locations used in this study, there is a significant improvement at 27 of them with a RMSD decrease 14 larger than 5%, a notable degradation at 20 sites with a RMSD increase larger than 5%, and less 15 than a 5% shift at the remaining 6 locations. In addition, a latitudinal clustering can be identified, as a large median improvement by 42.2% (RMSD-wise) is found at the 3 northernmost sites (Alert, 16 17 Ny-Alesund, and Barrow) and by 33.5% at the 18 locations of the Southern Hemisphere, while 18 there is a median degradation by 5.6% in the rest of the Northern Hemisphere.

19 Figure 6 shows the mean seasonal cycle of the simulated C_{CO2} , compared to the extended record 20 at three locations, one in each of the latitudinal areas defined above: Alert, South Pole, and Mauna 21 Loa, respectively. We note that using the optimised parameters sets tends to reduce the seasonal 22 amplitude of C_{CO2}, with in the Northern Hemisphere an earlier phasing for the "breathing of the 23 biosphere". At station Alert, there is a significant adjustment of the simulated seasonal cycle, when 24 changing from the default to the multi-site parameterization of the ORCHIDEE model. This 25 correction chiefly benefits the seasonal amplitude, which is decreased and becomes remarkably 26 close to that observed. The analysis of the contribution of the 11 sub-continental regions in the 27 simulated atmospheric signal (see sect. 2.4), grouped in Fig. 6D in larger regions, indicates that the 28 major terrestrial contribution to this result are changes in C_{CO2} due to the boreal Northern 29 Hemisphere fluxes. It is consistent with the decrease of the NEE seasonal amplitude produced by 30 the multi-site optimization at sites in boreal evergreen needleleaf forests, boreal deciduous 31 broadleaf forests and C3 grasslands (Figs 1C and 3A), dominant in this region. Separate global 32 simulations using optimised parameterization for one PFT at a time show that the degraded phasing 33 at Alert produced by the multi-site approach in Fig. 6A mainly stems from the contributions of BorENF and C3 grasslands ecosystems (not shown). While a mild multi-site phase deterioration 34 35 from the prior parameterization is found at the site level in BorENF (Fig. 3A), it is not the case for

C3 grassland and it may thus question the representativeness of the flux measurements sites used,
 with respect to high-latitudes ecosystems in general.

3 At station South Pole, the model-data fit is also mostly enhanced after the optimization by a significant decrease of the seasonal amplitude of C_{CO2} , which is more than twice as large in the prior 4 5 simulation as in the measured data. Besides, the "regionalized" analysis indicates that the corrections are primarily due to the reduced seasonal amplitude of C_{CO2} components from temperate 6 South America and southern Africa, and contributions from the boreal Northern Hemisphere are 7 also noticeable (not shown). We therefore deduce that the optimization of C3 grasslands parameters 8 9 is the most influential factor explaining the improved simulation of C_{CO2} at this station, but also that 10 the influence of boreal needleleaf evergreen forests cannot be neglected here.

11 The reduction of the simulated cycle amplitude is too strong at station Mauna Loa, which, 12 combined with earlier seasonality, leads to a poorer model-data fit after optimization. The remote 13 location of Mauna Loa (north Pacific) makes it sensitive to influences from most of the Northern 14 Hemisphere. We find that the main drivers of the simulated correction are flattened, earlier C_{CO2} 15 variations in temperate and boreal regions of North America and Asia, and Europe (not shown). These results thus reflect part of the reduction of the seasonal amplitude of NEE in boreal 16 17 ecosystems and C3 grasslands noticed at Alert and South Pole stations. The degraded model-data fit 18 between optimised C_{CO2} and data from Mauna Loa also suggests that the boreal correction of NEE 19 amplitude is too strong or insufficiently compensated at large scale by the amplification of the 20 seasonal cycle at temperate latitudes visible at TempENF and TempDBF sites (Figs. 1C and 3A).

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22 Finally, using the multi-site-optimised model overall brings a small improvement of the 23 modelled interannual variability of C_{CO2}, with a median reduction of 3.9% for the RMSD between 24 modelled and measured monthly anomaly (not shown). Forty-five locations, out of the 53 used in 25 this study, display an improvement with RMSD decreases up to 27%, while at the remaining 8 sites 26 the degradation of the simulated interannual variability remains small with RMSD increases always 27 smaller than 1.5% (not shown). These results suggest that despite the relative shortness (one to three 28 years) of most of the FluxNet datasets selected to optimise the ORCHIDEE model, the diversity of 29 the covered weather situations gives a modest, yet consistent source of information to better 30 reproduce interannual variations of carbon fluxes at the global scale.

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3.5.2 Global scale phenology index

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Figure 7 reports for each optimised PFT the correlation factor between weekly values of measured NDVI and modelled FAPAR during the period 2000-2010 (see sect. 2.4), for both the

prior and optimised model. There is no result for BorDBF whose vegetation fraction never exceeds 1 40% in our case. All remaining six PFTs exhibit a higher median correlation factor when using the 2 3 multi-site parameterization, which means that the modelled leaf seasonal cycle better matches the 4 global scale observations. This median improvement seems to accurately reflect the overall trend 5 for TempDBF-, BorENF- and C3grass-dominated pixels, while a larger inter-pixel variability is introduced in the case of temperate evergreen forests. The improved modelled seasonality is related 6 7 to the more accurately simulated GPP at FluxNet sites after multi-site optimization, the latter being in turn partly driven by the improvement of the seasonal variations of simulated LAI. The dominant 8 9 feature seems to be a shorter growing season length for TempDBF, which is consistent with the 10 site-level simulations of GPP seasonality for this PFT (Fig. 5A), and an earlier beginning of the 11 growing season for C3 grasses (not shown). Note that this improvement also explains most of the 12 increased correlation factors in temperate and boreal evergreen forests, since these PFTs do not 13 present a climate-driven leaf phenology in the current formulation of the ORCHIDEE model. 14 Consequently, deciduous and herbaceous PFTs are the only significant contributors to the seasonal 15 cycle at such a coarse resolution, even when these ecosystems are secondary and/or the understory within an evergreen-dominated forest. Lastly, the score for TropEBF remains poor because the 16 17 model wrongly simulates the leaf renewal and the hydric stress during the dry season, as discussed in Sects. 3.1 and 3.4. 18

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3.6 Limitations of the current approach: summary and discussion

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The limitations to our model-data fusion method highlighted throughout the results section are of three kinds, somewhat interlocked: 1) within the limits of the model structure, 2) how adequate the chosen set of optimised parameters was and 3) how close to the optimal values the optimization algorithm tuned these parameters.

26 Taking these items in reverse order, we first acknowledge that using a variational 27 optimization algorithm with a model with non-linearities might expose to miss the global minimum 28 of the cost function, and indeed a few obvious convergence failures cases have been found for some 29 single-site optimizations in TropEBF, TempENF, and boreal forests. Some functions of the 30 ORCHIDEE model could potentially be linearized to generate a more accurate tangent linear model 31 -and to advantageously avoid to use finite-differences for some phenological parameters (see Sect. 32 2.1)-, while remaining coherent with the model's philosophy. It might imply a demanding effort of 33 model recoding, but it has already been done for another LSM (Knorr et al., 2010). Alternatively, 34 stochastic optimization approaches could yield better convergence, as they can circumvent the 35 linearity constraint. While a single-site model-data fusion study with the same LSM showed

advantageous results for a genetic Monte-Carlo-based technique over its variational counterpart (Santaren et al., 2013), no major difference was found by (Ziehn et al., 2012) between Monte-Carlo and gradient-based approaches when optimizing a simpler LSM with atmospheric CO_2 observations. In the case of a multi-site optimization efforts, we suggest that the cost function "smoothing" discussed in Sect. 3.2 could make the convergence efficiency less sensitive to the choice of the minimization approach, while keeping in mind the much lower computational time required in the variational case.

Second, the number of optimised parameters remains somewhat modest as compared to the 8 9 diversity of processes modelled in the ORCHIDEE model. Our choice was partly driven by a model sensitivity criterion, while the actual leverage of an optimised parameter on model outputs also 10 11 depends on the uncertainty associated to this very parameter (Dietze et al., 2014). It can result in selecting some parameters that are already reasonably well known but that have medium-to-high 12 13 model sensitivity and thus with low overall leverage, while poorly known parameters with 14 mild-to-low model sensitivity could have a comparatively higher value for the optimization. In addition, as our focus was on the carbon cycle, only a few water-and-energy-related parameters 15 were considered. Notably, the correction of LE partly benefited from that of NEE via transpiration, 16 17 but the soil evaporation optimization was neglected despite being a significant -and debated- player of the terrestrial water cycle (Schlesinger and Jasechko, 2014). 18

19 The third hindering factor to simulating carbon and water fluxes close to their true value is 20 the "observation error", i.e. the uncertainty arising from the simplification needed to make 21 ecosystem functioning fit within explicit equations plus the error made associated to the 22 measurements, fluxes and meteorological forcing included. Although this error is rarely quantified 23 in model-data fusion efforts, model-data fit analyses and uncertainty budgets showed in this study 24 that the relative importance of this observation error greatly varies from one PFT to another -and is 25 potentially dominated by the model error component in the case simulations at flux towers sites 26 (Kuppel et al., 2013). It is the highest in tropical evergreen broadleaf forests, where parameter optimization will likely be of limited help until a more realistic phenological scheme is 27 28 implemented. Regarding the simulations of LE in general, the small amount of related parameters 29 optimised makes it difficult to assess to which extent the nearly-unchanged flux uncertainty comes 30 from the parameter scarcity or structural inaccuracies in the model, stressing again the need for a 31 better consideration of water and energy cycles together with that of carbon in future model-data 32 fusion efforts.

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34 4 Conclusions

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1 Generalizing the results of (Kuppel et al., 2012) across ecosystems, this study has shown that a 2 significant degree of improvement is introduced to the simulation of carbon and water fluxes, 3 through a generic optimization approach with in situ measurements of NEE and LE fluxes, relying on the traditional PFT classification used in many land surface models. At the global scale, this 4 5 optimization method allows first a better simulation of the seasonal foliar cover. Second, the multi-site parameter set has a significant leverage upon the simulated seasonality of atmospheric 6 7 C_{CO2}, with performances somewhat spatially heterogeneous and depending on the PFT considered, while a small, yet encouraging improvement of the simulated interannuality of C_{CO2} is found. The 8 9 remaining discrepancies in C_{CO2} indicate that combining atmospheric CO2 concentration and a larger number of flux towers observations, in a Carbon Cycle multi-Data Assimilation Systems 10 11 (CCDASs, e.g., (Kaminski et al., 2013)), would be beneficial. Using more site-years of flux data 12 will also allow a systematic in situ evaluation of the multi-site parameters across time periods. 13 regions and climate regimes by separating training sites from evaluation sites. Such procedure was 14 not applied in this study due to the small number of sites for some PFTs, but remains essential to 15 test a LSM used for climate projections. More generally, we suggest that the assimilation of FluxNet data should be considered as a baseline for the development of multi-data assimilation 16 17 systems where more complementary data streams are combined. In particular, daytime and nighttime NEE could replace the daily values used here, and adding measurements of leaf area 18 19 index, soil respiration fluxes (e.g. chamber measurements), biomass and litter/soil carbon pools, 20 would help better separating the processes and constraining environmental drivers, as would a 21 simultaneous parameter optimization of both over- and understory PFT fractions. The FluxNet 22 multi-site approach can also be used to characterize the structural, parametric and total uncertainties 23 associated with the simulated annual biospheric carbon balance at regional-to-global scales, and to 24 compare it with 1) the discrepancies of results between global ecosystem models (Sitch et al., 25 2008), and 2) the error carried by the terrestrial carbon fluxes estimated via inverse modeling with 26 atmospheric transport models (e.g., (Chevallier et al., 2010)). The underlying problem is thus to 27 evaluate what would be gained from simultaneously assimilating various data streams covering different spatial and temporal scales into a terrestrial ecosystem model, and how the PFT 28 29 classification should be refined to maximize this improvement. In parallel, by using a diagonal prior 30 covariance matrix for parameter error, within a same PFT and across PFTs, we implicitly assumed 31 that all parameters could in principle be efficiently corrected as independent random distributions. It 32 ignores the fact that a covariance structure interlinking the optimised parameterization would be 33 necessary to translate the interconnectedness of ecophysiological processes within a given PFT. For 34 instance, the allocation of carbon within the plant reservoirs depends on specific allometric relations 35 and on photosynthesis rate; these relations would need to be embedded in the prior parameter error

1 covariance matrix. Additionally, the influence of nearby individuals of other PFTs (e.g., the 2 understory) should be accounted for when correcting parameters of a given PFT. Together with a 3 simultaneous optimization of several PFTs, building standard spatialized parameter covariance 4 tables from databases of plant traits and soil characteristics (e.g., (Kattge et al., 2011)) and 5 'preliminary' posterior multi-site parameter error covariance matrices (e.g., supplementary material 6 of (Kuppel et al., 2012)) might soon become necessary to consistently apply model-data fusion to 7 more sophisticated mechanistic ecosystem models.

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5 Code availability

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11 The code of the data assimilation available source system is at 12 https://pypi.python.org/pypi/ORCHISM. Regarding the ORCHIDEE vegetation model, the source 13 files of the Tag version 1.9.5.2 used for this study can be obtained upon request (see 14 http://labex.ipsl.fr/orchidee/index.php/contact), while the associated documentation can be found at 15 https://forge.ipsl.jussieu.fr/orchidee/wiki/Documentation. Note that the tangent linear version of the ORCHIDEE model has been generated using a commercial software (TAF, see sect. 2.2). For this 16 17 reason, only the 'forward' version of the ORCHIDEE model is available for sharing, to which only the finite differences method is employed for parameter optimization. Finally, the source code of the 18 19 LMDz atmospheric transport model can be found at <u>http://web.lmd.jussieu.fr/trac</u>.

20

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- 4

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Table 1. Parameters of ORCHIDEE optimised in this study. The prior values are given for each PFT, and multi-site posterior values are in bold font. A hyphen means that the parameter is not optimised, *spinup* that the spinup value is taken, and **site** that the posterior value is site-specific.

Parameter	Description	Plant functional type ^a						
		Trop	Temp	Temp	Temp	Bor	Bor	<u>C3</u>
		EBF	ENF	EBF	DBF	ENF	DBF	grass
Photosynt	hesis							
$V_{\rm cmax}$	Maximum carboxylation rate	65	35	45	55	35	45	70
$G_{\rm s, slope}$	(μmol.m ⁻² .s ⁻¹) Ball-Berry slope	7 0.28 9	31.94 9	47.84 9	55.83 9	32.36 9	32.97 9	51.10 9
$\mathcal{C}_{\mathrm{Tmax}}$	Offset controlling the maximum	8.756 55	8.841 38	10.99 48	6.000 38	7.961 38	7.714 38	9.970 41.13
$\mathcal{C}_{\mathrm{Topt}}$	photosynthesis temperature (°C) Offset controlling the optimal	55.31 37	40.41 25	49.66 32	36.09 26	36.42 25	36.70 25	40.20 27.25
$\mathcal{C}_{\mathrm{Tmin}}$	photosynthesis temperature (°C) Offset controlling the minimal	35.93 2	17.49 -4	28.82 -3	28.44 -2	26.48 -4	28.71 -4	29.76 -3.25
	photosynthesis temperature (°C)	1.356	-7.536	-6.062	-0.219	-6.167	-2.563	-3.403
Phenology	V							
SLA	Specific leaf area (foliar surface per dry	0.0154	0.0093	0.02	0.026	0.0093	0.0260	0.0260
LAI _{MAX}	matter content, m ² .g ⁻¹) Maximum LAI (m ² .m ⁻²)	0.0169 7	0.0200 5	0.0252 5	0.0400 5	0.0090 4.5	0.0233 4.5	0.0345 4.5
$K_{ m lai,happy}$	Minimum fraction of LAI _{MAX} to stop	7.000 0.5	5.000 0.5	5.000 0.5	3.949 0.5	4.500 0.5	4.960 0.5	2.349 0.5
$K_{ m pheno,crit}$	carbohydrate use Multiplicative factor for growing season	0.500 -	0.500 -	0.500 -	0.321 1	0.500 -	0.547 1	0.408 1
$\mathcal{C}_{\mathrm{T,senes}}$	start threshold Offset controlling the temperature	-	-	-	1.510 12	-	0.758 7	0.729 -
$L_{ m agecrit}$	threshold for senescence (°C) Critical age for leaves (days)	730	910	730	14.36 180	910	7.899 180	120
LAI _{init}	Initial LAI (m ² .m ⁻²)	717.9 spinup	1084 spinup	709.2 spinup	165.1 -	790.5 spinup	163.3 -	113.9 <i>spinup</i>
		site	site	site		site		site
Soil water	availability							
$f_{ m stressh}$	Parameter reducing the hydric limitation	6	6	6	6	6	6	6
Dpu _{cste}	of photosynthesis Total depth of the soil water reservoir (m)	6.507 2	7.146 2	7.135 2	5.039 2	4.881 2	5.505 2	5.131 2
<i>Hum</i> _{cste}	Parameter describing the exponential root	2.377 0.8	2.387 1	1.536 0.8	0.959 0.8	2.012 1	2.303 1	1.865 4
	profile (m ⁻¹)	0.718	1.102	0.743	1.577	1.874	0.676	2.800
Autotroph	ic respiration							
$MR_{\rm a}$	Slope of the temperature dependence	0.16	0.16	0.16	0.16	0.16	0.16	0.16
MR _b	Offset of the temperature dependence of	0.105 1	0.127 1	0.156 1	0.094 1	0.185 1	0.178 1	0.174 1

$GR_{\rm frac}$	maintenance respiration Fraction of biomass available for growth	0.929 0.28	0.772 0.28	0.928 0.28	0.622 0.28	0.710 0.28	1.212 0.28	1.140 0.28
	respiration	0.269	0.250	0.265	0.206	0.303	0.301	0.317
Heterotrophic respiration								
$K_{ m soilC}$	Scaling factor for all initial soil carbon	1	1	1	1	1	1	1
Q_{10}	stocks after spinup Factor of the temperature control function	site 1.994	site 1.994	site 1.994	site 1.994	site 1.994	site 1.994	site 1.994
$HR_{\mathrm{H,b}}$	Parameter of the soil/litter moisture	2.119 2.4	1.676 2.4	2.067 2.4	2.182 2.4	2.879 2.4	2.663 2.4	2.778 2.4
$HR_{\mathrm{H,c}}$	control function Offset of the soil/litter moisture control	2.356 -0.29	2.387 -0.29	2.343 -0.29	2.191 -0.29	2.503 -0.29	2.457 -0.29	2.489 -0.29
	function	-0.332	-0.272	-0.329	-0.544	-0.192	-0.252	-0.304
Decompos	sition							
$h_{ m crit,litter}$	Total litter height (m)	0.08	0.08	0.08	0.08	0.08	0.08	0.08
$Z_{ m decomp}$	Factor of the exponential profile of soil	0.0697 0.2	0.0434 0.2	0.0613 0.2	0.0200 0.2	0.0213 0.2	0.114 0.2	0.0358 0.2
	temperature and moisture	0.371	0.649	0.175	0.142	0.662	0.474	0.448
Energy ba	llance							
$K_{ m albedo,veg}$	Multiplicative factor of surface albedo	1	1	1	1	1	1	1
$Z0_{\rm overheight}$	Reference roughness length (m)	1.031 0.0625	1.042 0.0625	0.930 0.0625	1.110 0.0625	1.076 0.0625	1.048 0.0625	0.989 0.0625
		0.0648	0.0877	0.0359	0.0200	0.0200	0.0513	0.0200

^a TropEBF = tropical evergreen broadleaf forest; TempENF = temperate evergreen needleleaf forest; TempEBF = temperate evergreen broadleaf forest; TempDBF = temperate deciduous broadleaf forest; BorENF = boreal evergreen needleleaf forest; BorDBF = boreal deciduous broadleaf forest; C3grass = C3 grassland.



Figure 1. Model-data (A) RMSD and (B) bias for the daily NEE time series at each site (filled circles), grouped and averaged by PFT (horizontal bars), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange). (C) PFT-averaged mean seasonal cycle of NEE, for the training observations (black) and the three aforementioned cases, smoothed with a 15-day-moving-average window.



Figure 2. Model-data (A) RMSD and (B) bias for the daily LE time series at each site (filled circles), grouped and averaged by PFT (horizontal bars), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange). (C) PFT-averaged mean seasonal cycle of LE, for the training observations (black) and the three aforementioned cases, smoothed with a 15-day-moving-average window.



Figure 3. PFT-averaged model phase coefficient versus model-to-data amplitude ratio, for the detrended smooth seasonal cycles of **(A)** NEE and **(B)** LE fluxes. Simulations using prior parameters (green) are compared to multi-site (blue) and single-site (orange) optimizations, with the measured reference indicated by the intersection of the dashed lines.

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Figure 4. Uncertainty of simulated daily (A) NEE and (B) LE fluxes. For each PFT, the horizontal lines give the average of the individual site values (filled circles), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange).



Figure 5. PFT-averaged mean seasonal cycles of (A) the photosynthetic carbon flux and (B) the respiration flux, smoothed with a 15-day-moving-average window. The simulations using prior (green), single-site (orange) and multi-site (blue) parameterizations are compared to the evaluative observation-derived flux estimates (black).



Figure 6. Detrended mean seasonal cycle of the atmospheric CO₂ concentrations at (A) Alert, (B) South Pole and **(C)** Mauna Loa locations during the 1989-2009 period: the optimization-independent concentrations records (black) are compared to simulations where the biospheric contribution is calculated using the ORCHIDEE model with default (green) and multi-site (blue) parameterization, with the model-data RMSD given between brackets. (D) Regional contributions to the mean seasonal cycle simulated at Alert.



Figure 7. Correlation factor between weekly time series of modelled FAPAR and independent measurements of NDVI, for the 2000-2010 period. The results are grouped using the dominant PFT at each pixel, for global simulations with default (green) and multi-site parameterization (blue). The central horizontal bar indicates the median value, the top and bottom of the boxes correspond to the first and last quartile, and the 5- and 95-percentile are given by the 'error bars'.