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Using model reduction to predict the soil-surface C18OO flux: an example of representing complex biogeochemical dynamics in a computationally efficient manner

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Abstract. Earth system models (ESMs) must calculate largescale interactions between the land and atmosphere while accurately characterizing fine-scale spatial heterogeneity in water, carbon, and other nutrient dynamics. We present here a high-dimension model representation (HDMR) approach that allows detailed process representation of a coupled carbon and water tracer (the δ^{18} O value of the soil-surface CO₂ flux (δF_s) in a computationally tractable manner. δF_s depends on the δ^{18} O value of soil water, soil moisture and temperature, and soil CO2 production (all of which are depth dependent), and the δ^{18} O value of above-surface CO₂. We tested the HDMR approach over a growing season in a C₄dominated pasture using two vertical soil discretizations. The difference between the HDMR approach and the full model solution in the three-month integrated isoflux was less than 0.2% (0.5 mol m⁻² ‰), and the approach is up to 100 times faster than the full numerical solution. This type of model reduction approach allows representation of complex coupled biogeochemical processes in regional and global climate models and can be extended to characterize subgridscale spatial heterogeneity.

1 Introduction

Atmospheric CO₂ has substantial impacts on global climate, both over the long term and, as we have witnessed since the beginning of the industrial revolution, much shorter timescales (Watson et al., 2001). As a result, the impacts of anthropogenic CO₂ emissions and climate system feedbacks on the long-term state and stability of the climate are currently the focus of much research. Since interactions with the terrestrial biosphere dominate spatial and inter- and intraannual variations in atmospheric CO₂ concentrations (Tans et al., 1990), developing reliable models of ecosystem CO₂ exchanges is necessary to predict future climate.

Terrestrial carbon cycle models used at the site and regional scales and in Earth system models (ESMs; e.g., Bonan et al., 2002; Denning et al., 1996; Parton et al., 1988) are based on representations of varying complexity of the biological, chemical, and physical processes governing carbon exchanges between the atmosphere, soils, and plants. In ESMs, however, the level of process representation possible is often a trade-off between the desire to mechanistically represent the process, ability to characterize surface and subsurface properties, and computational constraints. It is also now recognized that land models must represent some of the subgrid-scale heterogeneity known to exist at scales substantially finer than those represented in current ESMs ($\sim 100 \,\mathrm{km}$ resolution; King et al., 2010; Thompson et al., 2011), either explicitly or by integrating scaling rules based on mechanistic process representation.

Land models are often tested and calibrated against field eddy covariance measurements of net CO2 ecosystem exchange (NEE) (Baldocchi et al., 2001). Difficulties in interpreting these NEE measurements arise from landscape horizontal and vertical heterogeneity, footprint uncertainty, unsteady conditions, and stable nocturnal conditions (Aubinet et al., 2000; Baldocchi, 2003; Goulden et al., 1996). Further, ecosystem model development requires accurate estimates of the gross CO_2 fluxes comprising the net flux, i.e., the assimilated (photosynthetic) and respired fluxes. This partitioning is necessary since the processes controlling these fluxes respond differently to environmental forcings and therefore require separate model formulations and parameterizations.

Measurements of the stable isotope 18 O in CO₂ have been proposed as a tracer to partition measured net CO₂ fluxes into component gross fluxes (Yakir and Wang, 1996), identify regional distributions of CO₂ exchanges (Ciais et al., 1997a, b; Cuntz et al., 2003; Francey and Tans, 1987; Peylin et al., 1999), and investigate interactions between the C and water cycles (Buenning et al., 2012; Wingate et al., 2009). However, using measurements of 18 O in CO₂ for these methods requires accurate estimation of the δ^{18} O value of the soil-surface CO₂ flux (δF_s (‰)), which depends on a complex suite of interactions between the C and water cycles (Riley et al., 2002; Tans, 1998). Using this example, we illustrate here a computationally efficient approach to represent these dynamics in a manner appropriate for inclusion in regional and global models.

CO₂ is produced in soils by heterotrophic respiration and autotrophic root respiration. The depth distribution and magnitude of the soil CO₂ source depends on soil moisture and temperature, microbial substrate and nitrogen availability and quality, and root activity (e.g., Grant et al., 2001). Once produced, the dominant CO₂ transport pathway to the atmosphere is via diffusion through open soil pores. Although not impacting the gross CO₂ flux, hydration and subsequent partitioning back into the gas phase can substantially change the δ^{18} O value of the soil-gas CO₂. Upon dissolution, CO₂ can exchange ¹⁸O atoms with the water, thereby acquiring the ¹⁸O composition of the water. The impact of this exchange on the δ^{18} O value of soil water ($\delta_{\rm sw}$ (‰)) is small, since there are orders of magnitude more H2O than CO2 molecules in soil moisture. The competition between CO₂ diffusion through the open pore space and dissolution into the soil water can substantially impact δF_s (Miller et al., 1999; Riley, 2005).

Three classes of methods to estimate $\delta F_{\rm s}$ have been reported. Several authors have hypothesized that a depthintegrated $\delta^{18}{\rm O}$ value of soil water and a constant effective kinetic fractionation factor can be used (Ciais et al., 1997a, b; Miller et al., 1999; Yakir and Wang, 1996). Tans (1998) developed steady-state analytical solutions for $\delta F_{\rm s}$, which Stern et al. (2001) applied to study the impact of invasion fluxes on the net surface C¹⁸OO exchange. Finally, numerical modeling approaches have been developed to account for transient conditions and gradients in the $\delta^{18}{\rm O}$ value of the various water pools impacting $\delta F_{\rm s}$ (e.g., ISOLSM from Riley et al., 2002; and Stern et al. , 1999).

ISOLSM has been integrated into the general circulation model CCM3 (Buenning et al., 2012) to investigate the impact of ecosystems on the δ^{18} O value of atmospheric CO₂ (δ_a). However, the soil-gas diffusion and reaction submodels in ISOLSM are computationally expensive. The high-dimension model representation (HDMR) method applied

here allows reduction of the full model to a series of lookup tables, while still characterizing second order interactions between variables important in the system. This approach substantially reduces simulation runtime (by up to a factor of 100), while still generating accurate δF_s predictions.

The following sections describe the methods used in ISOLSM to predict δF_s , the HDMR approach, and the specific application of HDMR to estimating δF_s . The HDMR model is then applied to a C₄-dominated grass ecosystem as a test of the approach in a dynamic simulation. Finally, we discuss potential applications of this type of approach to representing complex biogeochemical processes and spatial heterogeneity in ESMs.

2 Methods

2.1 Estimating δF_s using ISOLSM

ISOLSM integrates modules that simulate ^{18}O ecosystem exchanges in H_2O and CO_2 with the land-surface model LSM1 (Bonan, 1996). LSM1 is a "big-leaf" model that calculates internally consistent ecosystem energy, CO_2 , and H_2O exchanges with the atmosphere. Soil moisture, advective water fluxes, and temperature, all of which impact δ_{sw} , are calculated at user-defined depths in the soil.

The isotopic mechanisms integrated in ISOLSM are described in detail by Riley et al. (2002); the model has been applied in a number of other studies of isotope and bulk C and water dynamics (Aranibar et al., 2006; Cooley et al., 2005; Henderson-Sellers et al., 2006; Lai et al., 2006; McDowell et al., 2008; Riley et al., 2003, 2008, 2009; Riley, 2005; Still et al., 2009; Torn et al., 2011). A brief description of the model follows to illustrate the nature of the interactions impacting $\delta F_{\rm s}$. ISOLSM solves for $\delta_{\rm sw}$ using an explicit method with boundary conditions specified for the δ^{18} O values of precipitation and above-canopy vapor. Surface evaporation is calculated in LSM1 using a laminar soil-surface boundary layer resistance and the gradient between vapor concentrations at the soil surface and canopy air. A similar approach is taken in ISOLSM to compute the soil-surface H₂¹⁸O flux. In this case, though, the additional effects of an equilibrium partitioning factor and a different laminar boundary layer resistance for the heavier isotopologue are included. Root water withdrawal from the soil profile (driven by transpiration) is calculated using modules from LSM1; root H₂¹⁸O withdrawal occurs without isotopic fractionation. In this paper, δ_{sw} is presented relative to Vienna Standard Mean Ocean Water (V-SMOW).

ISOLSM solves the transient mass balance relationships for each isotopologue using a Crank–Nicholson approach. The model includes a soil moisture and temperature dependent effective diffusivity and CO_2 source profile and allows for variations in above-surface CO_2 concentration and $\delta^{18}O$ value. The net soil-surface CO_2 and $C^{18}OO$ fluxes (F_s and

Table 1. Parameters and state variables used to generate the expansion functions. Spatial discretization scenarios D_1 and D_2 correspond to eight 2.5 cm and four 5 cm control volumes, respectively, in the top 20 cm of soil. All HDMR simulations are performed by dividing each parameter range into 100 equal spaces (i.e., N = 100).

Parameter or state variable	Units	Range
Soil moisture	$m^{3} m^{-3}$	0.1, 0.5
Soil temperature	K	283, 303
$\delta_{\rm sw}$, soil water δ^{18} O value	‰ (V-SMOW)	-12, 10
δ^{18} O value of atmospheric CO ₂	‰ (V-PDB-CO ₂)	-1, 1
Soil CO ₂ production	$\mu \mathrm{mol}\mathrm{m}^{-2}\mathrm{s}^{-1}$	2, 8
z_0 , exponential decay parameter	m	0.05, 0.2

 $F_{\rm s}^{18}$, respectively (µmol m⁻² s⁻¹)) are computed from the concentration gradients and diffusivities at the soil surface. Finally, the $\delta^{18}{\rm O}$ value of the soil-surface CO₂ flux is calculated as

$$\delta F_{\rm s}^{18} = \left(\frac{F_{\rm s}^{18}/F_{\rm s}}{r_{\rm pdb}} - 1\right) 1000,\tag{1}$$

where r_{pdb} is the Vienna Pee Dee Belemnite (V-PDB-CO₂) standard. As applied here, ISOLSM uses 2.5 cm control volumes to solve for δ_{sw} and twenty unevenly spaced control volumes down to 1 m depth for the soil-gas calculations. Model testing is described in Riley et al. (2003), and an application of ISOLSM to analyze the impact of near-surface δ_{sw} on δF_{s} is presented in Riley (2005).

2.2 High-dimensional model reduction

The HDMR technique described here (termed the cut-HDMR) is a special application of a group of tools designed to represent high-dimensional models (Alis and Rabitz, 2001; Rabitz and Alis, 1999; Rabitz et al., 1999). HDMR was developed to substantially decrease simulation runtime while retaining nonlinear interactions between state variables and model parameters. Besides cut-HDMR, other versions of the HDMR approach have been applied to environmental modeling problems, e.g., random sampling HDMR (Li et al., 2006; Wang et al., 2003). The method has also been integrated with neural network approaches for high dimensionality problems (e.g., Manzhos and Carrington, 2008). The HDMR method has been used, for example, to study global atmospheric chemistry (Wang et al., 1999), stratospheric chemistry (Shorter et al., 1999), and atmospheric radiation transport (Shorter et al., 2000).

The HDMR approach maps a set of n input variables $\mathbf{x} = (x_1, x_2, ..., x_n)$ onto the desired output $g(\mathbf{x})$. In the case of estimating δF_s , the full set of input variables x_i are soil moisture, temperature, CO₂ production, and $\delta_{\rm sw}$ (all of which are depth dependent), and the δ^{18} O value of atmospheric CO₂ (Table 1). $g(\mathbf{x})$ represents δF_s at a particular

x and is expressed as an expansion of correlated functions $(f_0, f_i(x_i), f_{ij}(x_i, x_j), \text{ etc.})$:

$$g(\mathbf{x}) = f_0 + \sum_{i=1}^n f_i(x_i) + \sum_{1 \le i < j \le n}^n f_{ij}(x_i, x_j) + \dots + f_{12,\dots,n}(x_1, x_2, \dots, x_n).$$
 (2)

Here, f_0 is a constant that represents the system response at \boldsymbol{a} (i.e., $g(\boldsymbol{a})$), where \boldsymbol{a} is the reference point (the central point of the n-dimensional hypercube defined by \boldsymbol{x}); $f_i(x_i)$ characterizes the impact on $g(\boldsymbol{x})$ of a change in x_i , while other inputs are taken from the reference point \boldsymbol{a} ; $f_{ij}(x_i, x_j)$ characterizes the impact on $g(\boldsymbol{x})$ of simultaneous changes in x_i and x_j ; and $f_{12...n}(x_1, x_2, ..., x_n)$ gives the residual impact on $g(\boldsymbol{x})$ of all the variables simultaneously. The cut-HDMR approach ignores functions with greater than two variable interactions under the hypothesis that first and second order interactions dominate δF_s . The three expansion functions are calculated as

$$f_0 = g\left(\boldsymbol{a}\right),\tag{3}$$

$$f_i(x_i) = g(x_i, \mathbf{a}) - g(\mathbf{a}), \tag{4}$$

and

$$f_{ij}(x_i, x_j) = g(x_i, x_j, \mathbf{a}) - f_i(x_i) - f_j(x_j) - f_0.$$
 (5)

The nomenclature for g indicates that it is evaluated assuming all variables are at the reference point a except the specific value(s) of x contained in the parentheses. Subtracting off the lower-order expansion functions when calculating $f_{ij}(x_i, x_j)$ ensures a unique addition from $g(x_i, x_j, a)$.

2.3 Applying HDMR to calculate δF_s

For this work the HDMR expansion functions were generated using ISOLSM to evaluate δF_s at steady state for a suite of input variables. In general, the soil-gas system will not be in steady state, but as demonstrated below, excursions from the steady-state solution do not appreciably impact the predicted cumulative isoflux in this system. The impact and applicability of the steady-state assumption in different ecosystems and under different meteorological forcing will be evaluated in future work. Note that the HDMR method has also been used to propagate transient solutions of complex models (e.g., Shorter et al., 2000).

The input variables that comprise x are assigned from a range divided into N equal intervals (Table 1). While all ISOLSM simulations here used the spatial discretizations described in Riley et al. (2002), the HDMR expansion functions are evaluated with two vertical discretization scenarios (D₁ and D₂). Scenario D₁ uses 2.5 cm soil control volumes down to 20 cm depth and N = 100, and scenario D₂ uses average soil moisture, temperature, and $\delta_{\rm sw}$ in 5 cm increments down to 20 cm depth and N = 100.

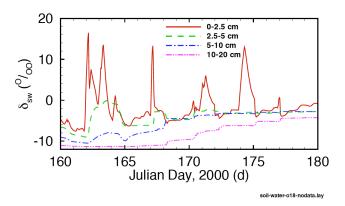


Fig. 1. Simulated δ_{sw} in four soil layers over a twenty-day period in June 2000. Spikes in δ_{sw} in the top 2.5 cm result from soil evaporation, precipitation, and wicking from lower soil layers.

To develop the HDMR expansion functions, ISOLSM is run to steady state for each set of conditions (i.e., each x). δF_s is then evaluated, and the expansion functions are calculated with Eqs. (3)–(5) and stored as look-up tables. Computing the expansion functions for each discretization took about seven days on a 2 GHz Atherton PC with 512 MB of RAM. During the HDMR simulation, first and second order interpolation routines are used to calculate the expansion functions for a specific input set x. The advantage to the HDMR approach is the ability to rapidly evaluate Eq. (2) once the expansion functions have been computed.

In ISOLSM the soil CO₂ source term is calculated as the sum of autotrophic and heterotrophic respiration, each with their own exponentially decaying depth profile defined by the parameters z_0^a and z_0^h (m), respectively. z_0^a and z_0^h are sensitive to soil moisture, becoming larger as the soil dries (i.e., the relative distribution of soil CO₂ production moves deeper as the soil dries). To save computational time, the HDMR expansion functions were generated with a single exponential parameter, z_0 . Therefore, in the simulations presented here, the HDMR model applies a parameter weighted by the predicted autotrophic, F_a (µmol m⁻² s⁻¹), and heterotrophic, F_h (µmol m⁻² s⁻¹), CO₂ sources to approximate the depth distribution of CO₂ production:

$$z_0 = \frac{z_0^{\rm a} F_{\rm a} + z_0^{\rm h} F_{\rm v} h}{F_{\rm a} + F_{\rm h}}.$$
 (6)

2.4 HDMR testing

The HDMR approach was tested using meteorological data from May–July 2000 in a C₄-dominated tallgrass prairie pasture in Oklahoma (36°56′ N, 96°41′ W). This dataset was used previously to develop and test ISOLSM (Riley et al., 2002, 2003). The site is in a region with various land uses, including crops, sparse trees, and other grasslands, has not been grazed since 1996, and is burned every spring. Maximum leaf area index is about 3, and maximum net ecosystem exchange during the growing season is about 35 μ mol m⁻² s⁻¹. The site

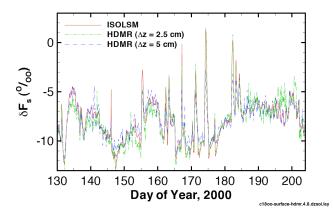


Fig. 2. Simulated $\delta F_{\rm S}$ over the growing season from ISOLSM and the HDMR approach using discretization scenarios D₁ and D₂. Variability in $\delta F_{\rm S}$ is large when $\delta_{\rm SW}$ variability in the top 2.5 or 5 cm is large.

and collection of meteorological forcing and flux data are described in detail in Suyker and Verma (2001) and Colello et al. (1998).

3 Results and discussion

The magnitude and vertical distribution of δ_{sw} is an important determinant of δF_s (Riley, 2005). In this system, low humidity, high air temperatures, and high soil evaporation rates generate strong δ_{sw} gradients in the top 5 cm of soil, making accurate prediction of δ_{sw} critical for predicting δF_s . For example, Fig. 1 shows predicted δ_{sw} for four soil layers over a twenty-day period in June 2000.

The spikes in δ_{sw} in the first soil layer occur for a number of reasons. Rapid increases in δ_{sw} are typically driven by large soil evaporative fluxes, which occur when the vapor gradient between the soil surface and canopy air is large. The δ^{18} O value of above-canopy vapor (δ_v) is impacted by surface evaporative fluxes, resulting in a feedback between δ_v and near-surface δ_{sw} . Because we lack continuous measurements of δ_v , we estimated it using a constant offset (7 ‰) from the estimated stem water δ^{18} O value. In reality, δ_v can change more rapidly than this approach allows, as shown in Helliker et al. (2002). Rapid decreases in δ_{sw} are caused by precipitation inputs; wicking of more depleted soil water from lower soil layers drives more gradual decreases.

The HDMR approach using both vertical discretizations (D_1 and D_2) accurately simulated δF_s over the growing season (Fig. 2). Figure 3 again compares the HDMR and ISOLSM predictions, but over a twenty-day period so that details in δF_s can be more easily seen. Also shown in Fig. 3 is the gradient in δ_{sw} over the top 5 cm of soil ($\nabla_{0-5\,cm}\delta_{sw}$ (‰ cm⁻¹)).

Differences between ISOLSM and HDMR predictions occur for several reasons. First, discretization scenario D_2 is unable to capture the impact on δF_s resulting from large

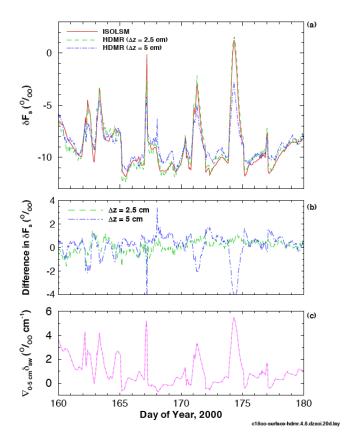


Fig. 3. (a) Same as in Fig. 2, but for a 20-day period. Also shown are (b) differences between the full ISOLSM model results and the HDMR predictions for $\Delta z = 2.5$ and 5 cm and (c) $\nabla_{0-5\text{cm}}\delta_{\text{SW}}$, the predicted gradient in δ_{SW} over the top 5 cm of soil. Differences between scenarios D_1 and D_2 are largest when near-surface δ_{SW} gradients are large. Discretization scenario D_1 more accurately predicts the impact of these gradients on δF_{S} since this HDMR solution is based on the identical spatial discretization as that of the ISOLSM simulation (i.e., 2.5 cm in the top 20 cm of soil).

 $\delta_{\rm sw}$ gradients between 0 and 5 cm depth. We have previously shown that these gradients can substantially impact δF_s (Riley, 2005). Following precipitation (e.g., days 162, 163, 164, 167, 172, and 174; Fig. 3), the enhanced soil-surface evaporation leads to $\nabla_{0-5\,\mathrm{cm}}\delta_{\mathrm{sw}}$ of up to 5 \% cm⁻¹. We have observed gradients of this magnitude in a sorghum field in Oklahoma (unpublished data), as have Miller et al. (1999) in their soil column experiments. The impact of these gradients on δF_s is better captured in scenario D_1 since this HDMR solution is based on the identical spatial discretization as that of the ISOLSM simulation (i.e., eight 2.5 cm control volumes in the top 20 cm of soil). Second, even in the absence of vertical spatial gradients in δ_{sw} , rapid changes in δ_{sw} will lead to errors in the HDMR predictions since the HDMR solution is based on the steady-state full model solution. However, the errors between the D₁ discretization scenario predictions and the ISOLSM solution are small during these periods of rapid change. These results imply that errors associated with

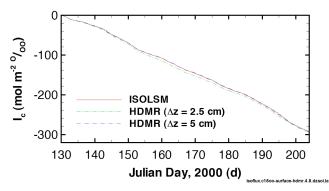


Fig. 4. Cumulative soil-surface isoflux calculated with ISOLSM and the HDMR approach using discretization scenarios D_1 and D_2 . The error in cumulative isoflux over the season for each HDMR scenario is about 0.2 % (0.5 mol m⁻² ‰).

the steady-state assumption are relatively small for the conditions simulated here. Third, using an approximation for z_0 (Eq. 2.4) will lead to errors in the depth distribution of CO₂ production, although the total production will be correct. Finally, the HDMR solution is linearly interpolated between the forcing values shown in Table 1; this interpolation will lead to some error. I have attempted to minimize this type of error by using relatively small increments between successive values at which the expansion functions were evaluated (i.e., N = 100).

The net impact of soil-surface CO_2 fluxes on the $\delta^{18}O$ value of atmospheric CO_2 is described by the instantaneous isoflux, I (µmol m⁻² s⁻¹ ‰), calculated as

$$I = (\delta F_{\rm s} - \delta_{\rm a}) F_{\rm s}. \tag{7}$$

The cumulative isoflux, $I_{\rm c}$ (mol m $^{-2}$ %0), is calculated as the time integral of I over the three-month period. $I_{\rm c}$ is accurately simulated by the HDMR approach for both discretization scenarios (Fig. 4). Differences in the HDMR model predictions from the full model solution during periods of large near-surface $\delta_{\rm sw}$ gradients did not substantially impact predictions of the cumulative isoflux over the three-month period. The error in cumulative isoflux after three months is about 0.2 % (0.5 mol m $^{-2}$ %0) for both discretization scenarios. The HDMR solution was computed \sim 50 and 100 times faster than the full ISOLSM numerical solution for discretization scenarios D₁ and D₂, respectively. This increased computational efficiency makes it practical to include the ISOLSM-based HDMR solution for $\delta F_{\rm s}$ in regional- and global-scale models.

In the broader context, spatial heterogeneity in hydrology and biogeochemical cycling occurs on scales substantially finer than can currently, and likely ever, be represented in ESMs. The actual transformation of soil organic matter and CO₂ production, for example, occurs at the 10s of nm scale, and is impacted by pore-scale heterogeneity in nutrients, water, organic molecules, mineral surfaces, microbes, and

others (Kleber et al., 2011). The microbial community acting at these scales is incredibly diverse (Goldfarb et al., 2011) as are the range of organic molecules being transformed and consumed (Kogel-Knabner, 2002; Sutton and Sposito, 2005). At the mm to cm scale, aggregation, macropores, plant roots, and other soil structural properties impact distributions of microbes and resources (Six et al., 2001). Vertical structure of hydrology and C inputs can vary on horizontal scales as small as a few meters and vertical scales on the order of 10 cm. Accounting for these types of heterogeneity across 10s of km in an ESM is a substantial challenge that high-dimensional model reduction techniques such as that presented here may help address.

4 Conclusions

Representing complex coupled hydrological and biogeochemical processes in an Earth system model may, depending on the level of mechanistic detail desired, require some level of model reduction to make the problem computationally feasible. We described here a high-dimensional model reduction approach to address one example of such a problem – estimating the δ^{18} O value of the soil-surface CO₂ flux. This flux is a complex function of the depth-dependent (a) δ^{18} O value of soil water, (b) soil moisture, (c) soil temperature, and (d) soil CO₂ production, as well as the δ^{18} O value of above-surface CO2. Mechanistic models that include these interactions (e.g., ISOLSM) may be too computationally expensive to integrate in regional and global models at their native spatial scale. The results presented here demonstrate that the HDMR technique accurately predicts δF_s up to 100 times faster than the full numerical solution.

Under rapidly changing soil moisture conditions, such as immediately after a precipitation event, the full numerical solution of the $C^{18}OO$ surface flux differs slightly from the HDMR solution. Errors in the HDMR solution arise from the steady-state assumption, approximation of the depth dependence of soil CO_2 production, and linear interpolation. However, these errors have a small impact on the predicted cumulative isoflux. The error in the cumulative isoflux over the growing season calculated with HDMR (compared to that calculated with the full model) was less than $0.2\,\%$.

Applying measurements of the δ^{18} O value of atmospheric CO_2 to partition measured net ecosystem fluxes into gross fluxes and, at the regional and global scale, to estimate spatially explicit CO_2 exchanges requires accurate prediction of the δ^{18} O value of the soil-surface CO_2 flux. Further, for regional and global simulations such a method must be computationally efficient. The HDMR method applied here shows great promise as a tool for addressing the need for mechanistic representation of processes across a wide range of scales and spatial heterogeneity.

Nomenclature

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