

1 **Supplementary Material:**

2 **1. Description of the new unified treatment of aerosol processing by convective clouds**

3 We begin by briefly reviewing the existing CAM5 treatment. The treatments of deep and
4 shallow convective clouds in CAM5 are described at length in Neale et al. (2010) and references
5 therein. The deep convection parameterization is based on Zhang and McFarlane (1995), and
6 considers an ensemble of updraft and downdraft plumes, although only the ensemble updraft and
7 downdraft properties are used for aerosol processing. The shallow convective parameterization
8 is based on Park and Bretherton (2009), represented by a single entraining-detraining updraft
9 plume. From the standpoint of aerosol processing, the deep and shallow convection treatments
10 are conceptually very similar. Also, both of the existing treatments of aerosol processing by
11 convective clouds consider wet removal and vertical transport separately and sequentially.

12 The wet removal of aerosols in CAM5 distinguishes between “in-cloud wet removal”
13 (activation of interstitial aerosol particles to become cloud-borne aerosol, following by
14 conversion of cloud-condensate and cloud-borne aerosol to precipitation) and “below-cloud wet
15 removal” (capture of interstitial aerosol particles by precipitation particles via impaction and
16 Brownian diffusion). Below-cloud wet removal is identical in the existing and new unified
17 treatments. Note that CAM5 treats cloud-borne aerosols within stratiform clouds explicitly in a
18 prognostic manner, and they are assumed to not interact with convective clouds. The
19 “interstitial” aerosol mixing ratios in the CAM5 code (\bar{q}_{AI*}) are defined to be the sum of
20 interstitial plus convective-cloud-borne aerosols, expressed as grid-cell averaged quantities. The
21 convective-cloud-borne aerosols are calculated in the wet removal routines in a diagnostic
22 manner.

23 The in-cloud aerosol wet removal parameterizations for shallow and deep convection utilize
 24 profiles of cloud fractional area (f_{CLDC}), in-cloud cloud-condensate mixing ratio ($ICWMR$, in
 25 kg/kg), and grid-cell mean precipitation production ($RPROD$, in kg/kg/s), to calculate a first-
 26 order rate loss rate (the rate at which cloud-condensate is converted to precipitation within the
 27 cloud),

$$28 \quad \lambda_{WETC} = RPROD / (f_{CLDC} ICWMR) . \quad (S1)$$

29 In the CAM5 convective-cloud wet removal, the cloud-borne aerosol mixing ratio within the
 30 convective cloud is assumed equal to the grid-cell mean interstitial aerosol mixing ratio at that
 31 level multiplied by a prescribed convective-cloud activation fraction, f_{ACTC} , which varies with
 32 aerosol mode and species. Over a model time-step Δt , a fraction $f_{WETC} = \text{MIN}(\Delta t \cdot \lambda_{WETC}, 1)$ of
 33 this cloud-borne aerosol is removed, and the change to the grid-cell mean interstitial aerosol is

$$34 \quad \Delta \bar{q}_{AI*} = -0.4 f_{CLDC} f_{WETC} f_{ACTC} \bar{q}_{AI*} \quad (S2)$$

35 where the 0.4 is a wet removal adjustment factor, applied because f_{CLDC} and f_{WETC} from the
 36 convective parameterizations would otherwise produce too much wet removal.

37 The deep convective vertical transport of aerosols and other trace species follows the
 38 assumption in the original ZM parameterization that the updrafts and downdrafts are described
 39 by steady-state bulk plume models representing the ensemble of up- and downdrafts in the
 40 clouds. Aerosol mixing ratios in the updraft ($q_{A,U}$) and downdraft ($q_{A,D}$) ensembles are calculated
 41 by integrating steady-state mass continuity equations either upwards or downwards:

$$42 \quad \frac{\partial(M_U q_{A,U})}{\partial p} = E_U (1 - f_{WET}) q_{A,E} - D_U q_{A,U} \quad (S3a)$$

$$43 \quad \frac{\partial(M_D q_{A,D})}{\partial p} = E_D(1 - f_{WET})q_{A,E} - D_D q_{A,D} \quad (S3b)$$

44 Here the U , D , and E subscripts denote updraft, downdraft, and environment, M is vertical mass
 45 flux of air (Pa/s), E is the positive portion of $\partial M / \partial p$ due to entrainment, $-D$ is the negative
 46 portion due to detrainment, p is pressure, and f_{WET} is the fractional wet removal of aerosols in the
 47 convective and stratiform clouds areas. The $(1 - f_{WET})$ factor applied to entrainment accounts for
 48 wet removal of aerosols that is applied prior to the deep convective transport, providing some
 49 coupling of wet removal and vertical transport. Also, $q_{A,E}$ is assumed equal to \bar{q}_{AI^*} . Equations
 50 S3a and S3b are solved to determine mixing ratios in the convective up- and downdrafts. The
 51 grid-cell mean interstitial plus convective-cloud-borne aerosol mixing ratios are then updated by
 52 solving

$$53 \quad \frac{\partial \bar{q}_{AI^*}}{\partial t} = -\frac{\partial}{\partial p} [M_U q_{A,U} + M_D q_{A,D} + M_E q_{A,E}] \quad (S4)$$

54 where $M_E = -(M_U + M_D)$ is the compensating vertical mass flux in the environment. The shallow
 55 convective transport of aerosols is treated similarly, but the $(1 - f_{WET})$ factor is not applied to
 56 entrainment, there is no downdraft, and the numerical discretization applied to the (S3-4) differs
 57 somewhat.

58 The main differences between the new unified treatment of aerosol processing by convective
 59 clouds and the previous CAM5 treatments are that (1) wet removal and vertical transport are
 60 treated simultaneously, (2) cloud-borne aerosols and aerosol activation are treated explicitly in
 61 the updraft, and (3) wet removal is applied to aerosols in the updraft. Similar to the previous

62 treatments, we assume that aerosol mixing-ratio profiles in the updraft and downdraft are steady-
 63 state. The mass-continuity equation for the updraft is:

$$64 \quad \frac{\partial(M_U q_{AX,U})}{\partial p} = E_U q_{AX,E} - D_U q_{AX,U} + A_U (\dot{q}_{AX,U})_{ACT} + A_U (\dot{q}_{AX,U})_{WET} \quad (S5)$$

65 where the AX subscript is either AI for an interstitial aerosol species or ACC for a convective-
 66 cloud-borne (activated) aerosol species. (Note that q_{AI} is interstitial aerosol only, while \bar{q}_{AI^*}
 67 includes the convective-cloud-borne aerosol.) The $(\dot{q}_{AX,U})_{ACT}$ and $(\dot{q}_{AX,U})_{WET}$ terms are the rates
 68 of change due to activation and in-cloud wet removal in the updraft, respectively. For the
 69 downdraft, we assume that only interstitial aerosol is entrained from the environment and there is
 70 no aerosol activation as the downdraft is never super-saturated. As a result, the downdraft
 71 contains only interstitial aerosol, and there is no in-cloud wet removal. Thus the downdraft
 72 mass-continuity equation is unchanged from (S3b).

73 Aerosol activation in the updraft includes activation at cloud-base and above cloud-base. The
 74 cloud-base activation uses the Abdul-Razzak and Ghan (2000) parameterization to diagnose the
 75 maximum supersaturation in a rising air parcel and the activation fraction (f_{ACTC}) for interstitial
 76 aerosol mass and number of each aerosol mode. This requires an updraft vertical velocity, w_U ,
 77 which can be diagnosed from $M_U = \rho A_U w_U g$, where ρ is air density, A_U is updraft fractional
 78 area, and g is the gravitational constant. The shallow convection parameterization assumes that
 79 $A_U = f_{CLDC}/2$, and this gives reasonable values for w_U . The deep convection parameterization
 80 provides no information on A_U , and using $A_U = f_{CLDC}/2$ gives unreasonably low values for w_U .
 81 Thus for deep convection we use empirical values for w_U based on measurements by Zipser and
 82 Lemone (1980) during GATE. The activation tendency needed in (A5) is then

$$83 \quad (\dot{q}_{AI,U})_{ACT} = -(\dot{q}_{ACC,U})_{ACT} = -(f_{ACTC} q_{AI,U}) / \Delta t_U \quad (S6)$$

84 where $\Delta t_U = \Delta z / w_U$ is the time for updraft air to move across a layer .

85 Several cloud modeling studies (Pinsky and Kahin, 3003; Segal et al., 2003; Yin et al., 2005;
 86 Phillips et al., 2007) suggest that supersaturations of a few tenths of a percent or more may be
 87 achieved in convective clouds above cloud-base, due to strong adiabatic cooling (from high
 88 updraft velocities) and relatively low hydrometeor surface area (due to conversion of cloud
 89 droplets to precipitation particles). Ghan et al. (2012) suggest that supersaturation above cloud-
 90 base should be diagnosed based on a balance between adiabatic cooling and water vapor
 91 condensation onto hydrometeors, but this requires knowledge of both the updraft velocity and
 92 hydrometeor size distribution. This information is lacking or very approximate in the current
 93 CAM5.0 convective cloud parameterizations, so currently we simply prescribe an above cloud-
 94 base supersaturation of 0.3%, based on the several cloud-modeling studies cited above. With
 95 this we can calculate the aerosol activation fractions as done in the Abdul-Razzak and Ghan
 96 (2000) parameterization.

97 The in-cloud wet removal tendency for cloud-borne aerosols in the updraft is given by

$$98 \quad (\dot{q}_{ACC,U})_{WET} = -\lambda_{WETC,U} q_{ACC,U} \quad (S7a)$$

99 and the wet-removal first-order loss rate is taken to be

$$100 \quad \lambda_{WETC,U} = RPROD / (A_U ICWMR) \quad (S7b)$$

101 This gives

$$102 \quad A_U (\dot{q}_{ACC,U})_{WET} = -(RPROD / ICWMR) q_{ACC,U} \quad (S7c)$$

103 After aerosol mixing ratios in the updrafts and downdrafts have been calculated, changes to
 104 the grid-cell mean aerosol mixing ratios are calculated by solving

$$105 \quad \frac{\partial \bar{q}_{AX}}{\partial t} = -\frac{\partial}{\partial p} [M_U q_{AX,U} + M_D q_{AX,D} + M_E q_{AX,E}] \quad (S8)$$

$$+ A_U (\dot{q}_{AX,U})_{ACT} + A_U (\dot{q}_{AX,U})_{WET} + A_E (\dot{q}_{AX,E})_{RES}$$

106 The right-most term involves resuspension in the environment of cloud-borne aerosols detrained
 107 from the updraft. Currently we assume complete resuspension for the detrained convective-
 108 cloud-borne aerosols, so there is no transfer of convective- to stratiform-cloud-borne aerosols.

109 **2. Aerosol and Aerosol-Cloud Processes in the CAM5**

110 We use a developmental version of the stand-alone CAM5, which has nearly identical
 111 physics to the released version CAM5.1. Aerosol evolution in CAM5 is controlled by a
 112 combination of emission, transport, aerosol microphysics (new particle formation, condensation,
 113 coagulation, aging, etc.), and dry and wet removal. Aerosol and cloud microphysics and their
 114 interactions are described and evaluated by Liu et al. (2012). Here we briefly summarize the
 115 processes in CAM5 that are relevant to aerosol (BC in particular) and evolution.

116 *1) Aerosol Mixing State and Aging*

117 CAM5 employs a modal aerosol module (MAM) to represent aerosols (Liu et al., 2012). The
 118 aerosol mixing-state and size distribution is represented by multiple log-normally distributed
 119 modes, with internal mixing assumed for aerosol species [e.g., sulphate, BC, primary organic
 120 matter (POM), secondary organic aerosol (SOA)] within each individual mode. Two versions of
 121 MAM are used in this study: a 3-mode “fast” representation (MAM3) and a more complex 7-

122 mode “benchmark” representation (MAM7). The major difference between MAM3 and MAM7
123 related to BC lies in the treatment of aging. In MAM3, BC and POM are emitted into the
124 accumulation mode, which also contains highly-hygroscopic sulphate and sea-salt and
125 moderately hygroscopic SOA. The freshly emitted BC and POM are thus immediately mixed
126 with these hygroscopic species in particles that can be viable cloud condensation nuclei (CCN),
127 depending on the amount of BC/POM emissions versus existing sulphate/sea-salt/SOA. In
128 MAM7, BC and POM are emitted into a primary carbon mode, which contains no other species.
129 The hygroscopicity of this mode depends on the assumed POM hygroscopicity which is
130 generally lower than that of the MAM3 accumulation mode. Thus in MAM7, the freshly emitted
131 BC and POM are in particles that are less-viable CCN and less likely to experience wet removal.
132 As hygroscopic species (e.g., H₂SO₄, NH₃ and semi-volatile organic vapors) condense onto
133 primary carbon mode particles, the particles are “aged” (become more hygroscopic) and are
134 gradually transferred into the MAM7 accumulation mode. The rate of transfer is controlled by
135 somewhat uncertain aging parameters, such as the number of mono-layers of sulphate coating
136 needed to make a fresh BC/POM particle a viable CCN (Liu et al. 2012).

137 *2) Aerosol-Cloud Interactions*

138 In CAM5, aerosol particles are assumed to either be suspended in the air or reside in cloud
139 droplets, and these are referred to as interstitial and cloud-borne aerosol, respectively. Particles
140 that are viable CCN and are within the cloudy portion of a grid cell are converted from the
141 interstitial state to the cloud-borne state through aerosol activation (or nucleation scavenging).
142 Cloud-borne aerosols in stratiform clouds are treated prognostically in CAM5: their mixing
143 ratios are saved between model time steps and evolve as a result of source, sink, and transport
144 processes. Their activation is parameterized using vertical velocity (resolved and sub-grid

145 turbulent) and aerosol properties of all the modes following Abdul-Razzak and Ghan (2000).
146 Activation may occur when aerosols are carried into clouds from below and when cloud fraction
147 increases. Therefore, liquid cloud fraction diagnosed from the triangular distribution of grid-
148 mean relative humidity in CAM5 is critical to aerosol activation. Cloud-borne aerosols in
149 convective clouds are treated diagnostically: their mixing ratios are diagnosed each model time
150 step (with no “memory”) from the interstitial aerosol mixing ratios. Cloud-borne BC particles are
151 returned to the interstitial state upon drop evaporation (i.e., resuspension). The representation of
152 activation/resuspension processes, and consequent effects on clouds and precipitation in the
153 model, has direct and indirect impacts on BC wet removal and transport.

154 *3) Removal*

155 Both interstitial and cloud-borne aerosol particles are subject to wet and dry removal
156 (deposition). CAM5 treats in-cloud and below-cloud wet removal of aerosols. In-cloud wet
157 removal involves activation of interstitial aerosol to become cloud-borne, followed by
158 conversion of cloud droplets (and the cloud-borne aerosol particles) to precipitation. The
159 activation step is described above. The removal rate of cloud-borne aerosol is equal to the rate at
160 which cloud-water is converted to precipitation, as determined by the model’s cloud
161 parameterizations. In-cloud wet removal through attachment of interstitial aerosol to ice particles
162 followed by conversion of ice particles to precipitation is currently not treated. Below-cloud wet
163 removal involves direct capture of interstitial aerosols by precipitation particles through a
164 number of processes (e.g., inertial impaction, Brownian diffusion) and is relatively inefficient for
165 aerosol in the accumulation mode size range. Different tunable parameters, which we refer to as
166 wet-removal adjustment factors (≤ 1), are applied to the calculation of the stratiform/convective
167 in-cloud and below-cloud scavenging rates to account for various uncertainties from the aerosol

168 mixing state, activation, and model-predicted cloud and precipitation properties (Liu et al.,
169 2012). When raindrops evaporate below cloud, a portion of the wet-scavenged aerosol is
170 resuspended as interstitial particles and this produces some downwards redistribution of aerosols.

171 For BC and sulphate (predominately sub-micron) in CAM5, dry removal accounts for about
172 16-18% and 11-12% of the total removal on a global annual basis (with the ranges reflecting
173 MAM3 and MAM7 values). Aerosol dry deposition velocities are calculated using the method
174 developed by Zhang et al. (2001) with model provided aerodynamic resistance, friction velocity,
175 and surface properties. Gravitational settling is also treated.

176 *4) Transport*

177 Interstitial aerosol particles in CAM5 are transported by resolved winds, turbulence, and
178 shallow and deep convection. Advection by resolved winds is neglected for cloud-borne aerosols
179 due to the assumption that aerosol particles in liquid clouds are relatively short-lived (Koch et
180 al., 2006). Stratiform-cloud-borne aerosols undergo turbulent vertical transport. Ghan and Easter
181 (2006) showed that neglecting transport of stratiform-cloud-borne aerosols by resolved winds
182 introduces small global mean biases in aerosol number concentrations at a coarse resolution
183 ($2^\circ \times 2.5^\circ$). Ma et al. (2012) have compared CAM5 simulations allowed to evolve freely with
184 simulations constrained by various reanalysis products and found that CAM5 Arctic circulation
185 patterns (mean and transient eddy) are quite reasonable. This suggests that transport of aerosols
186 by resolved winds in CAM5 is not a major contributor to the poor simulation of remote Arctic
187 aerosols.

188 **3. Sensitivity test on Emissions**

189 The simulations discussed in the main text use the IPCC AR5 emissions for year 2000. The
190 AR5 BC emissions for 1980 are quite different from the 2000 emissions due to a number of

191 socio-economic changes. Although the global annual emissions are lower for 1980 (6.9 Tg C yr^{-1})
192 1) than for 2000 (7.8 Tg C yr^{-1}), more importantly for the Arctic, as shown in Fig. S1, the DJF
193 emissions integrated between 40°N and 70°N were significantly higher in 1980 than in 2000
194 (1.87 vs. $1.25 \text{ Tg C yr}^{-1}$). At these latitudes, the summer (JJA) BC emissions are higher than
195 winter due to wildfire emissions. This summer increase is lower in 1980 than in 2000 (the ratios
196 of JJA to DJF emissions for 40 - 70°N are 1.12 and 1.46 respectively), and this could make a
197 difference to the seasonal cycle of Arctic BC. It should be noted that the AR5 SO_2 emissions for
198 years 1980 and 2000 have the similar difference in DJF between 40°N and 70°N (113% higher
199 emission in 1980; figure not shown).

200 Figure S2 compares simulated DJF BC in two identical simulations (based on the ALL_m7
201 configuration) but with the 1980 emissions and 2000 emissions, respectively. The zonal-mean
202 BC burden is smaller in the 1980 simulation south of 40°N (consistent with the distribution of
203 BC emissions) but is larger (by a factor of 1.5) from 50°N to 90°N . Previous studies have
204 identified N. Europe and Russia as major source regions for Arctic haze (Shindell et al., 2008;
205 Matsui et al., 2011), and the large 1980 to 2000 emissions change between 40°N and 70°N is
206 likely responsible for the difference in Arctic BC between the two simulations. Larger total
207 burden leads to larger cloud-borne burden and wet deposition flux as well, but the total removal
208 rates are almost identical in the two simulations (see Fig. S2b). The Arctic sulphate burden and
209 surface mixing ratios are doubled under the 1980 emissions scenario due to the even larger
210 increase in SO_2 emission than in 2000 (figure not shown).

211 With the 1980 emission, the predicted surface BC and sulphate seasonality over the Arctic
212 sites is further improved. This is because of the stronger DJF sources between 40° - 70°N in the

213 1980 emission inventory than in the 2000's, which more effectively increases the Arctic BC and
214 sulphate mixing ratios (from the surface to about 600 hPa) than sources from lower latitudes.

215 **4. Tables for model-observation comparison**

216 Table S1 summarizes how the modifications to CAM5 impact the simulated surface-level
217 BC compared to observations from three networks/compilations. In Liu et al. (2011b) and Wang
218 et al. (2011a), simulated BC are compared to observations from the IMPROVE and EMEP
219 networks and the combined compilations of Liou et al. (1996) and Cooke et al. (1999). Table
220 S1 lists the multi-site means and medians for these three datasets and additionally for the Zhang
221 et al. (2008) China dataset. The changes between the various simulations are considerably
222 smaller at these surface sites than the changes to the global annual burdens (Table 2 in the text).
223 This is not surprising for the IMPROVE and EMEP networks, where the sites are in the
224 continental US and Europe, relatively close to sources. The slower BC aging has small impacts
225 for the same reasons. The unified convection treatment lowers the simulated values at the sites
226 slightly, although it increases the global burden. The simulation with 1980 emissions has
227 noticeably higher mixing ratios over the IMPROVE and EMEP network sites because of
228 emissions changes in these regions. The simulated values for the base model configurations are
229 lower than observed, so model changes that increase BC burden and transport to the Arctic also
230 reduce the CAM5 low-bias for these datasets. All the simulations strongly underestimate the
231 China observations from Zhang et al. (2008), suggesting that BC emissions for this region may
232 be significantly underestimated. One of the most notable features is that the MMF simulation
233 gives much lower surface mixing ratios for the three datasets than the CAM5std and the CTRL
234 simulation, although the MMF global burden is about 50% higher. As shown in the BC vertical
235 distributions (see Figs. 9, 10 and 11), CAM5 often predicts a stronger near-surface peak than the

236 MMF at low- and mid-latitudes, suggesting stronger boundary-layer turbulent mixing and
237 vertical transport in the MMF. Correlation coefficients (not shown) vary only slightly between
238 the simulations, one exception being the 1980 emissions simulation and EMEP Network, but the
239 correlations are all rather low for that dataset.

240 Table S2 provides similar information for surface-level sulphate, using observations from the
241 IMPROVE, EMEP, and U. Miami (marine sites) networks. The changes between the various
242 simulations are larger than those for BC, but the changes are still smaller than the global annual
243 burden changes. As with BC, the changes increase sulphate mixing ratios, which increase the
244 high bias for the IMPROVE and EMEP continental sites, but improve (and even reverse) the low
245 bias for the U. Miami remote marine sites. The new unified convection (CONV) increases
246 surface mixing ratios, compared to the slight decrease for BC, which we attribute to their
247 different sources (locations and primary vs. secondary). Correlation coefficients again vary only
248 slightly between the simulations, except for the 1980 emissions simulation and EMEP Network.

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Table S1: Observed and simulated multi-site mean and median BC (in ng m^{-3} , with medians in parentheses) for IMPROVE network sites (annual means), EMEP network sites (annual means), Zhang et al. (2008) China sites, and Liousse et al. (1996) and Cooke et al. (1999) compilations (various time periods; L96&C99). The IMPROVE, EMEP, and Liousse-Cooke sites correspond to Figures 11a, 11b, and 13b of Liu et al. (2011b), respectively.

Case	IMPROVE	EMEP*	China**	L96&C99
Observed	257. (215.)	730. (620.)	3015. (3600.)	398. (123.)
MMF	148. (119.)	295. (290.)	652. (614.)	179. (47.)
CAM5std	206. (153.)	410. (391.)	891. (854.)	242. (61.)
CTRL	214. (158.)	423. (413.)	948. (914.)	256. (51.)
CONV	214. (160.)	409. (397.)	906. (882.)	242. (57.)
CONV_sact	209. (156.)	396. (387.)	918. (885.)	239. (65.)
CONV_FD	215. (166.)	422. (400.)	950. (905.)	247. (74.)
CONV_SF	218. (166.)	435. (416.)	968. (901.)	257. (67.)
CONV_m7	226. (170.)	430. (409.)	990. (914.)	260. (66.)
ALL_m3	222. (172.)	436. (412.)	967. (904.)	252. (64.)
ALL_m7	238. (190.)	476. (424.)	1049. (995.)	277. (75.)

* The 2 “urban background” sites (see Table 1 of Yttri et al., 2007) are excluded.

** The 5 sites in the “urban group” (see Table 2 of Zhang et al., 2008) are excluded.

Table S2: Observed and simulated multi-site means and medians for annual average sulphate (in $\mu\text{g m}^{-3}$, with medians in parentheses) for IMPROVE, EMEP, and University of Miami network sites. The IMPROVE, EMEP, and U. Miami sites correspond to Figures 9a, 9b, and 10 of Liu et al. (2011b), respectively.

Case	IMPROVE	EMEP	U. Miami
Observed	1.59 (0.98)	2.37 (2.18)	0.94 (0.43)
MMF	2.17 (1.81)	2.64 (2.80)	1.01 (0.61)
CAM5std	2.06 (1.63)	2.27 (2.39)	0.63 (0.35)
CTRL	2.23 (1.74)	2.44 (2.50)	0.68 (0.35)
CONV	2.37 (1.90)	2.52 (2.59)	0.83 (0.49)
CONV_sact	2.30 (1.85)	2.39 (2.48)	0.81 (0.42)
CONV_FD	2.44 (1.92)	2.62 (2.67)	0.87 (0.50)
CONV_SF	2.59 (2.05)	2.79 (2.94)	0.93 (0.54)
CONV_m7	2.44 (1.87)	3.10 (3.31)	0.87 (0.52)
ALL_m3	2.60 (2.00)	2.84 (2.92)	0.89 (0.54)
ALL_m7	2.74 (2.04)	3.64 (3.92)	0.97 (0.59)

Table S3: Observed (as listed in Table 1 of Wang et al., 2011b) and simulated global annual mean LWP, total precipitation rate (PRECT), residual fluxes at surface (RESSURF) and top of the model atmosphere (RESTOM) and cloud forcing (SWCF and LWCF).

Case	LWP (g m ⁻²)	IWP (g m ⁻²)	PRECT (mm d ⁻¹)	SWCF (W m⁻²)	LWCF (W m ⁻²)
Observed	(50,87)	-	2.61	(-46, -53)	(27, 31)
MMF	55.88	9.87	2.85	-50.48	25.96
CAM5std	41.15	17.77	2.96	-49.12	23.67
CTRL	41.04	17.17	2.98	-48.19	22.78
CONV	47.02	17.30	2.95	-51.42	23.78
CONV_sact	46.22	17.79	2.94	-52.06	24.74
CONV_FD	47.30	17.19	2.93	-50.17	23.60
CONV_SF	48.82	17.46	2.94	-52.00	24.03
CONV_m7	46.84	16.94	2.93	-50.64	23.40
ALL_m3	48.62	17.76	2.92	-51.60	24.84
ALL_m7	48.13	17.46	2.90	-50.69	24.39

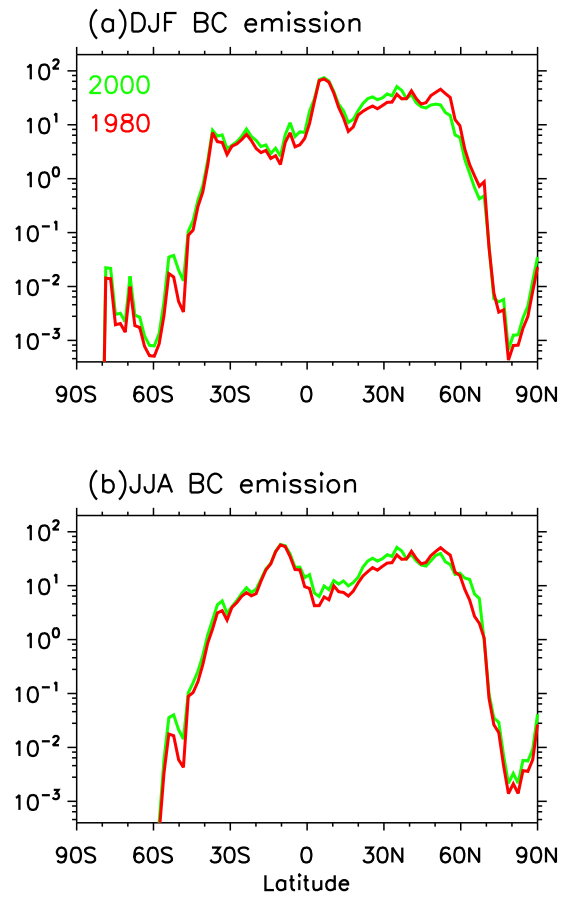


Figure S1: Seasonal zonal-mean BC emission rates ($kg C km^{-2} yr^{-1}$) for the year of 2000 and 1980 in (a) DJF and (b) JJA months.

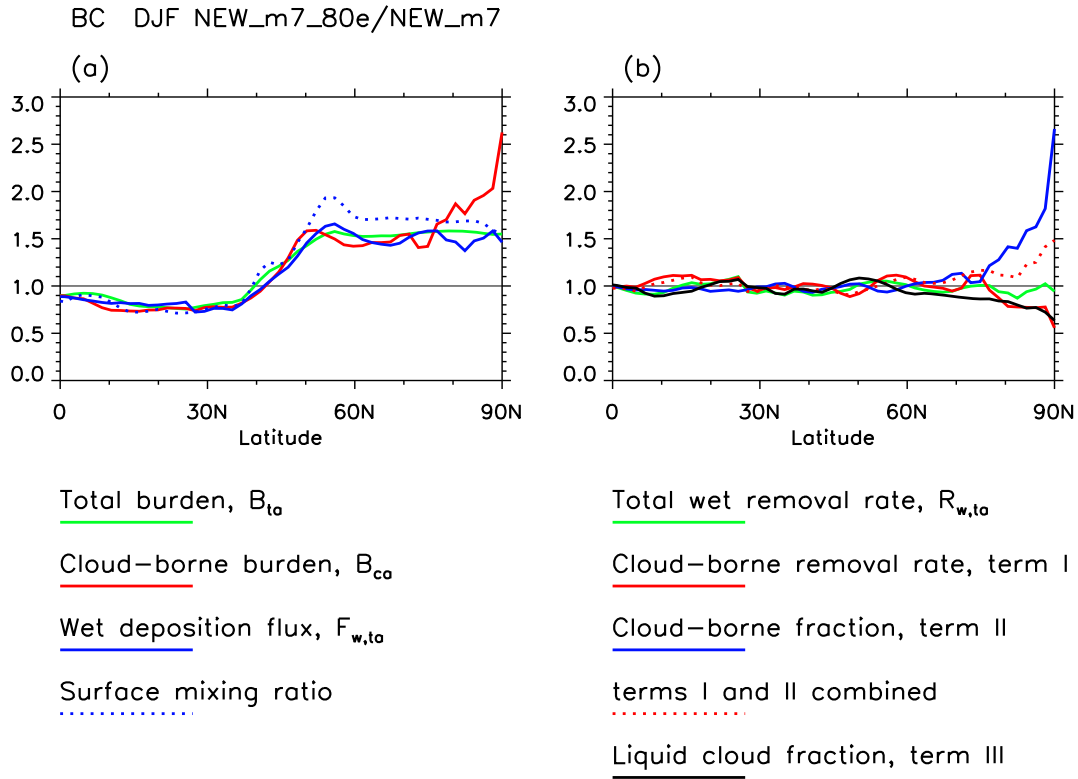


Figure S2: the ratios of the quantities related to BC burden and wet removal, as described in Eqs. (1-3) in the text, derived from two CAM5 simulations (close to the ALL_m7 setup) with year 1980 emissions and 2000 emissions respectively. Quantities are averaged zonally and over the Northern Hemisphere winter months (DJF).