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An approach to computing direction relations between separated object groups

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Abstract

Direction relations between object groups play an important role in qualitative spatial reasoning, spatial computation and spatial recognition. However, none of existing models can be used to compute direction relations between object groups. To fill this gap,

5 an approach to computing direction relations between separated object groups is proposed in this paper, which is theoretically based on Gestalt principles and the idea of multi-directions. The approach firstly triangulates the two object groups; and then it constructs the Voronoi Diagram between the two groups using the triangular network; after this, the normal of each Voronoi edge is calculated, and the quantitative expression
10 of the direction relations is constructed; finally, the quantitative direction relations are transformed into qualitative ones. The psychological experiments show that the proposed approach can obtain direction relations both between two single objects and between two object groups, and the results are correct from the point of view of spatial cognition.

15 1 Introduction

Direction relation, along with topological relation (Egenhofer and Franzosa, 1991; Roy and Stell, 2001; Li et al., 2002; Schneider and Behr, 2006), distance relation (Liu and Chen, 2003), and similarity relation (Yan, 2010), has gained increasing attention in the communities of geographic information sciences, cartography, spatial cognition,
20 and various location-based services (Cicerone and De Felice, 2004) for years. Its functions in spatial database construction (Kim and Um, 1999), qualitative spatial reasoning (Frank, 1996; Sharma, 1996; Clementini et al., 1997; Mitra, 2002), spatial computation (Ligozat, 1998; Bansal, 2011) and spatial retrieval (Papadias and Theodoridis, 1997; Hudelot et al., 2008) have attracted researchers' interest. Direction relation has also
25 been used in many practical fields (Zimmermann and Freksa, 1996; Kuo et al., 2009), such as combat operations (direction relation helps soldiers to identify, locate, and

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predict the location of enemies), driving (direction relation helps drivers to avoid other vehicles), and aircraft piloting (direction relation assists pilots to avoid terrain, other aircrafts and environmental obstacles).

A number of models for describing and/or computing direction relations have been proposed, including the cone-based model (Peuquet and Zhan, 1987; Abdelmota and Williams, 1994; Shekhar and Liu, 1998), the 2-D projection model (Frank, 1992; Nabil et al., 1995; Safar and Shahabi, 1999), the direction-relation matrix model (Goyal, 2000), and the Voronoi-based model (Yan et al., 2006). These models can compute direction relations between two single objects, but can not compute direction relations between two object groups. Nevertheless, objects on maps may be viewed as groups in many cases in light of Gestalt principles, such as proximity, similarity, common orientation/direction, connectedness, closure, and common region (Palmer, 1992; Weibel, 1996; Yan et al., 2008). In other words, objects close to each other, with similar shape and/or size, arranged in a similar direction, topologically and/or visually connected, with a closed tendency, and/or in the same region have a tendency to be viewed as a group (Fig. 1). Four categories of object groups can be differentiated according to the geometric ingredients of the single objects, i.e. point, linear, areal/polygonal, and complex object groups. Figure 2 shows a number of pairs of object groups. Thus, it is of great importance to find methods to obtain direction relations between object groups.

Because none of the models for computing direction relations between object groups has been proposed, this paper will focus on filling this gap. After the introduction (Sect. 1), existing models for computing direction relations will be discussed (Sect. 2); then the theoretical foundations of the new approach will be presented (Sect. 3), and a Voronoi-based model for computing directions between object groups will be proposed (Sect. 4); after that, a number of experiments will be shown to demonstrate the validity of the proposed approach (Sect. 5); finally, some conclusions will be made (Sect. 6).

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2 Analysis of existing models

To propose a model for computing direction relations between object groups, it should be pertinent to summarize and analyze existing ones previously to show their advantages and disadvantages.

5 To facilitate the discussion in the following sections, it is designated that

1. A is the reference object (or object group), and B is the target object (or object group);
2. $\text{Dir}(A, B)$ is the qualitative description of direction relations from A to B ;
3. $D(A, B)$ is the quantitative description of direction relations from A to B ; and
4. Only extrinsic reference frame is employed for direction relations.

10

15

- The cone-based model (Peuquet and Zhan, 1987) partitions the 2-dimensional space around the centroid of the reference object into four direction regions corresponding to the four cardinal directions (i.e. N, E, S, W). The direction of the target object with respect to the reference object is determined by the target object's presence in a direction partition for the reference object. If the target object coincides with the reference object, the direction between them is called "same".

This model is developed primarily to detect whether a target object exists in a given direction or not. If the distance between the two objects is much larger than their size, the model works well; otherwise special method must be used to adjust the area of acceptance.

20

If objects are overlapping, intertwined, or horseshoe-shaped, this model uses centroids to determine directions (Peuquet and Zhan, 1987) and the results are misleading sometimes. In addition, if a target object is in multiple directions, such as {N, NE, E}, this model does not provide a knowledge structure to represent multiple directions (Goyal, 2000).

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5 The 2-D projection model approximates objects by their MBRs; therefore, the spatial relation may not necessarily be the same as the relation between exact representations of the objects, because the model can not capture the details of objects in direction descriptions (Goyal, 2000). So this model can be only used for the qualitative description of direction relations.

10 15 The direction-relation matrix model (Goyal, 2000) partitions space around the MBR of the reference object into nine direction tilts, i.e. N, NE, E, SE, S, SW, W, NW, and O (same direction). A direction-relation matrix is constructed to record if a section of the target object falls into a specific tilt. Further, to improve the reliability of the model, a detailed direction-relation matrix capturing more details by recording the area ratio of the target object in each tilt is employed.

20 25 The direction-relation matrix model provides a knowledge structure to record multi-level directions. However, it can not obtain $D(A, B)/\text{Dir}(A, B)$ from $D(B, A)/\text{Dir}(B, A)$ and vice versa (Yan et al., 2006).

– The Voronoi-based model (Yan et al., 2006) uses “direction group” because people describe directions between two objects using multiple directions. A direction group consists of multiple directions, and each direction includes two components: the azimuths of the normals of direction Voronoi edges between two objects and the corresponding weights of the azimuths (Fig. 3).

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The Voronoi-based model can describe direction relations quantitatively and qualitatively, and can obtain $D(B, A)$ by $D(A, B)$. Direction relations are recorded in 2-dimensional tables.

The above four models may be compared using the following five criteria (Goyal,
5 2000; Yan et al., 2006).

1. Simplicity: computation of the direction relations between arbitrary two objects is not time-consuming, and the model is easy to be understood;
2. inversion: $\text{Dir}(B, A)/D(B, A)$ can be obtained by $\text{Dir}(A, B)/D(A, B)$;
3. correctness: results obtained is consistent with human's spatial cognition;
- 10 4. quantification: the model can give quantitative representations of direction relations; and
5. qualification: the model can give qualitative representations of direction relations.

Table 1 shows the advantages and disadvantages of the above models. Obviously, none of the existing models meet the five criteria. And particularly, none of them can
15 be used to compute direction relations between object groups.

3 Theoretical foundations of multi-directions

Direction relations between object groups need to be described using multiple directions in many cases. The examples of multiple directions are very common in the geographic space. Especially, if two object groups are intertwined, enclosed, or overlapping
20 with each other, descriptions of direction relations with multiple directions becomes unavoidable.

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3.1 Examples of multi-directions

- Example 1: UniRoad composed of three roads passes through University A composed of many buildings (Fig. 4). The direction relations between the road and the university can not be simply described by a single cardinal direction.
- Example 2: A very common case is: a road runs approximately parallel with a river. In Fig. 5, a man may say “the road is to the northeast of the river” when he is at P ; and he maybe say “the road is to the north of the river” when he is at Q ; however, if he walks to R , he may say: “the road is to the east of the river.” Nevertheless, all three answers are intuitively partial and unacceptable. To give a whole description, it is reasonable to combine of the three answers.
- Example 3: In Fig. 6, village A (a group of buildings) is half-enclosed by river R (a group of river branches). A single cardinal direction obtained by the cone-based model (e.g. A is at the south of R) can not describe their direction relations clearly.

3.2 Cognitive explanation of multi-directions

From the point of view of perception, in any case, the following two principles remain unquestionable in direction judgments.

- Relations between the sum of the whole and its parts: “The sum of the whole is greater than its parts” (Wertheimer, 1923; Clifford, 2002) is the idea behind the principle of Gestalt. It’s the perception of a composition as a whole. Human’s perception of the piece is based on their understanding of all the bits and pieces working in unison.
- People usually ignore the trivial of spatial objects but get the sketches of the whole before they judge directions. Their judgments are based on the sketches

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5 but not on details. This process implies the idea of cartographic generalization. The generalization methods in direction judgments are a little bit different from that used in traditional map generalization (Weibel, 1996). The generalization scale depends on the size of the field formed by the two object groups. The larger the distance between the two groups, the larger the objects are generalized.

Proximity: The principle of proximity or contiguity states that nearby objects can be regarded as a group and more correlated (Alberto and Charles, 2011).

Such examples exist almost everywhere in daily life. In Fig. 6, the three directions are obtained by the three pairs of proximal sections of the road and the river. Hence, 10 “Judging directions by proximal sections” will be one of the most important principles in the new model.

3.3 Expression of multi-directions

In our daily life, when a man says “the hospital is to the east of the school”, he generally has an imaginary ray (here, ray is directly borrowed from its mathematical concept) 15 in his brain, pointing from the hospital to the school indicating the direction. Hence, it is a natural thought to express direction relations using such rays. If multi-directions exist between two object groups, a combination of multiple rays can be utilized to denote their direction relations, each ray corresponding to a cardinal direction (Yan et al., 2006). For example, in Fig. 6, the directions from the river (A) to the road (B) may be 20 expressed using a direction set $\text{Dir}(A, B) = \{\text{NE}, \text{N}, \text{E}\}$.

3.4 Reasonability of using Voronoi Diagram to express directions

It is difficult to get a certain ray pointing from one object to another; however, the 25 normals of the ray, i.e. the Voronoi Diagram of the two objects, can be obtained. Because a ray and its normal are perpendicular to each other, the ray can be obtained easily by its normals.

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Figure 7 presents the Voronoi Diagrams and the ray between two point objects and between a point object and a linear object, respectively. Obviously, each of the rays (normal of the Voronoi Diagram) denotes the direction relations.

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4 A Voronoi-based model

5 To simplify the following discussion, the two object groups in Fig. 6 will be used as an example. Here, River basin R is the reference object group; the village V is the target object group. The eight-direction system (i.e. eight directions E, NE, N, NW, W, SW, S, and SE are discerned) will be employed. Because both quantitative and qualitative direction relations are widely used in daily life, the proposed model will express direction
10 relations in quantitative and qualitative ways.

4.1 Framework of the model

The new model for computing quantitative and direction relations consists of four procedures:

15 1. cartographic generalization of the two object groups;
2. construction of the Voronoi Diagram;
3. computation of quantitative direction relations; and
4. construction of qualitative direction relations.

4.2 Cartographic generalization of the two object groups

According to “the relations between the sum of the whole and its parts”, cartographic
20 generalization is a first necessary step in human’s direction judgments. This procedure aims at simplifying object groups so that direction computation can be done in a simple way.

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Suppose that the diameter of convex hull of the two objects is d , formula (1) is used to simplify spatial objects.

$$S = d \times [1 - \cos(\varepsilon/2)]/2 \quad (1)$$

Where, S is the generalization scale of the objects, i.e. the details whose size are less than S will be simplified; ε is an angle. It equals 90° in the four-direction system and 45° in the eight-direction system.

The generalized result of Fig. 6 is shown in Fig. 8a, which can be used for computing direction relations in the eight direction system.

4.3 Construction of the Voronoi Diagram

10 It is well known that Delaunay triangulation is a useful and efficient tool in spatial adjacency/proximity analysis (Li et al., 2002); hence, it is used to get proximal sections of the two object groups. On the other hand, the Delaunay triangular network and the Voronoi Diagram are dual of each other (Arias et al., 2011); thus the Voronoi Diagram of the two object groups can be easily obtained by their Delaunay triangular network.

15 The Voronoi Diagram can be obtained by following steps.

First, construct a point set consisting of all of the vertices of the two object groups.

Second, construct the Delaunay triangular network (Fig. 8b) of the point set.

If the three vertices of a triangle belonging to one object group, it is called a “first type triangle”; otherwise, it is called a “second type triangle”.

20 Next, delete all of the first type triangles. The remaining triangles compose the proximal area (Fig. 8c) of the two groups.

Finally, generate the Voronoi Diagram (Fig. 8d) using the remaining triangles.

4.4 Computation of quantitative direction relations

25 The Voronoi Diagram of two object groups generally consists of $n \geq 1$ Voronoi edges (e.g. the Voronoi Diagram in Fig. 8d has 15 edges); each Voronoi edge has a normal.

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Hence, a total of n normals can be obtained to denote the direction pointing from the reference object group to the target object group. In other words, there are n directions between the two object groups.

To describe direction relations quantitatively with the n directions, following three strategies are employed.

- A single direction can be described using the azimuth of the normal of the Voronoi edge.

An azimuth of a ray is the angle measured clockwise from the positive end of the vertical axis of the Cartesian coordinate system to the ray. Figure 9 shows the azimuth (α) of ray OA.

- To differentiate the importance of each direction, each direction is assigned a weight value which is the percentage of the length of each corresponding Voronoi edge.

Because each Voronoi edge corresponds to a single direction, the Voronoi Diagram may be generalized using formula (1) as the criteria to simplify the final expression of the direction relations.

- To facilitate saving direction relations in databases, all of the azimuths and their corresponding weights are listed in a 2-dimensional table.

The generalized Voronoi Diagram in Fig. 8d is shown in Fig. 10. Its Voronoi edges are labeled. Table 2 presents the quantitative direction relations of the two object groups. Each direction consists of an angle and a weight value. This quantitative result can be expressed as $D(R, V) = \{\langle 1, 11 \rangle, \langle 82, 20 \rangle, \langle 133, 26 \rangle, \langle 205, 16 \rangle, \langle 237, 27 \rangle\}$.

4.5 Construction of qualitative direction relations

To qualify the quantitative direction relations, following two steps are needed.

- Change the azimuths into qualitative directions.

In the eight-direction system, north means an azimuth in $(337.5^\circ, 0^\circ] \cup (0^\circ, 22.5^\circ]$; northwest an azimuth in $(22.5^\circ, 67.5^\circ]$; east an azimuth in $(67.5^\circ, 112.5^\circ]$; southeast an azimuth in $(112.5^\circ, 157.5^\circ]$; south an azimuth in $(157.5^\circ, 202.5^\circ]$; southwest an azimuth in $(202.5^\circ, 247.5^\circ]$; west an azimuth in $(247.5^\circ, 292.5^\circ]$; northwest an azimuth in $(292.5^\circ, 337.5^\circ]$.

- Combine the same cardinal directions, and add up their corresponding weights.

Table 3 shows the qualitative description of direction relations from R to V in Fig. 8. The directions of edge 4 and edge 5 are the same (SW); hence, they are combined and their weights are added up. This result can be $\text{Dir}(R, V) = \{\langle N, 11 \rangle, \langle E, 20 \rangle, \langle SE, 26 \rangle, \langle SW, 43 \rangle\}$. The qualitative description of direction relations in Fig. 8 is: 11 % of V is to the north of R , and 20 % of V is to the east of R , and 26 % of V is to the south east of R , and 43 % of V is to the south west of R .

5 Experiments and discussions

Whether the proposed approach is correct and valid should be tested by psychological experiments, because judgments of directions are rooted in human's spatial cognition (Egenhofer and Shariff, 1998; Gayal, 2000). For this purpose, the direction relations of 40 pairs of object groups were computed using a C# program implemented by the authors. They were drawn in a table and distributed to 33 testee (all testees are graduates of Lanzhou Jiaotong University, China). The natural language description of direction relations were attached to each pair of object groups. The testees were required to answer if they "totally agree", "agree", "unsure", or "do not agree" with each answer.

Figure 11 and Table 4 give eight typical examples of our experiment. The result of the psychological test is listed in Table 5. Some insights can be gained from the experiments.

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reasoning. Our further research will focus on improving this approach so that it can be used to process topologically intersected and/or contained object groups.

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Table 1. Comparison of the existing models.

Models	Simplicity	Inversion	Correctness	Qualification	Quantification
Cone-based model	Yes	Yes	Not always	Yes	No
2-D projection model	Yes	Yes	Not always	Yes	No
Direction-relation matrix model	Yes	No	Not always	Yes	Yes
Voronoi-based model	No	Yes	Yes	Yes	Yes

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Table 2. Quantitative expression of direction relations from R to V in Fig. 8.

labeled edge	Azimuth (°)	Weight (%)
1	1	11
2	82	20
3	133	26
4	205	16
5	237	27

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Table 3. Qualitative expression of direction relations from R to V in Fig. 8.

labeled edge	Direction	Weight (%)
1	N	11
2	E	20
3	SE	26
4, 5	SW	$16 + 27 = 43$

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Table 4. Qualitative direction relations of the pairs of object groups (the percentages are the weights of the directions).

Pair of groups	N %	NW %	W %	SW %	S %	SE %	E %	NE %
Fig. 11a	73.67	11.48						14.85
Fig. 11b	26.82	49.05	2.75					21.38
Fig. 11c	19.34	10.90	13.41	11.10	19.82	12.24	5.10	8.09
Fig. 11d	50.07	49.93						
Fig. 11e	5.03	13.82		18.54	21.40	1.58	21.87	17.75
Fig. 11f	34.44		5.81		33.80		20.69	5.26
Fig. 11g	16.17	5.66	1.78	14.83	24.28	2.23	17.95	17.10
Fig. 11h	12.94	5.74	4.67	8.15	18.14	13.93	19.58	16.85

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Table 5. Statistical results of the psychological test (%).

Pair of groups	Totally agree	Agree	Unsure	Do not agree
Fig. 11a	70	24	3	3
Fig. 11b	30	34	24	12
Fig. 11c	67	27	6	
Fig. 11d	67	27	6	
Fig. 11e	67	27	6	
Fig. 11f	48	36	16	
Fig. 11g	67	27	3	3
Fig. 11h	39	48	10	3
Mean	56.9	31.2	9.3	2.6

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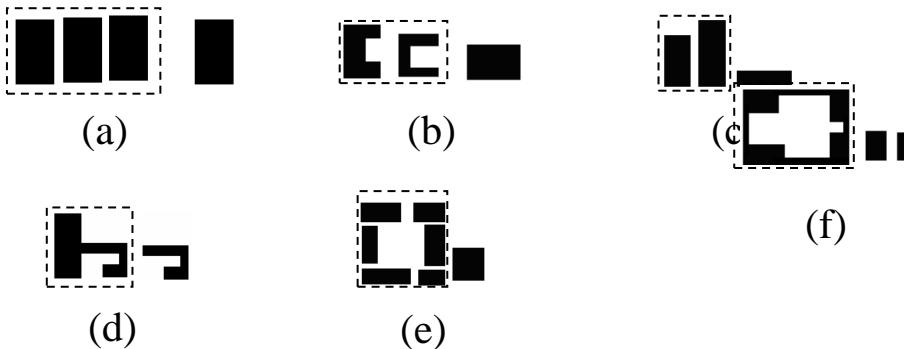


Fig. 1. Objects on maps are viewed as a group in light of the Gestalt principles: **(a)** proximity; **(b)** similarity; **(c)** similar direction; **(d)** connectedness; **(e)** closed tendency; and **(f)** same region. Note: the objects enclosed by a dash-lined rectangle are viewed as a group.

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Fig. 2. Examples of various pairs of object groups: **(a)** points-points; **(b)** points-lines; **(c)** points-polygons; **(d)** lines-lines; **(e)** lines-polygons; **(f)** polygons-polygons; **(g)** line-complex; and **(h)** complex-complex.

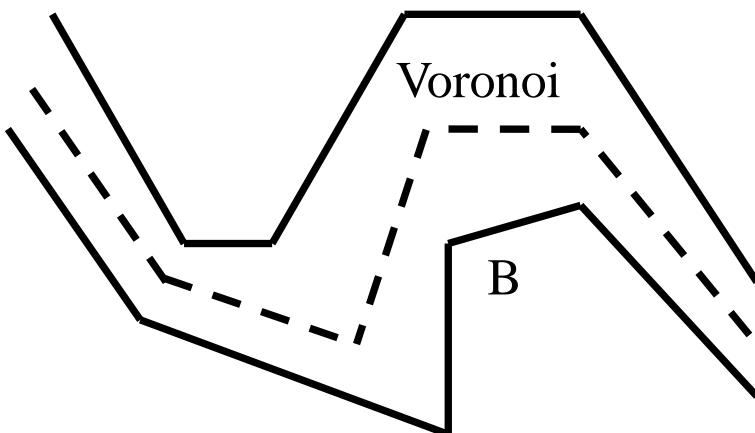


Fig. 3. Principle of the Voronoi-based model used to describe direction relations between single objects.

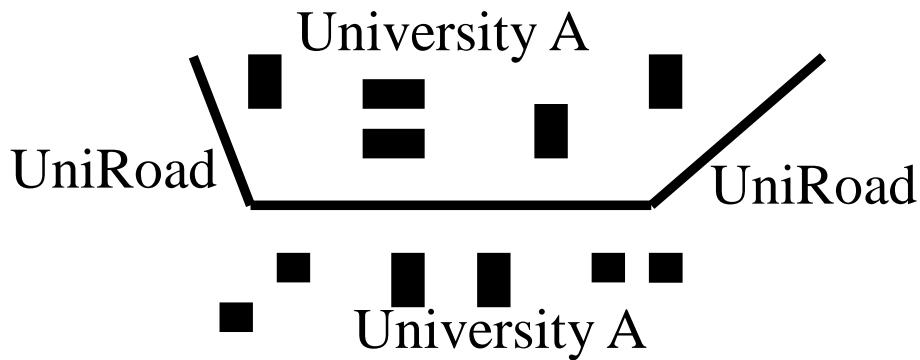


Fig. 4. Multi-directions are needed when two object groups are intertwined.

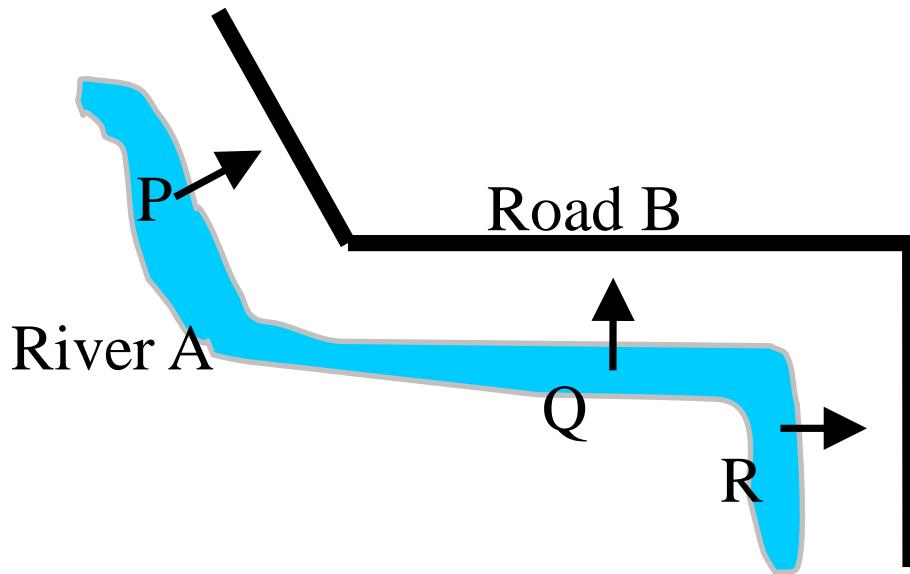


Fig. 5. Multi-directions between two approximately parallel object groups.

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A map of a river basin labeled "River basin R". The basin is roughly triangular in shape, with a winding river boundary. Inside the basin, a cluster of black squares represents "Village V".

Fig. 6. If an object group is half-enclosed by another group, a single direction is not enough to describe their direction relations.

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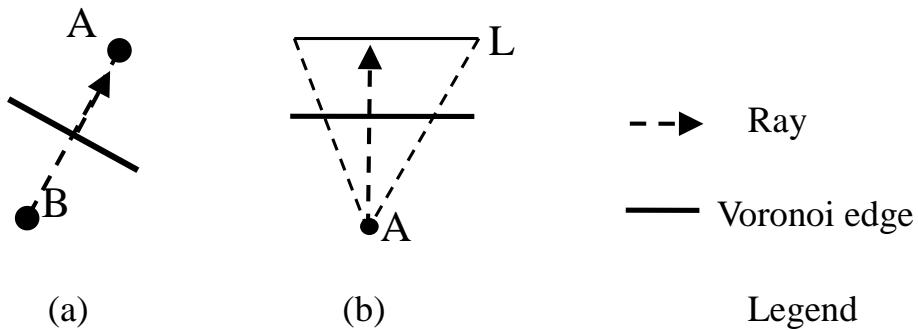


Fig. 7. Normals of the Voronoi edges used to denote directions.

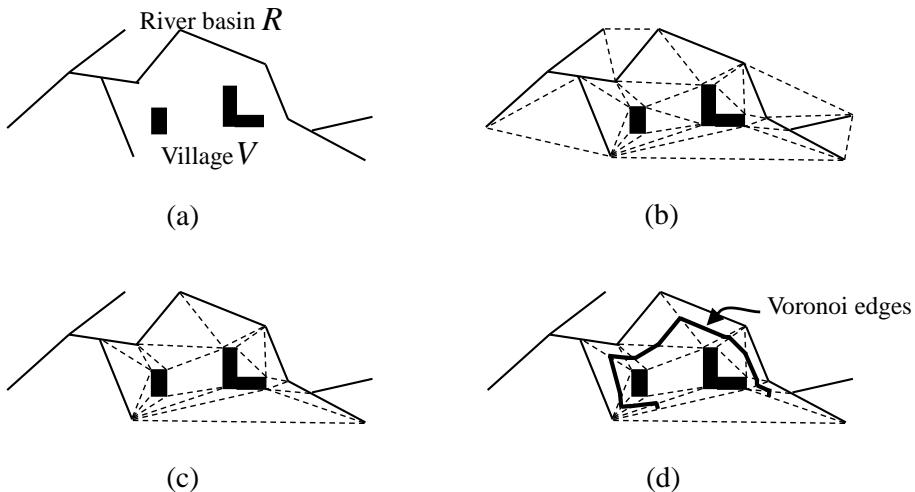


Fig. 8. Procedures of computing direction relations between two object groups: **(a)** generalized object groups; **(b)** triangulation of the object groups; **(c)** proximal sections of the object groups; and **(d)** Voronoi Diagram.

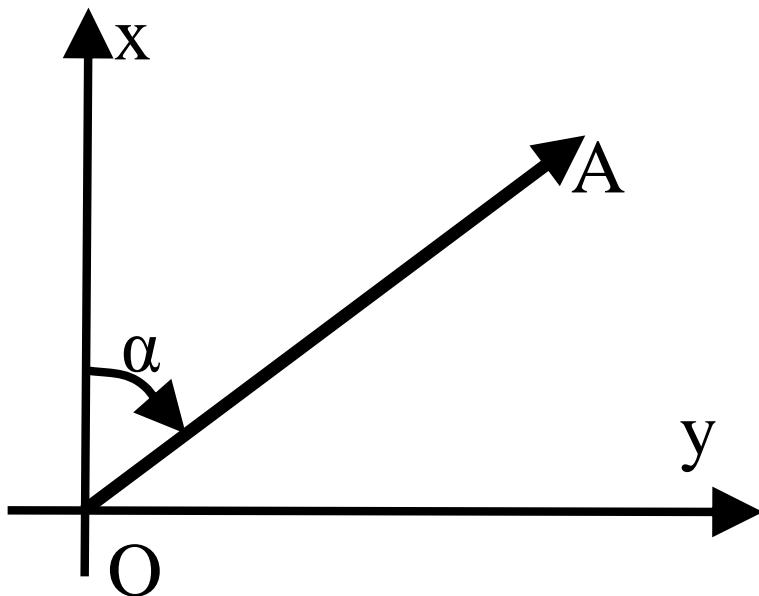
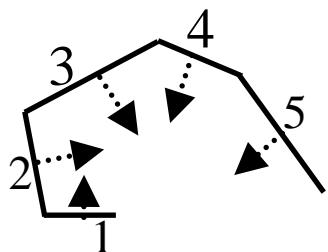


Fig. 9. Definition of azimuth.

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Legend
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Fig. 10. Simplified and labeled Voronoi edges with normals.

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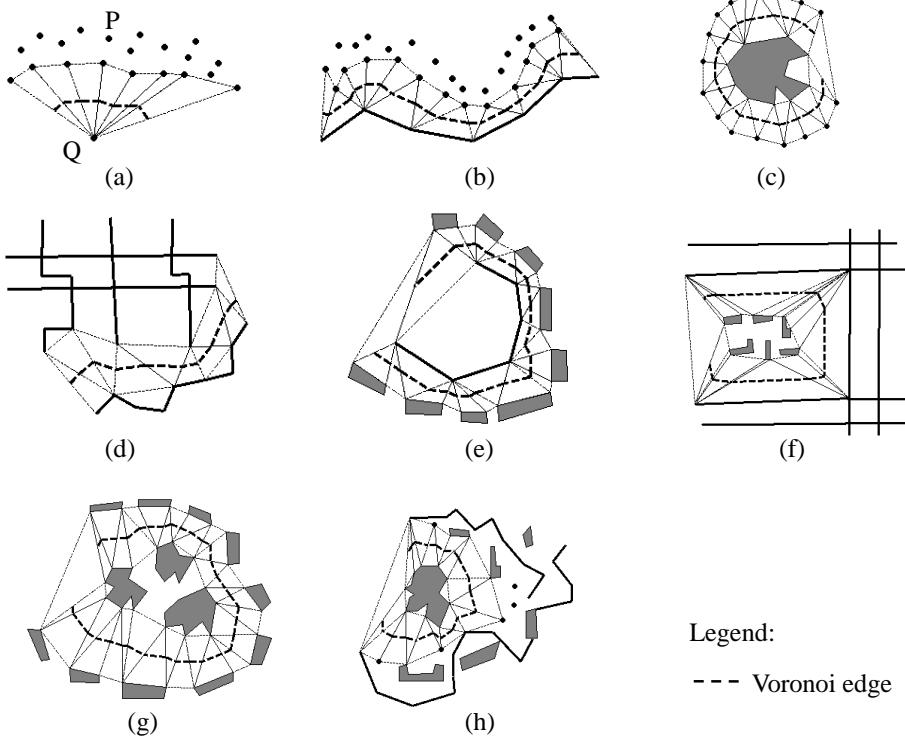


Fig. 11. Examples of pairs of object groups used in the experiment: **(a)** point → point group; **(b)** line → point group; **(c)** polygon → point group; **(d)** line → line network; **(e)** line → linear arranged polygon group; **(f)** polygon group → line network; **(g)** polygon cluster → linear arranged polygon group; **(h)** polygon → complex group with polygons, lines and points.