Manuscript prepared for Geosci. Model Dev. with version 5.0 of the LATEX class copernicus.cls.

Date: 12 August 2014

GEOtop 2.0.: Simulating the combined energy and water balance at and below the land surface accounting for soil freezing, snow cover and terrain effects

S. Endrizzi¹, S. Gruber², M. Dall'Amico³, and R. Rigon⁴

Correspondence to: Stefano Endrizzi (stefano.end@gmail.com)

Abstract. GEOtop is a fine scale grid-based simulator that represents the heat and water budgets at and below the soil surface. It describes the three-dimensional water flow in the soil and the energy exchange with the atmosphere, considering the radiative and turbulent fluxes. Furthermore, it reproduces the highly non-linear interactions between the water and energy balance during soil freezing and thawing, and simulates the temporal evolution of the water and energy budgets in the snow cover and their effect on soil temperature.

Here, we present the core components of GEOtop 2.0. and demonstrate its functioning. Based on a synthetic simulation, we show that the interaction of processes represented in GEOtop 2.0. can result in phenomena that are significant and relevant for applications involving permafrost and seasonally-frozen soils, both in high altitude and latitude regions.

1 Introduction

Frozen soil and snow cover interact in various ways with hydrology, climate, ecosystems and with human infrastructures. These natural systems are complex and characterised by many non-linear processes that operate and interact over different scales. Their mathematical representation and quantification is gaining in importance, especially in the light of global climate change. This importance derives on one hand

from the requirement to study more and more complex systems, and, on the other hand, this representation of more complex systems can inform decisions about their simplification (Freeze and Harlan, 1969). In fact, the systems of equations required for representing such environments are often simplified by excluding processes that are considered less important for the problems addressed. Such an a priori exclusion, however, may not be quantitatively justified and mostly dictated by the need for mathematical tractability. Estimating the error inherent in model simplifications is therefore desirable for weighing the costs and benefits of differing options.

There is a great diversity of models (understood here as mathematical representations of one or more processes) and simulators (computer programs, usually comprising implementations of several models to represent a natural system) to simulate cold regions processes. For example, models applied in permafrost environments are normally: (i) models applied at a local, regional, and continental scale that integrate a one-dimensional form of heat and water flow equation with phase change and predict the evolution of the depth of thaw; (ii) hydrological models commonly applied at a large scale that predict river discharge without accurately describing the coupling with the soil energy balance; and (iii) models that very accurately describe and couple water and energy subsurface flow in frozen soil, but do not consider the heat flux exchanged with the atmosphere. Table 1 provides an

¹Department of Geography, University of Zurich, Winterthurerstrasse 190, 8057 Zurich, Switzerland

²Carleton University, Department of Geography and Environmental Studies, 1125 Colonel By Drive, Ottawa, ON K1S 5B6, Canada

³Mountain-eering GmbH, Siemensstrasse 19, 39100 Bozen, Italy

⁴Dipartimento di Ingegneria Civile, Ambientale e Meccanica e CUDAM, Università di Trento, Via Mesiano 77, 38123 Trento, Italy

overview of some common frozen soil and permafrost models

If we consider models dealing more extensively with hydrology, sophisticated process-based models are available, like CROCUS (Brun et al., 1992), CATHY (Paniconi and Putti, 1994), ALPINE3D (Lehning et al., 2006), HYDRO-GEOSPHERE (Therrien and Sudicky, 1996), CATFLOW (Zehe et al., 2001), InHM (VanderKwaak and Loague, 2001), and SHETRAN (Abbott et al., 1986), but usually they cover either the cryosphere (with no care of water after melting) or the surface-subsurface fluxes in the above zero centigrades domain of temperatures (Barnett et al., 2005; Endrizzi and Marsh, 2010; Horton et al., 2006). In other models, like JULES (Best et al., 2011), VIC (Liang et al., 1994), tRIBS (Ivanov et al., 2004), JGRASS-NewAGE (Formetta et al., 2011), the whole system of interactions is accounted for, but the set of equations required for representing such environments are simplified with a priori parameterisations of some interaction of processes.

GEOtop 2.0 is a process based model which develops from the blueprint GEOtop 0.75 described in Rigon et al. (2006) and Bertoldi et al. (2006). It was built in the idea that the combination of terrain effects, energy and water balance produce unique results for different meteorological forcings, which makes difficult the a priori exclusion of any of the processes. GEOtop covers the full spectrum of hydrological fluxes, from the energy balance in the complex terrain to snow and vegetation. Therefore, it allows modelling the interactions between several hydrological, cryospheric, ecological and geomorphological processes in an interdisciplinary research framework. For example, it has been applied to model geomorphological processes like landslide triggering (Simoni et al., 2008), ecohydrological processes (Bertoldi et al., 2010; Della Chiesa et al., 2014), evapotranspiration (Kunstmann et al., 2013), and runoff production (Endrizzi et al., 2011). However, this paper mainly focuses on the aspects related to the cryosphere. In this context, permafrost research provides an intersections of phenomena related to frozen soil, the flow of water, and the snow pack.

As a novel combination of processes represented, this paper presents GEOtop 2.0, an improved version of the open-source software GEOtop, which now simulates the energy and water balance at and below the land surface, soil freezing, snow cover dynamics, and terrain effects. It is a research tool for studying, for example, the hydrological and thermal phenomena at locations that differ in soil types and topography to specific climatic forcings. Output consists of variables such as temperature, water and ice contents, or of integrated variables such as stream discharge. The software operates in pointwise and distributed modes and can be flexibly controlled, because all relevant parameters that govern e.g. discretisation, input/output or numerics can be set via keywords.

GEOtop describes the evolution in time of temperature and water content in the soil and snow cover and is driven by meteorological forcings. This is accomplished by solving the heat and water flow equations with boundary conditions accounting for the interactions with the atmosphere at the surface in terms of energy and water fluxes. The solution of the equations is obtained numerically in the soil domain and snow cover.

GEOtop 2.0. is significantly different from GEOtop 0.75. It includes a fully three-dimensional description of the Richards equation, whereas in the previous version the equation was only solved in the vertical direction and the lateral flow was parameterised, in a similar way as in large-scale land surface models. In the new version, a multilayer snow cover and the surface energy balance are fully integrated in the heat equation for the soil, which is solved with a rigorous numerical method based on Kelley (2003), while in the previous version, snow cover was described with a bulk method (Zanotti et al., 2004) and the surface energy balance, though complete in its components and accommodating complex terrain, was not numerically coupled to the soil heat equation. In GEOtop 2.0 (hereafter GEOtop), soil freezing and thawing are represented, meteorological forcings are distributed, and channel routing is described as overland flow with the shallow water equation neglecting the inertia. The description of vegetation with a double-layer surface scheme in order to more accurately represent the heat and vapour exchanges of vegetation with the soil surface and the atmosphere has also been included in GEOtop and described in Endrizzi and Marsh (2010). The code of GEOtop is publicly available in the terms described in A.

The core components of GEOtop are here presented. The description will particularly consider the soil volumetric system and the equations to be solved, the interaction with the atmosphere, the effects of complex terrain, the numerics, the representation of the snow cover, and the distribution of the meteorological data. It is shown that the simulator produces plausible results in its major components. In addition, a simulation experiment is presented in order to demonstrate that the combination of terrain effects, energy and water balance produce unique results for different meteorological forcings, making an a priori exclusion of any of these processes difficult and providing one important rationale for developing and using a simulator such as GEOtop.

2 Volumetric system

The volumetric system consists of a soil volume of a userspecified uniform depth (typically a few metres to hundreds of metres) and is discretized in several layers parallel to the surface. Close to the surface the layers are usually prescribed thinner than at depth, as the gradients of temperature and water content resulting from the interaction with the atmosphere are stronger. The surface can be additionally discretized spatially using a regular square grid. Therefore, the elementary units, here referred to as "cells", are given by the volumes re-

Table 1. Overview of existing simulators dealing with soil freezing processes. Abbreviations: in the snow column: dd = degree day factor, degree day f

Model	Snow	Soil energy balance	Soil water balance	Energy exchange with atmosphere	Discharge
Hinzman et al. (1998)		1d		woT	
Oleson et al. (2004)	mly	1d	1d	woT	yes
Lehning et al. (2006)	mly	1d	0d	wiT	yes
Marchenko et al. (2008)	mly	1d		woT	
Kuchment et al. (2000)	dd	1d	0d	woT	yes
Zhang et al. (2000)	ly	0d	0d	woT	yes
McKenzie et al. (2007)		3d	3d		yes
Daanen et al. (2007)		3d	3d		
Hansson et al. (2004)		3d	3d		yes
Painter (2011)		3d	3d		
GEOtop	mly	1d	3d	wiT	yes

sulting from the intersection of layers parallel to the surface with the columns defined in a direction normal to the surface.

The heat and water flow equations are not fully coupled numerically, but they are linked in a time-lagged manner (e.g., Panday and Huyakorn, 2004). This method allows keeping the complexity of the numerics moderate, while the equations are solved reasonably fast.

2.1 Heat equation

As explained in Appendix B, the equation representing the energy balance in a soil volume subject to phase change is:

$$\frac{\partial U^{ph}}{\partial t} + \boldsymbol{\nabla} \bullet \boldsymbol{G} + S_{en} - \rho_w \left[L_f + c_w (T - T_{ref}) \right] S_w = 0 \ \ (1)$$

where U^{ph} is the volumetric internal energy of soil (J m⁻³) subject to phase change, t (s) time, $\nabla \bullet$ the divergence operator, G the heat conduction flux (W m⁻²), S_{en} the sink term of energy losses (W m⁻³), S_w the sink term of mass losses (s⁻¹), L_f (J kg⁻¹) is the latent heat of fusion, ρ_w the density of liquid water in soil (kg m⁻³), T (°C) the soil temperature and T_{ref} (°C) the reference temperature at which the internal energy is calculated. Writing G according to the Fourier's law and considering Eq. B9, Eq. 1 becomes:

$$\frac{\partial U^{ph}}{\partial t} + \nabla \bullet (-\lambda_T \nabla T) + S_{en} - u_f S_w = 0$$
 (2)

where λ_T is the thermal conductivity (W m⁻¹ K⁻¹). Equation 2 is numerically solved one-dimensionally neglecting the lateral gradients, and is integrated assigning the heat fluxes at the upper and lower boundaries of the domain. The upper boundary is given by the interface with the atmosphere or snowpack. At the lower boundary an energy flux is prescribed. This can be assigned externally as a parameter and,

depending on the conditions and depth of the soil column, this depends on terrain geometry and transient effects that often overprint the deep geothermal heat flow locally (Gruber et al., 2004). The sink term S_{en} can also be assigned externally.

Since the total mass of water is kept constant and is given by the resolution of the water balance equation in time lagged manner, the unknown of Eq. 2 is T. However, the equation determines the mass that changes phase. Since ice has a lower density than liquid water, freezing would lead to unrealistically large gauge pressures that cannot be converted into an expansion of the soil matrix, due to the lack of a mechanical model. Therefore, similarly to Dall'Amico et al. (2011a), a rigid soil scheme is assumed, which implies that no volume expansion during freezing is allowed, and the densities of ice and liquid water are equal, and set to 1000 kg m^3 .

The expression of dU^{ph} , defined in Eq. B12, implies a proper description of soil freezing and thawing processes. Water phase change from liquid to solid state in the soil is not an isothermal process like in free-surface water (e.g., Wettlaufer and Worster, 2006). Rather, phase change occurs over a range of temperatures. Several authors (e.g., Spaans and Baker, 1996) have defined fixed relations between unfrozen water content and temperature, referred to as "freezing soil characteristic curve". This is a simplification, since more complex behaviours have been observed (Koopmans and Miller, 1966). The ice volumetric content can then be calculated as the difference of total and unfrozen water contents. The definition of the freezing soil characteristic curve allows expressing dU^{ph} in the following way:

$$dU^{ph} = CdT + \rho_w \left[L_f + (c_w - c_i)(T - T_{ref}) \right] d\theta_w^{ph} = C_a dT$$
(3)

where C is the volumetric heat capacity (J m $^{-3}K^{-1}$) defined in Appendix B, c_i and c_w (J kg $^{-1}$ K $^{-1}$) are the specific ther-

mal capacity of ice and liquid water, respectively, and C_a is referred to as apparent heat capacity, function of temperature, defined as:

$$C_a = C + \rho_w \left[L_f + (c_w - c_i)(T - T_{ref}) \right] \frac{d\theta_w^{ph}}{dT}$$
(4)

2.1.1 Thermal conductivity

The thermal conductivity (λ_T) in Eq. 2 is a combination of the thermal conductivities of each component of the soil multiphase mixture $(\lambda_{sp}$ for soil particles, λ_i for ice, λ_w for liquid water, and λ_a for air). It is, therefore, a non-linear function of temperature, since the proportion of liquid water and ice contents depends on temperature. While a simple additive mixing law is exact for the heat capacity, the behaviour of a multiphase mixture concerning the thermal conductivity is much more complex. Several non-linear mixing laws have been proposed (e.g., de Vries, 1963; Johansen, 1975; Balland and Arp, 2005). GEOtop uses the one proposed by Cosenza et al. (2003), which was derived in analogy to the dielectric permittivity, namely:

$$\lambda_T = \left[\theta_{sp} \sqrt{\lambda_{sp}} + \theta_w \sqrt{\lambda_w} + \theta_i \sqrt{\lambda_i} + \theta_a \sqrt{\lambda_a} \right]^2 \tag{5}$$

where θ_{sp} (-) is the soil porosity, and θ_a (-) is the fraction of air or gaseous components, given by

$$\theta_a = \theta_{sp} - \theta_w - \theta_i \tag{6}$$

2.1.2 Soil freezing characteristic curve

Dall'Amico et al. (2011a) derived the soil freezing characteristic curve from the soil water retention curve using the Van Genuchten parameters (Van Genuchten, 1980). They assumed a rigid soil scheme and use the "freezing = drying" assumption (Miller, 1965), which implies that: (i) the freezing (thawing) water is like evaporating (condensing) water; (ii) the ice pressure is equal to the air pressure; (iii) the water and ice content in the soil are related to the soil water retention curve. However, the assumption that ice is always at the air pressure may be restrictive in permafrost modelling, since ice pressure at depth may be significantly high. Nevertheless, this can be extended. Instead of assuming that ice is at the air pressure, it can be more generally supposed that liquid water is not subjected to external pressures, which, on the other hand, are completely supported by the soil matrix and the ice. This entails that, when pore water is subjected to an external pressure (e.g., hydrostatic) it starts to freeze, the liquid water is completely unloaded of this pressure once the first ice is formed. Therefore, liquid water pressure would unrealistically undergo a pressure jump when freezing starts. However, since the focus of GEOtop is to simulate soil temperature and moisture dynamics (and not ice pressure), this is deemed reasonable.

2.2 Water flow equation

As explained in Appendix B, the system of equations representing the water balance in the soil is:

$$\begin{cases} \frac{\partial \theta_w^{ph}}{\partial t} + \frac{\rho_i}{\rho_w} \frac{\partial \theta_i}{\partial t} = 0\\ \frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet \boldsymbol{J}_w + S_w = 0 \end{cases}$$
(7)

where $d\theta_w^{ph}$ (-) is the fraction of liquid water content in soil subject to phase change, $d\theta_w^{fl}$ (-) is the fraction of liquid water content transferred by water flux, ρ_i the density of ice (kg m⁻³), θ_i (-) is the fraction of ice in soil, and J_w (m s⁻¹) the flux of liquid water. This equation describes the water flow occurring below the soil surface (subsurface flow) and is normally referred to as variably saturated Richards' equation. According to Darcy's law, J_w can be written as:

$$\boldsymbol{J}_{w} = -K\boldsymbol{\nabla}\left(\psi + z_{f}\right) \tag{8}$$

where K (m s⁻¹) is the hydraulic conductivity, ψ (m) the liquid water gauge pressure head and z_f (m) the elevation head, i.e. the elevation above a reference level. When ψ is positive, water pressure is higher than the atmospheric pressure, and soil is saturated. When ψ is negative, soil is unsaturated. According to (Dall'Amico et al., 2011a), in variably saturated conditions it is:

$$\psi = \begin{cases} \min(0, \psi_{w0}) + \psi_T(T) & \text{if } T < T^* \\ \psi_{w0} & \text{if } T \ge T^* \end{cases}$$

$$(9)$$

where $\psi_T(T)$ is the temperature dependent soil matric potential determining the contribute of freezing below the melting temperature T^* (°C), and ψ_{w0} (m) is the matric potential corresponding to the total water content. The function $\psi_T(T)$ is defined in Dall'Amico et al. (2011a). As described in section 2.1.2, it is assumed that when soil is freezing, the external pressure is completely carried by the ice.

When soil is unsaturated (ψ < 0), the water content θ_w is calculated by means of the soil water retention curve according to the Van Genuchten (1980) model. When soil is saturated (ψ \geq 0), θ_w should always be equal to the saturated value. However, a biunique relation between θ_w and ψ is needed in order to numerically solve the equation. Therefore, the concept of specific storativity (S_s in m⁻¹) is used (Ray, 1996), which is defined as the volume of water added to storage, per unit volume and per unit rise in pressure head. Therefore, it is:

$$\theta_{w} = \begin{cases} \theta_{r} + (\theta_{sp} - \theta_{r}) \cdot \left\{1 + \left[-\alpha \ \psi\right]^{n}\right\}^{-m} & \text{if } \psi < 0 \\ \theta_{sp} + S_{s}\psi & \text{if } \psi \geq 0 \end{cases}$$

(10)

where θ_r (-) is the residual water content and α (m⁻¹), and n (-) and m (-) are empirical parameters.

Defining H (m) as the sum of the pressure and potential heads:

$$H := \psi + z_f \tag{11}$$

the second part of Eq. 7, combined with Eq. 8, becomes:

$$\frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet (-K\nabla H) + S_w = 0 \tag{12}$$

Since temperature and ice content are kept constant (given by the resolution of the energy balance equation in time lagged manner), the matric potential ψ is just function of ψ_{w0} (defined in Eq. 9), which is eventually the only unknown of Eq. 12.

Analogous to the case of water content controlled only by drying processes, the hydraulic conductivity K is dependent on the soil matric potential ψ associated with liquid water (Mualem, 1976). However, the presence of ice may significantly reduce the hydraulic conductivity due to the apparent pore blockage effect exerted by ice: this is accounted for by further reducing the hydraulic conductivity by an impedance factor smaller than 1 and equal to $10^{-\omega q}$ (Hansson et al., 2004; Kurylyk and Watanabe, 2013), where ω is a coefficient and q is the ice fractional content given by $\theta_i/(\theta_s-\theta_r)$.

Equation 12 is solved in a fully three-dimensional way in order to describe the both gradients of H in the direction parallel and normal to the surface. Once the soil becomes saturated as a result of a precipitation or melting snow, normal gradients may become very small in comparison to those in the parallel direction, which, in turn, are responsible for the routing of water through the soil.

2.3 Overland flow

The surface (or overland) water flow must also be considered to consistently describe the water balance in the soil and the runoff mechanisms. This process is described with the approximation proposed by Gottardi and Venutelli (1993), who extended to the surface flow the validity of the Darcy law, which, strictly speaking, would not be valid being the flow turbulent. Using the water conservation and the Darcy law for the overland flow, the surface water balance can be written as:

$$\frac{\partial \psi|_{z=0}}{\partial t} - \nabla \bullet \left[\psi|_{z=0} K_{sur} \nabla \left(\psi|_{z=0} + z_f|_{z=0} \right) \right] - P_e = 0$$
(13)

where $\psi|_{z=0}$ and $z_f|_{z=0}$ are respectively the liquid water pressure head and the elevation head at the soil surface, K_{sur}

(m s⁻¹) the conductance, in analogy to K defined in eq. 8, P_e (m s⁻¹) the effective precipitation per unit horizontal surface that reaches the soil surface, including snowmelt flow and deducting evaporation from the soil. The variable $\psi|_{z=0}$ cannot be negative in this equation and is written in place of the water depth above the surface. Following Gottardi and Venutelli (1993) the conductance is

$$K_{sur} = c_s \psi|_{z=0}^{\gamma} \left(\frac{\partial \psi|_{z=0}}{\partial s}\right)^{-0.5}$$
(14)

where s (m) is the length along the direction of maximum local slope, c_s the surface roughness coefficient (m^{1- γ} s⁻¹) and γ an exponent between 0 and 1 that varies according to the formulation of c_s . For example, in the formulation of Manning's it is $c_s = n_r^{-1}$ and $\gamma = \frac{2}{3}$, where n_r is Manning coefficient. In the formulation of Chezy it is $c_s = C_r$ and $\gamma = \frac{1}{2}$, where C_r is the Chezy coefficient). Eq. 13 actually works as a boundary condition at the soil surface for Eq. 12.

2.4 Numerics

In order to reduce the complexity of the numerical method, Eqs. 2 and 12 are linked in a time-lagged manner, instead of solving them in a fully coupled way. Both equations have the same form, which can be generalised as

$$\frac{\partial F(\chi)}{\partial t} + \nabla \bullet (-\kappa(\chi) \nabla \chi) + S = 0 \tag{15}$$

where χ is the unknown, function of space and time, F a non-linear function of the unknown (corresponding to the internal energy content for the heat equation and the total water content for the water flow equation), S the sink term and κ a conductivity, function of the unknown.

All the derivatives are discretized as finite differences. Therefore, the following relation is obtained:

$$\frac{F(\chi_i^{n+1}) - F(\chi_i^n)}{\Delta t} - \sum_{j=1}^{M} \frac{\kappa_{ij}^m}{D_{ij}} (\chi_j^m - \chi_i^m) + S_i = G_i$$

$$i = 1, 2, \dots, N \quad (16)$$

where the equation is written for the generic i-th cell, n represents the previous time step, at which the solution is known, n+1 is the next time step, at which the solution is unknown. Δt is the time step, j is the index of the M adjacent cells with which the i-th cell can exchange fluxes, m represents a time instant between n and n+1, κ_{ij} the conductivity between the cell i and j, D_{ij} the distance between the centers of the cells i and j, S_i the sink terms, and G_i the residual that is to be minimised for finding a solution. Equation 16 is a system of N equations, and the second term of the left hand side is the sum of the fluxes exchanged with the neighbouring cells. The variables at the instant m are represented with a linear combination between the instant n and n+1. If

m=n the method is fully explicit and unstable, if $m=n+\frac{1}{2}$ the method has a second order precision but may might not be always stable, if m=n+1 the method has a first order precision but is unconditionally stable. Since there are more concerns on stability than precision, the latter is the chosen method.

A solution of Eq. 16 is sought with a special Newton-Raphson method, with the following sequence (Kelley, 2003):

$$\boldsymbol{\chi}^{n+1} = \boldsymbol{\chi}^n + \lambda_T \boldsymbol{d}(\boldsymbol{\chi}^n) \tag{17}$$

where χ and G are the vectors χ_i and G_i that appear in Eq. 16, d denotes the Newton direction, and λ_T is a scalar smaller than or equal to 1 referred to as path length, found with a line search method like the Armijo rule (Armijo, 1966). The quantity $\lambda_T d(\chi^n)$ is also referred to as Newton step. The Newton direction is obtained solving the following linear system

$$G'(\chi^n) d = -G(\chi^n) \tag{18}$$

where $G'(\chi)$ denotes the Jacobian matrix $G'(\chi)_{ij} = \partial G_i(\chi)/(\partial \chi_i)$.

If Eq. 15 is solved neglecting the lateral gradients, the number of adjacent cells that are actually considered is maximum 2 (i.e the cell below and above). Therefore, the matrix $G'(\chi^n)$ is tridiagonal and symmetric, and then invertible with simple direct methods (El-Mikkawy and Karawia, 2006). On the other hand, if Eq. 15 is solved fully three-dimensionally M can be up to 6, and, therefore, $G'(\chi^n)$ is a symmetric and sparse matrix. Its inversion is a more complex problem (Niessner and Reichert, 1983). In this case, the linear system in Eq. 18 is solved approximatively with an iterative method, the BiCGSTAB Krylov linear solver (Van Der Vorst, 1992). This iterative process becomes an inner iteration, nested in the outer iteration defined in Eq. 17.

3 Energy exchange with the atmosphere

The heat flux exchanged with the atmosphere (S), hereafter referred to as "surface heat flux", is given by the sum of net shortwave (solar) radiation (SW), net longwave radiation (LW), and turbulent fluxes of sensible (H) and latent heat (LE), namely

$$S(T) = SW + LW(T) + H(T) + LE(T, \theta_w)$$
(19)

The surface heat flux is dependent on the temperature of the surface, which is, in turn, the unknown of the equation. In addition, the latent heat flux also depends on the soil moisture at the surface, which is a further coupling term to the water flow equation. All the fluxes in Eq. 19 are positive if they are directed towards the surface. The following section discusses how the components of the surface heat flux are calculated in the simple case of horizontal flat terrain. Then, in Section

4 the case with complex terrain is presented. Depending on the input data available, radiation components can be either assigned directly in input or calculated by the model.

3.1 Shortwave radiation

The net shortwave radiation appearing in Eq. 19 is a balance given by the incoming radiation SW_{in} from the atmosphere and the reflected radiation SW_{out} , which is given by SW_{in} multiplied by the broadband albedo.

Incoming shortwave radiation on a flat ground surface is the result of the top-of-atmosphere (SW_{toa}) shortwave radiation, and atmosphere and cloud transmissivities (respectively τ_a and τ_c):

$$SW_{in} = SW_{toa} \cdot \tau_a \cdot \tau_c \tag{20}$$

While SW_{toa} can easily be expressed with analytical formulae depending on solar height and azimuth (e.g., Iqbal, 1983), the transmissivities are more complex and uncertain to calculate. The calculation of the atmosphere transmissivity are fully described in Appendix D1.

Albedo is treated differently according to whether the ground surface is snow free or snow covered. In the former case the albedo varies linearly with the liquid water contents of the top soil layer, while, in the latter, the formulation of Dickinson et al. (1993) is used. This formulation i) accounts for the decrease of the snow reflectance with the time from the last significant snowfall, ii) partitions the spectrum into visible and near infrared components and considers different coefficients, iii) considers an increase of albedo at lower sun angles as a result of the Mie scattering properties of snow grains (Hock, 2003). In addition, snow albedo is decreased for shallow snowpacks since a significant portion of incoming shortwave radiation is actually absorbed by the soil surface (Tarboton and Luce, 1996).

3.2 Longwave radiation

The net longwave radiation in Eq. 19 is a balance of the component LW_{in} coming from the atmosphere and LW_{out} emitted by the surface. Differently from the shortwave radiation, the two components are independent and calculated separately.

The incoming longwave radiation at the surface is the integrated result of the radiation emitted at different levels in the atmosphere with different temperatures and gas concentrations. Clear-sky radiation is calculated with one of the several empirical formulations present in literature (e.g., Brutsaert, 1975a; Satterlund, 1979; Idso, 1981; Konzelmann et al., 1994; Dilley and O'Brien, 1997), which in general apply the Stefan-Boltzmann law using the air temperature measured at the surface (T_a in K) with an effective atmosphere emissivity ϵ_a (-) dependent on air temperature T_a and water vapor pressure e_a (bar), namely:

$$LW_{in,clear} = \epsilon_a (T_a, e_a) \cdot \sigma \cdot T_a^4$$
(21)

where σ is the constant of Stefan-Boltzmann $(5.67 \cdot 10^8 \text{ W})$ m^{-2} K⁻⁴). The relations in the literature differ on the expression of ϵ_a (e.g. Brutsaert, 1975a; Idso, 1981; Konzelmann et al., 1994; Prata, 1996; Dilley and O'Brien, 1997). In cloudy skies the emissivity of the atmosphere is increased to a value ϵ_c , which may be significantly higher than ϵ_a . There is a rather high uncertainty in the formulations for ϵ_c , which is evident in the spread of the results if different empirical formulations are used (e.g., Gubler et al., 2012; Flerchinger et al., 2009). In particular, the problem is more evident in case of intermediate fractional cloud covers. Most formulations for ϵ_c use information on the cloud-covered fraction of the sky (Deardorff, 1978), which is mostly obtained with visual observation. As an alternative, Crawford and Duchon (1998) proposed a direct relation between the shortwave radiation cloud transmissivity (τ_c) and ϵ_c :

$$\epsilon_c = \tau_c + (1 - \tau_c) \cdot \epsilon_a \tag{22}$$

which provides a linear interpolation between the clear sky emissivity value and the black-body emissivity in the ideal case of cloud cover completely obscuring the ground. This relation is used in GEOtop since it provides a direct estimation of ϵ_c from incoming shortwave radiation without using the cloud-cover fraction of the sky. However, τ_c is primarily affected by the cloud cover around the solar disk and not much by cloud cover far from it. Sicart et al. (2006) showed that this bias is eased if relative long time averages (such as daily) of τ_c are taken. In GEOtop this average time is set as a parameter, but normally ranges between 4 hours and 1 day. Longer average intervals reduce the cloudiness directionality bias, while shorter ones allow an estimation of the day evolution of the cloud cover. This feature is particularly useful for the estimation of τ_c during the night, which is estimated with a linear interpolation between the value before sunset and after sunrise (Gubler et al., 2012).

The outgoing longwave radiation (LW_{out}) emitted by the surface can also be calculated with the Stefan-Boltzmann law:

$$LW_{out} = \epsilon_s \cdot T_s^4 \tag{23}$$

where T_s is the temperature of the surface (K) and ϵ_s is the emissivity of the surface. The latter is set as a parameter if the surface is snow covered. Otherwise, similarly to albedo, it is interpolated between a dry and wet value according to the water content of the first soil layer (Snyder et al., 1998).

3.3 Turbulent fluxes

The turbulent fluxes of sensible (H) and latent heat (LE) are calculated with the flux-gradient relationship (Brutsaert, 1975b; Panoksky and Dutton, 1984; Garratt, 1992):

$$H = \rho_a c_p w_s \frac{T_a - T_s}{r_a} \tag{24}$$

$$LE = \beta L_e \rho_a c_p w_s \frac{Q_a - \alpha Q_s^*}{r_a}$$
 (25)

where ρ_a is the air density [kg m⁻³], c_p the specific heat at constant pressure (J kg⁻¹ K⁻¹), w_s the wind speed (m s⁻¹), L_e the specific heat of vaporization (J kg⁻¹), Q_s^{\star} the saturated specific humidity (kg kg $^{-1}$) at the surface, Q_a the specific humidity of the air, and r_a the aerodynamic resistance (-). The α and β coefficients take into account the soil resistance to evaporation, and only depend on the liquid water pressure close to the soil surface. They are calculated according to the parameterization of Ye and Pielke (1993), which considers evaporation as the sum of the proper evaporation from the surface and diffusion of water vapour in soil pores at greater depths. The aerodynamical resistance is obtained applying the theory of Monin Obukhov (Monin and Obukhov, 1954), which requires that known values of wind speed, air temperature, and specific humidity are available at least at a two different heights above the surface. Known values at only one height above the surface are sufficient if it is assumed that just above the surface (properly at zero height above the surface): i) the value of air temperature is equal to the value of soil temperature at the surface (this assumption also leads to the boundary condition non-linearity), ii) the specific humidity is equal to αQ_s^{\star} , and iii) wind speed is zero.

4 Complex terrain

Complex terrain significantly complicates the representation of the surface heat flux with respect to the ideal flat terrain case. This paragraph shows how the effects of complex terrain are taken into account in the calculation of the components of the surface heat flux.

4.1 Shortwave radiation

Incoming shortwave radiation is always partitioned in two components: a direct component that comes from the direction of the sun, and a diffuse component assumed to be isotropic. Since incoming shortwave radiation is often measured as global (i.e. sum of direct and diffuse components), it becomes important to differentiate in its direct and diffuse portions since the two components react differently to complex terrain. Erbs et al. (1982) provided an empirical expression relating k_t , the ratio of the hourly diffuse radiation to the hourly global radiation to the hourly radiation at the top of the atmosphere (namely $\tau_a \cdot \tau_c$). So far all the radiation components are relative to flat surfaces.

In complex terrain: i) the direct component is obtained multiplying the direct component for the flat surface by the ratio $\frac{\cos(\theta_n)}{\cos(\theta_v)}$, where θ_n is the angle between the normal to the surface and the direction of the sun, and θ_v the angle between the vertical and the direction of the sun (solar angle

deviation); ii) the direct component may be shaded by the surrounding topography (cast shadow) or it can happen that the angle θ_n be larger than 90 degrees (self shadow); iii) there is also a component of incoming shortwave resulting from reflections from the surrounding terrain, which are assumed to be isotropic in the terrain view angle; and iv) the diffuse radiation coming from the sky, assumed isotropic, has to be reduced according to the visible sky angle.

The incoming shortwave radiation is calculated as follows:

- Clear-sky global radiation on a flat terrain surface is obtained from Eq. 20.
- Cloud transmittance is obtained either from Eq. D5 or as the ratio of measured global radiation to clear-sky global radiation (both on a flat terrain surface).
- The diffuse and direct portions of incoming shortwave radiation on a flat ground surface are calculated according to the formula of Erbs et al. (1982). The diffuse radiation obtained is referred to as hemispheric diffuse radiation, because it considers the sky unobstructed.
- Direct radiation is corrected according to topography, accounting for shadowing and solar incidence angle.
- Diffuse radiation is calculated as two components: i) one coming from the atmosphere calculated multiplying the hemispheric diffuse radiation by the sky view factor (V_f) , which is a topographical parameter that accounts for the portion of the sky that is actually seen from a pixel and varies from 0 (sky not visible) to 1 (flat terrain case, where the sky view angle is the entire hemisphere); and ii) a second component resulting from the shortwave radiation reflected from the terrain seen from the pixel (surrounding terrain). This component can be calculated with complex algorithms that account for all pixels visible from the pixel of interest p (Helbig et al., 2009). This is not performed in GEOtop, which, instead, calculates this radiation component with either of two simple methods: either it is considered that the terrain surrounding a generic pixel p has the same outgoing shortwave radiation as p (that is $SW_{out,p}$), and, so, the radiation from the surrounding terrain is given by $(1-V_f) \cdot SW_{out,p}$ (one-dimensional approximation), or the average of outgoing shortwave radiation in a certain area is taken $(SW_{out,av})$ and the radiation from the surrounding terrain is considered as $(1-V_f) \cdot SW_{out,av}$ (two-dimensional approximation).

4.2 Longwave radiation

As for diffuse shortwave radiation, in complex terrain incoming longwave radiation comes from both the atmosphere and the surrounding terrain. The former is given by the incoming longwave radiation calculated as in the flat case multiplied by V_f . The component emitted from the surrounding terrain is

calculated with the same two methods shown for shortwave radiation.

4.3 Turbulent fluxes

The turbulent exchange in complex terrain has been observed to significantly deviate from the theory of Monin-Obukhov, which is built from the premise that terrain is flat and infinitely homogeneous (e.g., De la Casiniere, 1974). In particular, a maximum wind speed is often observed near the surface as a result of wind gravity flows, whereas according to the theory the wind profile should be logarithm (in neutral atmosphere) with a small deviation due to temperature gradients (Halberstam and Schieldge, 1981; Meesters et al., 1997; Wagnon et al., 1999). Including these effects in a model like GEOtop would require solving the Navier-Stokes equations for the wind field, which is beyond the purposes of the model. However, it has been also observed (e.g., Denby and Greuell, 2000) that if the measurements of wind, temperature and relative humidity are performed as close as possible to the surface, the conditions are actually closer to the assumptions of the theory of Monin-Obukhov. This justifies the application of the theory in GEOtop also for complex terrain.

Since meteorological variables are measured only at a limited number of locations, a statistical distribution method is required to assign meteorological forcings (wind, temperature, and relative humidity) for the surface energy balance to the whole surface. This issue is described in Appendix C.

5 Snow Cover

The snow cover plays an important role as it buffers the energy and mass exchanges between the atmosphere and soil. Important processes related to the snow cover dynamics include snow warming and cooling, melting and refreezing, water percolation, accumulation due to snow precipitation, avalanches, deposition of wind blown snow, erosion due to wind, and densification due to snow metamorphism.

The system of equations for snow is similar to the set of Equations 1 and 7 used for the soil matrix, as snow may also be considered a porous material. However, snow has the following peculiarities: a) the snow volume of control is ephemeral, i.e. it may disappear as a result of melting; b) the rigidity to the structure is given by the ice grains; c) the porosity of snow ϕ_s is variable and depends on the ice content θ_{is} ; d) the control volume is not fixed, but is subject to variations due to accumulation, compaction and melting processes; e) the capillarity effects are in general not significant (Jordan, 1991).

In GEOtop snow is computed solving in sequence: i) the heat equation, ii) snow metamorphism, iii) water percolation, iv) accumulation. The simplified effects of avalanches and blowing snow are also considered in a simplified way, but they will not be dealt with in this paper.

5.1 Snow volumetric system

Let us call V_s the control volume (m³) of snow: the sum of the liquid, solid and gaseous contents in the volume must equal 1 for continuity:

$$\theta_{ws} + \theta_{is} + \theta_q = 1 \tag{26}$$

where θ_{ws} (-) is the liquid volumetric fraction, θ_{is} (-) the solid water volumetric fraction, and θ_g (-) the gaseous volumetric fraction. Considering that the rigidity to the structure is given by the ice grains, snow porosity ϕ (-) may be calculated as the available pores excluding the ice grains, i.e.:

$$\phi_s = \theta_{ws} + \theta_g = 1 - \theta_{is} \tag{27}$$

Snow porosity is not constant as it depends on the snow metamorphism.

5.2 Heat equation

Following the approach used for the soil, the heat equation for snow becomes similar to Eq. B7, the internal energy of the snow being:

$$U_s = (\rho_i c_i \theta_{is} + \rho_w c_w \theta_{ws}) (T_s - T_{ref}) + L_f \rho_w \theta_{ws}$$
 (28)

where T_s (°C) is the snow temperature. The heat equation is solved neglecting the lateral gradients with the same numerical method used to solve the heat equation in the soil. The boundary condition at the interface with the atmosphere is given by the surface heat flux, as described in the previous section. At the interface with the soil surface the heat exchange is given by the conduction heat flux, which is dependent on the temperature gradient in proximity to the interface. This last exchange flux actually couples the heat equations in the soil and snow, which have to be solved together in a system.

A freezing characteristic curve is defined also for snow in order to derive an expression for the apparent heat capacity. However, the phase change in the snow takes place virtually at 0°C, since the pores are large enough that temperature depressions due to capillarity effects are not significant (Jordan, 1991). The definition of a freezing characteristic curve has mostly a numerical reason, therefore the curve must approach as much as possible a step function in correspondence of 0 °C. A simple relation relating temperature and the ratio between liquid water content and total water content in the snow is used (Jordan, 1991):

$$\frac{\theta_{ws}}{\theta_{ws} + \frac{\rho_i}{\rho_w} \theta_{is}} = \frac{1}{1 + (a T_s)^2} \tag{29}$$

where a (°C⁻¹) is a constant. The higher value this constant is set to, the closer to a step function the curve is, but, at the same time, the more difficult the numerical resolution is. Jordan et al. (1999) set the constant to 10^2 . However, values up to 10^5 can be assigned.

The heat flux at the soil-snow interface is calculated defining an effective thermal conductivity at the interface, and the temperature gradient calculated with the temperatures of the lowest snow layer and the top soil layer. The effective thermal conductivity is sought in a similar way as the effective thermal conductivities at the interfaces between soil layers with Eq. 5 proposed by Cosenza et al. (2003).

Similarly, the thermal conductivity of snow is calculated with Eq. 5 or other formulations (Sturm et al., 1997; Yen, 1981; Calonne et al., 2011).

5.3 Metamorphism

GEOtop describes the densification that the newly fallen snow rapidly undergoes (destructive metamorphism) as well as the slow compaction process as a result of the snow weight (overburden), using the empirical formulae of Anderson (1976), improved by Jordan (1991) and Jordan et al. (1999). The constructive metamorphism leading to new shapes of the snow crystals, like hoar layers, is not represented.

The equation describing snow densification is applied separately for each snow layer and is written as (Anderson, 1976):

$$\frac{1}{D}\frac{\partial D}{\partial t} = C_1 + C_2 \tag{30}$$

where D is the thickness of the snow layer, and C_1 and C_2 are respectively the total fractional compaction rate (s⁻¹) as a result of destructive metamorphism and overburden. Eq. 30 is integrated with the same time step Δt used for the heat equation, assuming that the snow layer has a thickness D_0 (known) at the beginning of the time step and a thickness D_1 at the end. The integration is carried out as follows:

$$\int_{D_0}^{D_1} \frac{dD}{D} = \int_{0}^{\Delta t} (C_1 + C_2) dt \tag{31}$$

which gives

$$D_1 = D_0 \exp(C_1 + C_2) \Delta t \tag{32}$$

The formulations of the compaction rates are reported in Appendix D2.

5.4 Water percolation

The equation governing the water balance in each snow layer is the second part of Eq. 7, which, considering a 1D discretisation and integrating along the vertical direction, results in:

$$\frac{\partial \theta_{ws}^{fl}}{\partial t} + \frac{J_{ws}^{up} - J_{ws}^{dw}}{D} + S_{ws} = 0 \tag{33}$$

where J_{ws}^{up} (m s⁻¹) is the incoming flux from above and J_{ws}^{dw} is the outgoing downward flux. Following Colbeck (1972),

the flux J_{ws} occurs as soon as θ_{ws} reaches a certain threshold value accounting for the capillary retention, i.e. the irreducible water saturation S_r (-), which is set as a snow porosity fraction $(S_r \cdot \phi_s)$. S_r normally ranges between 4 and 7% (Colbeck, 1972). The flux J_{ws} is calculated according to Darcy's law but neglecting the capillarity effects and using only the gravimetric gradient:

$$\begin{cases} \text{if } \theta_{ws} \ge S_r \cdot \phi_s \colon & J_{ws} = -K_s \cos \beta \\ \text{else } J_{ws} = 0 \end{cases}$$
 (34)

where β (°) is the local slope angle and K_s (m s⁻¹) is the hydraulic conductivity for snow. K_s is calculated according to the model of Brooks and Corey (1964), as in Jordan (1991):

$$K_s = K_{s,max} S_e^3 \tag{35}$$

where $K_{s,max}$ (m s $^{-1}$) the maximum hydraulic conductivity for the snow, and S_e (–) is the effective saturation, which is given by

$$S_e = \frac{\theta_{ws} - S_r \cdot \phi_s}{\phi_s - S_r \cdot \phi_s} \tag{36}$$

The maximum hydraulic conductivity may significantly vary with snow properties and aging, however, a constant value of $5 \cdot 10^{-3}$ m s⁻¹ is used, which is typical for an isothermal snowpack according to Shimizu (1970).

The water flux in an isothermal snowpack is usually very fast, as a result of the high porosity of snow. On the other hand, in non-isothermal snowpacks water may percolate into a cold snow layer and be there refrozen. This has the net effect to slow down the percolation process. Therefore, the hydraulic and thermal control on water percolation have significantly different time scales. The water flow is then calculated in an uncoupled way in the following steps: i) the heat Equation (1) for the snow cover is solved assuming that the liquid water does not move, obtaining a "static" solution; ii) the incoming water flow from above is added (also rain for the upper layer); iii) the internal energy of the snow is adapted, assuming that there is an instantaneous energy mixing that may lead to the partial or complete refreezing of the liquid water: the energy state of the snow corresponding to an internal energy content equal to the sum of the internal energy content of the inflowing water (in terms of latent heat) and that of the snow before it receives the liquid water flux calculated; iv) finally the outgoing downward water flux is calculated with the new state variables.

5.5 Accumulation

In most cases, precipitation data is given only as total precipitation. The most common method for splitting this into rain and snow (e.g., US Army Corps of Engineers, 1956; Auer, 1974) is to define two air temperature thresholds: a higher value above which precipitation is only rain, and a

lower value below which precipitation is only snow (Kienzle, 2008). Garen and Marks (2005) proposed to use dew temperature instead, as the temperature interval in which both rain and snow precipitation are coexistent is in this case much smaller, so that just one threshold value can be defined. In GEOtop both methods are available where the threshold temperatures are set as parameters (for air temperature normally around -1°C and 3°C) and in between a linear interpolation is performed.

Fresh snow density depend on grain size and crystal type, as they affects the way fresh snow is deposited. Smaller grains with simpler shape pack more efficiently and lead to denser snow. These effects, however, are indirectly described parameterising the density in function of air temperature and wind, which are easier to measure and have been correlated to fresh snow density in several studies (e.g., McGurk et al., 1988). The following formula proposed by Jordan et al. (1999) is used, which incorporates both temperature and wind effects

$$\rho_{ns} = \begin{cases} 500 - 475.5 \, \exp\left[-1.4 \left(5.0 - T_a\right)^{-1.15} - 8 \cdot \frac{w_s^{1.7}}{1000}\right] \\ \text{if} \ T_a > 13^{\circ}\text{C} \\ \\ 500 - 452.0 \, \exp\left[-8 \cdot \frac{w_s^{1.7}}{1000}\right] \quad \text{elsewhere} \end{cases}$$

where ρ_{ns} is the density of the new snow (kg m⁻³).

5.6 Discretisation

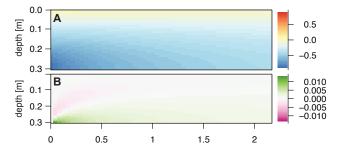
The snowpack, according to the thermal gradients, may be roughly classified into three regions: an upper, middle, and bottom portion. In the upper and bottom regions the vertical gradients are often high, as a result of the interactions with the atmosphere and the underlying soil respectively. On the other hand, in the middle region the vertical gradients are weaker. The snow discretisation in GEOtop is done in order to accurately describe the thermal gradients in the snowpack and avoid the allocation of unnecessary memory. The total number of layers, in fact, depends on the mass of snow present, whereas the distribution of layers in the snowpack privileges the upper and bottom zones.

The details of the snow discretisation scheme is reported in Appendix D3. Dall'Amico (2010) provides a test case of the snow discretization comparing the surface temperature of the previous and the new discretisation scheme.

6 Testing GEOtop

To add credibility to the results of the subsequent experiment, we demonstrate here that GEOtop produces plausible results in its major components.

Temperature and temperature differences [°C]



Total water content and total water content differences [-]

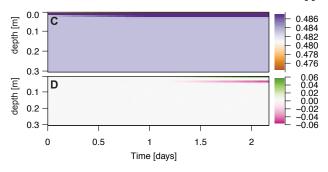


Fig. 1. Evolution of temperature (A) and total water content (C) for simulations with a time step of 1 second. The difference to the solutions with a time step of 1 hour are also shown for temperature (B) and total water content (D) based on subtracting the hourly solution from the 1-second solution.

6.1 Time-lagged vs coupling solution

The error due to linking the heat and water flow equations in a time-lagged manner instead of fully numerically coupling is here evaluated experimentally. For this purpose, we initialise a 0.3 m deep column of sandy loam with a uniform pressure head of -0.1 m and a linear temperature profile between 0 °C at the top and -1 °C at the bottom. No energy and water is exchanged with the outside. Running this simulation over time, the temperature of the soil column will approach a uniform value and pressure gradients due to freezing will redistribute water. Finally, to estimate the magnitude of error inherent in using a linked solution, we compare results based on time steps of 1 second and 1 hour. The temperature and total water content (i.e. liquid and frozen) as well as deviations between both simulations are shown in Fig. 1. As the deviations in temperature are negligible and those in liquid water are on the order of $\pm 6\%$, the linked solution is deemed acceptable in this context.

6.2 Frozen soil scheme

The performance of the frozen soil model has been evaluated by comparison with analytical solutions and experimental results by Dall'Amico et al. (2011a).

6.3 Snow model

The performance of GEOtop with respect to snow has been evaluated using the data published by Morin et al. (2012) at Col de Porte, a mountain pass in the French Alps at 1326 m a.s.l. near Grenoble. The model was driven by hourly measured near-surface meteorological data: air temperature, relative humidity, downwelling shortwave and longwave radiation, wind speed, air pressure and precipitation provided by the Meteo France weather station located at the pass. The simulation was performed with standard parameters without improving the results by trial and error or fitting. Similar to the evaluation of the snow simulator CROCUS (Brun et al., 1992) by Vionnet et al. (2012), we quantify performance based on daily averages of snow depth and water equivalent using the bias and the root mean squared deviation (RMSD) for the months December to May during the years 2001 to 2011. Fig. 2 reports the results for the year 2001/2002. The other years as well as the parameter file used are available in the Supporting Material (respectively GEOtop-ColDePorte.pdf and GEOtop.inpts.ColDePorte). For snow water equivalent, we obtain a RMSD of 37.1 mm (39.7, 37.0 mm) and a bias of -3.2 mm (-17.3, -2.3 mm). For snow depth, the RMSD is 0.15 m (0.11, 0.13 m) and the bias is 0.07 m (-0.01, 0.08 m). For comparison, the range of values reported for two different versions of Crocus (Vionnet et al., 2012) are given in brackets. Based on visual inspection, soil temperatures below the snow cover are represented reasonably well.

6.4 Complex topography and temperature

In order to demonstrate the performance with respect to topography, we used near-surface temperatures measured in steep bedrock that accumulates nearly no snow. The sites chosen for this demonstration are two contrasting sites: "Jungfrau ridge south" and "Jungfrau ridge north" (PER-MOS, 2009), positioned at a horizontal distance of about 20 m, the first is sun-exposed and the latter is shaded, resulting in a mean annual temperature difference of nearly 8 °C. Both sites are located in proximity to Jungfraujoch, a mountain pass in the Swiss Bernese Alps at 3470 m a.s.l.. Horizon shading and sky view factor are parameterised based on fish-eye photography (Gruber et al., 2003). The simulations are driven by air temperature, relative humidity, wind speed, wind direction and global radiation from the SwissMetNet station Jungfraujoch. This driving station has a horizontal distance of about 1.2 km to the rock temperature measurements and is about 150 m lower in elevation. Air temperature measurements have been extrapolated using the standard lapse rate of 0.0065 °C/m. No snow cover is simulated. The results are reported in Fig. 3 and the parameter file used is available in the Supporting Material (GEOtop.inpts.JungfrauJoch). Based on the comparison with around 50,000 hourly measurements at each loca-

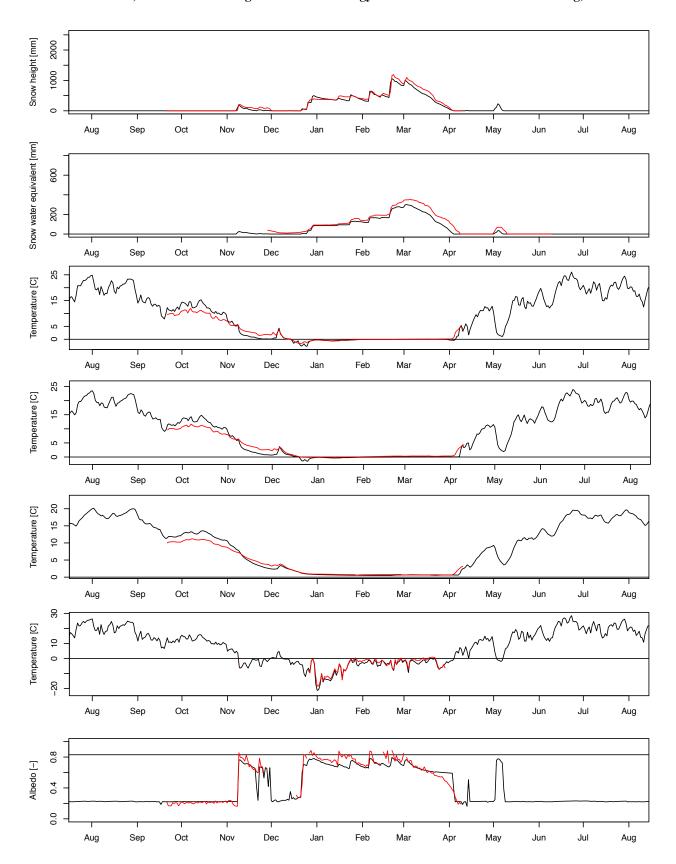


Fig. 2. Snow model testing: comparison of measured (red line) and simulated (black line) results at Col de laPorte (Morin et al., 2012) in the year 2001-2002. Starting from top to bottom, snow height, snow water equivalent, soil temperature at 10 cm depth, 20 cm depth, 50 cm depth, ground surface temperature and albedo comparisons are reported.

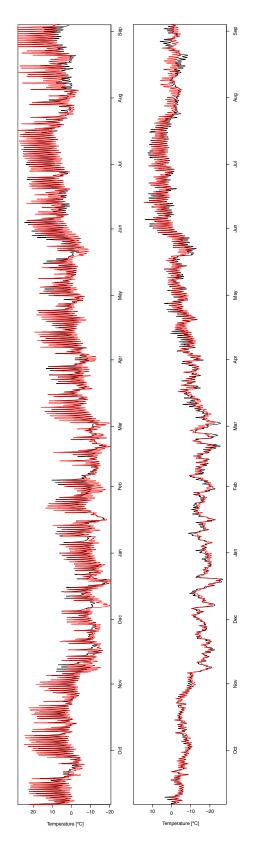


Fig. 3. Temperature in complex topography: comparison of measured (red line) and simulated (black line) results at Jungfrau ridge south (left) and north (right) during year 2005/2006. Measured data are taken from PERMOS (2009).

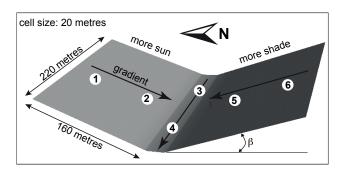


Fig. 4. Synthetic catchment and location of points analysed. The converging topography has a sun-exposed and a more shaded side. It is varied with respect to the inclination angle of its hillslopes β . Channel inclination, in the direction from point 3 to 4, is always 5° .

tion (south/north), we obtain a bias of -0.63/-0.68 $^{\circ}$ C and a RMSD of 4.37/2.01 $^{\circ}$ C.

6.5 Sensitivity study

The work of Gubler et al. (2013) demonstrates the robustness of GEOtop as it is built on more than two million highly diverse simulations that converged. This study further revealed that the sensitivity of ground temperatures to changes in temporal of spatial discretisation are moderate, and that equilibria independent of initial conditions can be reached reliably.

7 Simulation experiment

In order to demonstrate the relevance of the modelling approach, GEOtop has been run in a catchment made up of two hillslopes forming a convergent topography (Fig. 4). Different simulations have been set up that differ in i) topography, and ii) model configuration with respect to the water balance. It is considered a gravel soil with a saturated hydraulic conductivity of 0.002 m s⁻¹, thermal conductivity (of the soil matrix) of 2.5 W m⁻¹ K⁻¹, θ_r = 0.057, θ_{sp} = 0.487 and the following Van Genuchten parameters: $\alpha = 2.0 \text{ m}^{-1}$ and n= 1.8. The soil has been discretized with 80 layers: the first 4 layers starting from the surface have thicknesses ranging from 0.01 to 0.08 m, in consideration of the high vertical gradients of temperature and water pressure, the lowest 15 layers have thicknesses ranging from 0.2 to 0.5 m whereas the remaining layers have thickness of 0.1 m. Overall, the soil domain reaches a depth of 10.5 m. The surface has been represented with square pixels of a dimension of 20 m.

Topographical differences have been created by varying the inclination angle of the lateral slopes (β in Fig. 4) from 5° to 20°. The longitudinal slope (from point 3 to 4 in Fig. 4) of 5° and the average elevation (3000 m) are kept constant. The two topographies are hereafter referred to as 5° and 20° topography, respectively.

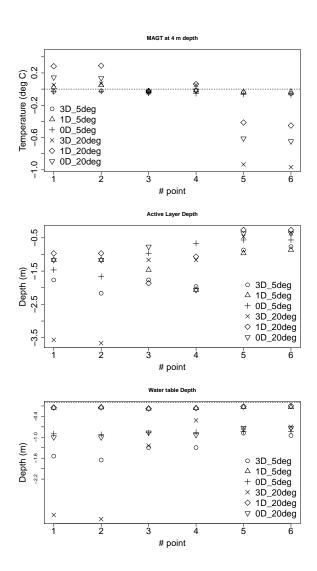


Fig. 5. Mean annual ground temperature at a depth of 4 m, active layer depth, and water table depth for the six points shown in Fig. 4 given by the six simulations that have been performed.

The following water balance configurations, which are here referred to for simplicity as 3D, 1D, and 0D, are considered. 3D means that the full three-dimensional variably saturated Richards equation with the surface flow is used. In 1D, the Richards equation is solved only in one-dimension, i.e. in the vertical, and no lateral subsurface drainage is considered. Surface flow occurs as lateral flow only on the surface. In 0D, the soil water balance is not solved, and no infiltration is described. Therefore, the total water content always remains at its initial value, however, soil water will undergo freezing and thawing.

Six simulations have been then performed: 5° (topography) 3D, 5° 1D, 5° 0D, 20° 3D, 20° 1D, and 20° 0D. They have been run for the hydrological year 2001–2002 (from 1 October 2001 to 30 September 2002) using meteorological

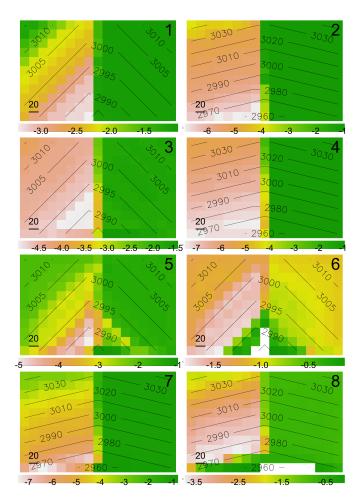


Fig. 6. Distributed results: active layer depth for the simulations 5° 0D (1), 20° 0D (2), 5° 1D (3), 20° 1D (4), active layer depth (5) and mean annual water table depth (in metres) (6) for the simulation 5° 3D, and active layer depth (7) and mean annual water table depth (8) for the simulation 20° 3D. All depths and the scale are in metres, and the elevations in metres above sea level. Consistently with Fig. 4, North is towards the left, and the left and right slopes have respectively a south and north aspect.

data measured at the station of Davos, Switzerland, located at 1595 m a.s.l. and operated by Meteoswiss. Air temperature was extrapolated using the standard lapse rate of 0.0065 K m⁻¹. This year was chosen because it is the most similar to the average year in the 1981–2010 period, if the cumulated winter precipitation (from October to May) and the average air temperature in the summer (from June to September) are considered. The first quantity represents a proxy for snow precipitation and the second one approximates summer warming. Respective values are 452 mm and 10.6 °C for the hydrological year 2001–2002, and 479 mm and 10.6 °C for the average year in the period 1981–2010 period.

The system was initialized considering an absence of snow cover, uniform soil temperature of -1 °C, and soil deeper

than 1 m saturated, and hydrostatic pressure profile in both the saturated and unsaturated portions (prolonging the hydrostatic pressure profile also for negative pressures). However, in order to reduce the influence of the arbitrariness of the initial condition, a spin-up simulation has been performed for 100 years. At the end of the spin-up the catchment is still completely underlain by permafrost, with active layer depths ranging from 1 to 7 m. Since the response time of permafrost soil is extremely slow, a longer spin-up simulation would probably enhance the spatial variability of the active layer depth and completely thaw permafrost in some part of the catchments. However, a 100 years spin-up is considered acceptable in this context, since we are mainly interested in the approach evaluation.

In order to evaluate the set of simulations the following steps are followed: i) annual average variables in the single points shown in Fig. 4 are compared, ii) annual average distributed variables are compared and their spatial distribution in the catchment discussed, and iii) the time evolution of some variables for a selected point is shown. Figure 5 shows the mean annual temperature at a 4 m depth, the active layer depth (considered as the lowest depth of thaw reached during the summer), and the annual average water table depth (the average was calculated only when there is actually a water table) for the six points for the six simulations. Point 1 and 2 are both on the south slope at short distance apart and have very similar temperature values, but the different topographies and water balance descriptions give significantly different values of temperatures, which range between +0.3°C (permafrost thawed) and slightly negative values (permafrost still present at a 4 m depth). The active layer and water table depth show significant differences in the simulations (of the order of 1-2 m), with slightly deeper values for Point 2, which is downstream. Point 3 and 4 are located in the channel portion and also exhibit similar values. The results of the six simulations give temperature ranges between slightly positive and slightly negative values and differences of the order of 1-2 m in active layer and water table depths. Points 5 and 6 are located in the north slope and result significantly colder than the other points, with temperatures ranging from -1°C and slightly negative values, and active layer and water table depths ranging from 0.3 m to 1 m. It is therefore important to notice that both different topographies and different hypotheses on soil water balance have a significant effect on the results.

Figure 6 shows the spatial distribution of the active layer depth and the depth of thaw. If the water balance is not solved (0D simulation), the spatial variability of the active layer is given by aspect and elevation only. In the north slope the values are rather homogeneous around 1 m, while in the south slope they are significantly dependent on altitude, ranging from 1 m at the top to 3 m at the bottom for the 5° topography, and from 4 m to 7 m for the 20° topography. If the water balance is solved 1D, the effect of altitude and aspect is attenuated, and the spatial variability reduced. If a full 3D water

balance is considered, a clear relation between active layer depth and water table can be recognized. Where water table is shallower and, therefore, soil is wetter, the active layer is deeper. In the 5° topography, the water table at the lowest elevations of the south slope is at the surface. For mid elevations water table depth reaches a maximum value of about 2 m, and then for higher elevations it decreases to values of about 1-1.5 m. This is probably a consequence of the strong dependance of active layer on elevation. However, the active layer depth has a larger spatial variability than in the 0D water balance case, since it reaches values up to 5 m at the bottom of the south slope (instead of 3 m) and up to 2.5 m at the bottom of the north slope (instead of 1 m). This is probably a result of the interplay between soil moisture and freezingthawing energetics, which is added to the spatial variability induced by slope and aspect. The 20° topography has similar features, but the lateral drainage in this steeper topography adds active layer spatial variability in a lesser degree than in the 5° topography.

Figure 7 shows the temporal evolution of temperature, and liquid, solid and total water content in soil and snow for point 1 shown in Fig. 4. All charts also report the lower and upper boundaries of the thawed layer, and the water table. Temperature is in general negative and close to 0 °C except at the surface. The soil is completely frozen from mid December to mid June, and the thawed portion reaches the maximum depth in mid September, which is kept until almost mid November, when the freezing front from above, starting in October, gets significantly low. The charts of liquid water, ice and total water content show that three regions, from top to bottom, can roughly be distinguished: i) a region relatively rich in total water at the top (hereafter referred to as "wet region"), ii) a drier region in the lower portion of the active layer ("dry region"), and iii) the "undisturbed frozen region" below. The wet region starts to develop in the autumn when the active layer starts freezing and is initially bordered below by the freezing front. It gets then wetter as a result of early snow melting and, probably, water transfer from slightly warmer wet region below. Liquid water content is low (< 0.1) and ice content is high (> 0.3) when the wet region is frozen, and temperature is significantly low (around -2 °C). When the wet region thaws in the summer it gets even wetter as a result of infiltration. However, thawing takes place at a relatively slow rate in this region, as a result of the high ice content and, therefore, the high energy content required to melt it. The dry region has slowly lost the initial water content in many years due to the lateral drainage during the summer. When the thawing front reaches this region in late summer, the thawed soil depth sharply increases because the energy required to thaw the soil is relatively low. At the same time a large amount of liquid water is drained from the wet region above, which virtually disappears. This amount of liquid water is gradually drained horizontally, and it eventually accumulates in a thin layer in the lower part of the region. This layer gets thinner as the season progresses, but

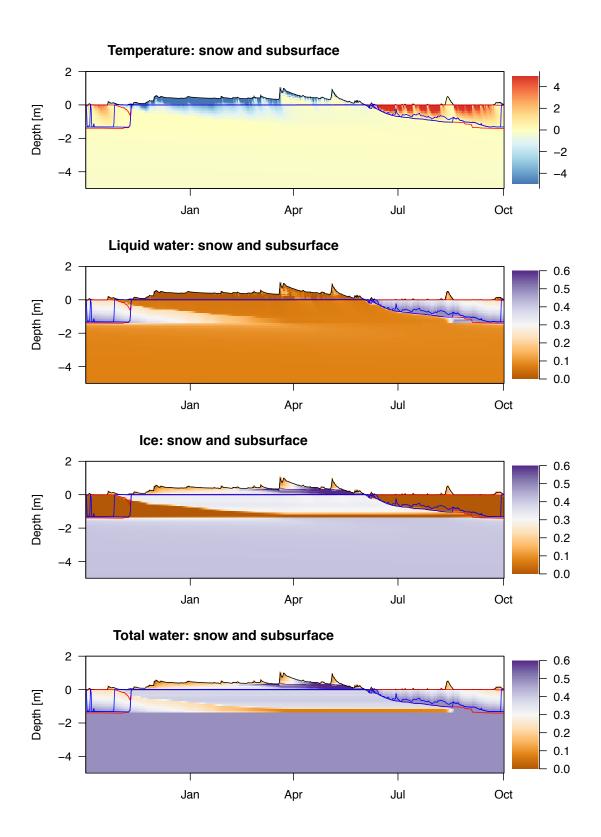


Fig. 7. Time evolution of temperature, and liquid, solid, and total water content for soil and snow in Point 1, as shown in Fig. 4, for the simulation for the 5° topography 3D. The blue line indicates the water table, while the lower and upper borders of the thawed layer are shown in red. Negative depths correspond to soil, and positive depths to the snow cover.

it does not immediately disappear when the region freezes in early winter, as a result of relatively high (though negative) temperature. The undisturbed region below was never affected by summer thawing, and the total water content is still dependent on the initial condition. Even though a spin-up simulation has been performed repeating for 100 years the meteorological data corresponding to the hydrological year 2001-2002, it is not guaranteed that an equilibrium state has been reached, and, therefore, a longer spin-up simulation could entail different conditions.

8 Conclusions

GEOtop 2.0 describes the energy balance in the soil and snow taking into account the interactions with the atmophere and solves a fully three-dimensional form of the water flow equation. It uses a simplified, but physically consistent parameterisation of the soil water retention curve to describe soil freezing characteristics in saturated and unsaturated conditions. In its numerical implementation, GEOtop 2.0. uses sophisticated integration methods, which allow convergence even in cases where parameters have nearly discontinuous behaviour, and results in proper conservation of mass and energy. This allows the investigation of complex hydrologic phenomena in cold regions for which no compound parameterization may exist.

The model has shown a consistent physical realism, and the comparison with snow cover data has resulted in a reasonable agreement. An experiment with varying model structure, carried out by differing the treatment of water transport in the soil, has highlighted that significant differences of temperature, water fluxes, and water table depths can result from this. Furthermore, the spatial differentiation of these results in response to topography highlights the complex nature of the phenomena investigated and represented.

GEOtop 2.0 represents a wider range of processes in the water and the energy budgets at fine scales than most other simulators. It thus allows studying their interactions without introducing "ad hoc" solutions that may compromise the representation of complexity. In this publication, we have described the details and functioning of fine scale hydrology and its interaction with frozen soil and snow cover. However, the model could be applied for a much wider range of environments and scientific issues.

Appendix A

Use and license of GEOtop

GEOtop 2.0. is provided with a GNU General Public License, version 3 (GPL-3.0). The source code, a first version of the manual (Dall'Amico et al., 2011b), and some template simulations are available through google code at the address: https://code.google.com/p/geotop/. Gubler et al.

(2013) provide a good starting point for the selection of many parameter values, however, optimal choices and sensitivities may differ from application to application.

Appendix B

System of equations

The Equations representing the water and energy balance in a soil matrix, as outlined in Dall'Amico et al. (2011a), are respectively:

$$\frac{\partial \theta_w}{\partial t} + \frac{\rho_i}{\rho_w} \frac{\partial \theta_i}{\partial t} + \nabla \bullet \boldsymbol{J}_w + S_w = 0$$
 (B1)

$$\frac{\partial U}{\partial t} + \nabla \bullet J + \nabla \bullet G + S_{en} = 0$$
 (B2)

where all the symbols are described in the Table D3. The variation of the water content θ_w and internal energy U may be divided into the component due to "phase change" (superscript "ph") and the component due to water "flow" (superscript "fl"):

$$d\theta_w := d\theta_w^{fl} + d\theta_w^{ph} \tag{B3}$$

$$dU := dU^{ph} + dU^{fl} \tag{B4}$$

According to this assumption, Equations B1, after some rearrangements, becomes:

$$\frac{\partial \theta_w^{ph}}{\partial t} + \frac{\rho_i}{\rho_w} \frac{\partial \theta_i}{\partial t} = -\left(\frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet \boldsymbol{J}_w + S_w\right)$$
(B5)

Equalizing the both members of the Equation B5 to a common value, say zero, eventually one obtains an equivalent system for the water balance equation:

$$\begin{cases} \frac{\partial \theta_w^{ph}}{\partial t} + \frac{\rho_i}{\rho_w} \frac{\partial \theta_i}{\partial t} = 0\\ \frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet \boldsymbol{J}_w + S_w = 0 \end{cases}$$
(B6)

The components "fl" and "ph" of the internal energy may be derived starting from the definition of the internal energy U (Dall'Amico et al., 2011a):

$$U = C \cdot (T - T_{ref}) + L_f \rho_w \theta_w \tag{B7}$$

where $C:=\rho_{sp}c_{sp}(1-\theta_{sp})+\rho_ic_i\theta_i+\rho_wc_w\theta_w$ is the volumetric heat capacity (J m $^{-3}K^{-1}$). Differentiating Eq. B7 one obtains:

$$dU = C dT + (T - T_{ref})dC + L_f \rho_w d\theta_w =$$

$$= C dT + \rho_i c_i d\theta_i (T - T_{ref}) + u_f d\theta_w$$
(B8)

where:

$$u_f := \rho_w \left[L_f + c_w (T - T_{ref}) \right]$$
 (B9)

From the first Equation in B6 the variation of the ice content may be referred to the variation of θ_n^{ph} :

$$d\theta_i = -\frac{\rho_w}{\rho_i} d\theta_w^{ph} \tag{B10}$$

Substituting Eq. B3 and Eq. B10 in Eq. B8, after some calculations, it is obtained:

$$dU = C dT + \rho_w \left[L_f + (c_w - c_i)(T - T_{ref}) \right] d\theta_w^{ph} + u_f d\theta_w^{fl}$$
(B11)

where one can define:

$$dU^{ph} := C \ dT + \rho_w \left[L_f + (c_w - c_i)(T - T_{ref}) \right] d\theta_w^{ph}$$
(B12)
$$dU^{fl} := u_f \ d\theta_w^{fl}$$
(B13)

The flux J is the heat advected by flowing water and equals to:

$$\boldsymbol{J} = u_f \cdot \boldsymbol{J}_w \tag{B14}$$

Substituting B4 and B13 in Eq. B2 and considering that $\nabla \bullet J = u_f(\nabla \bullet J_w)$ one obtains:

$$\frac{\partial U^{ph}}{\partial t} + \nabla \bullet G + u_f \left(\frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet J_w \right) + S_{en} = 0 \quad (B15)$$

From the second Eq. of B6:

$$\frac{\partial \theta_w^{fl}}{\partial t} + \nabla \bullet \boldsymbol{J}_w = -S_w \tag{B16}$$

Eventually Eq. B15 becomes:

$$\frac{\partial U^{ph}}{\partial t} + \nabla \bullet G + S_{en} - u_f S_w = 0$$
(B17)

Appendix C

Distribution of meteorological data

In the GEOtop code a complete set of routines finalized at the spatial interpolations of meteorological variables. Air temperature is distributed according to Liston and Elder (2006a). All the measurements at different elevations are converted into values corresponding to a unique reference elevation according to a spatially constant lapse rate, which can however vary in time. The obtained values are spatially interpolated with the geostatistical method of Barnes (1964). On the interpolated temperature field, still referred to the reference elevation, the elevation correction given by the lapse rate multiplied by the difference between actual elevation and reference elevation, is applied. Relative humidity is converted into dew temperature, and the same interpolation method used for air temperature is used with a dew temperature lapse rate, which is normally smaller than the air temperature lapse rate

(Liston and Elder, 2006a). Precipitation is also distributed with the same method. An adjustment factor considering the dependence of precipitation on the elevation, in analogy to lapse rate for air temperature, is also included and calculated according to Thornton et al. (1997).

Wind speed is an important factor affecting the value of the fluxes. In order to describe the effect of topography on the surface energy balance it is important to consider in the model a topographically-dependent wind field. A full resolution of the fluid dynamic equations would be too computationally heavy for GEOtop. The wind field is instead parameterised using topography (Liston and Elder, 2006a). In particular, the parameterisation is implemented correcting the wind speed with factors depending on slope and curvature of the surface:

$$w_s = w_{s0}(1 + c_s S + c_c C) \tag{C1}$$

where w_s is the wind speed modulus, w_{s0} the wind speed modulus ideally unaffected by topography, S the slope of the curve given by the intersection of the surface and by a vertical plane oriented in direction of the wind, C the curvature of the same curve, and c_s and c_c are calibration parameters. Wind direction is corrected according to Ryan (1977) in order to represent wind skirting round topographic obstacles.

Recently GEOtop has been also enabled to exploit MeteoIO (http://models.slf.ch/p/meteoio/), a library developed by the Snow and Avalanche Research institute of Davos (Switzerland) aimed at caching, filtering, resampling and spatial interpolating meteorological variables.

Appendix D

Modeling details

D1 Atmospheric transmissivity

The atmosphere transmissivity is here defined as the ratio of the clear-sky incoming shortwave on a flat surface to SW_{toa} , and is calculated following Meyers and Dale (1983):

$$\tau_a = \tau_R \tau_q \tau_w \tau_{aer} \tag{D1}$$

where τ_R is the transmission coefficient after Rayleigh scattering, τ_g after absorption by permanent gases, τ_w after absorption by water vapor, and τ_{aer} after absorption and scattering by aerosols. These coefficients are expressed as follows, respectively from Atwater and Brown (1974), McDonald (1960), and Houghton (1954):

$$\tau_R \tau_g = 1.021 - 0.084 \left[m_o \left(9.49 \cdot 10^{-4} \cdot p + 0.051 \right) \right]^{0.5} (D2)$$

$$\tau_w = 1 - 0.077(wm_o)^{0.3} \tag{D3}$$

$$\tau_{aer} = 0.95^{m_o} \tag{D4}$$

where p is the air pressure (in [bar]), m_o is the optical air mass (the length of the path through the atmosphere to sea

level traversed by light rays), and w is the precipitable water (in [cm]) at sea-level pressure (total amount of water vapour in the zenith direction from the sea level to the top of the atmosphere).

The cloud transmissivity is defined as the ratio of the variably cloudy-sky to the clear-sky incoming shortwave on a flat surface, and is a complex function of cloud cover fraction, heights, and types. In GEOtop, this variable is calculated a posteriori from the available measurements of incoming shortwave radiation and also used as a measure of cloud cover in the calculation of incoming longwave radiation, which is not frequently available from measurements. In the few cases when measurements of incoming shortwave radiation are not available and a visual estimation of the cloud cover fraction is available, the cloud transmissivity is obtained from the simple formulation of Kimball (1928), namely

$$\tau_c = 1 - 0.71 \cdot c \tag{D5}$$

where c is the cloud cover fraction, from 0 (clear sky) to 1 (overcast sky).

D2 Snow metamorphism compaction rates

The total fractional compaction rates are given by Anderson (1976) eventually modified by Jordan et al. (1999):

$$C_1 = -\alpha_s \exp\left(-0.04 \cdot T_s\right) \tag{D6}$$

where α_s equals to:

$$\begin{cases}
\alpha_{s} = -2.778 \cdot 10^{6} \cdot c_{3} \cdot c_{4} \\
\text{if } \rho_{i}\theta_{is} \leq 100: \ c_{3} = 1 \\
\text{if } \rho_{i}\theta_{is} > 100: \ c_{3} = \exp\left[-0.046(\rho_{i}\theta_{is} - 100)\right] \\
\text{if } \rho_{w}\theta_{ws} = 0: \ c_{4} = 1 \\
\text{if } \rho_{w}\theta_{ws} > 0: \ c_{4} = 2
\end{cases}$$
(D7)

The above equation states that a compaction of 1% per hour (Anderson, 1976) is present at a snow density smaller than or equal to $100~{\rm kg~m^{-3}}$ (cutoff density) at $0^{\circ}{\rm C}$ and without liquid water. If liquid water is present, the coefficient is increased by 50%. For densities larger than the cutoff density, α_s decreases very rapidly, becoming one tenth at a density of $150~{\rm kg~m^{-3}}$ and one hundredth at $200~{\rm kg~m^{-3}}$. Furthermore, the compaction decreases with snow temperature, and at a temperature of about -17 °C it is two times as much as the value at a temperature of $0~{\rm ^{\circ}C}$.

The parameter C_2 is related to the ratio between the weight of the overlying snow column P_s (N m⁻²) calculated at the centre of the considered snow layer and the snow viscosity η (N s m⁻²):

$$C_2 = -\frac{P_s}{\eta} \tag{D8}$$

where

$$\eta = 3.6 \cdot 10^6 \exp(-0.08 \cdot T_s) \cdot \exp(0.021 \cdot \rho_{sn})$$
 (D9)

being $\rho_{sn} := \rho_i \theta_{is} + \rho_w \theta_{ws}$ (kg m⁻³) the snow density.

Densification takes place also when melting occurs. When ice melts in a specific snow layer, it is considered that the thickness of the layer reduces proportionally to the ice content. This makes sense, as the snow depth is a result of the ice grains structure. This leads to an increase in density, since the same total water content will occupy a smaller volume. Densification occurs also when liquid water starts to refreeze and the new ice will fill the empty pores. On the other hand, a snow layer may be subject to a density decrease as a result of the percolation process, because the total water volume in the layer will decrease, but not its volume. All these processes are also included in the model.

Another snow densification process is related to wind loads. When the wind speed is higher than a threshold (set to the wind value at which snow starts to be drifted), the wind load is considered as an additional overburden. This describes the snow packing at the surface, which leads to a progressive resistance to being drifted (Liston and Elder, 2006b).

D3 Snow discretization

The mass of snow per unit area (kg m⁻²) present in a snow layer l is referred to as M_l , and the total mass of snow per unit area present in the snowpack is named M_{tot} . GEOtop requires four parameters to set the snow layering scheme:

- M_{up}^* and M_{dw}^* (kg m⁻²), which are the maximum mass per unit area of the snowpack in the upper and bottom regions, respectively;
- M_l^* (kg m $^{-2}$), which is the maximum admitted mass for a single layer (it must be $M_l^* \leq M_{up}^*$ and $M_l^* \leq M_{dw}^*$);
- N_{mid}^* (-), which is the maximum number of layers admitted in the middle region.

As described in Table D1, the number of regions used to describe the snowpack depends on M_{tot} : i) if $M_{tot} < M_{up}^*$, only the upper region is used, which extends throughout the whole snowpack; ii) if M_{tot} is larger than M_{up}^* , but smaller than $M_{up}^* + M_{dw}^*$, also the bottom region is created with mass $M_{tot} - M_{up}^*$; iii) if $M_{tot} > M_{up}^* + M_{dw}^*$, then also the middle region is defined.

At each time step the layers are re-organized (in number, thickness, mass content and internal energy) according to the evolution of the snowpack. In particular, as outlined in Table D2, three processes may occur:

Table D1. definition of snow discretisation regions

case	upper	middle	bottom
$0 < M_{tot} \le M_{up}^*$	X	/	/
$M_{up}^* < M_{tot} \le M_{up}^* + M_{dw}^*$	X	/	X
$M_{tot} > M_{up}^* + M_{dw}^*$	X	X	X

Table D2. Available processes in a layer and triggering condition

operation	region	triggering condition
layer splitting layers merging layers merging	upper region middle region all	$ ho_{ns}D>M_l^*$ new snow & $N_{mid}>N_{mid}^*$ melting in one time step

- Layer splitting: if the mass of the top snow layer as a result of new snow accumulation exceeds the maximum allowed mass $(M_l > M_l^*)$, then it is split in two layers in such a way that the lower new layer keeps a mass equivalent to M_l^* and the new surface layer has the remainder of the mass. In case the total mass of the upper region exceeds the threshold M_{up}^* , then the lower layer is pushed to the middle or lower region.
- Layers merging: two adjacent layers may be merged into one layer that will have the sum of ice and liquid water content of the layers to merge, and temperature resulting from the energy content given by the sum of the energy contents of the layers to merge. Layer merging happens in the following cases: i) if the number of layers of the middle zone N_{mid} exceed N_{mid}^* , then two adjacent layers of the middle zone are merged. The choice falls on the two adjacent layers that have the smallest combined mass: this allows keeping the layers in the middle region of similar snow mass content and prevents from excessively smoothing the snow vertical profile; ii) if a snow layer completely loses its ice mass in a one-time-step integration of the heat equation, the snow layer that would disappear is merged with the underlying layer and then the heat equation is re-integrated.

Acknowledgements. This study was funded through the nanotera.ch project X-Sense. Model experiments were supported by the AAA/SWITCH funded Swiss Multi Science Computing Grid project (www.smscg.ch) with computational infrastructure and support. Customized libraries (gGEOtop and GC3Pie) and user support were kindly provided by GC3: Grid Computing Competence Center (www.gc3.uzh.ch). The International Foundation High Altitude Research Stations Jungfraujoch and Gornergrat supported field work for rock temperatures near Jungfraujoch. We acknowledge MeteoSwiss for providing driving climate time series at Corvatsch and Davos. Many people participated directly or indirectly in many

development phases of GEOtop during the last decade. The keywords method actually used in GEOtop I/O had a first realisation with work of Emanuele Cordano; Glen Liston gave the code of his MicroMet model in FORTRAN from which derives the actual improved code used in GEOtop. Thomas Haiden offered the C code for estimating direct solar radiation and shadows, which was subsequently further tested, modified and embedded in GEOtop. Matteo Dall'Amico thanks the Monalisa project financed by the Autonomous Province of Bolzano that supported his work on GEOtop. Riccardo Rigon thanks the HydroAlp project of the Autonomous Province of Bolzano that supported his work. The authors thank Stefano Cozzini (Exact lab, Trieste, Italy), Gianfranco Gallizia and Angelo Leto for their help as computer scientists in the implementation of GEOtop 2.0.

Table D3. Table of symbols for soil balance and surface and subsurface water flow equations

Symbol	Name	Value or Range	Unit
\overline{t}	time		S
T	temperature		$^{\circ}C$
$ ho_w$	density of liquid water in soil	1000	${ m kg}~{ m m}^{-3}$
ρ_i	density of ice	918	${\rm kg~m}^{-3}$
ρ_{sp}	density of soil particles		${ m kg}~{ m m}^{-3}$
θ_w	fraction of liquid water in soil		dimensionless
θ_i	fraction of ice in soil		dimensionless
z_f	elevation with respect to a reference		m
z_0	elevation at the soil surface		m
z	position in the soil column along the vertical		m
Δz_l	depth of the cell l		m
g	gravity acceleration	9.81	$m s^2$
β	slope angle		dimensionless
θ_a	fraction of air or gaseous components in the soil		dimensionless
θ_{sp}	soil saturated water content (soil porosity)		dimensionless
θ_r	residual water content		dimensionless
Θ_v	$ heta_w + heta_i$		dimensionless
Θ_m	$ heta_w + rac{ ho_i}{ ho_w} heta_i$		dimensionless
ψ_{w0}	soil matric potential corresponding to Θ_v		m
ψ^{w0}	liquid water pressure head		m
$\stackrel{arphi}{\psi}_T$	soil matric potential resulting from the generalized Clapeyron Equation		m
T_m	water melting temperature at atmospheric pressure	273.15	K
T^*	depressed water melting temperature under unsaturated conditions	273.13	K
T_{ref}	reference temperature, usually set to T_m		K
	parameter according to Van Genuchten (1980)		m^{-1}
α	parameter according to Van Genuchten (1980)		dimensionless
m = m	parameter according to Van Genuchten (1980)	usually: $m := 1 - n^{-1}$	dimensionless
$oldsymbol{J}_w$	volumetric liquid water flux	usuany. $m := 1 - n$	$\mathrm{m}\mathrm{s}^{-1}$
K	hydraulic conductivity		${ m m~s}^{-1}$
	total thermal conductivity of soil		$W m^{-1} K^{-1}$
λ_T	thermal conductivity of the soil particles		$W \text{ m}^{-1} \text{ K}^{-1}$
λ_{sp}		0.6	W m - K = K - 1
λ_w	water thermal conductivity	0.6	$W \text{ m} - K$ $W \text{ m}^{-1} \text{ K}^{-1}$
λ_i	ice thermal conductivity	2.29	${ m W \ m} { m K} { m W \ m}^{-1} { m K}^{-1}$
λ_a	air thermal conductivity	2.29	
L_f	latent heat of fusion	333.7	kJ kg ⁻¹
$\frac{\gamma}{\alpha}$	coefficient in the conductance formulation		dimensionless
C	total volumetric thermal capacity of soil		$J m^{-3} K^{-1}$
C_a	volumetric apparent thermal capacity of soil	2115	$J m^{-3} K^{-1}$
c_i	specific thermal capacity of ice	2117	$J kg^{-1} K^{-1}$
c_w	specific thermal capacity of water	4188	$J kg^{-1} K^{-1}$
c_{sp}	specific thermal capacity of soil particles		$J kg^{-1} K^{-1}$
c_s	soil surface roughness coefficient		$m^{1-\gamma}s^{-1}$
P_e	effective precipitation		${\rm m}{\rm s}^{-1}$
U	volumetric internal energy of soil		$\mathrm{J}\mathrm{m}^{-3}$
s	length along the direction of maximum slope		m
S_{en}	sink term of energy losses		$\mathrm{W}\mathrm{m}^{-3}$
S_s	soil specific storativity		m^{-1}
S_w	sink term of mass losses		s^{-1}
\boldsymbol{G}	heat conduction flux in the ground		$\mathrm{W}~\mathrm{m}^{-2}$
J	heat flux due to water advection		${ m W}~{ m m}^{-2}$

Table D4. Table of symbols for the atmospheric variables

Symbol	Name	Value or Range	Unit
$\overline{SW_{in}}$	incoming shortwave radiation		$\mathrm{W}\mathrm{m}^{-2}$
SW_{out}	outgoing shortwave radiation		${ m W~m^{-2}}$
SW_{toa}	shortwave radiation at top of atmosphere		${ m W~m^{-2}}$
LW_{in}	incoming longwave radiation		${ m W~m}^{-2}$
LW_{out}	outgoing longwave radiation		${ m W~m^{-2}}$
H	sensible heat flux		${ m W~m^{-2}}$
LE	latent heat flux		${ m W~m^{-2}}$
LW_{out}	outgoing longwave radiation		${ m W~m^{-2}}$
Q_s^*	saturated air specific humidity		${ m kg~kg^{-1}}$
Q_a	specific air humidity		${ m kg~kg^{-1}}$
r_a	aerodynamic resistance		dimensionless
L_e	specific heat of evaporization		$\rm Jkg^{-1}$
$ ho_a$	air density		${ m kg~m}^{-3}$
c_p	specific heat at constant pressure		${ m kg}~{ m m}^{-3}$
$ ho_a$	air density		${ m kg}~{ m m}^{-3}$
$ au_a$	atmospheric trasmissivity		dimensionless
$ au_c$	cloud trasmissivity		dimensionless
$ au_R$	trasmissivity for Rayleigh scattering		dimensionless
$ au_g$	gas absorption trasmissivity		dimensionless
$ au_w$	water vapor trasmissivity		dimensionless
$ au_{aer}$	aerosols trasmissivity		dimensionless
ϵ_a	atmosphere emissivity		dimensionless
ϵ_c	cloudy emissivity		dimensionless
e_a	water vapour pressure		bar
σ	Stefan Boltzmann constant	$5.67 \ 10^8$	$\mathrm{W}~\mathrm{m}^{-2}~\mathrm{K}^{-4}$
c	cloud fraction		dimensionless
p	air pressure		bar
T_a	Air temperature		$^{\circ}\mathrm{C}$
w_s	Wind speed		$\mathrm{m}~\mathrm{s}^{-1}$

Table D5. Table of symbols for the snow

Symbol	Name V	alue or Range	Unit
U_s	volumetric internal energy of snow		$\mathrm{J}\mathrm{m}^{-3}$
θ_{ws}	fraction of liquid water in snow		dimensionless
$ heta_{is}$	fraction of ice in snow		dimensionless
S_e	effective saturation		dimensionless
S_r	irreducible water saturation		dimensionless
K_s	snow hydraulic conductivity		${ m m~s^{-1}}$
P_s	weight of overlying snow column		Pa
T_s	snow temperature		$^{\circ}\mathrm{C}$
D	snow layer height		m
ϕ_s	snow porosity		dimensionless
C_1	compaction rate (destructive metamorphism)		s^{-1}
C_2	compaction rate (overburden)		s^{-1}
η	snow viscosity		${ m N~s~m^{-2}}$
J_{ws}	water flux in snow		${ m m~s^{-1}}$
$ ho_{ns}$	density of new snow		${ m kg}~{ m m}^{-3}$
M_{tot}	mass per unit surface of the whole snowpack		${\rm kg}~{\rm m}^{-2}$
M_{up}^*	max mass per unit surface of the upper region		${\rm kg}~{\rm m}^{-2}$
M_{dw}^*	max mass per unit surface of the lower region		${\rm kg}~{\rm m}^{-2}$
M_l^*	max mass per unit surface admitted for a layer		${\rm kg}~{\rm m}^{-2}$
M_l	mass per unit surface of a layer		${ m kg}~{ m m}^{-2}$
N_{mid}^*	max number of layers admitted for the middle region		dimensionless
N_{mid}	number of layers of the middle region		dimensionless

References

- Abbott, M., Bathurst, J., Cunge, J., O'Connell, P., and Rasmussen, J.: An introduction to the European Hydrological System Systeme Hydrologique Europeen, "SHE", 1: History and philosophy of a physically-based, distributed modelling system, Journal of Hydrology, 87, 45 59, 1986.
- Anderson, E. A.: A point energy and mass balance model of a snow cover, Tech. rep., Office of Hydrology, National Weather Service, Silver Spring, MA, USA, 1976.
- Armijo, L.: Minimization of functions having Lipschitz continuous first partial derivatives, Pacific Journal of mathematics, 6, 1966.
- Atwater, M. and Brown, P. S.: Numerical computation of the latitudinal variations of solar radiation for an atmosphere of varying opacity, Journal of Applied Meteorology, 13, 289–297, 1974.
- Auer, A. H. J.: The rain versus snow threshold temperatures, Weatherwise, 27, 67, 1974.
- Balland, V. and Arp, P.: Modeling soil thermal conductivities over a wide range of conditions, Journal of Environmental Engineering and Science, 4, 549–558, 2005.
- Barnes, S. L.: A technique for maximizing details in numerical weather map analysis, J. Appl. Meteor., 3, 396–409, 1964.
- Barnett, T., Adam, J., and Lettenmeier, D.: Potential impacts of a warming climate on water availability in snow-dominated regions, Nature, 438, 303–309, 2005.
- Bertoldi, G., Rigon, R., and Over, T. M.: Impact of watershed geomorphic characteristics on the energy and water budgets, J. Hydromet., 7, 389–403, 2006.
- Bertoldi, G., Notarnicola, C., Leitinger, G., Endrizzi, S., Zebisch, M., Della Chiesa, S., and Tappeiner, U.: Topographical and ecohydrological controls on land surface temperature in an alpine catchment, Ecohydrology, 3, 189–204, http://dx.doi.org/10.1002/eco.129, 2010.
- Best, M. J., Pryor, M., Clark, D. B., Rooney, G. G., Essery, R. L. H., Ménard, C. B., Edwards, J. M., Hendry, M. A., Porson, A., Gedney, N., Mercado, L. M., Sitch, S., Blyth, E., Boucher, O., Cox, P. M., Grimmond, C. S. B., and Harding, R. J.: The Joint UK Land Environment Simulator (JULES), model description Part 1: Energy and water fluxes, Geoscientific Model Development, 4, 677–699, 2011.
- Brooks, R. H. and Corey, A. T.: Hydraulic properties of porous media, Hydrology paper, 3, Colorado State University, Fort Collins, 1964.
- Brun, E., David, P., Sudul, M., and Brunot, G.: A numerical model to simulate snow-cover stratigraphy for operational avalanche forecasting, Journal of Glaciology, 38, 1992.
- Brutsaert, W.: On a derivable formula for long-wave radiation from clear skies, Water Resources Research, 11, 742–744, 1975a.
- Brutsaert, W.: A theory for local evaporation (or heat transfer) from rough and smooth surfaces at ground level, Water Resources Research, 11, 543–550, 1975b.
- Calonne, N., Flin, F., Morin, S., Lesaffre, B., du Roscoat, S. R., and Geindreau, C.: Numerical and experimental investigations of the effective thermal conductivity of snow, Geophysical Research Letters, 38, L23 501, 2011.
- Colbeck, S. C.: A theory of water percolation in snow, J. Glaciol., 11, 369–385, 1972.
- Cosenza, P., Guerin, R., and Tabbagh, A.: Relationship between thermal conductivity and water content of soils using numerical modelling, European Journal of Soil Science, 54, 581–587,

- 2003.
- Crawford, T. M. and Duchon, C. E.: An improved parameterization for estimating effective atmospheric emissivity for use in calculating daytime downwelling longwave radiation, Journal of Applied Meteorology, 38, 474–480, 1998.
- Daanen, R., Misra, D., and Epstein, H.: Active-layer hydrology in nonsorted circle ecosystems of the Arctic tundra, Vadose Zone Journal, 6, 694–704, 2007.
- Dall'Amico, M.: Coupled water and heat transfer in permafrost modeling, Ph.D. thesis, Institute of Civil and Environmental Engineering, Universita' degli Studi di Trento, Trento. Available from http://eprints-phd.biblio.unitn.it/335/, 2010.
- Dall'Amico, M., Endrizzi, S., Gruber, S., and Rigon, R.: A robust and energy-conserving model of freezing variably-saturated soil, The Cryosphere, 5, 469–484, 2011a.
- Dall'Amico, M., Endrizzi, S., Gruber, S., and Rigon, R.: GEOtop Users Manual. Version 1.0, Technichal report, Mountain-eering Srl, Siemensstr. 19 Bolzano, Italy, 2011b.
- De la Casiniere, A. C.: Heat exchange over a melting snow surface, J. Glaciol., 13, 55–72, 1974.
- de Vries, D. A.: Thermal properties of soils, North Holland, Amsterdam, Netherlands, 1963.
- Deardorff, J. W.: Efficient prediction of ground surface temperature and moisture with inclusion of a layer of vegetation, J. Geophys. Res., 83, 1889–1903, 1978.
- Della Chiesa, S., Bertoldi, G., Niedrist, G., Obojes, N., Endrizzi, S., Albertson, J. D., Wohlfahrt, G., Hörtnagl, L., and Tappeiner, U.: Modelling changes in grassland hydrological cycling along an elevational gradient in the Alps, Ecohydrology, doi: 10.1002/eco.1471, 2014.
- Denby, B. and Greuell, W.: The use of bulk and profile methods for determining surface heat fluxes in the presence of glacier winds, J. Glaciol., 46, 445–452, 2000.
- Dickinson, R. E., Henderson-Sellers, A., and Kennedy, P. J.: Biosphere-Atmosphere Transfer Scheme (BATS) version 1e as coupled to the NCAR Community Land Model, Tech. rep., National Center for Atmospheric Research, Boulder, CO, USA, 1903
- Dilley, A. C. and O'Brien, D. M.: Estimating downward clear sky long-wave irradiance at the surface from screen temperature and precipitable water, Q. J. R. Meteorological Sociecty, 124a, 1391– 1401, 1997.
- El-Mikkawy, M. and Karawia, A.: Inversion of general tridiagonal matrices, Applied Mathematics Letters, 19, 712–720, 2006.
- Endrizzi, S. and Marsh, P.: Observations and modeling of turbulent fluxes during melt at the shrub-tundra transition zone 1: point scale variations, Hydrology Research, 41, 471–491, 2010.
- Endrizzi, S., Quinton, W. L., and Marsh, P.: Modelling the spatial pattern of ground thaw in a small basin in the arctic tundra, The Cryosphere Discussions, 5, 367–400, http://www.the-cryosphere-discuss.net/5/367/2011/, 2011.
- Erbs, D. G., Klein, S. A., and Duffie, J. A.: Estimation of the diffuse radiation fraction for hourly, daily and monthly-average global radiation, Solar energy, 28, 293–302, 1982.
- Flerchinger, G. N., Xaio, W., Marks, D., Sauer, T. J., and Yu, Q.: Comparison of algorithms for incoming atmospheric long-wave radiation, Water Resources Research, 45, W03 423, 2009.
- Formetta, G., Mantilla, R., Franceschi, S., Antonello, A., and Rigon, R.: The JGrass-NewAge system for forecasting and managing

- the hydrological budgets at the basin scale: models of flow generation and propagation/routing, Geoscientific Model Development, 4, 943–955, 2011.
- Freeze, R. A. and Harlan, R. L.: Blueprint for a physically-based, digitally simulated hydrologic response model, J. Hydrol., 9, 237–258, 1969.
- Garen, D. C. and Marks, D.: Spatially distributed energy balance snowmelt modelling in a mountainous river basin: estimation of meteorological inputs and verification of model results, J. Hydrol., 315, 126–153, 2005.
- Garratt, J. R.: The Atmospheric Boundary Layer, Cambridge University Press, 1992.
- Gottardi, G. and Venutelli, M.: A control-volume finite-element model for two-dimensional overland flow, Advances in Water Resources, 16, 277–284, 1993.
- Gruber, S., Peter, M., Hoelzle, M., Woodhatch, I., and Haeberli, W.: Surface temperatures in steep alpine rock faces - a strategy for regional-scale measurement and modelling, in: Proceedings of the 8th International Conference on Permafrost, 2003.
- Gruber, S., Hoelzle, M., and Haeberli, W.: Rock-wall temperatures in the Alps: modelling their topographic distribution and regional differences, Permafrost and Periglacial Processes, 15, 299–307, 2004.
- Gubler, S., Gruber, S., and Purves, R. S.: Uncertainties of parameterized surface downward clear-sky shortwave and all-sky long-wave radiation, Atmospheric Chemistry and Physics, 12, 5077–5098, 2012.
- Gubler, S., Endrizzi, S., Gruber, S., and Purves, R. S.: Sensitivities and uncertainties of modeled ground temperatures in mountain environments, Geoscientific Model Development, 6, 1319–1336, 2013.
- Halberstam, I. and Schieldge, J. P.: Anomalous behavior of the atmospheric surface layer over a melting snowpack, J. Appl. Met., 20, 255–265, 1981.
- Hansson, K., Simunek, J., Mizoguchi, M., Lundin, L., and van Genuchten, M.: Water flow and heat transport in frozen soil numerical solution and freeze-thaw applications, Vadose Zone Journal, 3, 693–704, 2004.
- Helbig, N., Löwe, H., and Lehning, M.: Radiosity approach for the shortwave surface radiation balance in complex terrain, Journal of the Atmospheric Sciences, 66, 2900–2912, 2009.
- Hinzman, L. D., Goering, D. J., and Kane, D. L.: A distributed thermal model for calculating soil temperature profiles and depth of thaw in permafrost regions, J. Geophys. Res., 103, 975–991, 1998.
- Hock, R.: Temperature index melt modelling in mountain areas, J. Hydrol., 282, 2003.
- Horton, P., Schaefli, B., Mezghani, A., Hingray, B., and Musy, A.: Assessment of climate-change impacts on alpine discharge regimes with climate model uncertainty, Hydrological Processes, 20, 2091–2109, 2006.
- Houghton, H. G.: On the annual heat balance of the northern hemisphere, J. Meteor., 11, 1–9, 1954.
- Idso, S. B.: A set of equations for full spectrum and 8 to $14\mu m$ and 10.5 to $12.5\mu m$ thermal radiation from cloudless skies, Water Resources Research, 17, 295–304, 1981.
- Iqbal, M.: An introduction to solar radiation, Academic Press, Toronto, 1983.

- Ivanov, V. Y., Vivoni, E. R., Bras, R. L., and Entekhabi, D.: Catchment hydrologic response with a fully distributed triangulated irregular network model, Water Resources Research, 40, 1–23, 2004
- Johansen, O.: Thermal conductivity of soils, Ph.D. thesis, Norwegian Technical University, Trondheim, 1975.
- Jordan, R.: A one-dimensional temperature model for a snow cover: Technical documentation for SNTHERM 89, Tech. rep., US Army Cold Regions Research and Engineering Laboratory, Hanover, NH, USA, 1991.
- Jordan, R., Andreas, E. L., and Makshtas, A. P.: Heat budget of snow-covered sea ice at North Pole 4, J. Geophys. Res., 104, 7785–7806, 1999.
- Kelley, C.: Solving nonlinear equations with Newton's method, Society for Industrial Mathematics, 2003.
- Kienzle, S. W.: A new temperature based method to separate rain and snow, Hydrological Processes, 22, 5067–5085, 2008.
- Konzelmann, T., van de Wal, R. S. W., Greuell, W., Bintanja, R., Henneken, E. A. C., and Abe-Ouchi, A.: Parameterization of global and longwave incoming radiation for the Greenland Ice Sheet, Global and Planetary Change, 9, 143–164, 1994.
- Koopmans, R. W. R. and Miller, R. D.: Soil freezing and soil water characteristic curves, Soil Science Society of America Journal, 30, 680–685, 1966.
- Kuchment, L. S., Gelfan, A. N., and Demidov, V. N.: A distributed model of runoff generation in the permafrost regions, J. Hydrol., pp. 1–22, 2000.
- Kunstmann, H., Hingerl, L., Mauder, M., Wagner, S., and Rigon, R.: A combined water and energy flux observation and modelling study at the TERENO-preAlpine observatory, Climate and Land Surface Changes in Hydrology, 359, 2013.
- Kurylyk, B. and Watanabe, K.: The mathematical representation of freezing and thawing processes in variably-saturated, nondeformable soils, Advances in Water Resources, 60, 160–177, 2013.
- Lehning, M., Völksch, I., Gustafsson, D., Nguyen, T., Stähli, M., and Zappa, M.: ALPINE3D: a detailed model of mountain surface processes and its application to snow hydrology, Hydrol. Proc, 20, 2111–2128, 2006.
- Liang, X., Lettenmaier, D. P., Wood, E. F., and Burges, S. J.: A simple hydrologically based model of land surface water and energy fluxes for general circulation models, Journal of Geophysical Research: Atmospheres, 99, 14415–14428, 1994.
- Liston, G. E. and Elder, K.: A meteorological distribution system for high-resolution terrestrial modeling (MicroMet), Journal of Hydrometeorology, 11, 217–234, 2006a.
- Liston, G. E. and Elder, K.: A distributed snow-evolution modeling system (SnowModel), Journal of Hydrometeorology, 7, 1259– 1276, 2006b.
- Marchenko, S., Romanovsky, V., and Tipenko, G.: Numerical modeling of spatial permafrost dynamics in Alaska, in: Proceedings of the Ninth International Conference on Permafrost, vol. 2, pp. 1125–1130, 2008.
- McDonald, J. E.: Direct absorption of solar radiation by atmospheric water vapor, J. Meteor., 17, 319–328, 1960.
- McGurk, B., Azuma, D., and Kattelmann, R.: Density of new snow in the central Sierra Nevada, in: Proceedings 56th Western Snow Conference, 1988.

- McKenzie, J., Voss, C., and Siegel, D.: Groundwater flow with energy transport and water–ice phase change: Numerical simulations, benchmarks, and application to freezing in peat bogs, Advances in Water Resources. 30, 966–983, 2007.
- Meesters, A. G. C. A., Bink, N. J., Vugt, H. H., Cannemeijer, F., and Henneken, E. A. C.: Turbulence observations above a smooth melting surface on the Greenland ice sheet, Boundary Layer Meteorology, 85, 81–110, 1997.
- Meyers, T. and Dale, R.: Predicting daily insolation with hourly cloud height and coverage., Journal of Climate and Applied Meteorology, 22, 537–545, 1983.
- Miller, R.: Phase equilibria and soil freezing, in: Permafrost: Proceedings of the Second International Conference. Washington DC: National Academy of Science-National Research Council, vol. 287, pp. 193–197, 1965.
- Monin, A. S. and Obukhov, A. M.: Basic laws of turbulent mixing in the surface layer of the atmosphere, Tr. Akad. Nauk SSSR Geophiz. Inst., 24, 163–187, 1954.
- Morin, S., Lejeune, Y., Lesaffre, B., Panel, J.-M., Poncet, D., David, P., and Sudul, M.: An 18-yr long (1993–2011) snow and meteorological dataset from a mid-altitude mountain site (Col de Porte, France, 1325 m alt.) for driving and evaluating snowpack models, Earth System Science Data, 4, 13–21, 2012.
- Mualem, Y.: A new model for predicting the hydraulic conductivity of unsaturated porous media, Water Resour. Res., 12, 513–522, 1976.
- Niessner, H. and Reichert, K.: On computing the inverse of a sparse matrix, International Journal for Numerical Methods in Engineering, 19, 1513–1526, 1983.
- Oleson, K., Dai, Y., Bonan, G., Bosilovich, M., Dickinson, R., Dirmeyer, P., Hoffman, F., Houser, P., Levis, S., Niu, G., Thornton, P., Vertenstein, M., Yang, Z., and Zeng, X.: Technical description of the Community Land Model (CLM), Tech. Rep. NCAR/TN-461+STR, National Center for Atmospheric Research, Boulder, CO, USA, 2004.
- Painter, S. L.: Three-phase numerical model of water migration in partially frozen geological media: model formulation, validation, and applications, Computational Geosciences, 15, 69–85, 2011.
- Panday, S. and Huyakorn, P.: A fully coupled physically-based spatially-distributed model for evaluating surface/subsurface flow, Advances in Water Resources, 27, 361—382, 2004.
- Paniconi, C. and Putti, M.: A comparison of Picard and Newton iteration in the numerical solution of multidimensional variably saturated flow problems, Water Resour. Res., 30, 3357–3374, 1994.
- Panoksky, H. A. and Dutton, J. A.: Atmospheric Turbulence Models and Methods for Engineering Applications, John Wiley and Sons, 1984.
- PERMOS: Permafrost in Switzerland 2004/2005 and 2005/2006, in: Glaciological Report (Permafrost) No. 6/7 of the Cryospheric Commission of the Swiss Academy of Sciences, edited by Nötzli, J. and Vonder Mühll, D., University of Zurich, 2009.
- Prata, A. J.: A new long-wave formula for estimating downward clearsky radiation at the surface, Q. J. R. Meteorological Society, 122, 1127–1151, 1996.
- Ray, C.: Some Numerical Experiments on the Variably-Saturated Flow Equation, in: Subsurface-Water Hydrology, edited by Singh, V. and Kumar, B., vol. 16 of Water Science and Technology Library, pp. 49–63, Springer Netherlands, 1996.

- Rigon, R., Bertoldi, G., and Over, T. M.: GEOtop: a distributed hydrological model with coupled water and energy budgets, J. Hydromet., 7, 371–388, 2006.
- Ryan, B. C.: A mathematical model for diagnosis and prediction of surface winds in mountainous terrain, J. Appl. Meteor., 16, 571– 584, 1977.
- Satterlund, D. R.: An improved equation for estimating longwave radiation from the atmosphere, Water Resources Research, 15, 1649–1650, 1979.
- Shimizu, H.: Air permeability of deposited snow, vol. 22, Institute of Low Temperature Science, Sapporo, Japan, 1970.
- Sicart, J. E., Pomeroy, J. W., Essery, R. L. H., and Bewley, D.: Incoming longwave radiation to melting snow: observations, sensitivity and estimation in northern environments, Hydrological Processes, 20, 3697–3708, 2006.
- Simoni, S., Zanotti, F., Bertoldi, G., and Rigon, R.: Modelling the probability of occurrence of shallow landslides and channelized debris flows using GEOtop-FS, Hydrological Processes, 22, 532–545, 2008.
- Snyder, W. C., Wan, Z., Zhang, Y., and Feng, Y.-Z.: Classification-based emissivity for land surface temperature measurement from space, International Journal of Remote Sensing, 19, 2753–2774, 1998.
- Spaans, E. and Baker, J.: The soil freezing characteristic: its measurement and similarity to the soil moisture characteristic, Soil Science Society of America Journal, 60, 13–19, 1996.
- Sturm, M., Holmgren, J., König, M., and Morris, K.: The thermal conductivity of seasonal snow, J. Glaciol., 43, 26–41, 1997.
- Tarboton, D. G. and Luce, C. H.: Utah energy balance snow accumulation and melt model (UEB), Tech. rep., Utah Water Research Laboratory Utah State University and USDA Forest Service Intermountain Research Station, 1996.
- Therrien, R. and Sudicky, E.: Three-dimensional analysis of variably-saturated flow and solute transport in discretely-fractured porous media, Journal of Contaminant Hydrology, 23, 1–44, 1996.
- Thornton, P. E., W., R. S., and A., W. M.: Generating surfaces of daily meteorological variables over large regions of complex terrain, Journal of Hydrology, 190, 215–251, 1997.
- US Army Corps of Engineers: Snow hydrology, Summary report of the snow investigations, Tech. rep., US Army Corps of Engineers, North Pacific Division, Portland, OR, USA, 1956.
- Van Der Vorst, H. A.: BI-CGSTAB: A fast and smoothly converging variant of BI-CGSTAB for the solution of nonsymmetric linear systems, SIAM J. Sci. Stat. Comput., 13, 631–644, 1992.
- Van Genuchten, M. T.: A closed-form equation for predicting the hydraulic conductivity of unsaturated soils., Soil Sci. Soc. Am. J., 44, 892–898, 1980.
- VanderKwaak, J. E. and Loague, K.: Hydrologic-Response simulations for the R-5 catchment with a comprehensive physics-based model, Water Resources Research, 37, 999–1013, 2001.
- Vionnet, V., Brun, E., Morin, S., Boone, A., Faroux, S., Le Moigne, P., Martin, E., and Willemet, J.-M.: The detailed snowpack scheme Crocus and its implementation in SURFEX v7.2, Geoscientific Model Development, 5, 773–791, 2012.
- Wagnon, P., Ribstein, P., Kaser, G., and Berton, P.: Energy balance and runoff seasonality of a Bolivian glacier, Global Planet. Change, 22, 49–58, 1999.

- Wettlaufer, J. S. and Worster, M. G.: Premelting dynamics, Annual Review of Fluid Mechanics, 38, 427–452, 2006.
- Ye, Z. and Pielke, R. A.: Atmospheric parameterization of evaporation from non-plant-covered surfaces, J. Appl. Meteor., 32, 1248–1258, 1993.
- Yen, Y.: Review of thermal properties of snow, ice and sea ice, Tech. Rep. 81–10, Cold Regions Research and Engineering Laboratory, Hanover, NH, USA, 1981.
- Zanotti, F., Endrizzi, S., Bertoldi, G., and Rigon, R.: The GEOTOP snow module, Hydrol. Proc., 18, 3667–3679, 2004.
- Zehe, E., Maurer, T., Ihringer, J., and Plate, E.: Modeling water flow and mass transport in a loess catchment, Physics and Chemistry of the Earth, Part B: Hydrology, Oceans and Atmosphere, 26, 487 507, 2001.
- Zhang, Z., Kane, D. L., and Hinzman, L. D.: Development and application of a spatially-distributed Arctic hydrological and thermal process model (ARHYTHM), Hydrol. Proc, 14, 1017–1044, 2000.