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1 # Element tensors defining the local 3-by-3 block system
2 _A = Tensor(a)
3 _F = Tensor(L)
4
5 # Extracting blocks for Slate expression of the reduced system
6 A = _A.blocks
7 F = _F.blocks
8 Sexp = A[2, 2] - A[2, :2] * A[:2, :2].inv * A[:2, 2] # Slate expression for  $S^K$ 
9 Eexp = F[2] - A[2, :2] * A[:2, :2].inv * F[:2] # Slate expression for  $E^K$ 
10 S = assemble(Sexp, bcs=[...]) # Assemble  $S$ 
11 E = assemble(Eexp) # Assemble  $E$ 
12 lambda_h = Function(M) # Function to store the result:  $\Lambda$ 
13
14 # Solve for the Lagrange multipliers:  $\Lambda$ 
15 solve(S, lambda_h, E, solver_parameters={"ksp_type": "preonly", "pc_type": "lu"})
16 p_h = Function(V) # Function to store the result:  $P$ 
17 u_h = Function(U) # Function to store the result:  $U^d$ 
18 Lambda = AssembledVector(lambda_h) # Local coefficient vector:  $\Lambda^K$ 
19 P = AssembledVector(p_h) # Local coefficient vector:  $P^K$ 
20
21 # Intermediate expressions
22 Sd = A[1, 1] - A[1, 0] * A[0, 0].inv * A[0, 1]
23 Sl = A[1, 2] - A[1, 0] * A[0, 0].inv * A[0, 2]
24
25 # Slate expressions for local recovery
26 p_sys = Sd.solve(F[1] - A[1, 0] * A[0, 0].inv * F[0] - Sl * Lambda,
27 decomposition="PartialPivLu")
28 u_sys = A[0, 0].solve(F[0] - A[0, 1] * P - A[0, 2] * Lambda,
29 decomposition="PartialPivLu")
30 assemble(p_sys, p_h) # Solve for  $P$ 
31 assemble(u_sys, u_h) # Solve for  $U^d$ 

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