



*Supplement of*

**Modeling biochar effects on soil organic carbon on croplands in a microbial decomposition model (MIMICS-BC\_v1.0)**

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# Supporting information

**Table S1** Definitions, values and units of parameters in MIMICS.

Parameter	Description	Value	Unit
<b>Carbon pools</b>			
$LIT_m$	Metabolic litter pool	-	mg C cm <sup>-3</sup>
$LIT_s$	Structural litter pool	-	mg C cm <sup>-3</sup>
$MIC_r$	Microorganism with copiotrophic growth strategy	-	mg C cm <sup>-3</sup>
$MIC_k$	Microorganism with oligotrophic growth strategy	-	mg C cm <sup>-3</sup>
$SOC_p$	Physically-protected SOC pool	-	mg C cm <sup>-3</sup>
$SOC_c$	Chemical protected SOC pool	-	mg C cm <sup>-3</sup>
$SOC_a$	Available SOC pool	-	mg C cm <sup>-3</sup>
<b>Litter input parameters</b>			
$f_{met}$	Partitioning of litter inputs to $LIT_m$	0.85-0.013 (lignin/N)	-
$f_{i,met}$	Fraction of litter inputs transferred to $SOC_p$	0.05	-
$f_{i,STRU}$	Fraction of litter inputs transferred to $SOC_c$	0.05	-
<b>Microbial decomposition parameters</b>			
$V_{max}$	Microbial maximum reaction velocity	-	mg C (mg MIC) <sup>-1</sup> h <sup>-1</sup>
$K_m$	Half-saturation constant	-	mg C cm <sup>-3</sup>
$V_{slope}$	Regression coefficient (Eq. 2)	0.063 <sup>a</sup>	ln (mg C (mg MIC) <sup>-1</sup> h <sup>-1</sup> ) °C <sup>-1</sup>
$V_{int}$	Regression intercept (Eq. 2)	5.47 <sup>a</sup>	ln (mg C (mg MIC) <sup>-1</sup> h <sup>-1</sup> )
$av$	Tuning coefficient (Eq. 2)	8×10 <sup>-6</sup> <sup>a</sup>	-
$V_{mod-r}$	Modifies $V_{max}$ for fluxes into $MIC_r$	10, 2, 10 <sup>b</sup>	-
$V_{mod-k}$	Modifies $V_{max}$ for fluxes into $MIC_k$	3,3,2 <sup>c</sup>	-
$K_{slope}$	Regression coefficient (Eq. 3)	0.017, 0.027, 0.017 <sup>b,c</sup>	ln (mg C cm <sup>-3</sup> ) °C <sup>-1</sup>
$K_{int}$	Regression intercept (Eq. 3)	3.19 <sup>a</sup>	ln (mg C cm <sup>-3</sup> )
$ak$	Tuning coefficient (Eq. 3)	10 <sup>a</sup>	-
$K_{mod-r}$	Modifies $K_m$ for fluxes into $MIC_r$	0.125,0.5,0.25× $P_{scalar}$ <sup>b</sup>	-
$K_{mod-k}$	Modifies $K_m$ for fluxes into $MIC_k$	0.5,0.25,0.167× $P_{scalar}$ <sup>c</sup>	-
$P_{scalar}$	Physical protection scalar used in $K_{mod}$	(2.0 × (2.0 × e <sup>-2√fclay</sup> )) <sup>-1</sup>	-
$MGE$	Microbial growth efficiency	0.5,0.25,0.7,0.35 <sup>d</sup>	mg mg <sup>-1</sup>
$k_{mic}$	Microbial biomass turnover rate	5.2 × 10 <sup>-4</sup> × e <sup>0.3(fmet)</sup> × $\tau_{mod}$ <sup>e</sup> 2.4 × 10 <sup>-4</sup> × e <sup>0.1(fmet)</sup> × $\tau_{mod}$ <sup>e</sup>	h <sup>-1</sup>
$\tau_{mod}$	Modifies microbial turnover rate	0.8 < √NPP/100 < 1.2	-
$a_\tau$	Tuning coefficient of $K_{mic}$	1.0	-
$f_{rp}$	Fraction of $K_{mic}$ of $MIC_r$ partitioned to $SOC_p$	min (1.0, 0.13 × e <sup>1.3(fclay)</sup> ) <sup>f</sup>	-
$f_{kp}$	Fraction of $K_{mic}$ of $MIC_k$ partitioned to $SOC_p$	min (1.0, 0.02 × e <sup>0.8(fclay)</sup> ) <sup>f</sup>	-
$f_{rc}$	Fraction of $K_{mic}$ of $MIC_r$ partitioned to $SOC_c$	min (1.0 - $f_{rp}$ , 1.06 × e <sup>-2.6(fmet)</sup> ) <sup>f</sup>	-
$f_{kc}$	Fraction of $K_{mic}$ of $MIC_k$ partitioned to $SOC_c$	min (1.0 - $f_{kp}$ , 8.93 × e <sup>-2.6(fmet)</sup> ) <sup>f</sup>	-
$f_{ra}$	Fraction of $K_{mic}$ of $MIC_r$ partitioned to $SOC_a$	1.0 - $f_{rp}$ - $f_{rc}$	-
$f_{ka}$	Fraction of $K_{mic}$ of $MIC_k$ partitioned to $SOC_a$	1.0 - $f_{kp}$ - $f_{kc}$	-
$\beta$	Density-dependence exponent	Eq. 6	-
<b>Protected carbon parameters</b>			
$D$	Desorption rate from $SOC_p$ to $SOC_a$	Eq. 5	h <sup>-1</sup>
$KO$	Further modifies $K_m$ for oxidation of $SOC_c$	4, 4 <sup>e</sup>	-

Parameter	Description	Value	Unit
$k_d$	Tuning coefficient of the desorption rate	Eq. 5	-
$K_{ads}$	The sorption rate of SOC <sub>p</sub>	Eq. 8	h <sup>-1</sup>
$k_{ba}$	The binding affinity (Eq. 8)	1~16 <sup>g</sup>	(mg C·mg <sup>-3</sup> ) <sup>-1</sup>
$Q_{max}$	The maximum sorption capacity of SOC <sub>p</sub>	Eq. 9	mg C cm <sup>-3</sup>
<b>Biochar-related parameters</b>			
$f_{bp}$	Fraction of biochar carbon partitioned into SOC <sub>p</sub>	0.6	-
$f_{ba}$	Fraction of biochar carbon partitioned into SOC <sub>a</sub>	0.03-0.3 <sup>h</sup>	-
$f_{bc}$	Fraction of biochar carbon partitioned into SOC <sub>c</sub>	1.0 - $f_{bp}$ - $f_{ba}$	-
$f_{loss}$	Biochar fraction loss during addition	0.02 <sup>h</sup>	-
$f_d$	Coefficients for adjusting the desorption rate of SOC <sub>p</sub> with biochar addition (Eq. 15)	-0.15 ~0.15 <sup>h</sup>	ha t <sup>-1</sup> C
$f_v$	Coefficients for adjusting the microbial decomposition velocity with biochar addition (Eq. 16)	-0.15 ~0.15 <sup>h</sup>	ha t <sup>-1</sup> C

<sup>a</sup> From observations in German et al. (2012), as used in Wieder et al. (2014, 2015).

<sup>b</sup> For LIT<sub>m</sub>, LIT<sub>s</sub>, and SOC<sub>a</sub>, fluxes entering MIC<sub>r</sub>, respectively.

5 <sup>c</sup> For LIT<sub>m</sub>, LIT<sub>s</sub>, and SOC<sub>a</sub>, fluxes entering MIC<sub>k</sub>, respectively.

<sup>d</sup> 0.5 is the MGE of C fluxes from LIT<sub>m</sub> and SOC<sub>a</sub> to MIC<sub>r</sub>, 0.25 is for C flux from LIT<sub>s</sub> to MIC<sub>r</sub>, 0.7 is for fluxes from LIT<sub>s</sub> and SOC<sub>a</sub> to MIC<sub>k</sub>, 0.35 is for C flux from LIT<sub>m</sub> to MIC<sub>k</sub>.

<sup>e</sup> For MIC<sub>r</sub> and MIC<sub>k</sub>, respectively.

<sup>f</sup> Values from Zhang et al. (2020).

10 <sup>g</sup> Values from Wang et al. (2020).

<sup>h</sup> Ranges from Archontoulis et al. (2016).

**Table S2** Definitions and values of modified parameters used in default MIMICS.

Parameters <sup>d</sup>	Description	Original values <sup>a</sup>	Modified values
cn_leaf	The ratio of carbon to nitrogen in leaf	30	25 <sup>b</sup>
cn_root	The ratio of carbon to nitrogen in root	75	45 <sup>b</sup>
cn_stem	The ratio of carbon to nitrogen in stem	200	50 <sup>b</sup>
lig_c_leaf	The ratio of lignin to carbon in leaf	0.1	0.12 <sup>b</sup>
lig_c_root	The ratio of lignin to carbon in root	0.1	0.40 <sup>b</sup>
lig_c_stem	The ratio of lignin to carbon in stem	0.15	0.15 <sup>b</sup>
HI	Harvest index	-	0.45 <sup>c</sup>

15 <sup>a</sup> Values based on Zhang et al. (2020).

<sup>b</sup> Estimated values from Abiven et al. (2005).

<sup>c</sup> Value from Hicke and Lobell (2004).

<sup>d</sup> These parameters were assumed unchanged with biochar addition.

20 **Table S3** Prior parameter values, optimized values and ranges in the parameter optimization for various MIMICS versions.

Datasets	Model	Parameter	Prior value	Optimized value	Range <sup>c</sup>	Units
MIMICS	MIMICS-def	$a_v$	10	13.95	[0,30]	-
		$a_k$	5	16.36	[0,20]	-
		$k_d$	0.5	1.73	[0,3]	-
	MIMICS-T	$a_v$	10	8.34	[0,30]	-
		$a_k$	5	12.52	[0,20]	-
		$k_d$	0.5	2.57	[0,3]	-
		$\beta$	1	1.15	[0,2]	-
	MIMICS-TS	$a_v$	10	9.13	[0,30]	-
		$a_k$	5	17.72	[0,20]	-
		$k_d$	0.5	2.15	[0,3]	-
		$\beta$	1	1.35	[0,2]	-
		$k_{ba}$	6	8.60	[1,16]	-
		$c_1$	0.3	0.27	[0,0.8]	-
		$c_2$	3.0	2.16	[0,5]	-
	MIMICS-TSM <sub>a</sub>	$a_v$	10	8.50	[0,30]	-
		$a_k$	5	15.22	[0,20]	-
		$k_d$	0.5	2.03	[0,3]	-
		$\beta$	1	1.33	[0,2]	-
		$k_{ba}$	6	8.38	[1,16]	-
		$c_1$	0.3	0.42	[0,0.8]	-
		$c_2$	3	2.61	[0,5]	-
	MIMICS-TSM <sub>b</sub>	$a_v$	10	9.94	[0,30]	-
		$a_k$	5	19.42	[0,20]	-
		$k_d$	0.5	1.97	[0,3]	-
		$\beta$	1	1.36	[0,2]	-
		$k_{ba}$	6	6.51	[1,16]	-
		$c_1$	0.3	0.39	[0,0.8]	-
		$c_2$	3	1.55	[0,5]	-
MIMICS-TSM <sub>c</sub>	$a_v$	10	10.37	[0,30]	-	
	$a_k$	5	17.12	[0,20]	-	
	$k_d$	0.5	1.63	[0,3]	-	
	$\beta$	1	1.21	[0,2]	-	
	$k_{ba}$	6	9.61	[1,16]	-	
	$c_1$	0.3	0.28	[0,0.8]	-	
	$c_2$	3	2.24	[0,5]	-	
MIMICS <sub>T</sub> -BC	MIMICS <sub>T</sub> -BC <sub>def</sub>	none	none	none	none	none
	MIMICS <sub>T</sub> -BC <sub>D</sub>	$f_d$	-0.002	-0.0084 <sup>a</sup> (-0.0131 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
	MIMICS <sub>T</sub> -BC <sub>DV</sub>	$f_d$	-0.002	0.0168 <sup>a</sup> (-0.0125 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
		$f_v$	0.05	-0.0086 <sup>a</sup> (-0.0149 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
	MIMICS <sub>T</sub> -BC <sub>DV-SOCa</sub>	$f_d$	-0.002	-0.0096 <sup>a</sup> (-0.0030 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C

		$f_v$	0.05	0.0082 <sup>a</sup> (-0.0257 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
MIMICS <sub>TSMb-BC</sub>	MIMICS <sub>TSMb-BC<sub>def</sub></sub>	none	none	none	none	none
	MIMICS <sub>TSMb-BC<sub>D</sub></sub>	$f_d$	-0.002	-0.0121 <sup>a</sup> (-0.0122 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
	MIMICS <sub>TSMb-BC<sub>DV</sub></sub>	$f_d$	-0.002	0.0020 <sup>a</sup> (0.0934 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
		$f_v$	0.05	-0.0092 <sup>a</sup> (-0.0253 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
	MIMICS <sub>TSMb-BC<sub>DV-SOCa</sub></sub>	$f_d$	-0.002	0.0020 <sup>a</sup> (0.0107 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C
		$f_v$	0.05	-0.0098 <sup>a</sup> (-0.0260 <sup>b</sup> )	[-0.15,0.15]	ha t <sup>-1</sup> C

<sup>a</sup> The optimized parameter values using the short-term SOC data.

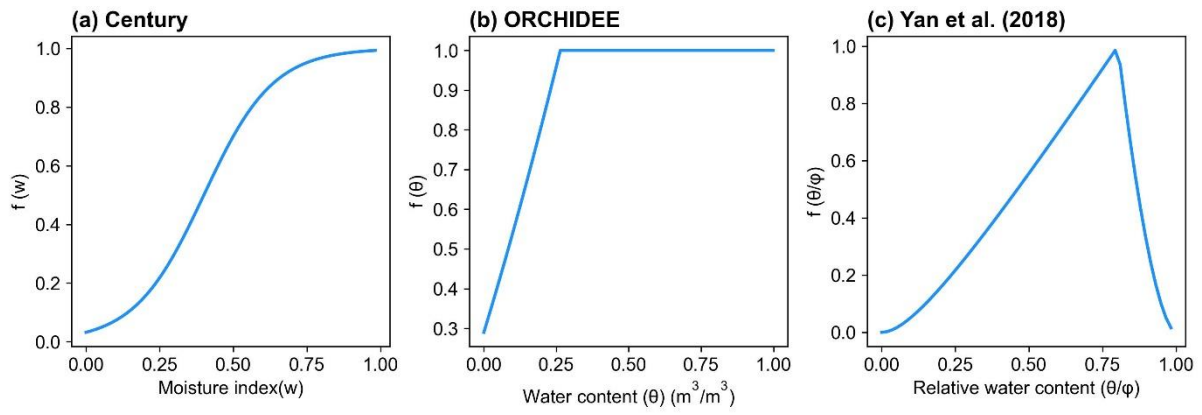
<sup>b</sup> The optimized parameter values using the long-term (extended to 8 yr) SOC data.

<sup>c</sup> The prescribed parameter ranges of  $a_v$ ,  $a_k$ ,  $k_d$ ,  $\beta$  are from Zhang et al. (2020).  $k_{ba}$  is from Wang et al. (2020).  $c_1$  and  $c_2$  are estimated from Mayes et al. (2012).  $f_d$  and  $f_v$  are from Archontoulis et al. (2016).

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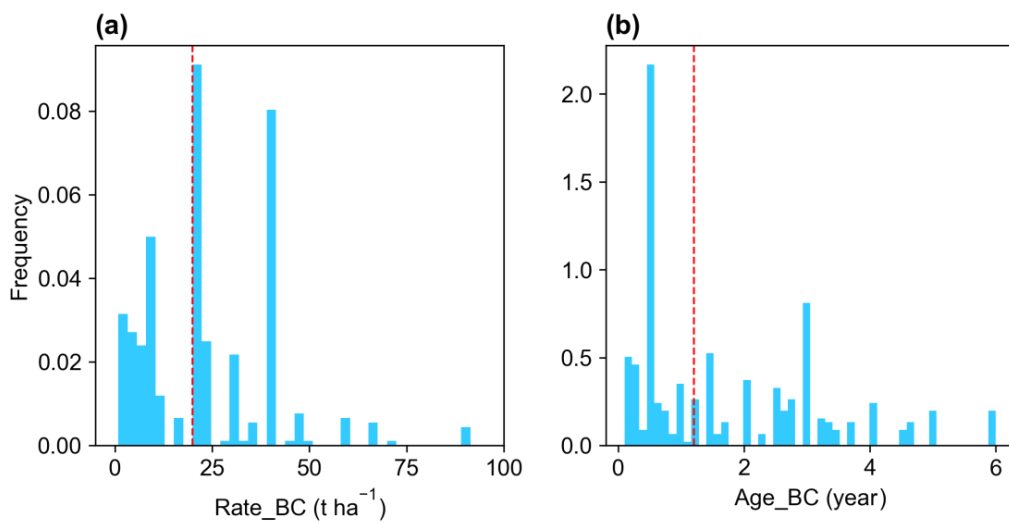
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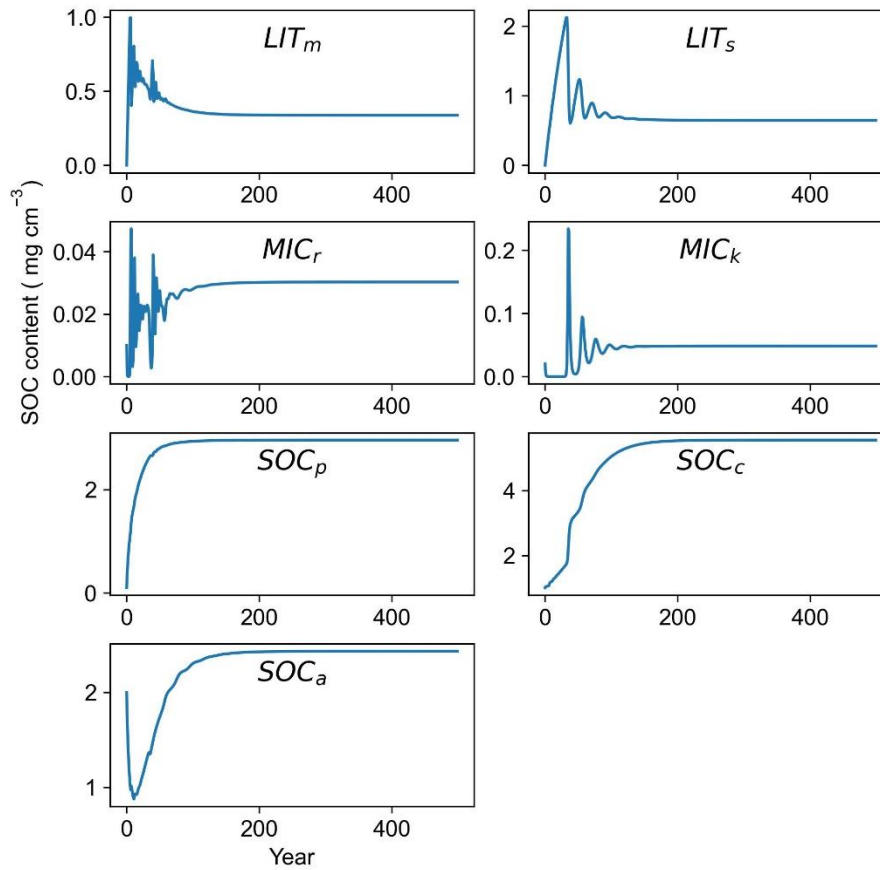
**Fig. S1** Soil moisture functions from (a) the Century model (Parton et al., 2000), (b) the ORCHIDEE-SOM model (Camino-Serrano et al., 2018) and (c) the mechanism-based soil moisture function from Yan et al. (2018).  $w$  is soil moisture indicator (AI, i.e., precipitation/potential evapotranspiration).  $\theta$  is soil water content,  $\phi$  is soil porosity, and  $\theta/\phi$  is relative water content.

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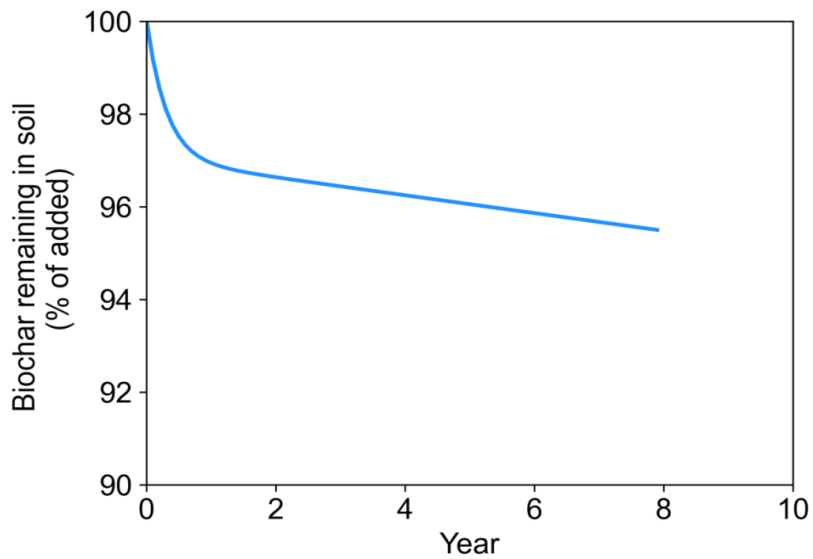
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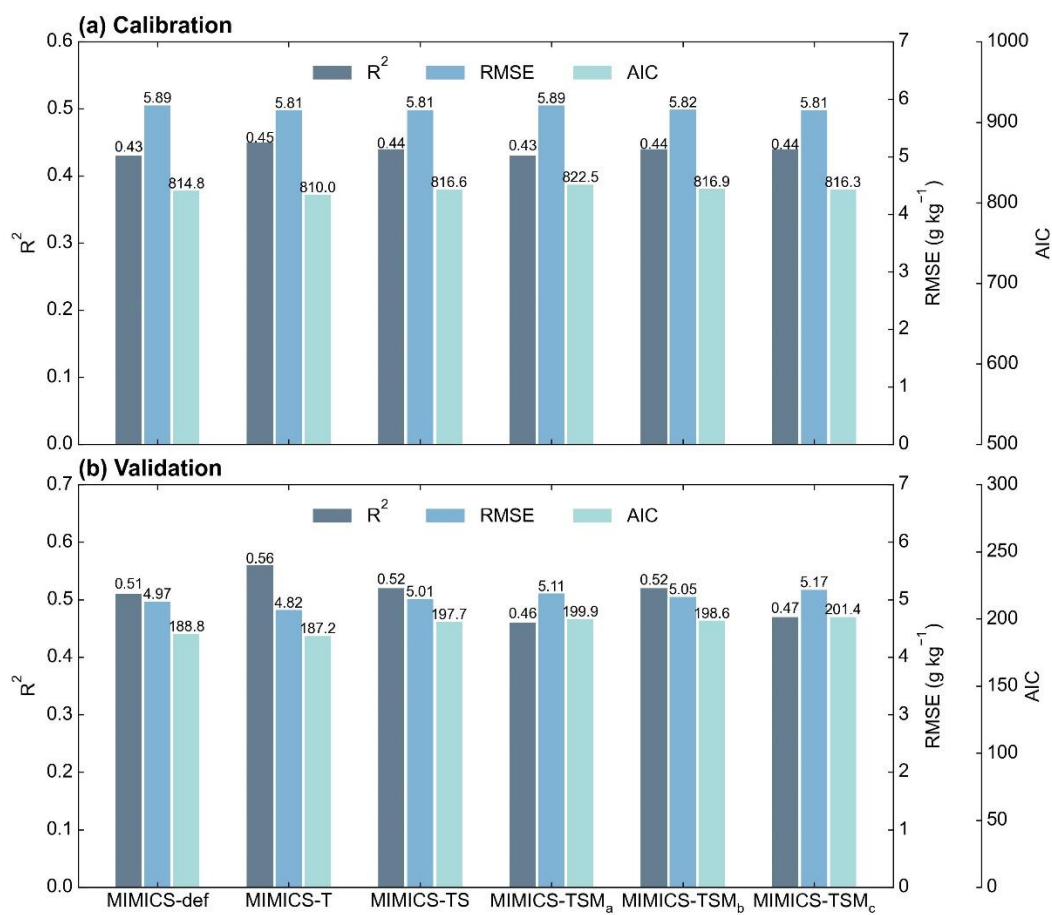
**Fig. S2** The frequency distribution of (a) biochar application rates (Rate\_BC) and (b) biochar addition periods (Age\_BC). Red dotted lines indicate the median values.



60 **Fig. S3** Temporal changes of seven SOC pools from a simulation of the MIMICS-TSM<sub>b</sub> version for 500 years using one random site (Lat, Lon =28.1°N, 113.2°E) as an example.



65 **Fig. S4** The biochar decomposition curve fitted with experimental data from Wang et al. (2016) using a double first-order exponential decay model ( $BC_{remain\%} = 3.02 \times e^{(-3.24 \times age_{bc})} + 97.02 \times e^{(-0.002 \times age_{bc})}$ ).

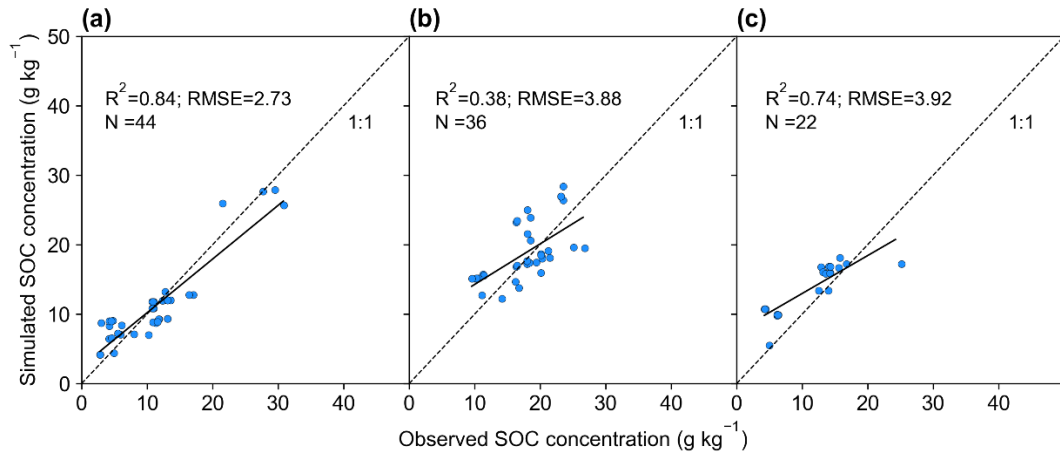


**Fig. S5** Comparison of  $R^2$ , RMSE and AIC of all MIMICS versions in model calibration (a) and validation (b).

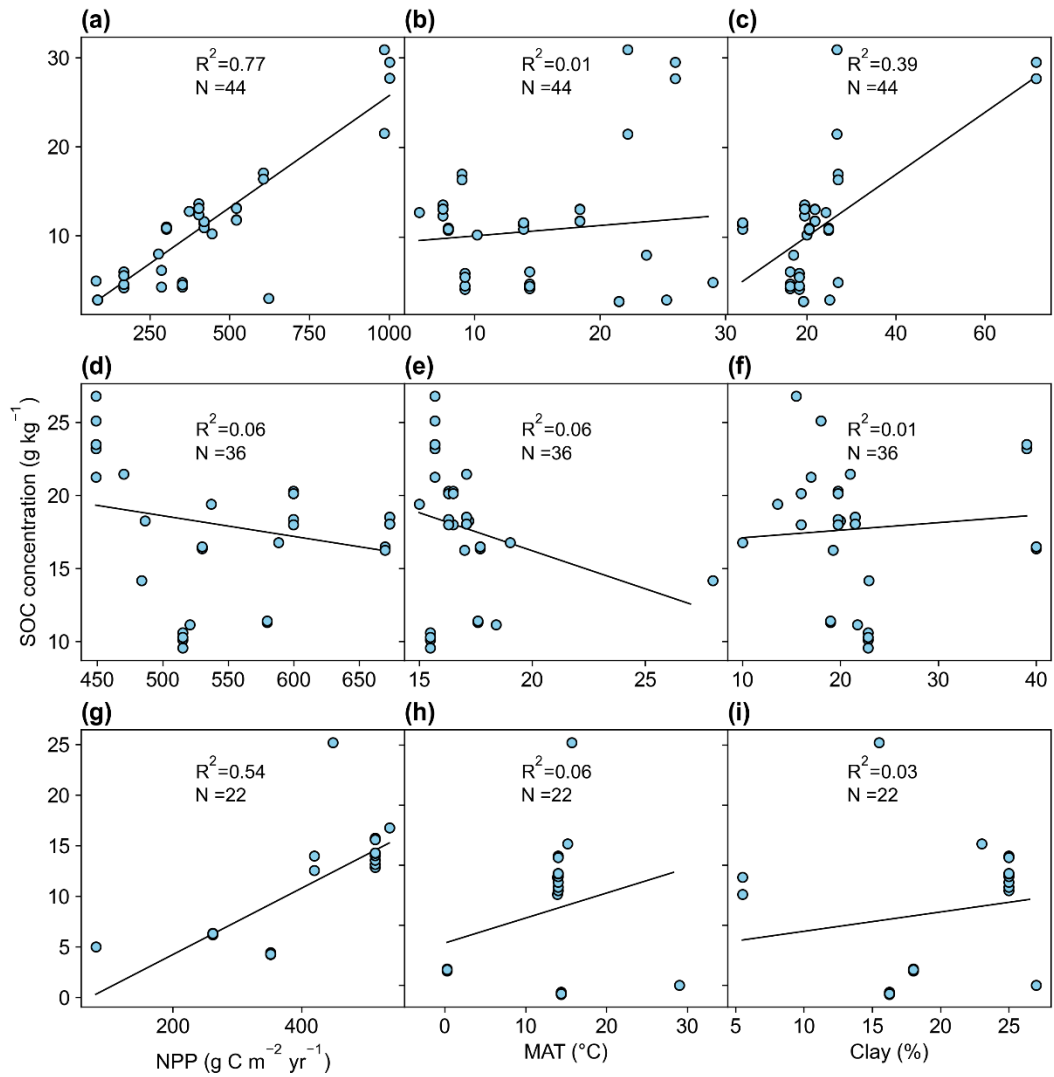
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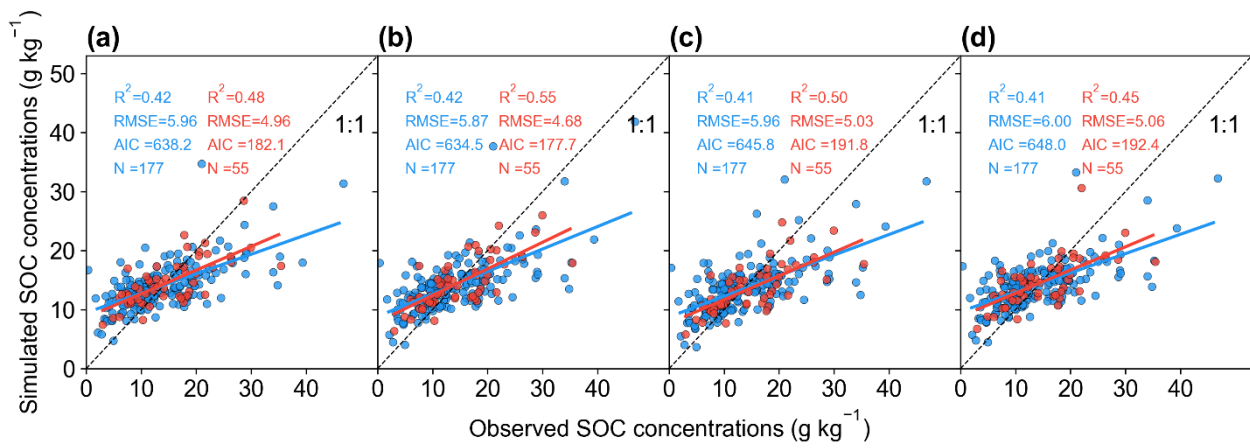




80 **Fig. S6** Relationship between observed and simulated SOC concentrations by MIMICS-TSM<sub>b</sub> for (a) maize, (b) rice and (c) wheat. The unit of RMSE is g kg<sup>-1</sup>.



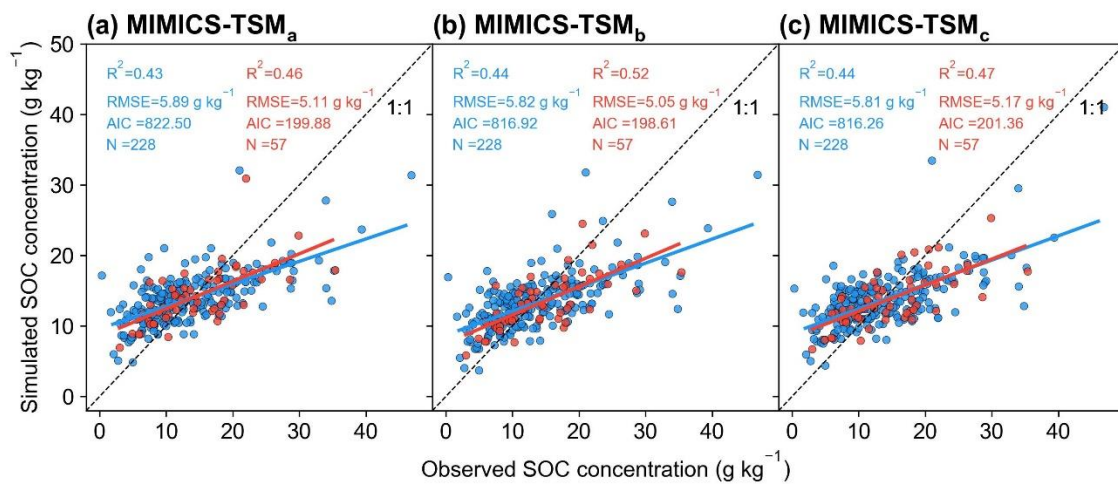
85 **Fig. S7** Correlation between SOC concentrations with NPP, MAT and Clay for maize (a-c), rice (d-f) and wheat (g-i).



**Fig. S8** Relationships between observed and simulated SOC concentrations aggregated within each  $0.5^\circ$  grid cell by MIMICS-def (a), MIMICS-T (b), MIMICS-TS (c) and MIMICS-TSM<sub>b</sub> (d). The unit of RMSE is  $\text{g kg}^{-1}$ . Blue and red dots represent observation sites for model calibration (80% sites) and validation (20% sites), respectively.

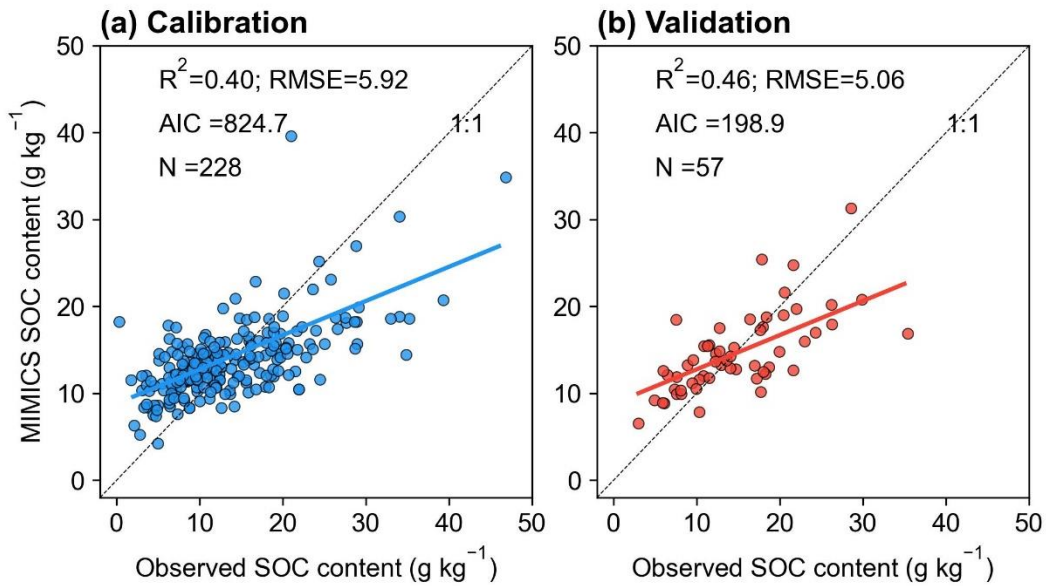
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**Fig. S9** Comparison between the observed and simulated SOC concentrations by (a) MIMICS-TSM<sub>a</sub>, (b) MIMICS-TSM<sub>b</sub> and (c) MIMICS-TSM<sub>c</sub>. Blue and red dots represent observation sites for model calibration (80% sites) and validation (20% sites), respectively.

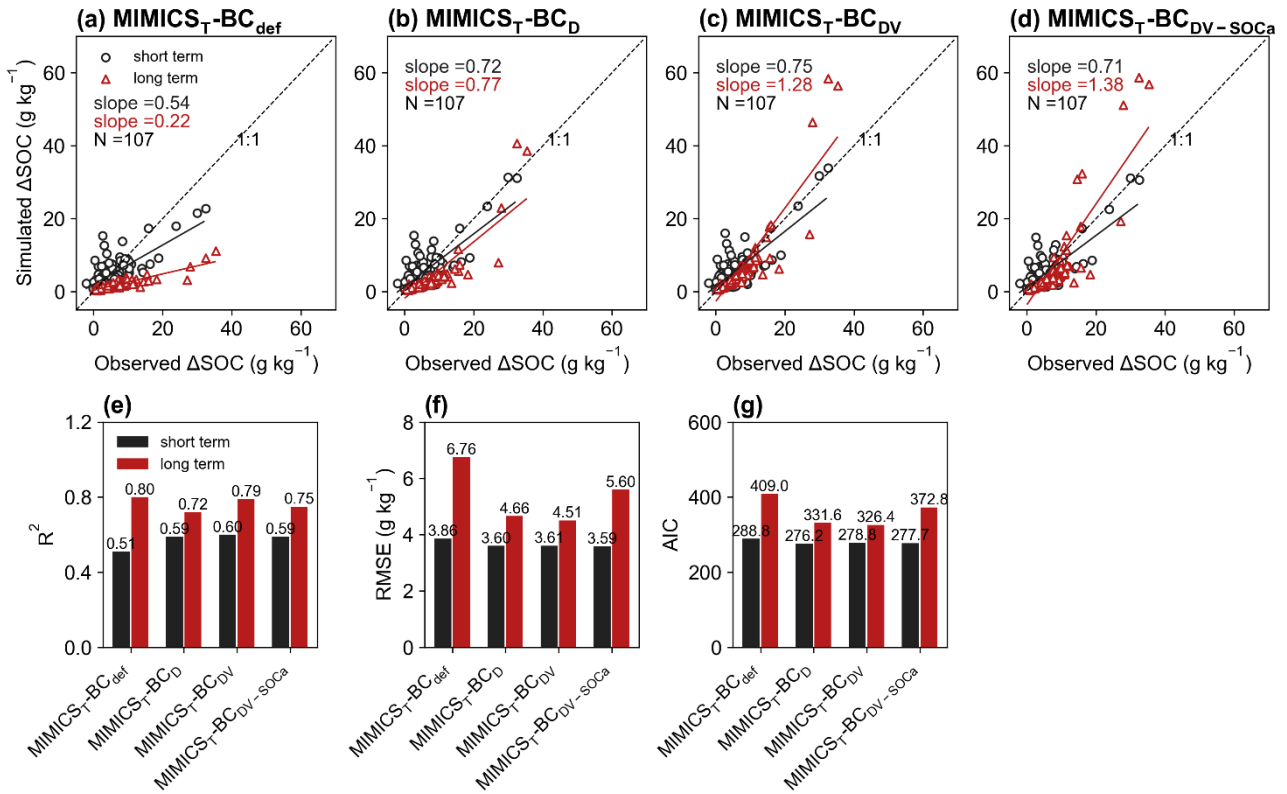
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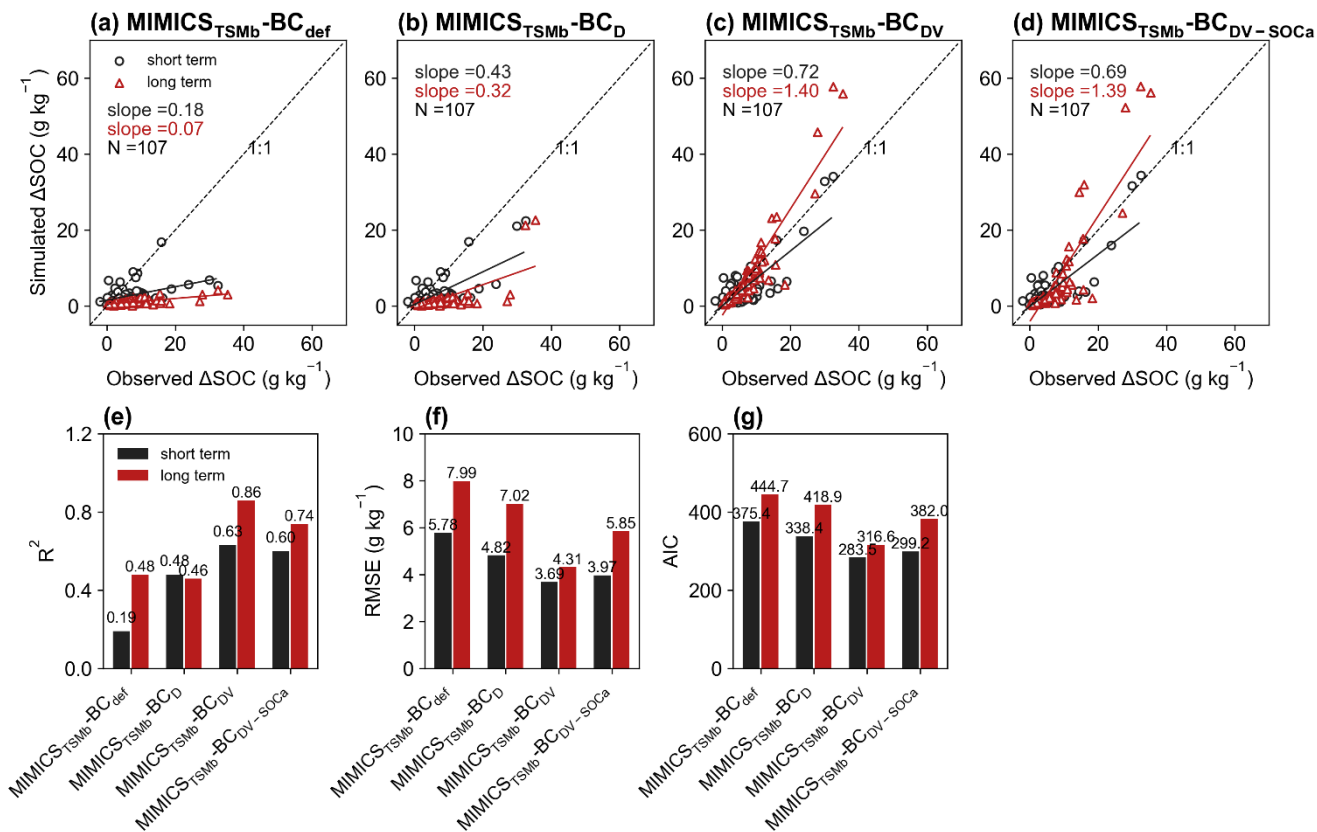
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**Fig. S10** Relationships between observed and simulated SOC concentrations by MIMICS-TSM<sub>b</sub> for (a) calibration and (b) validation assuming that the soil moist factor ( $f_{m2}(\theta)$ , Eq. 11) were multiplied by  $V_{max}$  and microbial turnover ( $\tau$ ) of MIC<sub>r</sub> and MIC<sub>k</sub>, instead of by  $V_{max}$  and  $K_m$  in **Section 2.1.4**.

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**Fig. S11** As Fig. 6 but for model calibration instead of validation.

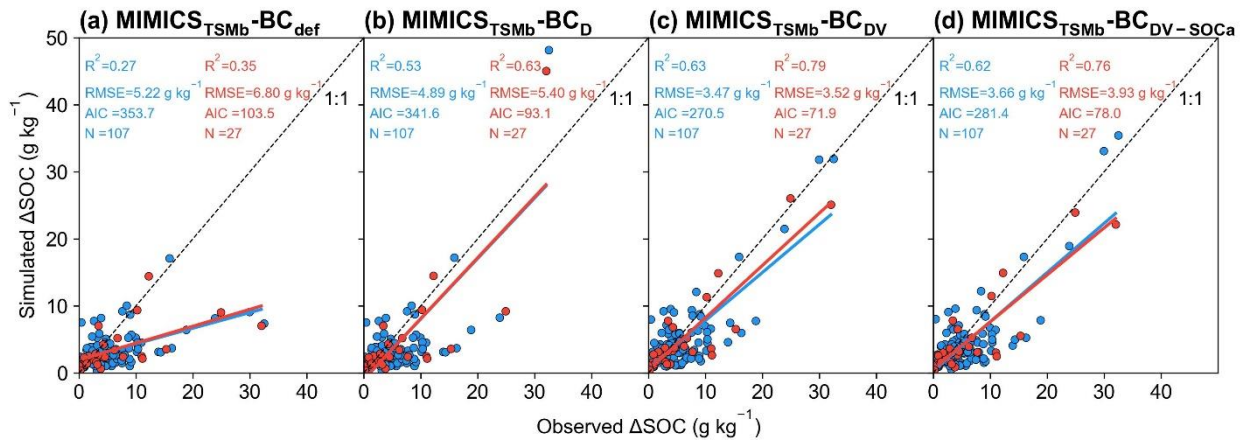


115 **Fig. S12** As Fig. 7 but for model calibration instead of validation.

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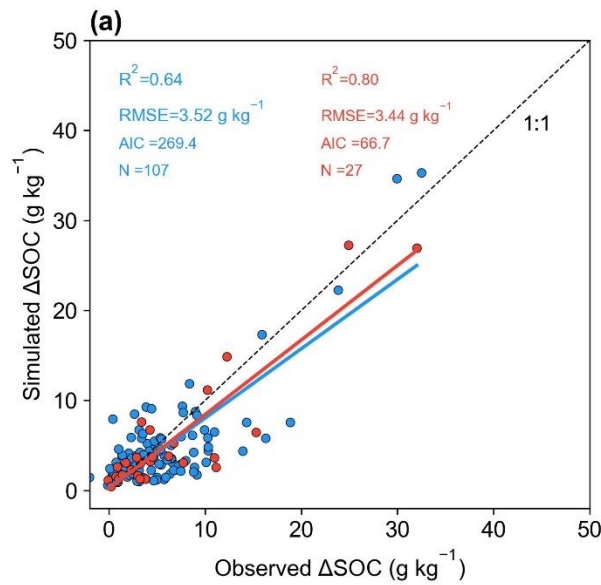
**Fig. S13** As Fig. 8 but for short-term SOC changes with biochar addition.



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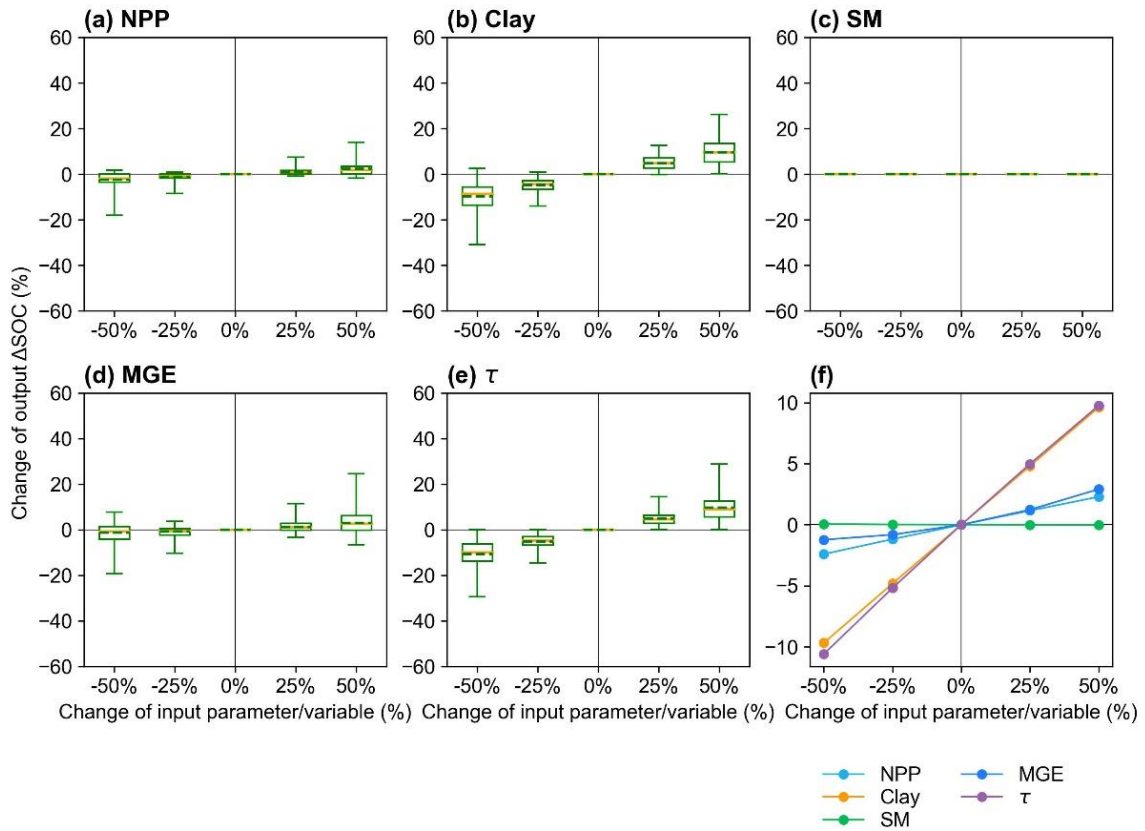
**Fig. S14** Relationships of short-term SOC changes after biochar addition between observations and models with (a) MIMICS<sub>TSMb-BC<sub>def</sub></sub>, (b) MIMICS<sub>TSMb-BC<sub>D</sub></sub>, (c) MIMICS<sub>TSMb-BC<sub>DV</sub></sub> and (d) MIMICS<sub>TSMb-BC<sub>DV-SOCa</sub></sub>. ( $f_{ba}=2\%$ ). Blue and red dots represent observation sites for model calibration (80% sites) and validation (20% sites), respectively.

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**Fig. S15** Relationships of short-term SOC changes after biochar addition between observations and models simulated with MIMICS<sub>TSMb-BC<sub>DV</sub></sub> version with four parameters optimized (optimized values:  $f_d=0.1123$ ,  $f_v=-0.0088$ ,  $f_{bp}=0.581$  and  $f_{ba}=0.0816$ ). Blue and red dots represent observation sites for model calibration (80% sites) and validation (20% sites), respectively.



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**Fig. S16** Sensitivity analysis of MIMICS<sub>TSMb-BCDV</sub> model input variables of (a) NPP, (b) Clay, (c) SM and parameters of (d) MGE (microbial growth efficiency, Fig. 1) and (e)  $\tau$  (microbial biomass turnover, Fig. 1). The yellow line and green dotted line in boxplot are median and mean values of output variable change (i.e., change of  $\Delta$ SOC, Eq. 19). The means of  $\Delta$ SOC changes with perturbations in calibrated sites are plot in (f).

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