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CranSLIK v1.0: stochastic prediction of oil spill transport and fate using approximation methods

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Abstract

This paper investigates the development of a model, called CranSLIK, to predict the transport and transformations of a point mass oil spill via a stochastic approach. Initially the various effects that affect the destination are considered and key parameters

- ⁵ are chosen which are expected to dominate the displacement. The variables considered are: wind velocity, surface water velocity, spill size, and spill age. For a point mass oil spill, it is found that the centre of mass can be determined by the wind and current data only, and the spill size and age can then be used to reconstruct the surface of the spill. These variables are sampled and simulations are performed using an open-
- source Lagrangian approach-based code, MEDSLIK II. Regression modelling is applied to create two sets of polynomials: one for the centre of mass, and one for the spill size. A minimum of approximately 80 % of the oil is captured for the Algeria scenario. Finally, Monte-Carlo simulation is implemented to allow for consideration of most likely destination for the oil spill, when the distributions for the oceanographic conditions are known.

1 Introduction

Whilst the frequency of spills occurring has dropped significantly in the last few decades, Etkin (2001), it does not diminish the inevitability of an oil spill occurring. Oil spills can cause large scale destruction of the environment, they have significant
²⁰ economical effects, and can result in human lives losses. They are inevitably the cause of environmental, economic, and human disaster. The Deepwater Horizon spill, for example, has been analysed extensively by Graham et al. (2011), members of the US National Commission on the BP Deepwater Horizon Oil Spill and Offshore Drilling. There is therefore much interest in being able to accurately predict the destination,
²⁵ transport, and transformation of an oil spill to minimise the resultant cost, both financial and environmental.



There are many complex phenomena affecting an oil spill, creating an advectiondiffusion-transformation process. These consist of a large number of effects: the advection due to currents, wind and waves, the diffusion due to the turbulence and the transformation processes, such as evaporation, natural dispersion, spreading etc.,

- which need to be considered for accurate fate and transport prediction. There are numerous equations available which are created to model these effects, based on both analytical and empirical approaches, however the complexity of the underlying physics is not yet fully understood. Reed et al. (1999) provide a very good summary of early models. Since then significant progress has been made in acquiring a deeper under standing of the involved complex phenomena, for example biodegredation is studied
- by McGenity et al. (2012).

Difficulty also arises from the side of uncertainty since exact quantities are not necessarily known beforehand due to the stochastic nature of certain variables, for example the sea surface velocity. The computational cost involved in running multiple cases,

or Monte-Carlo simulation, to consider the possible conditions is often far too great to be a viable approach. This becomes a severe impediment in cases of real accidents where a quick, or even real time, prediction becomes necessary.

Many models have been developed and used to predict the transport and transformation of an oil spill. These are either commercial, such as Li et al. (2013), or open-source,

- ²⁰ such as De Dominicis et al. (2013a). Regardless of the software tools employed, these models are not without their limitations. Often the computational cost involved in running a full simulation is too high. Alternatively, in order to be able to have a prediction in near real time, the model has to be simplified extensively, in terms of its physics, and therefore the simulation results are not of high accuracy.
- ²⁵ This paper investigates the use of stochastic methods to map the response from different input variables to create a robust and efficient software tool capable of effective prediction. This provides an estimation of the destination and spread of an oil spill subject to oceanographic conditions. Also, due to the minimal computational time required for the developed model, probable regions for the oil spill can be developed in real time



via Monte-Carlo simulation. This aids significantly in reducing the resultant financial and environmental cost of oil spills, predicting their likely development.

The key steps in developing our methodology can be outlined as follows:

- 1. identify the key parameters and their relative distributions necessary for short term oil spill prediction.
- 2. Apply sampling to the considered parameters to create a design hypercube.
- 3. Generate simulation data using the design hypercube.
- 4. Fit regression models to map the inputs to the response.
- 5. Use aforementioned regression model to create a prediction code.
- 10 6. Test the developed code against a real scenario and analyse the results.

In order to generate simulation data, we have used the MEDSLIK II model. This choice was based on a number of reasons, but predominantly due to its robustness and because it has been validated on multiple real spills as discussed in De Dominicis et al. (2013b, a).

15 2 Physics and mechanics of oil spills

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As stated in the introduction, one of the main complexities of modelling an oil spill is accurately accounting for the many complex physical phenomena that are the advection– diffusion–transformation processes. As the water and oil interact, there are several physical and chemical reactions which occur and increase the complexity of the resultant flow physics. Reed et al. (1999) provide a summary of the state of the art models

tant flow physics. Reed et al. (1999) provide a summary of the state of the art models available at the time of publishing. However, significant advances have been made since then, for example, the role of microorganisms in biodegredation is now better understood as discussed in McGenity et al. (2012). In particular, Reed et al. (1999)

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provide an in depth analysis into the transport and weathering procedures and the varying models used to account for complex flow behaviour. A diagram showing these effects can be seen in Fig. 1 (MEDESS-4MS, 2013; ITOPF, 2013).

The importance of these effects varies over time and a speculative mass balance can be seen in Fig. 2 (Mackay and McAuliffe, 1989). This implies that, for short term modelling, it is not necessary to fully resolve all phenomena. However, different considerations will need to be made in order to provide accurate predictions over longer periods of time.

2.1 Advection and turbulent diffusion

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Advection is a three dimensional process whereby the oil is transported due to wind, wave and current forcing. Traditionally this was thought to be a two dimensional effect however there have been numerous demonstrations of the importance of the vertical oil motion, including experimental (both field and laboratory) and computational simulation studies. Determining the magnitude of these effects is difficult due to the complex phenomenon that causes them.

The most important factor in the advection process is the current forcing. This is responsible for the majority of the displacement due to the direct contact between the water and the oil. The oil can also be transported vertically into the water column by the current and hence both the horizontal and vertical current shear are important in the motion of an oil spill (Reed et al., 1999).

Wind speed can be separated into two main components: long term and short term. The short term fluctuations are traditionally modelled by a Weibull distribution (de Prada Gil et al., 2012). Results have shown though that this may be a rather poor distribution. In Morgan et al. (2011) other possible distributions have been investigated

²⁵ and the produced results suggest that the 2-parameter Log-normal model is most appropriate for extreme wind speeds however still possesses significant errors. The wind speed also varies greatly upon the position on the globe one is interested in.



A similar problem exists for prediction of wave propagation. There is the generation of turbulent kinetic energy from the breaking of waves. Fay (1971) suggests that the first order effects of surface waves are negligible due to their periodic nature. The waves produce oscillatory forces which have a mean velocity component of zero. Therefore, over a sufficiently long time scale, the first order waves are negligible. Fay (1971) does however make note of the existence of non-linear waves which can affect the spread of oil.

2.2 Spreading

Another effect is the spreading of the oil due to film thickness and area. The classic equations to estimate the spread of an oil were defined by Fay (1971) and can be seen in Table 1. By making the assumption of no wind, wave or current effects, he suggested different spreading laws for both one-dimensional and axisymetric flows. The assumptions are justified in terms of importance, assuming that these effects are superimposed on the spreading motion. However, it is stated that without consideration of wind and wave effects, there is very little practical application for these equations. To derive his 15 equations, the various effects that might enhance or inhibit spreading are considered: gravity, inertia, surface tension, and friction. Whilst gravity acts in the vertical direction, there is a horizontal effect on the oil and an uneven pressure distribution is created. This forces the oil to spread out into an increasingly thin film over the surface of the water. The surface tension also plays a role in this expansion and eventually becomes 20 the main driving force. The rate of spread is restricted by the inertia and the friction. The effect of inertia decreases as the film becomes thinner. The friction is due to the small amount of water underneath the film.

2.3 Evaporation and emulsification

²⁵ Evaporation is one of the key oil transformation processes. Whilst the majority of the components are too heavy, there is a significant amount of short chain molecules which



evaporate. The rate of evaporation is determined by numerous effects, such as the wind speed and the temperature. The relationship is thought to be logarithmic with time due to the evaporation of less volatile components as discussed in ASCE Task Committee on Modelling of Oil Spills of the Water Resources Engineering Division (1996). Mackay and McAuliffe (1989) suggest a typical value of approximately 30 % in the first day or

- ⁵ and McAuliffe (1989) suggest a typical value of approximately 30% in the first day or so of spilling. According to Huang (1983), the models used for evaporation generally have similar approaches:
 - the oil is assumed to consist of numerous hydrocarbon groups
 - for each hydrocarbon group, the loss due to evaporation is assumed to follow
 - a logarithmic equation or first order kinetics
 - the evaporation rate is thought to be a function of the following physical parameters: spill area, wind speed, vapour pressure, slick thickness, and temperature.

Emulsification is the process where the oil adsorbs water. Stable emulsions can wave water levels of between 55 and 85%, expanding the spill volume by a large factor (Finigas et al., 1999). This is clearly very important in modelling the fate of an oil spill. It also affects the dissolution and the biodegredation processes.

2.4 Natural dispersion

Natural dispersion is also an important effect in the initial stages of the oil spill. This is defined as the breakup of the oil into small droplets and how these droplets spread and diffuse in the water column. The main source of dispersion is due to the turbulent mixing induced by the wind and wave propagation. There are a few different models available. Many are based on empirical data and can be expressed in a percentage of oil per day based on wind and sea conditions.



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2.5 Biodegredation

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This is where the oil is broken down by microorganisms into smaller elements which can be diffused. This is often exploited and such organisms are added to accelerate this effect for clean-up operations (US Congress, Office of Technology Assessment, 1991). The rate of biodegredation varies with many effects, such as the turbulent mixing rate and the abundance of oil eating microorganisms. Typically, this is a very slow process and is important in the very late stages of an oil spill. Organisms can also have other effects on the oil properties, for example an increase of oil viscosity. An in

depth analysis of biodegredation can be seen in Miiller et al. (1987).

3 Uncertainties and stochastic modelling

Another complexity in modelling arises from the uncertainty involved in prediction of oceanographic conditions and spill parameters. Many parameters, which are known to have an important role in the destination of an oil spill, are stochastic in nature and therefore difficult to accurately predict.

- ¹⁵ Wind forcing, i.e., the wind velocity components at 10 m above the sea surface, is provided by meteorological models, while currents and temperature are provided by oceanographic models. The current velocities used in this work come from the Mediterranean Forecasting System (MFS) described in Pinardi et al. (2003); Pinardi and Coppini (2010). The MFS system is composed of an Ocean General Circulation Model
- (OGCM) at 6.5 km horizontal resolution and 72 vertical levels (Tonani et al., 2008; Oddo et al., 2009). Every day MFS produces forecasts of temperature, salinity, intensity and direction of currents for the next ten days. Once a week, an assimilation scheme, as described in Dobricic and Pinardi (2008), corrects the model's initial guess with all the available in-situ and satellite observations, producing analyses that are initial condi-
- tions for ten days ocean current forecasts. The modelled currents and wind fields can be affected by uncertainties that arise form model initial conditions, boundaries, forcing



fields, parametrisations, etc. In this paper the hourly mean analyses have been used to eliminate the additional uncertainty connected with forecasts for both atmospheric and oceanographic input data.

One example is the wind velocity. This is usually modelled using a Weibull distri-⁵ bution (de Prada Gil et al., 2012). However, a two-parameter Log-normal model has been suggested as more appropriate for modelling of extreme values, although it still demonstrates significant errors (Morgan et al., 2011).

Whilst many of these parameters may be measurable at the initial time, prediction of the oil spill destination requires reasonable estimation of the conditions over the simulation period. There are numerous methods for circumventing this problem; usually the stochastic parameters are extrapolated from previous values however this can

frequently cause gross errors. This hinders the accuracy of real time prediction.

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In this problem, it is necessary to apply sampling to ensure that the considered points are representative of the domain. This problem cannot be approached deterministically

- ¹⁵ due to the continuous nature of the parameters making the consideration of every possible quantity. There are numerous methods of sampling available. Monte-Carlo simulation is the simplest. However, due to the time constraints is not suitable for the model development. Another alternative could be importance sampling, which adopts a Monte-Carlo style simulation, but biases the output to favour areas of greater interest,
- for example the tails of the distribution. This however is also inappropriate since the entire distribution is of interest, and it is still relatively expensive. Instead, a Latin Hyper-Cube (LHC) method will be used, where the distribution is separated into block of equal probability and then a random value is chosen from each block. This has the advantage of requiring a smaller amount of necessary simulations to create a good design and here a probability and block. The method will be used and block are simulated by the second design and here a smaller amount of necessary simulations to create a good design and here a simulations is the title block.
- hence is relatively inexpensive. The main disadvantage is that it does not necessarily guarantee a well stratified design (Myers et al., 2009).

A simple 3rd order polynomial regression model is used to map the responses. It was found that lower order models are too sensitive to the fluctuating component present



in the simulation data. This is the same reason which prevents the use of radius basis functions (RBF) in place of a polynomial.

It is also possible that the input variables will possess cross correlation. Therefore mixed variable terms, i.e. x_1x_2 , have to be included in the model.

5 4 Probabilistic assessment of oil spill spread

As previously stated, the underlying physics of an oil spill is very complex. Existing solvers require resolving many of the underlying phenomena. The paper uses a non-intrusive method, whereby the regression model is developed using the results from the solver, and does not require being programmed into the solver itself. There are numerous benefits from this approach. Primarily it is performed to simplify the problem however it also means that the developed methodology can easily be applied to data from any source.

4.1 MEDSLIK II

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Since the transport of oil is of such interest, there has been an effort to develop codes
 which accurately model the spread. One such code is MEDSLIK II. The model solves the advection-diffusion processes using a Lagrangian particle formalism, meaning that the oil slick is broken into a number of constituent particles. While the transformation processes act on the entire oil slick surface. It has been shown to provide accurate results in a number of real scenarios (De Dominicis et al., 2013a; Coppini et al., 2011).
 Results are produced reasonably quickly which is favourable since many simulations

²⁰ Results are produced reasonably quickly which is favourable since many simulati are necessary to apply the regression model.

There are four main inputs required: oil spill data, wind field, sea surface temperature, and structure of sea currents. The frequency of the oceanographic data is an important factor since these can change dramatically in a relatively short period of time. MEDSLIK



Il applies a linear interpolation in time between two subsequent current and wind fields to calculate the current and wind at the model time step.

The test case included with the program is for an oil spill in Algeria. This consisted of 680 tons of crude oil being spilled and validation was carried out to check the accuracy

⁵ of the prediction over a 36 h period. The accuracy was found to be in good agreement with the observed results (De Dominicis et al., 2013a). This model has also been validated for the Lebanon crisis where the predicted oil slick at sea and coastal deposits were in agreement with observations (Coppini et al., 2011).

Additional details regarding the development and validation of MEDSLIK II can be seen in De Dominicis et al. (2013b, a).

4.2 Sampling

To develop the model, it is necessary to sample the chosen variables. This has been done using the Latin-hyper cube technique, which involves splitting the distribution into blocks of equal probability, then a random value is chosen from each block. A brief experiment was conducted and it was determined that a minimum of 6 samples are required to capture a reasonably complex shape, the Weibull distribution. Note however that it is not possible to predict the shape of the resultant graph beforehand however it is expected to be more simple than the test shape. A zero point has also been considered for investigation of simulation noise generated by MEDSLIK II to simulate

turbulence. The variables have also been decoupled by consideration of a point mass oil spill subject to oceanographic conditions. The result was that the destination can be determined by the current and wind velocities, and the size of the spill depends on the initial spill size as well as the spill age, that is time since initial spill.

The distribution for wind speed is widely accepted to be reasonably well represented

by a Weibull distribution with shape and scale parameters 2.26 and 9.02 respectively (de Prada Gil et al., 2012). However it is somewhat more complicated to find a distribution for the current speed as this varies over the globe. Since the pattern is almost entirely that of wind driven circulation, it is likely the same underlying distribution with



varying coefficients based on location. Here, the current velocity for the test case has been analysed and a Weibull distribution superimposed, leading to the coefficients 1.9967 and 0.2132 for shape and scale respectively. This limits the versatility of the developed model since the test case is in the Mediterranean Sea, which is known for its relatively low current velocities. Performing the prediction for a value outside the sam-

⁵ relatively low current velocities. Performing the prediction for a value outside the sampled range is not recommended due to extrapolation errors. Therefore, if one wished to consider a value outside of the sampled range, additional simulations would have to be performed.

The sampled values for wind and current velocities, and the angles can be seen in Table 2. Note that to simplify the required number of simulations, the developed model will displace the spill depending on the angle between the current and wind velocities, with the current velocity treated as an axis, and then translated to meaningful coordinates. Data has been generated from the stated input values for a simulation time of 36 h.

¹⁵ In order to map the responses, a third order polynomial approximation was calculated using the method of least squares. It has been found that the zero point fluctuations from the random walk procedure appear to skew the results disproportionally with lower order models.

For the spill size, a slightly different approach was taken, where the developed equation comes from $r = g(\theta)$, i.e. a radial function is developed, as oppose to a Cartesian. This assists in ensuring a periodic, or near periodic model. Note that both a polynomial and sinusoidal functions were investigated and the polynomial appears to produce less skewed results in the central region and hence the polynomial function was chosen. But as outer rings are of greater interest either choice could be acceptable.

²⁵ Seven values have been sampled for the wind and current magnitudes however only five angles have been considered. This is because the angle refers to the angle between the wind and current velocities, and since the current velocity is used as an axis, symmetry can be applied to reduce the number of necessary values in this parameter.



Therefore five values over a semi-circle are chosen, which corresponds to 8 values over a circle.

4.3 Developed methodology

Once the polynomials have been created, it is necessary to outline the developed methodology for prediction of an oil spill, using the calculated coefficients. The flow chart of the developed model can be seen in Fig. 3. The actual code has been written in the commercial software package MATLAB[®] (2011) and the statistics toolbox is used for the Monte-Carlo simulation to generate the random numbers.

An overview of the methodology is as follows:

- Interpretation of oceanographic data. The key parameters in the prediction are the wind and current velocities. MEDSLIK II produces column structured data for these from the raw NetCDF files. The prediction code is capable of reading these and converting them to block structure and converting from latitude and longitude to metres. A modified version of this code has also been written for the purposes of Monte-Carlo simulation, where the user inputs a desired wind and current velocity directly.
 - Centre of mass. To investigate the behaviour of the centre of mass, the wind, current and angle variables have been considered. A polynomial has been developed which links these variables to predict displacement in the *x* and *y* planes. The oceanic data is interpolated to find the parameters at the spill location and these are fed into the regression model to predict a new centre. Since the current direction is treated as an axis, the displacement with respect to this is first calculated, and then translated into more meaningful coordinates.
 - Reconstruction of surface. Now the centre of mass has been predicted, the surface reconstruction of the oil spill can be considered. Since this is not linked to the destination of the centre of mass, the rings are created around the origin and



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then displaced by the calculated displacement of the centre of mass. If desired, a contour can then be fitted according to these concentration rings. These are 4th order polynomials and require the initial spill size (tons) and the spill age (hours).

 Set values for next iteration. For the next time step, it is necessary to set the new centre of mass for the oil spill. At this stage, the centre of mass can be corrected based on observation to produce more accurate results.

5 Case study

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In order to validate CranSLIK, it is necessary to investigate its performance when applied to oceanographic conditions. Note the model has been verified against the sampled points and over 99.5 % of the oil was captured for each case after 1 h of simulation. It was also found that the prediction becomes less accurate for extended periods. The wind and current velocities were both found to produce near-linear displacement with respect to time, when considered individually. The developed model works by hourly prediction which causes cumulative errors in extended simulation. Hindcast modelling, updating the centre of mass every hour, is therefore recommended to minimise error. The spill size prediction remains very accurate, above 99%, over a 36 h period suggesting that hindcast modelling is not required to be applied to this part of the code.

5.1 Algeria test case

The case considered uses the oceanographic data for the Algeria spill on the 6 August 2008 and a point mass oil spill is released from latitude 38.240° and longitude 5.981°. It is found that the proportion of oil captured becomes poor when a full 36 h prediction is performed, the accuracy rapidly drops after the 4 h mark as shown in Fig. 4. However, under the application of hindcast modelling, where the centre of mass is updated every hour based on model data, the minimum accuracy is greatly improved. This is likely due

to cumulative errors during prediction. These errors could be present in the developed



model, however, since the model has been verified, it may be an error due to the oceanographic data. The model assumes that the oceanographic conditions at the start of the simulation period are representative of the conditions over the period. This however is not necessarily true and therefore the prediction is less accurate when these conditions change greatly over the simulation period. It is possible in this case

these conditions change greatly over the simulation period. It is possible in this case to apply an interpolation since the quantities for the next time step are known however this would not be possible in a real scenario.

Figure 5 shows the displacement error of the centre of mass, when this value is updated at different intervals. It is clear that the error is far smaller when the simulation is only predicting for an hour and then updating.

With regards to the spill size only, the accuracy appears to be very good, as seen in Fig. 6. Compared to the accuracy of the centre of mass prediction, this appears to be far more accurate suggesting that the weakest component of this model is the centre of mass prediction; however the overall accuracy appears to be reasonably good, a minimum of 80 % when hourly prediction is used as seen in Fig. 4. This also justifies the decoupling of variables.

The supplementary animation shows the predicted oil spill (black rings) and the MEDSLIK II result (background contour) for a 36 h simulation period for this test case. The centre of mass for the prediction is updated every hour. The lowest proportion of oil captured is approximately 80 % with the average being about 91 %.

5.2 Sensitivity analysis

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It is also of interest to consider the sensitivity of CranSLIK with respect to the different input parameters. This is summarised in Table 3.

The most sensitive variables appear to be the current magnitude and angle. This is expected since the displacement due to current velocity is far greater than that due to the wind velocity, and since the majority of the oil is contained close to the centre, the dispersed elements do not skew the results significantly and hence there is some leeway with the spill size. This was expected since the current is more displacing than the



wind, and it was concluded the wind is less important when the sensitivity of variables was investigated in MEDSLIK II (De Dominicis et al., 2013a).

5.3 Monte-Carlo simulation

CranSLIK assumes that the wind and current data at the start of the hour are representative of the full hour. This however is not necessarily true since oceanographic conditions may change. Therefore more accurate prediction may be possible if an interpolation is applied to the data and expected fields are created. However this is not relevant for prediction of real-time oil spills. In such scenarios it may be of interest to generate an expected region for the oil spill.

¹⁰ Due to the incredibly low computational cost required by CranSLIK, a Monte-Carlo simulation can be performed in a very low time frame, approximately 1000 simulations per second on an AMD Phenom II X4 3.6 GHz processor. This can be used to generate an expected region for the oil spill and aid in clean up and recovery operations.

For the Algeria test case, the Monte-Carlo simulation was performed using input distributions developed from the available data. However, due to the 60 h period of data, there exists a bimodal peak in the simulation results representative of the alternating current forcing as shown in Fig. 7. This is present when the simulation is performed using 5000 and 10 000 samples also. This result is not too helpful because of the bimodal peak. However, it does demonstrate the versatility and robustness of the developed model. If the distribution for a location is known, more meaningful results can be produced.

5.4 Discussion

Whilst CranSLIK appears to perform well for the tested scenarios, it is necessary to identify the assumptions made while modelling. Firstly, the displacement of the centre of mass is correlated to the wind and current velocities only, while the spill area

is determined by the quantity of oil spilled and the age. Although these variables are



considered dominant, in an fully robust model further simulations considering different variables should be performed. This would lead to an even more accurate prediction, however would require more complicated approximations to account for these variables and their correlations. Secondly, further from MEDSLIK II which was employed, other oil

- ⁵ spill prediction codes and softwares may be used and compared identifying their performance in aspects of accuracy and computational effort and at the same time highlight efficiency of the proposed non-intrusive methodology. Finally, only one particular type of oil spill has been considered: point-mass. Since the developed model moves a centre of mass, and then reconstructs the surface, it is possible to mark several centre of
- ¹⁰ masses and predict their destinations. The problem then becomes surface reconstruction which would require additional simulations. Also, as with any stochastic problem, additional data could lead to a better regression fit and hence better prediction.

5.5 Technical specifications

The oil spill model code CranSLIK v1.0 is available as an open source code that can be downloaded together with test case data and output example from the website http://public.cranfield.ac.uk/e102081/CranSLIK. CranSLIK is available under the GNU General Public License (GNU-GPL Version 3, 29 June 2007). The code is written in the commercial software package MATLAB[®] (2011). The model code can run on any computer and operating system that supports Matlab.

20 6 Conclusions

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This paper describes the development of CranSLIK, a model for the prediction of the destination and spread of an oil spill via a stochastic approach. The key parameters were identified as wind velocity, current velocity, spill size and time, and a design square was created for the required samples. The simulations were then performed using MEDSLIK II and regression modelling was applied to create two equations: one to



predict the centre of mass, and one to predict the spill size. The developed code has been presented and discussed. It was then validated against a real test case. Finally, the efficiency of the model is exploited using Monte-Carlo simulation for the purposes of generating maximum likelihood regions. This has limited use when applied to the 5 Algeria test case due to insufficient data to more accurately fit a distribution.

The developed model appears to perform well when applied to the Algeria test case considered, with a minimum of 80% of the oil captured when using hourly prediction. The major strength of the developed model is the efficiency and the minimal time required to perform Monte-Carlo simulation and generate maximum likelihood regions. However, for this to provide useful results, it is necessary for a distribution or a reasonable estimate of expected oceanographic conditions. This paper serves as a demonstration of an alternative method for fast prediction of the advection-diffusion-

transformation of an oil spill. The assumptions have been discussed and areas for further work highlighted. Whilst the key variables were considered, it has been identi-¹⁵ fied that consideration of additional variables could result in improved accuracy. As with all investigations involving stochastic parameters, additional data samples could also improve the results.

Supplementary material related to this article is available online at http://www.geosci-model-dev-discuss.net/6/7047/2013/ gmdd-6-7047-2013-supplement.zip.

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 Table 1. Spreading laws for oil spills (Fay, 1971).

	0 (/ =)	Axisymmetric (r =)
Viscous k _{1v}	$\Delta gAt^{2})^{1/3} \\ (\Delta gA^{2}t^{3/2}/v^{1/2})^{1/4} \\ \delta^{2}t^{3}/\rho^{2}v)^{1/4}$	$\frac{k_{2i}(\Delta V t^2)^{1/4}}{k_{2v}(\Delta g V^2 t^{3/2} / v^{1/2})^{1/6}}$ $\frac{k_{2v}(\delta^2 t^3 / \rho^2 v)^{1/4}}{k_{2t}(\delta^2 t^3 / \rho^2 v)^{1/4}}$

A = volume of oil per unit length normal to x;

g = acceleration due to gravity;

k = proportionality constants:

 $k_{1i} = k_{1v} = 1.5, k_{1t} = 1.33, k_{2i} = 1.14, k_{2v} = 1.45, k_{2t} = 2.30;$

- / = length of 1-D oil slick;
- *r* = maximum radius of axisymmetric oil slick solubility;

t = time since initiation of spread;

V = volume of oil in axisymmetric spread;

x = dimension of direction in 1-D spread;

 σ = spreading coefficient;

v = kinematic viscosity of water;

 ρ = density of water;

 Δ = ratio of density difference between water and oil to density of water.



Table 2. Sampled	l values for centre	of mass prediction.
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Wind magnitude (in ms ⁻¹)	Current magnitude (in ms ⁻¹)	Angle (in radians)
0	0	0
2.0887	0.0505	$\pi/4$
5.7691	0.1497	π/2
6.1600	0.2488	$3\pi/4$
7.7913	0.3480	π
10.1252	0.4472	_
15.2786	0.5464	-





Table 3. Sensitivity of variables for the first hour of the Algeria scenario. Upper and lower ranges for 90 % accuracy are given.

Variable	Lower limit	Upper limit	Observed
Wind magnitude	-2.0423	9.3860	4.3454
Current magnitude Wind angle	0.0065 -2.5844	0.1130 -0.2280	0.0653 -1.5202
Current angle	-1.7279	-0.6605	-1.4048
Spill size	163.2	NA	680



Fig. 1. Weathering process, from ITOPF (2013).





Fig. 2. Speculative mass balance, from Mackay and McAuliffe (1989).







Fig. 3. Flowchart of the developed model.



Fig. 4. Proportion of oil captured using different update frequencies.

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Interactive Discussion



Fig. 5. Centre of mass prediction using different update frequencies.





Interactive Discussion





Fig. 7. Monte-Carlo simulation of the Algeria test case, 1 h simulation.

