

1 Running title: Radiation of Individual Plants

2 **IPR 1.0: an efficient method for calculating solar radiation**  
3 **absorbed by individual plants in sparse heterogeneous**  
4 **woody plant communities**

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9

10 **Abstract**

11 Climate change may alter the spatial distribution, composition, structure, and functions of  
12 plant communities. Transitional zones between biomes, or ecotones, are particularly sensitive  
13 to climate change. Ecotones are usually heterogeneous with sparse trees. The dynamics of  
14 ecotones are mainly determined by the growth and competition of individual plants in the  
15 communities. Therefore it is necessary to calculate solar radiation absorbed by individual  
16 plants for understanding and predicting their responses to climate change. In this study, we  
17 developed an individual plant radiation model, IPR (version 1.0), to calculate solar radiation  
18 absorbed by individual plants in sparse heterogeneous woody plant communities. The model  
19 is developed based on geometrical optical relationships assuming crowns of woody plants are  
20 rectangular boxes with uniform leaf area density. The model calculates the fractions of sunlit  
21 and shaded leaf classes and the solar radiation absorbed by each class, including direct  
22 radiation from the sun, diffuse radiation from the sky, and scattered radiation from the plant  
23 community. The solar radiation received on the ground is also calculated. We tested the  
24 model by comparing with the analytical solutions of random distributions of plants. The tests  
25 show that the model results are very close to the averages of the random distributions. This  
26 model is efficient in computation, and can be included in vegetation models to simulate long-  
27 term transient responses of plant communities to climate change. The code and a user's  
28 manual are provided as supplements of the paper.

1 **1 Introduction**

2 Climate change is expected to alter the composition (species types and their density), structure  
3 (heights, leaf area, crown size, etc.), and spatial distribution (locations and extents) of  
4 terrestrial ecosystems (Cramer et al., 2001), which directly affect animals' habitats and human  
5 applications of the lands, and have strong feedbacks on the climate system (Parry et al.,  
6 2007). Transitional zones between biomes, or ecotones, are particularly sensitive to climate  
7 change and could provide early signs of climate change impacts (Fankhauser et al., 2001).  
8 Transitional zones are usually heterogeneous with sparse trees, such as the tree-line between  
9 boreal forest and Arctic tundra (The width of the tree-line usually ranges about 100 km  
10 (Timoney et al., 1992)), parklands and savannah. Field observations and remote sensing data  
11 (aerial photos and satellite images) have detected increases in greenness (Xu et al., 2013) and  
12 changes in density and height of trees and shrubs in the transitional zones between boreal  
13 forest and Arctic tundra (Gamache and Payette, 2004; Sturm et al., 2001; Tape et al., 2006).  
14 Relative changes in height, crown size, and the density of trees, shrubs and herbs usually  
15 occur before major shifts in biomes as projected by some vegetation models (e.g., Gamache  
16 and Payette, 2004; Tape et al., 2007; Callaghan et al., 2005). Novel ecosystem types could  
17 appear as well since individual species independently adjust to climate forcing (Overpeck et  
18 al., 2003; Walker et al., 2006). To understand and predict these transient changes, it is  
19 essential to consider light competition among different species in plant communities (the  
20 words "light" and "radiation" are used interchangeably in this paper). In sparsely vegetated  
21 regions, the solar radiation received on the ground is important as well for soil thermal and  
22 hydrological conditions, especially for permafrost conditions in cold regions.

23 Different methods have been developed to calculate solar radiation absorbed by plants. The  
24 major approaches include the one-big-leaf method (considering the whole canopy as one layer  
25 (e.g., Sellers et al., 1992)), the two-big-leaf method (dividing the canopy into sunlit and  
26 shaded leaves (e.g., Norman, 1980; Wang and Leuning, 1998)), using Beer's law to estimate  
27 radiation distribution in canopies assuming canopies are uniform turbid media (Monsi and  
28 Saeki, 1953), and two-stream approximation considering scattering and absorption of down-  
29 welling and up-welling light in canopies (Dickinson, 1983). All these approaches assume that  
30 the canopy is a uniform layer covering the entire study area. More detailed numerical canopy  
31 radiation models have been developed for energy balance and for remote sensing applications  
32 (e.g., Cescatti, 1997; Gastellu-Etchegorry et al., 2004; Kobayashi and Iwabuchi, 2008; Li et

1 al., 1995; Prince, 1987; Myneni et al., 1995; Wang et al., 2007). However, these models are  
2 time consuming in computation and usually do not pay much attention to light competition  
3 among individual plants and species.

4 In the past decade, several models considered the composition of different plant types in plant  
5 communities and their competition for light and other resources (e.g., Foley et al., 1996; Sitch  
6 et al., 2003; Zhang et al., 2002). For example, Sitch et al. (2003) considered the light  
7 competition among plant functional types based on leaf area index of individual plants and  
8 their density, but did not consider the effects of plant heights on light competition. Foley et al.  
9 (1996) assumed that trees are always higher than grasses for light competition. Zhang et al.  
10 (2002) used a similar approach but considered three strata (upper-story, under-story, and  
11 ground-growth). Ryel et al. (1990) simulated light competition in multi-species crop  
12 communities based on the foliage composition of the species in each canopy layer. These  
13 studies considered the vertical structure of the canopies but assumed that the canopy  
14 layers/strata are uniform and cover the entire study area continuously. Several studies  
15 developed three-dimensional models to simulated radiation distribution in sparsely distributed  
16 trees, mainly for fruit orchards (de Castro and Fetcher, 1998; Oyarzun et al., 2007; West and  
17 Welles, 1992; Baldocchi and Collineau, 1994). However, the plant communities considered  
18 are usually composed of only one type of trees. Therefore there is no light competition among  
19 plant species or types. Song and Band (2004) develop a model to simulate the spatial patterns  
20 of solar radiation under forest of discrete crowns. The approach could be improved to  
21 calculate solar radiation received by individual plants.

22 Another issue in vegetation models is their complexity and applicability. Stand-based  
23 vegetation models represent the competition of vegetation types based on average individuals  
24 and the canopy of each vegetation type is assumed continuously distributed (e.g., Foley et al.,  
25 1996; Sitch et al., 2003; Zhang et al., 2002). Such simplification significantly reduced the  
26 requirement of input data and computation cost, and the models can be used for large areas  
27 spatially explicitly. On the other hand, individual-based vegetation models consider the  
28 competition of individual plants (e.g., Sato et al., 2007). Explicit ray tracing methods can also  
29 be used to calculate the light interception of individual plants (e.g., Kobayashi and Iwabuchi,  
30 2008). Such models are useful for process understanding. However their input data  
31 requirement and computation cost are high and these models are difficult to cover large areas  
32 at high spatial resolution.

1 In this study, we develop an individual plant radiation model, IPR (version 1.0), based on  
2 geometrical optical relationships. It is an efficient method to calculate the solar radiation  
3 absorbed by average individual plants in sparse heterogeneous woody plant communities (i.e.,  
4 the canopy is discontinuous and composed of different plant types or the same type but with  
5 different heights). Solar radiation under the woody plants is calculated as well. This model  
6 may be useful to improve the accuracy of light competition among different vegetation types  
7 in stand-based vegetation models. In the paper, we first described the assumptions and the  
8 algorithms of the model. Then we tested the model by comparing with the results of the  
9 random approach and the two-big-leaf method, and by sensitivity analysis. Some important  
10 features and limitations of the model were highlighted in the discussion section.

## 11 **2 Methodology**

### 12 **2.1 The assumptions of the model**

13 Natural plant communities, especially in northern high latitudes, are usually composed of  
14 trees, shrubs, herbs, mosses and lichens. To simplify the calculation, the IPR model was  
15 developed based on the following seven assumptions for plant communities and three  
16 assumptions for radiation conditions: 1) the plant community may include woody plants (trees  
17 and shrubs), herbs, and mosses/lichens in a large flat area (the area is so large that the margin  
18 effects can be ignored); 2) woody plants are higher than herbs, and herbs are higher than  
19 mosses/lichens; 3) woody plants can be categorized into several strata based on their heights  
20 and crown sizes, which can be different species or one species but in different ages; 4) the  
21 plants of each woody stratum are distributed somewhat regularly (equivalent to the average of  
22 random distributions), mixed with plants of other woody strata and are trying to avoid  
23 overlapping with one another (Ward et al., 1996); 5) the herb stratum is distributed uniformly,  
24 and is treated collectively without considering individual plants; 6) mosses/lichens cover the  
25 entire ground or cover part of the ground randomly; 7) the crowns of woody plants are treated  
26 as rectangular boxes, and the leaf area density is distributed uniformly within a box; 8) the  
27 sky diffuse radiation is from the whole hemisphere and is in isotropic distribution, as used by  
28 Goudriaan (1977); 9) scattered radiation generated from reflection and transmission in  
29 canopies is in all directions, and the recollision probability remains constant in successive  
30 scattering (Panferov et al., 2001; Smolander and Stenberg, 2005); and 10) both the sky diffuse  
31 radiation and the scattered radiation are uniformly distributed in a crown.

1 There are several reasons for the treatment of crowns as somewhat regularly distributed but  
2 not exactly regular (the assumption 4). First, plants tend to be distributed somewhat regularly  
3 because of the competition (Ward et al., 1996); second, although plants of one stratum can be  
4 distributed regularly based on geometry assuming equal spacing among nearest plants (e.g., at  
5 centers and nodes of hexagons), it is difficult to distribute plants of two or more strata without  
6 overlapping among plants of different strata; and third, the fractions of sunlit leaf area can be  
7 different between the average of random distribution and exact regular distribution. Crowns  
8 of woody plants can be in different shapes depending on the genetic features of the species  
9 and the environment. To simplify the calculation, we treated crowns as rectangular boxes.  
10 Oyarzun et al. (2007) also treated fruit-tree crowns as prisms in orchards. However, their  
11 prism-shaped crowns are always aligned with the rows of the plants in an orchard, while we  
12 assumed that a crown looks like a rectangular box (or looks like a rectangle with the same  
13 optical length) in all azimuth directions and there is always a side facing the sun considering  
14 that crowns are usually symmetrical. Crowns, especially when they are large and dense,  
15 usually have much less leaves in the centre of the crown, thus the optical length crossing the  
16 crown horizontally is not proportional to its geometric length. More importantly, this  
17 simplified treatment of the crowns allows quasi-analytical solutions and greatly improves the  
18 efficiency and precision of the calculation.

19 Based on this rectangular box assumption, the leaf area density of a crown can be expressed  
20 as

$$21 \quad \rho = L_0 / [D^2(H - h)], \quad (1)$$

22 where  $\rho$  is the leaf area density of the crown ( $\text{m}^2$  leaf/ $\text{m}^3$  space),  $L_0$  is the leaf area of the  
23 crown ( $\text{m}^2$  leaf/plant), or expressed as  $L_0 = LAI_p \cdot D^2$ .  $LAI_p$  is the local leaf area index of the  
24 individual crown, defined as the ratio between the leaf area of the crown and the ground area  
25 directly projected under the crown ( $\text{m}^2$  leaf/ $\text{m}^2$  land).  $D$  is the width of the crown (m),  $H$  and  $h$   
26 are the heights (m) of the top and bottom of the crown, respectively.

## 27 **2.2 The algorithms of the model**

28 Solar radiation absorbed by leaves includes direct solar radiation (or solar beam), diffuse  
29 radiation from the sky (or simply called diffuse radiation), and scattered radiation which is  
30 defined as the radiation generated by reflection and transmission of direct and diffuse  
31 radiation intercepted by leaves. Because the solar radiation intercepted by sunlit leaves is

1 much higher than that of the shaded leaves, an efficient way to up-scale photosynthesis from  
2 leaves to canopy is to divide the canopy into sunlit and shaded leaf classes (Norman, 1993).  
3 Therefore, we calculated the fractions of sunlit and shaded leaf classes of individual plants  
4 and the solar radiation absorbed for each class based on geometric optical relationships. Sunlit  
5 leaves and sunlit ground receive solar beam, diffuse radiation and scattered radiation, while  
6 shaded leaves and shaded ground receive only diffuse radiation and scattered radiation. The  
7 radiation on the ground is considered as the radiation available for mosses and lichens.

8 The following sections describe the detailed algorithms of the IPR model. Section 2.2.1 first  
9 calculates the fractions of sunlit leaf area for the woody strata. This is the core of the IPR  
10 model. Diffuse radiation can be considered as isotropic beams from all the directions of the  
11 hemisphere, therefore the relative diffuse radiation can be calculated by integration of the  
12 sunlit fractions from different directions of the hemisphere. Section 2.2.2 calculates the  
13 fraction of sunlit leaf area and the relative diffuse radiation for the herb stratum. Since the  
14 herb stratum is assumed a uniform layer, the two-big-leaf method (Norman, 1982) can be  
15 used. After the interception of the woody and the herb strata, the fraction of sunlit area and  
16 the relative diffuse radiation on the ground can be determined (Section 2.2.3). Section 2.2.4  
17 calculates the intensity of the direct and diffuse radiation intercepted by the woody and herb  
18 strata and the ground. Sections 2.2.5 estimates the scattered radiation absorbed by the woody  
19 and the herb strata and the ground. And section 2.2.6 sums up the direct, diffuse and scattered  
20 radiation for sunlit and shaded leaves of the woody and herb strata and the ground.

## 21 **2.2.1 The fractions of sunlit leaf area and the relative diffuse radiation of** 22 **the woody strata**

23 When a solar beam goes through a small column of plant canopy (Fig. 1), the sunlit leaf area  
24 can be estimated based on Norman (1982)

$$25 \quad dL_b = F_l / K [1 - \exp(-K \cdot \rho \cdot l)] dA, \quad (2)$$

26 where  $dL_b$  is the sunlit leaf area of the column ( $\text{m}^2$  leaf),  $dA$  (in  $\text{m}^2$ ) is the area of the column  
27 directly facing the beam, and  $F_l$  is the solar beam before entering the column, expressed as  
28 the fraction of sunlit area on a surface.  $l$  is the length of the column or the path length of light  
29 (m), and  $\rho$  is the density of the leaf area of the column ( $\text{m}^2$  leaf/ $\text{m}^3$  space), which can be  
30 calculated by Eq. (1).  $K$  is effective light extinction coefficient including the clumping effects

$$31 \quad K = K_0 \cdot \Omega, \quad (3)$$

1 where  $K_0$  is the light extinction coefficient when leaves are randomly distributed, and is a  
 2 constant of 0.5 (Norman, 1982).  $\Omega$  is the clumping index of the leaves in the crown (Chen and  
 3 Black, 1992). The solar beam after the interception of the canopy can be determined based on  
 4 the Beer-Lambert law

$$5 \quad F_2 = F_1 \cdot \exp(-K \cdot \rho \cdot l), \quad (4)$$

6 where  $F_2$  is the solar beam after the interception of the canopy, expressed as the fraction of  
 7 sunlit area on a surface. The solar beam intercepted by the column of canopy would be

$$8 \quad dF = F_1 - F_2 = F_1[1 - \exp(-K \cdot \rho \cdot l)], \quad (5)$$

9 where  $dF$  is the solar beam intercepted by the column of canopy (in the same unit as  $F_1$  and  
 10  $F_2$ ). The shading effects of this column on subsequent objects can be expressed as

$$11 \quad f = F_2/F_1 = \exp(-K \cdot \rho \cdot l), \quad (6)$$

12 where  $f$  is the shading effects of the column on subsequent objects (in fractions ranged from 0  
 13 to 1.  $f = 1$  for no shading, and  $f = 0$  for completely shaded).

14 For a plant at any moment, the total sunlit leaf area of the crown is the integration of  $dL_b$  for  
 15 the entire crown. For rectangular box shaped crowns, we can integrate numerically by  
 16 dividing the crown into small slices parallel to the solar beam (Fig. 2a). The length of a slice  
 17 or the light path length (equivalent to  $l$  in Eq. (2)) can be calculated analytically based on the  
 18 height of the slice when the beam enters it (Fig. 2). There are two cases: When  $\tan\theta \leq (H_i -$   
 19  $h_i)/D_i$  (Fig. 2b)

$$20 \quad l_{zi} = \begin{cases} 0 & (z_i \leq h_i \text{ or } z_i \geq H_i + D_i \cdot \tan\theta) \\ (z_i - h_i)/\sin\theta & (D_i \cdot \tan\theta + h_i \geq z_i > h_i) \\ D_i/\cos\theta & (H_i \geq z_i > D_i \cdot \tan\theta + h_i) \\ D_i/\cos\theta - (z_i - H_i)/\sin\theta & (H_i + D_i \cdot \tan\theta > z_i > H_i) \end{cases}, \quad (7a)$$

21 and when  $\tan\theta > (H_i - h_i)/D_i$  (Fig. 2c)

$$22 \quad l_{zi} = \begin{cases} 0 & (z_i \leq h_i \text{ or } z_i \geq H_i + D_i \cdot \tan\theta) \\ (z_i - h_i)/\sin\theta & (H_i \geq z_i > h_i) \\ (H_i - h_i)/\sin\theta & (h_i + D_i \cdot \tan\theta \geq z_i > H_i) \\ D_i/\cos\theta - (z_i - H_i)/\sin\theta & (H_i + D_i \cdot \tan\theta > z_i > h_i + D_i \cdot \tan\theta) \end{cases}, \quad (7b)$$

23 where  $l_{zi}$  is the path length of light going through a slice of crown of a plant of stratum  $i$ .  $z_i$  is  
 24 the height when the solar beam enters the crown slice, and  $dz_i$  is the thickness of the crown

1 slice in vertical direction (m) (Fig. 2a). The cross-section area of the crown slice directly  
 2 facing the solar beam can be expressed as

$$3 \quad dA_i = D_i \cdot \cos \theta \cdot dz_i, \quad (8)$$

4 where  $dA_i$  is the area of the crown slice directly facing the solar beam (equivalent to  $dA$  in Eq.  
 5 (2)).  $\theta$  is the elevation angle of the sun.  $D_i$  is the width of the crown (m),  $H_i$  and  $h_i$  are the  
 6 heights of the top and bottom of the crown, respectively (m) (the subscript  $i$  is for a plant of  
 7 stratum  $i$ , or sometimes simply called plant  $i$ ).

8 Some of the solar beam may be blocked by its neighbouring plants. For a stratum  $j$ , only the  
 9 plants growing in a stripe of  $D_i+D_j$  wide in the direction of the sun can shade plant  $i$  (Fig. 3).  
 10 Their shading effects can be estimated by dividing the land stripe into  $D_j$  by  $D_i+D_j$  rectangles  
 11 (except the first rectangle close to plant  $i$ , whose width is defined by Eq. (14)) to calculate the  
 12 shading effects of the plants of stratum  $j$  in each rectangle (Fig. 3)

$$13 \quad f_{i,jk} = (1 - p_j) + p_j \cdot f_{0i,jk}, \quad (9)$$

14 where  $f_{i,jk}$  is the average shading effects on a slice of crown of plant  $i$  by the plants of stratum  $j$   
 15 in rectangle  $k$  shown in Fig. 3. It is the weighted sum of the solar beam from the gaps (no  
 16 shading) and the solar beam going through the crowns of plants of stratum  $j$ .  $f_{0i,jk}$  is the  
 17 shading effects on a slice of crown of plant  $i$  by a crown of plant  $j$  in rectangle  $k$ .  $p_j$  is the  
 18 probability of solar beam going through crowns of stratum  $j$  in the rectangle. It equals to the  
 19 fraction of the land area covered by the crowns of the plants of the stratum (therefore it did  
 20 not change with  $i$  and  $k$ ), and can be calculated as

$$21 \quad p_j = D_j^2 \cdot d_j, \quad (10)$$

22 where  $d_j$  is the density of plants of stratum  $j$  (plants/m<sup>2</sup>). Since the width of the rectangle is  $D_j$ ,  
 23 there is only one row of plants of stratum  $j$  in a rectangle (i.e., the solar beam goes through no  
 24 more than one crown of stratum  $j$  in a rectangle). Therefore  $f_{0i,jk}$  can be calculated based on  
 25 Eq. (6) for a slice of crown

$$26 \quad f_{0i,jk} = \exp(-K_j \cdot \rho_j \cdot l_{zj,k}), \quad (11)$$

27 where  $K_j$  is the effective light extinction coefficient for plant  $j$ ,  $l_{zj,k}$  is calculated by Eq. (7) but  
 28 for plants of stratum  $j$  in rectangle  $k$  corresponding to the height  $z_{j,k}$ , which depends on the  
 29 distance between the plant  $i$  and plants of stratum  $j$  in rectangle  $k$  (Fig. 3)



1  $z_{j,k} = z_i + X_{i,jk} \cdot \tan \theta,$  (12)

2 where

3  $X_{i,jk} = X_{i,j1} + (k-1)D_j,$  (13)

4 and

5  $X_{i,j1} = [0.5(1 - E_{Tj}) + E_{ij}]D_j.$  (14)

6 Where  $X_{i,jk}$  is the distance between the edge of the crown of plant  $i$  and the farther edge of the  
 7 crown of plant  $j$  in rectangle  $k$ , and  $X_{i,j1}$  is the distance when  $k$  equals 1 (the first rectangle  
 8 near plant  $i$ . Figure 3).  $E_{ij}$  is the fraction of crown of plant  $i$  overlapped vertically with the  
 9 crown of plant  $j$ , and  $E_{Tj}$  is the total fraction of the crowns of all the plant strata overlapped  
 10 with a crown of stratum  $j$  on average, calculated as

11  $E_{Tj} = \sum_{m=1}^N p_m \cdot E_{jm},$  (15)

12 where  $N$  is the total number of woody strata of the plant community.  $E_{jm}$  is the fraction of  
 13 crown of plant  $j$  overlapped vertically with the crown of plant  $m$ , defined as

14  $E_{jm} = \begin{cases} 0 & (h_m \geq H_j \text{ or } H_m \leq h_j) \\ \left[ \min(H_j, H_m) - h_m \right] / (H_j - h_j) & (H_j \geq h_m \geq h_j) \\ \left[ H_m - \max(h_j, h_m) \right] / (H_j - h_j) & (H_j \geq H_m \geq h_j) \end{cases},$  (16)

15 where  $\min()$  and  $\max()$  are operations to get the minimum and the maximum of the variables  
 16 in the brackets, respectively. Since  $E_{jm}$  is calculated relative to the crown height of plant  $j$ , it  
 17 can be different from  $E_{mj}$ . Similar to  $E_{mj}$ ,  $E_{ij}$  is the fraction of crown of plant  $i$  overlapped  
 18 vertically with the crown of plant  $j$ . Equation (14) was designed that way so that  $X_{i,j1}$   
 19 approximately equals  $D_j$  (plant  $j$  is very close to plant  $i$ ) when the woody plants are dense ( $E_{Tj}$   
 20  $\approx 1$ );  $X_{i,j1}$  is about  $1.5D_j$  when the woody plants are sparse ( $E_{Tj} \approx 0$ ); and  $X_{i,j1}$  can be less than  
 21  $0.5D_j$  when stratum  $j$  is completely above or below stratum  $i$  ( $E_{ij} = 0$ ), especially when the  
 22 woody plants are dense ( $E_{Tj} \approx 1$ ).

23 The shading effects on a slice of crown by all the neighbouring plants of stratum  $j$  can be  
 24 expressed as

25  $F_{1,ij} = \prod_{k=1}^{Mj} f_{i,jk},$  (17)

1 where  $\Pi$  is for multiplying all the terms for  $k$  ranging from 1 to  $M_j$ . The shading effects on a  
 2 slice of crown by all the neighbouring plants of all the strata can be expressed as

$$3 \quad F_{1,i} = \prod_{j=1}^N F_{1,ij} = \prod_{j=1}^N \prod_{k=1}^{M_j} f_{i,jk}, \quad (18)$$

4 where  $F_{1,i}$  is the shading effects on a slice of crown  $i$  by all the neighbouring plants of all the  
 5 strata, or the fraction of direction radiation available for entering the slice of the crown of  
 6 plant  $i$  after the interception of all its neighbouring plants.  $M_j$  is the total number of rectangles  
 7 considered in calculating the shading effects of stratum  $j$  on plant  $i$ . It can be estimated by

$$8 \quad M_j = 1 + (X_{\max} - X_{i,j1} - D_i)/D_j, \quad (19)$$

9 where  $X_{\max}$  is a predefined maximum distance for shading effects (e.g., 100 m) beyond that  
 10 the shading effects of neighbouring plants are negligible. The total sunlit leaf area of the  
 11 crown  $i$  is the integration of Eq. (2) for all the slices of the crown (using Eq. (8) for  $dA$  and  
 12 Eq. (18) for  $F_l$  and integrating  $dz_i$  from  $h_i$  to  $H_i + D_i \cdot \tan \theta$ )

$$13 \quad L_{bi} = D_i \cdot \cos \theta / K_i \int_{h_i}^{H_i + D_i \cdot \tan \theta} [1 - \exp(-K_i \cdot \rho_i \cdot l_{zi})] \cdot \prod_{j=1}^N \prod_{k=1}^{M_j} f_{i,jk} \cdot dz_i, \quad (20)$$

14 where  $L_{bi}$  is the total sunlit leaf area of the plant  $i$  ( $\text{m}^2$  leaf/plant) when the elevation of the sun  
 15 is  $\theta$ .  $K_i$  is the effective light extinction coefficient of plant  $i$ . The fraction of sunlit leaf area  
 16 would be

$$17 \quad f_{\text{sunlit},i} = L_{bi} / L_{0i}, \quad (21)$$

18 where  $f_{\text{sunlit},i}$  is the fraction of sunlit leaf area of a plant of stratum  $i$ .  $L_{0i}$  ( $\text{m}^2$  leaf/plant) is the  
 19 total leaf area of a plant of stratum  $i$ .

20 The fraction of the sunlit area on a horizontal surface after the interception of all the woody  
 21 strata,  $F_{2w}$ , can be estimated by

$$22 \quad F_{2w} = 1 - \sum_{i=1}^N L_{bi} \cdot d_i \cdot K_i / \sin \theta. \quad (22)$$

23  $F_{2w}$  would be the solar beam available for the herb stratum under the woody strata, expressed  
 24 as the fraction of the sunlit area.

25 We assume that diffuse radiation is from the entire hemisphere and is in isotropic distribution,  
 26 and diffuse radiation is uniformly distributed within a crown. Thus, diffuse radiation

1 intercepted by a crown can be calculated by integration of the sunlit fractions from different  
 2 directions of the hemisphere. Since we assume that the intensity of diffuse radiation is the  
 3 same in all directions, the integration will be the average of the sunlit fractions for the  
 4 elevation angles from 0 to  $\pi/2$

$$5 \quad F_{d,i} = 2/\pi \int_0^{\pi/2} f_{sunlit,i}(\beta) d\beta, \quad (23)$$

6 where  $F_{d,i}$  is the relative diffuse radiation intercepted by the leaves of stratum  $i$ , expressed as  
 7 the ratio to the diffuse radiation above the canopy of the plant community.  $f_{sunlit,i}(\beta)$  is the  
 8 fraction of sunlit leaf area of the crown  $i$  when the elevation angle of the beam is  $\beta$ , calculated  
 9 by Eq. (21).

### 10 **2.2.2 The fraction of sunlit leaf area and the relative diffuse radiation of** 11 **the herb stratum**

12 We assume that the herb stratum is distributed uniformly; therefore its fraction of sunlit leaf  
 13 area can be calculated using the two-big-leaf method (Norman, 1982)

$$14 \quad f_{sunlit,h} = F_{2w} \cdot \sin \theta / (K_h \cdot LAI_h) [1 - \exp(-K_h \cdot LAI_h / \sin \theta)], \quad (24)$$

15 where  $f_{sunlit,h}$  is the fraction of the sunlit leaf area of the herb stratum,  $LAI_h$  is the leaf area  
 16 index of the herb stratum ( $\text{m}^2 \text{ leaf}/\text{m}^2 \text{ ground}$ ),  $K_h$  is the effective light extinction coefficient  
 17 of the herb canopy, and  $F_{2w}$  is the solar beam available after the interception of the woody  
 18 strata, calculated by Eq. (22).

19 Similar to Eq. (23), the relative diffuse radiation intercepted by the herb stratum can be  
 20 calculated as the average of the sunlit fractions for all the elevation angles from 0 to  $\pi/2$

$$21 \quad F_{d,h} = 2/\pi \int_0^{\pi/2} f_{sunlit,h}(\beta) d\beta, \quad (25)$$

22 where  $F_{d,h}$  is the relative diffuse radiation intercepted by leaves of the herb stratum, expressed  
 23 as the ratio to the diffuse radiation above the canopy of the plant community.

### 24 **2.2.3 The fraction of sunlit area and the relative diffuse radiation on the** 25 **ground**

26 Since the herb stratum is assumed a uniform canopy, its effects on the fraction of sunlit area  
 27 on the ground can be expressed based on Beer's law (Monsi and Saeki, 1953)

$$f_{sunlit, g} = F_{2w} \exp(-K_h \cdot LAI_h / \sin \theta), \quad (26)$$

where  $f_{sunlit, g}$  is the fraction of sunlit area on the ground below the herb stratum. The exponential multiplier is the fraction intercepted by the herb stratum.

Similar to Eq. (23), the relative diffuse radiation on the ground can be estimated by the average of  $f_{sunlit, g}$  for all the elevation angles from 0 to  $\pi/2$

$$F_{d, g} = 2/\pi \int_0^{\pi/2} f_{sunlit, g}(\beta) d\beta, \quad (27)$$

where  $F_{d, g}$  is the relative diffuse radiation on the ground, expressed as the ratio to the diffuse radiation above the canopy of the plant community.

#### 2.2.4 Direct and diffuse radiation intercepted by plants and the ground

The direct radiation intercepted by sunlit leaves can be expressed as

$$I_{b, i} = I_{b0} \cdot K_i / \sin \theta, \quad (28)$$

$$I_{b, h} = I_{b0} \cdot K_h / \sin \theta, \quad (29)$$

where  $I_{b, i}$  and  $I_{b, h}$  are the direct radiation intercepted by sunlit leaves of the woody plant  $i$  and the herb stratum, respectively ( $\text{W}/\text{m}^2$  leaf),  $I_{b0}$  is the direct radiation on a horizontal surface above the canopy of the plant community ( $\text{W}/\text{m}^2$  ground). The diffuse radiation intercepted by leaves can be calculated by

$$I_{d, i} = I_{d0} \cdot F_{d, i}, \quad (30)$$

$$I_{d, h} = I_{d0} \cdot F_{d, h}, \quad (31)$$

where  $I_{d, i}$  and  $I_{d, h}$  are diffuse radiation intercepted by leaves of woody plant  $i$  and the herb stratum, respectively ( $\text{W}/\text{m}^2$  leaf).  $I_{d0}$  is the diffuse radiation above the canopy of the plant community ( $\text{W}/\text{m}^2$  ground).

The direct radiation in the sunlit area on the ground equals  $I_{b0}$ , and the diffuse radiation on the ground,  $I_{d, g}$ , would be  $I_{d0} \cdot F_{d, g}$  ( $F_{d, g}$  is calculated by Eq. (27)).

#### 2.2.5 Scattered radiation absorbed by the woody and herb strata and the ground

The scattered radiation received by a woody plant includes scattered radiation generated by its own crown and the scattered radiation from surrounding plants, the latter part usually is very

1 small so we omitted it in the model. The scattered radiation absorbed by a unit leaf area can  
 2 be estimated based on Smolander and Stenberg (2005)

$$3 \quad I_{s1,i} = I_{s0,i} \cdot \alpha_i \cdot r_i / [1 - (1 - \alpha_i)r_i], \quad (32)$$

4 where  $I_{s1,i}$  is the average scattered radiation absorbed by a unit leaf area of plant  $i$  ( $\text{W}/\text{m}^2$  leaf).  
 5  $\alpha_i$  is the light absorption coefficient of the leaves of plant  $i$ .  $I_{s0,i}$  is the average scattered  
 6 radiation ( $\text{W}/\text{m}^2$  leaf, averaged for all the leaves in the crown) generated by reflection and  
 7 transmission when direct and diffuse radiation are first intercepted by leaves of plant  $i$  (zero  
 8 order scattering), and  $r_i$  is the recollision probability of scattered radiation, which is assumed  
 9 remaining constant in successive scattering (Smolander and Stenberg, 2005).  $I_{s0,i}$  and  $r_i$  can be  
 10 estimated by

$$11 \quad I_{s0,i} = (1 - \alpha_i)[I_{b,i} \cdot f_{sunlit,i} + I_{d,i}], \quad (33)$$

$$12 \quad r_i = 1 - \exp(-K_i \cdot \rho_i \cdot l_{ai}), \quad (34)$$

13 where  $l_{ai}$  is the average path length from a light source within the crown to outside of the  
 14 crown, approximated as the average length from the centre of the crown to the six sides of the  
 15 rectangular box

$$16 \quad l_{ai} = (H_i - h_i)/6 + D_i/3. \quad (35)$$

17 The scattered radiation received by the herb stratum includes the scattered radiation from the  
 18 above woody strata and the scattered radiation generated within the herb canopy. On the top  
 19 of the herb stratum, the scattered radiation from the above woody plants can be estimated as  
 20 the difference between the scattered radiation generated by the woody plants and the amount  
 21 of scattered radiation absorbed by the woody plants

$$22 \quad I_{s1,h} = 0.5 \sum_{i=1}^M (I_{s0,i} - I_{s1,i}) \cdot L_{0i} \cdot d_i, \quad (36)$$

23 where  $I_{s1,h}$  is the average scattered radiation from the woody plants on a horizontal surface  
 24 above the herb stratum ( $\text{W}/\text{m}^2$  ground). A factor of 0.5 was used in the equation because a  
 25 horizontal surface below the woody crowns can only receive the downward scattered  
 26 radiation (half of the total scattered radiation) from the woody strata. The average scattered  
 27 radiation generated within the herb canopy can be estimated by

$$28 \quad I_{s0,h} = (1 - \alpha_h)[I_{b,h} \cdot f_{sunlit,h} + I_{d,h}], \quad (37)$$

1 where  $I_{s0,h}$  is the average scattered radiation generated by reflection and transmission when  
 2 direct and diffuse radiation are first intercepted by leaves of the herb stratum ( $\text{W/m}^2$  leaf), and  
 3  $\alpha_h$  is the light absorption coefficient of the herb stratum. The scattered radiation received by  
 4 the herb leaves are the sum of the scattered radiation from above woody plants and the  
 5 scattered radiation generated within the herb canopy. The former can be estimated similar to  
 6 the estimation for diffuse radiation, while the latter can be estimated similar to Eq. (32)

$$7 \quad I_{s,h} = \alpha_h \cdot I_{s1,h} \cdot F_{d0,h} + I_{s0,h} \cdot \alpha_h \cdot r_h / [1 - (1 - \alpha_h)r_h], \quad (38)$$

8 Where  $I_{s,h}$  is the average scattered radiation absorbed by leaves of the herb stratum ( $\text{W/m}^2$   
 9 leaf).  $F_{d0,h}$  is the relative diffuse radiation for herb stratum when there is no woody stratum,  
 10 calculated by Eq. (25) but with  $F_{2w} = 1$  for  $f_{sunlit,h}$  estimation in Eq. (24).  $r_h$  is the recollision  
 11 probability of scattering radiation in the herb canopy, and can be estimated based on  
 12 Smolander and Stenberg (2005)

$$13 \quad r_h = 0.88[1 - \exp(-0.7 \cdot LAI_h^{0.75})]. \quad (39)$$

14 Similarly, the scattered radiation received on the ground,  $I_{s,g}$ , can be estimated by

$$15 \quad I_{s,g} = I_{s1,h} \cdot F_{d0,g} + 0.5I_{s0,h} \cdot \exp(-0.5K_h \cdot LAI_h), \quad (40)$$

16 where  $F_{d0,g}$  is the relative diffuse radiation on the ground when there is no woody stratum,  
 17 calculated by Eq. (27) but with  $F_{2w} = 1$  for  $f_{sunlit,g}$  estimation in Eq. (26). The factor 0.5 is used  
 18 because only half of the scattered radiation reaching the ground (the other half scatters to the  
 19 sky from the top of the herb stratum).

## 20 **2.2.6 Solar radiation absorbed by sunlit and shaded leaves and the** 21 **ground**

22 The sunlit leaves receive direct radiation from the sun, diffuse radiation from the sky, and  
 23 scattered radiation, while the shaded leaves receive only diffuse radiation from the sky and  
 24 scattered radiation. Therefore the total solar radiation absorbed by sunlit and shaded leaves  
 25 would be

$$26 \quad I_{sunlit,i} = \alpha_i(I_{b,i} + I_{d,i}) + I_{s1,i}, \quad (41)$$

$$27 \quad I_{shaded,i} = \alpha_i \cdot I_{d,i} + I_{s1,i}, \quad (42)$$

$$28 \quad I_{sunlit,h} = \alpha_h(I_{b,h} + I_{d,h}) + I_{s,h}, \quad (43)$$

$$1 \quad I_{shaded,h} = \alpha_h \cdot I_{d,h} + I_{s,h}, \quad (44)$$

2 where  $I_{sunlit,i}$  and  $I_{shaded,i}$  are the total solar radiation ( $\text{W}/\text{m}^2$  leaf) absorbed by sunlit and shaded  
3 leaves of the woody stratum  $i$ , respectively, and  $I_{sunlit,h}$  and  $I_{shaded,h}$  are the total solar radiation  
4 ( $\text{W}/\text{m}^2$  leaf) absorbed by sunlit and shaded leaves of the herb stratum, respectively. For the  
5 ground, the total radiation absorbed on sunlit and shaded areas can be expressed as

$$6 \quad I_{sunlit,g} = \alpha_g (I_{b0} + I_{d,g} + I_{s,g}), \quad (45)$$

$$7 \quad I_{shaded,g} = \alpha_g (I_{d,g} + I_{s,g}), \quad (46)$$

8 where  $I_{sunlit,g}$  and  $I_{shaded,g}$  are the total solar radiation ( $\text{W}/\text{m}^2$  ground) absorbed by sunlit and  
9 shaded areas of the ground, respectively.  $\alpha_g$  is the light absorption coefficient of the ground  
10 (the albedo of the ground would be  $1 - \alpha_g$ ). The average solar radiation absorbed on the ground  
11 would be

$$12 \quad I_{avg,g} = I_{sunlit,g} \cdot f_{sunlit,g} + I_{shaded,g} \cdot (1 - f_{sunlit,g})$$

$$13 \quad = \alpha_g (I_{b0} \cdot f_{sunlit,g} + I_{d,g} + I_{s,g}), \quad (47)$$

14 where  $I_{avg,g}$  is the average solar radiation absorbed on the ground ( $\text{W}/\text{m}^2$  ground). Part of the  
15 solar radiation received on the ground will be reflected. In this study we did not consider the  
16 contribution of this reflected radiation to the leaves.

### 17 **2.3 Inputs and outputs of the model and calculation procedure**

18 The inputs for the IPR model include plant community features and the radiation conditions  
19 above the plant community. The plant community features include the number of woody plant  
20 strata ( $N$ ), the features of each woody stratum (plant density ( $d_i$ ), heights of the top and the  
21 bottom of the crown ( $H_i$ , and  $h_i$ , respectively), crown width ( $D_i$ ), leaf area of the crown ( $L_{oi}$ ),  
22 light absorption coefficient ( $\alpha_i$ ), and the clumping index of the leaves ( $\Omega_i$ ), and the features of  
23 the herb stratum (leaf area index ( $LAI_h$ ), light absorption coefficient ( $\alpha_h$ ), and the clumping  
24 index ( $\Omega_h$ )). The radiation conditions above the plant canopy include the elevation angle of  
25 the sun ( $\theta$ ), and direct and diffuse radiation on a horizontal surface above the plant  
26 community at the time ( $I_{b0}$  and  $I_{d0}$ , respectively). There are two computing parameters: The  
27 maximum distance for shading effects ( $X_{max}$ ) and the integration interval ( $dz_i$ ). One hundred  
28 meters for  $X_{max}$  is large enough, and  $dz_i$  can be defined as  $0.01(H_i - h_i)$ .

1 The outputs of the model include the fractions of the sunlit leaf area for each woody stratum  
2 and the herb stratum, and the fraction of sunlit area on the ground, the radiation of the sunlit  
3 and shaded leaf classes of each woody stratum and the herb stratum, and the radiation on  
4 sunlit and shaded areas on the ground, and the average radiation on the ground. The code for  
5 calculating the diurnal variations of the radiation conditions and a user's manual of the model  
6 can be found in the supplements.

7 The IPR model first calculates the fraction of the sunlit leaf area for each elevation angle from  
8 0 to  $\pi/2$  with a small step (e.g.,  $\pi/36$ , or 18 steps). The relative diffuse radiation for each  
9 stratum and on the ground can be calculated by numerically integrating the above results with  
10 the elevation angle. The fraction of sunlit leaf area of each stratum can be interpolated from  
11 the above calculation based on the elevation of the sun at the time. Then the solar radiation  
12 absorbed by a plant of each stratum and on the ground can be calculated based on the direct  
13 and diffuse radiation above the plant community at the times.

## 14 **2.4 Testing of the model**

### 15 **2.4.1 Comparing with the fraction of sunlit leaf area calculated by the** 16 **random approach**

17 In IPR, the calculation of solar radiation for herb stratum is based on Norman (1982), which  
18 has been tested and used widely. Diffuse radiation is calculated in a similar way as for direct  
19 radiation but the beams are from the entire hemisphere. Therefore the core of the IPR model is  
20 the calculation of the fraction of sunlit leaf area of individual plants of woody strata. Detailed  
21 field measurements are not available for model test. However, we can test the model by  
22 numerically tracing light beams to calculate sunlit leaf area assuming plants are randomly  
23 distributed (abbreviated as the random approach). Following is the description of the random  
24 approach.

25 (1) Defining an area. This is the area in which neighbouring plants can cast shadows to a  
26 plant of stratum  $i$  located at the middle of one end of the area or the stripe shown in light grey  
27 in Fig. 4. The width of the stripe is the crown width  $D_i$  plus the maximum of crown width of  
28 all the strata in the plant community. The length of the stripe ( $X_{max}$ ) was set as 100 m (the  
29 shading effects on plant  $i$  is ignorable for plants beyond this distance).



1 (2) Determining the number of woody plants in the stripe. The number of woody plants for  
2 each stratum in the stripe can be determined based on the area of the stripe and the density of  
3 each woody stratum.

4 (3) Putting the woody plants randomly in the stripe. First we generate a pair of random  
5 numbers as the possible location of a plant in the stripe. Then we check its distance from the  
6 existing plants in the stripe to make sure that the crown of this plant does not overlap with the  
7 existing plants. If the distance was less than the minimum distance to one of the existing  
8 plant, we re-generated a pair of random numbers for a new location and checked again until  
9 the distance requirement was satisfied. Plants of two woody strata can distribute  
10 independently if one stratum is completely over or below the other stratum.

11 (4) Calculating sunlit leaf area numerically. We divide the crown of plant  $i$  into small cells  
12 (Fig. 4). A light beam going through a cell may go through crowns of its neighbouring plants.  
13 Based on the locations and crown sizes of the plants, we can geometrically determine whether  
14 a neighbouring plant can intercept the light beam (Fig. 4). If so, its shading effects can be  
15 calculated based on Eq. (11) (the height  $z_i$  in Eq. (7) can be determined according to the  
16 height of the cell, the distance between the two plants, and the elevation angle of the beam).  
17 The size of the cell was defined as  $\Delta z = 0.01(H_i - h_i)$  and  $\Delta y = 0.01D_i$ . The sunlit leaf area of  
18 the crown is the total of the sunlit area of all the cells.

19 (5) Repeating steps 2 – 4 until the calculated fraction of sunlit leaf area is stable. The  
20 calculated fraction of sunlit leaf area under each case of the random distribution of  
21 neighbouring plants is different. But their average become very stable after 300 random cases  
22 (the variation is less than 0.001 for the fraction of sunlit leaf area). Therefore, we ran 300  
23 random distribution cases for each test and then used the average to compare with the result of  
24 the IPR model.

### 25 **2.4.2 Sensitivity tests**

26 When a plant community has two or more strata and plant density is high, the random  
27 approach cannot distribute the plants randomly without overlapping. Thus we cannot use the  
28 random approach to test the IPR model in such cases. Instead we tested the sensitivity of the  
29 model to plant densities to show its consistency under different plant densities. We also  
30 compared the IPR results with that of the two-big-leaf method with different plant densities  
31 for one-stratum communities and for two-stratum plant communities when the crowns are in

1 the same heights and when the crowns of one stratum are completely above the other. Such  
2 comparisons not only can test the IPR model when the canopy is almost completely covers  
3 the ground, they also show the errors of the two-big-leaf method when the crowns are sparse.

### 4 **3 Results and analyses**

#### 5 **3.1 Comparing with the fractions of sunlit leaf area calculated using the** 6 **random approach**

##### 7 **3.1.1 One-stratum plant communities**

8 Figure 5 shows comparisons of the fraction of sunlit leaf area ( $f_{sunlit}$ ) calculated by IPR and the  
9 average of the random approach under different plant density, local leaf area index of the  
10 individual crown ( $LAI_p$ ), and the elevation angle of the sun ( $\theta$ ).  $f_{sunlit}$  calculated by the IPR  
11 model is very close to the average of the random approach in all the cases.  $f_{sunlit}$  increases with  
12 the decrease in plant density because of the decrease in shading effects by surrounding plants.  
13 For the same reason, the effects of plant density are stronger when  $\theta$  is low.  $f_{sunlit}$  of different  
14 plant density converges with increase in  $\theta$ , and reaches the same value when the light is  
15 straight down, as  $f_{sunlit}$  in that case only depends on  $LAI_p$ .  $f_{sunlit}$  decreases with the increase in  
16  $LAI_p$  for a given  $\theta$  (Fig. 5a-c). If we reduce the plant height by half without changing  $LAI_p$ ,  
17  $f_{sunlit}$  decreases significantly (almost equals to doubling  $LAI_p$ ) when  $\theta$  is low (comparing Fig.  
18 5b and 5d). This is because reducing crown height without changing  $LAI_p$  increases the leaf  
19 area density or increases optical thickness when  $\theta$  is low. The effect of height is not  
20 significant when  $\theta$  is high.

##### 21 **3.1.2 Two-stratum plant communities**

22 For two-stratum plant communities, the fractions of sunlit leaf area calculated by IPR are very  
23 close to the averages of the random approach as well for different heights (Fig. 6). When the  
24 heights of the two strata are the same, the fractions of the sunlit leaf area for the two strata are  
25 the same (Fig. 6a), and are almost the same as the results using one-stratum but double the  
26 plant density (the curve is not shown since it is overlapped with other curves in Fig. 6a).  
27 When one stratum becomes higher, the  $f_{sunlit}$  of the upper stratum increases and the  $f_{sunlit}$  of the  
28 lower stratum decreases because of the increased shading effects of the upper stratum on the  
29 lower one (see gradual changes from Fig. 6a to 6e). The  $f_{sunlit}$  of the lower stratum is close to

1 that of the upper stratum when  $\theta$  is near  $90^\circ$  as the upper stratum has little shading effects on  
2 the low stratum in that case.

3 Figure 7 shows comparisons under different combinations of crown heights, plant density,  
4 crown width, and leaf area.  $f_{sunlit}$  calculated by the IPR model is very close to the average of  
5 the random approach in the different cases. Reducing the density of the lower stratum does  
6 not affect much the taller stratum. However, reducing the density of the taller stratum  
7 increases  $f_{sunlit}$  for both strata (Fig. 7a and 7b). Increasing  $LAI_p$  (no change in crown width) of  
8 the taller stratum reduces its  $f_{sunlit}$ , especially when  $\theta$  is high, but that does not affect much  
9  $f_{sunlit}$  of the lower stratum, because its light mainly comes from the gaps of the taller stratum  
10 (Fig. 7b and 7c). Reducing crown width (no change in  $LAI_p$ ) can slightly increase  $f_{sunlit}$  when  $\theta$   
11 is low, because the path length of light going through the crown becomes shorter (Fig. 7d).  
12 Figure 7(d-f) shows again that the relative heights of the plants have a significant impact on  
13 light competition among plant strata.

### 14 **3.1.3 Plant communities with three or more strata**

15 The fraction of sunlit leaf area calculated by the IPR model is very similar to the average of  
16 the random approach for plant communities with three and four strata as well (Fig. 8). The  
17 relative heights are the major factor affecting  $f_{sunlit}$  for each stratum (the three strata are  
18 overlapped vertically in Fig. 8a and 8c while they were not overlapped in Fig. 8b).  $f_{sunlit}$  of the  
19 low stratum also depends on its own crown features and its plant density (comparing stratum  
20 3 in Fig. 8a with 8c).

## 21 **3.2 Sensitivity analyses**

### 22 **3.2.1 One-stratum plant communities**

23 The fractions of sunlit leaf area and sunlit area on the ground are very sensitive to plant  
24 density and local leaf area index of the plants (Fig. 9).  $f_{sunlit}$  decreases with increase in plant  
25 density (all curves show declining patterns in Fig. 9a to 9c), but the decrease becomes smaller  
26 when  $\theta$  is higher (comparing the curves with the same colour from Fig. 9a to 9c), because the  
27 shading effects of neighbouring plants is less severe when  $\theta$  is higher ( $f_{sunlit}$  is independent of  
28 plant density when light is straight down since there is no shading among plants at all in that  
29 case). The fraction of sunlit area on the ground decreases quickly with increase in plant  
30 density. Similar to the changes in  $f_{sunlit}$ , the fraction of sunlit area on the ground increases with

1 increase in  $\theta$  due to decrease of the shading effects (comparing the curves with the same  
2 colour from Fig. 9d to 9f). Increase in  $LAI_p$  reduces  $f_{sunlit}$ , and also significantly reduces the  
3 fraction of sunlit area on the ground. Since the relative diffuse radiation (intercepted by leaves  
4 or on the ground. Fig. 9g and 9h) is an integration of all the elevation angles, its sensitivity to  
5 plant density is similar to that of the sunlit fraction (intercepted by leaves or on the ground)  
6 when  $\theta$  is around  $45^\circ$ .

7 Crown width affects  $f_{sunlit}$  mainly when plants are sparse and the elevation angle of the sun is  
8 low ( $LAI_p$  was kept constant in the tests) (Fig. 10). This is because the solar beam goes  
9 through a longer path in a crown when the crown is wider and  $\theta$  is lower. This effect becomes  
10 relatively small when plants are dense. The fraction of sunlit area on the ground is more  
11 dependent on the fraction of ground covered by crowns (calculated by  $D^2 \cdot d$ ) rather than crown  
12 width. The effect of crown heights on the fraction of sunlit area on the ground is very small  
13 (assuming no changes in  $LAI_p$ , plant density, and crown width. Figures are not shown).  
14 However, crown heights are very important for light competition among plant strata, as  
15 discussed in the previous section and will be emphasized in the following section as well.

### 16 **3.2.2 Two-stratum plant communities**

17 Figure 11 shows the sensitivity of the fractions of sunlit area and relative diffuse radiation (on  
18 the leaves and on the ground) to plant density for two-stratum plant communities. Increasing  
19 the density of the taller stratum has stronger impacts than that of the lower stratum, especially  
20 when  $\theta$  is low (comparing the black curve with the blue curve in each panel in Fig. 11a to  
21 11f). Even when the total fractions of land covered by the two strata do not change,  
22 increasing the density of the taller stratum (decreasing the density of the lower stratum at the  
23 same time) always results in a decrease of  $f_{sunlit}$  for both strata (The green curves in Fig. 11a to  
24 11f). The  $f_{sunlit}$  of the lower stratum is more sensitive than that of the taller stratum to changes  
25 in plant density of either one or both strata when  $\theta$  is not very high (comparing the curves of  
26 the same colour (excepted the green curves) between Fig. 11a and 11d, 11b and 11e, 11c and  
27 11f, respectively). The  $f_{sunlit}$  of the lower stratum increases with the increase in  $\theta$ , because  
28 more light can reach the lower stratum through the gaps of the taller stratum (Comparing the  
29 curves of the same colour from Fig. 11d to 11f).

30 The fraction of sunlit area on the ground decreases with the increase in the density of either  
31 stratum, and is more related with the total plant density of the two strata (Fig. 11g to 11i). The

1 fraction of sunlit area on the ground is higher when  $\theta$  is higher, since more light can reach the  
2 ground from gaps among plants. Similar to  $f_{sunlit}$ , the relative diffuse radiation intercepted by  
3 the lower stratum is more sensitive than that of the taller stratum to plant density of either  
4 stratum (Fig. 11j and 11k). The relative diffuse radiation on the ground depends on the total  
5 plant density of the two strata (Fig. 11l).

6 These sensitivity tests show that the IPR model can calculate the solar radiation intercepted by  
7 leaves and the ground consistently from very sparse to continuous plant communities.

### 8 3.2.3 Comparing with results of the two-big-leaf method

9 Figure 12 shows comparisons of the fractions of sunlit leaf area calculated between the IPR  
10 model and the two-big-leaf method (Assuming that the canopy covers the ground uniformly.  
11 The leaf area index was calculated as  $D^2 \cdot d \cdot LAI_p$ ). The two-big-leaf method significantly over-  
12 estimates  $f_{sunlit}$  when plants are sparse and  $\theta$  is high. Another difference is their variation  
13 patterns:  $f_{sunlit}$  calculated by the two-big-leaf method always increases with the increase in  $\theta$ ,  
14 whereas  $f_{sunlit}$  calculated by IPR usually increases at the beginning, and then decreases  
15 gradually with the increase in  $\theta$ , especially when plants are sparse. When  $\theta$  is very low,  
16 increasing  $\theta$  significantly reduces the shading of neighbouring plants, thus  $f_{sunlit}$  increases  
17 rapidly. When  $\theta$  is high, however, increasing  $\theta$  results in more light reaching the ground from  
18 the gaps among the crowns, thus  $f_{sunlit}$  decreases with  $\theta$ . The two-big-leaf method cannot  
19 capture this variation pattern. The difference between IPR and the two-big-leaf method  
20 becomes smaller when the plant community is denser (or the gaps among crowns are smaller),  
21 especially when  $\theta$  is low. When the canopy completely covers the ground, the  $f_{sunlit}$  calculated  
22 by the IPR model are almost the same as that of the two-big-leaf method. The differences are  
23 less than 0.002 for one-stratum plant communities and for two-stratum communities with  
24 crowns of one stratum completely above the other; and the differences are less than 0.02 for  
25 two-stratum communities when the heights of the crowns are the same (Figures were not  
26 shown since their difference is too small).

## 27 4 Discussion and conclusions

28 Motivated to understand and predict the dynamics of vegetation in northern high latitudes  
29 under climate warming, we developed an approach to calculate solar radiation absorbed by  
30 individual plants in sparse heterogeneous woody plant communities based on geometrical  
31 optical relationships. The core of the calculation is to determine the fraction of sunlit leaf area

1 of sparse woody plants. We tested the model by comparing with the numerical simulations  
2 assuming plants are distributed randomly. The results show that the IPR calculated fractions  
3 of sunlit leaf area of the individual plants are very close to the averages of random  
4 distributions of the plants, and the results are consistent for different heights, crown width,  
5 leaf area, plant density, and under different elevation angles of the sun.

6 Comparing to the two-big-leaf method (e.g., Sellers et al., 1992; Norman, 1980; Wang and  
7 Leuning, 1998), the IPR model can be used for continuous and discontinuous plant canopies.  
8 IPR gives almost the same results as the two-big-leaf method when the canopy is continuous.  
9 When crowns are sparse, the IPR model can consider the light directly reaching the ground  
10 from the gaps of the crowns, and therefore is more accurate than the two-big-leaf method. In  
11 addition, the IPR model can be used for plant communities composed of several different  
12 woody strata, and each plant stratum does not need to be continuous. Thus, IPR can calculate  
13 the competition of light among woody plant types.

14 Comparing to individual-based radiation and vegetation models (e.g., Sato et al., 2007;  
15 Kobayashi and Iwabuchi, 2008), IPR calculates the solar radiation conditions of average  
16 individual woody crowns. IPR only calculates the solar radiation of one average individual  
17 plant for each woody stratum in the plant community rather than every individual woody  
18 plant. Thus it represents the conditions of typical plants of different strata. This is similar to  
19 the treatment of plant functional types in stand-based vegetation dynamic models (e.g., Sitch  
20 et al., 2003); therefore IPR could be used to improve the accuracy of light competition in  
21 these models. On the other hand, IPR focuses on solar radiation intercepted by crowns  
22 without considering directional reflectance to the sky (as some models for remote sensing  
23 purposes, e.g., Li et al., 1995; Myneni et al., 1995; Kobayashi and Iwabuchi, 2008), thus  
24 greatly simplifies the calculation and increased the computation efficiency.

25 Although the fraction of sunlit leaf area can be calculated numerically if we know the  
26 locations of all the plants in a community, the calculation is very time consuming. As we did  
27 in the random approach for the model testing, which needs to run about 300 random cases to  
28 get the average stabilized since the results are different for different random cases.  
29 Furthermore, the average of the random distribution calculated by the IPR is more  
30 ecologically meaningful than the individual random cases because the daily average light  
31 conditions of a plant is somewhat equivalent to the average of many random cases  
32 corresponding to different azimuth directions with the changes of time in a day. That is why

1 the light conditions and the related ecological functions of one plant (e.g., photosynthesis,  
2 energy and water fluxes) averaged for a day or longer are similar to other plants of the same  
3 stratum although at any moment the light conditions can be very different from plant to plant.  
4 In addition to the solar radiation intercepted by individual woody plants and the herb strata,  
5 the IPR model also calculates the radiation condition on the ground, which is important for  
6 the growth of mosses and lichens, and for the whole ecosystems as well by directly affecting  
7 soil thermal and hydrological conditions, such as permafrost and active-layer thickness  
8 (Zhang et al., 2008). Since the IPR model is efficient in computation, it can be used for long-  
9 term, transient, spatial modelling for climate change impact assessment and predictions.

10 The crowns of woody plants in IPR are represented by rectangular boxes with uniform leaf  
11 area densities. Such a treatment allows for a quasi-analytical solution and greatly reduced  
12 computation time. For example, the interception of a light beam going through a slice of a  
13 crown can be expressed by Eq. (7). However, crowns can be in very different shapes and non-  
14 foliage objects (the trunk and branches) also intercept light. The leaf area density is usually  
15 not uniform within a crown, and radiative transfer process can be very complex. Therefore  
16 some modification and improvement are needed in the future to make the model better  
17 reflecting the field conditions.

18 We developed the IPR model using Microsoft Visual C++. The supplement 1 of the paper  
19 provides the code of the model to calculate the diurnal variations of solar radiation of  
20 different plant strata and on the ground in a day. It can be easily included as a module in  
21 vegetation models. A user's manual of the model has been included in supplement 2 as well.

22

## 1 Notations

- 2  $D$  crown width of a plant (m).  $D_i$  and  $D_j$  are for plants of woody stratum  $i$  and  $j$ ,  
3 respectively.
- 4  $d$  plant density of a stratum (plants/m<sup>2</sup>).  $d_i$  and  $d_j$  are for the densities of woody stratum  $i$   
5 and  $j$ , respectively.
- 6  $dA$  the area (m<sup>2</sup>) of a small column of canopy (perpendicular to the direction of the light  
7 beam).  $dA_i$  is the area of a crown slice of a plant  $i$ .
- 8  $dF$  the light intercepted by a small column of canopy. Its unit is the same as the unit of the  
9 beam of light entering the column.
- 10  $dL_b$  the sunlit leaf area (m<sup>2</sup> leaf) of a small column of canopy or a crown slice.
- 11  $dz_i$  the thickness (m) of a crown slice in vertical direction for a plant of stratum  $i$ .
- 12  $E_{jm}$  the fraction of the crown of plant  $j$  overlapped vertically with crown of plant  $m$ ,  
13 calculated by Eq. (16). Similarly,  $E_{ij}$  is the fraction of the crown of plant  $i$  overlapped  
14 vertically with the crown of plant  $j$ .
- 15  $E_{Tj}$  the total fraction of the crowns of all the plant strata overlapped with a crown of  
16 stratum  $j$  on average, calculated by Eq. (15).
- 17  $F_{d,g}$  the relative diffuse radiation received on the ground, expressed as the ratio to the  
18 diffuse radiation on a horizontal surface above the plant community.
- 19  $F_{d,h}$  the relative diffuse radiation intercepted by the herb stratum, expressed as the ratio to  
20 the diffuse radiation on a horizontal surface above the plant community.
- 21  $F_{d0,h}$  the relative diffuse radiation intercepted by the herb stratum when there is no woody  
22 strata, calculated by Eq. (25) but with  $F_{2w} = 1$  in Eq. (24) for  $f_{sunlit,h}$  estimation.
- 23  $F_{d,i}$  the relative diffuse radiation intercepted by woody stratum  $i$ , expressed as the ratio to  
24 the diffuse radiation on a horizontal surface above the plant community.
- 25  $F_{d0,g}$  the relative diffuse radiation received on the ground when there is no woody strata,  
26 calculated by Eq. (27) but with  $F_{2w} = 1$  in Eq. (26) for  $f_{sunlit,g}$  estimation.
- 27  $F_1$  the solar beam before enters a column of canopy, expressed as the fraction of sunlit  
28 area on a surface.
- 29  $F_2$  the solar beam after going through a column of canopy, expressed as the fraction of  
30 sunlit area on a surface.
- 31  $F_{2w}$  the solar beam available for the herb stratum after the interception of the woody strata,  
32 expressed as the fraction of the sunlit area on a horizontal surface.



- 1  $f$  the shading effects of a small column of canopy on subsequent objects (Equation (6)).  $f$   
2  $= 1$  for no shading, and  $f = 0$  for completely shaded).
- 3  $f_{i,jk}$  the average shading effects on a slice of crown of plant  $i$  by plants of stratum  $j$  in  
4 rectangle  $k$  shown in Fig. 3.
- 5  $f_{sunlit,i}$  the fraction of sunlit leaf area of woody stratum  $i$ .
- 6  $f_{sunlit,h}$  the fraction of sunlit leaf area of the herb stratum.
- 7  $f_{sunlit,g}$  the fraction of sunlit area on the ground, which is the fraction of sunlit area available  
8 for mosses and lichens.
- 9  $f_{0i,jk}$  the shading effects on a slice of crown of plant  $i$  by a crown of plant  $j$  in rectangle  $k$ .  
10 shown in Fig. 3
- 11  $H$  the height of the top of the crown (m).  $H_i$  and  $H_j$  are for plants of woody stratum  $i$  and  
12  $j$ , respectively.
- 13  $h$  the height of the bottom of the crown (m).  $h_i$  and  $h_j$  are for plants of woody stratum  $i$   
14 and plant  $j$ , respectively.
- 15  $I_{avg,g}$  the average solar radiation absorbed on the ground ( $\text{W/m}^2$  ground).
- 16  $I_{b,h}$  the direct solar radiation intercepted by sunlit leaves of the herb stratum ( $\text{W/m}^2$  leaf).
- 17  $I_{b,i}$  the direct solar radiation intercepted by sunlit leaves of woody stratum  $i$  ( $\text{W/m}^2$  leaf).
- 18  $I_{b0}$  the direct solar radiation on a horizontal surface above the plant community ( $\text{W/m}^2$   
19 ground).
- 20  $I_{d,g}$  the diffuse radiation received on the ground ( $\text{W/m}^2$  ground).
- 21  $I_{d,h}$  the diffuse radiation intercepted by leaves of the herb stratum ( $\text{W/m}^2$  leaf).
- 22  $I_{d,i}$  the diffuse radiation intercepted by leaves of woody stratum  $i$  ( $\text{W/m}^2$  leaf).
- 23  $I_{d0}$  the diffuse radiation on a horizontal surface above the plant community ( $\text{W/m}^2$   
24 ground).
- 25  $I_{s,g}$  the scattered radiation received on the ground ( $\text{W/m}^2$  ground).
- 26  $I_{s,h}$  the average scattered radiation absorbed by the herb stratum ( $\text{W/m}^2$  leaf).
- 27  $I_{shaded,g}$  solar radiation absorbed by shaded area on the ground ( $\text{W/m}^2$  ground).
- 28  $I_{shaded,h}$  solar radiation absorbed by shaded leaves of the herb stratum ( $\text{W/m}^2$  leaf).
- 29  $I_{shaded,i}$  solar radiation absorbed by shaded leaves of the woody stratum  $i$  ( $\text{W/m}^2$  leaf).
- 30  $I_{sunlit,g}$  solar radiation absorbed by sunlit area on the ground ( $\text{W/m}^2$  ground).
- 31  $I_{sunlit,h}$  solar radiation absorbed by sunlit leaves of the herb stratum ( $\text{W/m}^2$  leaf).
- 32  $I_{sunlit,i}$  solar radiation absorbed by sunlit leaves of the woody stratum  $i$  ( $\text{W/m}^2$  leaf).

|    |            |   |
|----|------------|---|
| 1  | $I_{s0,h}$ | the average scattered radiation generated by reflection and transmission when direct and diffuse radiation is first intercepted by leaves of the herb stratum ( $\text{W}/\text{m}^2$ leaf).                              |
| 2  |            |   |
| 3  | $I_{s0,i}$ | the average scattered radiation ( $\text{W}/\text{m}^2$ leaf) generated by reflection and transmission when direct and diffuse radiation is first intercepted by leaves of woody plant $i$ ( $\text{W}/\text{m}^2$ leaf). |
| 4  |            |   |
| 5  |            |   |
| 6  | $I_{s1,h}$ | the average scattered radiation on the top of the herb stratum generated by the woody plants ( $\text{W}/\text{m}^2$ ground).   |
| 7  |            |   |
| 8  | $I_{s1,i}$ | the average scattered radiation absorbed by a unit leaf area of plant $i$ ( $\text{W}/\text{m}^2$ leaf).  |
| 9  | $i$        | used as a subscript for a plant of a woody stratum.   |
| 10 | $j$        | used as a subscript for a plant of a woody stratum.   |
| 11 | $K$        | effective extinction coefficient for a beam of light. $K_i$ and $K_j$ are for plants of woody stratum $i$ and $j$ , respectively.   |
| 12 |            |   |
| 13 | $K_0$      | the extinction coefficient when leaves are distributed randomly. It equals 0.5.   |
| 14 | $K_h$      | the effective extinction coefficient of the herb stratum.   |
| 15 | $k$        | a sequence number for a rectangle in Fig. 3 for calculating the shading effects of neighbouring plants.   |
| 16 |            |   |
| 17 | $L_0$      | the total leaf area of a crown ( $\text{m}^2$ leaf/plant). $L_{0i}$ is for a plant of stratum $i$ .   |
| 18 | $LAI_p$    | the local leaf area index of an individual plant, defined as the ratio between the leaf area of the plant and the land area directly below the crown ( $\text{m}^2$ leaf/ $\text{m}^2$ ground).                           |
| 19 |            |   |
| 20 | $LAI_h$    | the leaf area index of the herb stratum ( $\text{m}^2$ leaf/ground).  |
| 21 | $L_{bi}$   | the total sunlit leaf area of the woody plant $i$ ( $\text{m}^2$ leaf/plant).   |
| 22 | $l$        | the path length (m) of light for a small column of crown.   |
| 23 | $l_{ai}$   | the average path length (m) of light from a light source in the crown of plant $i$ to outside of the crown.   |
| 24 |            |   |
| 25 | $l_{zi}$   | the path length (m) of the light going through a crown slice of a plant $i$ with $z_i$ as the height of the light entering the crown slice. $l_{zj}$ is similar to $l_{zi}$ but for a plant of stratum $j$ .              |
| 26 |            |   |
| 27 |            |   |
| 28 | $l_{zj,k}$ | the path length (m) of light calculated by Eq. (7) but for plants of stratum $j$ in rectangle $k$ corresponding to the height $z_{j,k}$ .   |
| 29 |            |   |
| 30 | $M_j$      | the total number of rectangles considered for calculating the shading effects of plants of stratum $j$ , estimated by Eq. (19).   |
| 31 |            |   |
| 32 | $m$        | used as a subscript for a plant of a woody stratum.   |
| 33 | $N$        | the total number of woody strata of the plant community.  |

|    |            |  |
|----|------------|--|
| 1  | $p_j$      | the probability of light going through the crowns of stratum $j$ in a rectangle area. It         |
| 2  |            | equals to the fraction of the land area covered by the crowns of the plants of the               |
| 3  |            | stratum. $p_1, p_2$ and $p_m$ are for plants of stratum $1, 2,$ and $m,$ respectively.           |
| 4  | $r_i$      | the recollision probability of scattered radiation in the crown of plant $i.$                    |
| 5  | $r_h$      | the recollision probability of scattered radiation in the herb canopy.                           |
| 6  | $X_{i,jk}$ | the distance between the edge of the crown of plant $i$ and the farther edge of the crown        |
| 7  |            | of plant $j$ in rectangle $k$ (Fig. 3)   |
| 8  | $X_{i,j1}$ | the distance $X_{i,jk}$ when $k$ equals 1 (the first rectangle near plant $i$ shown in Fig. 3).  |
| 9  | $X_{max}$  | a predefined maximum distance (e.g., 100 m) for shading effects calculation. Beyond              |
| 10 |            | that distance, the shading effects of plants are negligible.                                     |
| 11 | $z_i$      | the height (m) when light beam enters a crown slice for a plant of stratum $i.$                  |
| 12 | $z_{j,k}$  | the height (m) when light beam enters a crown slice for plants of stratum $j$ in rectangle       |
| 13 |            | $k,$ calculated by Eq. (12).   |
| 14 | $\alpha_g$ | the absorption coefficient of the ground (the albedo of the ground would be $1 - \alpha_g$ ).    |
| 15 | $\alpha_h$ | the absorption coefficient of the leaves of the herb stratum.                                    |
| 16 | $\alpha_i$ | the absorption coefficient of the leaves of the woody stratum $i.$                               |
| 17 | $\beta$    | the elevation angle of the light beam (radians).   |
| 18 | $\rho$     | the density of the leaf area of a crown ( $m^2$ leave/ $m^3$ space). It can be calculated by Eq. |
| 19 |            | (1). $\rho_i$ and $\rho_j$ are for plants of stratum $i$ and $j,$ respectively.                  |
| 20 | $\theta$   | the elevation angle of the sun (its unit is in radians in equations, but in degrees in           |
| 21 |            | figures).  |
| 22 | $\Omega$   | clumping index of the leaves. $\Omega_i$ is for woody stratum $i.$                               |
| 23 | $\Omega_h$ | clumping index of the herb stratum.  |
| 24 |            |  |

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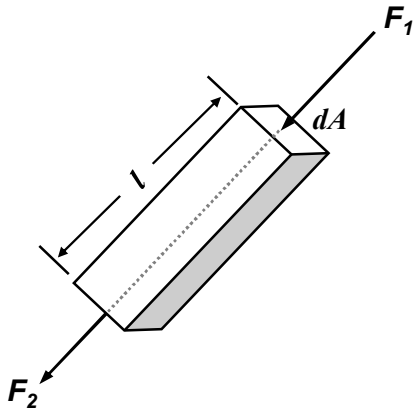
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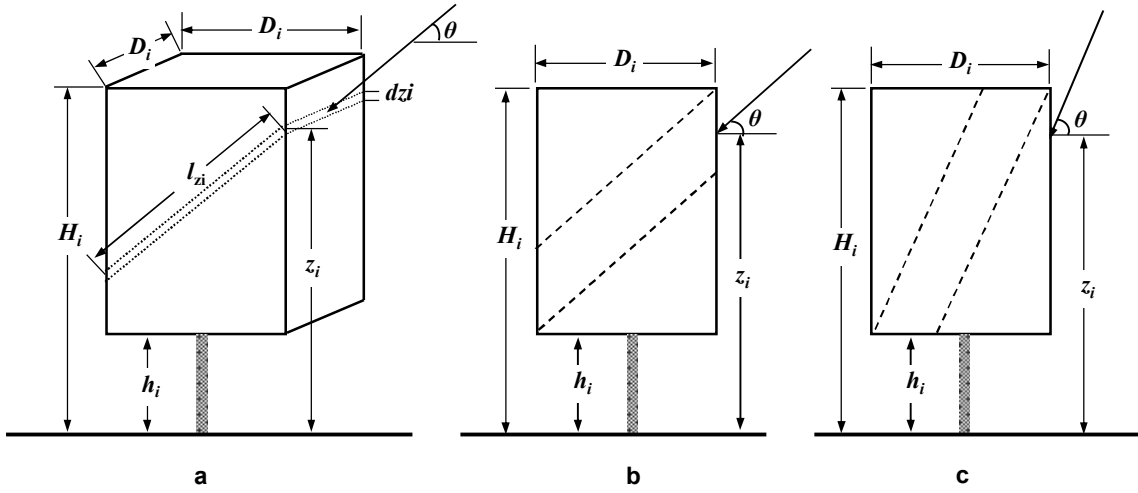




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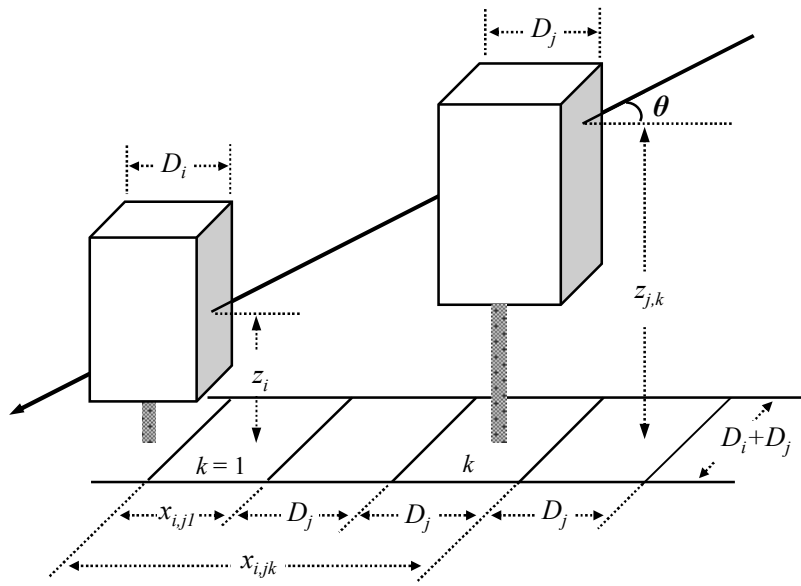
2 Figure 1. A general scheme and the related variables for interception of a light beam by a  
3 small column of canopy.

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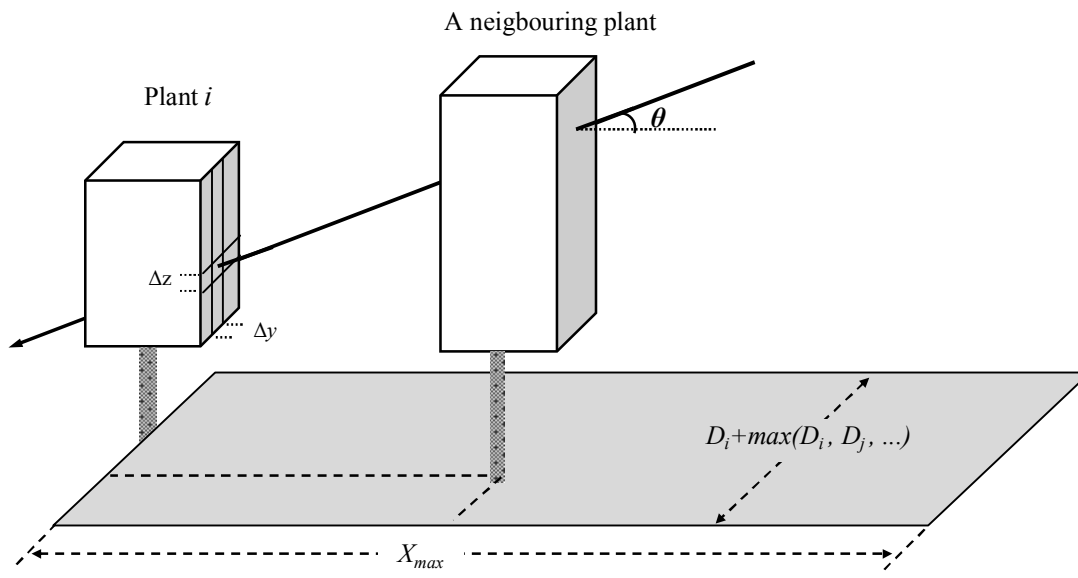
Figure 2. a) a three-dimensional show for a light beam going through a slice of crown and the related variables, and (b and c) two-dimensional shows for the two cases when a light beam going through a crown.



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2 Figure 3. The scheme to calculate the shading effects of neighbouring plants in the model.

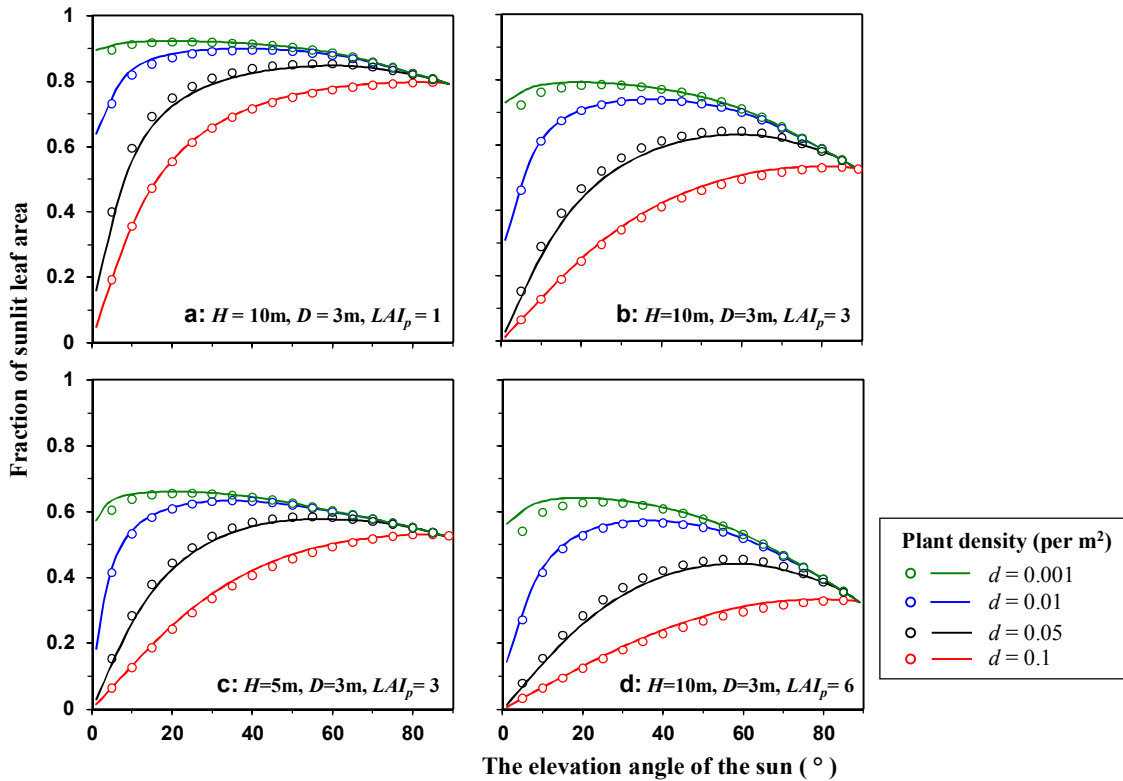
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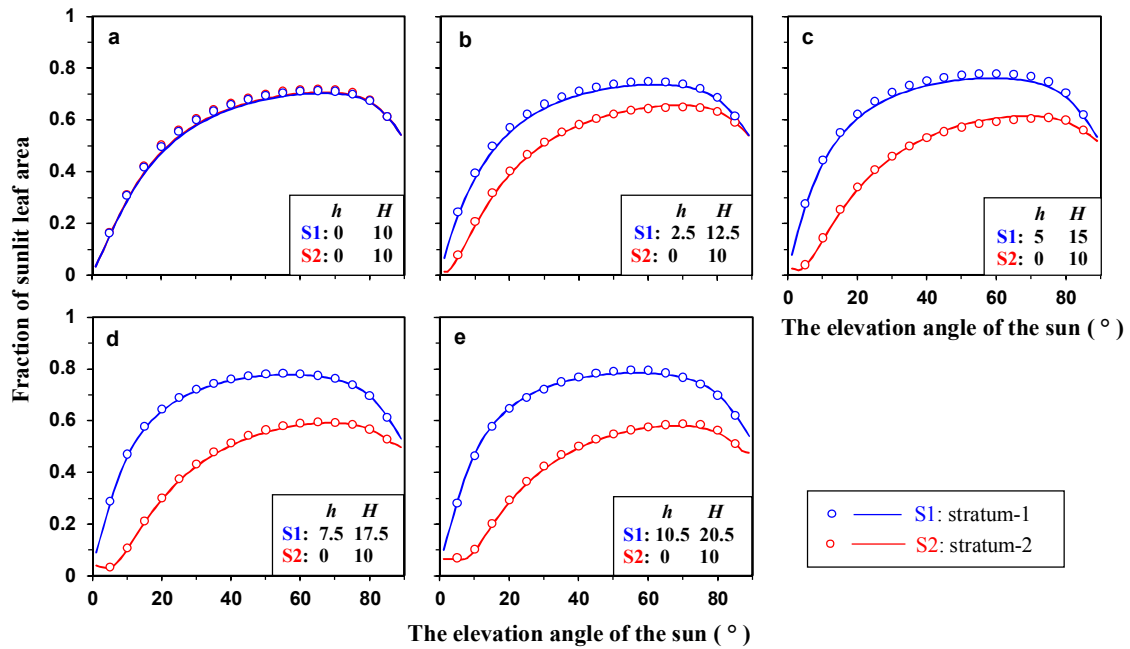
2 Figure 4. The scheme of the random approach for numerically calculating sunlit leaf area and  
 3 the shading effects of the neighbouring plants.  $\max(D_i, D_j, \dots)$  is for the maximum of the  
 4 crown width of all the plant strata in the plant community.

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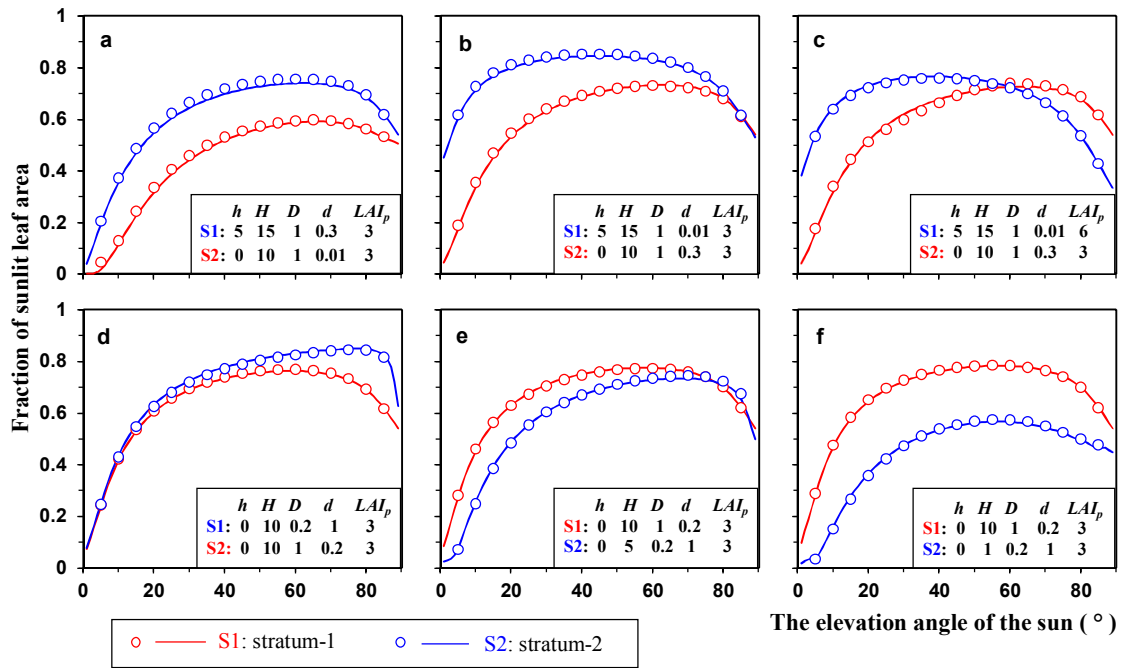
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2 Figure 5. Comparisons of the calculated fractions of sunlit leaf area between the IPR model  
 3 (curves) and the average of the random approach (circles) for one-stratum plant communities  
 4 of different heights ( $H$ ), crown width ( $D$ ), local leaf area indices ( $LAI_p$ ) and plant densities ( $d$ ).  
 5 Different colours correspond to different plant densities shown in the legend. The top height  
 6 of crown, crown width and local leaf area indices are shown in the panels. The bottom height  
 7 of the crown ( $h$ ) is 0 m. The circles for  $d = 0.1$  plants/m<sup>2</sup> were calculated assuming plants are  
 8 distributed regularly because plants cannot be distributed randomly without overlapping in  
 9 such a dense plant community.



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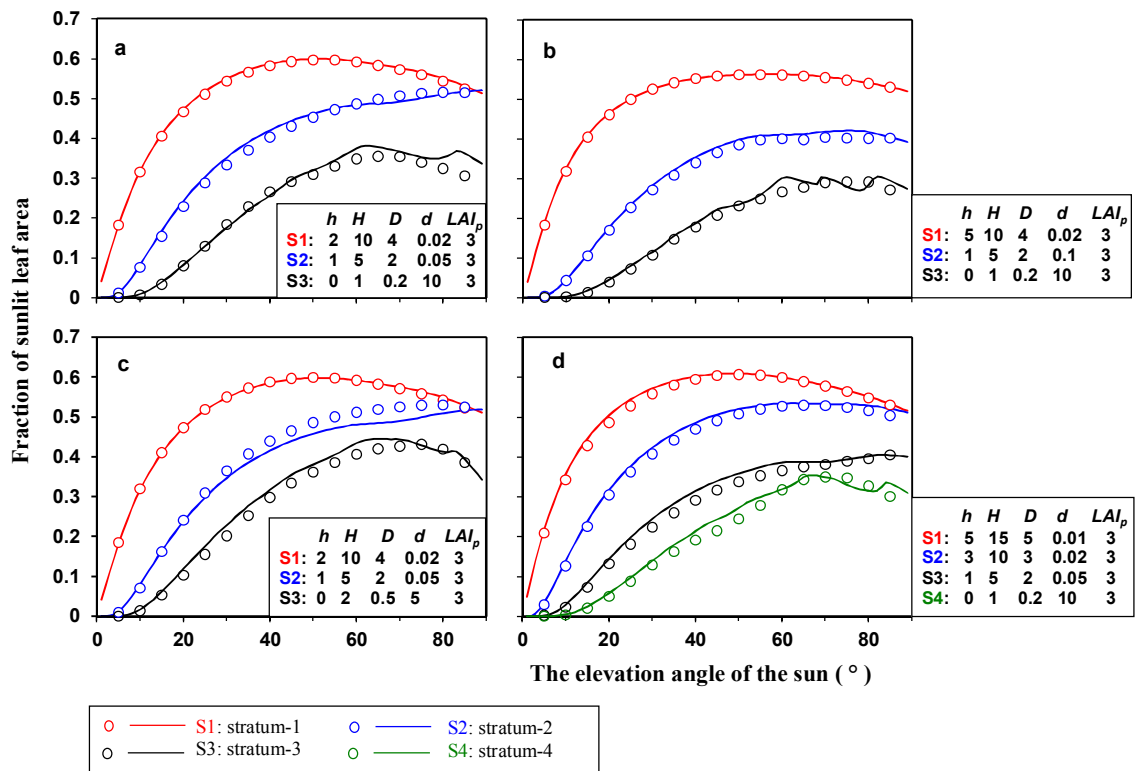
2 Figure 6. Comparisons of the calculated fractions of sunlit leaf area between the IPR model  
 3 (curves) and the random approach (circles) for two-stratum plant communities of different  
 4 heights (Stratum-1 is shifted higher and higher). Blue and red colours are for stratum-1 (S1)  
 5 and stratum-2 (S2), respectively. The top and bottom heights of the crowns ( $h$  and  $H$ ) were  
 6 shown in each panel. Other parameters are the same (crown width  $D = 1$  m, local leaf area  
 7 index  $LAI_p = 3$ , plant density  $d = 0.2$  plants/m<sup>2</sup>).



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2 Figure 7. Comparisons of the calculated fractions of sunlit leaf area between the IPR model  
 3 (curves) and the random approach (circles) for two-stratum plant communities. Red and blue  
 4 are for stratum-1 (S1) and stratum-2 (S2), respectively. Their crown parameters are listed in  
 5 each panel ( $H$  and  $h$  are the heights of the top and bottom of the crown, respectively (m),  $D$  is  
 6 the width of the crown (m),  $d$  is the density of plants (plants/m<sup>2</sup>), and  $LAI_p$  is the local leaf  
 7 area index (m<sup>2</sup> leaf/m<sup>2</sup> ground)).

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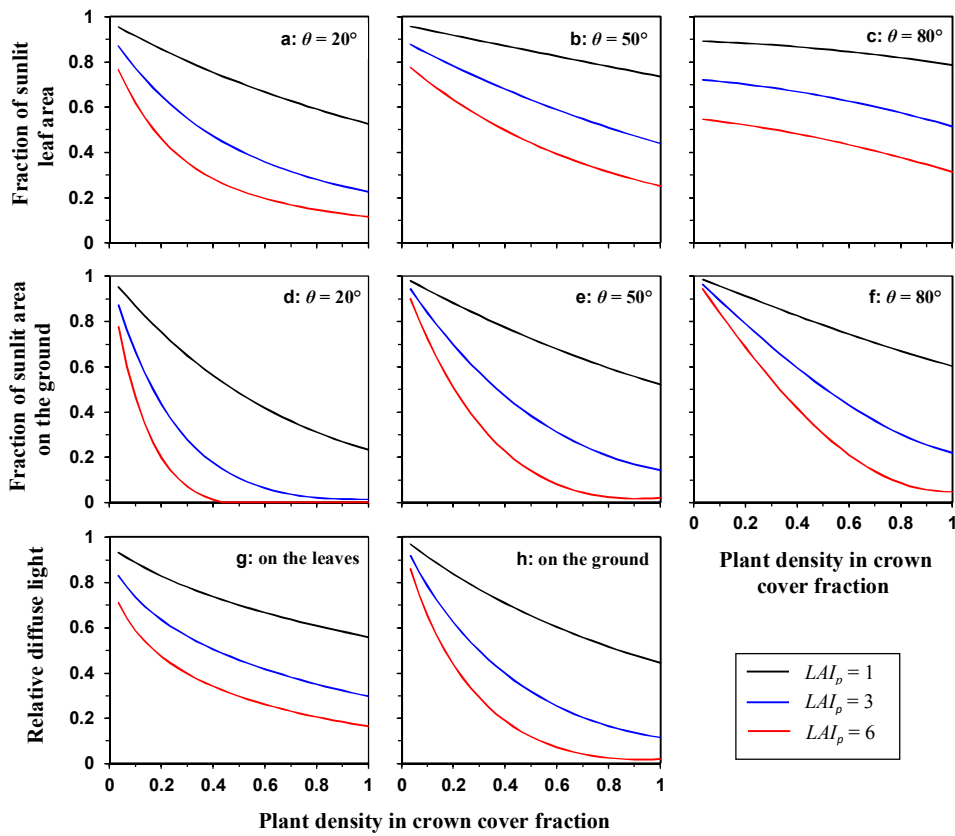


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2 Figure 8. Comparisons of the calculated fractions of sunlit leaf area between the IPR model  
 3 (curves) and the random approach (circles) for (a-c) three-stratum plant communities and for  
 4 (d) four-stratum plant communities. Different colours are for different strata. The crown  
 5 parameters are listed within or beside each panel (*H* and *h* are the heights of the top and  
 6 bottom of the crown, respectively (m), *D* is the width of the crown (m), *d* is the density of  
 7 plants (plants/m<sup>2</sup>), and *LAI<sub>p</sub>* is the local leaf area index (m<sup>2</sup> leaf/m<sup>2</sup> ground)).

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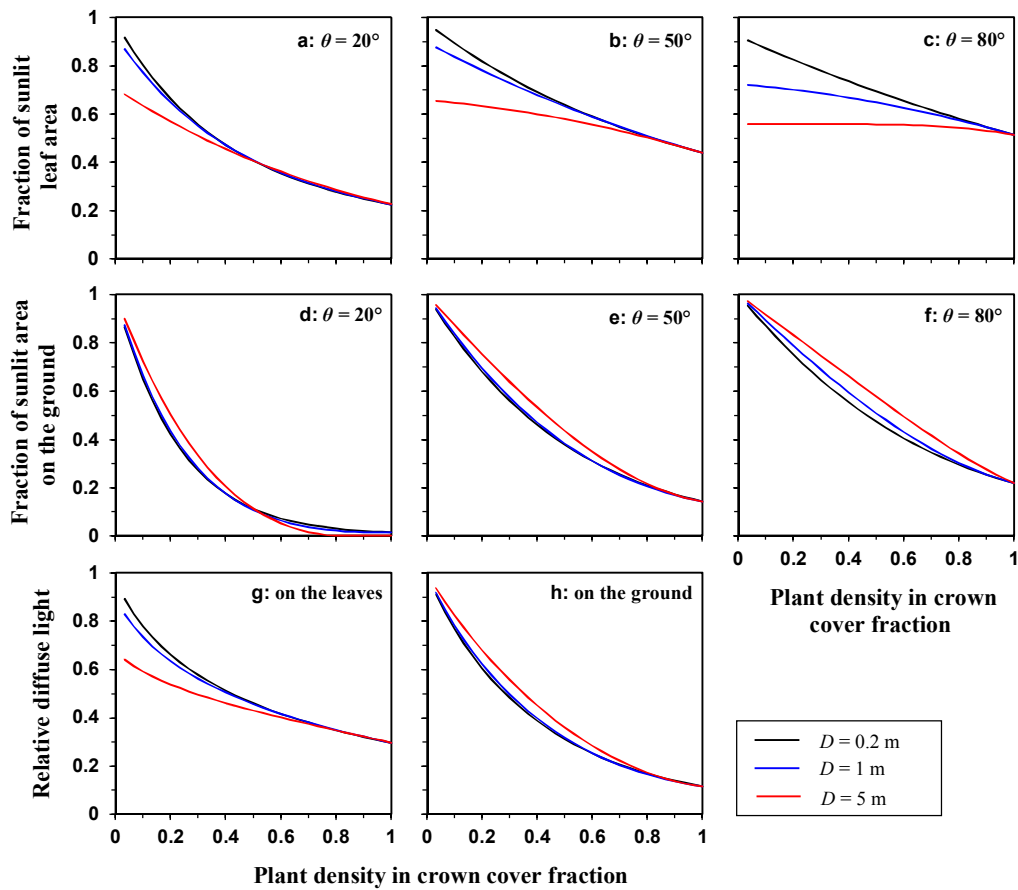




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2 Figure 9. The sensitivity of the fractions of sunlit area on the leaves and on the ground to  
 3 plant density and the local leaf area index of the plant. Plant density is expressed as the  
 4 fraction of land covered by crowns, defined as the fraction of land area covered by crowns,  
 5 calculated by  $D^2d$  ( $D$  is the width of the crown and  $d$  is the number of plants per square  
 6 meter). The relative diffuse light is the ratio to the diffuse light on a horizontal surface above  
 7 the canopy. The plant communities are composed of only one stratum ( $h = 0$  m,  $H = 10$  m,  $D = 1$   
 8 m).

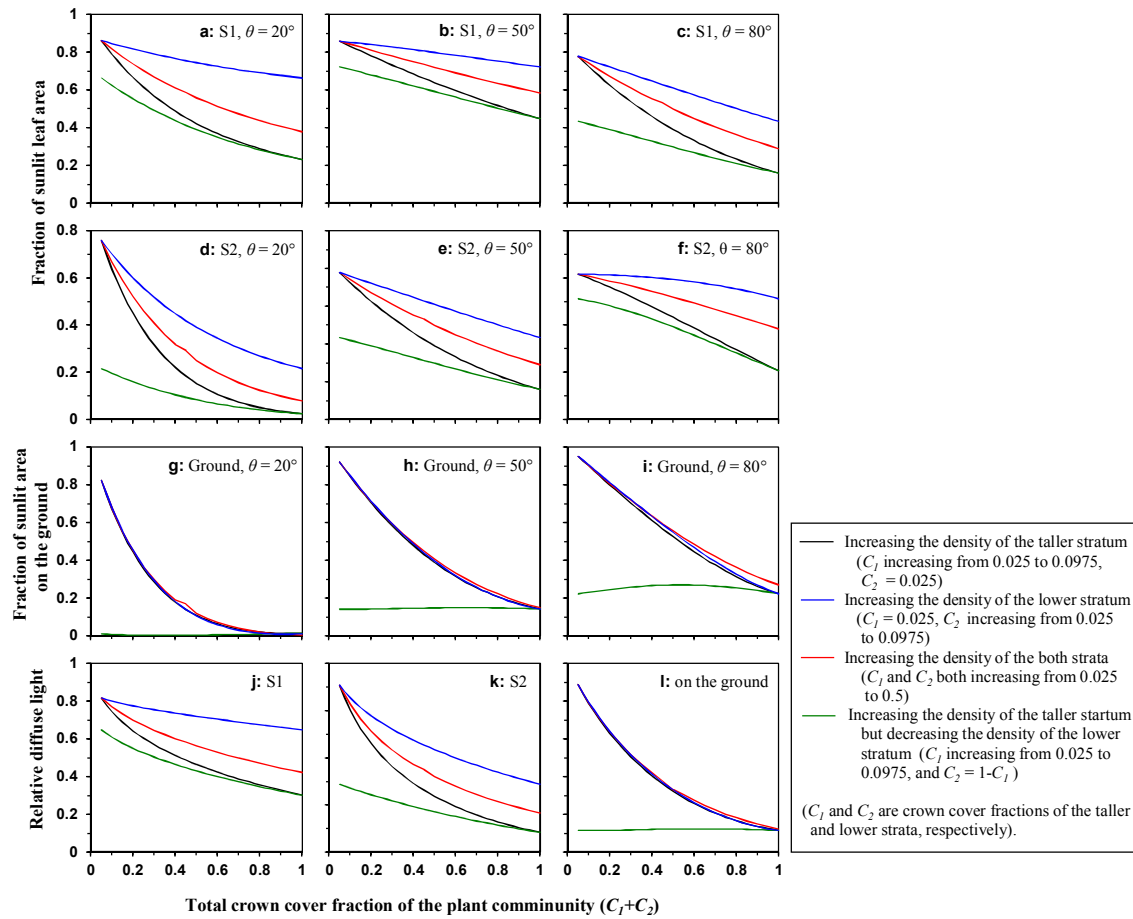
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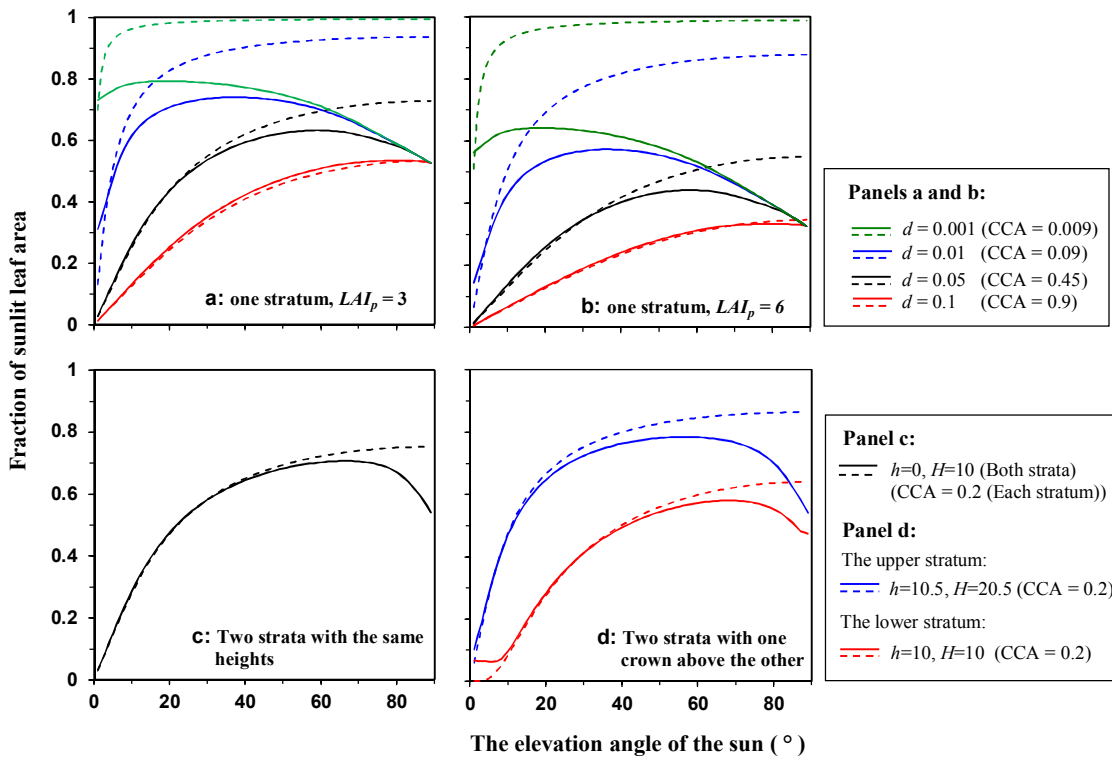
2 Figure 10. The sensitivity of the fractions of sunlit area (on the leaves and on the ground) and  
 3 relative diffuse radiation to plant density and crown width. Plant density is expressed as  
 4 crown cover fractions, calculated by  $D^2d$  ( $D$  is the width of the crown and  $d$  is the number of  
 5 plants per square meter). The relative diffuse light is the ratio to the diffuse light on a  
 6 horizontal surface above the canopy. The plant communities are composed of only one  
 7 stratum ( $h=0$  m,  $H=10$  m,  $LAI_p=3$ ).

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2 Figure 11. The sensitivity of the fractions of sunlit area (on the leaves and on the ground) and  
 3 relative diffuse radiation to plant density for two-stratum plant communities (the taller stratum  
 4 (S1):  $h_1=2$  m,  $H_1=10$  m,  $D_1=1$  m,  $LAI_{p1}=3$ ; the lower stratum (S2):  $h_2=0$  m,  $H_2=5$  m,  $D_2=1$   
 5 m,  $LAI_{p2}=3$ ). Plant density is expressed as crown cover fractions for both strata ( $C_1$  and  $C_2$ ),  
 6 calculated by  $D_1^2 d_1$  and  $D_2^2 d_2$ , respectively ( $D_1$  and  $D_2$  is the widths of the crowns of the two  
 7 strata, respectively, and  $d_1$  and  $d_2$  are the numbers of plants per square meter for the two  
 8 strata, respectively). The relative diffuse light is the ratio to the diffuse light on a horizontal  
 9 surface above the canopy.



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Figure 12. Comparisons of the calculated sunlit leaf area fractions between the IPR model (the solid curves) and the two-big-leaf method (the dash curves). Panels a and b are for one-stratum plant communities with different local leaf area index ( $LAI_p$ ) and plant densities ( $d$ ) (shown in each panel and the legend). The other parameters are the same: the bottom height of the crown  $h = 0$  m, the top height of the crown  $H = 10$  m, and crown width  $D = 3$  m. The fraction of crown covered area (CCA) was calculated by  $D^2 \cdot d$  and is also shown in the legend. Panel c and d are for two-stratum plant communities with the same crown heights and one crown above the other, respectively (crown heights and CCA are shown in the legend). The other crown parameters are the same: crown width  $D = 1$  m, local leaf area index  $LAI_p = 3$ , and plant density  $d = 0.2$  plants/m<sup>2</sup>. For the two-big-leaf method, the leaf area index of a stratum was calculated as  $D^2 \cdot d \cdot LAI_p$ .