

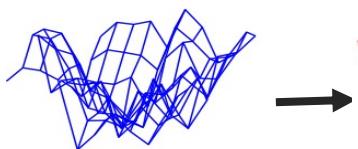
Expected  $\Delta TS_{m,s}$  obtained from  $\Gamma_m$



Step 1: derive the posterior distribution of coefficient terms ( $\beta$ ) :

$$f(\beta | \hat{\lambda}, \Delta TS_{m,s}) f_{\hat{\lambda}}(\hat{\lambda})$$

For k in 1 ... no. of bootstraps:



(a) Sample around the expected  $\Delta TS_{m,s}$  to obtain a bootstrap-sampled set of  $\Delta TS_{m,s}$

(b) Fit on the bootstrap-sampled set of  $\Delta TS_{m,s}$  to get an estimate of  $\lambda$  ( $\hat{\lambda}_k$ ).

Estimate of  $f(\beta | \hat{\lambda}, \Delta TS_{m,s})$  at bootstrap round k

$$\beta_k \sim \mathcal{N} \left[ \begin{pmatrix} \mu_{\beta_{k,0}} \\ \vdots \\ \mu_{\beta_{k,j}} \end{pmatrix}, \begin{pmatrix} \sigma_{\beta_{k,0}}^2 & \cdots & \sigma_{\beta_{k,j}} \sigma_{\beta_{k,0}} \\ \vdots & \ddots & \vdots \\ \sigma_{\beta_{k,0}} \sigma_{\beta_{k,j}} & \cdots & \sigma_{\beta_{k,j}}^2 \end{pmatrix} \right]$$

(c) Fit on the actual set of  $\Delta TS_{m,s}$  using the  $\hat{\lambda}_k$  value derived in step (1b) to get an estimate of the distribution of  $\beta$ .



Step 2: sample  $\Delta TS_{m,s}$  using  $f(\beta | \hat{\lambda}, \Delta TS_{m,s}) f_{\hat{\lambda}}(\hat{\lambda})$  obtained in Step 1

For i in 1 ... no. of samples:

(a) Randomly generate a number,  $l$ , between 1 and the no. of bootstraps



$$\beta_l \sim \mathcal{N} \left[ \begin{pmatrix} \mu_{\beta_{l,0}} \\ \vdots \\ \mu_{\beta_{l,j}} \end{pmatrix}, \begin{pmatrix} \sigma_{\beta_{l,0}}^2 & \cdots & \sigma_{\beta_{l,j}} \sigma_{\beta_{l,0}} \\ \vdots & \ddots & \vdots \\ \sigma_{\beta_{l,0}} \sigma_{\beta_{l,j}} & \cdots & \sigma_{\beta_{l,j}}^2 \end{pmatrix} \right]$$



(b) Draw coefficient terms from the distribution obtained at the  $l^{th}$  bootstrap round.

(c) Estimate  $\Delta TS_{m,s}$  using the coefficient terms drawn in step (2b)