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1 # Additional constants and definition of compressible reference state:
2 Ra = Constant(1e5) # Rayleigh number
3 Di = Constant(0.5) # Dissipation number
4 T0 = Constant(0.091) # Non-dimensional surface temperature
5 tcond = Constant(1.0) # Thermal conductivity
6 rho_0, alpha, cpr, cvr, gruneisen = 1.0, 1.0, 1.0, 1.0, 1.0
7 rhobar = Function(Q, name="CompRefDensity").interpolate(rho_0 * exp(((1.0 - X[1]) * Di) / alpha))
8 Tbar = Function(Q, name="CompRefTemperature").interpolate(T0 * exp((1.0 - X[1]) * Di) - T0)
9 alphabar = Function(Q, name="IsobaricThermalExpansivity").assign(1.0)
10 cpbar = Function(Q, name="IsobaricSpecificHeatCapacity").assign(1.0)
11 chibar = Function(Q, name="IsothermalBulkModulus").assign(1.0)
12 FullT = Function(Q, name="FullTemperature").assign(Tnew+Tbar)
13
14 -----
15 # Equations in UFL:
16 I = Identity(2)
17 stress = 2 * mu * sym(grad(u)) - 2./3.*I*mu*div(u)
18 F_stokes = inner(grad(v), stress) * dx - div(v) * p * dx - (dot(v, k) * (Ra * Ttheta * rhobar * alphabar - (Di/
    gruneisen) * (cpr/cvr)*rhobar*chibar*p) * dx)
19 F_stokes += -w * div(rhobar*u) * dx # Mass conservation
20 F_energy = q * rhobar * cpbar * ((Tnew - Told) / delta_t) * dx + q * rhobar * cpbar * dot(u, grad(Ttheta)) * dx +
    dot(grad(q), tcond * grad(Tbar + Ttheta)) * dx + q * (alphabar * rhobar * Di * u[1] * Ttheta) * dx - q * (
    (Di/Ra) * inner(stress, grad(u)) ) * dx
21
22 -----
23 # Temperature boundary conditions:
24 bctb, bctt = DirichletBC(Q, 1.0 - (T0*exp(Di) - T0), bottom), DirichletBC(Q, 0.0, top)
25
26 -----
27 # Pressure nullspace:
28 stokes_solver = NonlinearVariationalSolver(stokes_problem, solver_parameters=solver_parameters,
    transpose_nullspace=p_nullspace)

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