



Supplement of

CoupModel (v6.0): an ecosystem model for coupled phosphorus, nitrogen, and carbon dynamics – evaluated against empirical data from a climatic and fertility gradient in Sweden

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Global sensitivity analysis of all new P parameters and relevant N parameters

1. Parameters and the associated ranges

The P parameters introduced in Coup-CNP, along with N process parameters relevant for plant photosynthesis, nutrient uptake parameters and fungal growth parameters, were selected for a global sensitivity analysis (Table S.1). Overall, 34 parameters were analyzed, with these parameters further grouped into 13 categories: (1) Initial value ($Ini_{P,h}$); (2) N uptake ($o_{uptNhumus}$); (3) P uptake ($o_{uptPhumus}$, p_{iavail}); (4) Source (k_w , n_H , pH_{opt}); (5) Partitioning ($p_{max,ads}$, $c_{50,ads}$); (6) Photosynthesis ($p_{cp,opt}$, $n_{cn,opt}$, $p_{cp,th}$, $n_{cn,th}$); (7) GPP allocation (p_{avail} , n_{avail} , p_{fopt}); (8) Fungi (k_{rm} , p_{Irate}); (9) P demand to fungi ($p_{i,rate}$, $p_{cpfungimax}$, $p_{cpfungimin}$, $p_{olit,rate}$, $p_{ohum,rate}$); (10) N demand to fungi ($n_{NH4rate}$, $n_{NO3rate}$, $n_{olit,rate}$, $n_{ohum,rate}$); (11) P transformation (cp_m , m_{retain}); (12) P demand to plant (cp_{leaf} , min, $cp_{stem, min}$, $cp_{croot, min}$, $cp_{root, min}$); and (13) Erosion (p_{base} , p_{Δ} , q_{thr}). The parameter ranges were obtained by varying the default values reported in Table 3 by \pm 50 % (Table S.1). The default values were used as a reference since they have been calibrated against observations of forest growth, leaf nutrient ratios and nutrient leaching.

The initial soil C and soil N values (Table 1) for each region were kept constant. Due to uncertainties in the soil P data for deeper soil layers, we included the initial value of soil humus P in the global sensitivity analysis. The initial value of total organic P in humus varied from 8.45 to 21.16 g P m⁻² for the 64°N region (Table S.1). This defined total P range translates to a total soil C/P ratio of 315-788, which is similar to the synthesized literature value (N/P between 10 to 25, see section 3.2) for this region.

For the 56°N region, the initial value of soil humus P varied from 18.42 to 53.9 g P m⁻² (Table S.1), translating to a soil C/P ratio of 188-550. This range was set to be wide enough to cover the current synthesized literature value 198-495 for the region, along with additional data from the Swedish Forestry Agency concerning the humus layer (e.g. C/P of 188 in Gynge, Table 1). To summarize, the ranges of initial soil P tested in the sensitivity analysis cover the C/P ranges of the regional sites presented in data from the Swedish Forestry Agency and relevant literature.

2. Model design

We conducted a Monte Carlo-based global sensitivity analysis for 34 parameters (Table S.1) for two regions: the northernmost 64^oN region, characterized by N limitation, and the southernmost 56^oN region, characterized by P limitation. The probability distribution function for each parameter was assumed to be uniform. Random sampling was used to generate random sets of parameter values. Overall, 600 runs were conducted for each region. We evaluated the responses of a number of model variables to changes in the analyzed parameters. The importance of the 34 parameters was analyzed based on changes in the C, N, and P components that are vital for ecosystem functioning. More specifically, we assessed the magnitude of changes in ecosystem C change, total C harvested, plant C change, soil C change, plant N change, soil N change, plant P change, soil P change, and N/P response on GPP. Correlation analysis (Pearson correlation coefficient, r) was used to rank the parameters based on importance. The analysis proceeded as follows: first, model performance indicators including correlation of determination, R², and mean error with respect to the reference model run (i.e. Fig. 2) were estimated for each model run; then, Pearson correlation coefficient (r) was calculated from the parameter and the model performance indicators. Thus, a high r value

between a parameter and the R² (or ME) value of a selected variable means that the parameter is important in regulating the dynamics (or magnitude) selected variable. We chose $r \ge 0.2$ or ≤ -0.2 as a threshold for parameter importance.

3. Parameter sensitivity

The global sensitivity analysis results identified three important parameters for the regulation of forest ecosystem C, N and P cycling. These include initial soil organic P ($Ini_{P,h}$), the coefficient for short-cut N uptake from the humus pool ($o_{uptNhumus}$) and the coefficient for short-cut P uptake from the humus pool ($o_{uptPhumus}$) (Table S.2, Table S.3). The northern regions were more sensitive to changes in $o_{uptNhumus}$, a finding which reflects the N-limited nature of the 64⁰N region, whereas the southern 56⁰N region was more sensitive to $Ini_{P,h}$ due to P limitation (Figs. S.1, S.2, S.3, S.4).

The first parameter with a large impact on model output was the initial vale of soil P, which determines the P content in soil organic matter. The importance of the initial value of humus P, $Ini_{P,h}$, again confirms that the C/P and N/P ratios in organic matter have crucial roles in determining the ecosystem C, N and P fluxes and pool sizes, as we concluded in the main paper. In addition, very few parameter from the source category (parameters controls weathering rates, e.g. pH_{opt}) showed a noticeable impact on model output (Table S.2). This confirms that the internal cycling of P is more important in regulating ecosystem C, N and P dynamics than the current weathering inputs in Swedish forests.

Parameters related to N/P uptake ($o_{uptNhumus}$, $o_{uptPhumus}$) and P transformation (cp_m) also significantly affected model output. These parameters represent processes that directly control N and P availability or release from mineralization, which are important to regulating photosynthesis and forest growth (Table S.2, Table S.3).

The third set of parameters identified through the sensitivity analysis covered plant growth and dynamics, including three categories: P demand to P ($cp_{leaf, min}, cp_{leaf, root}$); Photosynthesis ($n_{cn,opt}, n_{cn,th}, p_{cp,opt}, p_{cp,opt}$); and GPP allocation (p_{fopt}) (Table S.2, Table S.3). These parameters regulate C allocation within the plants, plant stoichiometry, as well as plant-fungi symbiosis. Interestingly, total harvested C was negatively correlated with the C allocated to symbiotic fungi (p_{fopt}) for both regions.

Changes in many parameters were found to impact more than one simulated variable. The sign of the correlation between a parameter and soil nutrient (N/P) change, is flipped for that of plant nutrient (N/P) change (Table S.2, Table S.3). This is expected as the nutrients are generally relocate between plant and soil, with minor inputs. The interaction between N and P was identified in the sensitivity analysis. For instance, changes in two parameters ($Ini_{P,h}$, cp_m) regulating P availability in the soil consistently had a large influence on the simulated response of N on GPP (Table S.2, Table S.3).

The global sensitivity analysis highlighted the importance of initial organic P and the short-cut uptake coefficients. We conducted an additional analysis by removing the three key parameters ($Ini_{P,h}$, $o_{uptNhumus}$, $o_{uptPhumus}$) from the global sensitivity analysis. We then re-ran the model, 300 runs for the northernmost 64^{0} N region, with the remaining 31 parameters. The results are shown in Table S.4. This analysis identified the parameters with the largest effect on model output to be those that had been included in the initial second and third set of sensitive

parameters, notably, P transformation (cp_m), plant P demand ($cp_{leaf, min}, cp_{leaf, root}$), Photosynthesis ($n_{cn,opt}, n_{cn,th}, p_{cp,opt}, p_{cp,opt}$) and GPP allocation (p_{fopt}) (Table S.2, Table S.3).

The fourth set of key parameters represent fungi-related processes. Among these, fungal respiration rate (k_{rm}), GPP allocation to fungi (p_{fopt}), fungal litter rate (p_{lrate}), and N demand to fungi ($n_{NO3rate}$, $n_{NH4rate}$) were shown to have the most significant effects on model output (Table S.4). Parameters in the partitioning ($c_{50,ads}$, $p_{max,ads}$) and weathering (pH_{opt} , k_w) categories had the least significant effect on model output (Table S.4).

Table S.1 List of parameters, and the corresponding ranges, used in Monte Carlo based sensitivity analysis. For a detailed explanation, including equations, for the parameters, see section 3 in the paper. Please note that the initial value for total humus P had different ranges in the 64^{0} N and 56^{0} N region.

Category	Symbol	Parameter	Equation	Min	Max	Unit
Initial value	Ini _{P,h}	Initial value for total	-			g P m ⁻²
		organic P of humus		8.45	53.9	
N uptake	OuptNhumus	Coefficient for	-			day-1
		shortcut N uptake				
		from humus		2.50×10^{-6}	1.50×10^{-5}	
P uptake	O uptPhumus	Coefficient for	-			day ⁻¹
		shortcut P uptake			_	
	_	from humus		5.00×10-6	2.75×10-5	
Source	k_w	Integrated	(1)	4×10-7	1.2×10-6	day-1
		weathering rate		0.107	0.407	
Source	n_H	Weathering pH	(4)	0.135	0.405	-
		response coefficient			10.5	
Source	pH_{opt}	Weathering pH	(4)	3.5	10.5	-
		response base				
		coefficient	(7)	0.0001	0.0002	D
Partitioning	$p_{max,ads}$	Langmuir max	(5)	0.0001	0.0003	g P g
D mutiti and a		Longroup holf	(5)	2.5, 10-5	7.5.10-5	sol1
Partitioning	C 50,ads	Langmuir nall	(5)	2.5×10 ⁵	7.5×10°	g P m -
Dh at a grunth a gig		Saturation coefficient C/D optimal (loof)	(0)	125	275	$\sim C \sim D^{-1}$
Photosynthesis Dhotosynthesis	$p_{cp,opt}$	C/P optimal (leaf)	(8)	125	375	$gC gP^{-1}$
Photosynthesis	n _{cn,opt}	C/N optimial (leaf)	-	12.3	37.3 800	gC gIN
Photosynthesis	$p_{cp,th}$	C/F threshold (leaf)	(0)	400	800 75	gC gF
CDD allogation	<i>N_{cn,th}</i>	C/N threshold (lear)	-	57.5	73	ge gn
GFF anocation	Pavail	reduction of C	(9)	0.00043	0.00133	-
		allocation to fungi				
		under high P				
		availability				
GPP allocation	navail	Coefficient for the		0.000195	0.000585	-
	aran	reduction of C				
		allocation to fungi				
		under high N				
		availability				
GPP allocation	p_{fopt}	The optimum ratio	(11)	0.11	0.33	-
		for C allocation				
		between fungi and				
		root				
Fungi	k_{rm}	Fungal respiration		0.005	0.015	day ⁻¹
		coefficient				
Fungi	p_{lrate}	Fungal litterfall rate	(15)	0.00225	0.00675	day ⁻¹
P demand to	$p_{i,rate}$	Potential unit fungal	(19)	0.00005	0.00015	$g P g C^{-1}$
fungi		mycelia uptake rate				$m^{-2} day^{-1}$
		PO ₄	ļ	0.0055		
N demand to	n _{NH4rate} /	Potential unit fungal		0.0002	0.0006	$g N g C^{-1}$
fungi	<i>n_{NO3rate}</i>	mycelia uptake rate				m^{-2} day
		NH ₄ /NO ₃				10

N demand to	$n_{olit,rate}/$	Potential unit fungal		0.00001	0.00003	g N g C ⁻¹
fungi	nohum, rate	mycelia uptake rate				m ⁻² day ⁻¹
		organic N.				
P demand to	Denfungimar	Fungal maximum	(17)	100	300	$\sigma C \sigma P^{-1}$
fungi	Peppungunar	C/P	(1)	100	200	80.81
Puntake	n	Maximum PO	(21)	0.004	0.012	_
1 иргаке	Piavail	untaka fraction for	(21)	0.004	0.012	-
			(00)	50	150	
P demand to	$p_{\it cpfungimin}$	Fungal minimum	(22)	50	150	-
fungi		C/P	-	_		
P demand to	$p_{Litterf}$	Potential unit fungal	(23)	0.00001	0.00003	g P g C ⁻¹
fungi	p_{Humusf}	mycelia uptake rate				m ⁻² day ⁻¹
		organic P				
Р	cp_m	C/P of non	(A.3)	175	525	-
transformation	-	symbiotic microbes				
P demand to	CDleaf min		(A.9)	110	330	-
nlant	-F reag, min	Minimum C/P (leaf)	()			
P demand to	cn	Minimum C/P for	$(\Delta 9)$	2000	6000	_
nlant	CP stem, min	stem and coarse	(11.))	2000	0000	_
piani	/ cp_{croot} ,					
	min			200	(00	
P demand to	$cp_{root, min}$	Minimum C/P ratio	(A.9)	200	600	-
plant		(fine roots)				1
Erosion	p_{base}	P concentration	(A.14)	1.35×10^{-6}	4.05×10 ⁻⁴	mg l ⁻¹
		scaling coefficient				
		for surface erosion 1				
Erosion	p_{Δ}	P concentration	(A.14)	3.5×10 ⁻⁶	1.05×10 ⁻³	mg l ⁻¹
		scaling coefficient				_
		for surface erosion 2				
Erosion	<i>a</i> _{thr}	Critical surface flow	(A.14)	0.5	15	mm dav⁻
	1.00	rate for erosion			-	1
Р	m	Mobile coefficient	-	0.1	03	_
transformation	norelain	describing the		0.1	0.5	
iransjormation		fraction of D and N				
		naction of F and N				
		internel mehile mel				
		mernal mobile pool				
		when the plants goes				
		into dormancy				

Variables	Parameters controlling dynamics			Parameters controlling magnitude				
	(\mathbb{R}^2)				(ME)			
Ecosystem C	cp_m	Ini _{P,h}	OuptNhumus		OuptNhumus	cp_m		
change	0.23	0.2	0.2		0.8	0.32		
Total C	O uptNhumus	cp_m	pH_{opt}	p_{fopt}	O uptNhumus	$n_{cn,th}$	p_{fopt}	
harvest	0.29	0.27	0.2	-0.2	0.83	0.25	-0.2	
Plant C	cp_m	O uptNhumus			O uptNhumus	cp_m	$n_{cn,th}$	p_{fopt}
change	0.21	0.2			0.82	0.23	0.24	-0.21
Soil C	OuptNhumus	cp_m			OuptNhumus	cp_m	Ini _{P,h}	
change	0.78	0.34			0.7	0.42	0.23	
Plant N	OuptNhumus	$cp_{\mathit{leaf, min}}$			OuptNhumus	<i>n</i> _{cn,th}	Ini _{P,h}	
change	0.28	0.2			0.8	-0.34	-0.22	
Soil N	O uptNhumus	cp_m			O uptNhumus	Ini _{P,h}	<i>n</i> _{cn,th}	
change	0.25	0.2			-0.74	0.25	0.36	
Plant P	OuptNhumus				Ini _{P,h}	cp_m	$p_{cp,th}$	
change	0.31				0.71	0.39	-0.2	
Soil P	OuptNhumus				Ini _{P,h}	cp_m	$p_{cp,opt}$	$p_{cp,th}$
change	0.35				-0.70	-0.4	-0.41	0.2
Response of	Ini _{P,h}	cp_m	n _{cn,opt}		Ini _{P,h}	cp_m	O uptNhumus	
N on GPP	0.38	0.29	-0.26		-0.4	-0.31	0.25	
Response of	Ini _{P,h}	O uptNhumus	$n_{cn,th}$	$p_{cp,opt}$	Ini _{P,h}	$p_{cp,opt}$	cp_m	OuptNhumus
P on GPP	-0.53	0.33	0.22	-0.2	0.55	0.37	0.31	-0.31

Table S.2. List of parameters with the largest influences on the simulated C, N and P fluxes and pools for the northernmost 64^{0} N region. Parameter importance was ranked by the given correlation coefficient (r) between the parameter and the model performance indicator.

Variables	Parameters controlling dynamics (R ²)			Parameters controlling magnitude				
				(ME)				
Ecosystem					Ini _{P,h}	O _{uptNhumus}	cp_m	OuptPhumus
C change					0.45	0.28	0.25	0.24
Total C	O uptNhumus	$n_{cn,th}$			O uptNhumus	O uptPhumus	$n_{cn,th}$	p_{fopt}
harvest	0.23	0.2			0.39	0.29	0.28	-0.2
Plant C	O _{uptNhumus}				O _{uptNhumus}	O _{uptPhumus}	<i>n</i> _{cn,th}	Ini _{P,h}
change	0.35				0.36	0.29	0.26	0.22
Soil C	Ini _{P,h}	cp_m			Ini _{P,h}	cp_m		
change	0.39	0.25			0.61	0.39		
Plant N	Ini _{P,h}	cp_m			Ini _{P,h}	O uptNhumus	cp_m	p_{fopt}
change	0.33	0.23			-0.61	0.4	-0.34	-0.26
Soil N	Ini _{P,h}	cp_m			Ini _{P,h}	cp_m	O _{uptNhumus}	
change	0.27	0.24			0.61	0.34	-0.26	
Plant P	Ini _{P,h}	OuptNhumus	$cp_{min,leaf}$	$cp_{min,root}$	Ini _{P,h}	cp_m		
change	-0.37	0.27	-0.27	-0.22	0.78	0.41		
Soil P	Ini _{P,h}	$cp_{min,root}$	OuptNhumus	$cp_{min,leaf}$	Ini _{P,h}	cp_m		
change	-0.4	-0.28	0.27	-0.27	-0.77	-0.4		
Response	<i>n</i> _{cn,opt}				Ini _{P,h}	cp_m	O _{uptNhumus}	
of N on	-0.3				-0.68	-0.24	0.22	
GPP								
Response	Ini _{P,h}	cp_m	O uptNhumus		Ini _{P,h}	cp_m	$p_{cp,opt}$	
of P on GPP	-0.75	-0.25	0.21		0.70	0.26	0.23	

Table S.3. List of parameters with the largest influences on the simulated C, N and P fluxes and pools for the southernmost 56^{0} N region. Parameter importance was ranked by the given correlation coefficient (r) between the parameter and the model performance indicator.

Table S.4. List of parameters with the largest influences on the simulated C, N and P fluxes and pools for the northernmost 64^{0} N region, excluding initial soil P and short-cut uptake coefficients for N and P. Parameter importance was ranked by the given correlation coefficient (r) between the parameter and the model performance indicator.

Variables	Parameters controlling dynamics				Parameters controlling magnitude			
	(\mathbf{R}^2)				(ME)			
Ecosystem	n _{NO3rate}	p_{Humusf}	m _{retain}	cp _{min,root}	<i>n</i> _{cn,th}	<i>k</i> _{rm}	p_{fopt}	<i>n_{NH4rate}</i>
C change	0.35	-0.23	0.23	-0.27	0.7	0.49	-0.38	-0.37
Total C	p_{fopt}	<i>n</i> _{cn,th}	$cp_{min,leaf}$		<i>n</i> _{cn,th}	k _{rm}	p_{fopt}	<i>n_{NH4rate}</i>
harvest	-0.49	0.47	-0.27		0.63	0.57	-0.4	-0.35
Plant C	<i>n</i> _{cn,th}	<i>p</i> _{fopt}			$n_{cn,th}$	krm	p_{fopt}	<i>n</i> _{NH4rate}
change	0.47	-0.3			0.63	0.54	-0.43	-0.36
Soil C	p_{lrate}	cp _{min,root}	n _{cn,opt}	$p_{cp,opt}$	$n_{cn,th}$	n _{NH4rate}	cp _{min,croot}	C 50, ads
change	-0.29	-0.28	0.26	-0.22	0.72	-0.31	-0.29	-0.22
Plant N	<i>n</i> _{cn,th}	C50,ads	p _{iavail}	navail	<i>n</i> _{cn,th}	p _{lrate}	q_{thr}	k_w
change	-0.42	0.28	0.25	0.25	-0.86	-0.3	0.28	-0.25
Soil N	<i>cp</i> _{min,stem}	$p_{cp,opt}$	p _{iavail}	<i>p</i> _{fopt}	<i>n</i> _{cn,th}	C50,ads	$p_{cp,th}$	p _{lrate}
change	0.23	0.23	-0.22	0.2	0.78	-0.26	0.22	0.23
Plant P	$cp_{min,leaf}$	cp_m	n _{cn,opt}	$p_{max,ads}$	cp_m	$p_{max,ads}$	pH_{opt}	k _{rm}
change	-0.71	-0.54	-0.36	0.23	0.84	-0.32	-0.3	0.28
Soil P	$cp_{min,leaf}$	cp_m	n _{cn,opt}	$p_{cp,opt}$	cp_m	krm	pH_{opt}	$p_{max,ads}$
change	-0.73	-0.56	-0.32	-0.25	-0.83	-0.32	0.32	0.30
Response	n _{cn,opt}	<i>n</i> _{cn,th}	p _{i,rate}	$p_{cp,th}$	n _{cn,opt}	$n_{cn,th}$	p _{i,rate}	
of N on	-0.53	0.31	-0.31	-0.22	0.47	-0.37	0.29	
GPP								
Response	p _{cp,opt}	$cp_{min,leaf}$	cp_m	$p_{cp,th}$	p _{cp,opt}	$cp_{min,leaf}$	<i>p</i> _{Humusf}	
of P on	-0.64	-0.39	-0.38	0.26	0.53	-0.5	-0.38	
GPP								



Fig. S.1 Plant and soil changes in C, N and P in relation to the two most influential parameters (initial soil humus P ($Ini_{P,h}$) and the coefficient for short-cut N uptake from humus ($o_{uptNhumus}$)) for the northernmost region (64⁰N).



Fig. S.2 Responses of N and P on GPP in relation to the two most influential parameters (initial soil humus P ($Ini_{P,h}$) and the coefficient for short-cut N uptake from humus ($o_{uptNhumus}$)) for the northernmost region (64⁰N).



Fig. S.3 Plant and soil changes in C, N and P in relation to the two most influential parameters (initial soil humus P ($Ini_{P,h}$) and the coefficient for short-cut P uptake from humus ($o_{uptPhumus}$)) for the southernmost region (56⁰N).



Fig. S.4 Responses of N and P on for GPP in relation to the two most influential parameters (initial soil humus P ($Ini_{P,h}$) and the coefficient for short-cut P uptake from humus ($o_{uptPhumus}$)) for the southernmost region (56⁰N).

Data availability

The files used to generate the sensitivity analysis were archived at Zenodo (<u>https://doi.org/10.5281/zenodo.4291963</u>), also they will be made available from the CoupModel webpage <u>www.coupmodel.com</u>.