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*Supplement of*

## **Implementation of the RCIP scheme and its performance for 1-D age computations in ice-sheet models**

**Fuyuki Saito et al.**

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## S1 Comprehensive experiment sheets

In addition to the experiments presented in the main paper, several experimental configuration combinations of parameters are examined. In this Supplement, some representative results of them are provided. All of the experiments shown are examined under non-steady surface mass balance configurations. Each page contains two figures: the upper one is the result obtained using a square-wave type surface mass balance input, while the lower is one with the same configuration except for applying a cosine-wave type input. One figure contains five sub-figures. (a) profiles of the computed age, (b,d) The computed age differences relative to the result of the `RCIP+corr` case, and (c,e) the annual layer thickness. The upper sub-figures (a-c) show the profiles in terms of depths, while the lower sub-figures (d-e) show them in terms of the computed ages. The surface mass balance input used in each experiment is shown in the lower left figure for only first 200 or 100 kyr. The prescribed time evolution of ice-thickness is also shown in the lower left figure for the non-steady thickness experiments. The grey and black lines in (a,c,e) correspond to ‘benchmark’ profiles which are computed using constant surface/basal mass balance and thickness.

Figures S1 to S6 are the results of a most standard experiments: constant  $H = 3000\text{ m}$ ,  $a_H, a_L = 3, 1.5 \text{ cm yr}^{-1}$ ,  $P_T = 100 \text{ kyr}$ ,  $P_H : P_L = 1 : 1$ , and the uniform discretization of 129 levels (see Eq.57 in the main text about definition of  $a_H, a_L, P_T, P_H$  and  $P_L$ ). Basal mass balances are set as constant  $M_b = 0 \text{ mm yr}^{-1}$  (S1,S2),  $M_b = 0.3 \text{ mm yr}^{-1}$  (S3,S4), and  $M_b = 3 \text{ mm yr}^{-1}$  (S5,S6). All of the results are the snapshots at  $t = 1 \text{ Myr}$ .

Figures S7 to S12 are the same combination as presented above except for  $a_L = 0.75 \text{ cm yr}^{-1}$ . Figures S13 to S18 are the same except for  $a_L = 0 \text{ cm yr}^{-1}$ . Figures S19 to S22 are the same except for  $a_L = -15 \text{ cm yr}^{-1}$ .

Two types of sensitivity experiments regarding to the shape of prescribed time-evolution of surface mass balance inputs are performed: one type obtained using a different  $P_H : P_L$ , and the other using a different  $P_T$ . Figures S23 to S26 are the results obtained using a longer  $P_H$ , as  $P_H : P_L = 7 : 1$ , and Figures S27 to S30 are the results using a shorter  $P_H$ , as  $P_H : P_L = 1 : 7$ . Figures S31 to S38 are the results obtained using  $P_T = 50 \text{ kyr}$ , Figures S39 to S46 using  $P_T = 20 \text{ kyr}$ , and Figures S47 to S54 using  $P_T = 10 \text{ kyr}$ .

Two types of sensitivity experiments regarding to the shape of prescribed time evolution of ice-thickness are performed: one type with  $\tau_H = 10 \text{ kyr}$  (Figs.S55 to S58), and the other with  $\tau_H = 3 \text{ kyr}$  (Figs.S59 to S62). (see Eq.61 in the main text about definition of  $\tau_H$ ).

The series of experiments obtained using constant  $H = 3000\text{ m}$  and  $M_b = 0 \text{ mm yr}^{-1}$  are repeated by higher resolution configurations. Figures.S63 to S70 are the results of  $P_T = 100 \text{ kyr}$ ; Figures.S71 to S94 are results obtained using a uniform discretization of 513 levels. Figures.S95 to S126 are the same results but using a smooth non-uniform discretization of 513 levels. Figures.S127 to S158 are the same results but using a non-smooth non-uniform discretization of 477 levels. The snapshots at  $t = 2 \text{ Myr}$  are plotted for those experiment with higher resolutions. Designs of these higher resolution discretization are shown in Fig. 14 in the main text.

Furthermore, the series of experiments obtained using constant  $H = 3000\text{ m}$  and  $M_b = 0 \text{ mm yr}^{-1}$  are repeated by lower resolution configurations. Figures.S159 to S166 are the results of  $P_T = 100 \text{ kyr}$ , obtained using a uniform discretization of 33 levels.

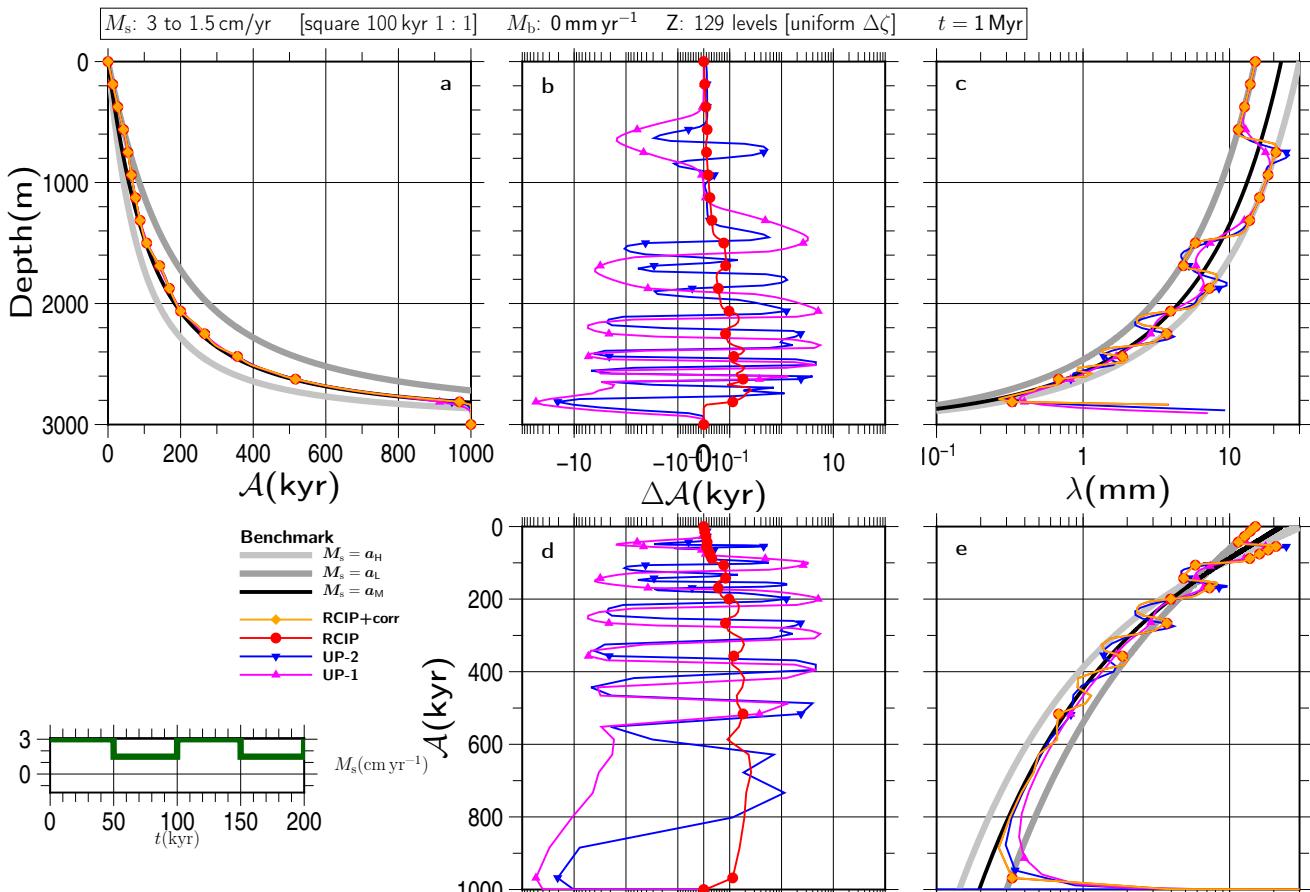


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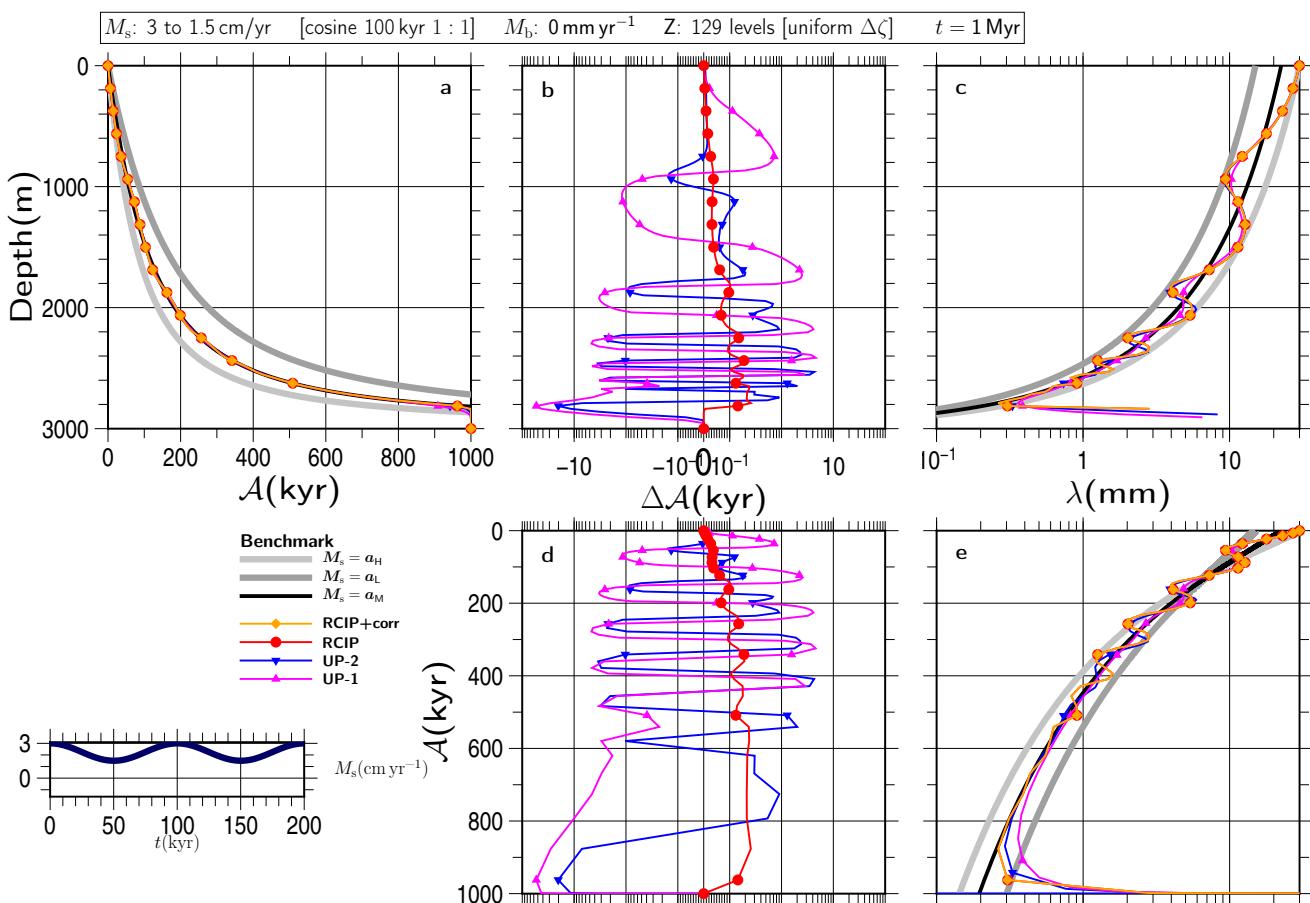


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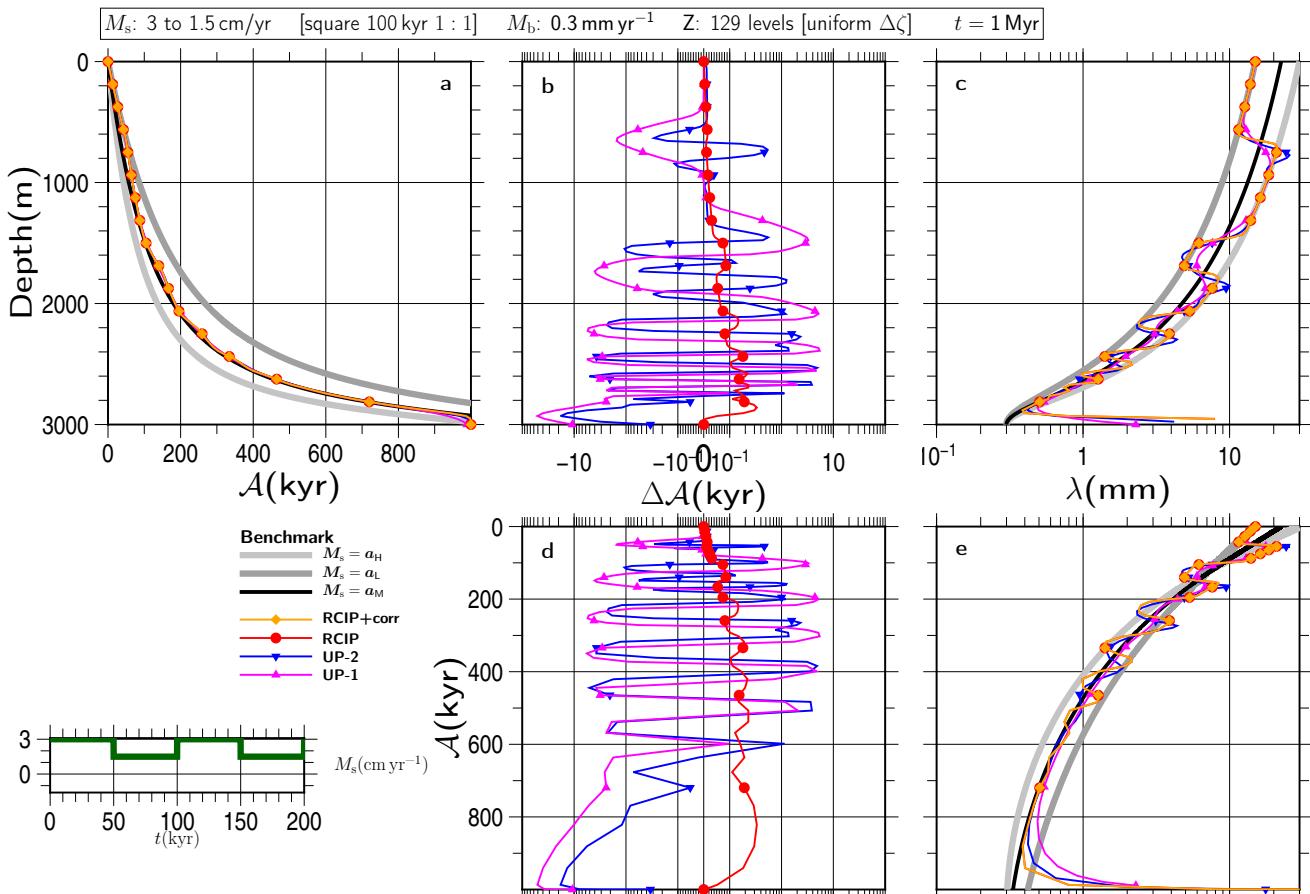


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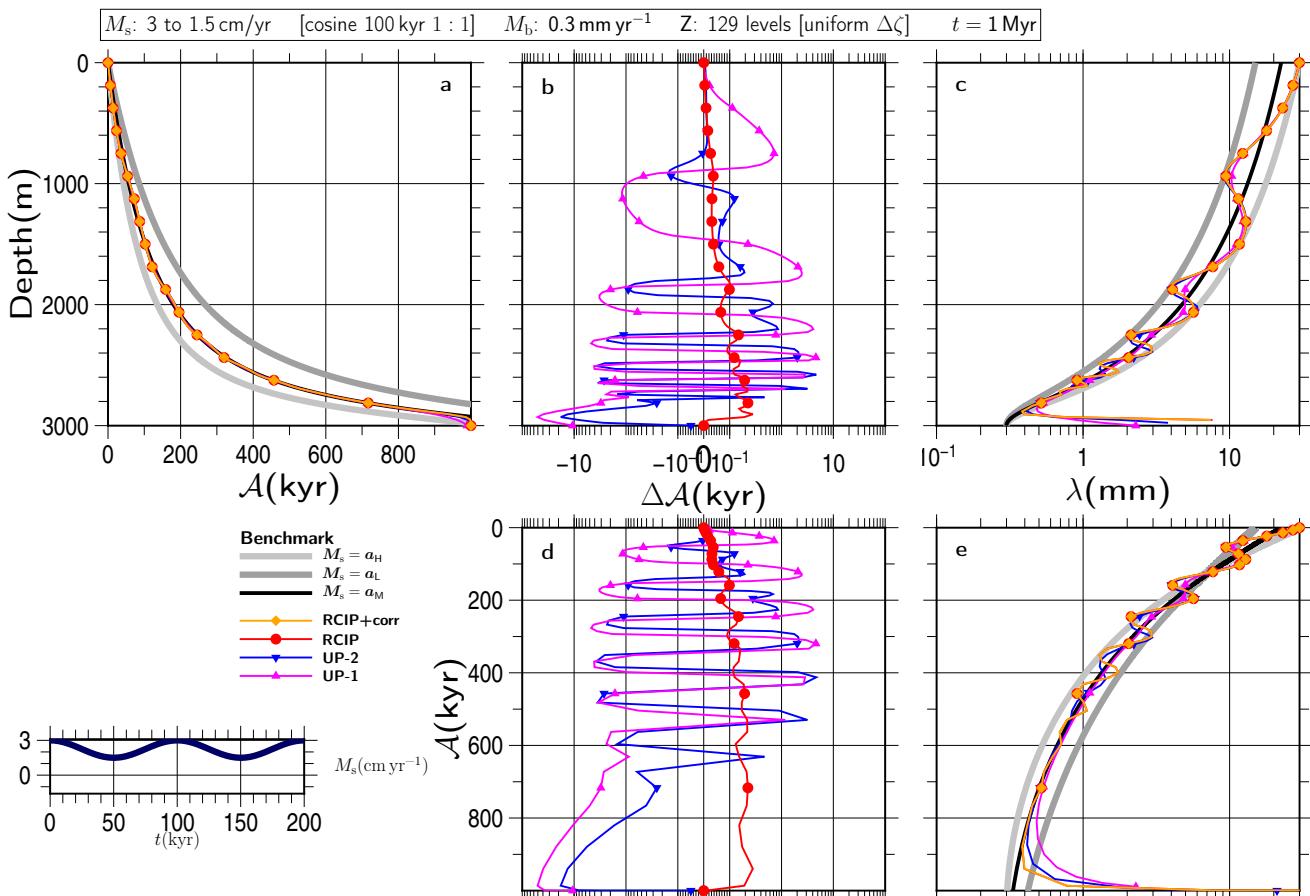


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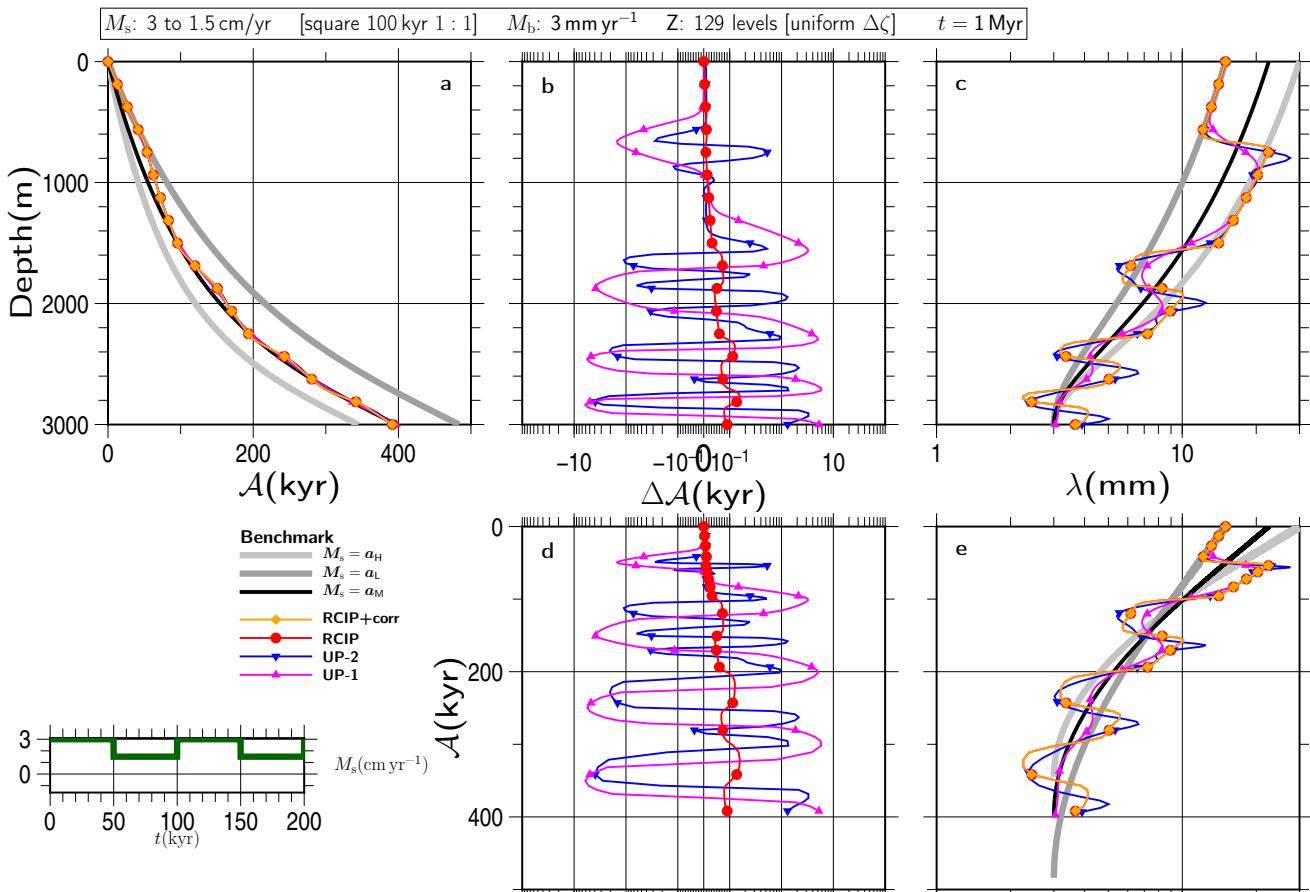


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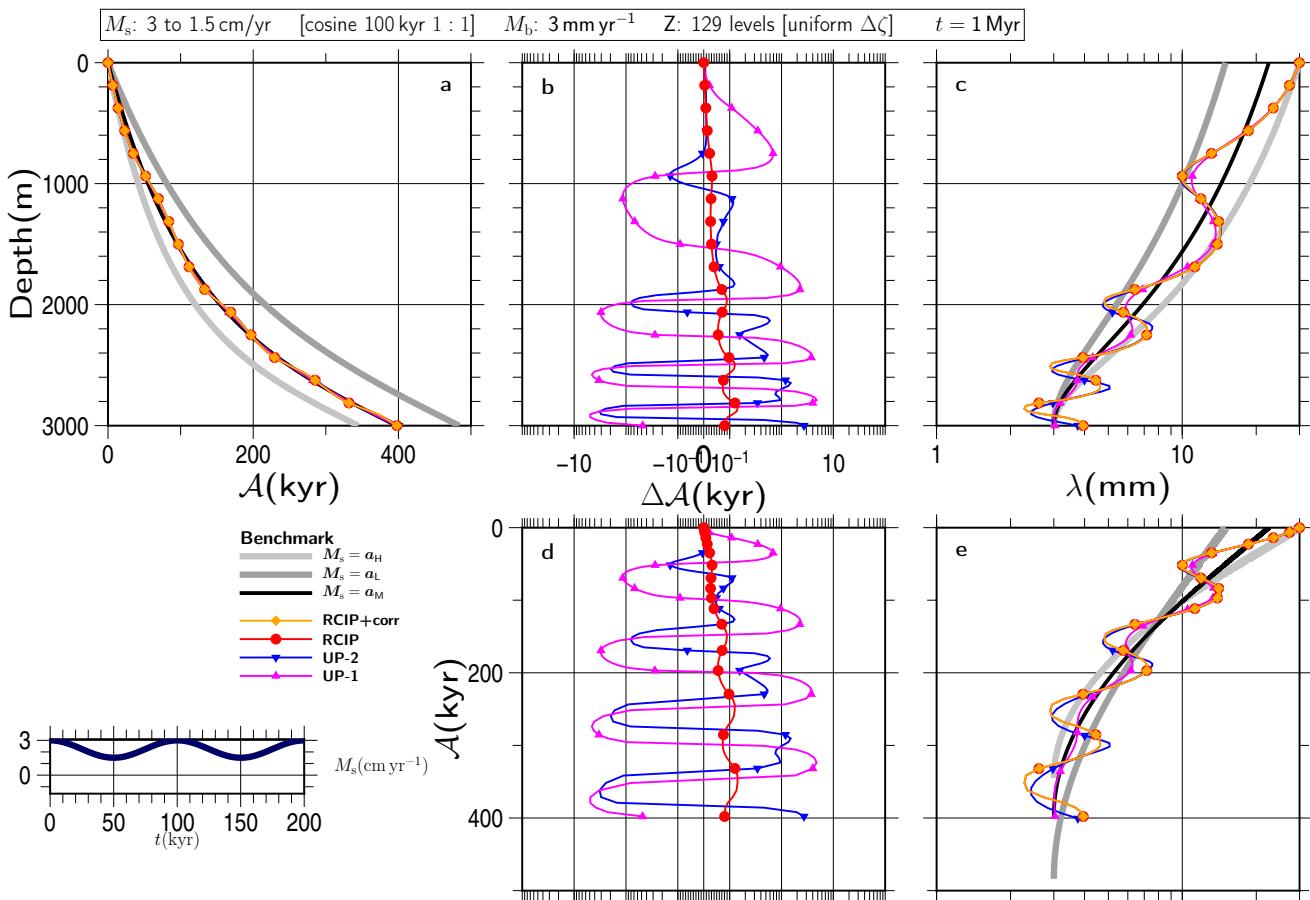


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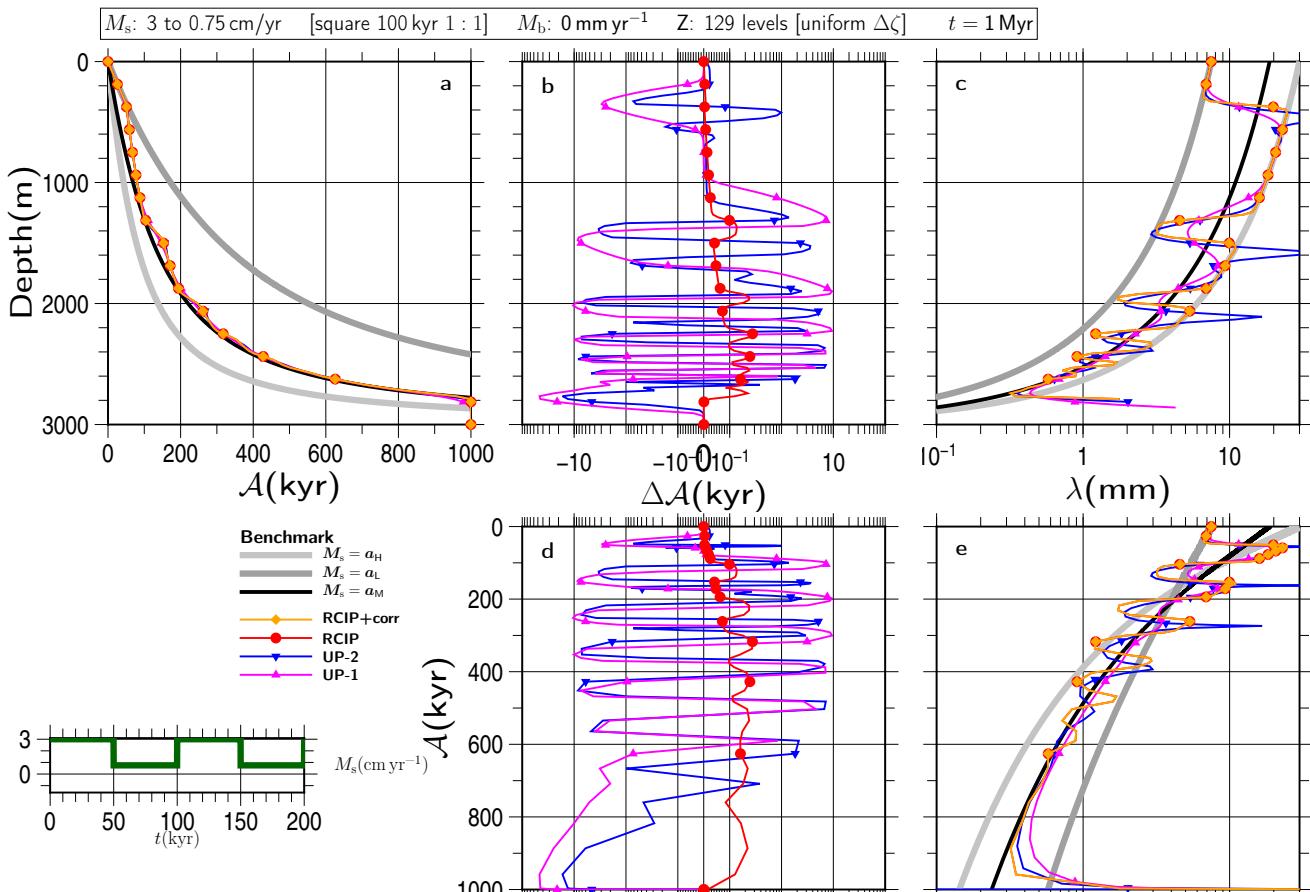


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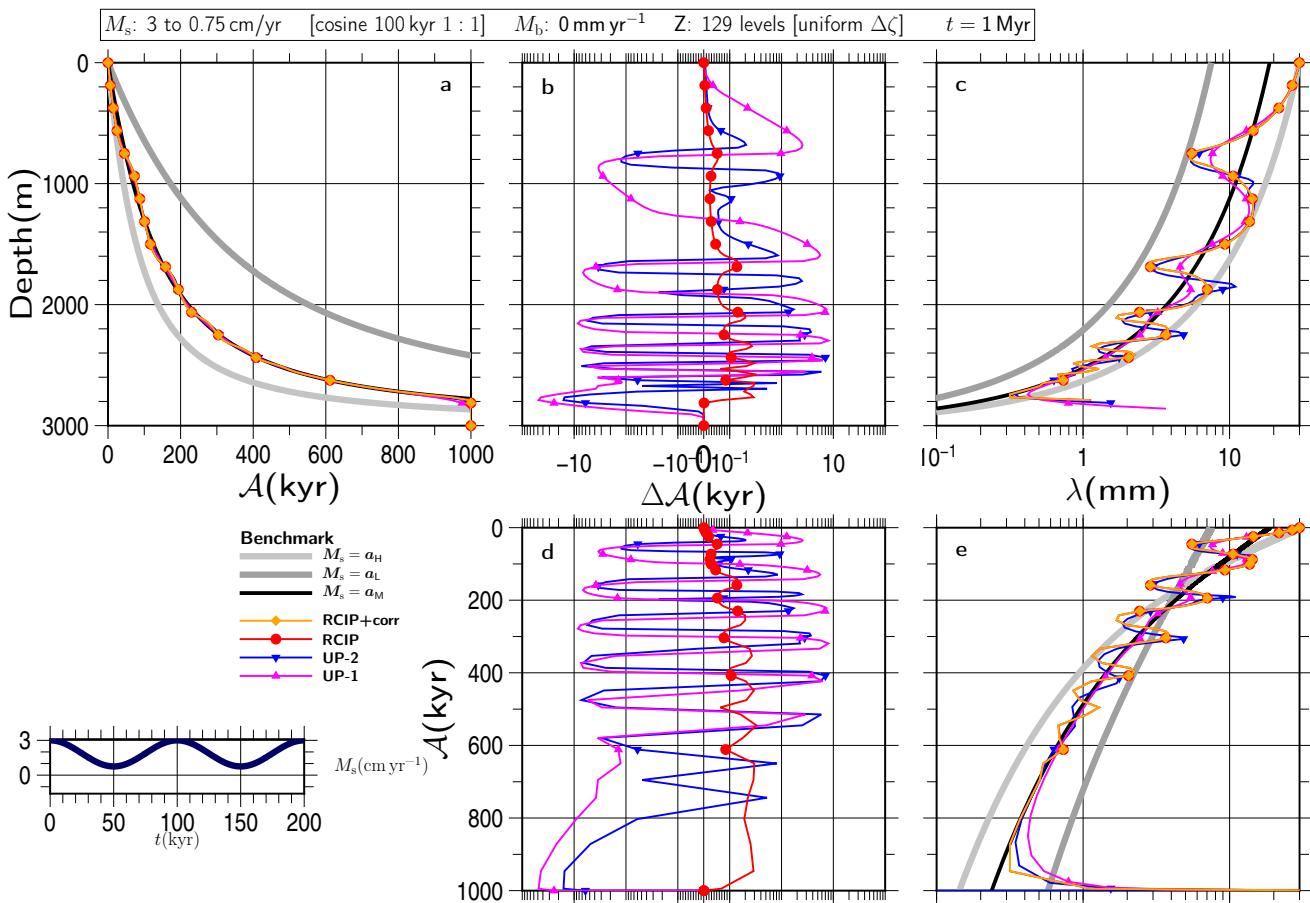


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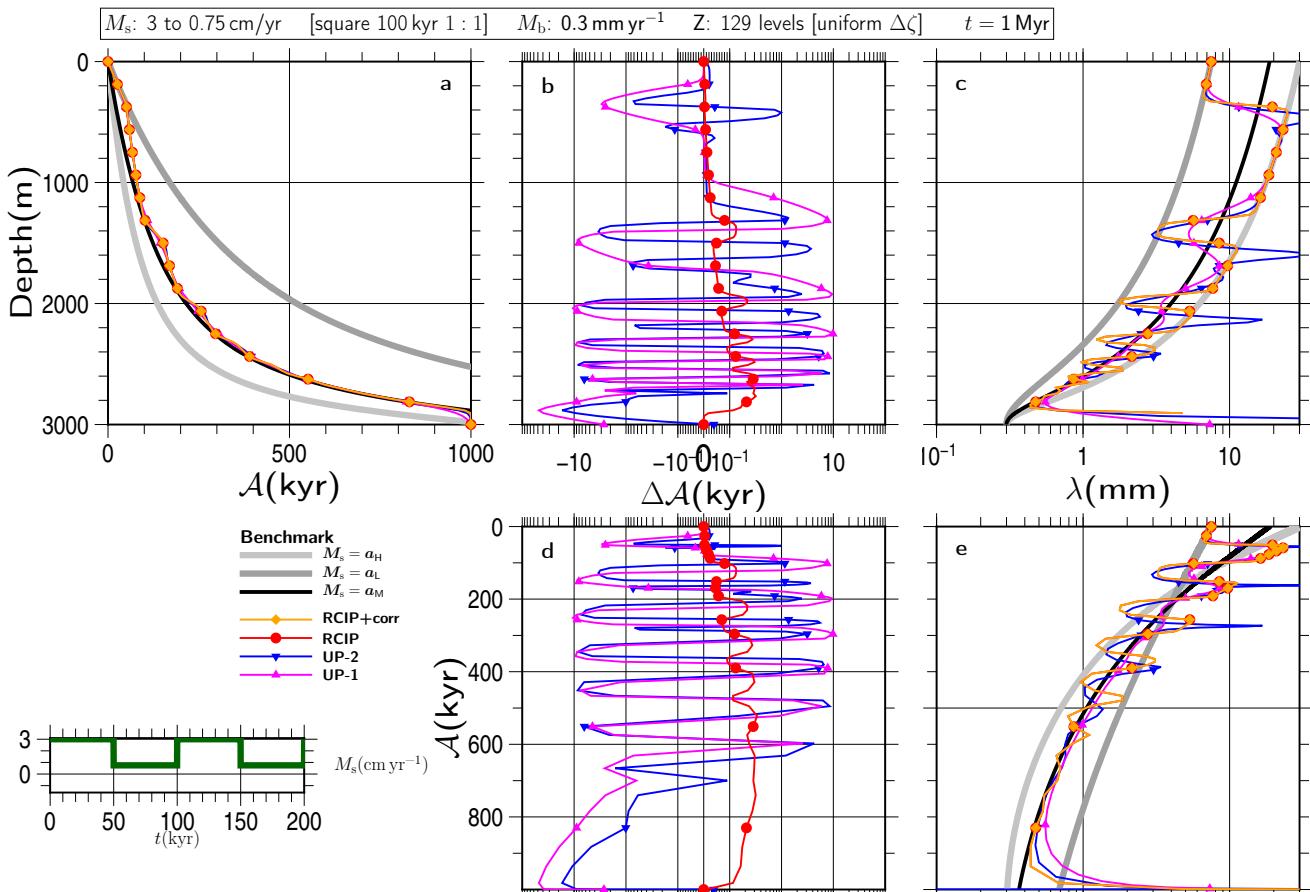


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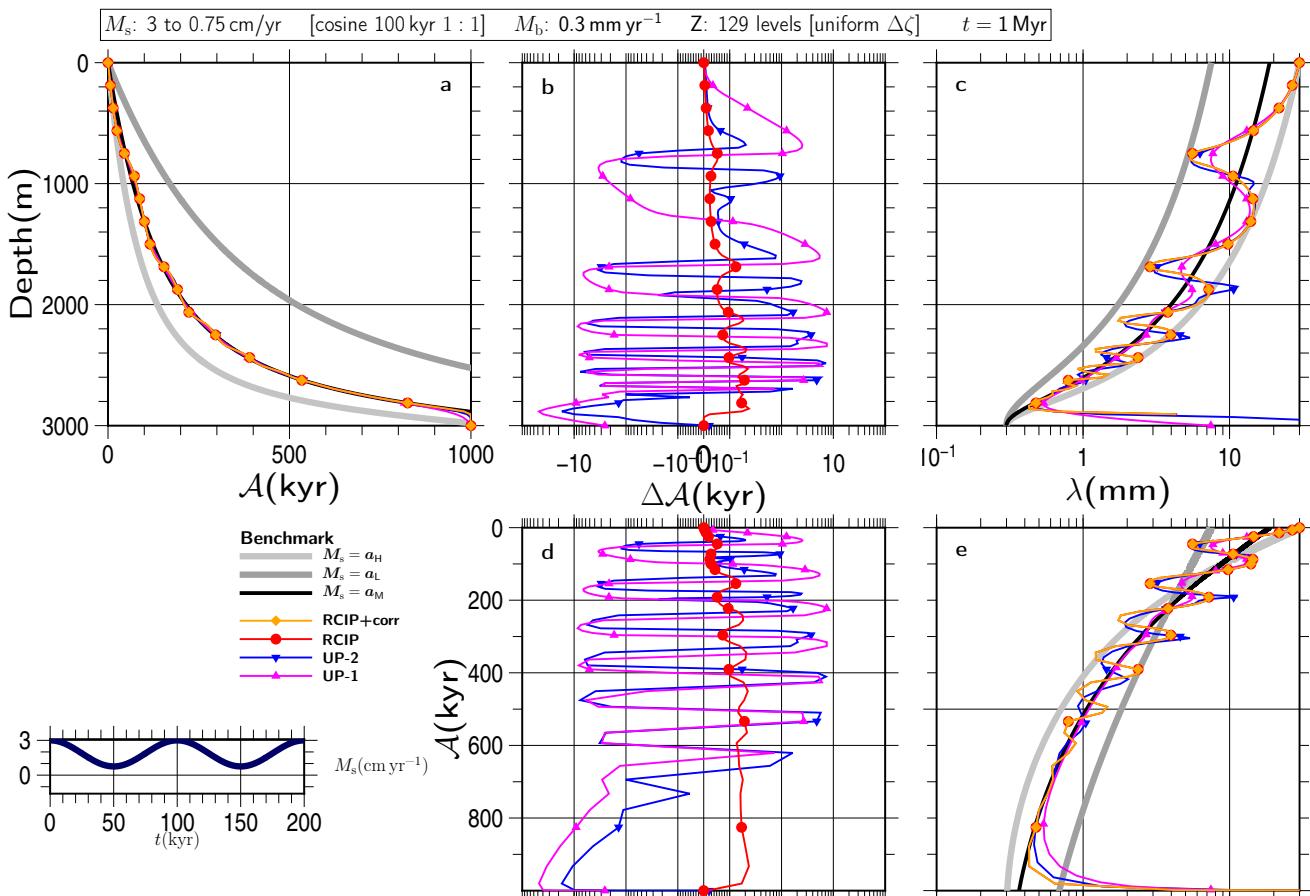


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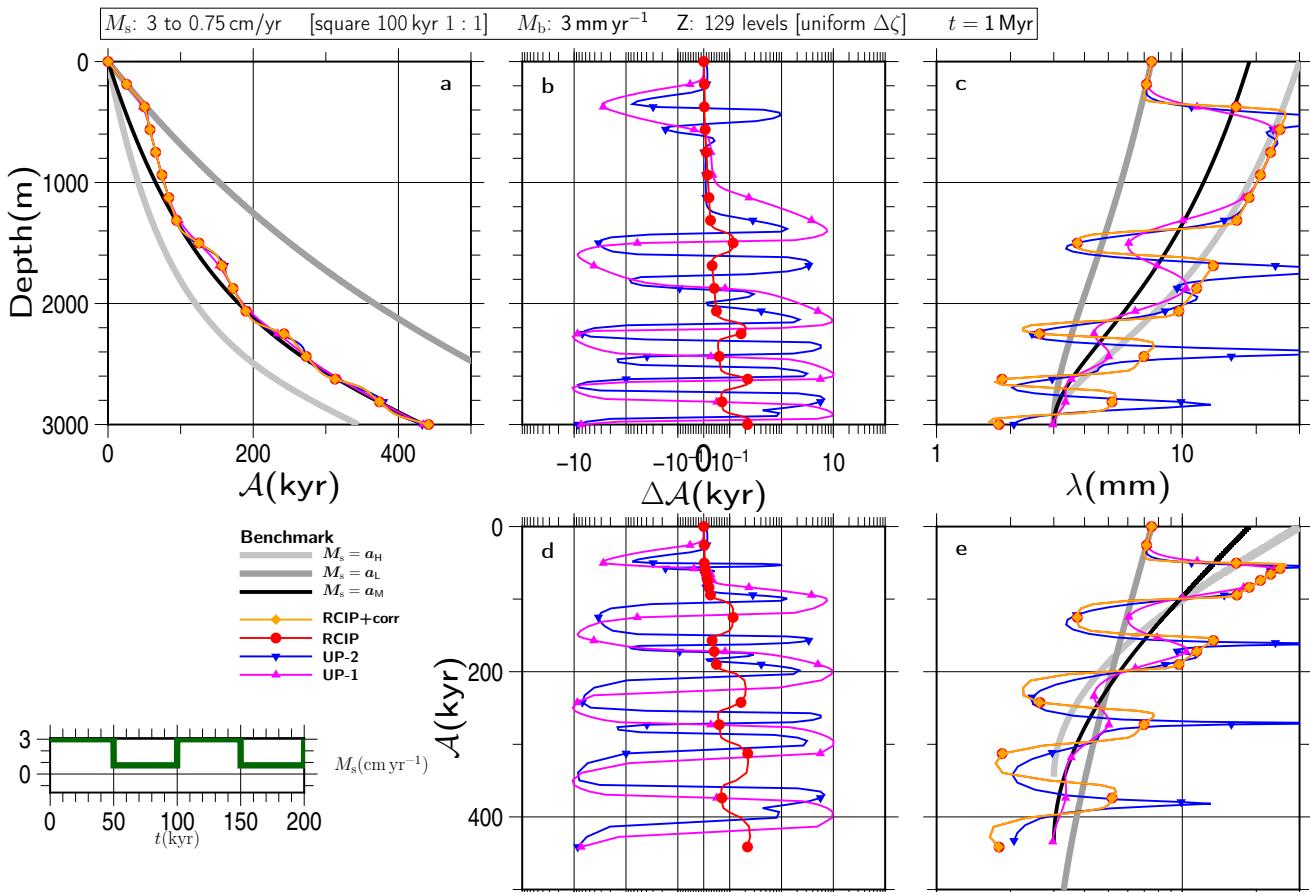


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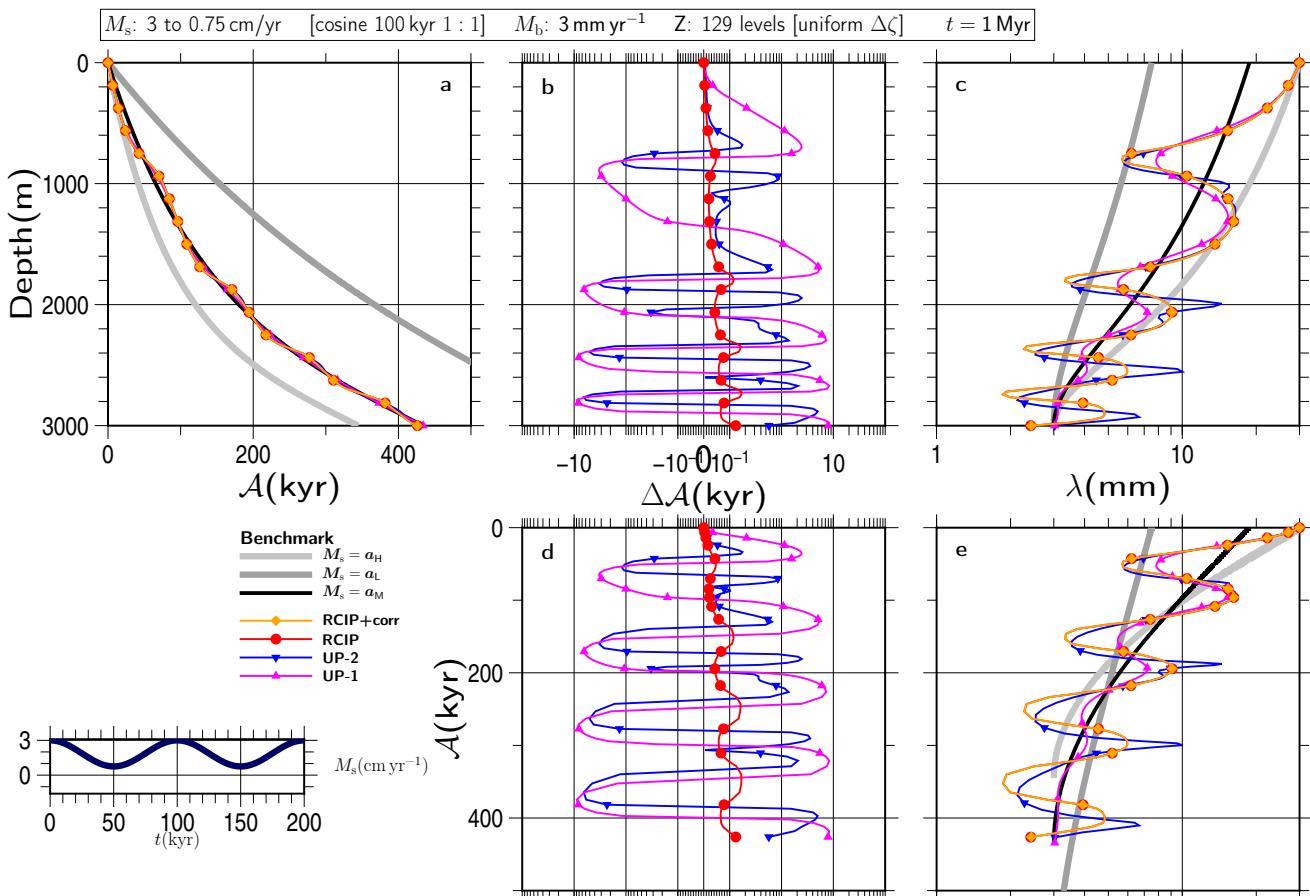


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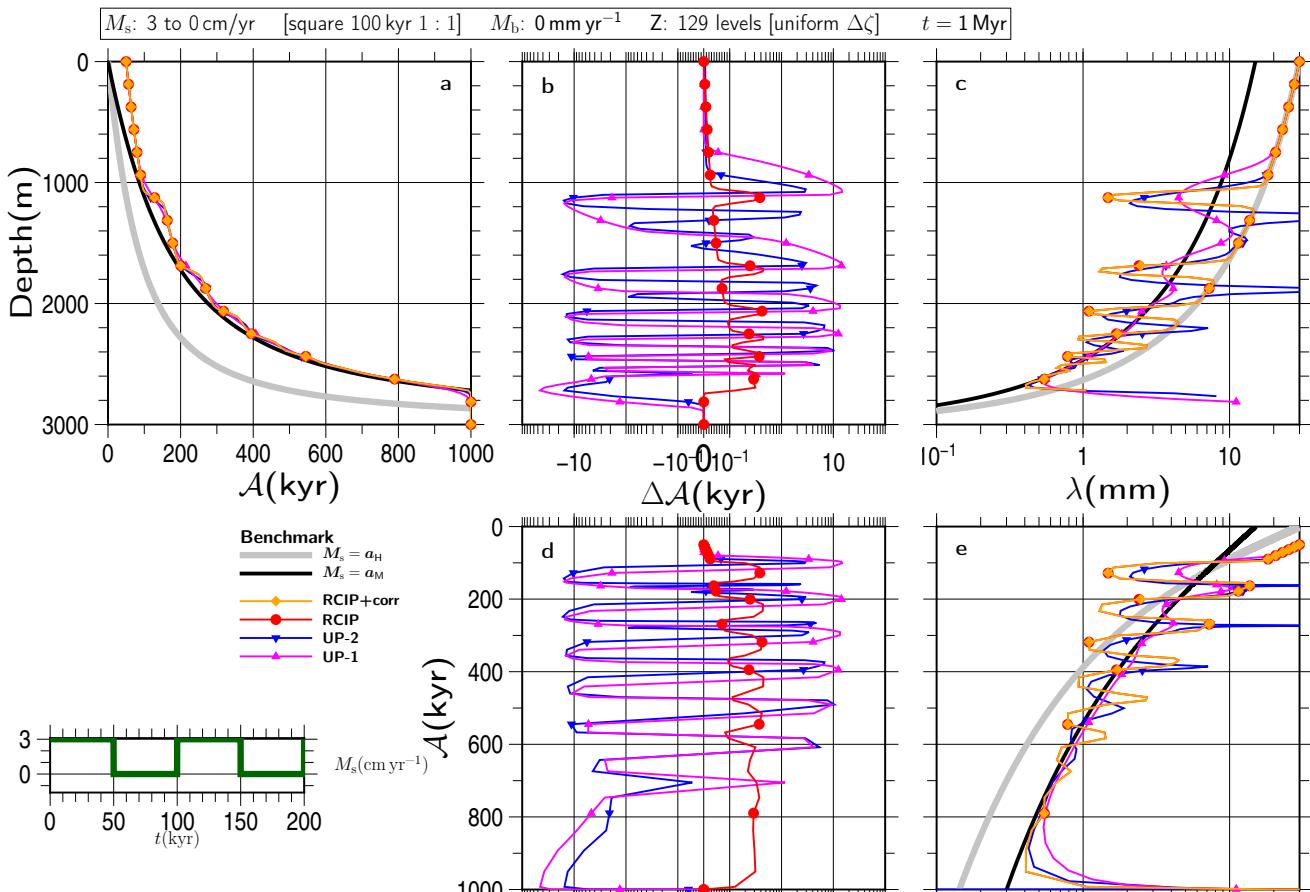


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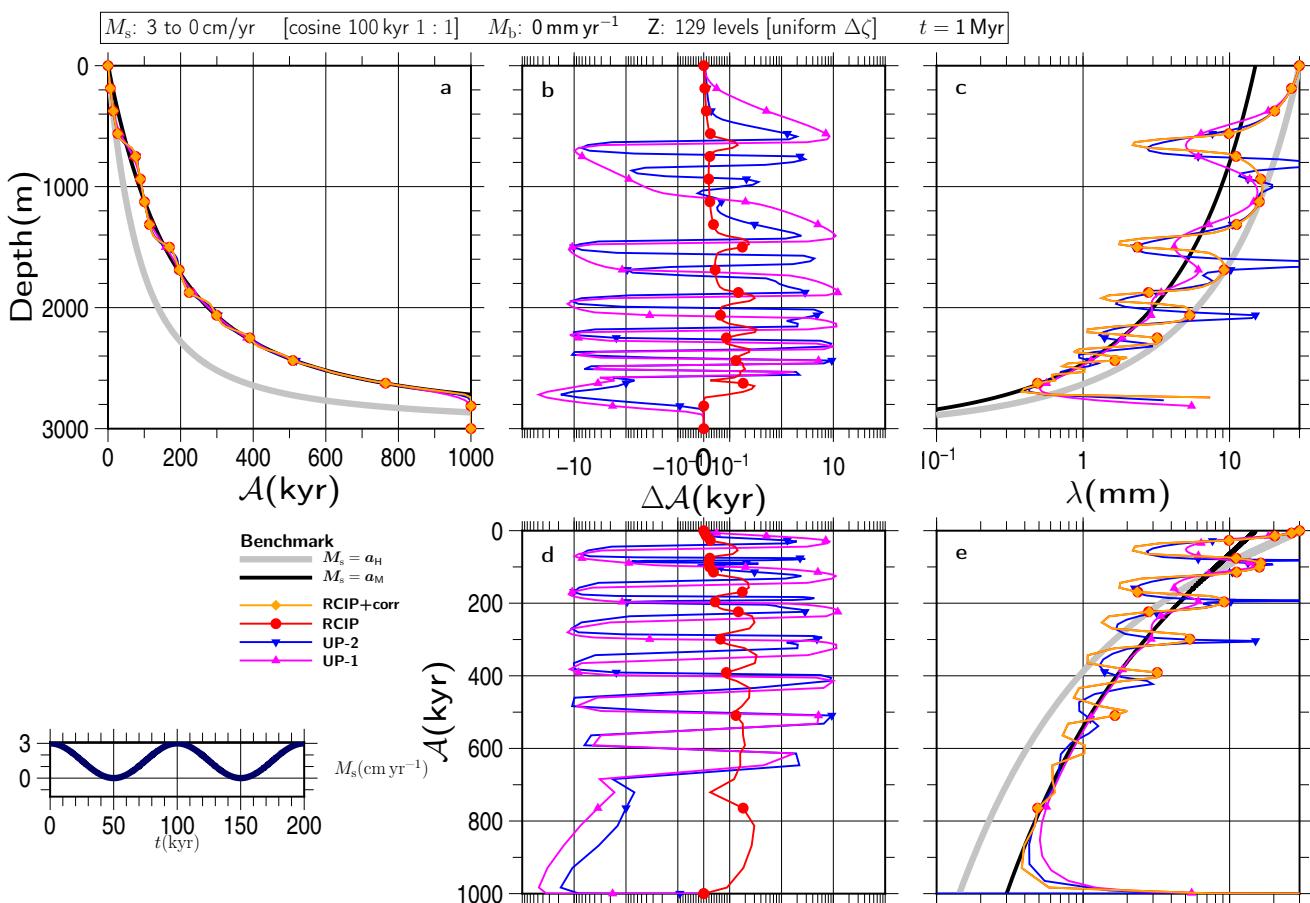


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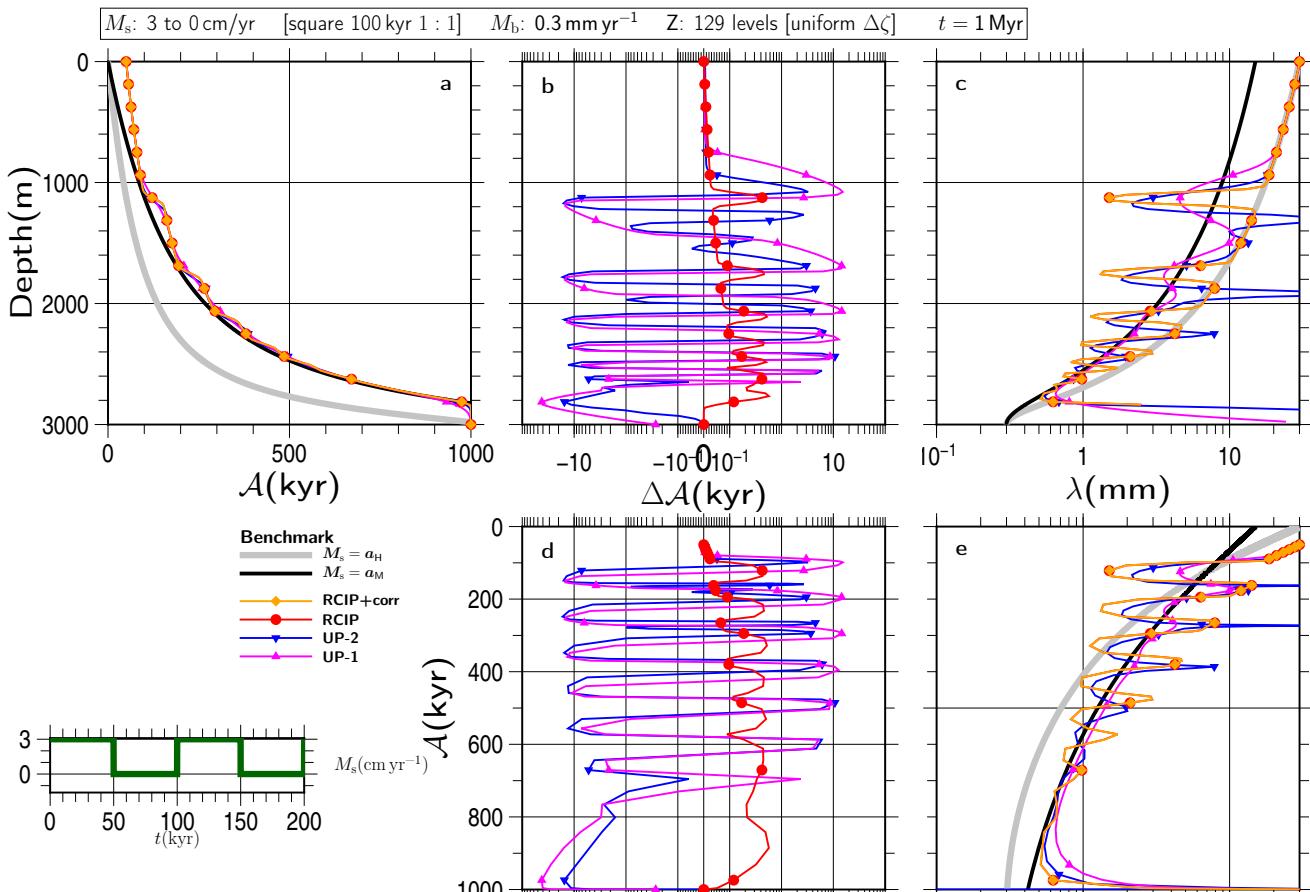


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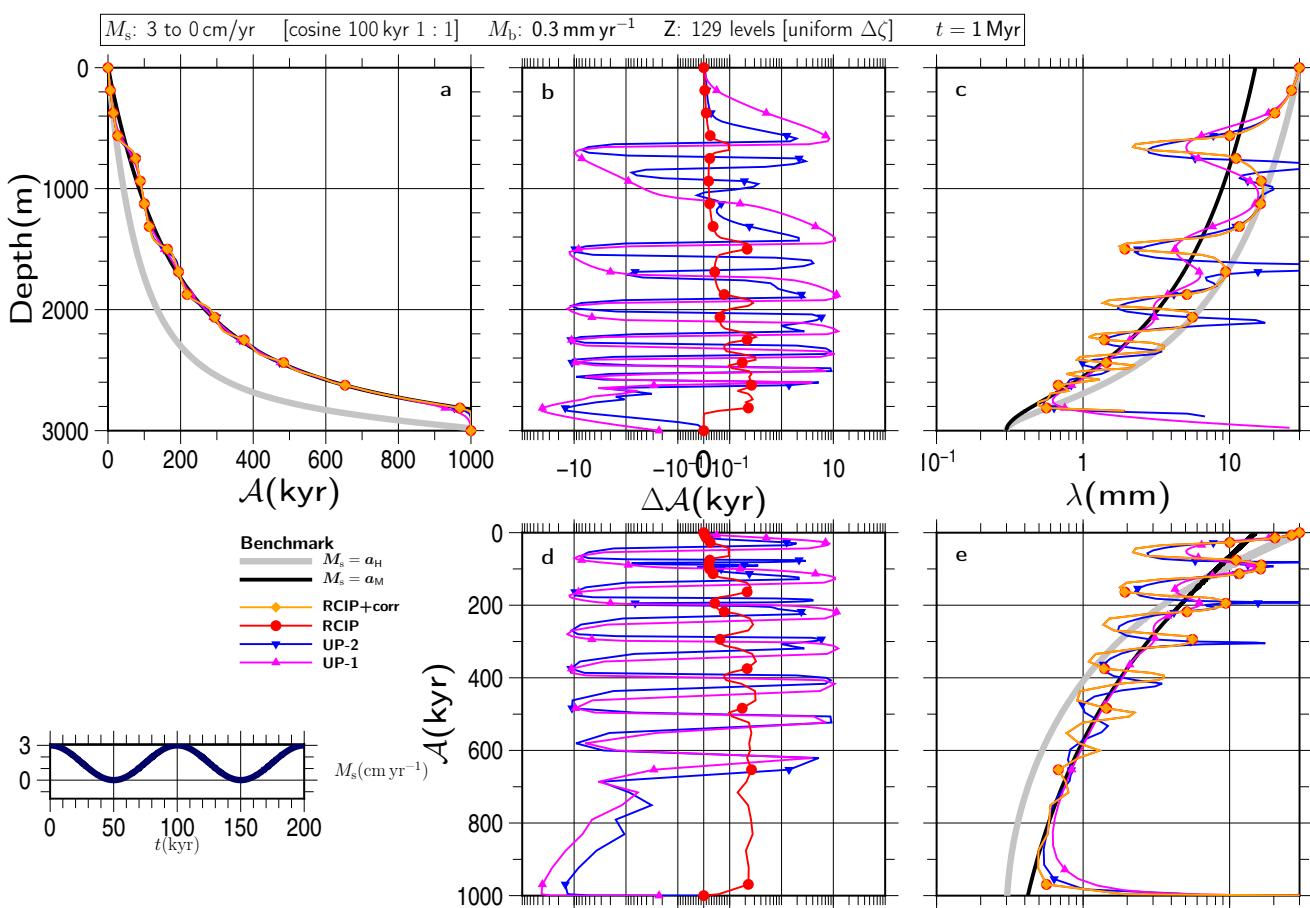


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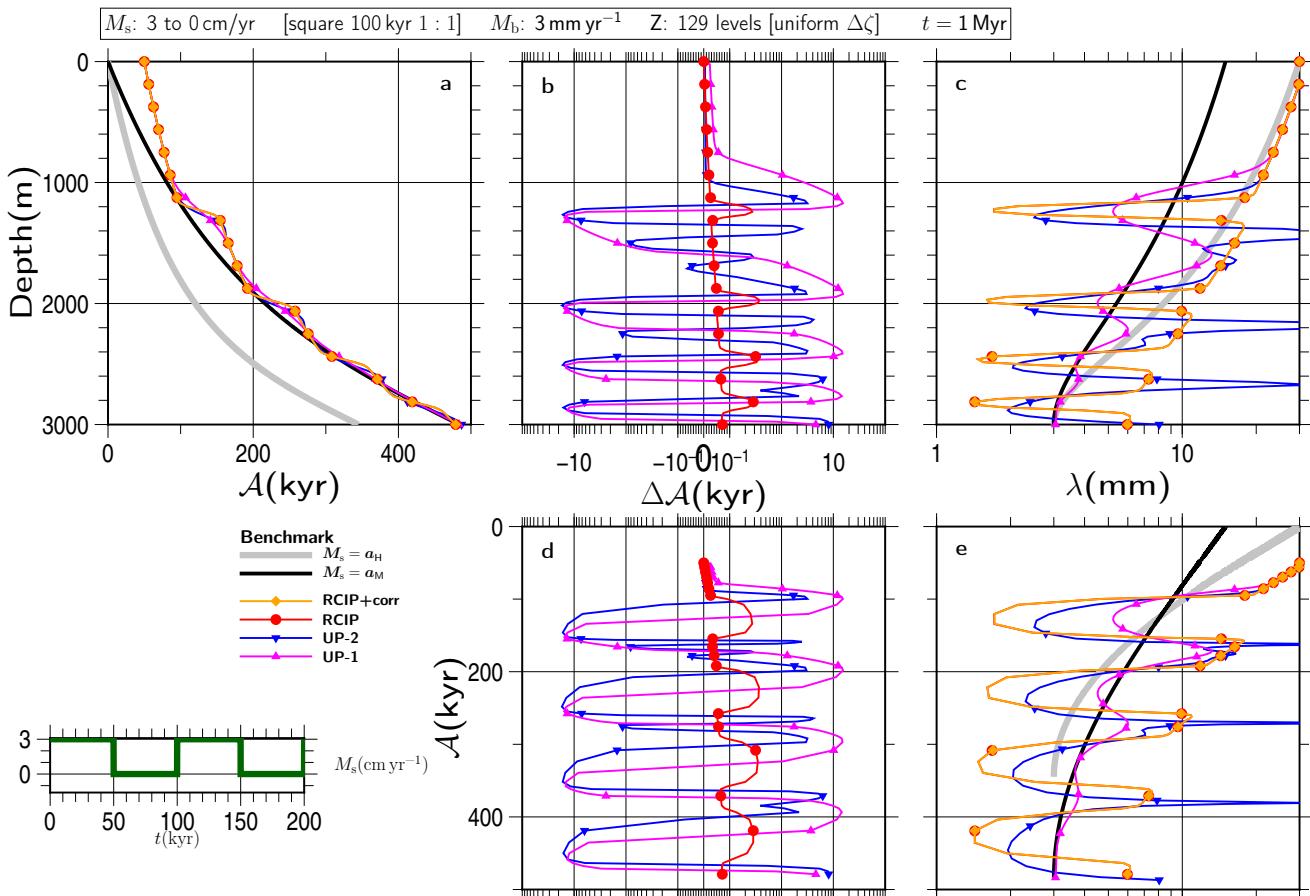


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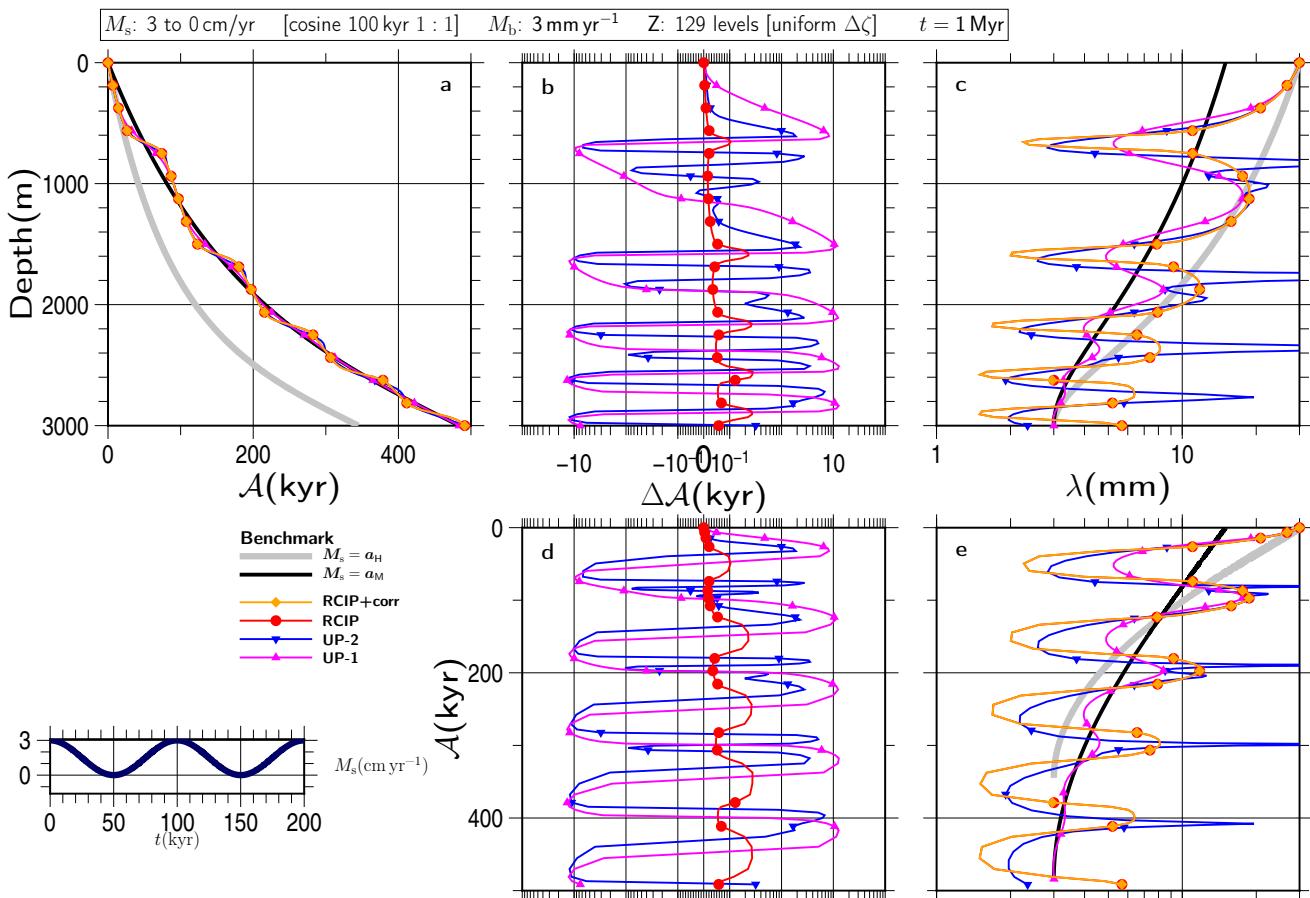


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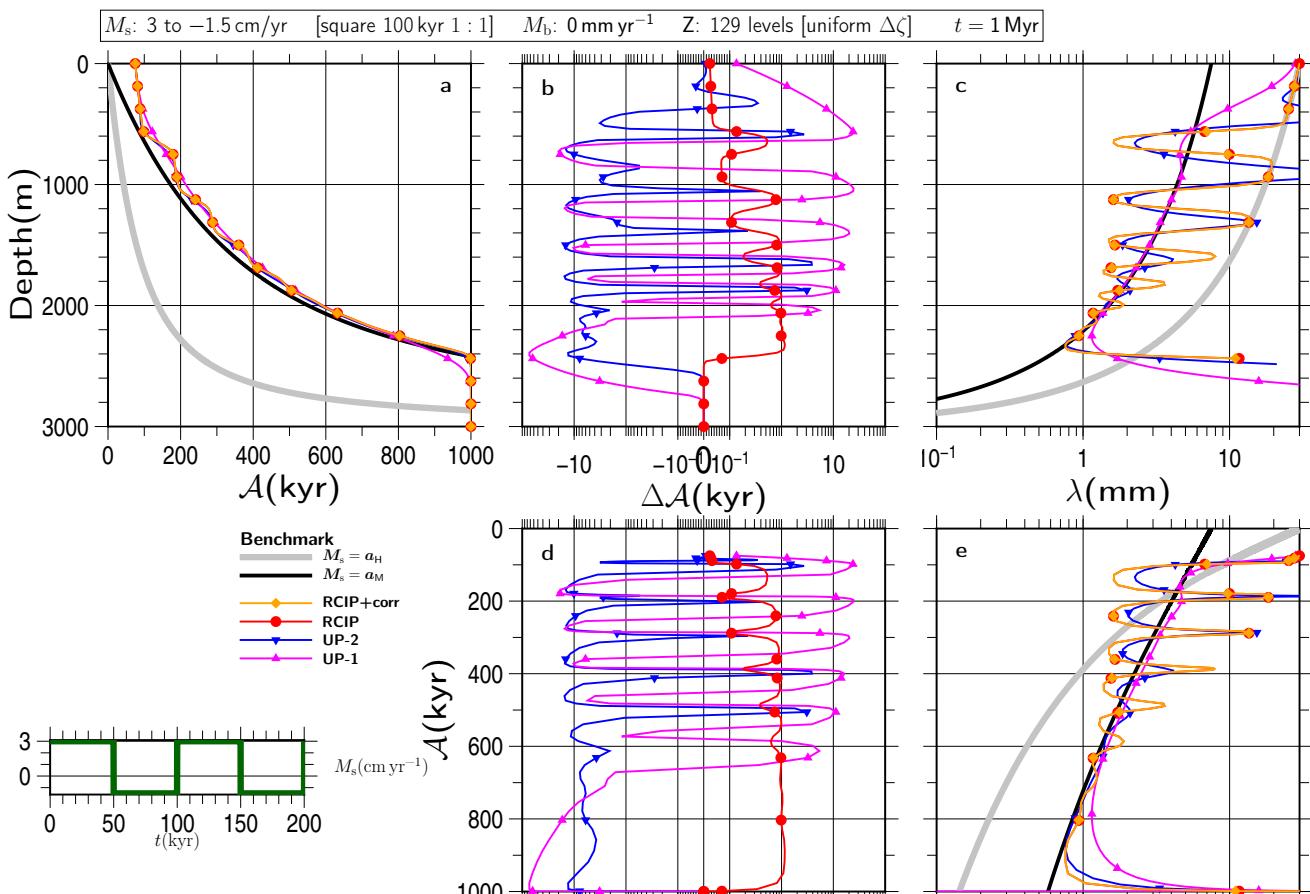


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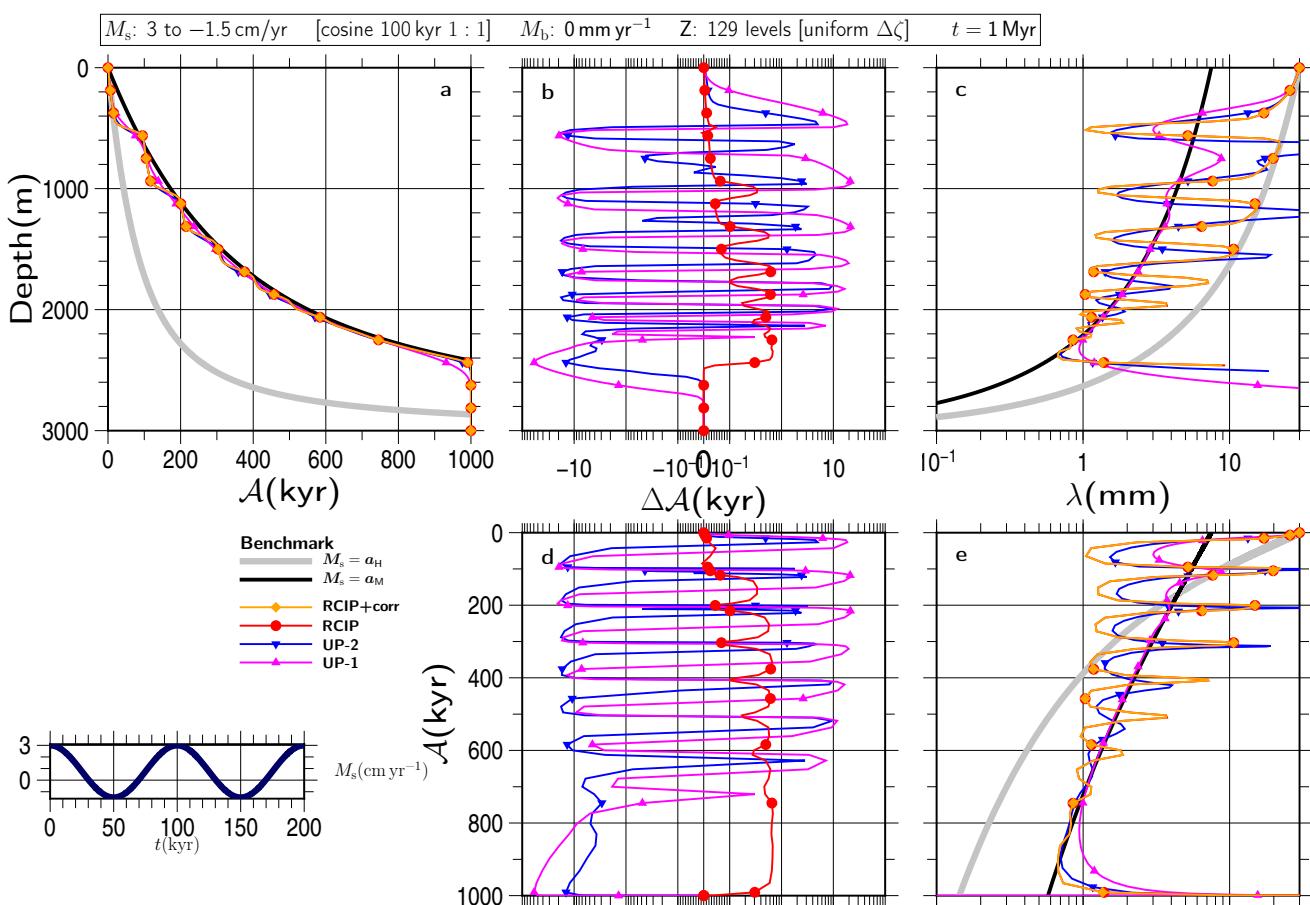


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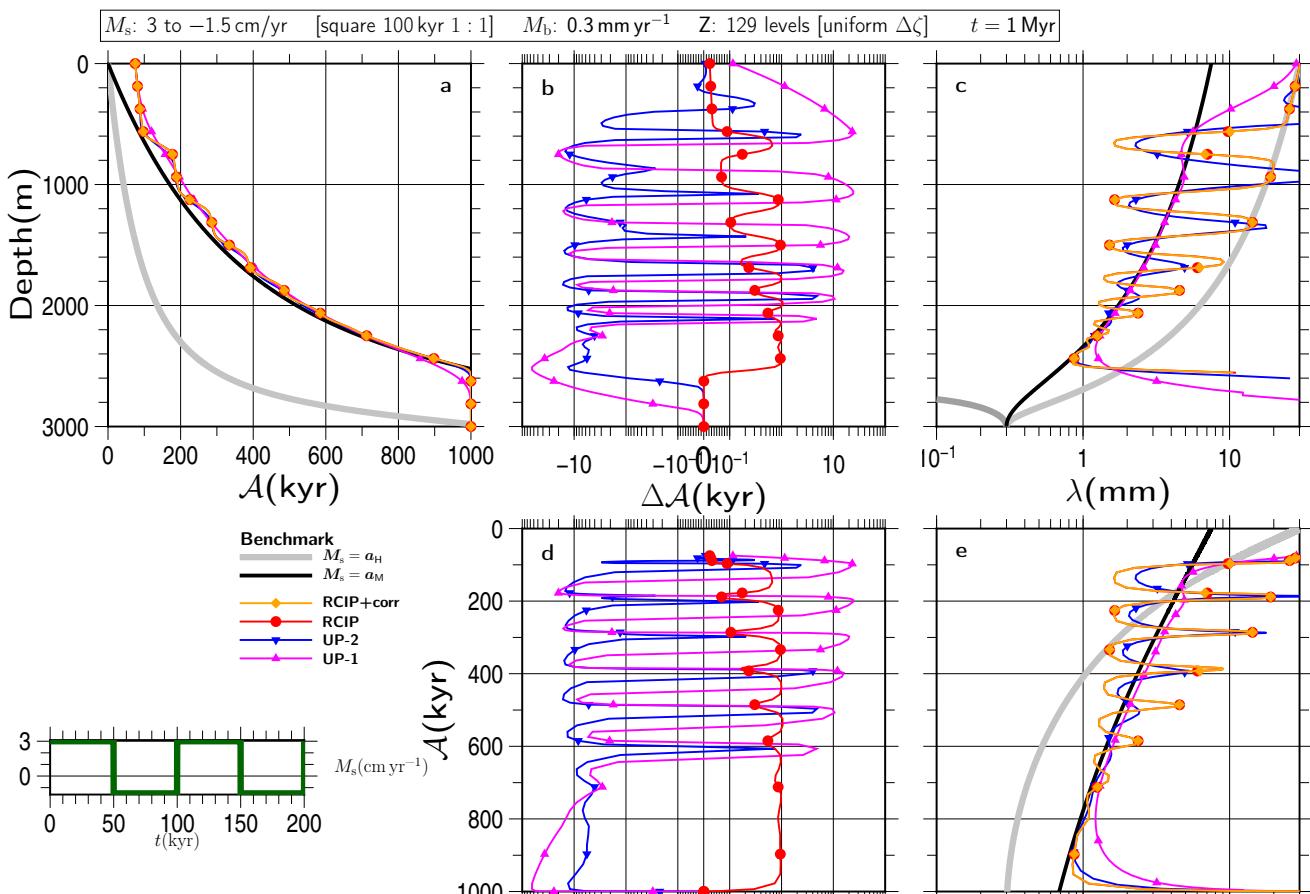


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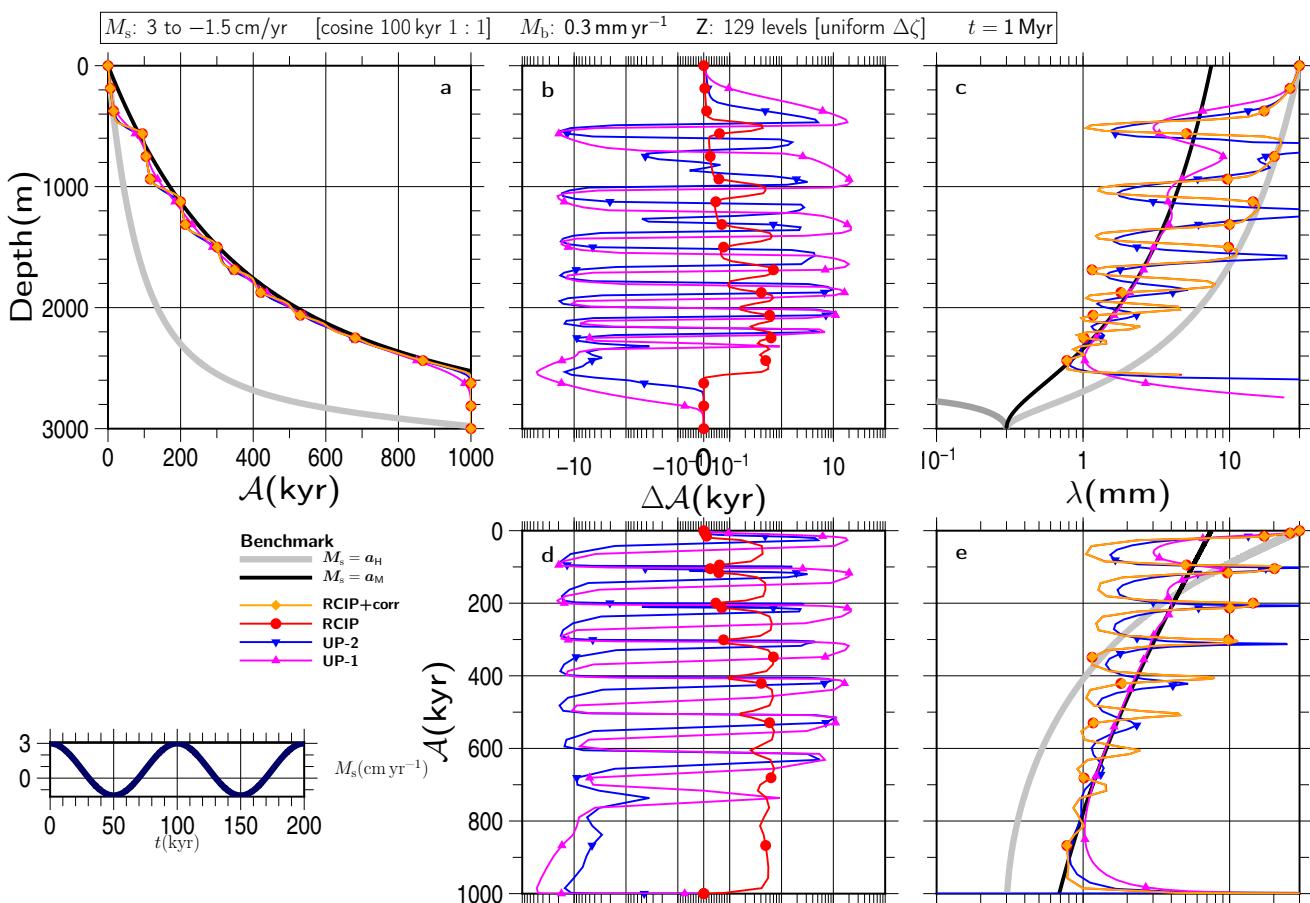


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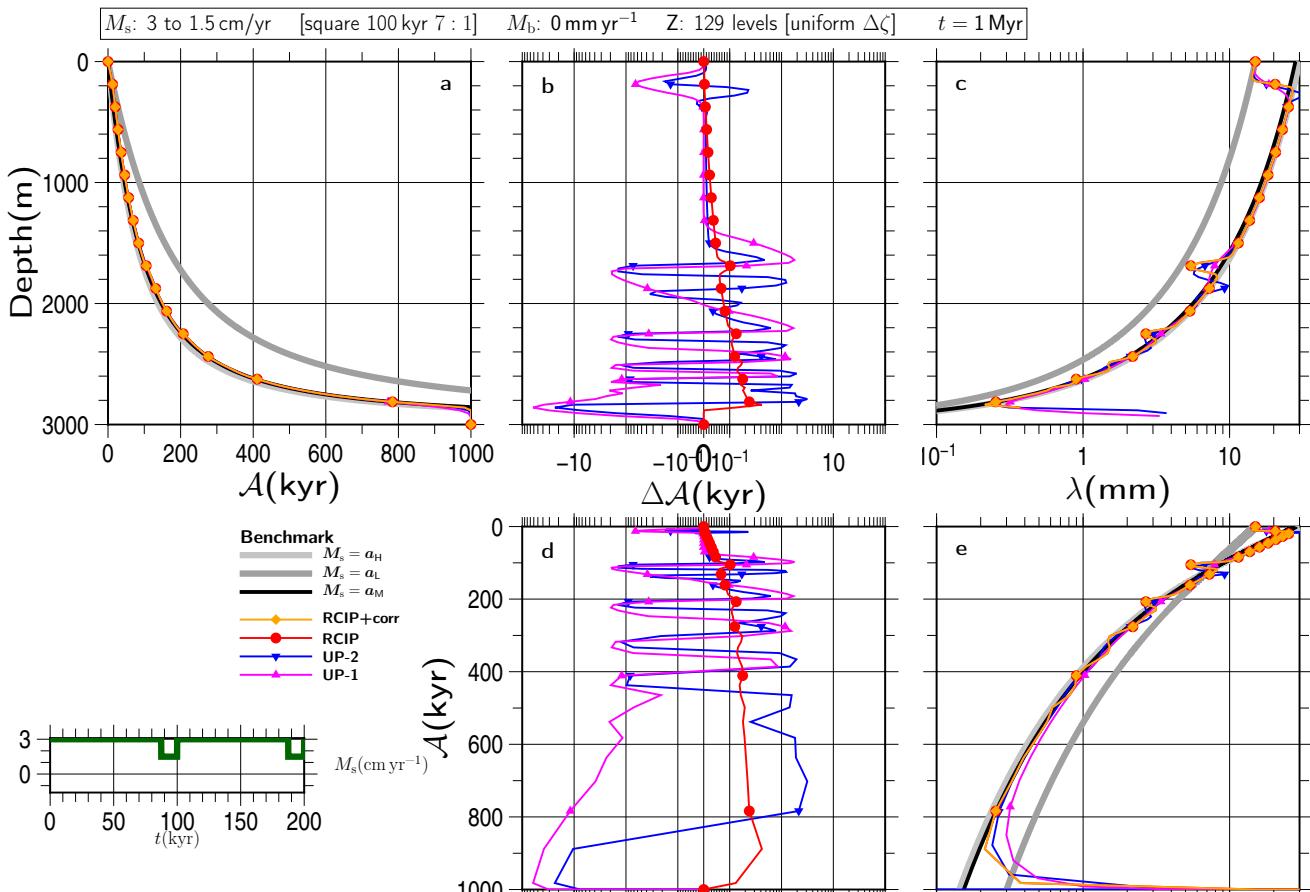


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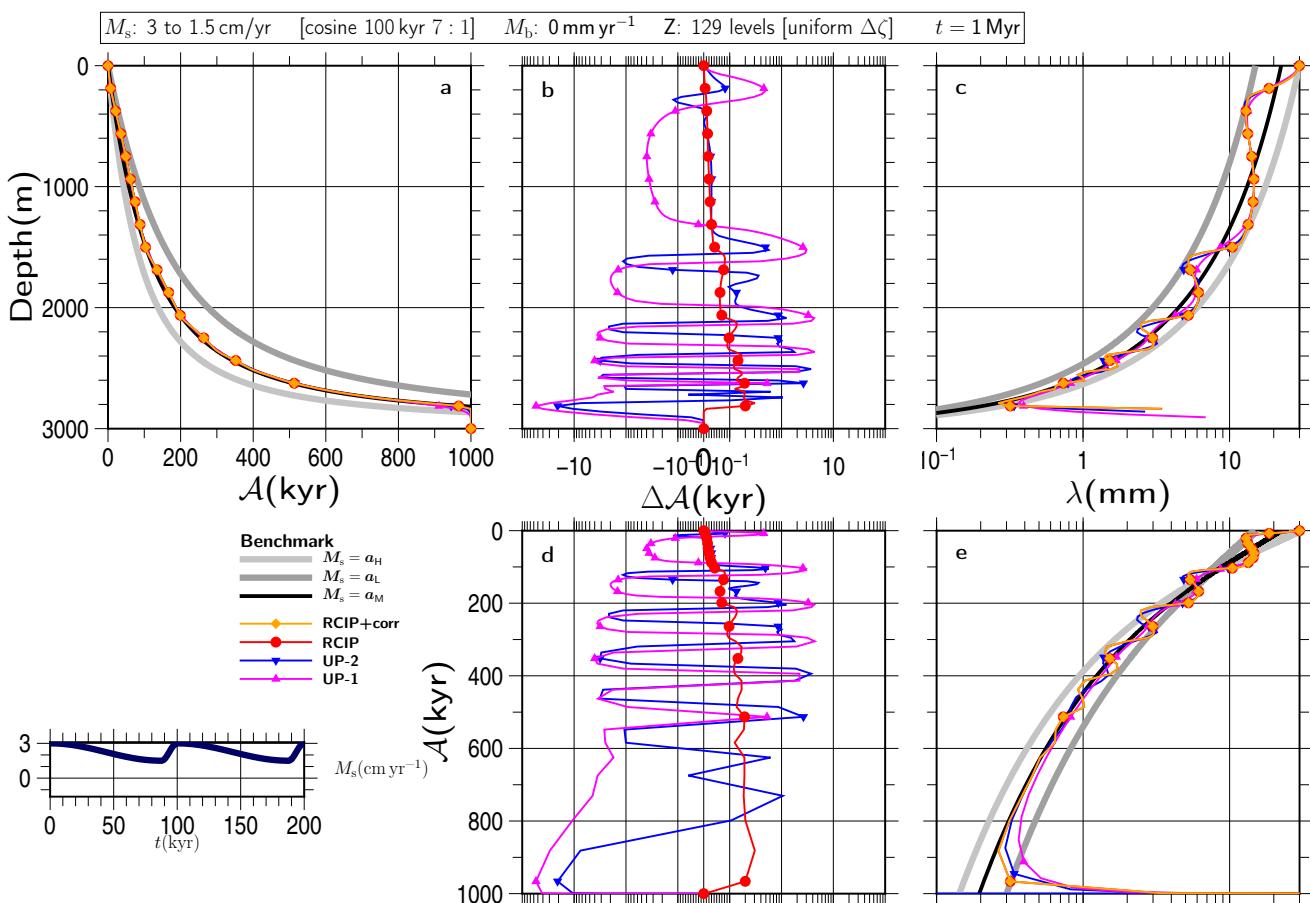


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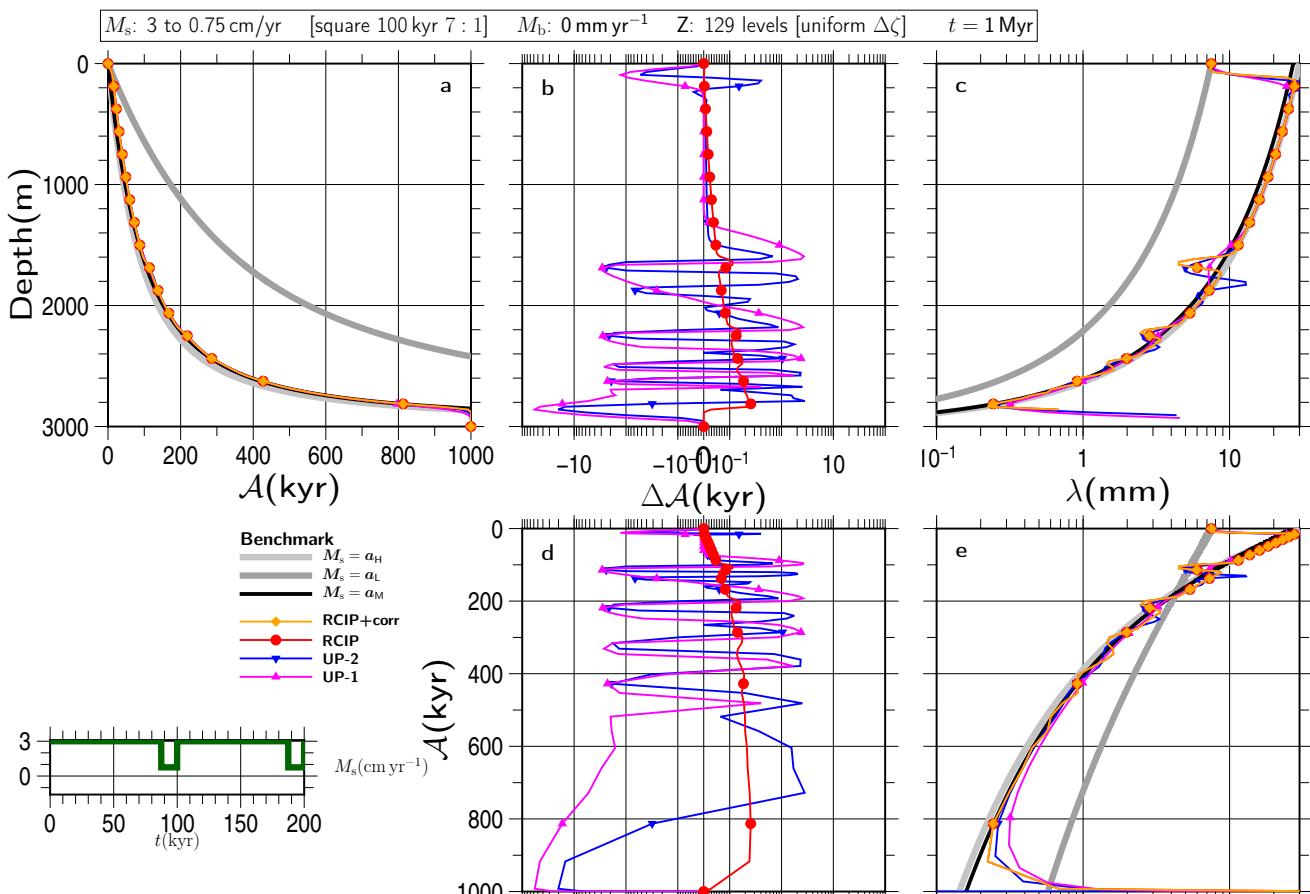


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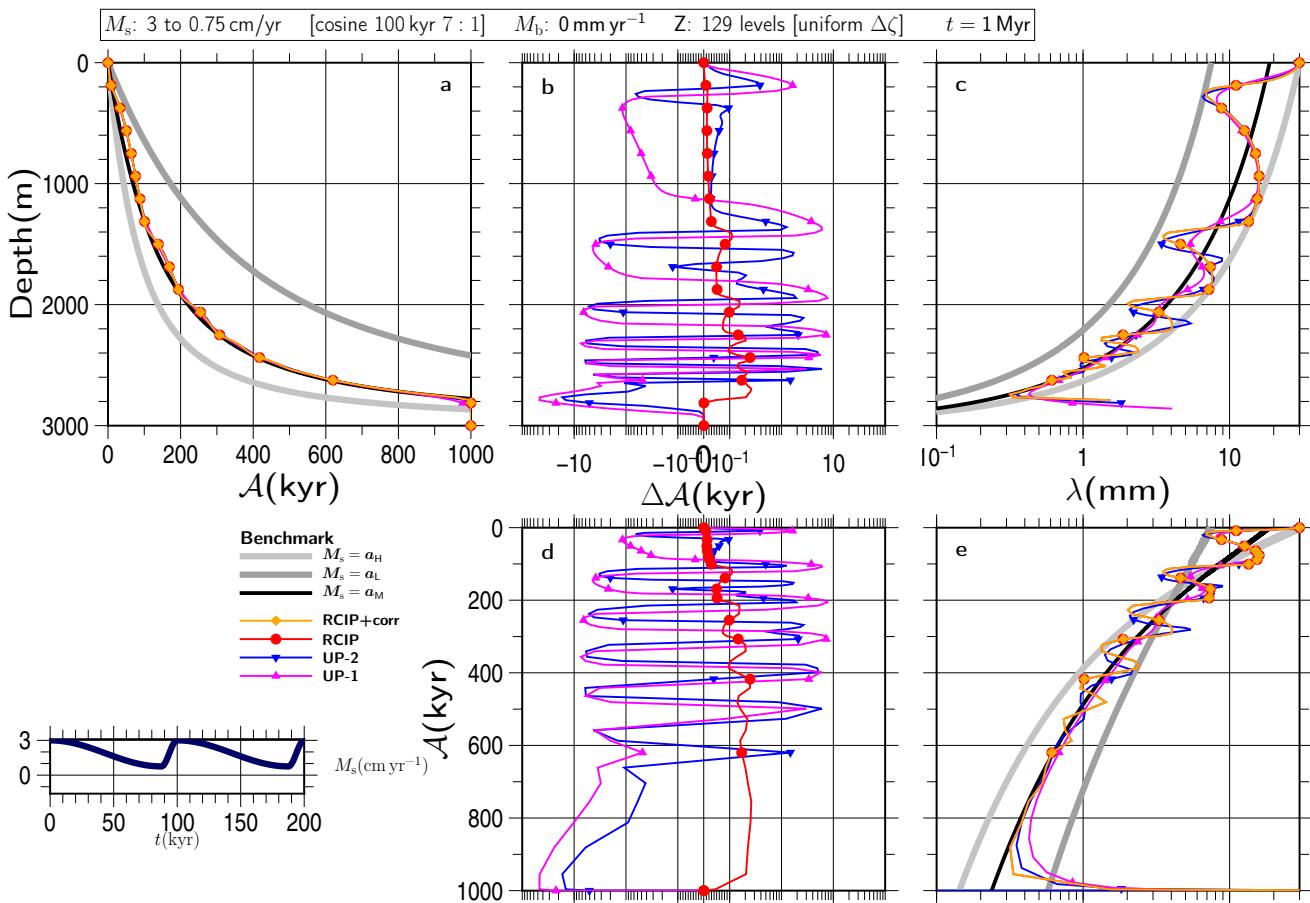


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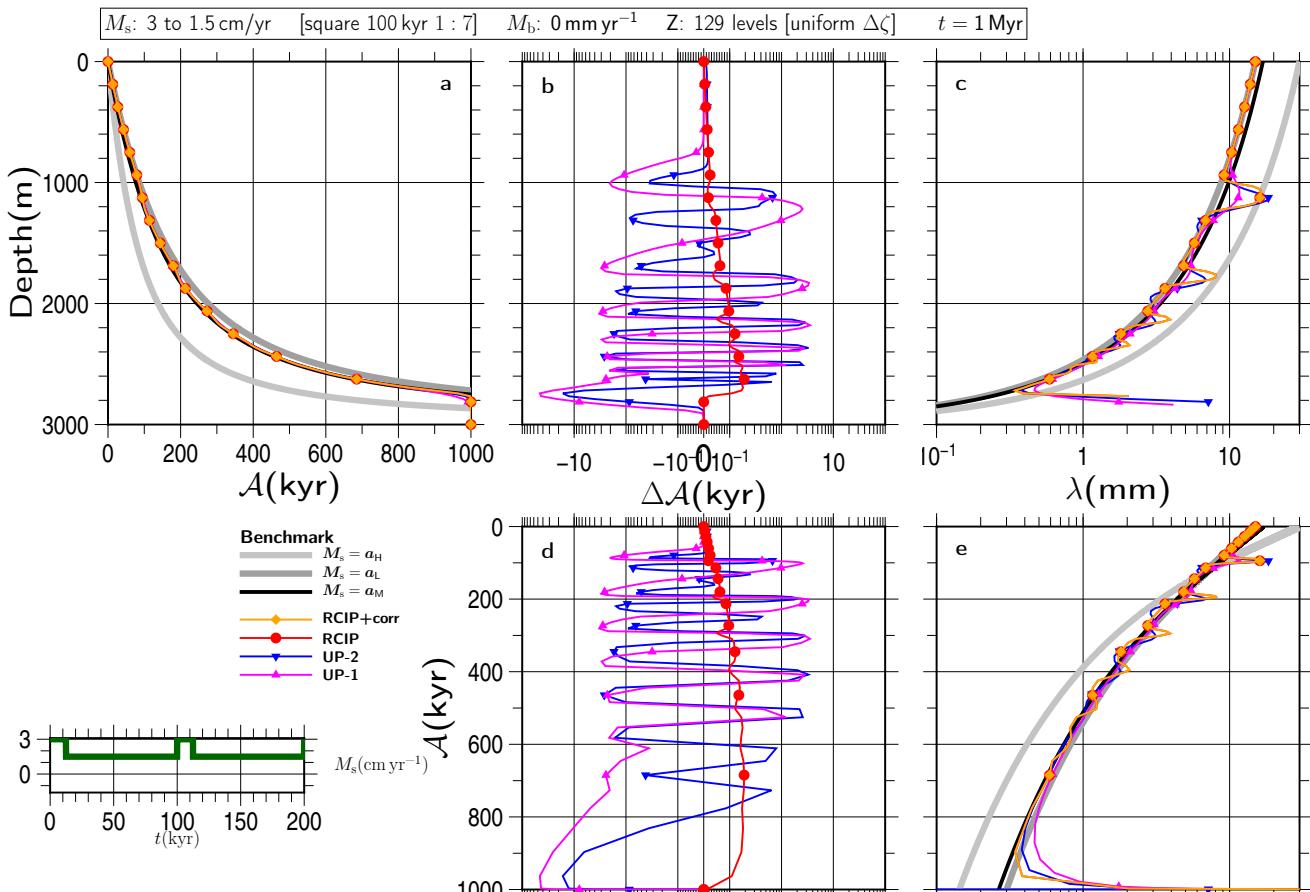


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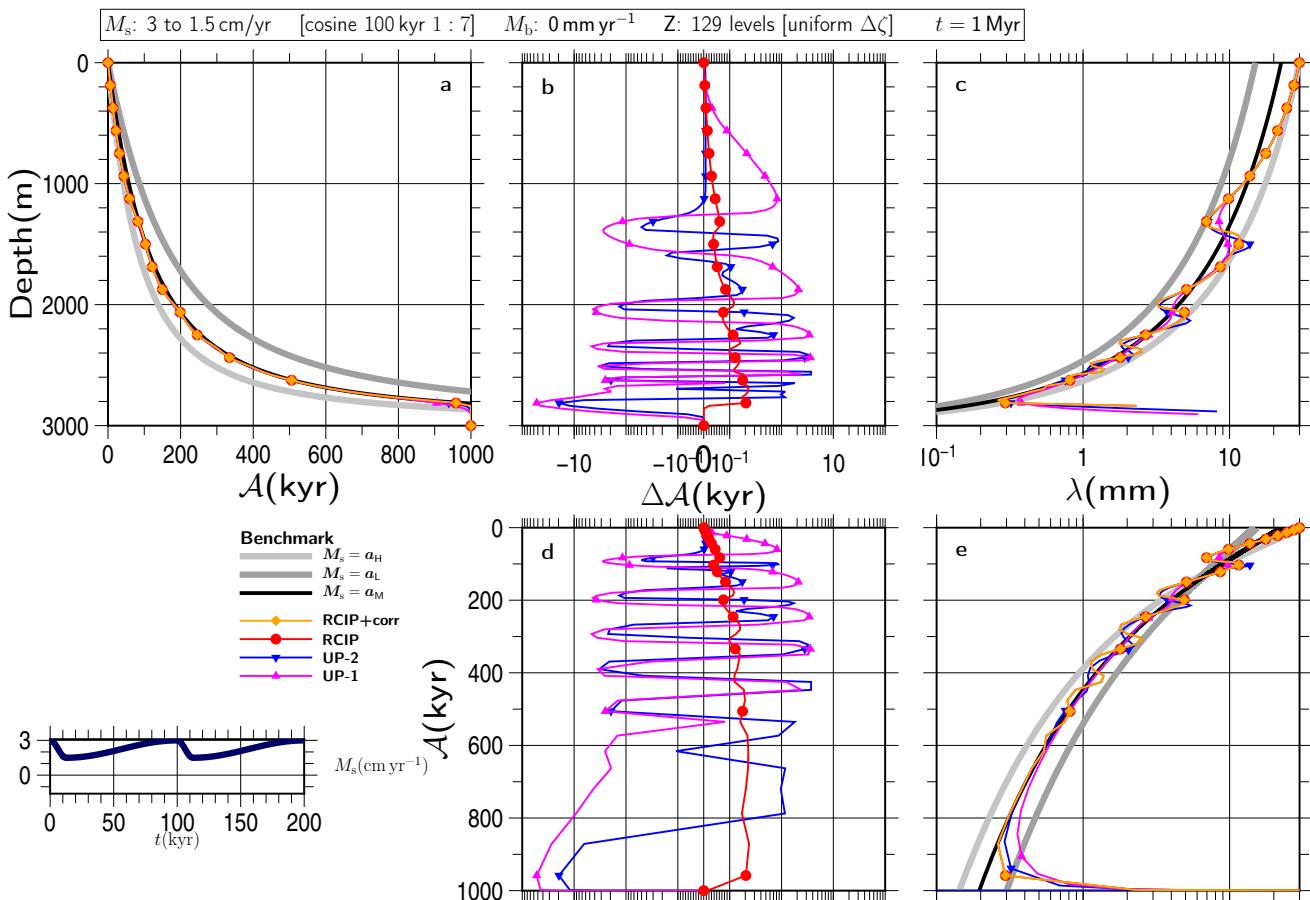


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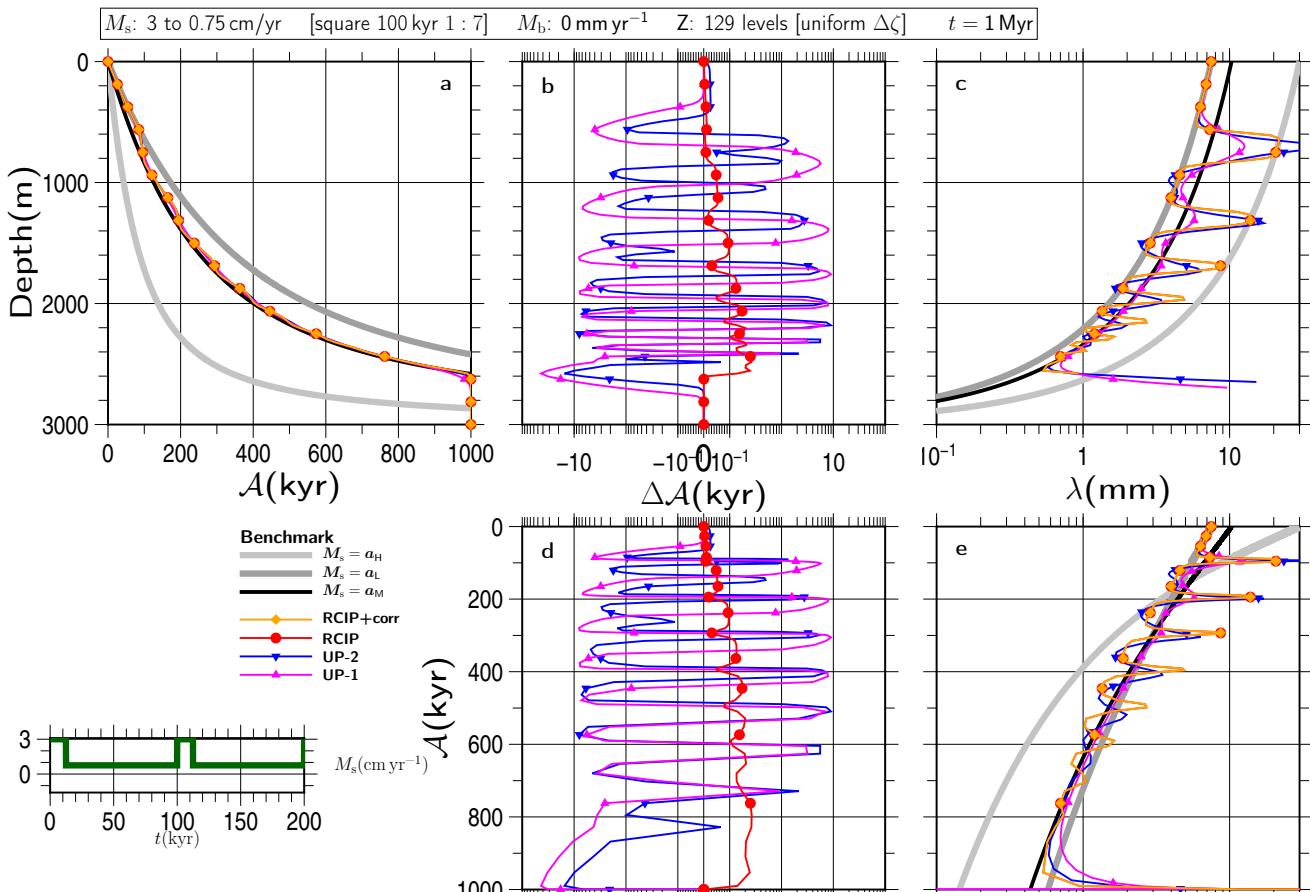


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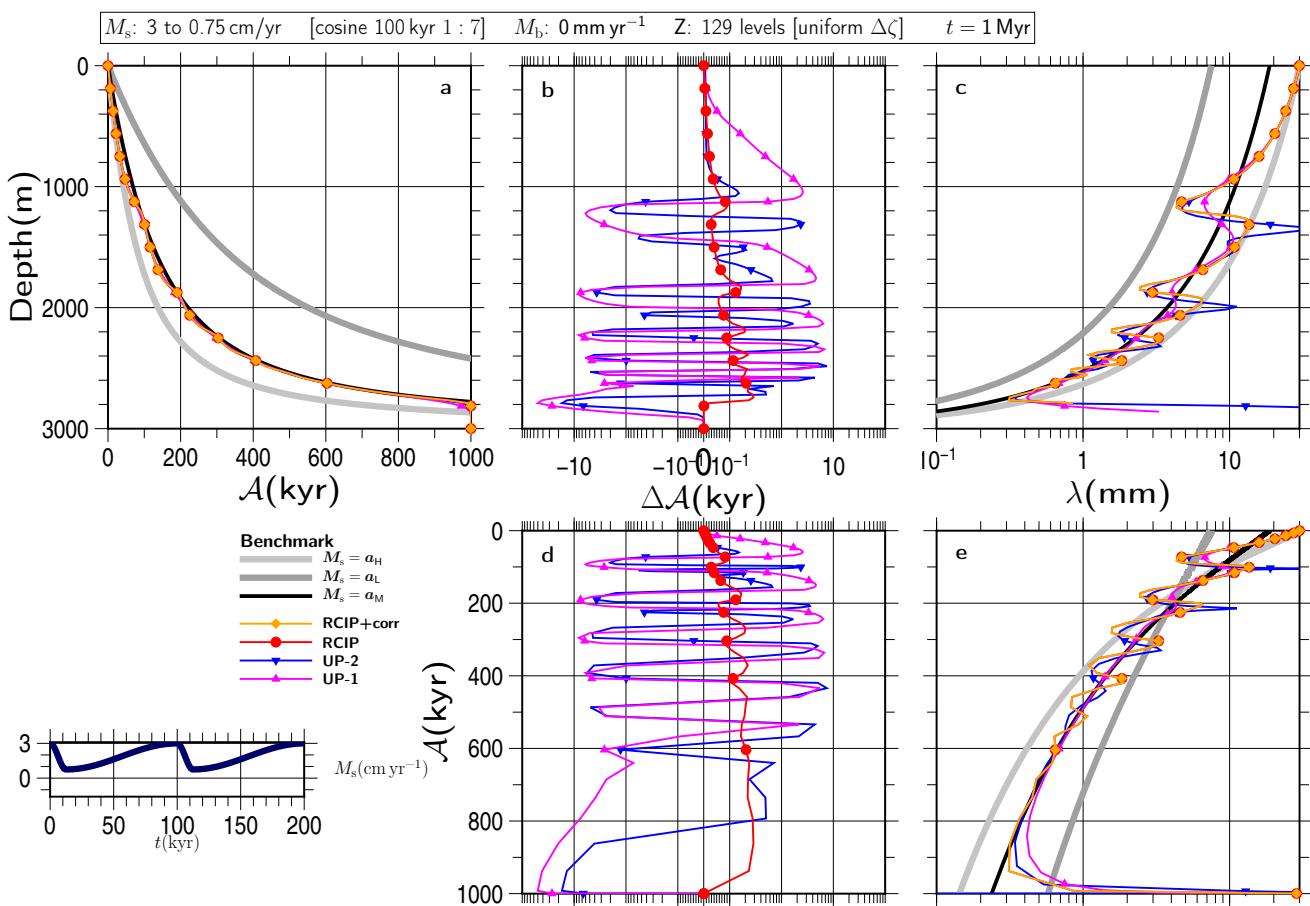


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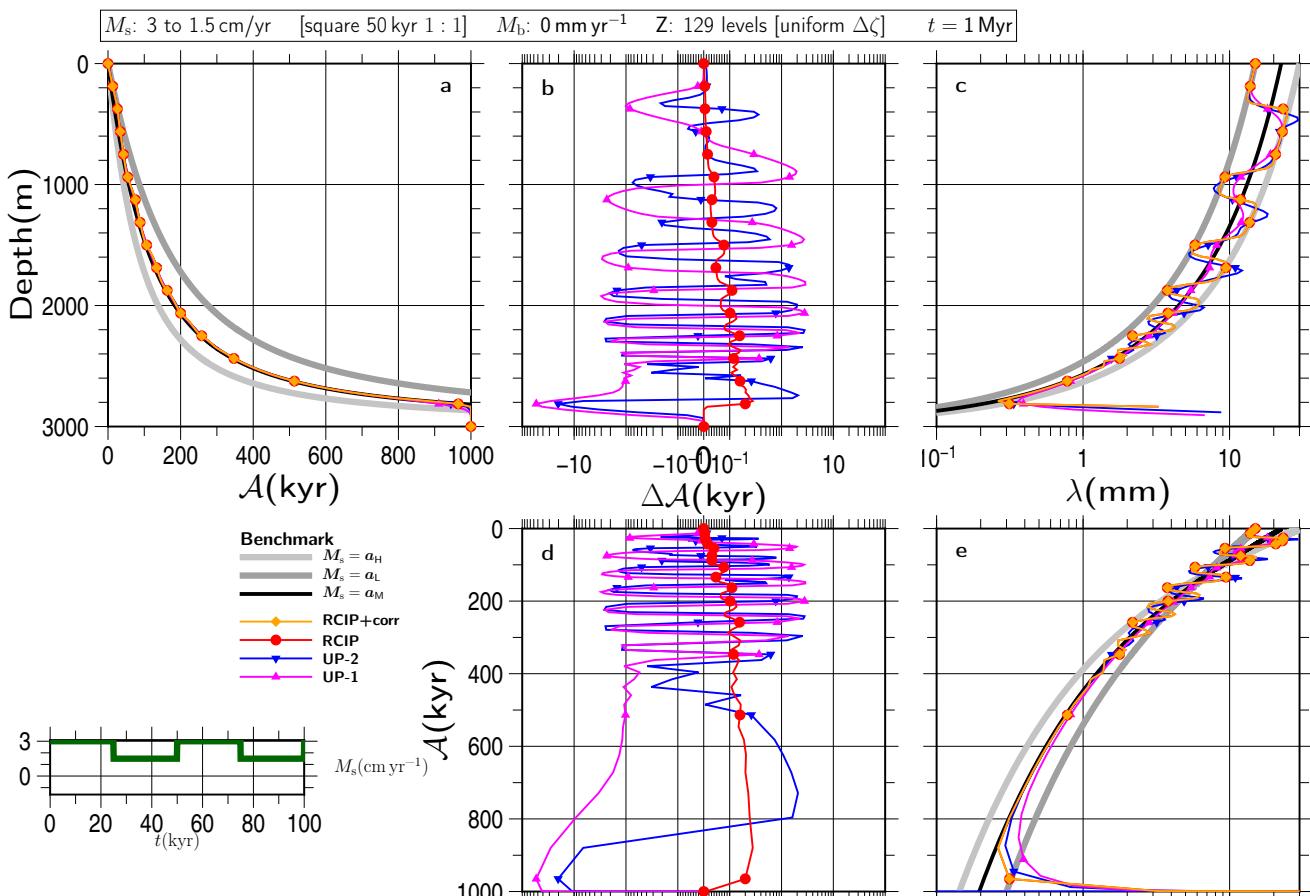


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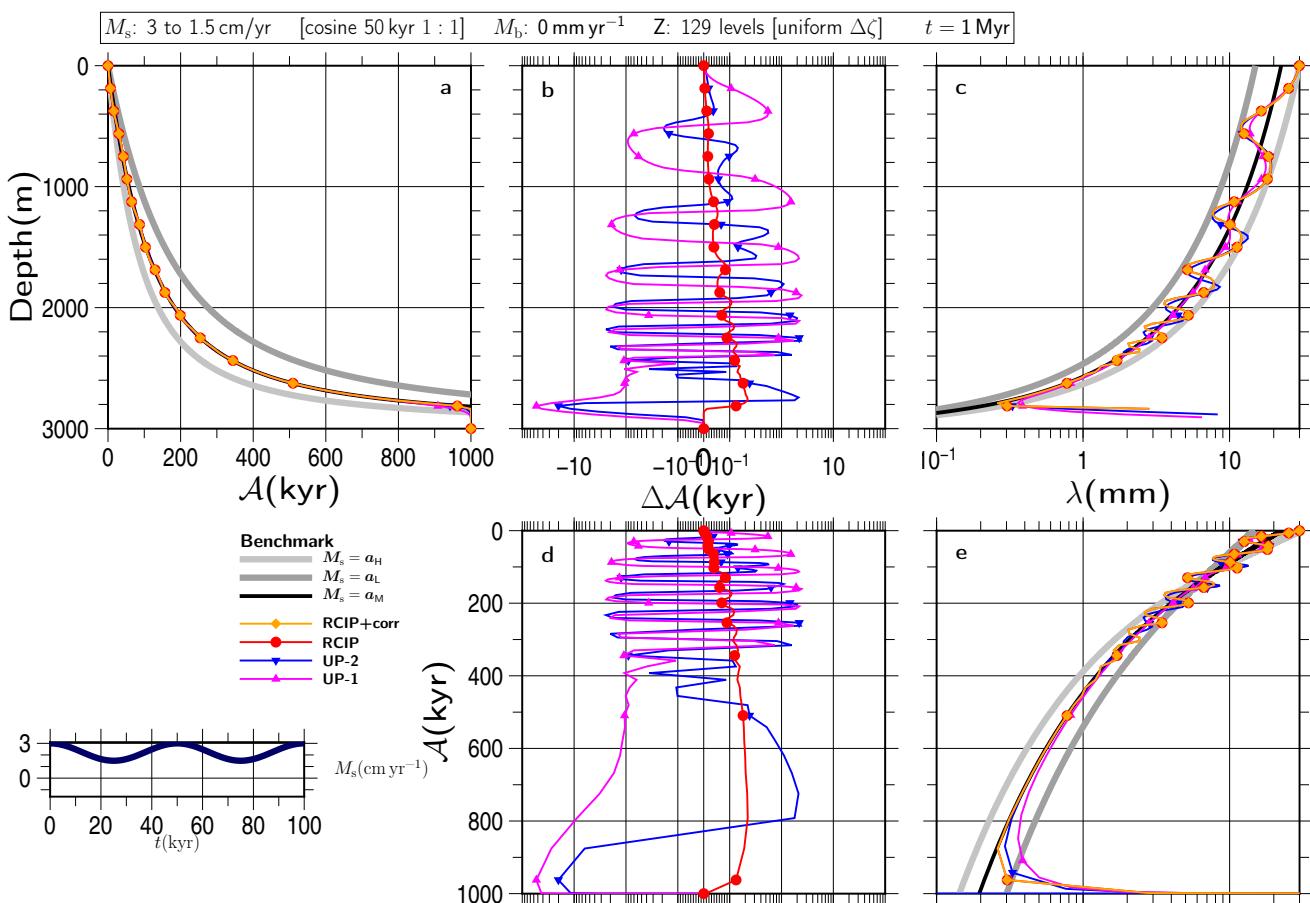


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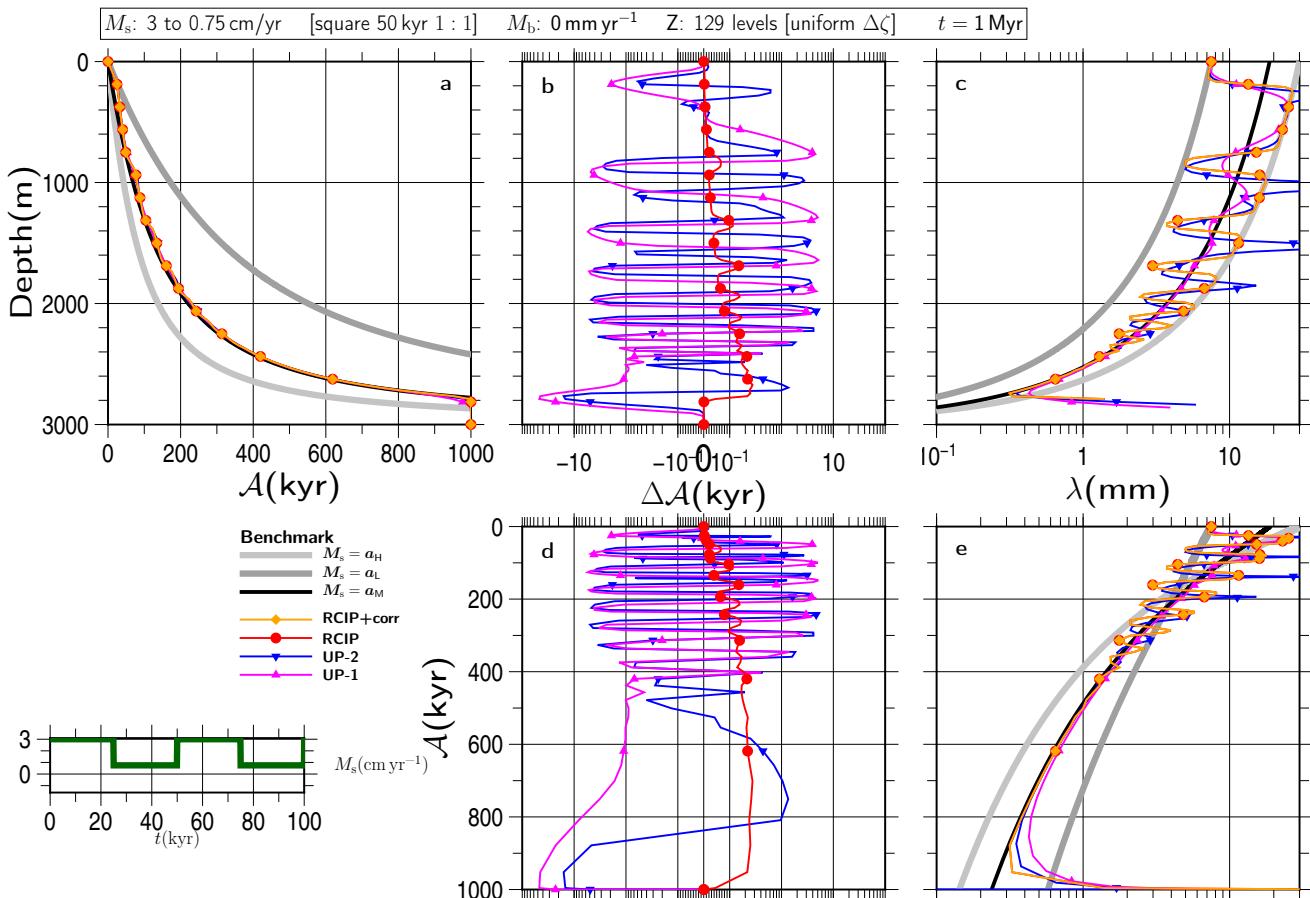


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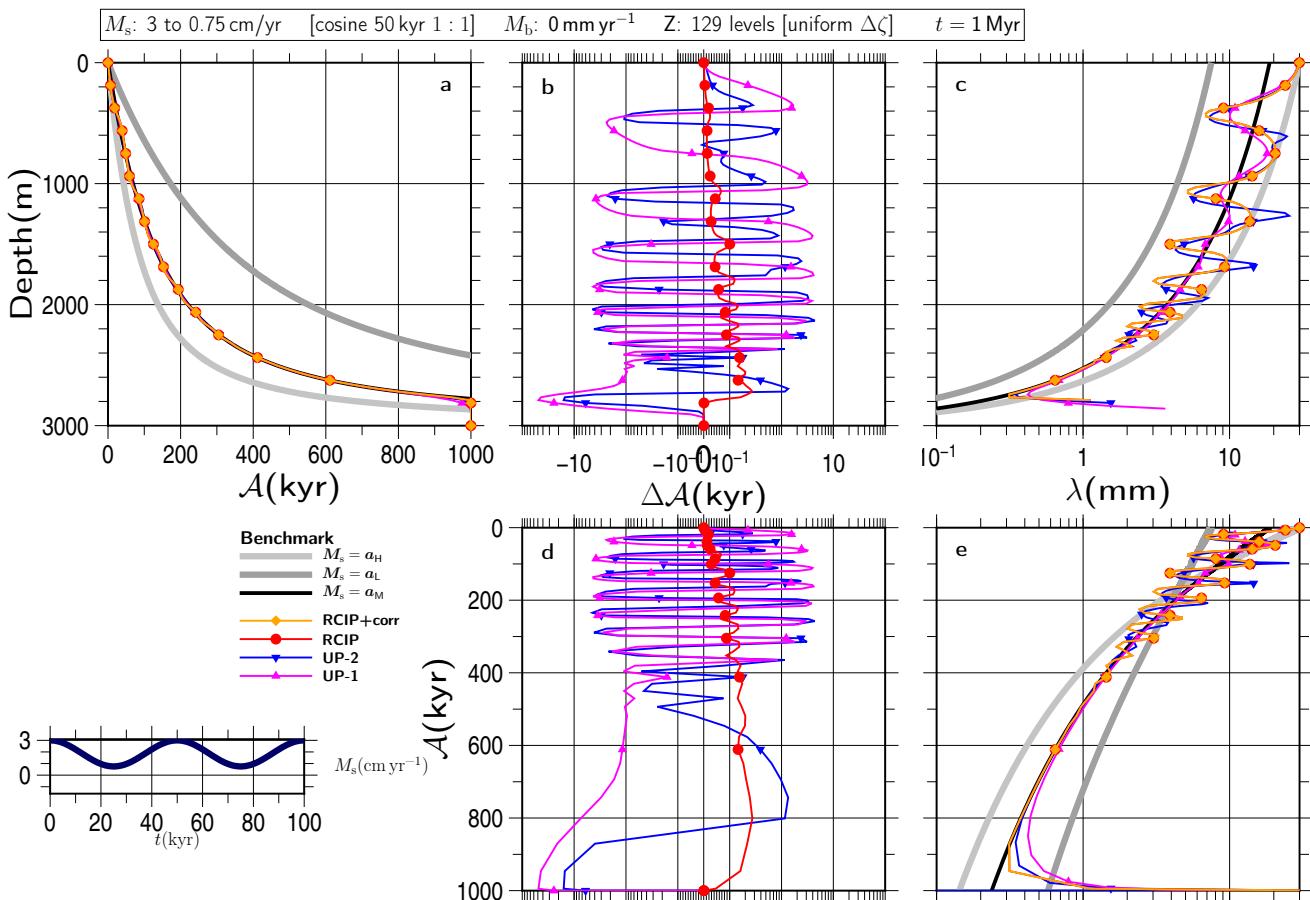


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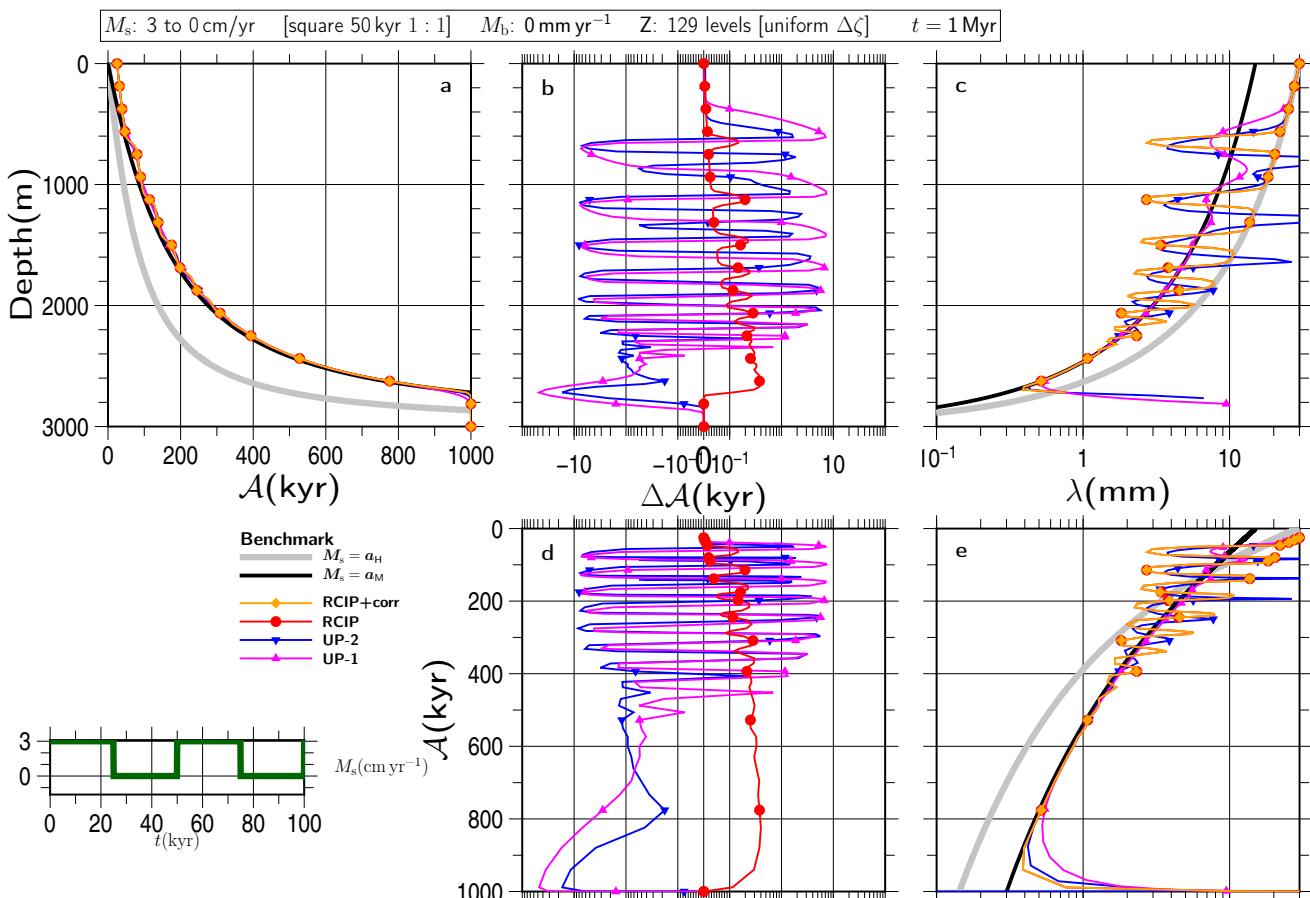


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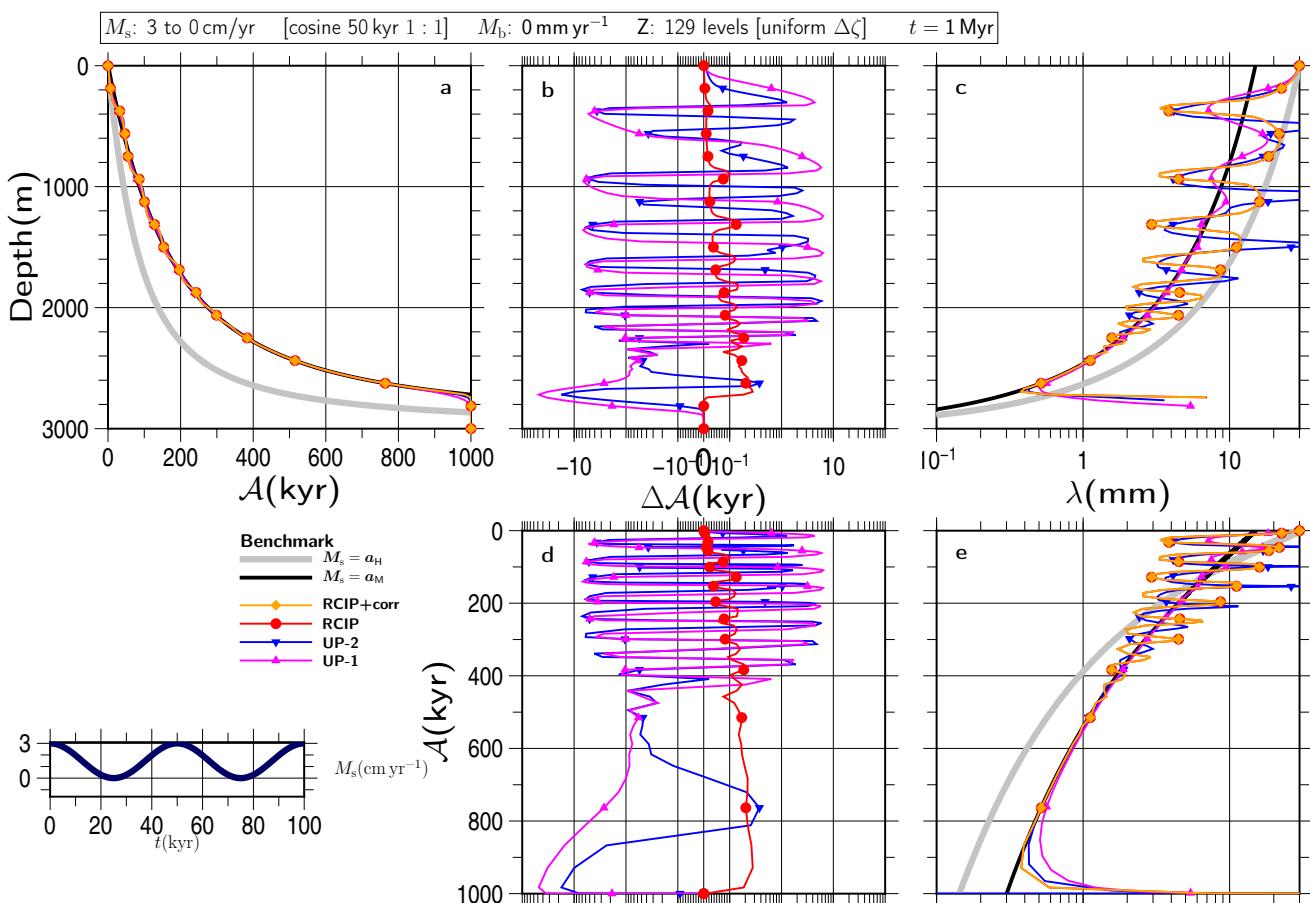


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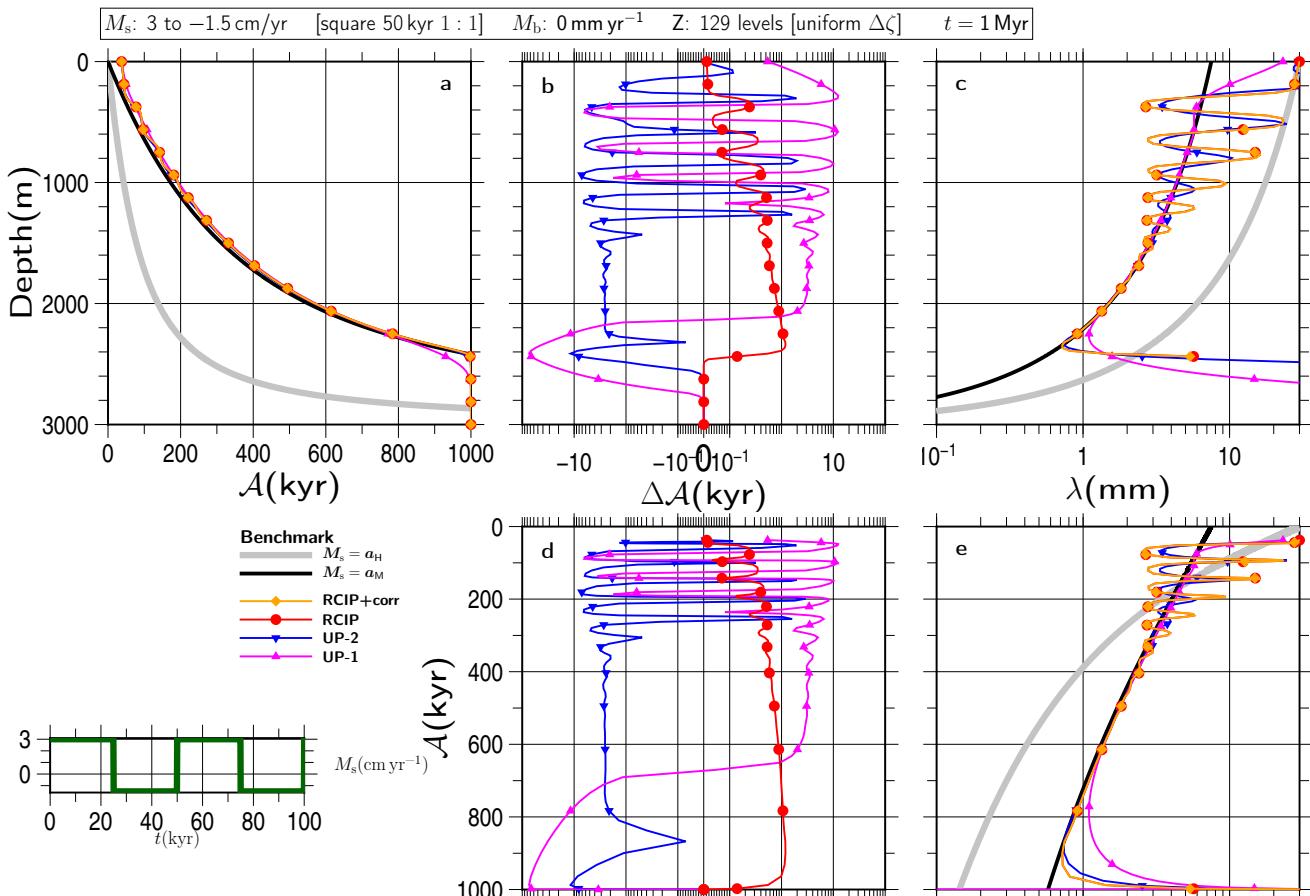


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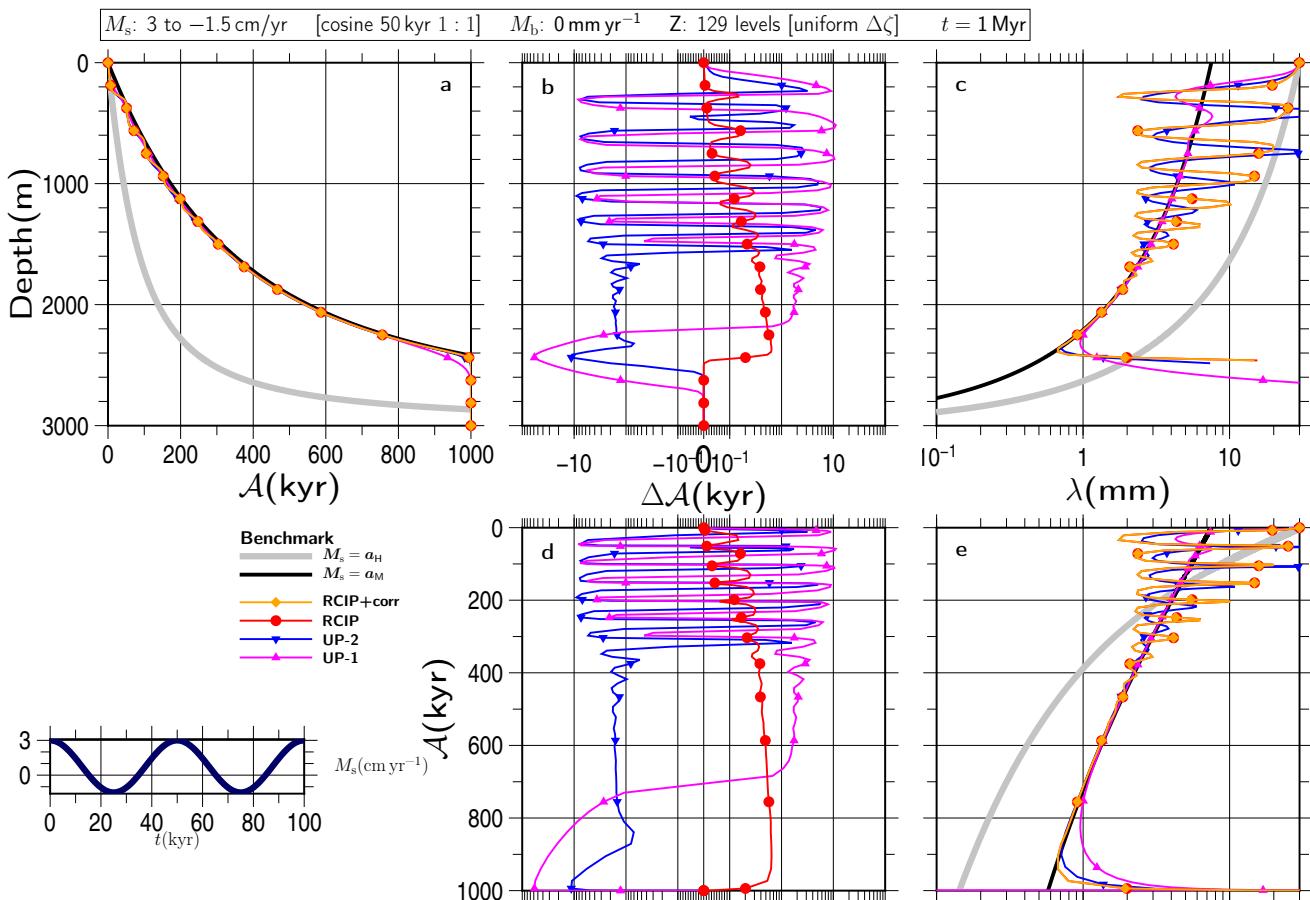


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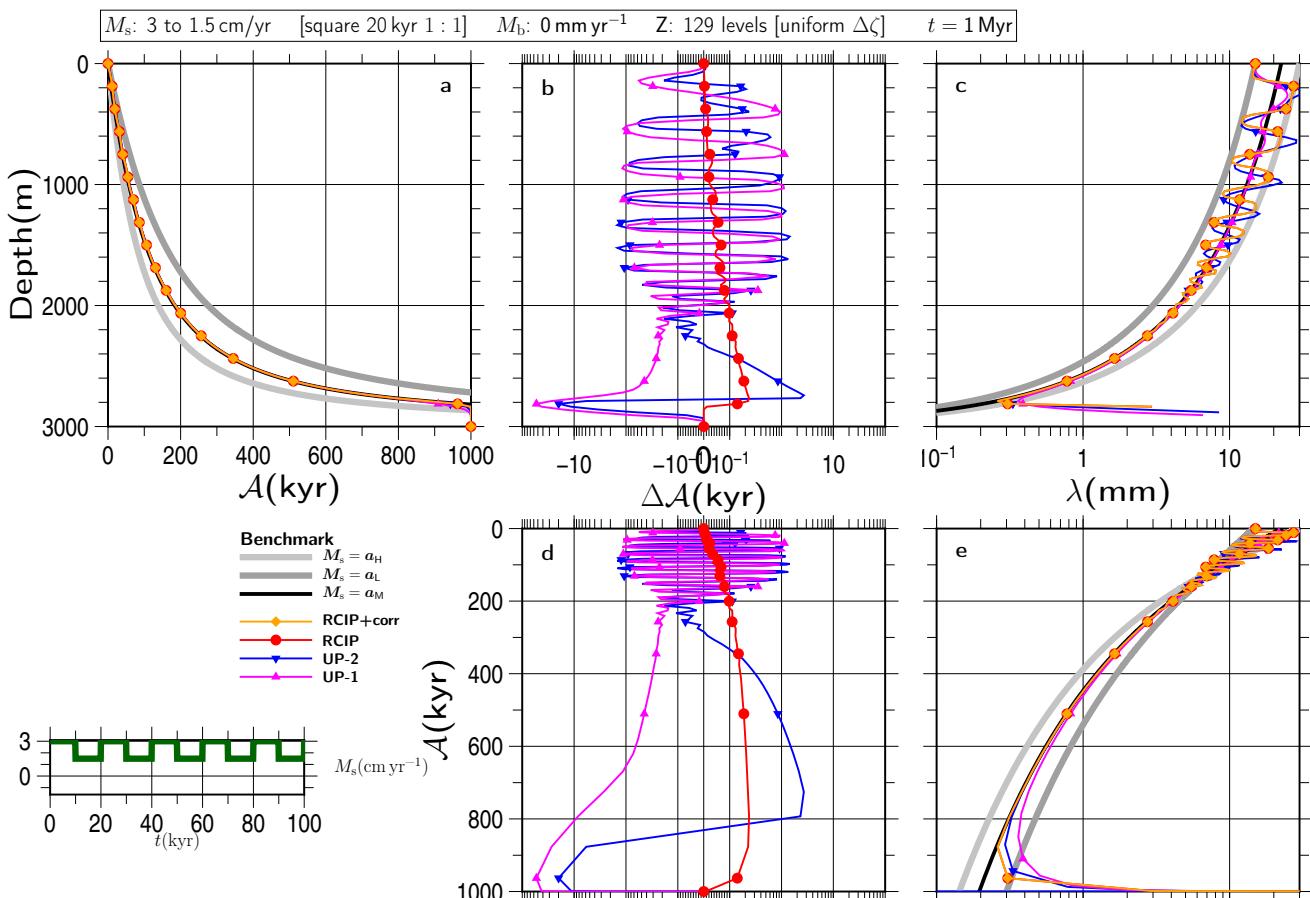


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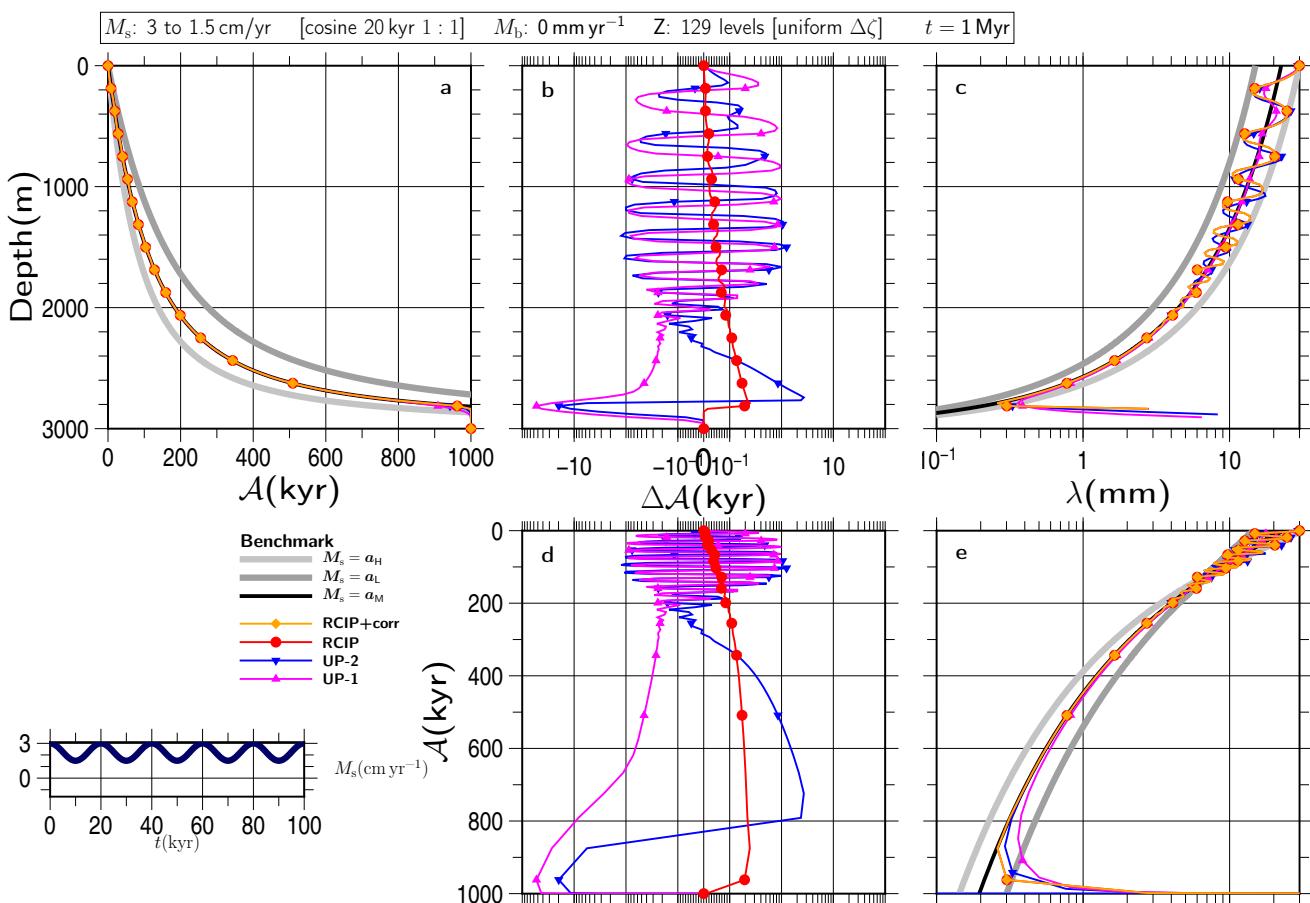


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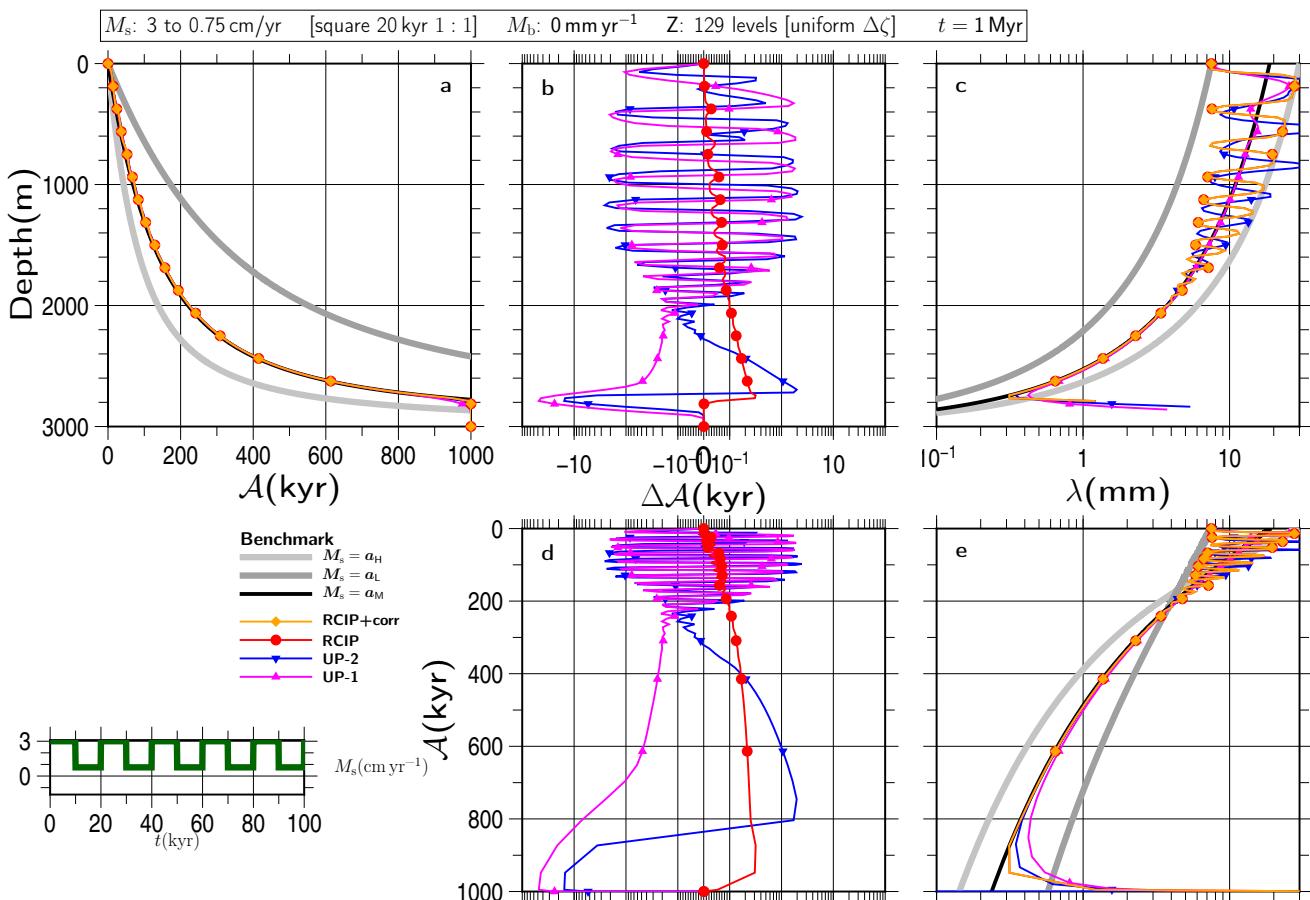


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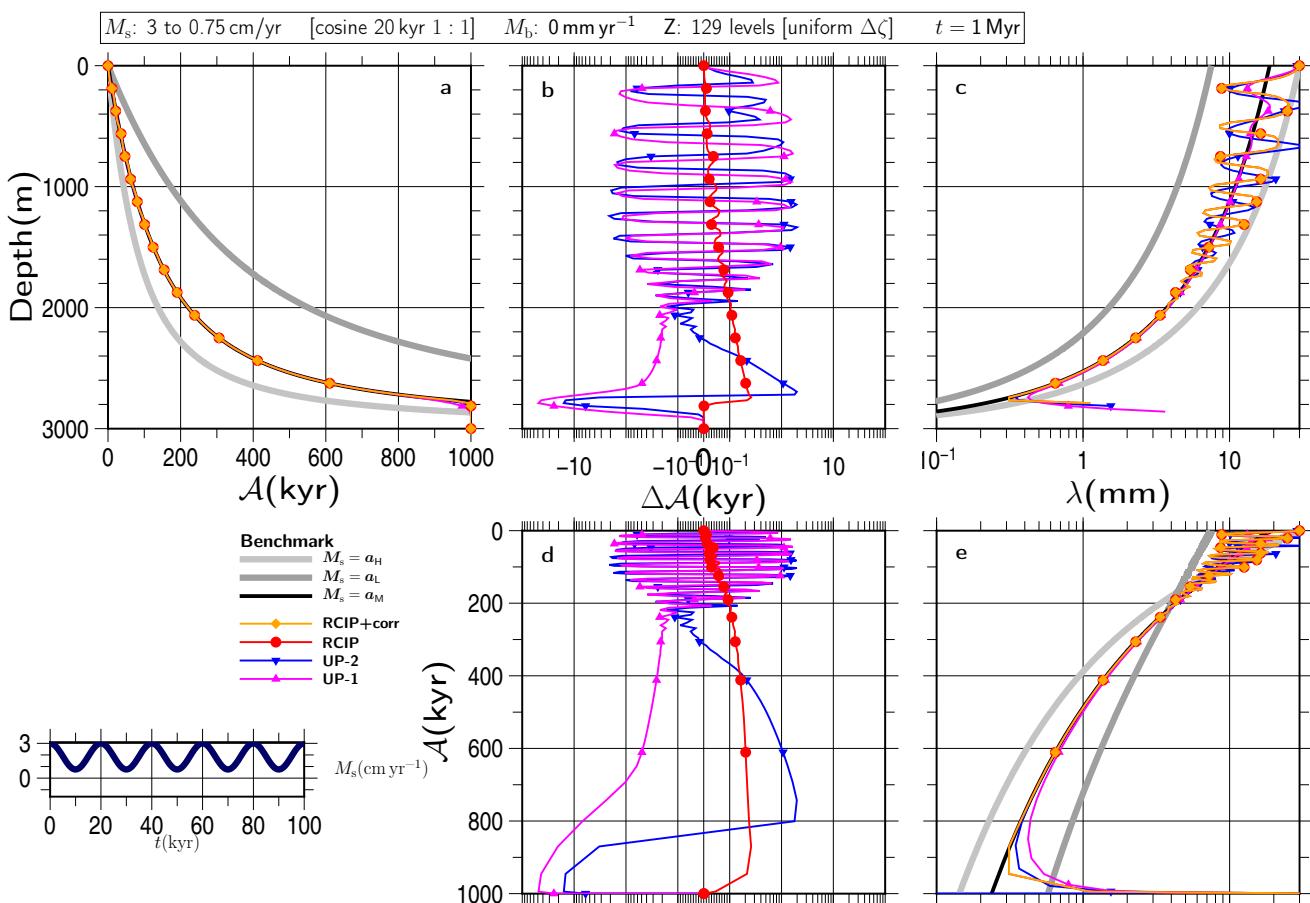


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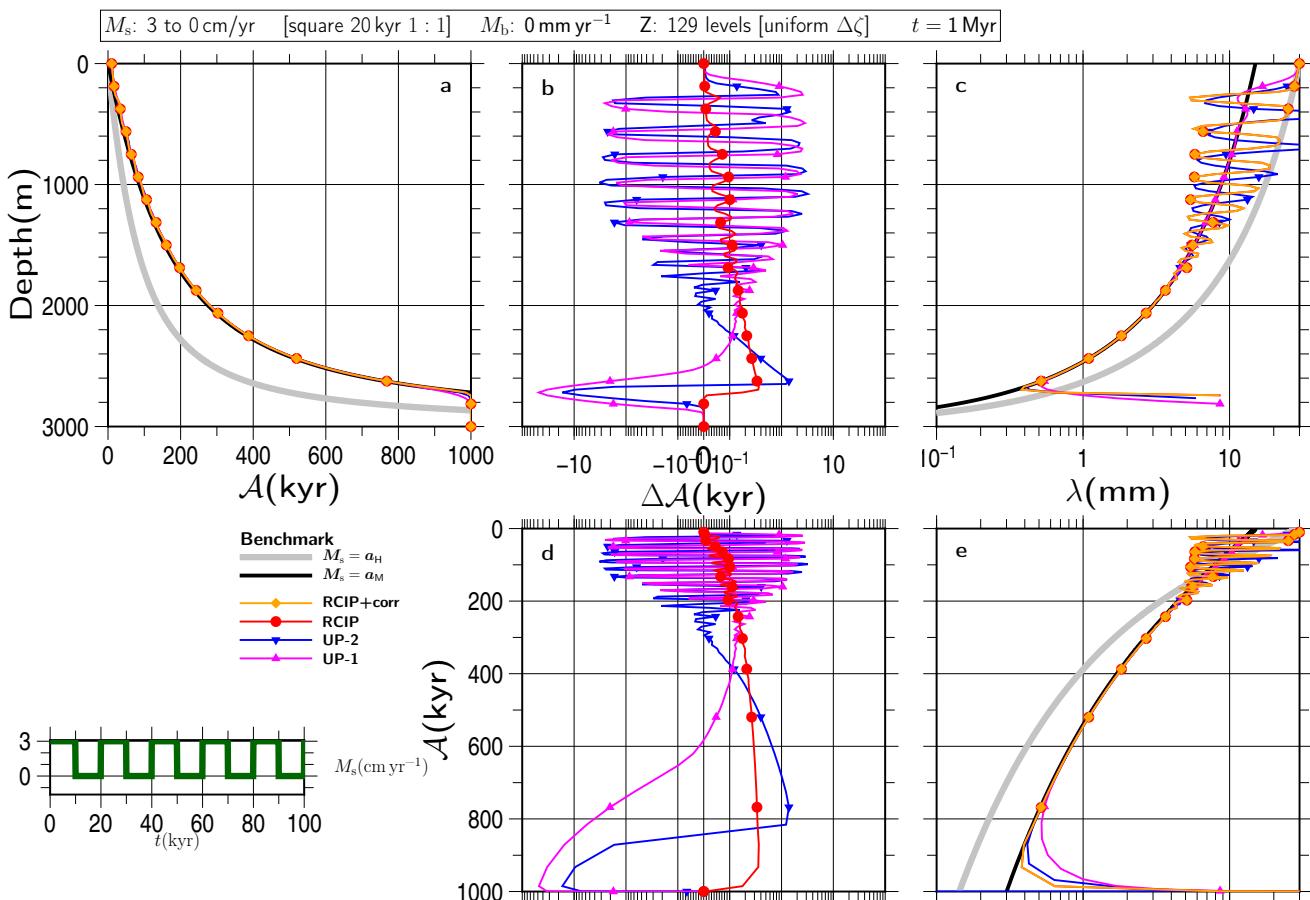


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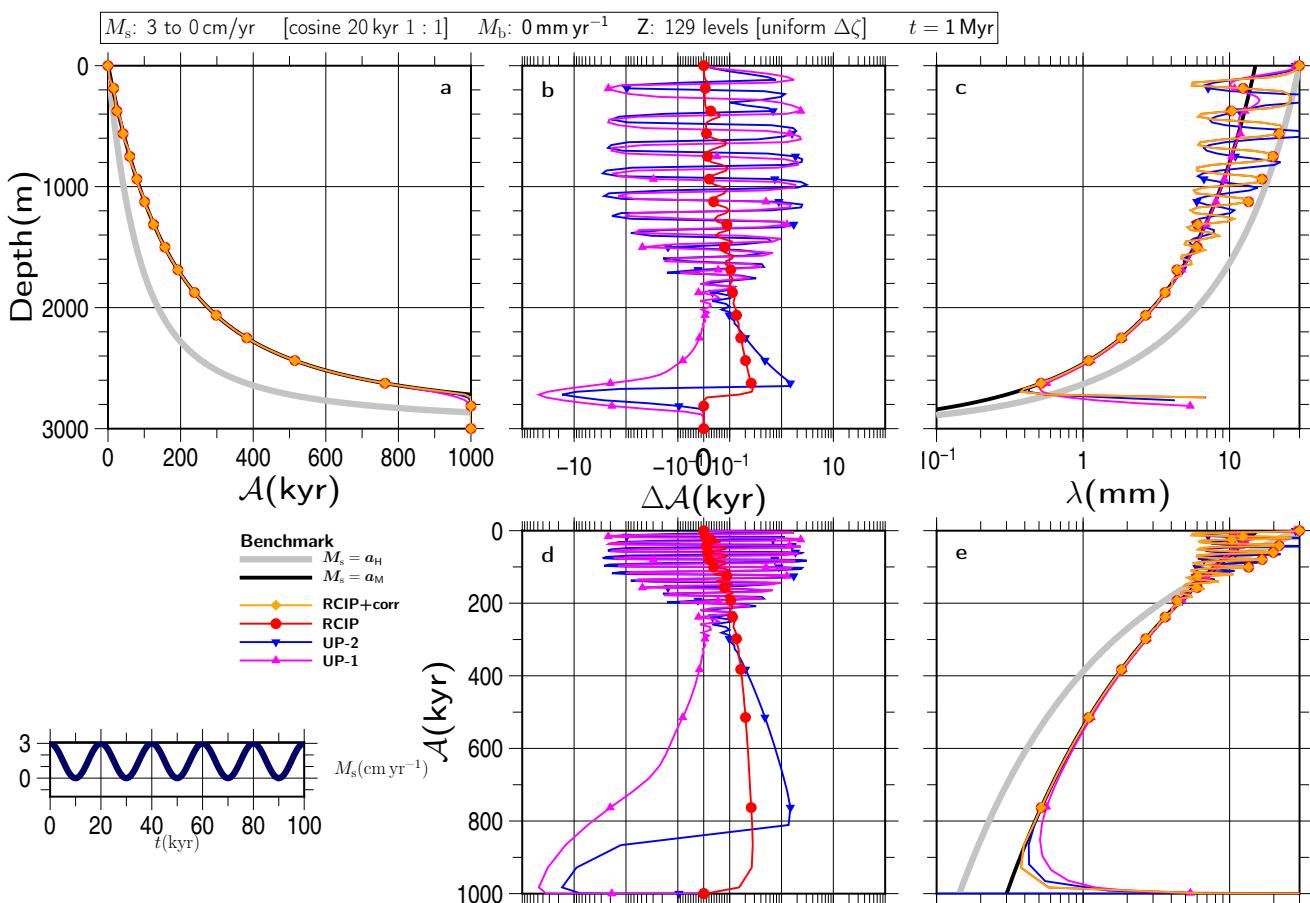


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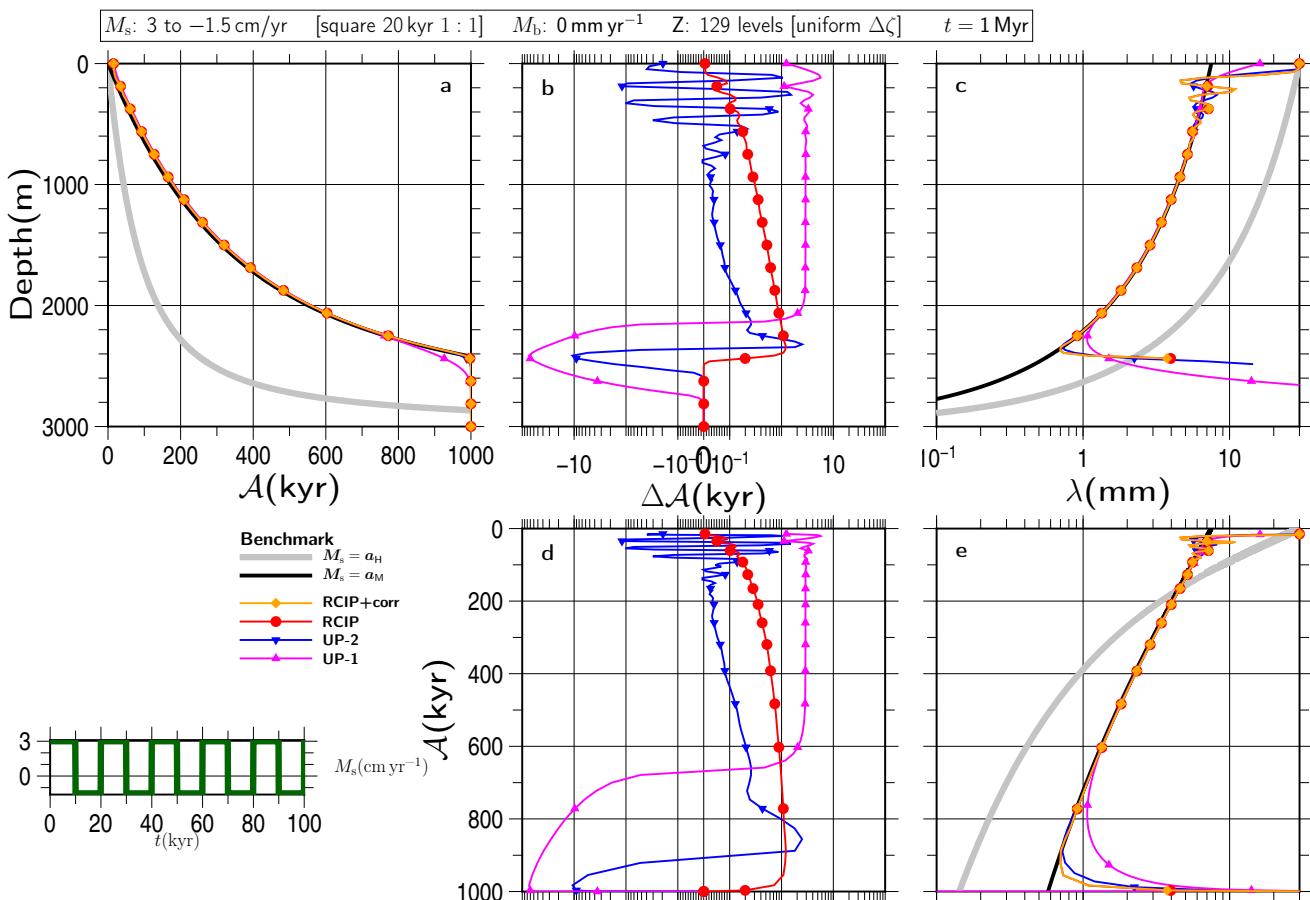


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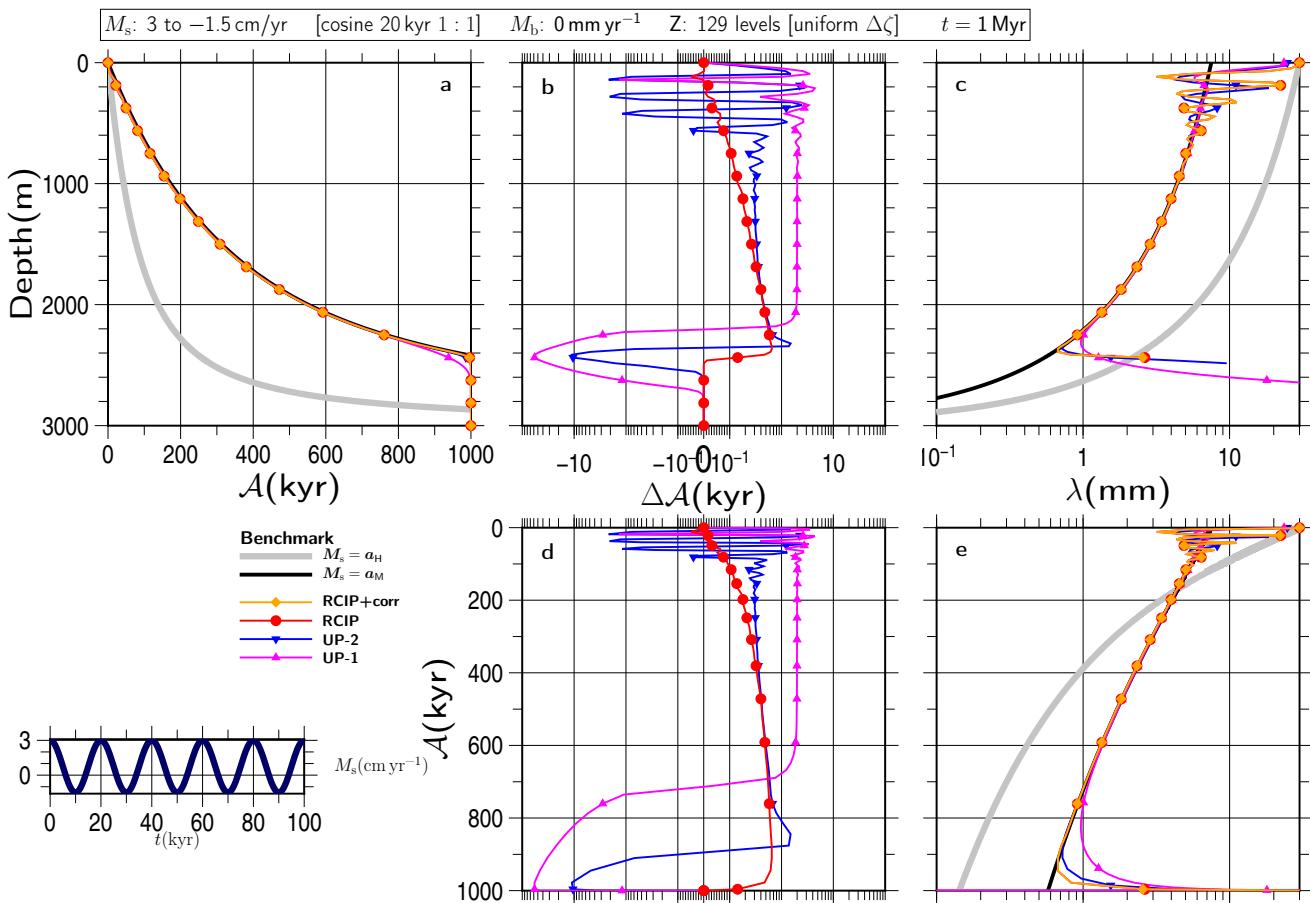


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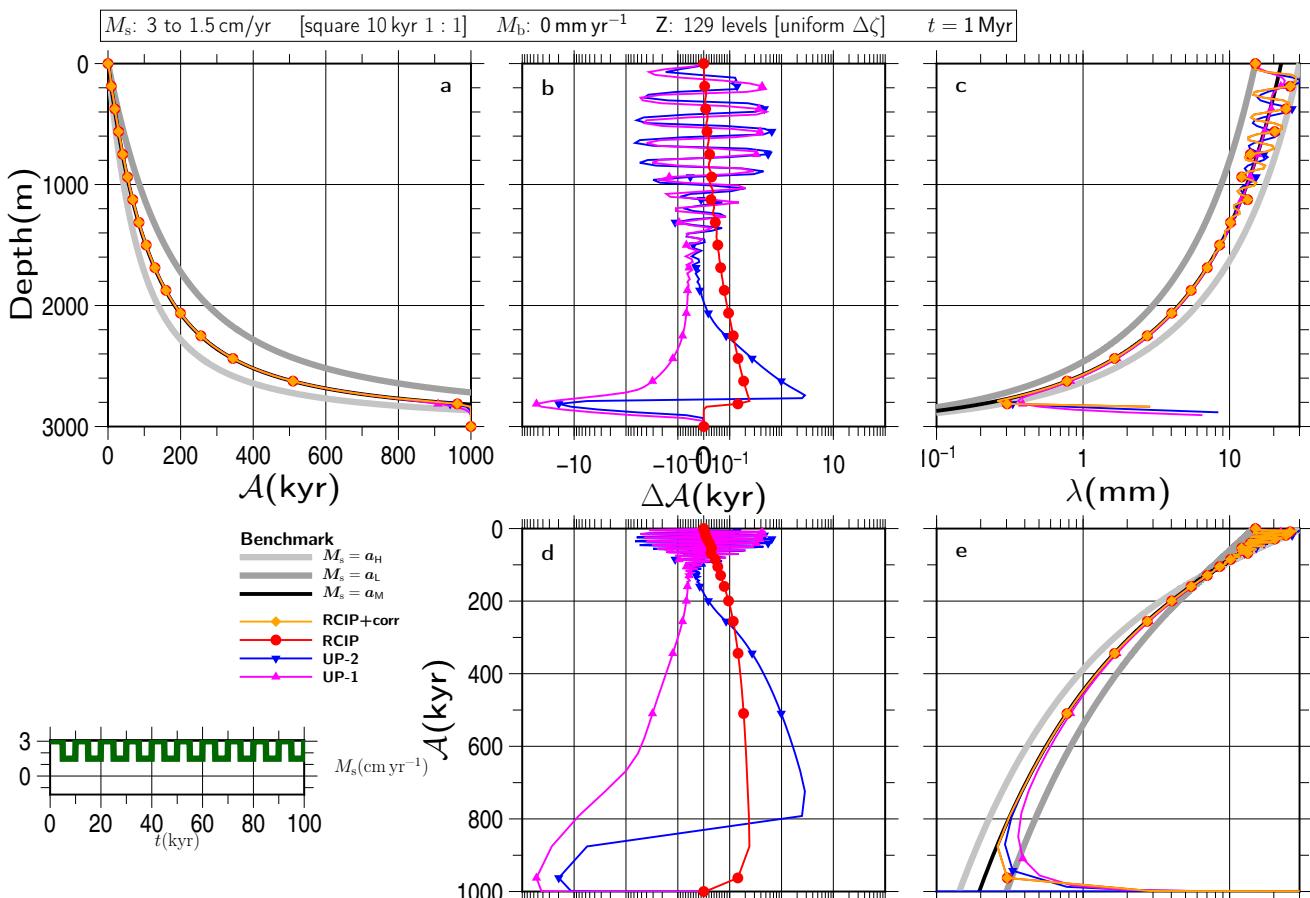


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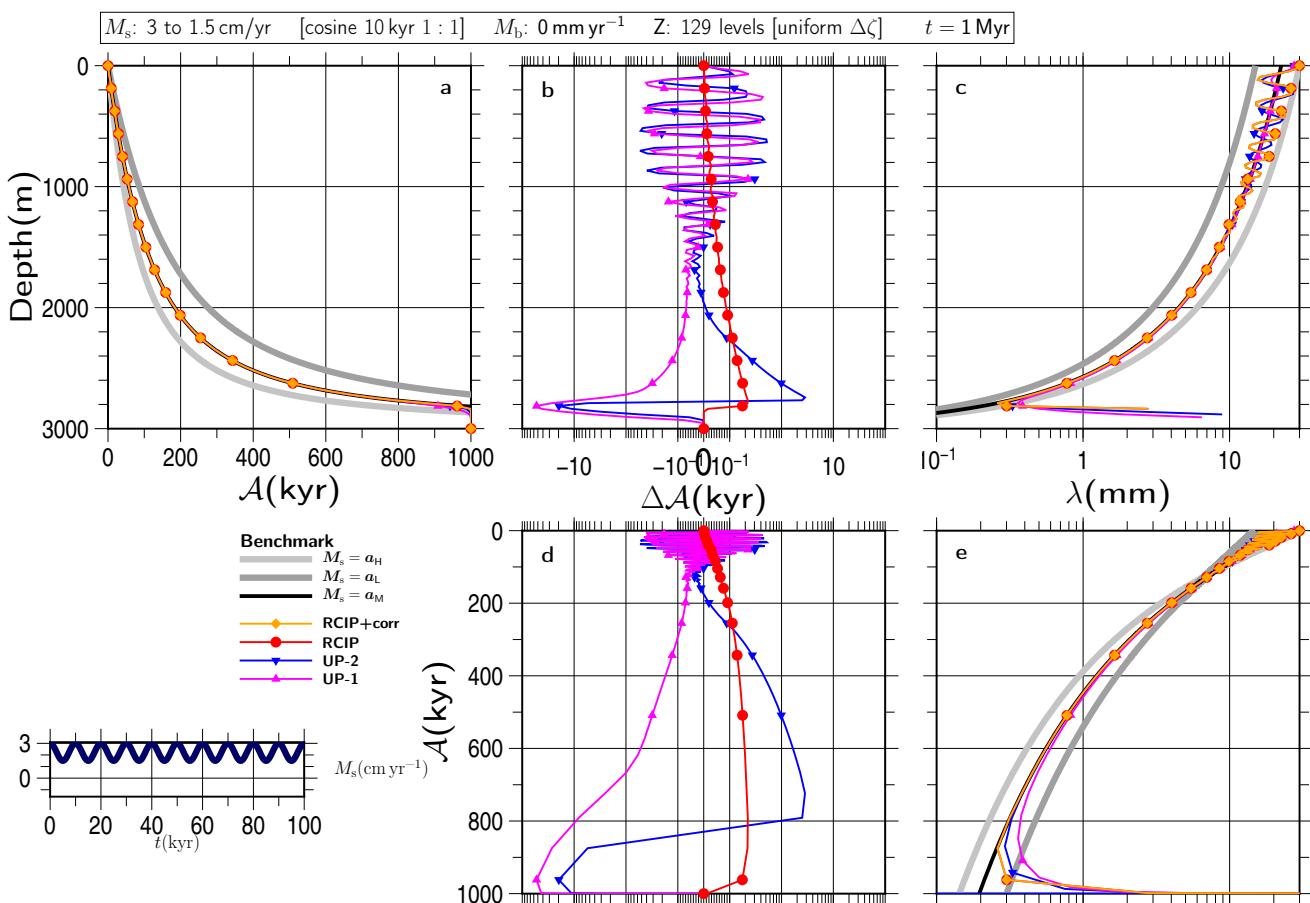


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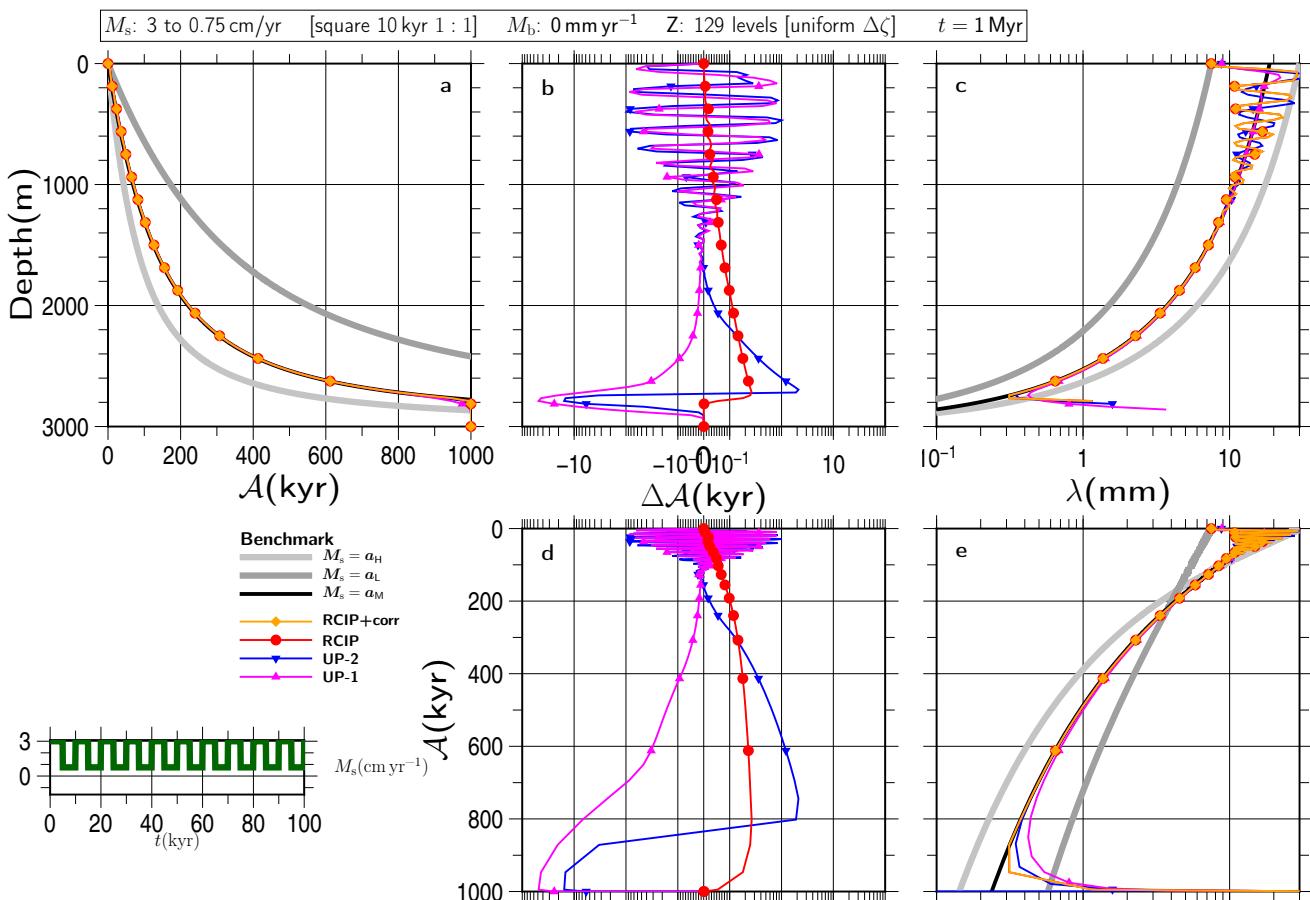


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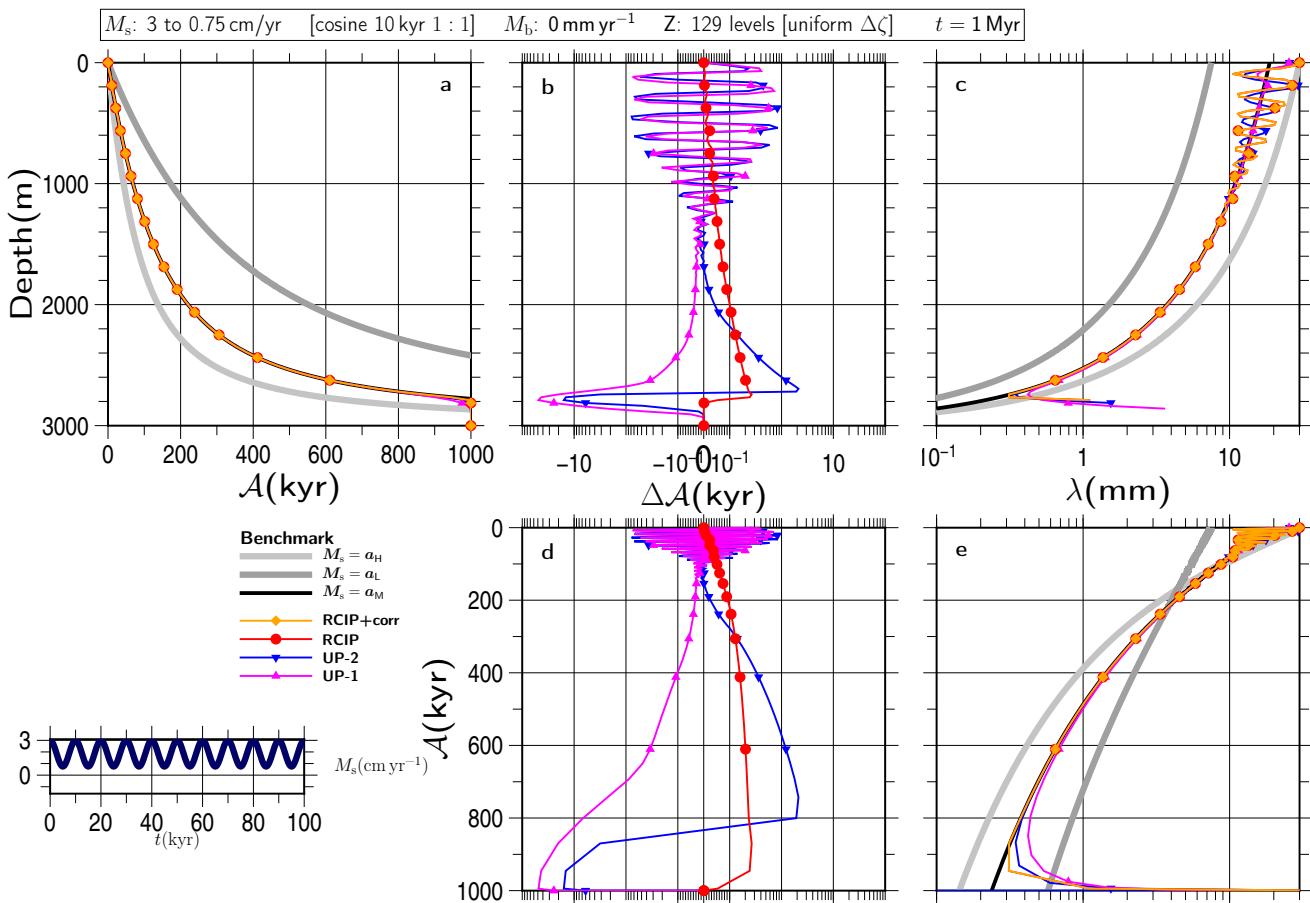


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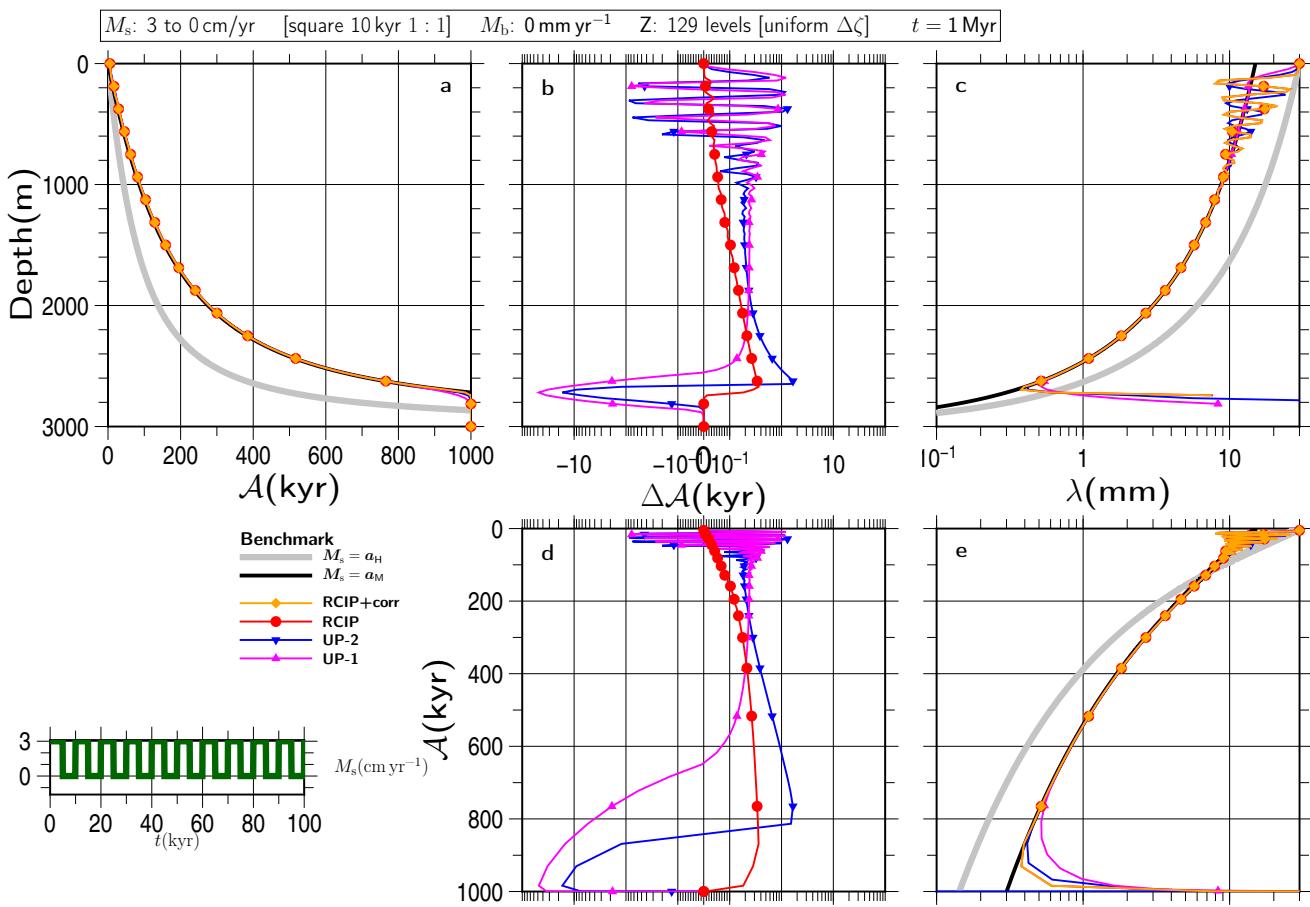


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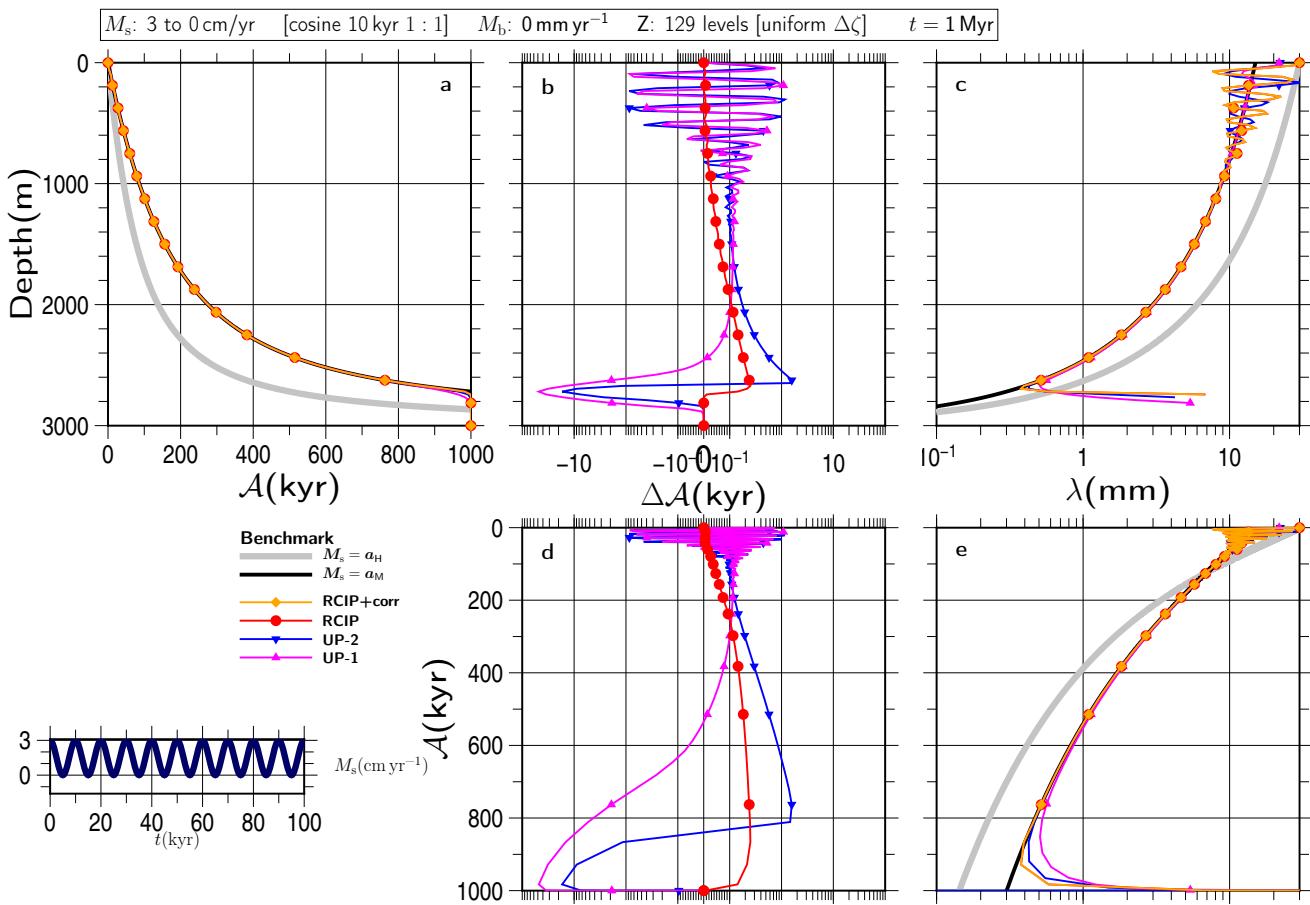
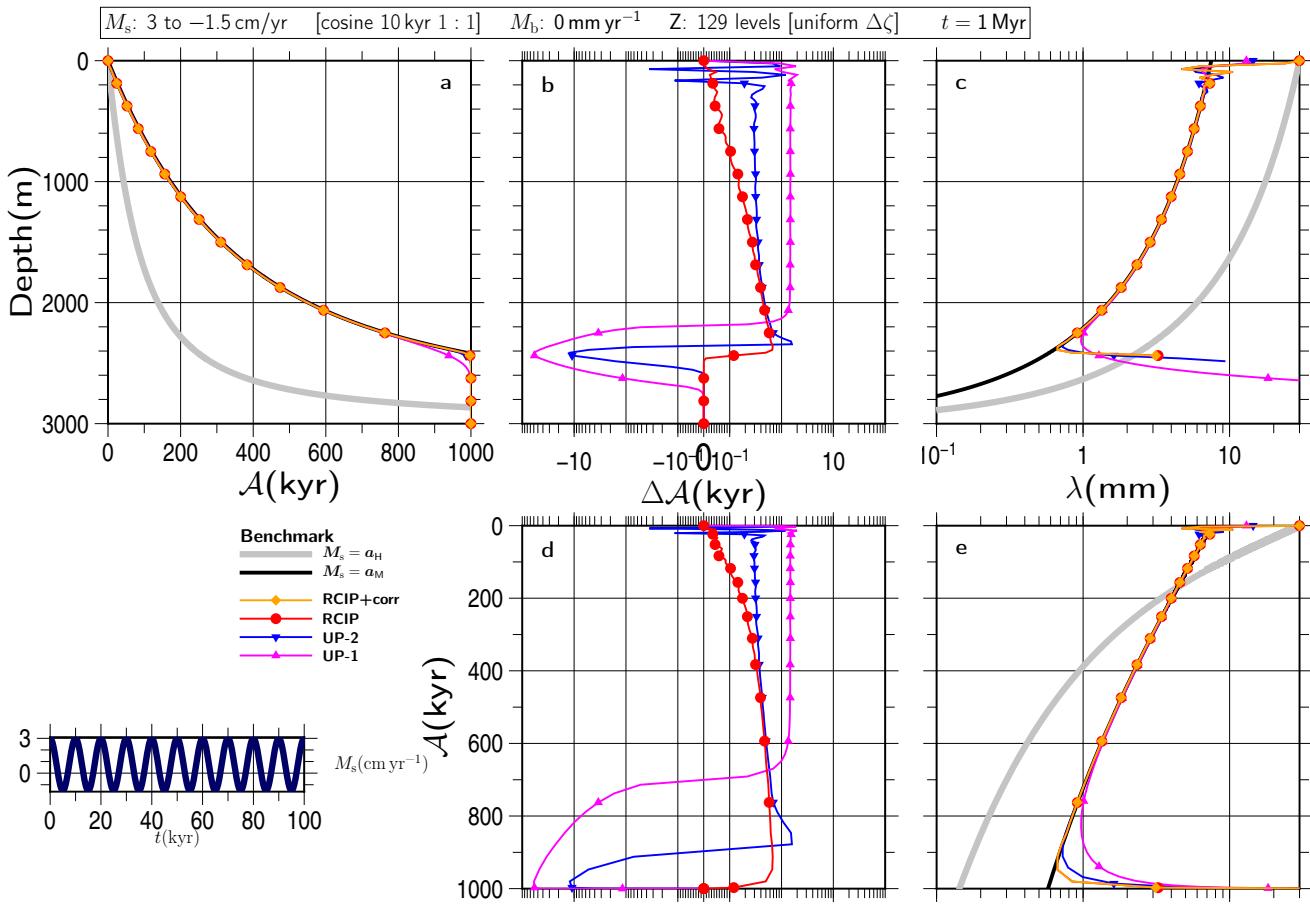
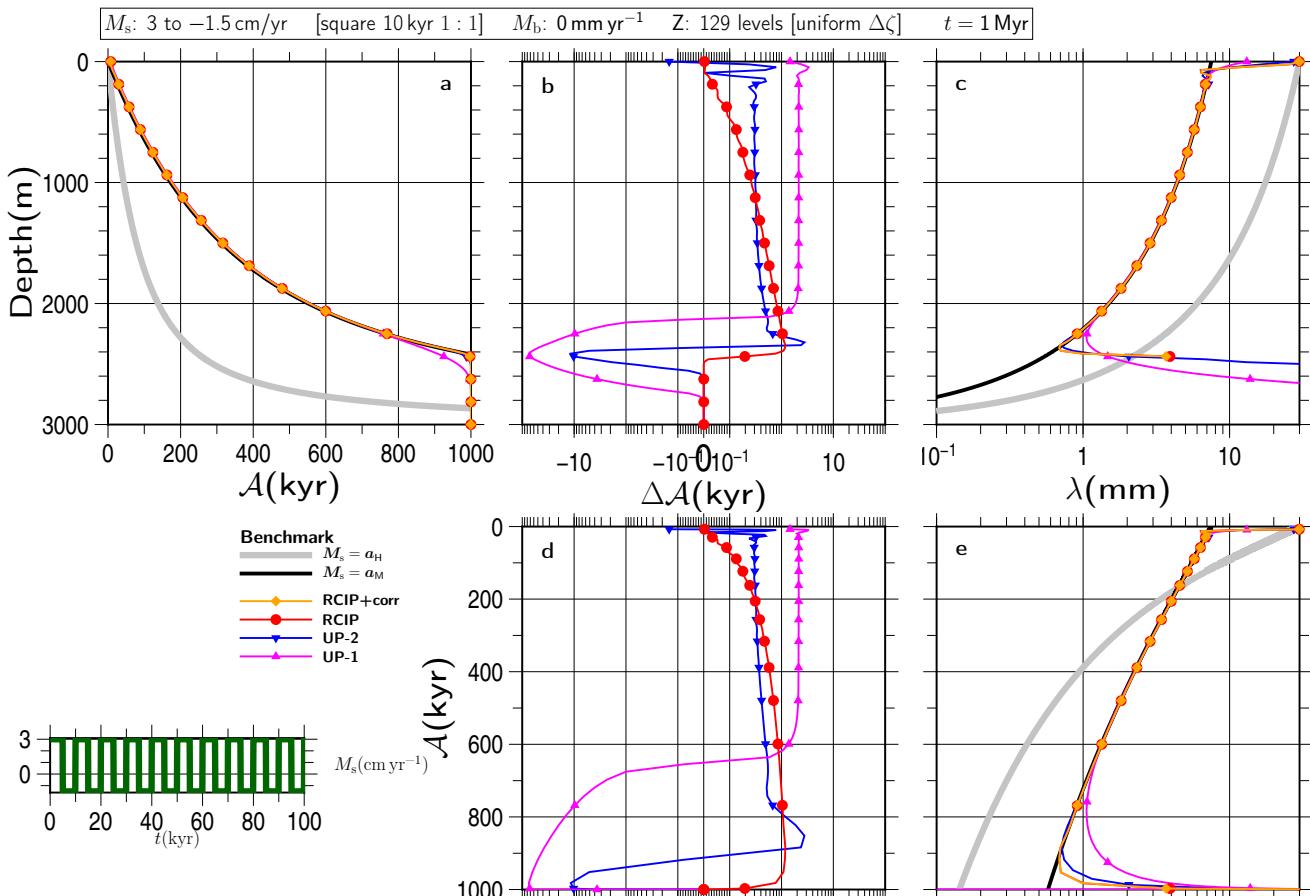


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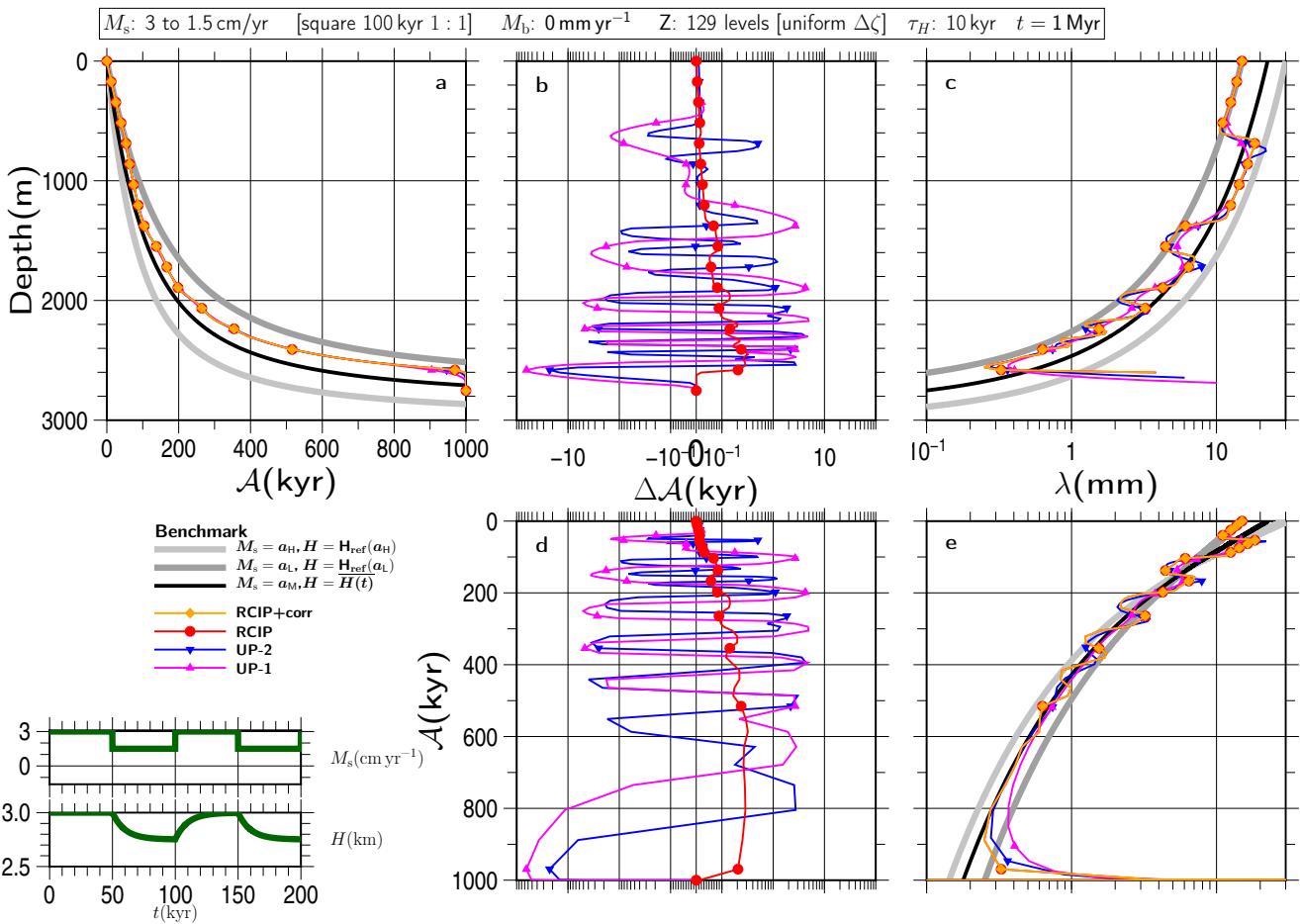


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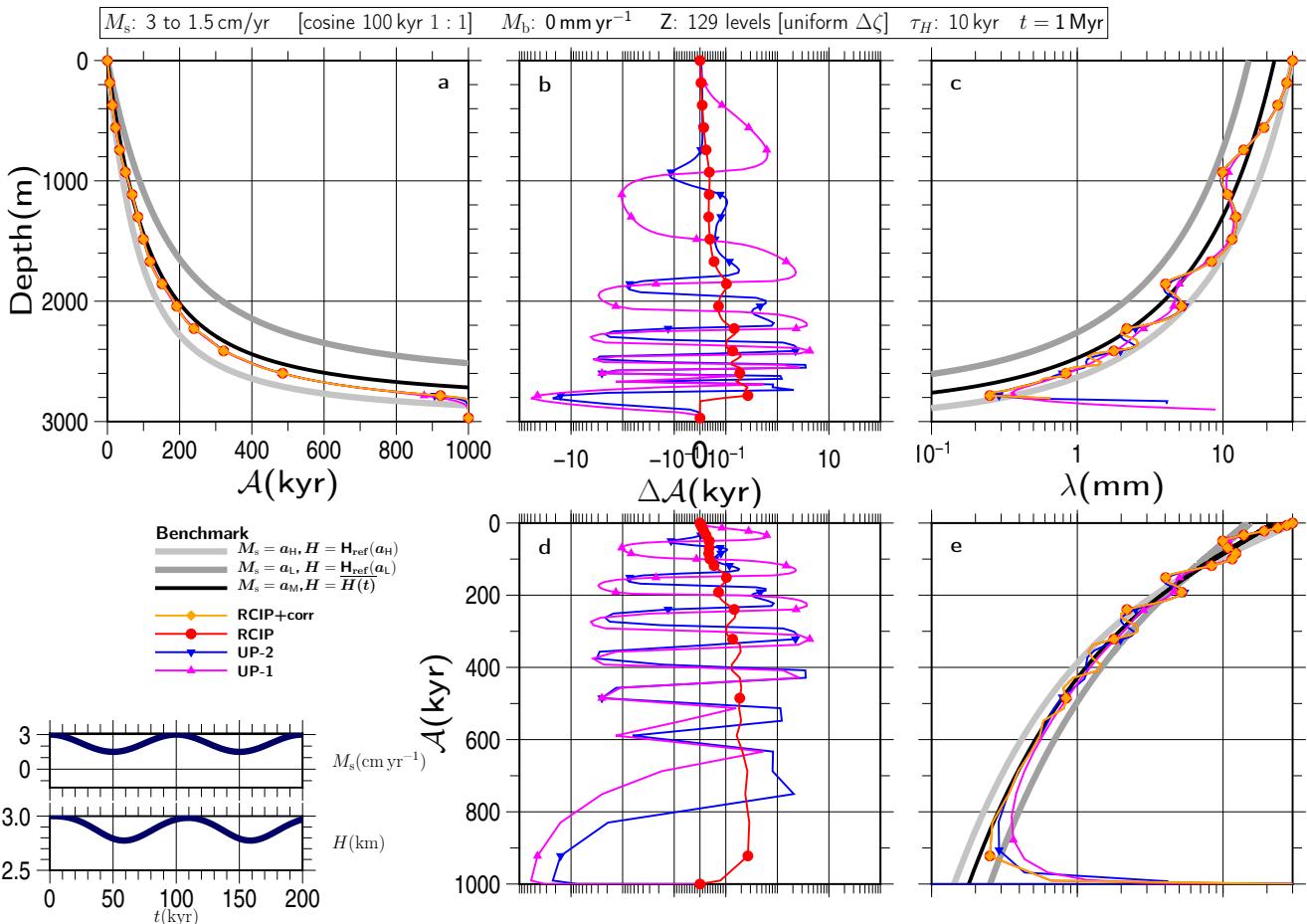


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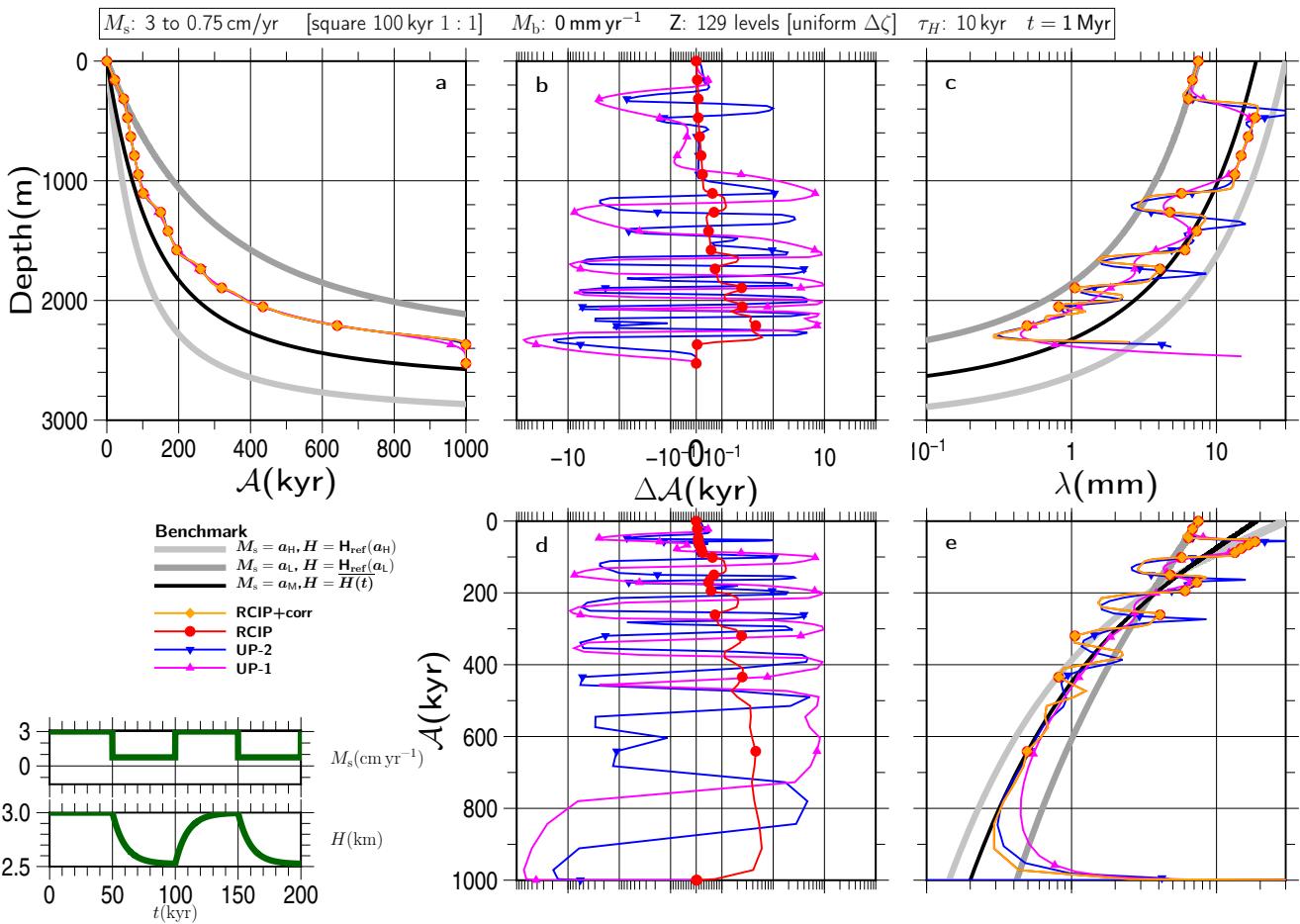


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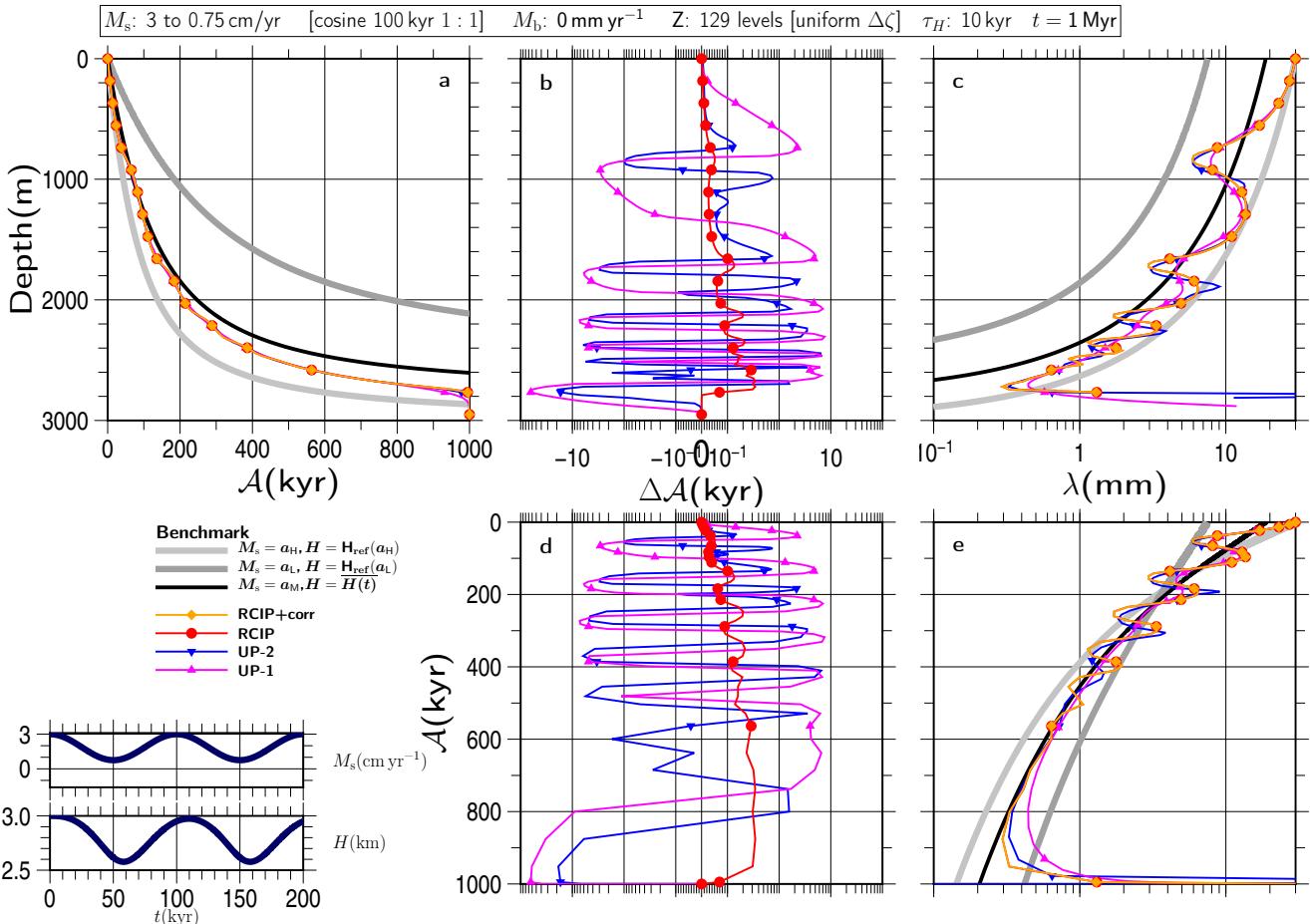


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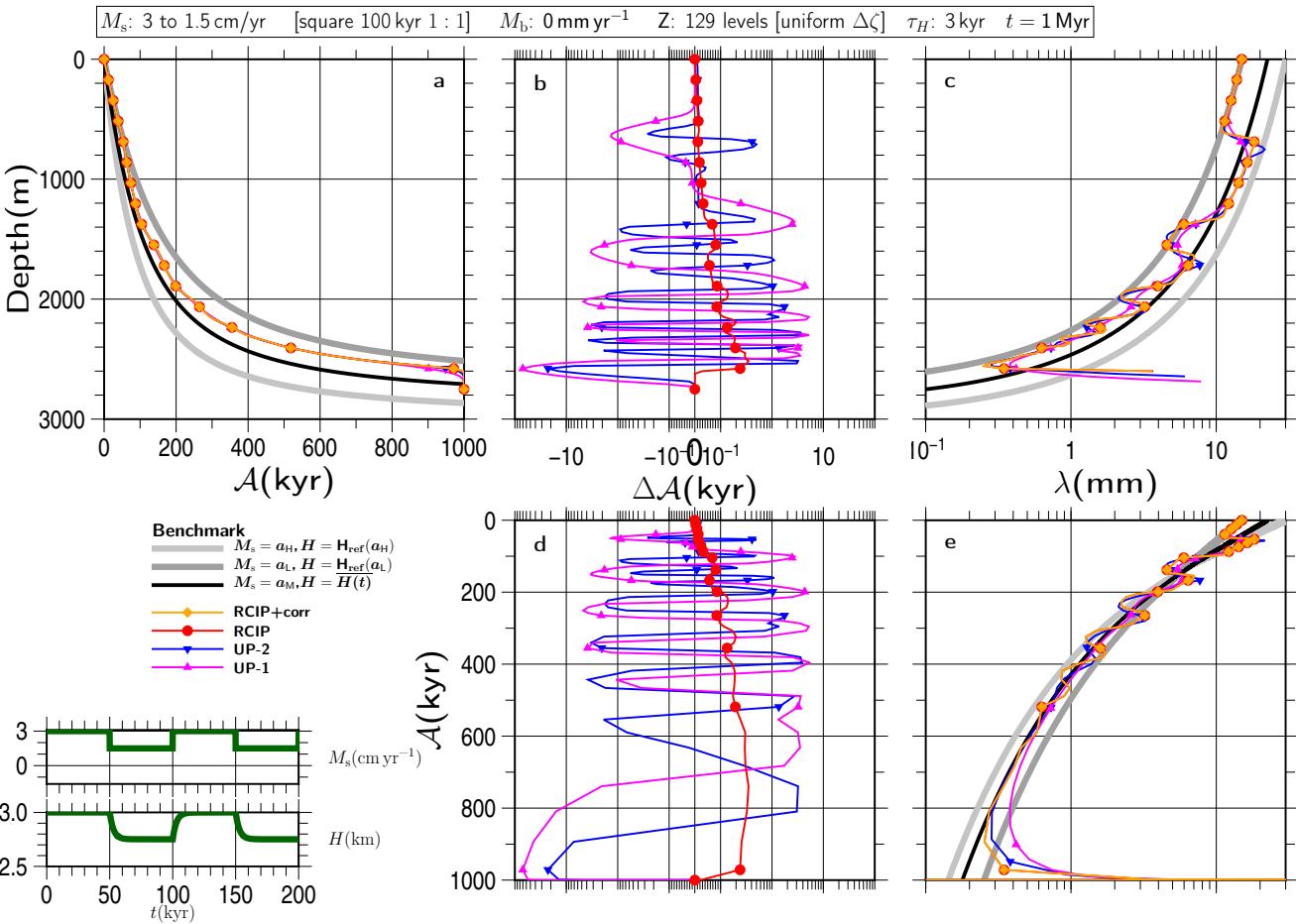


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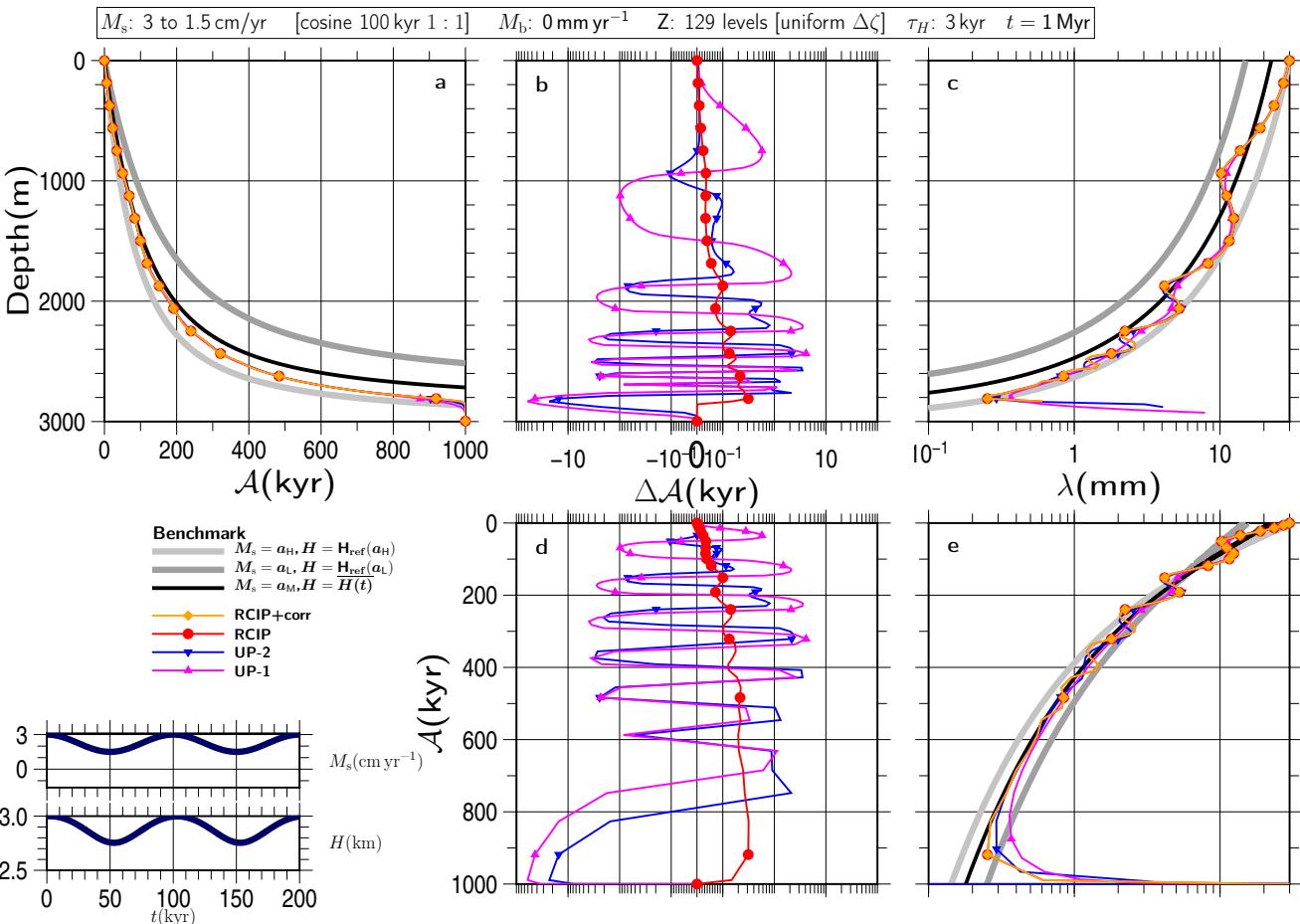


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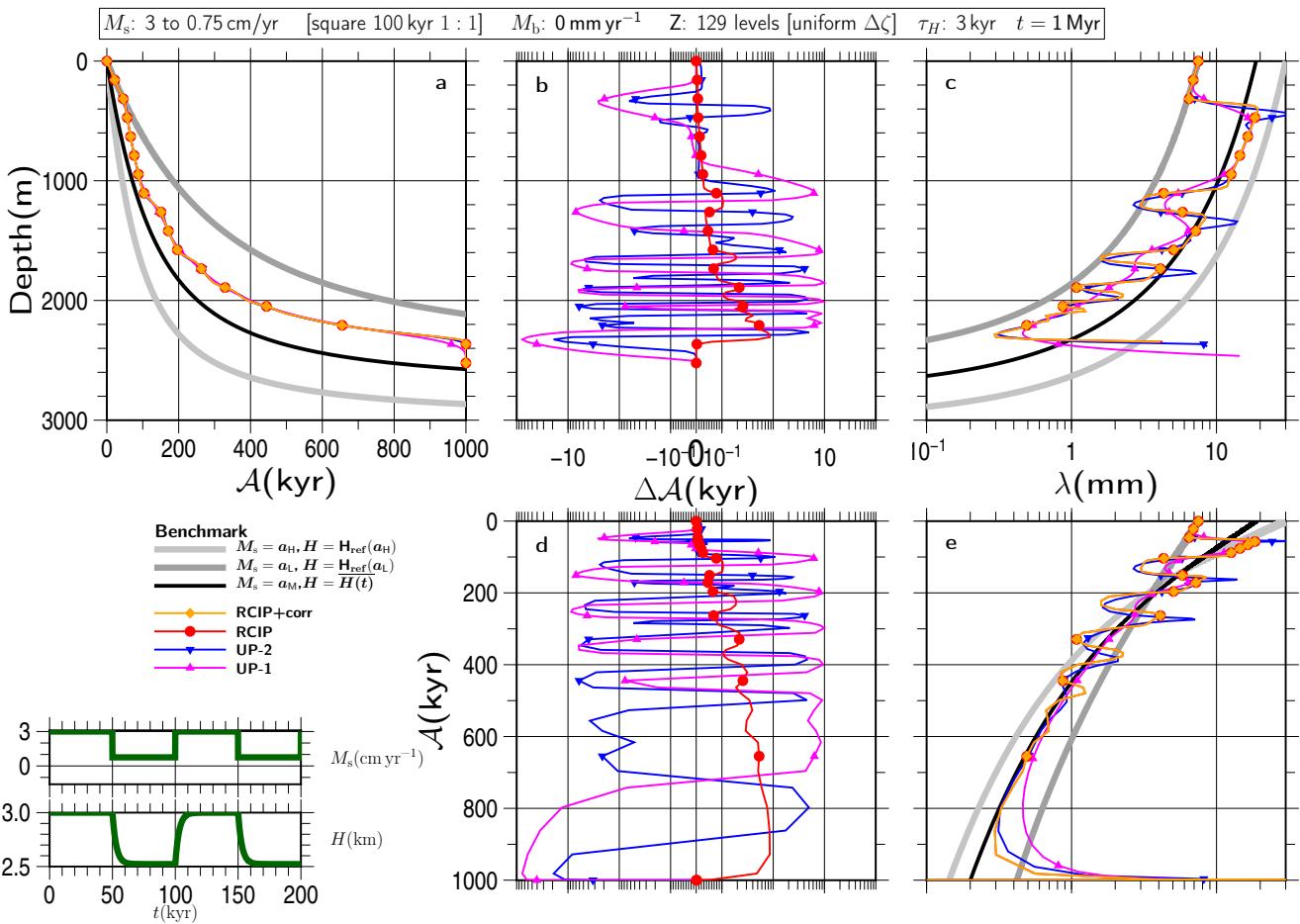


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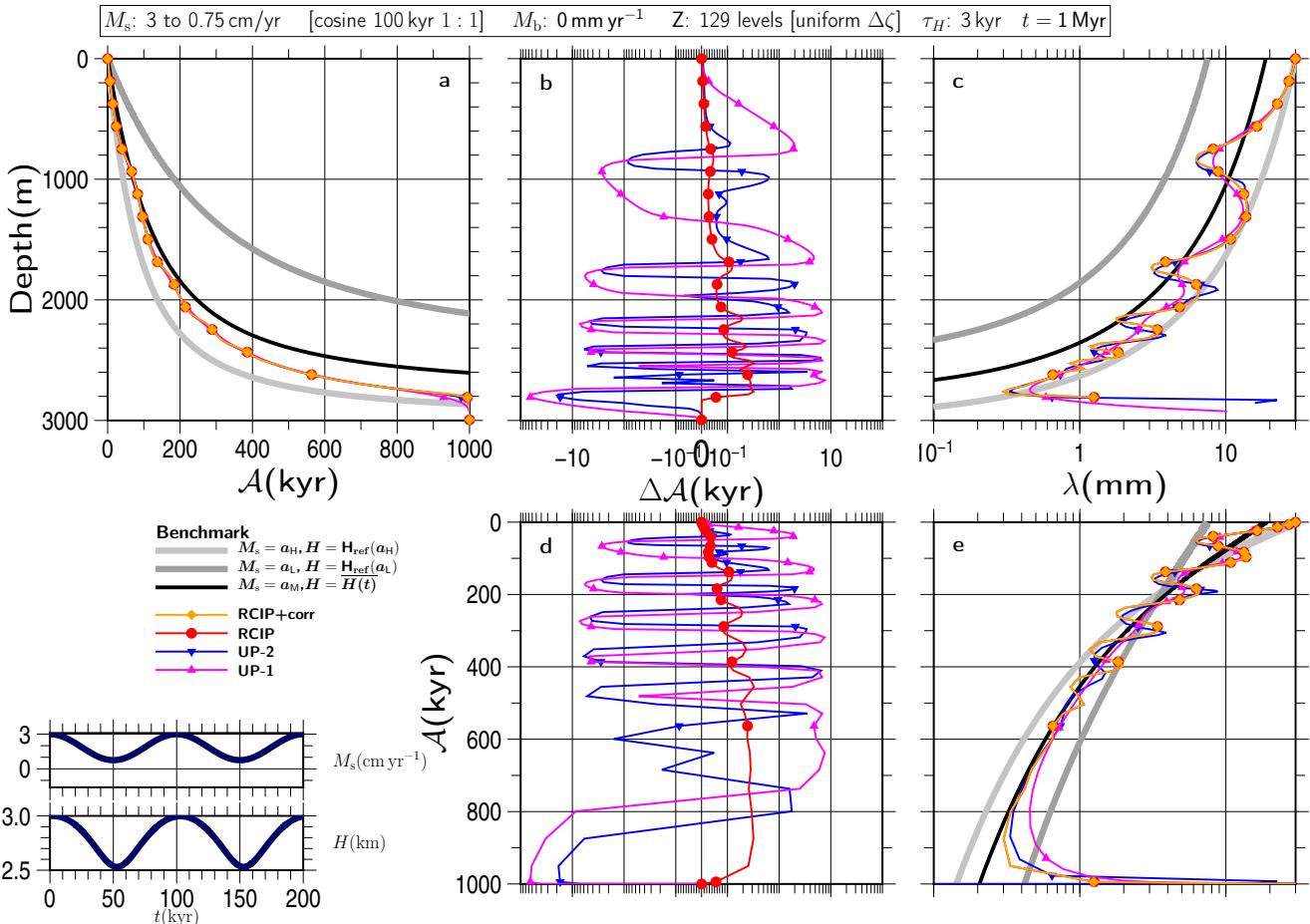


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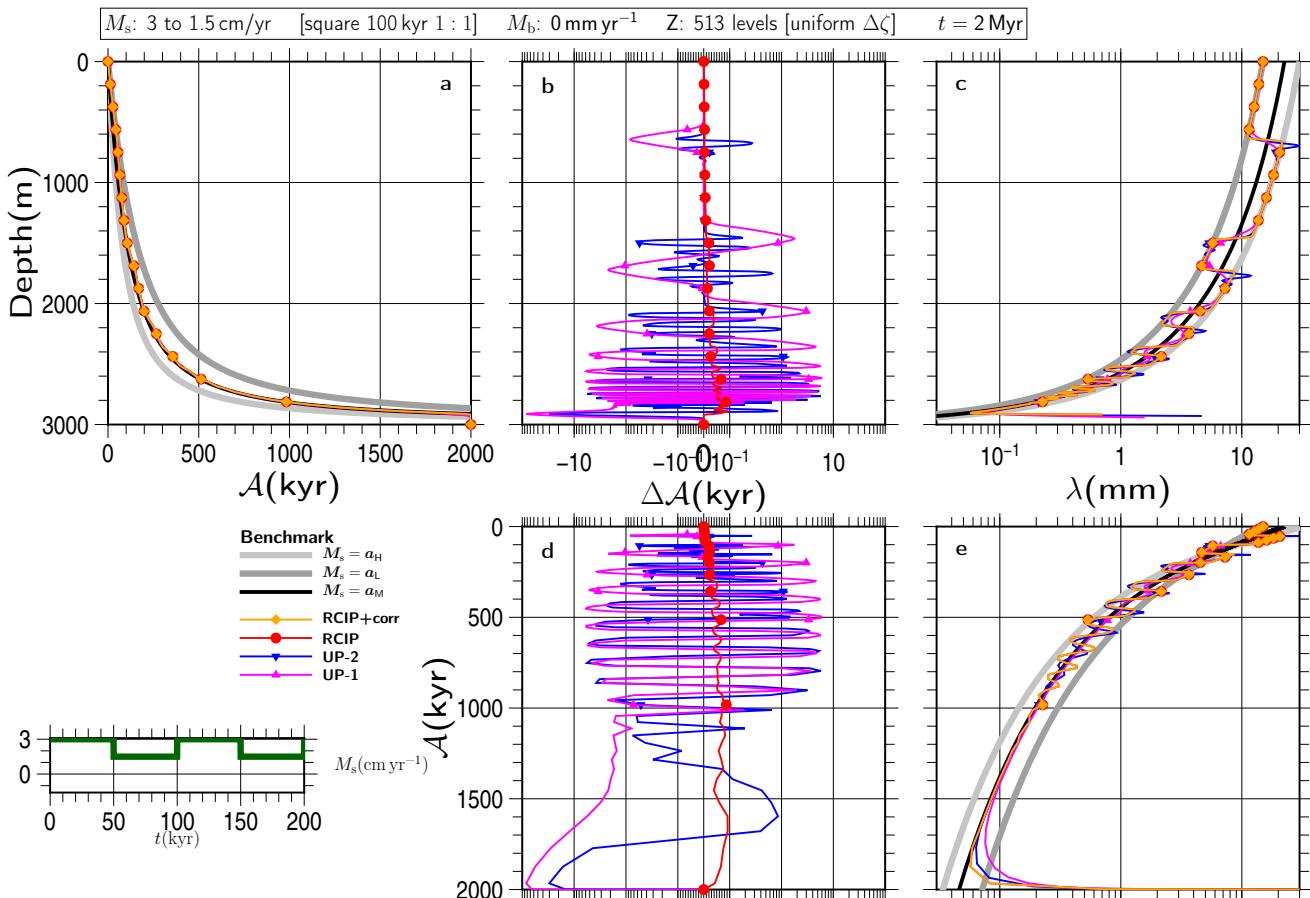


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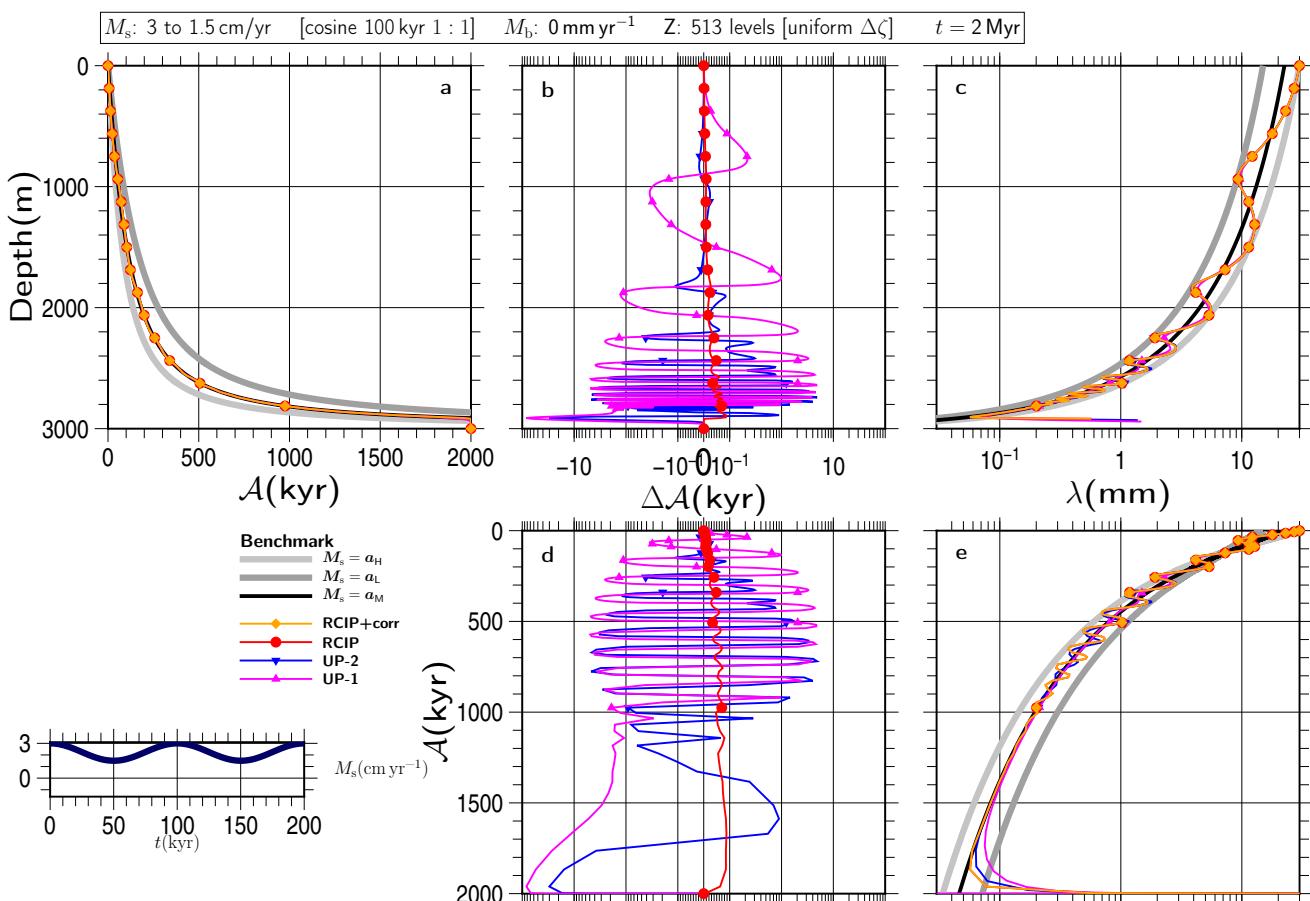


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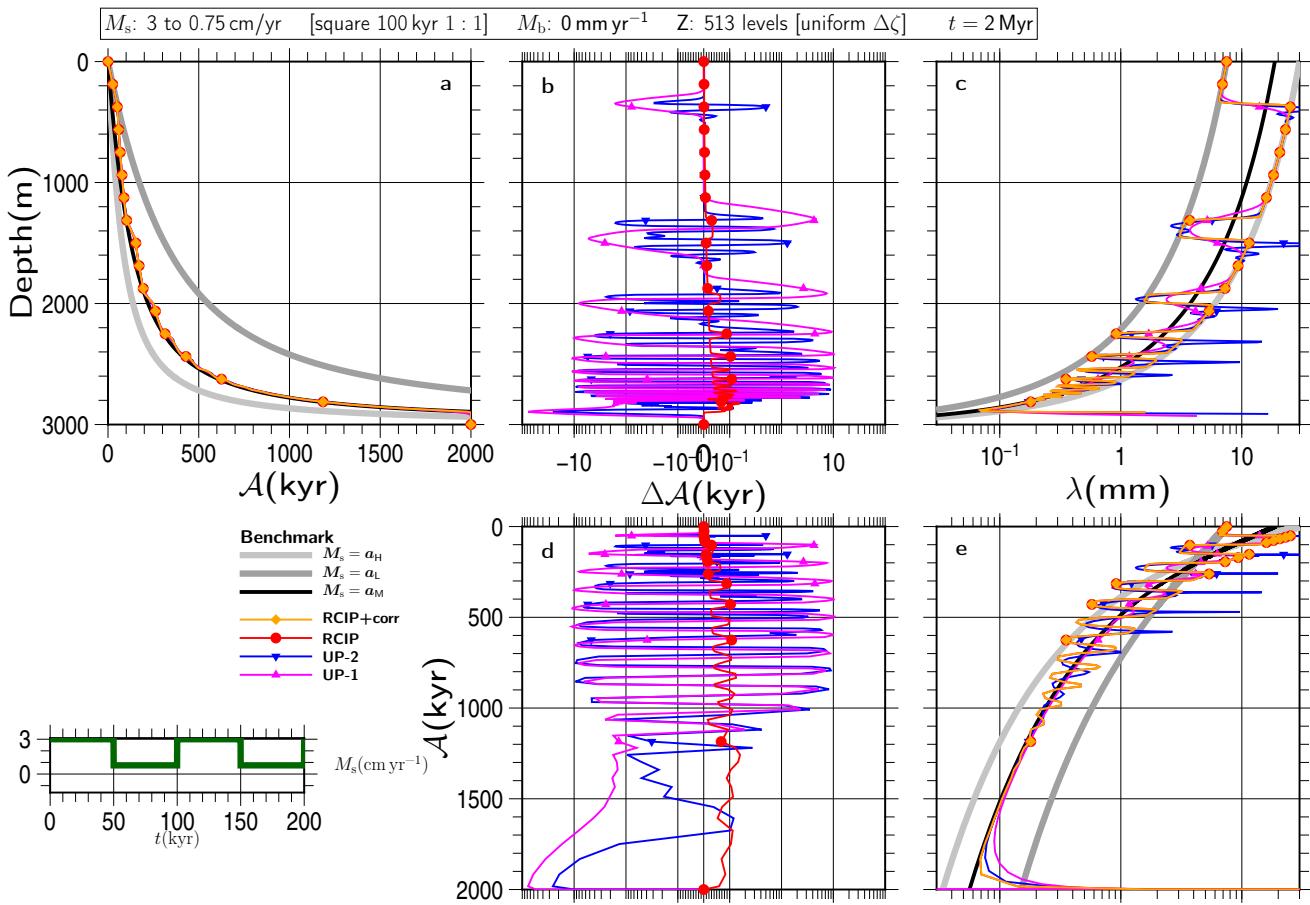


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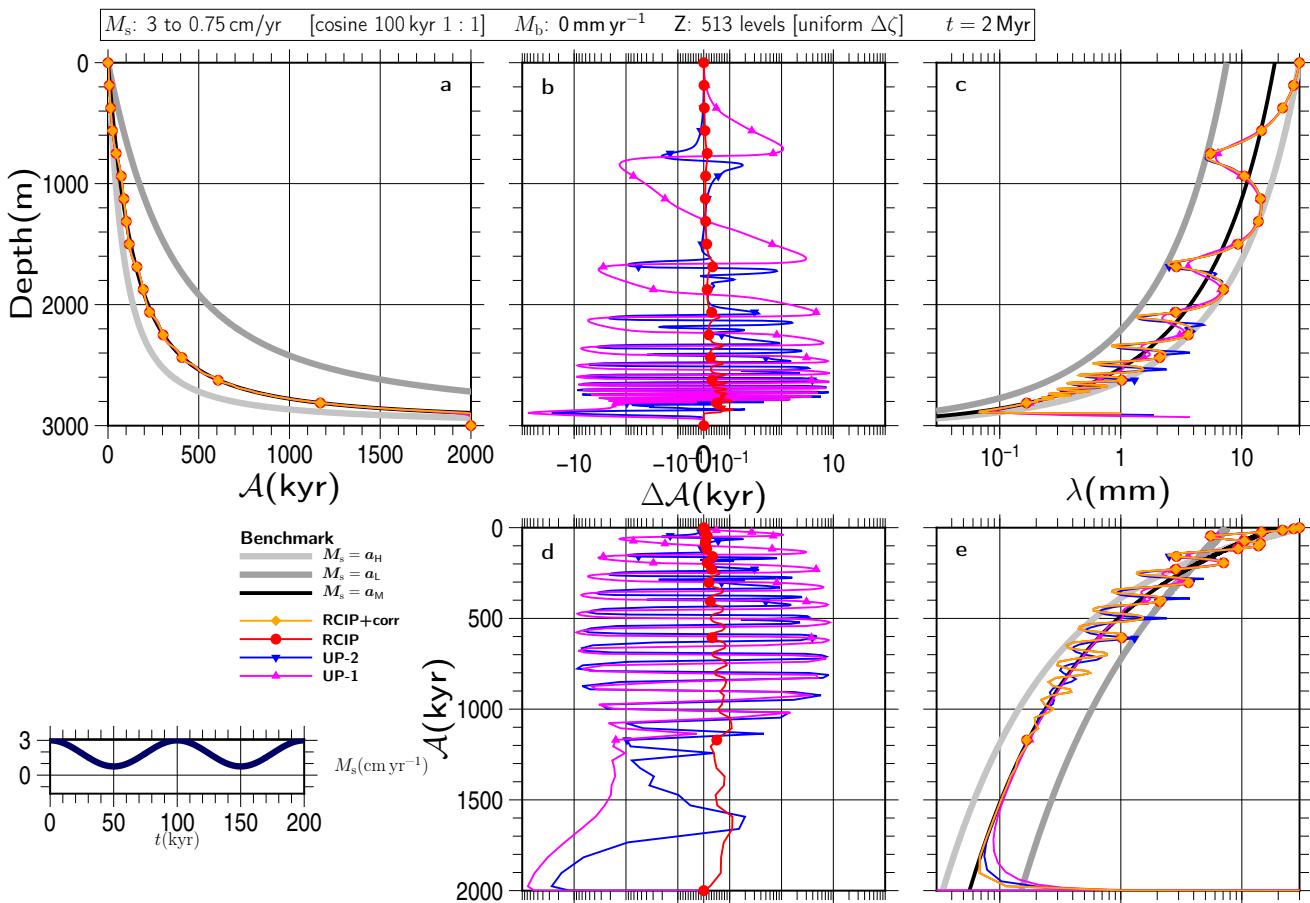


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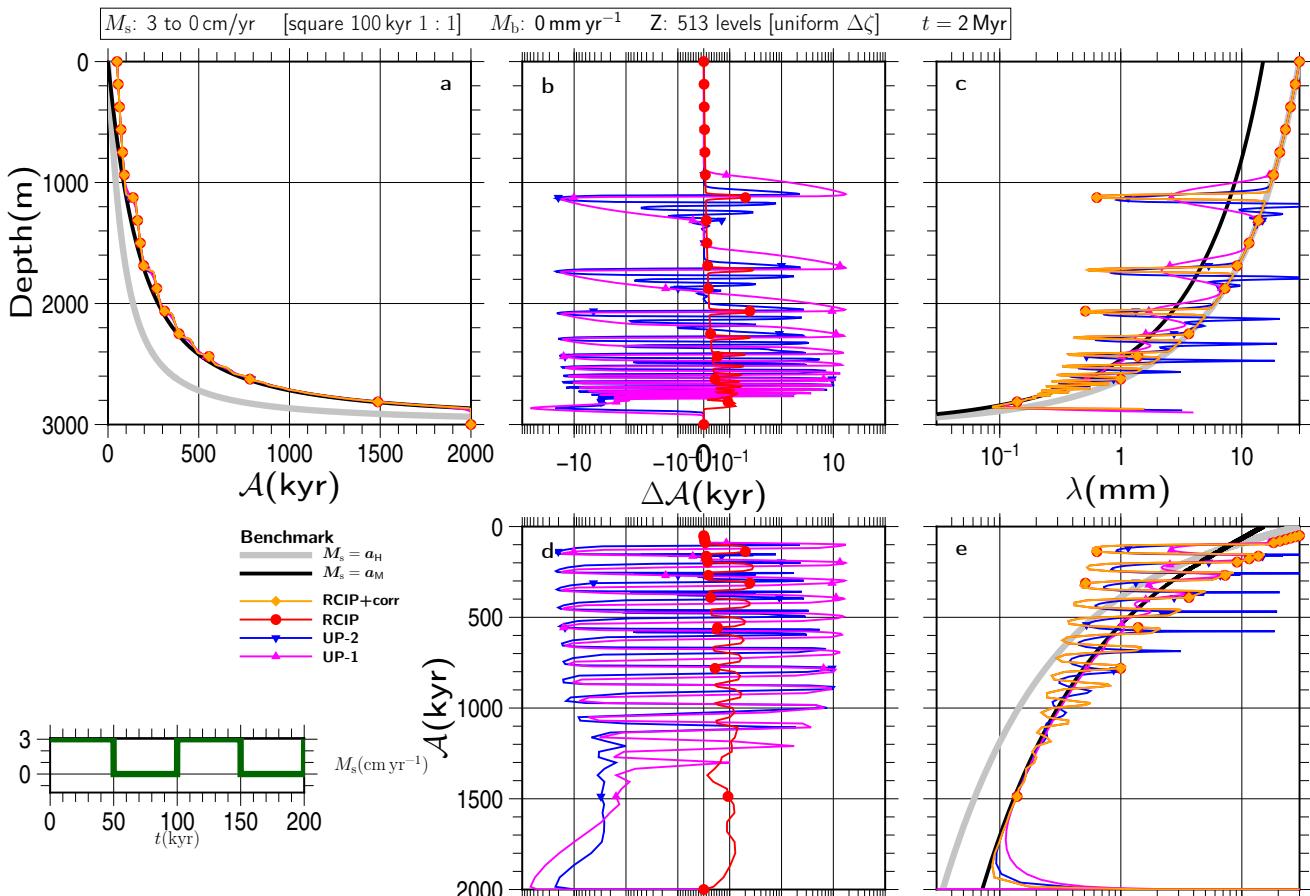


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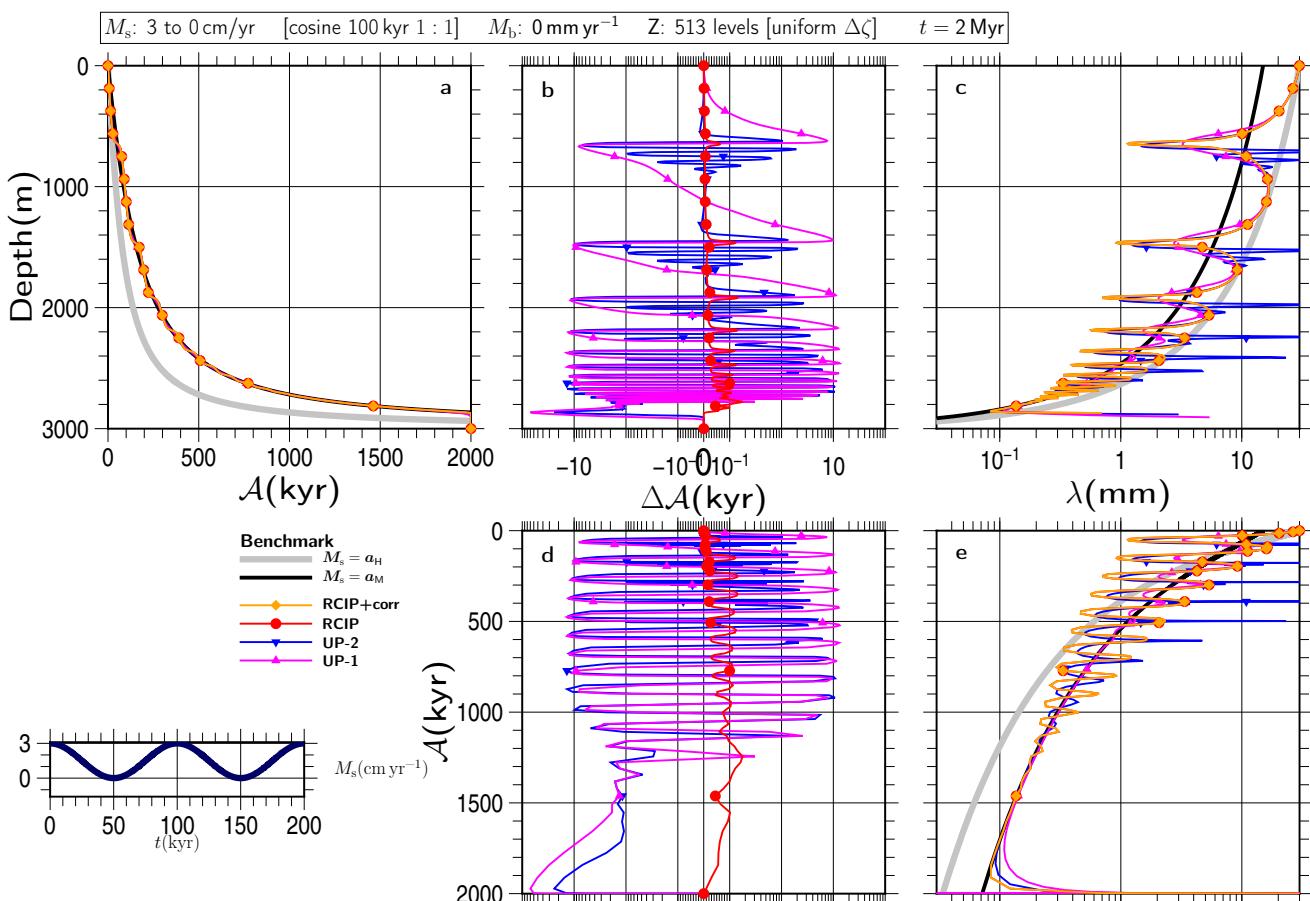


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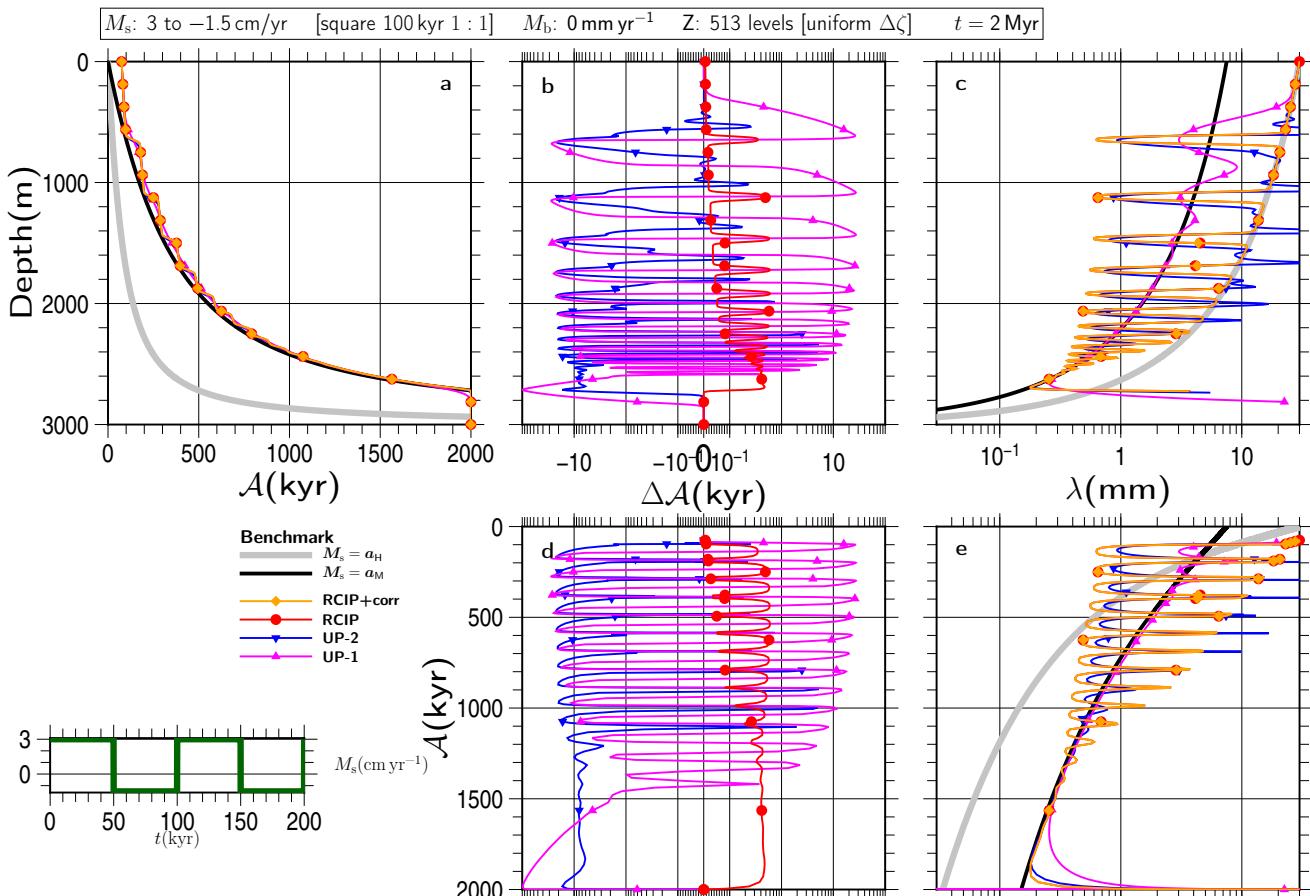


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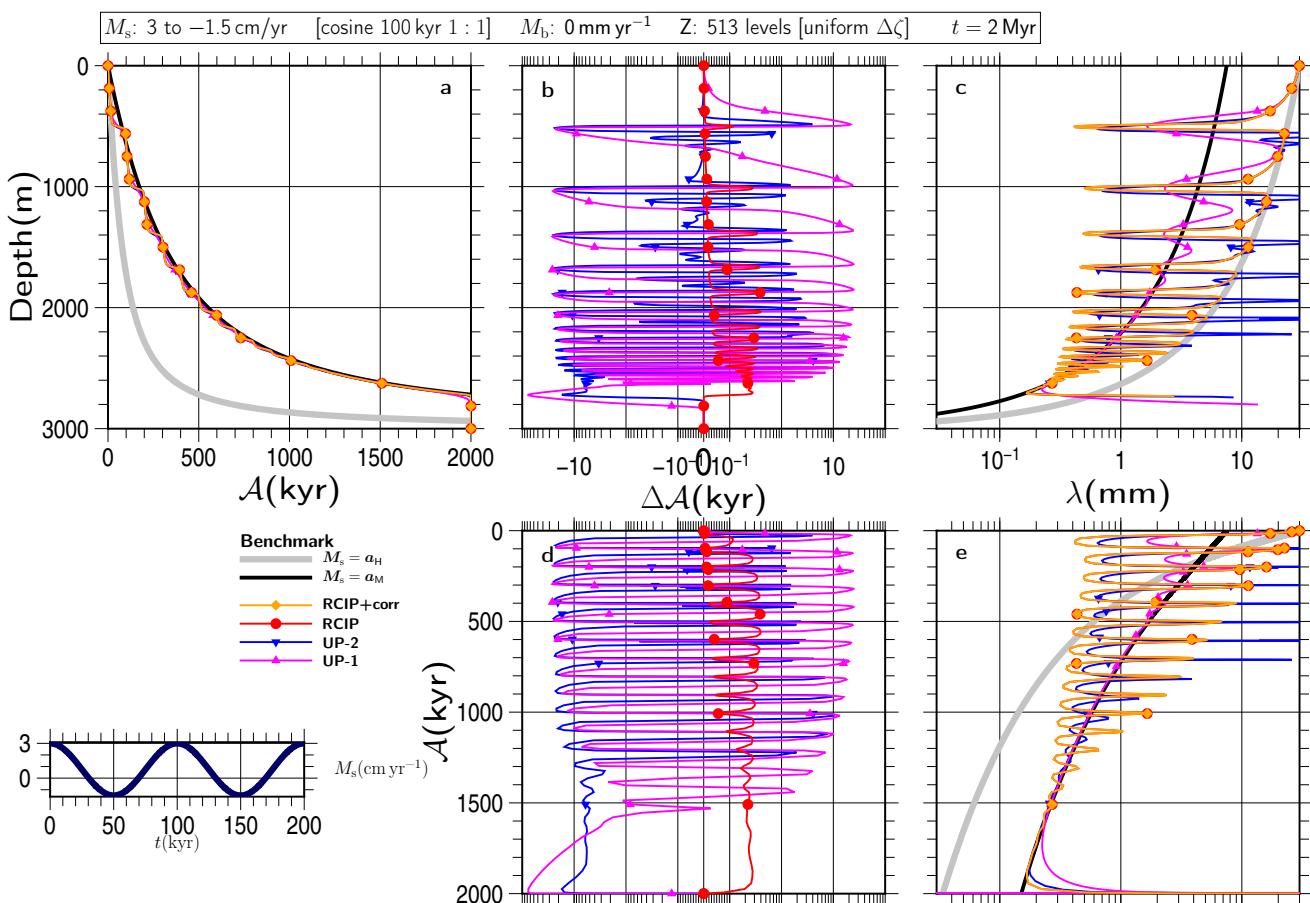


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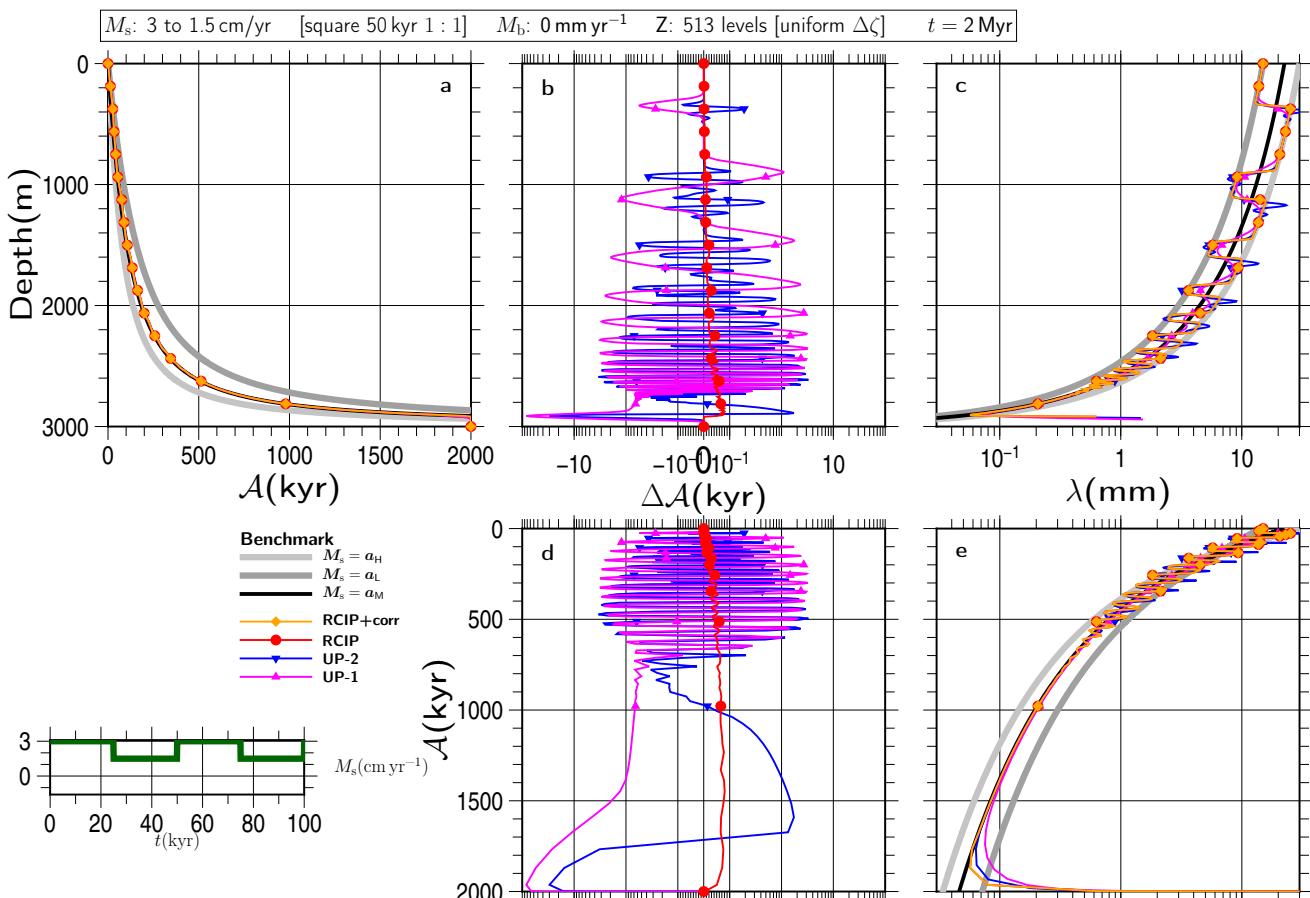


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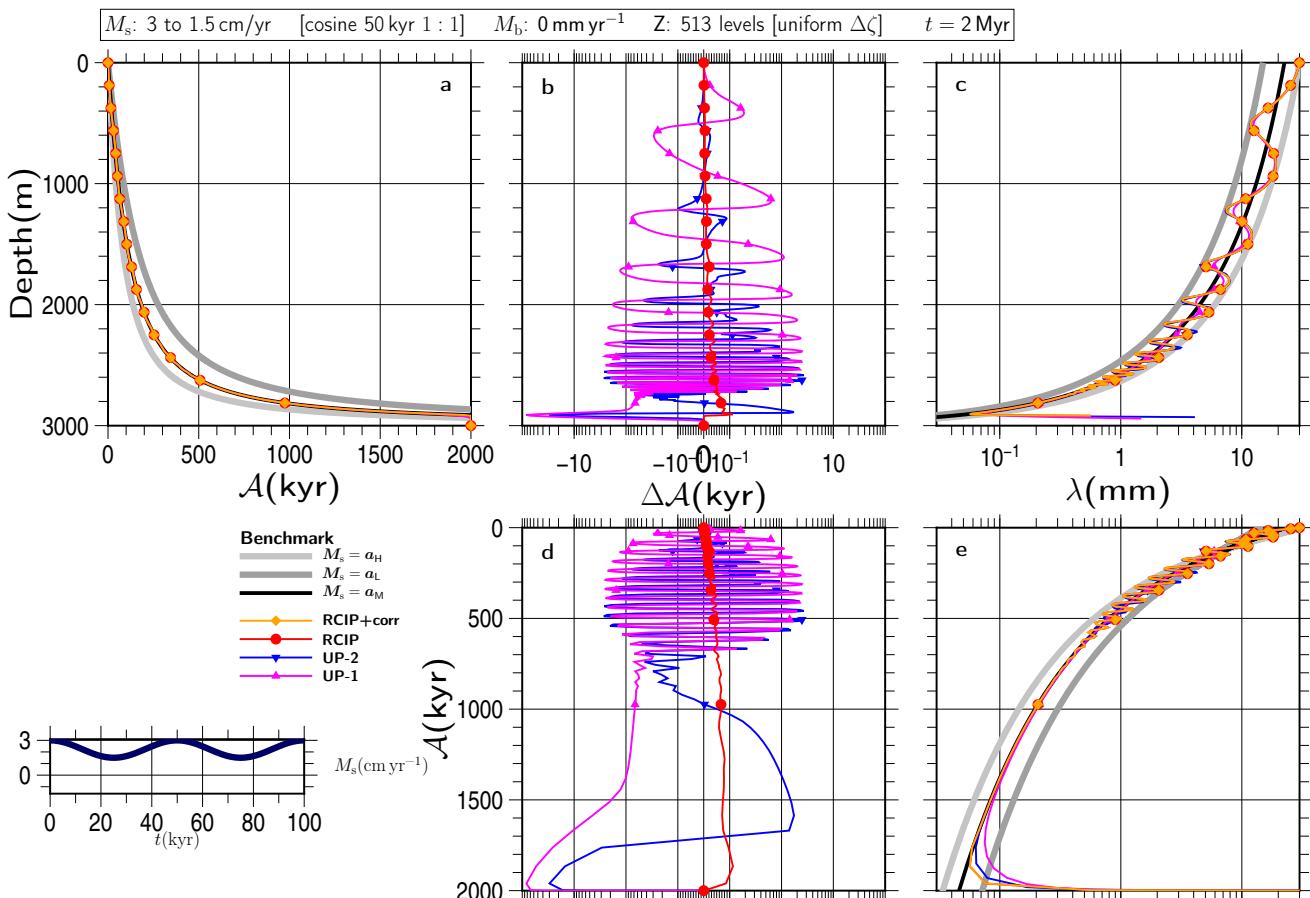


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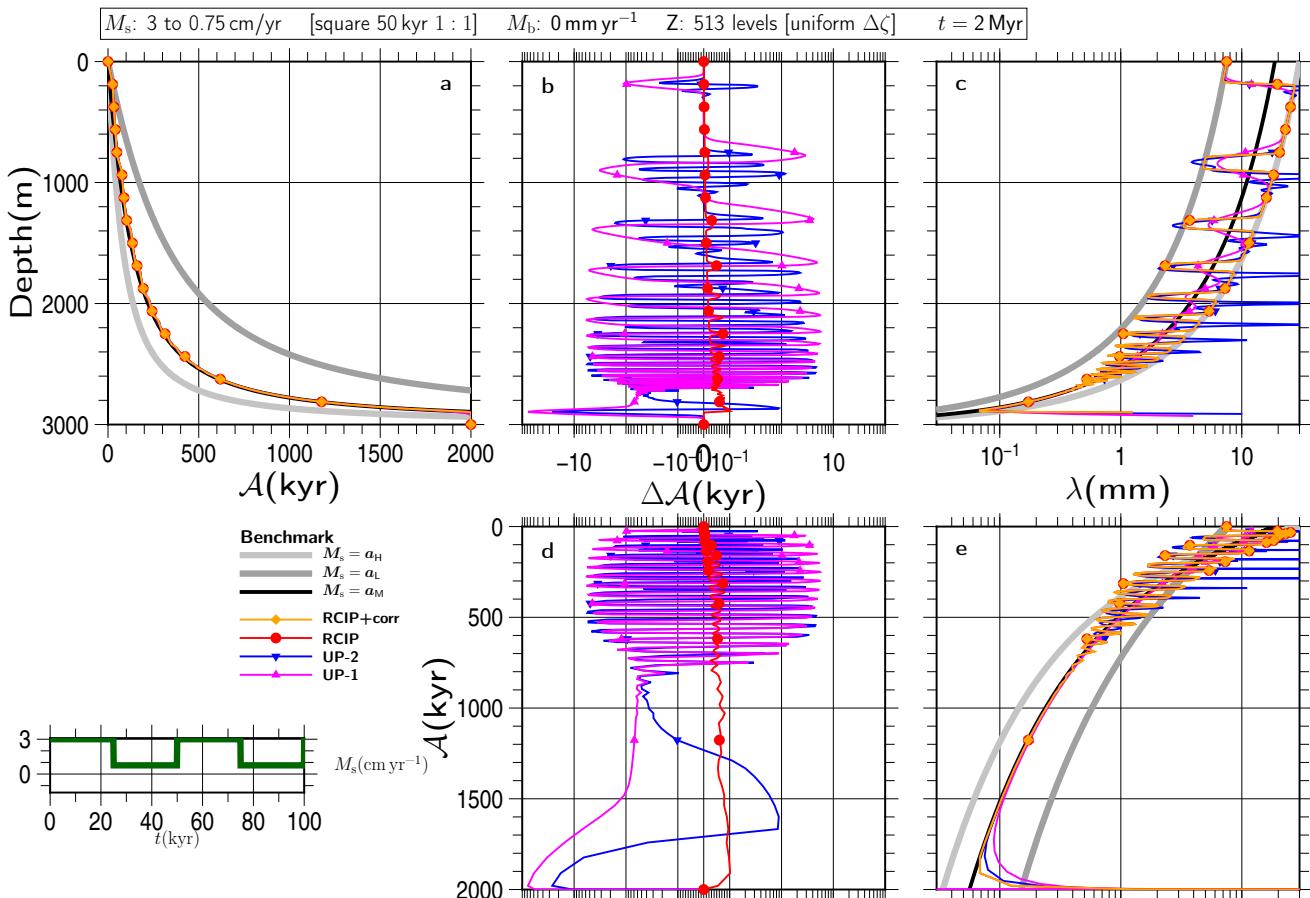


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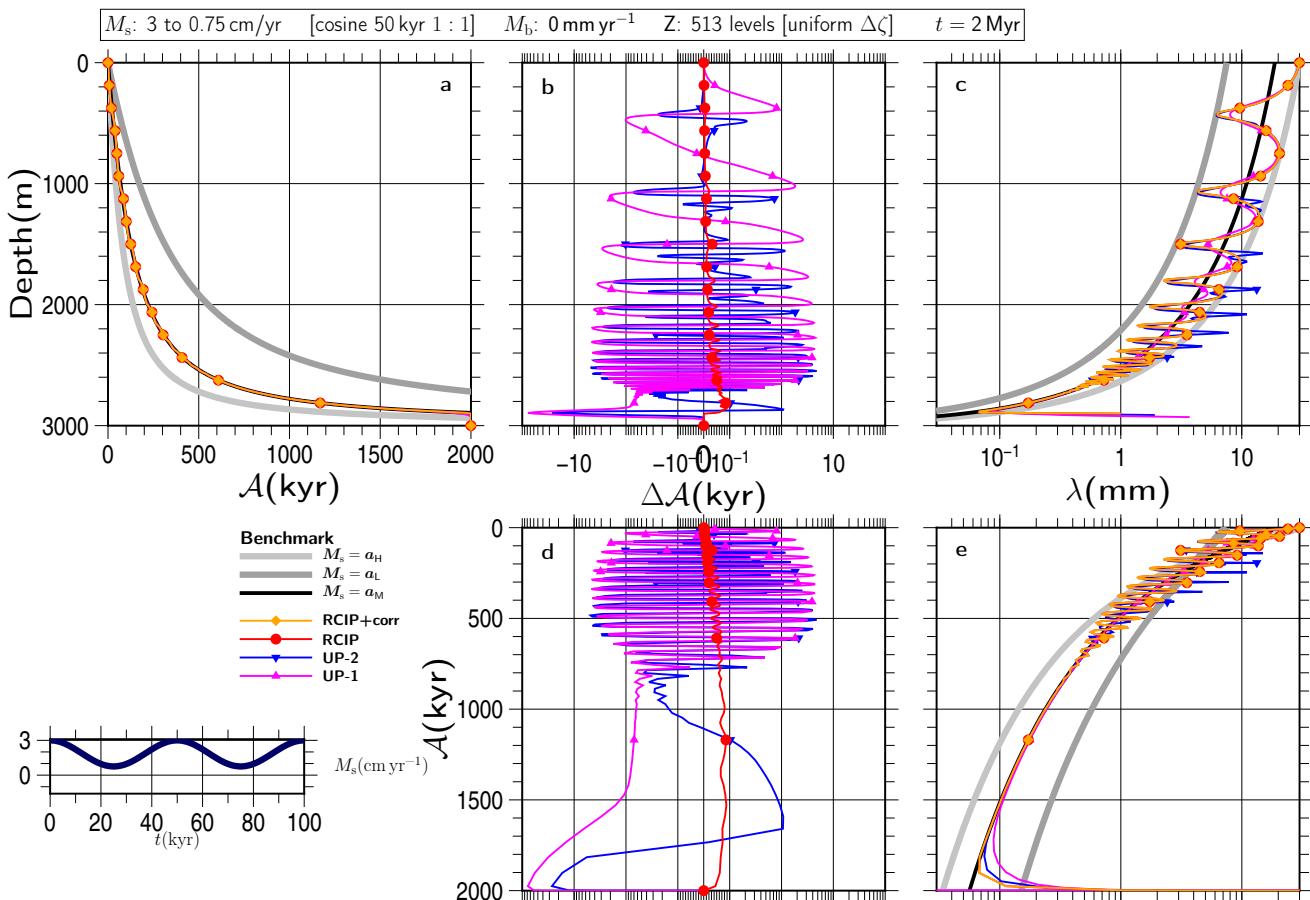


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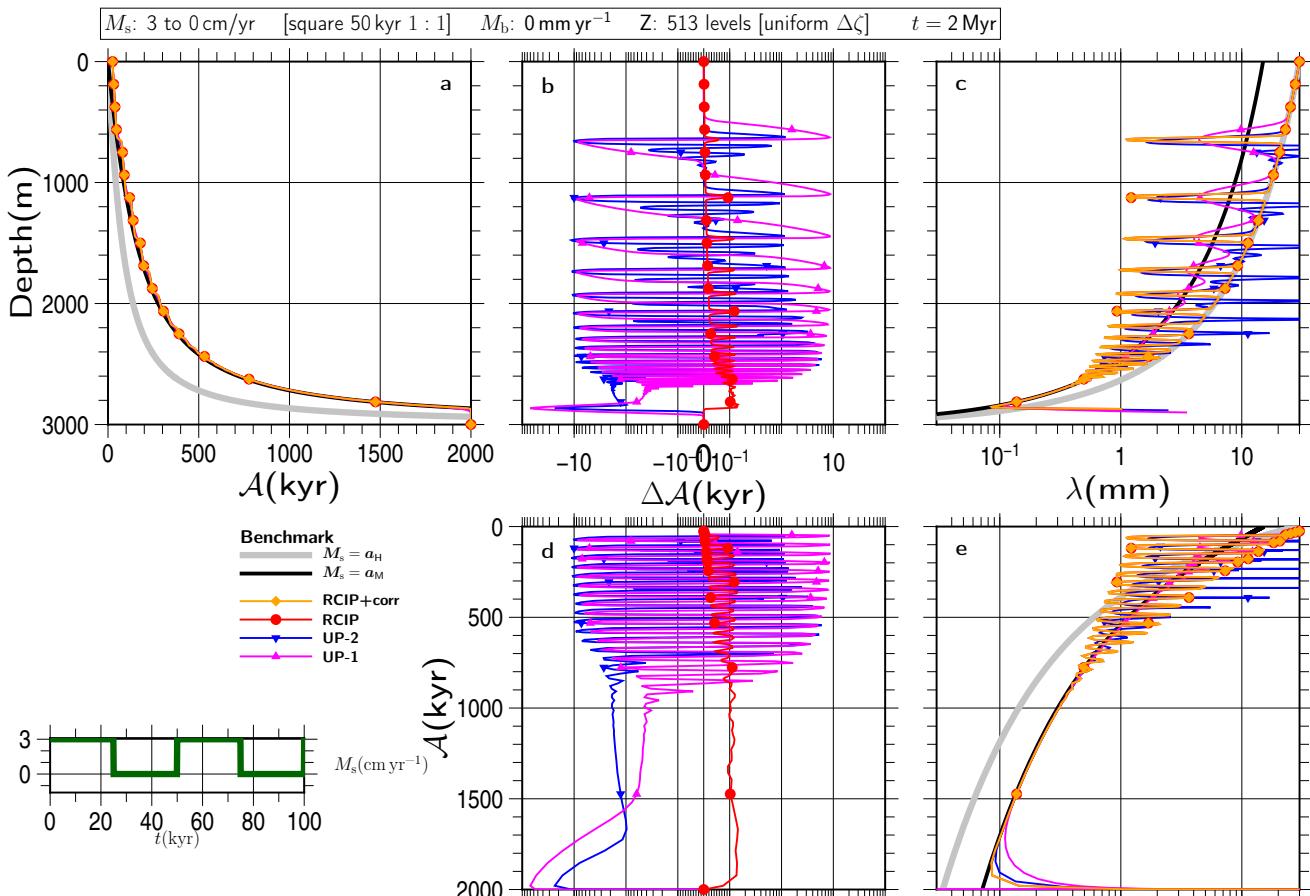


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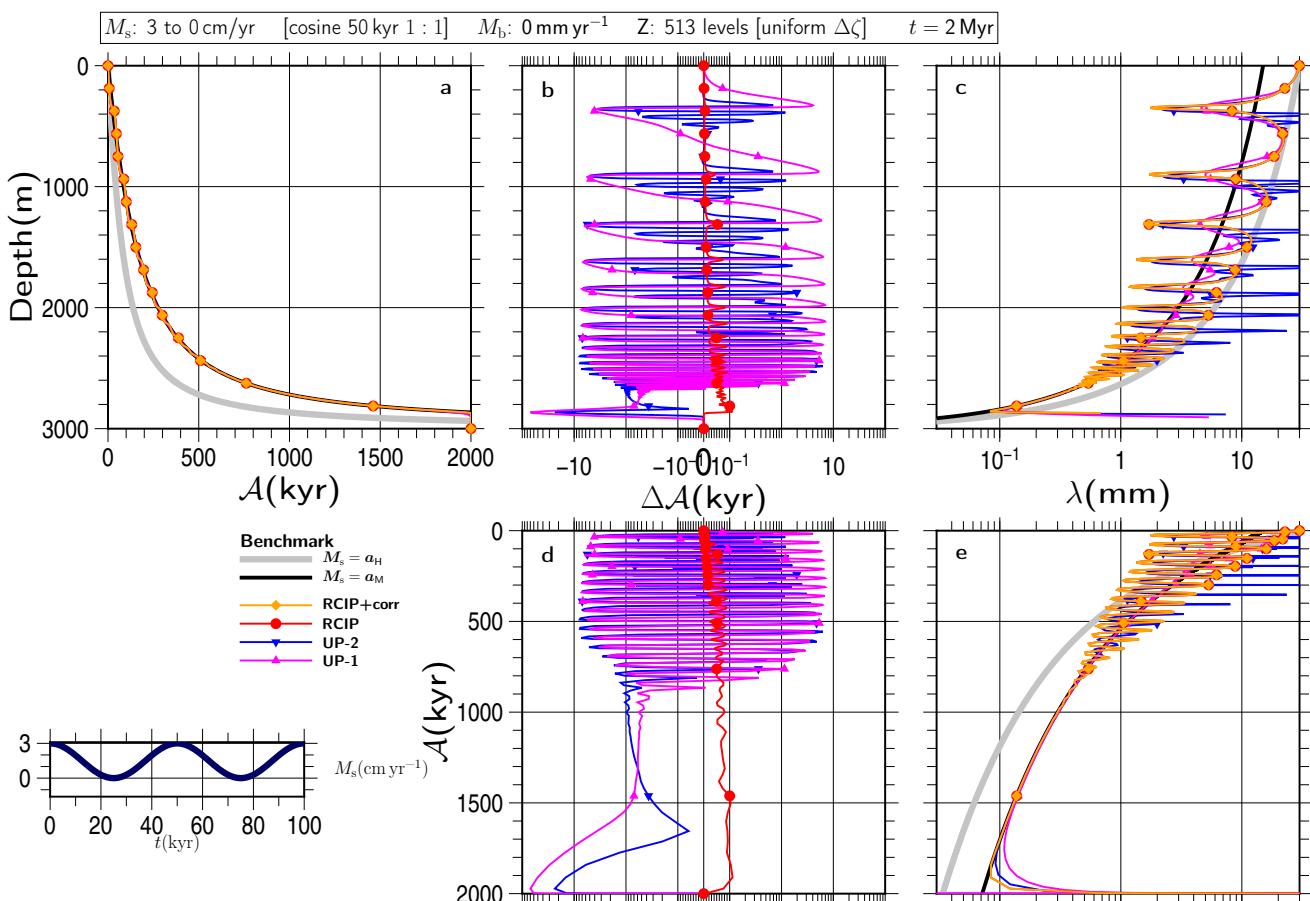


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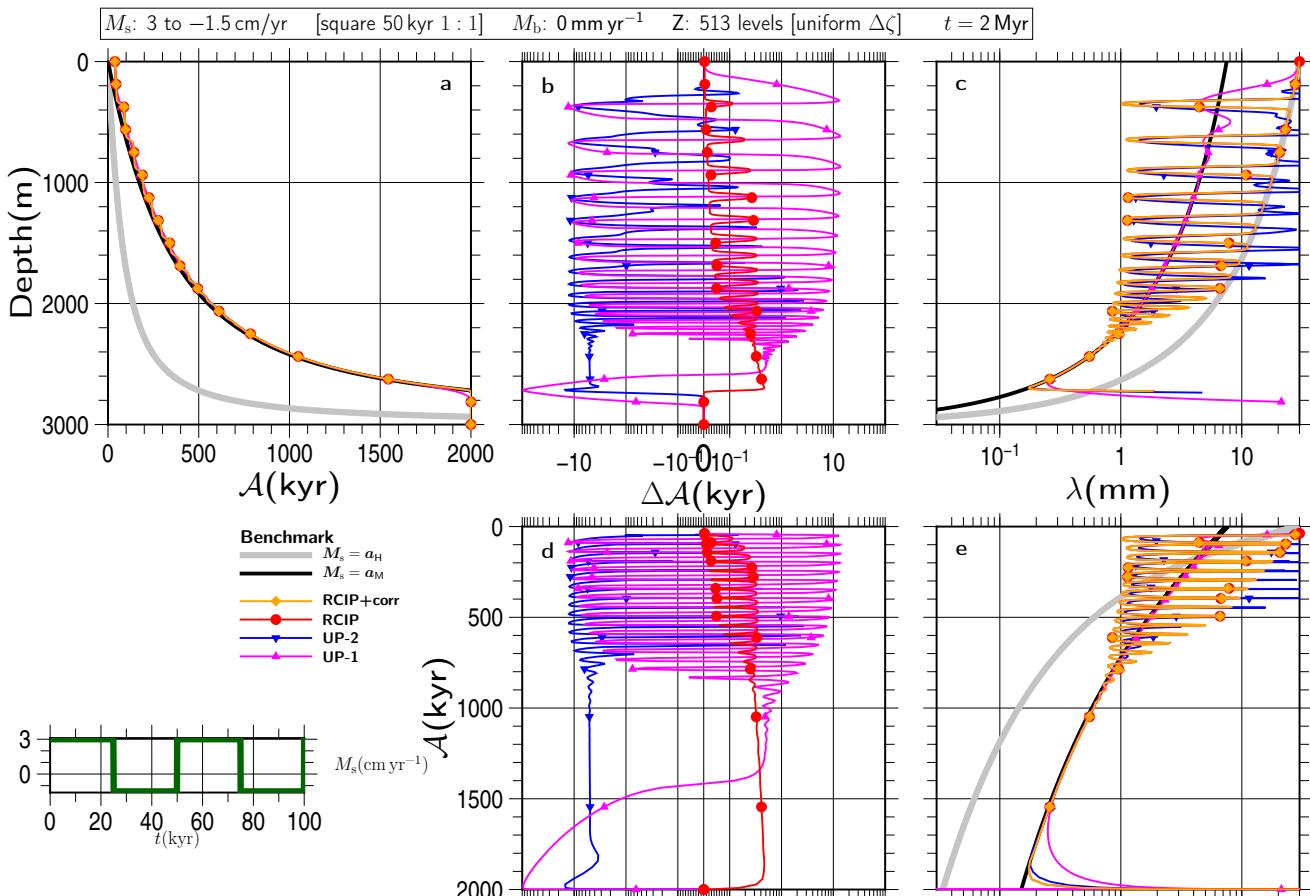


Figure S77

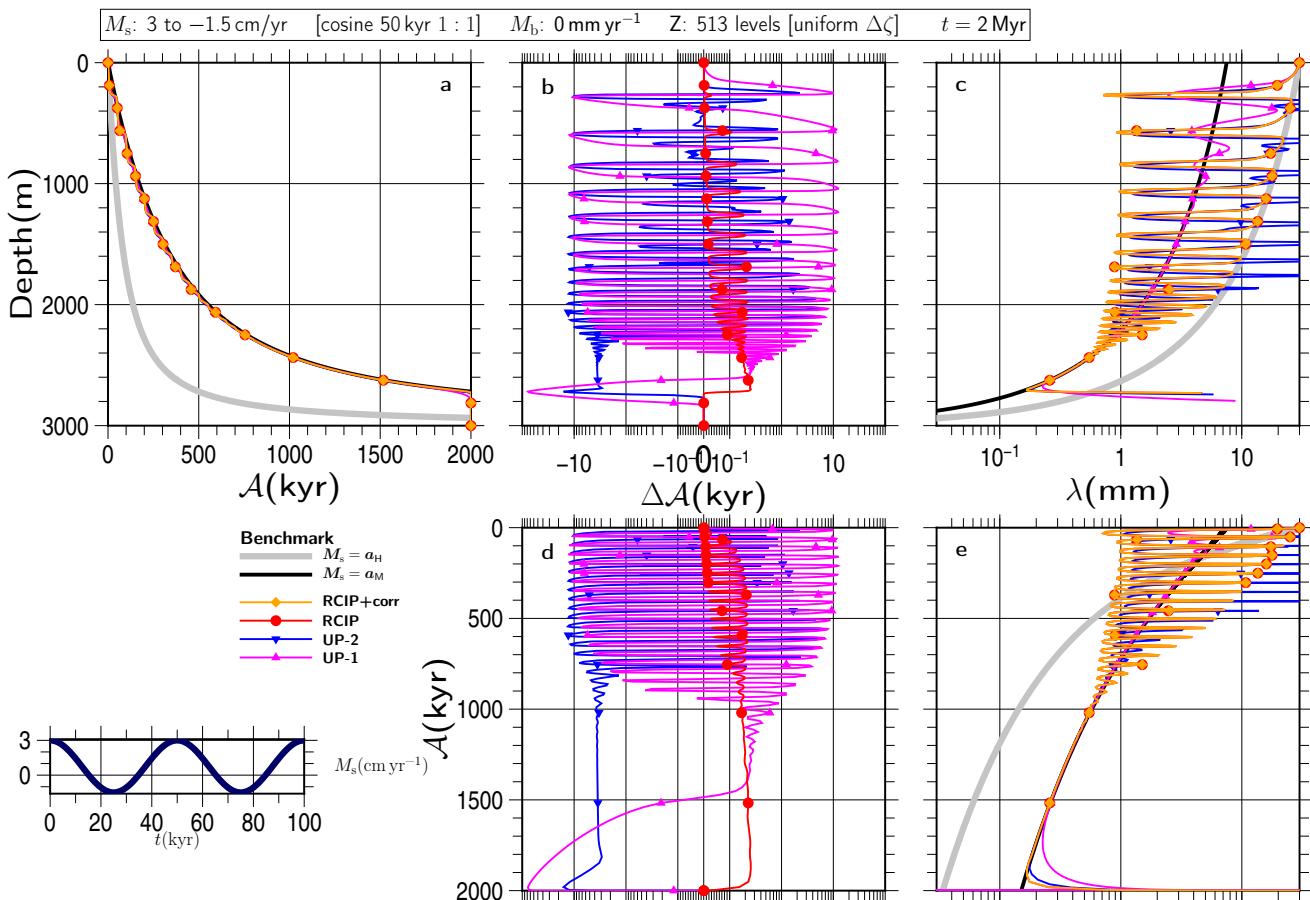


Figure S78

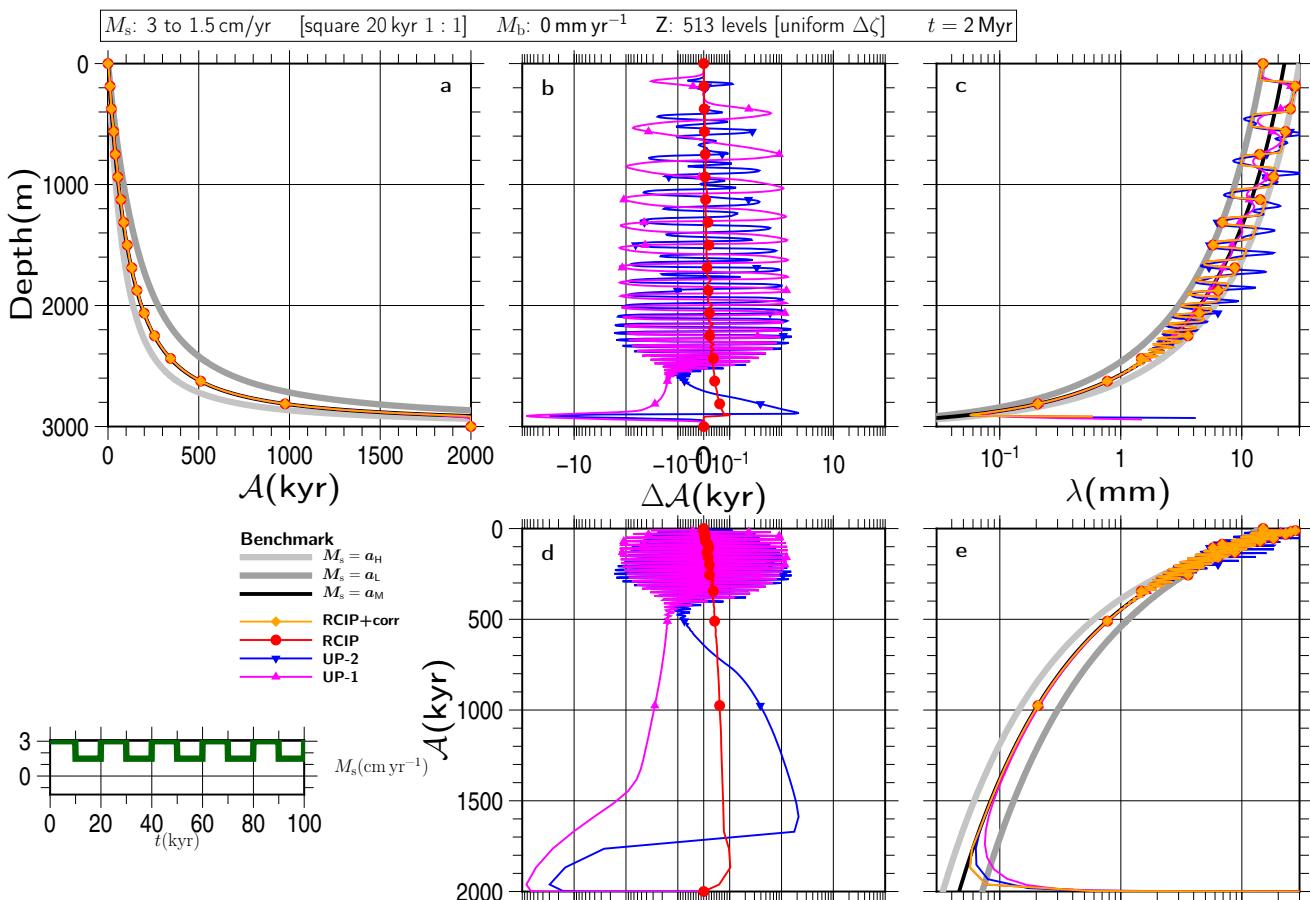


Figure S79

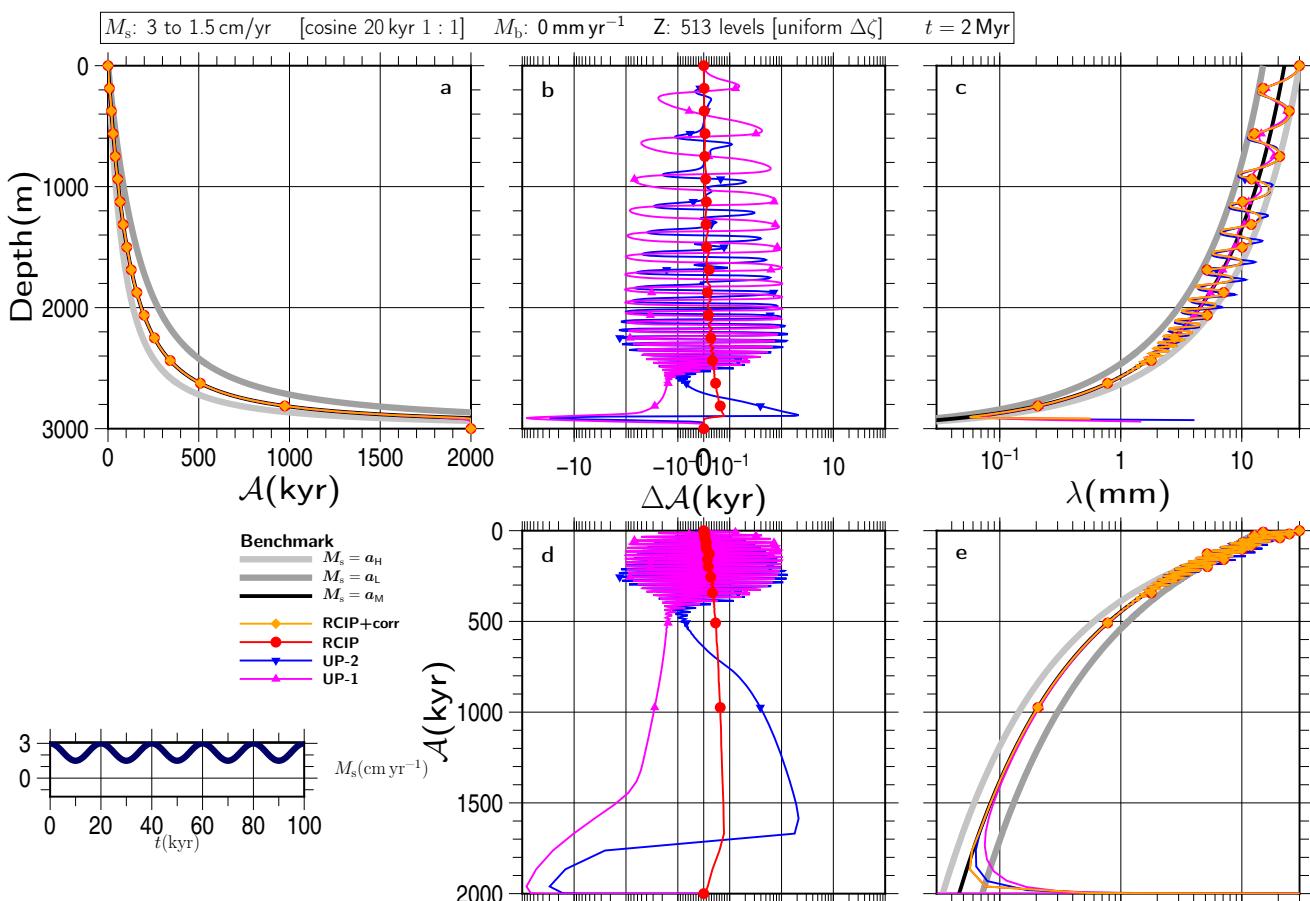


Figure S80

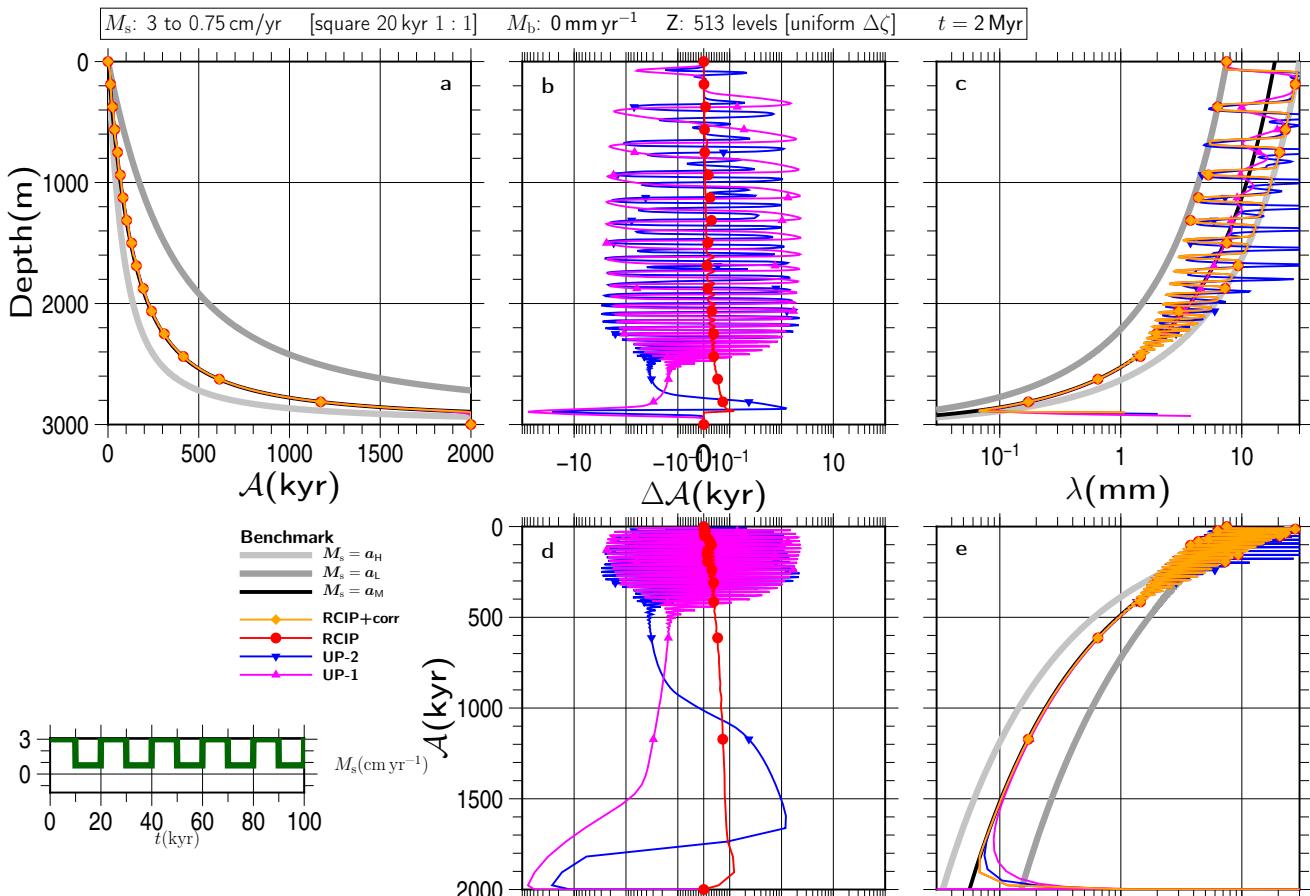


Figure S81

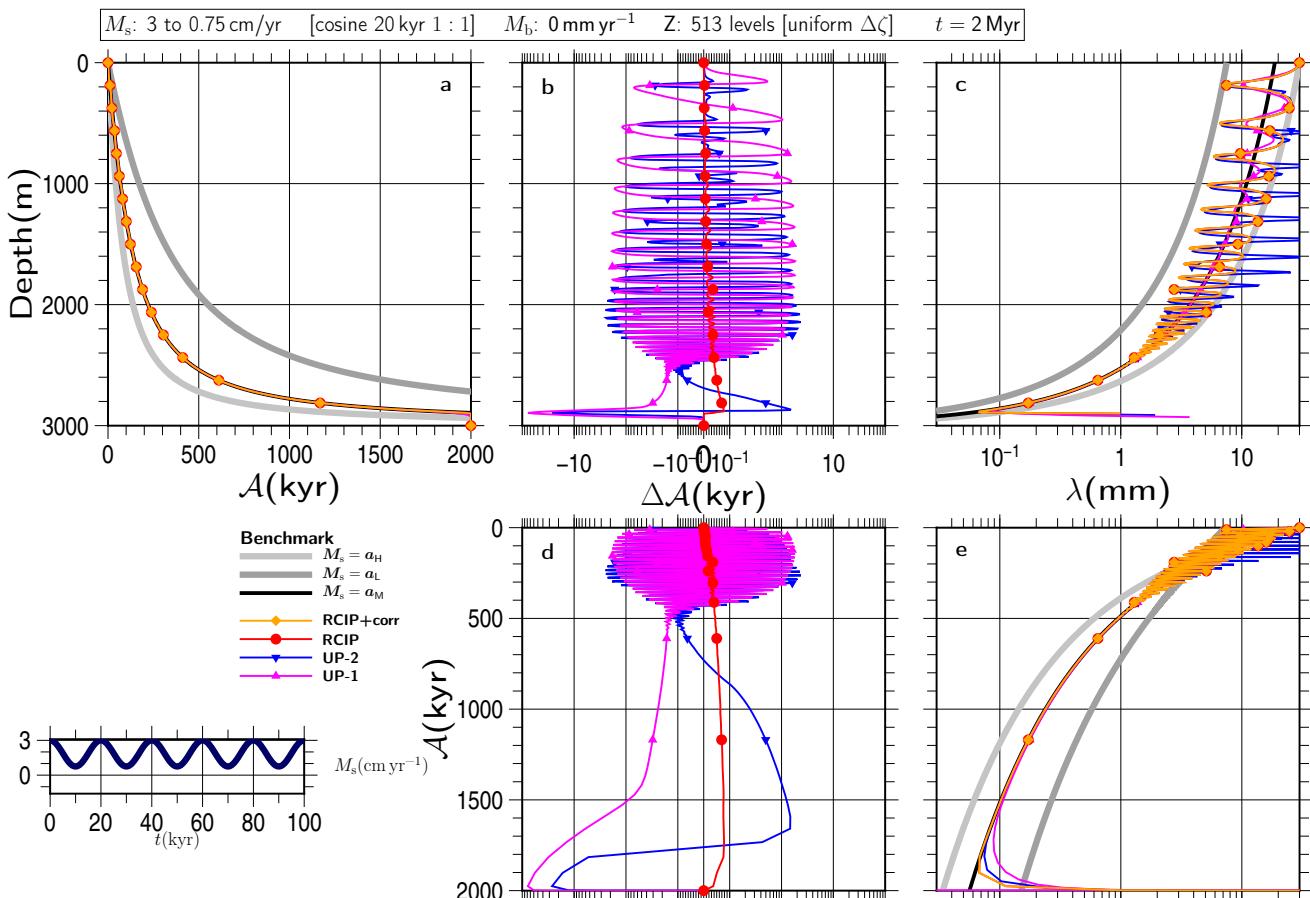


Figure S82

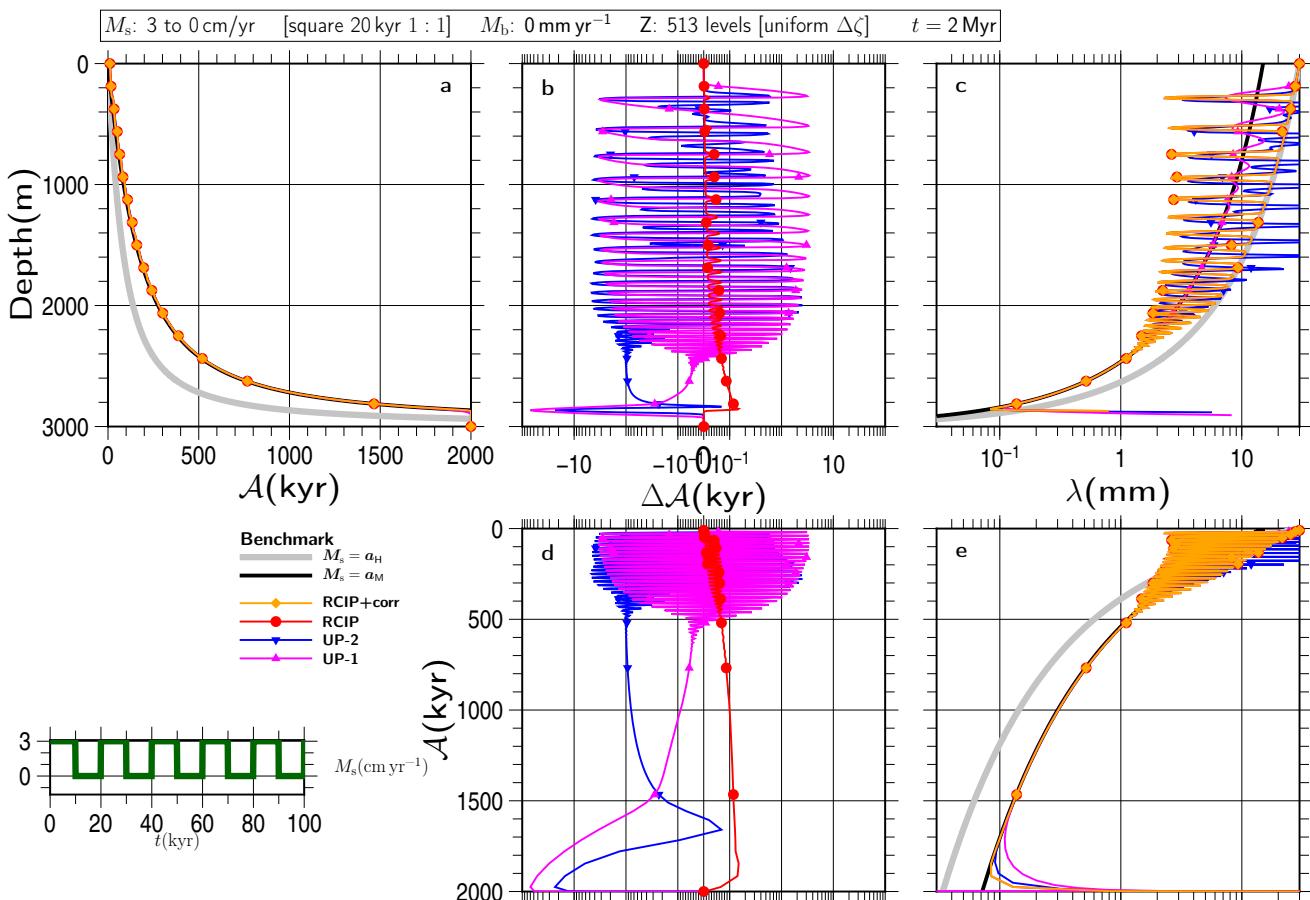


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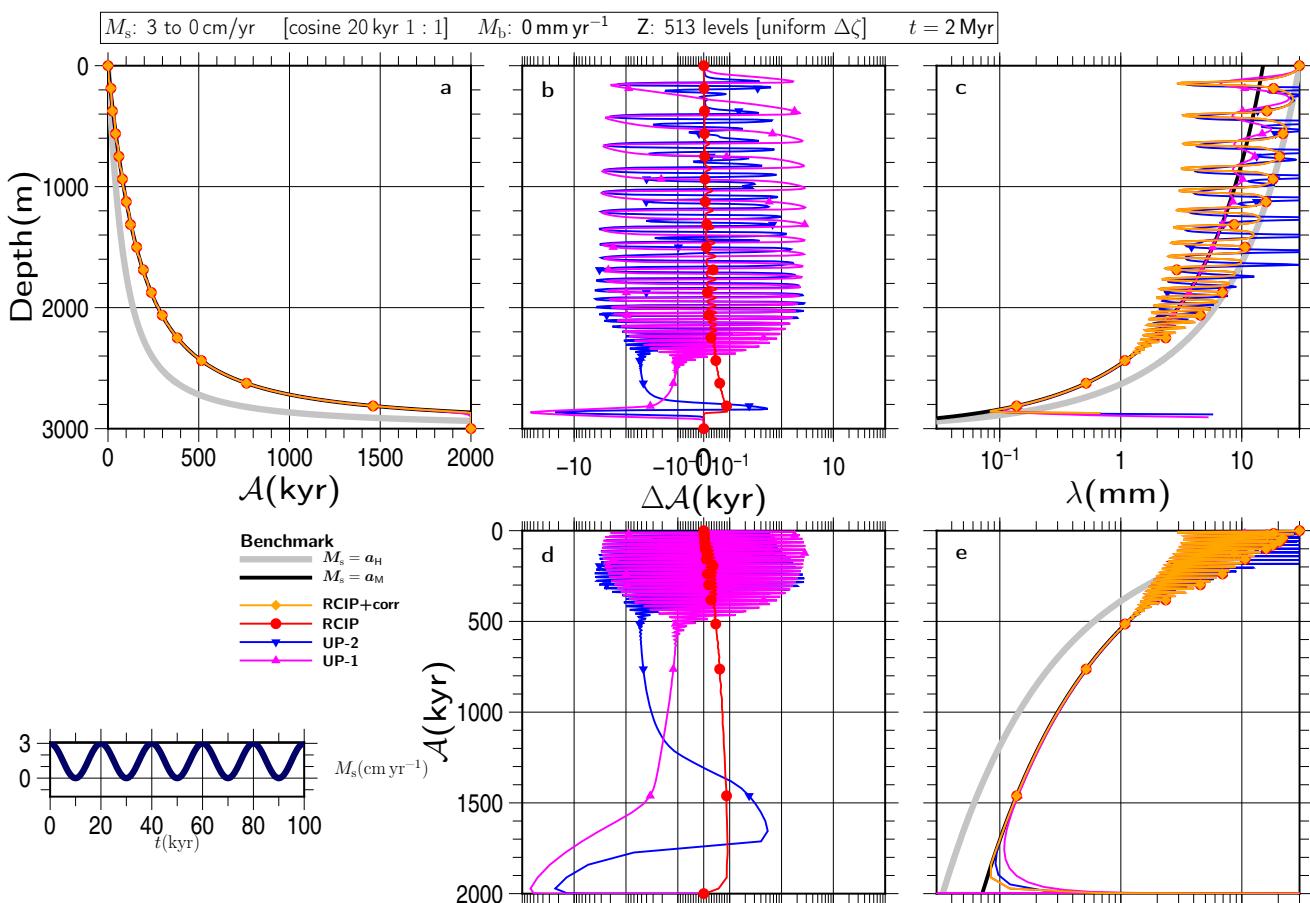


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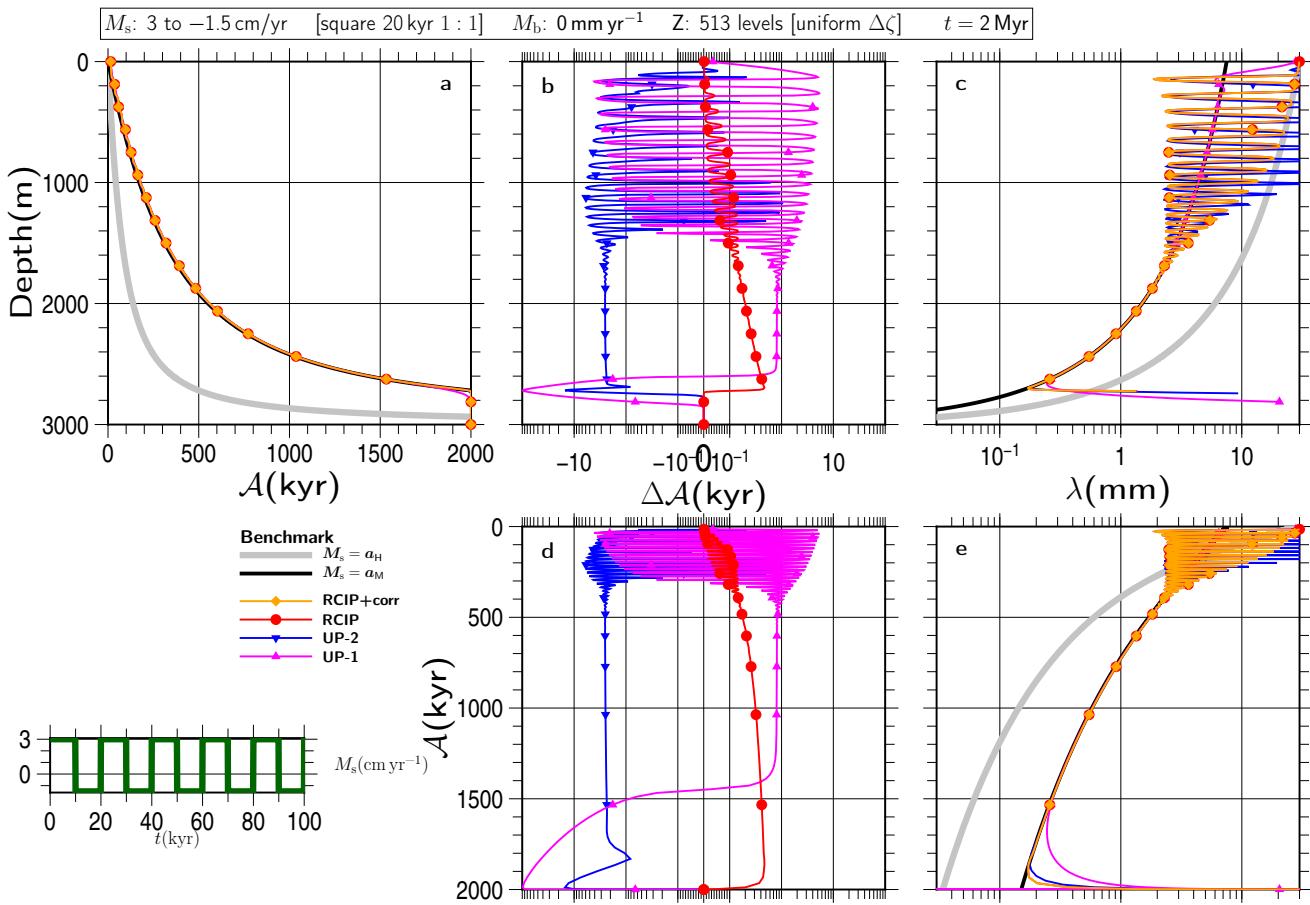


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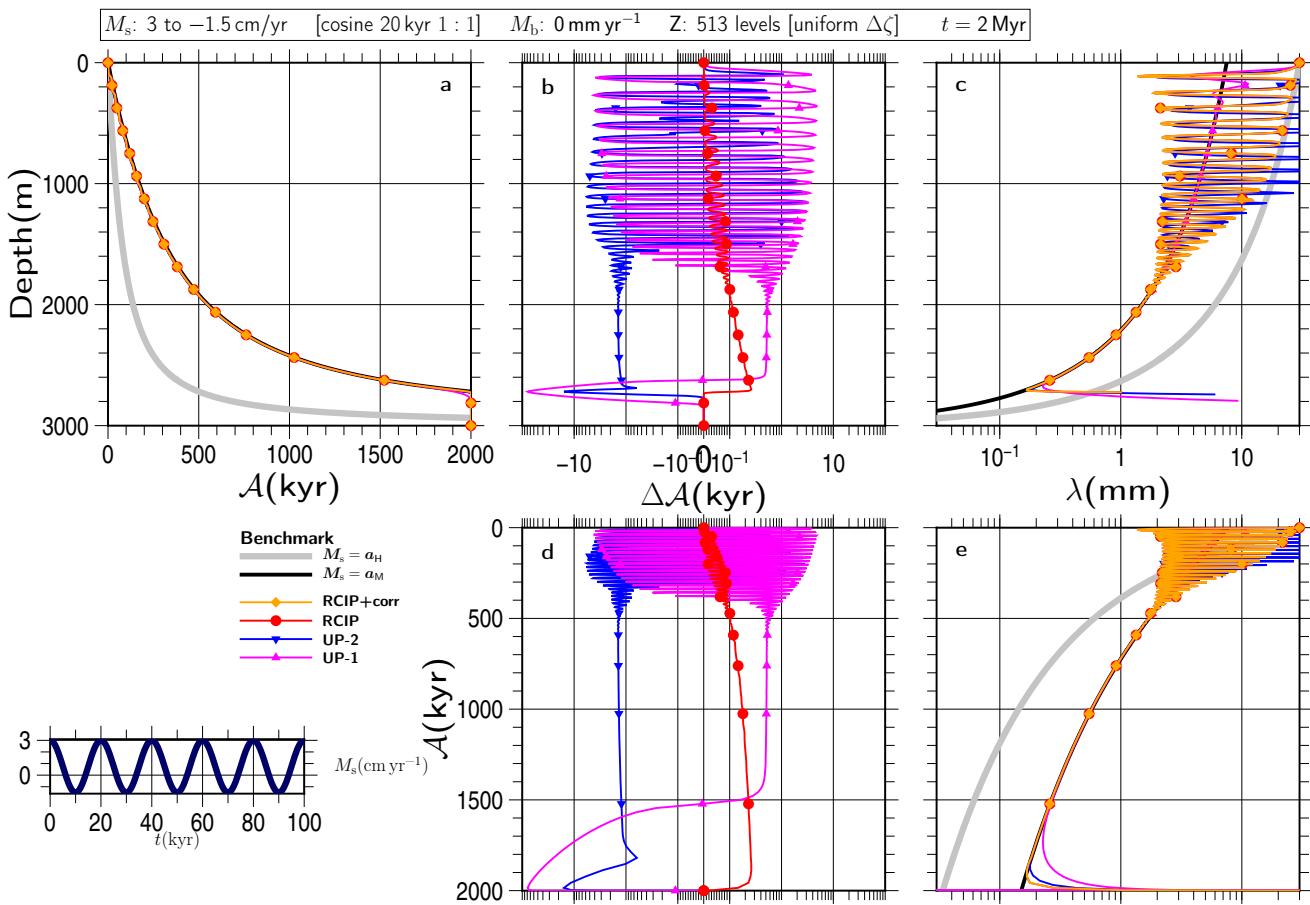


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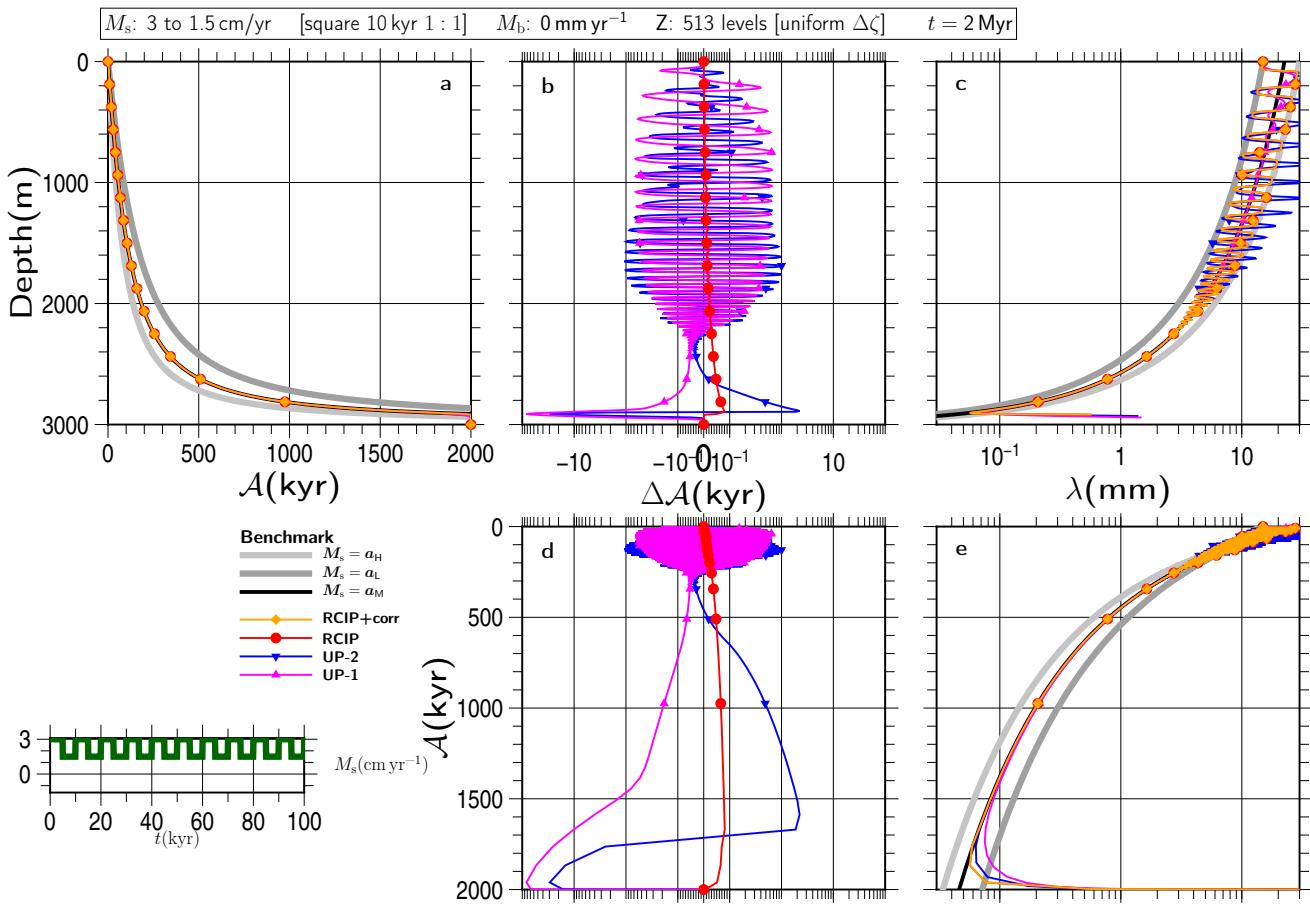


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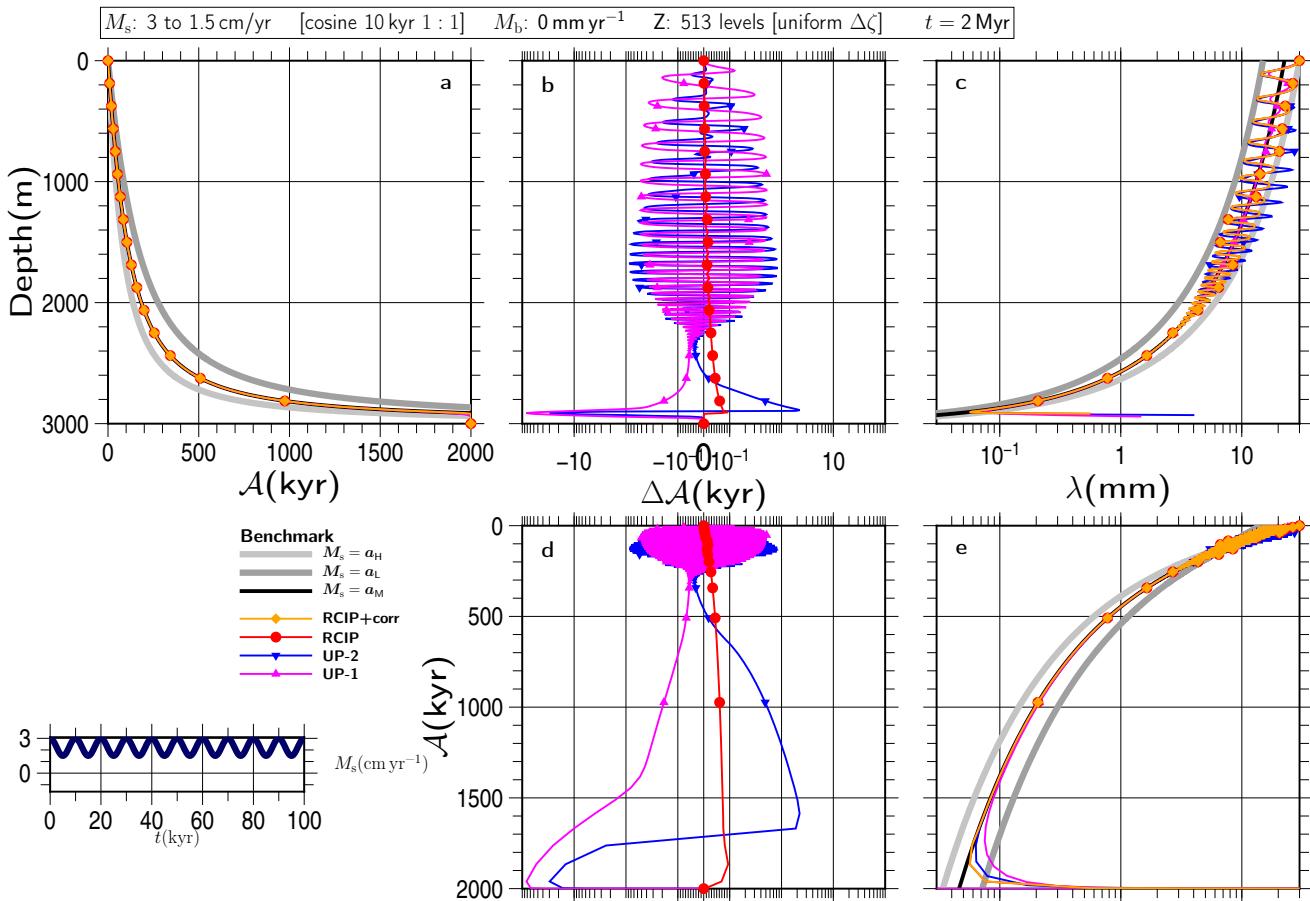


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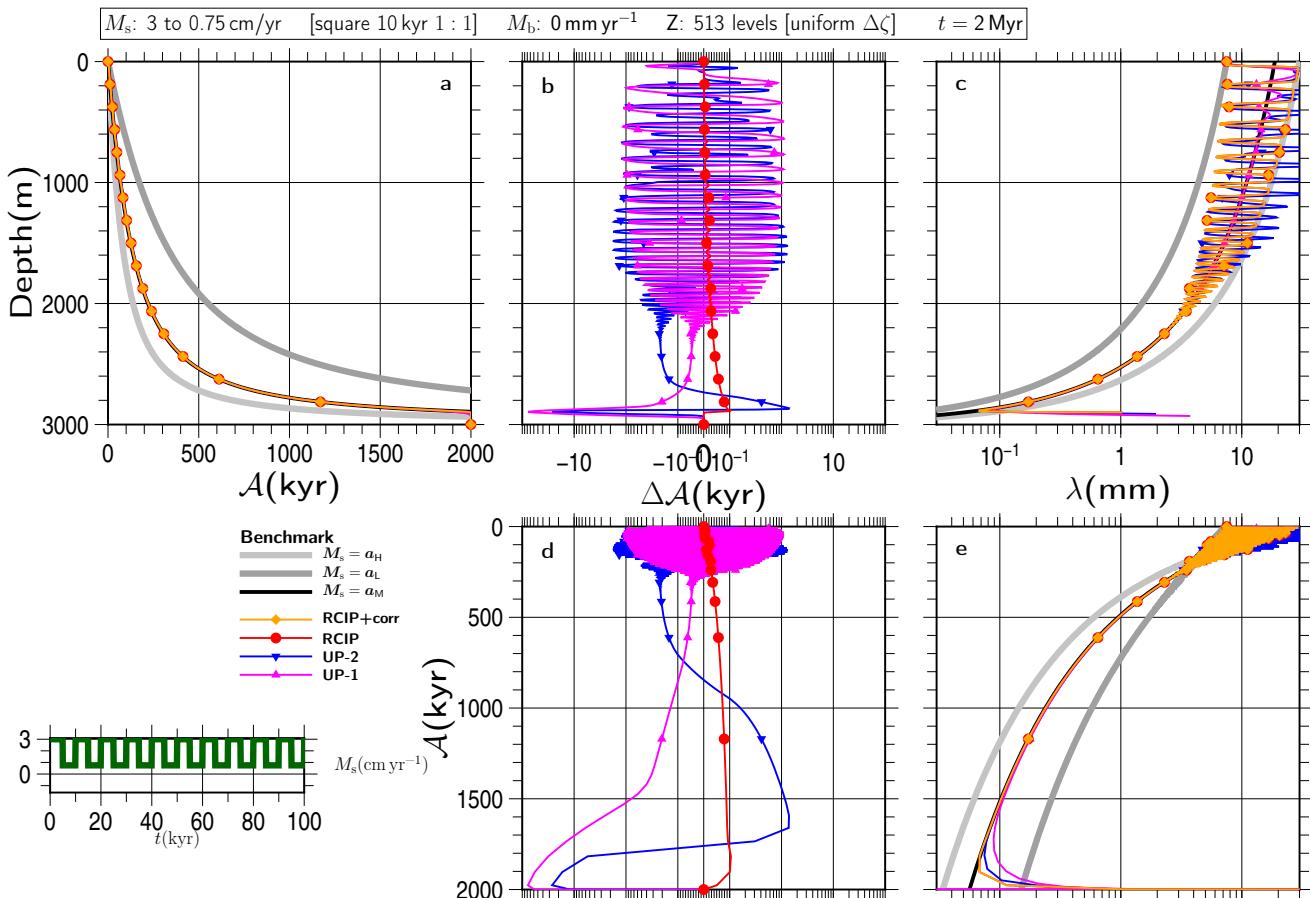


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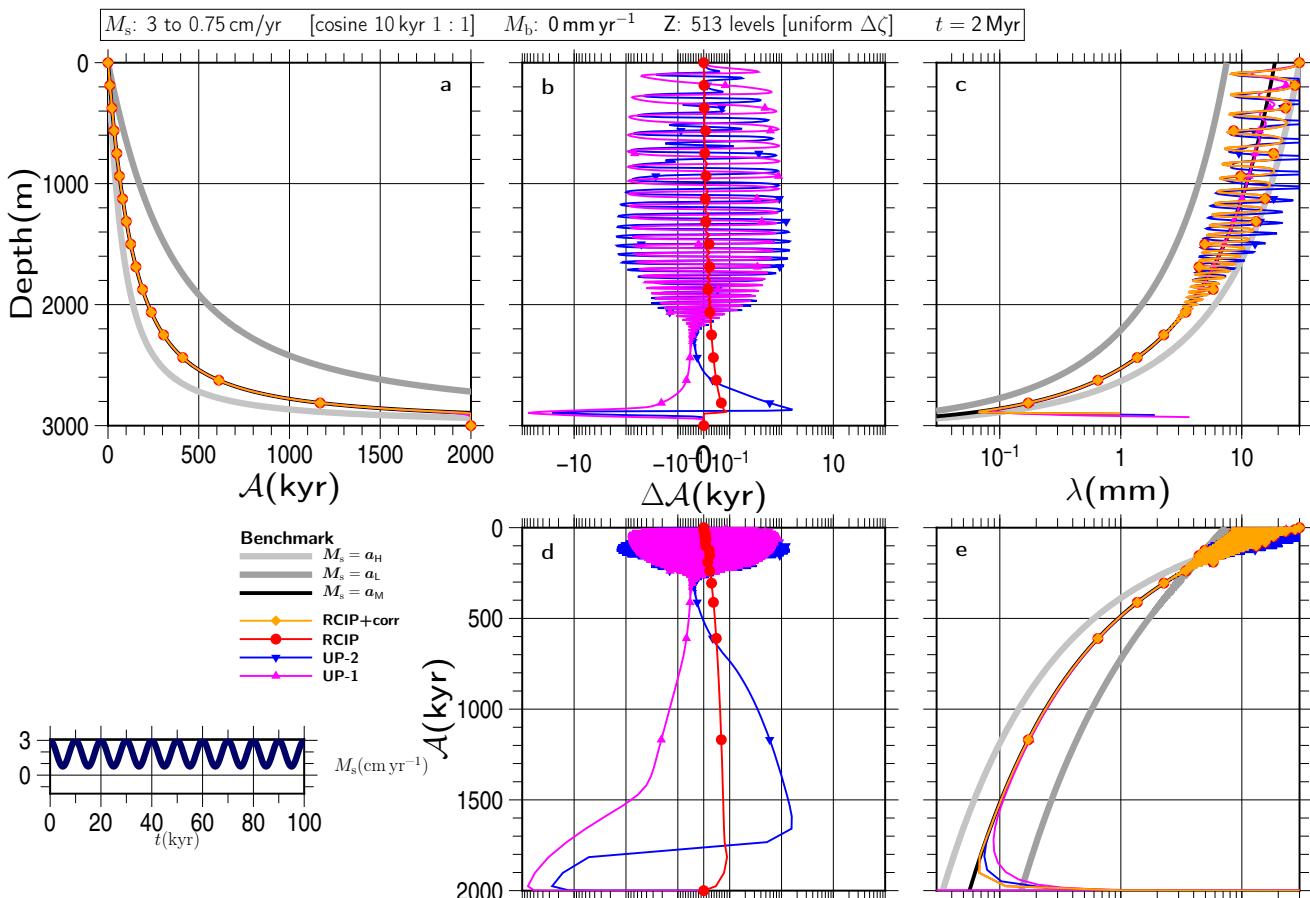


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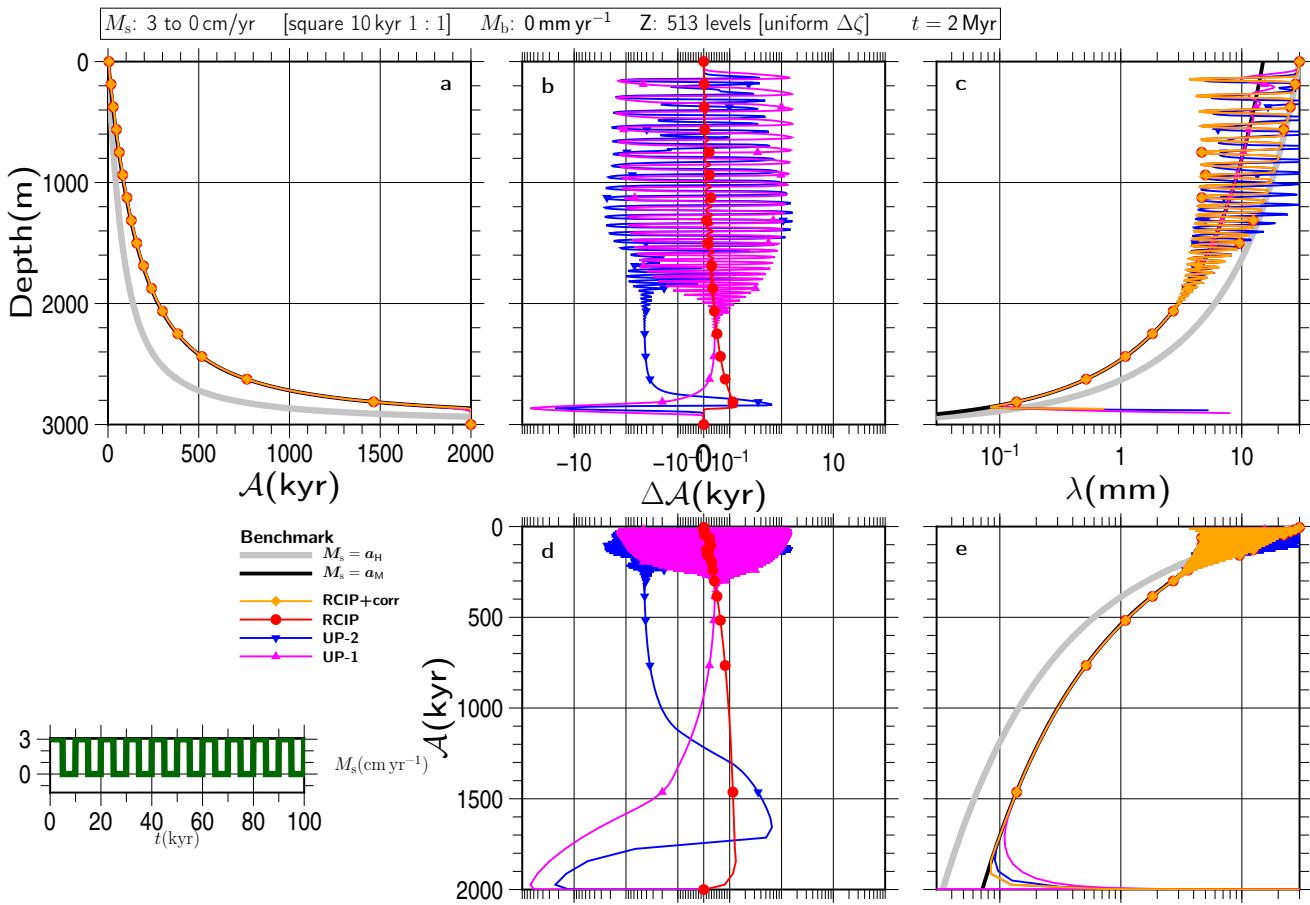


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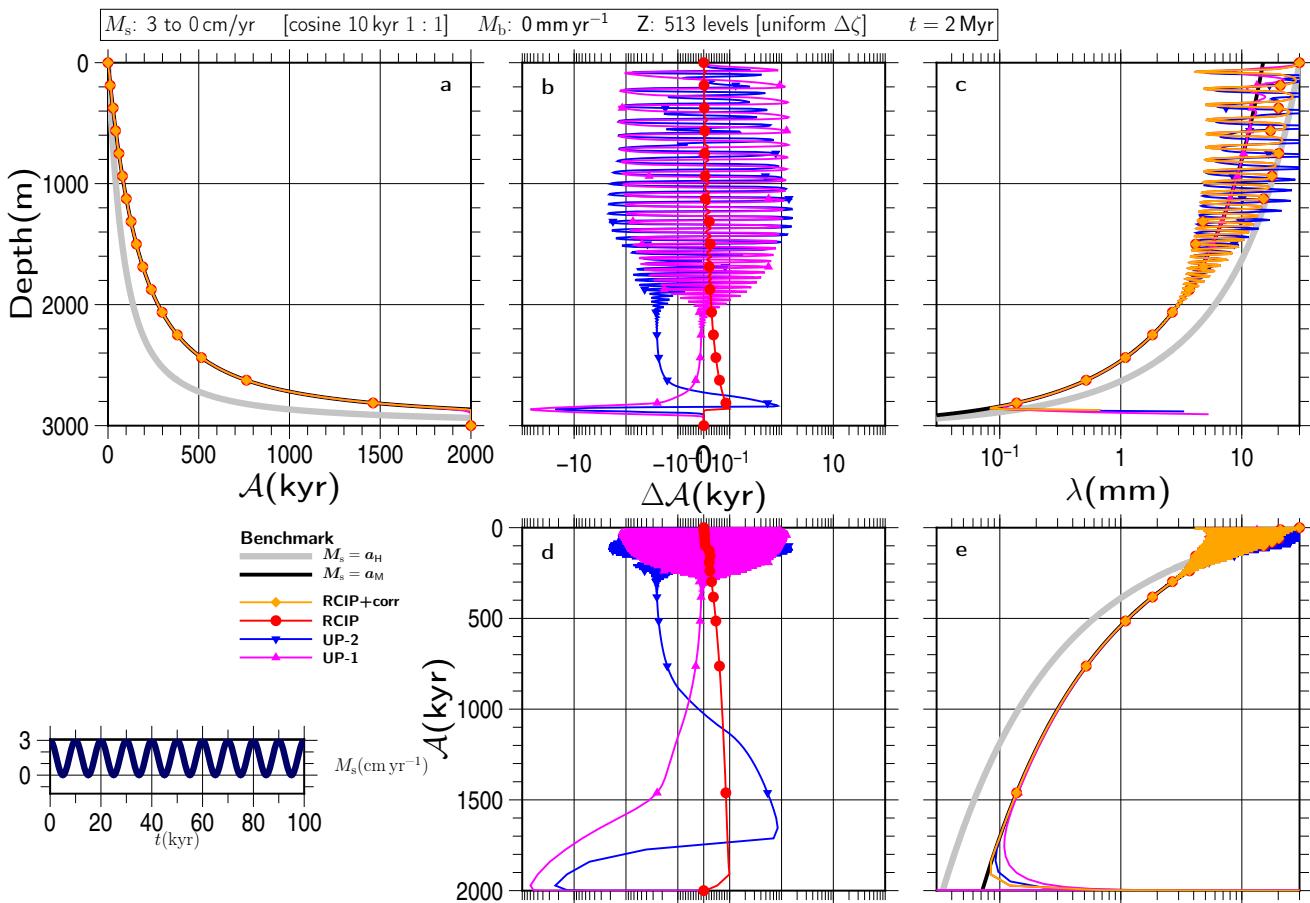


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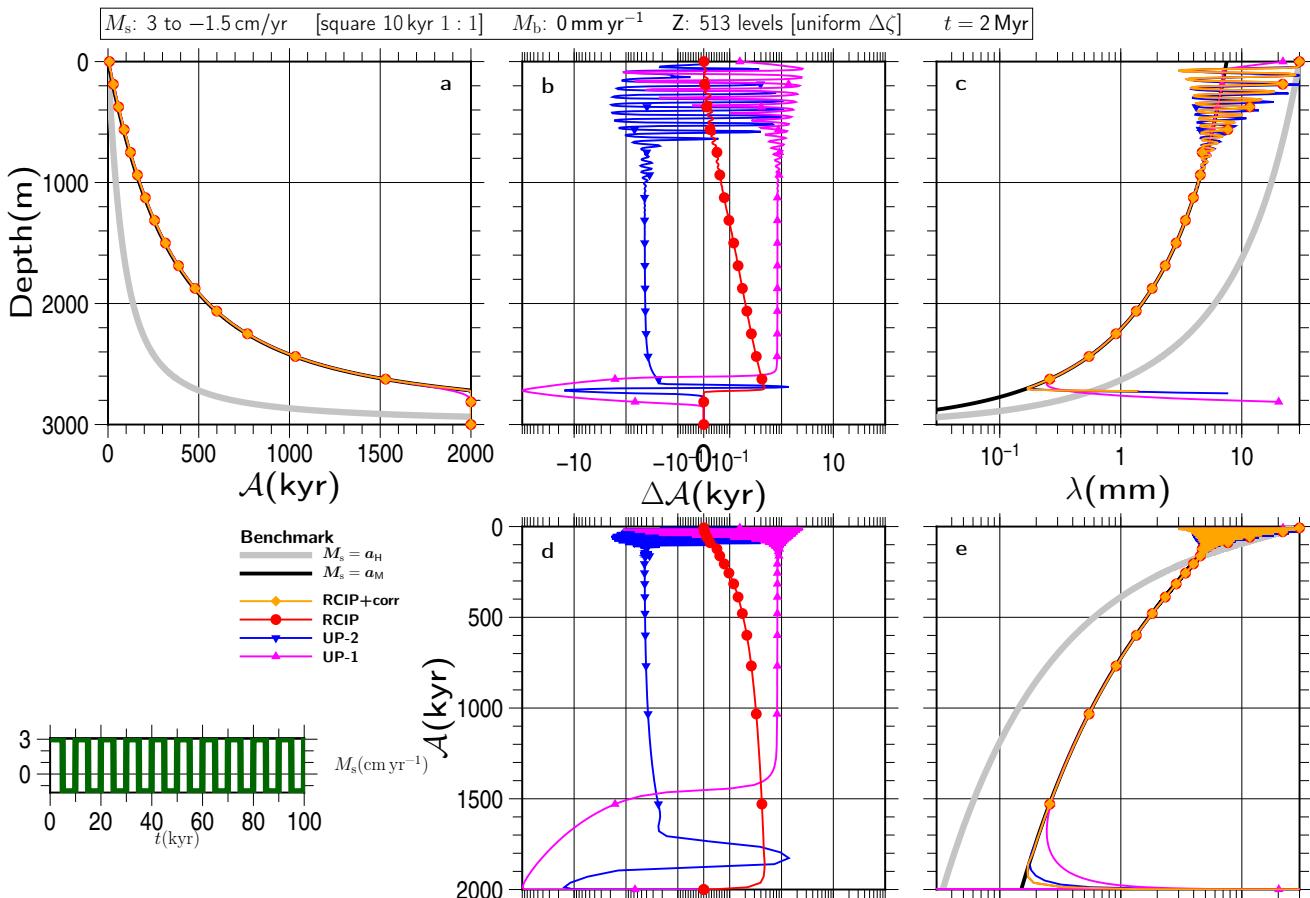


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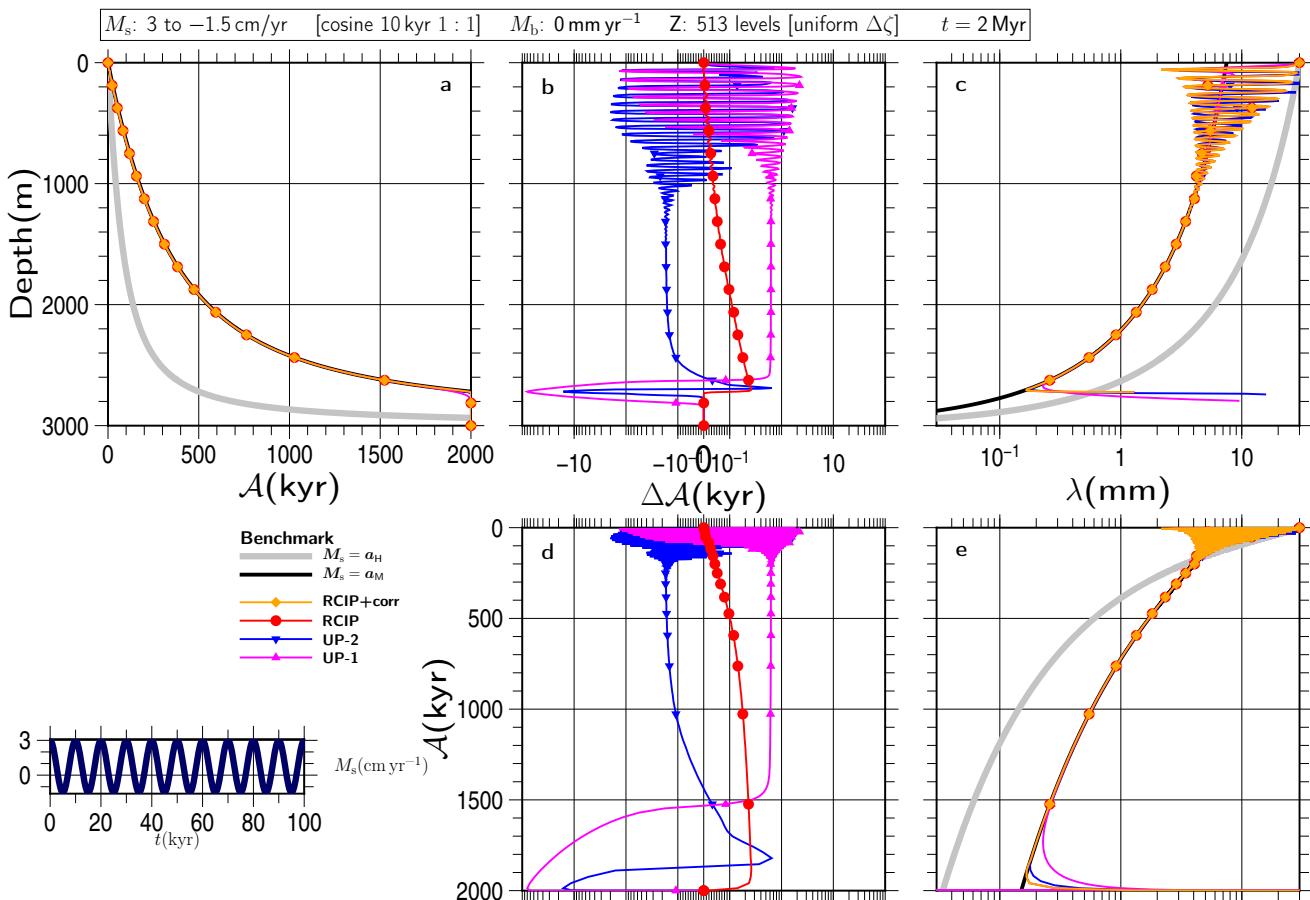


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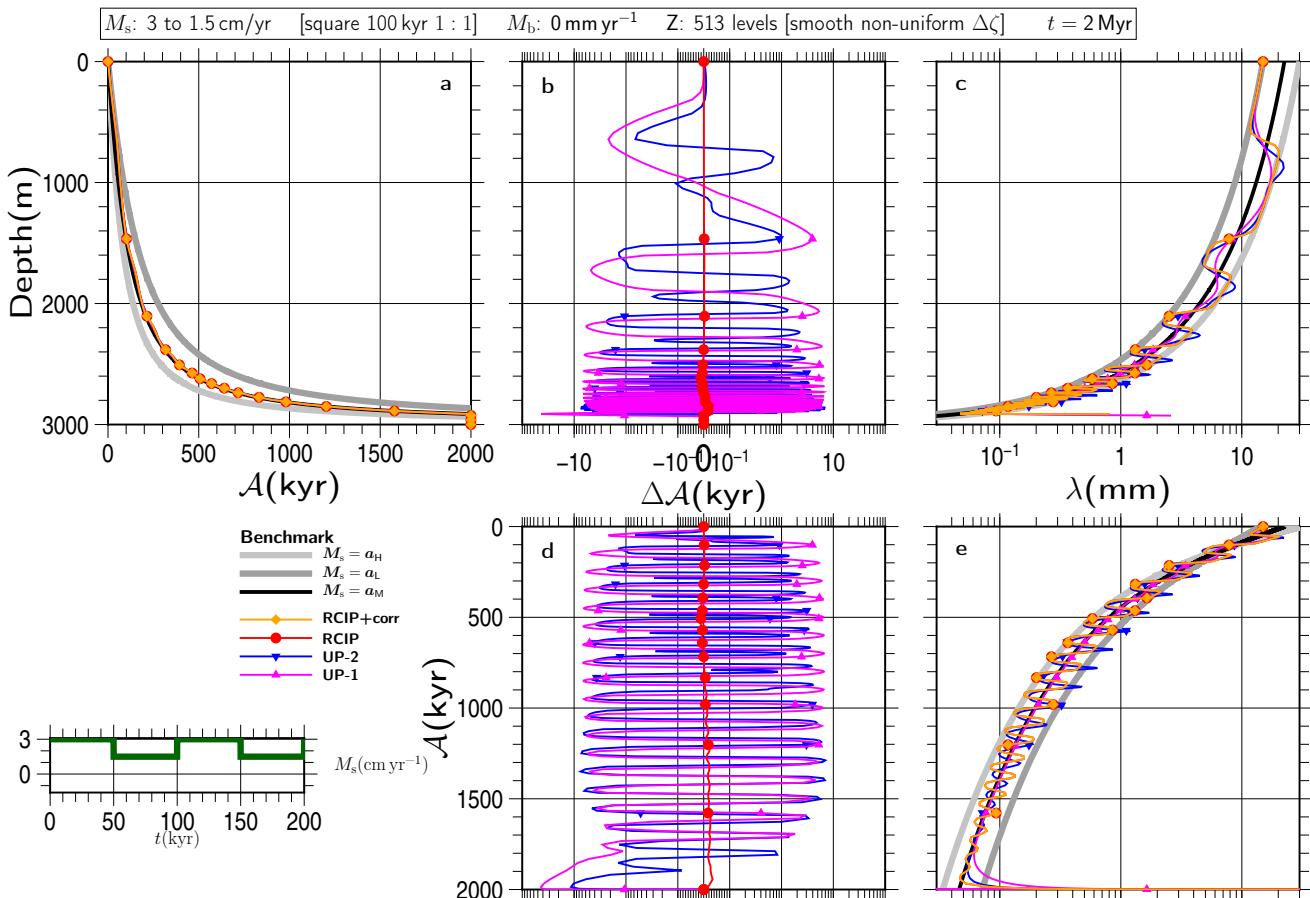


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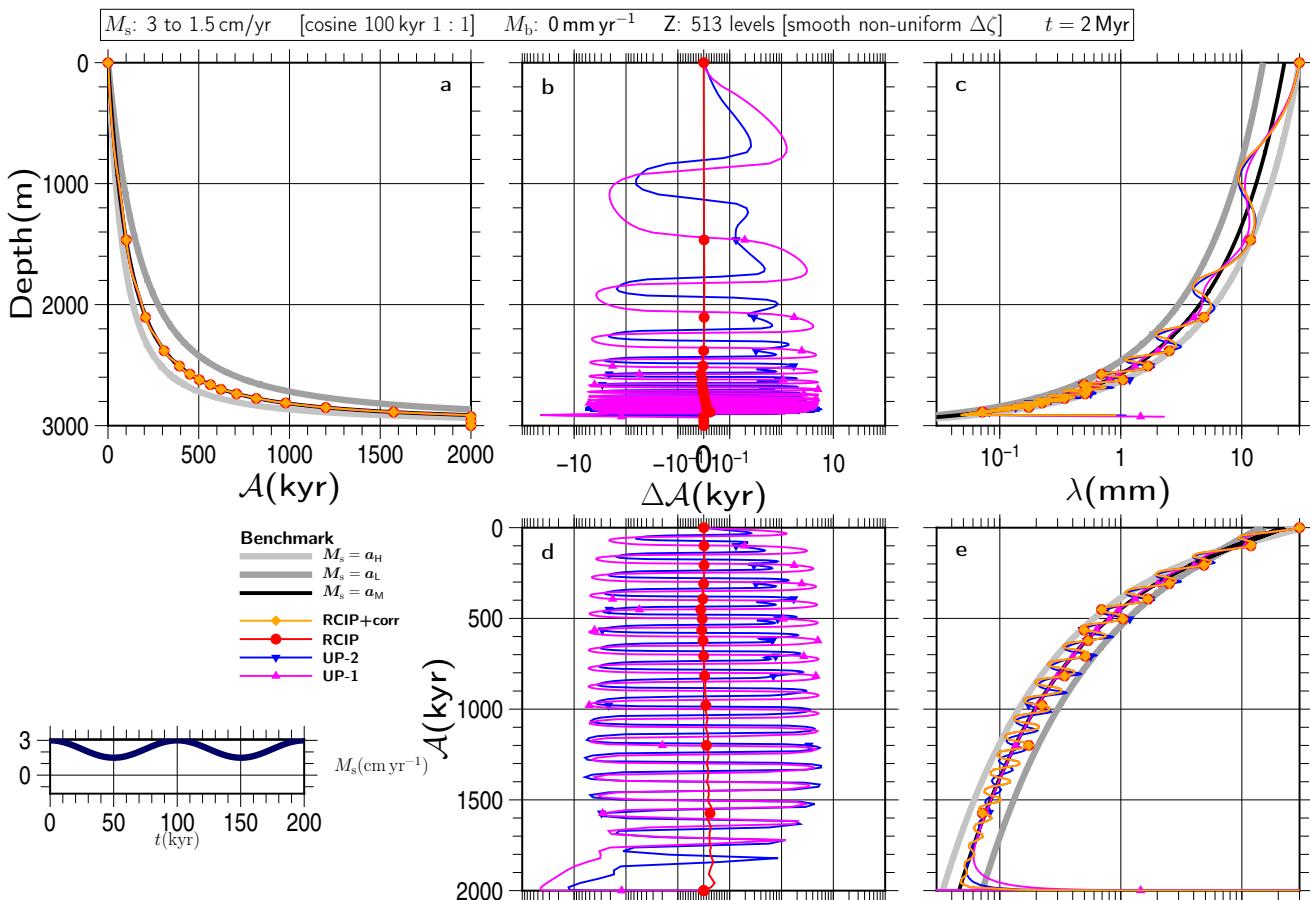


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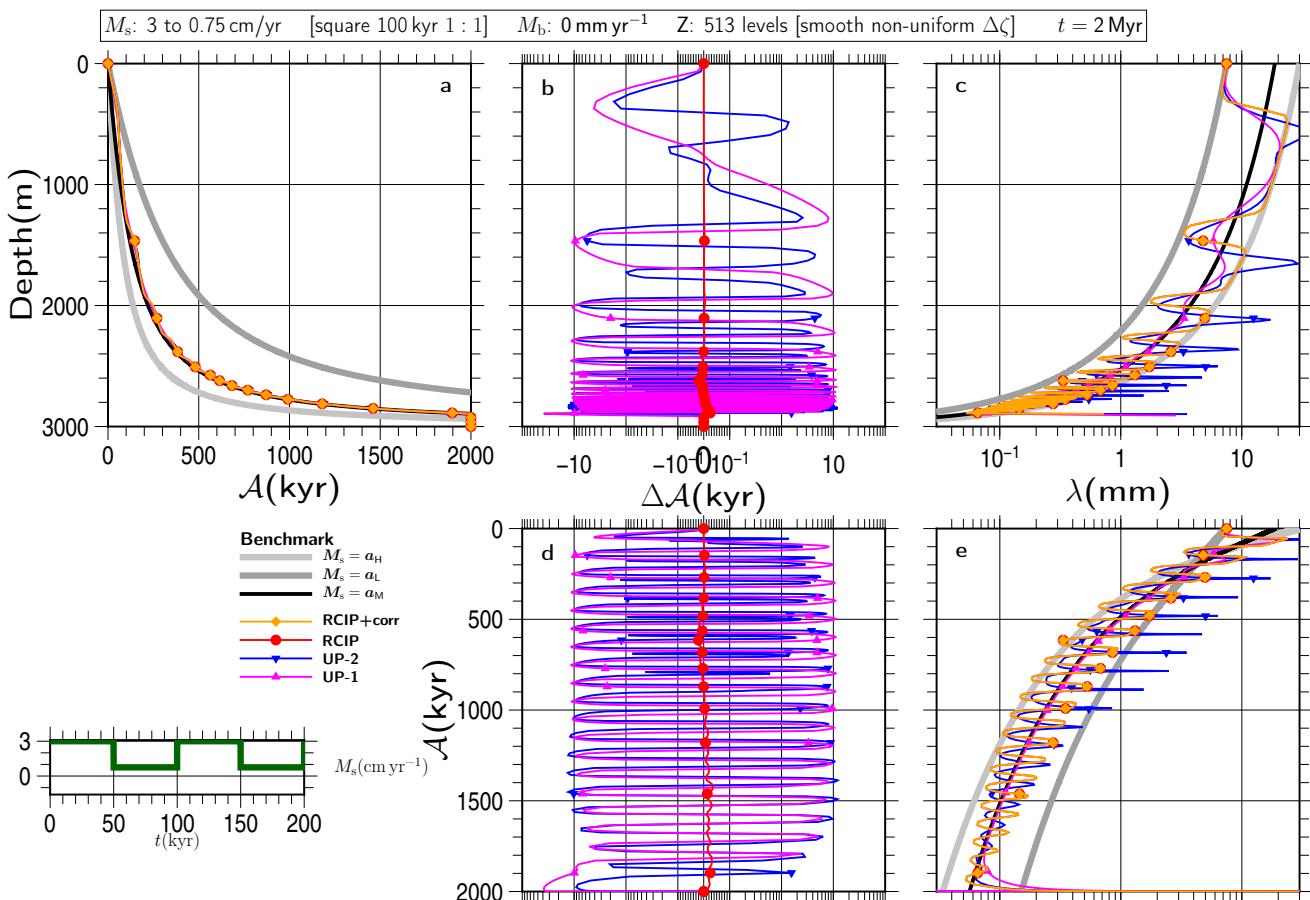


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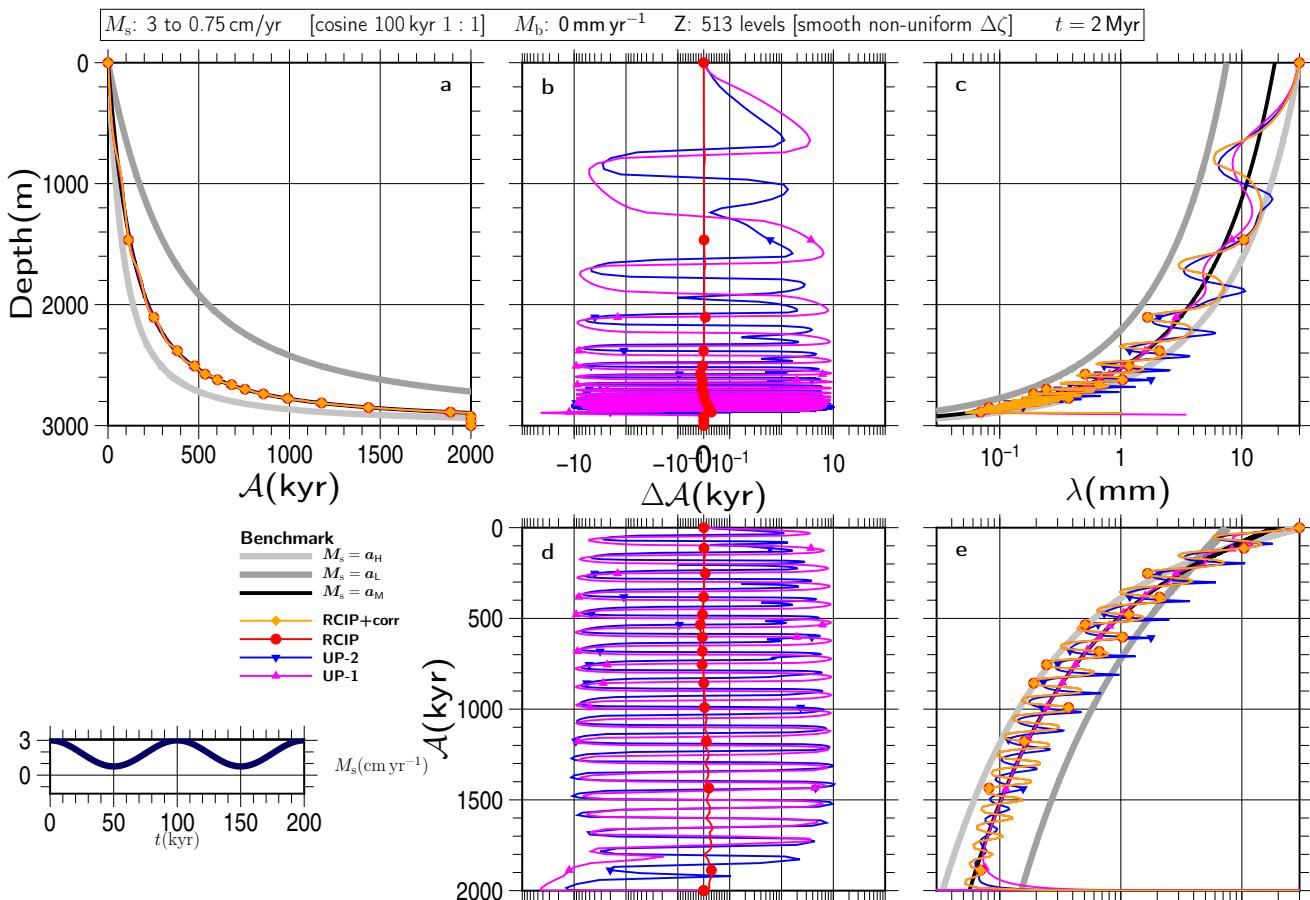


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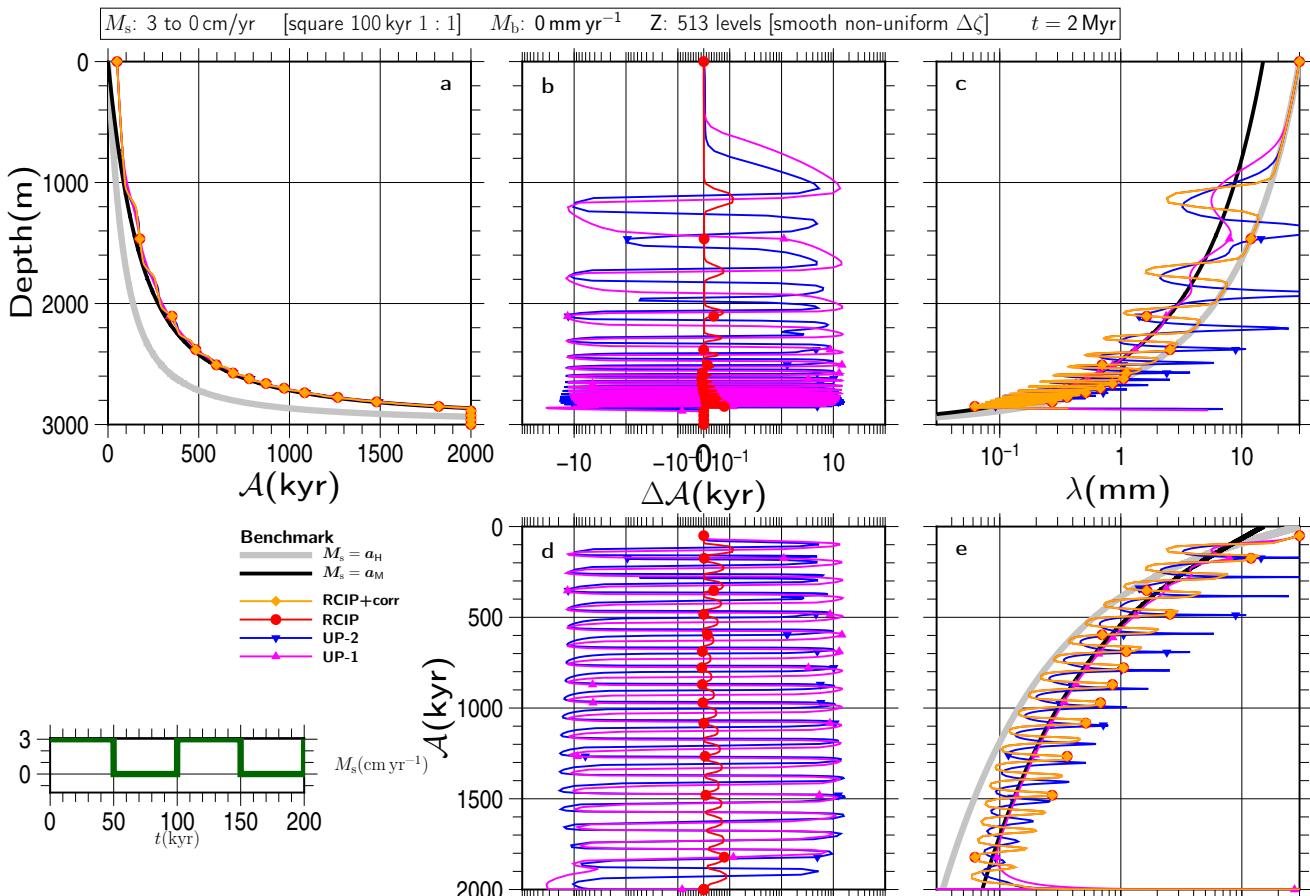


Figure S99

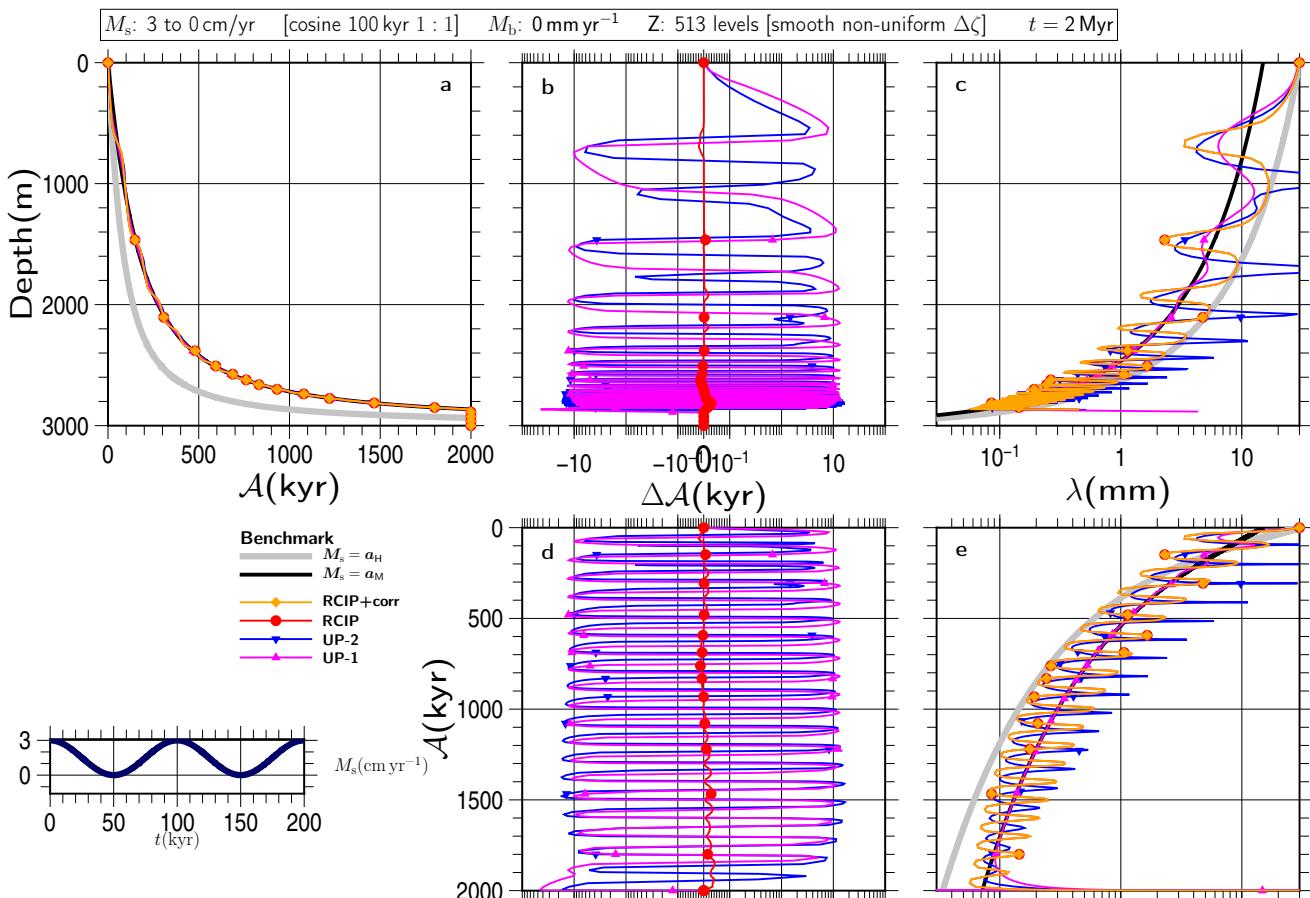


Figure S100

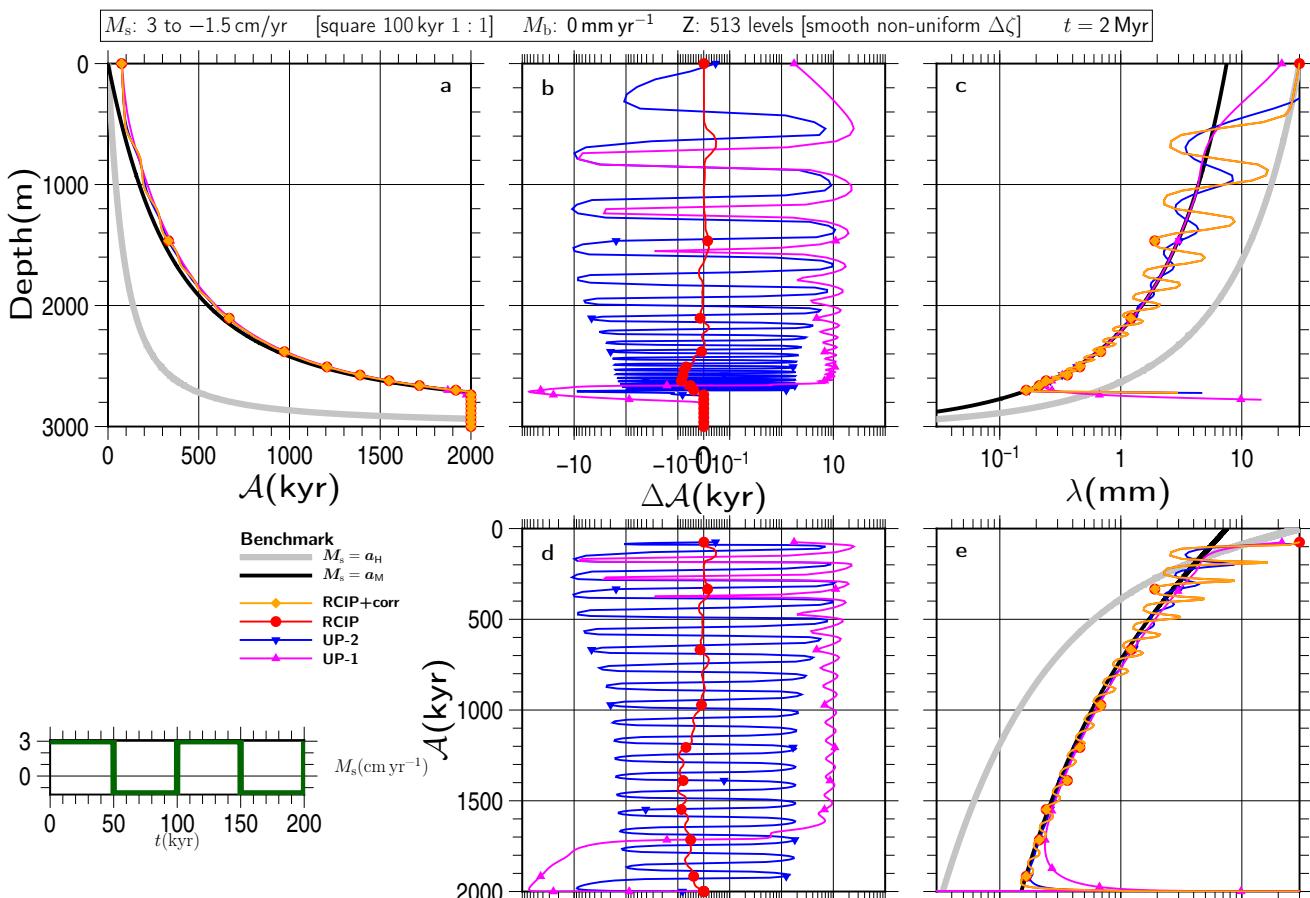


Figure S101

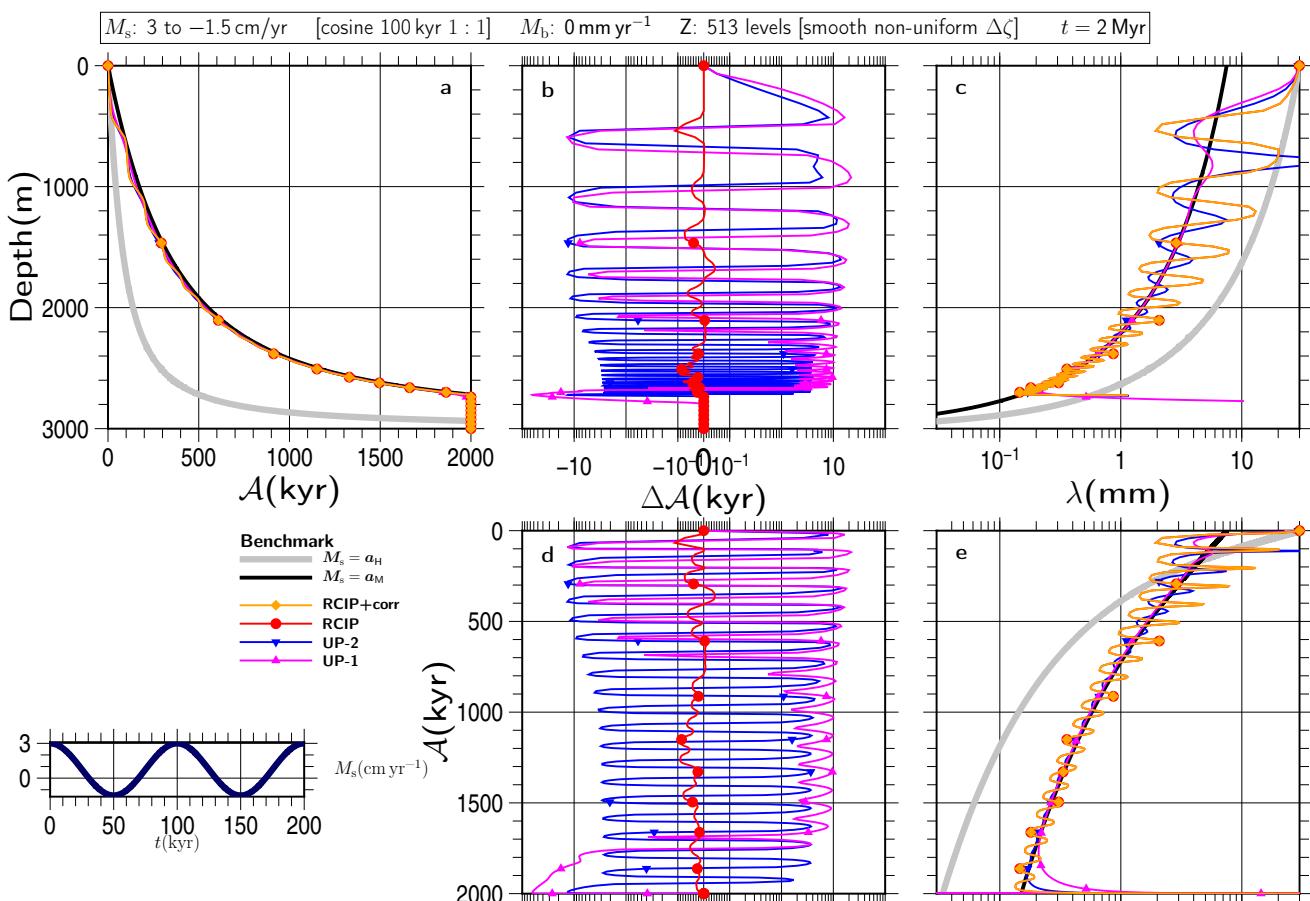


Figure S102

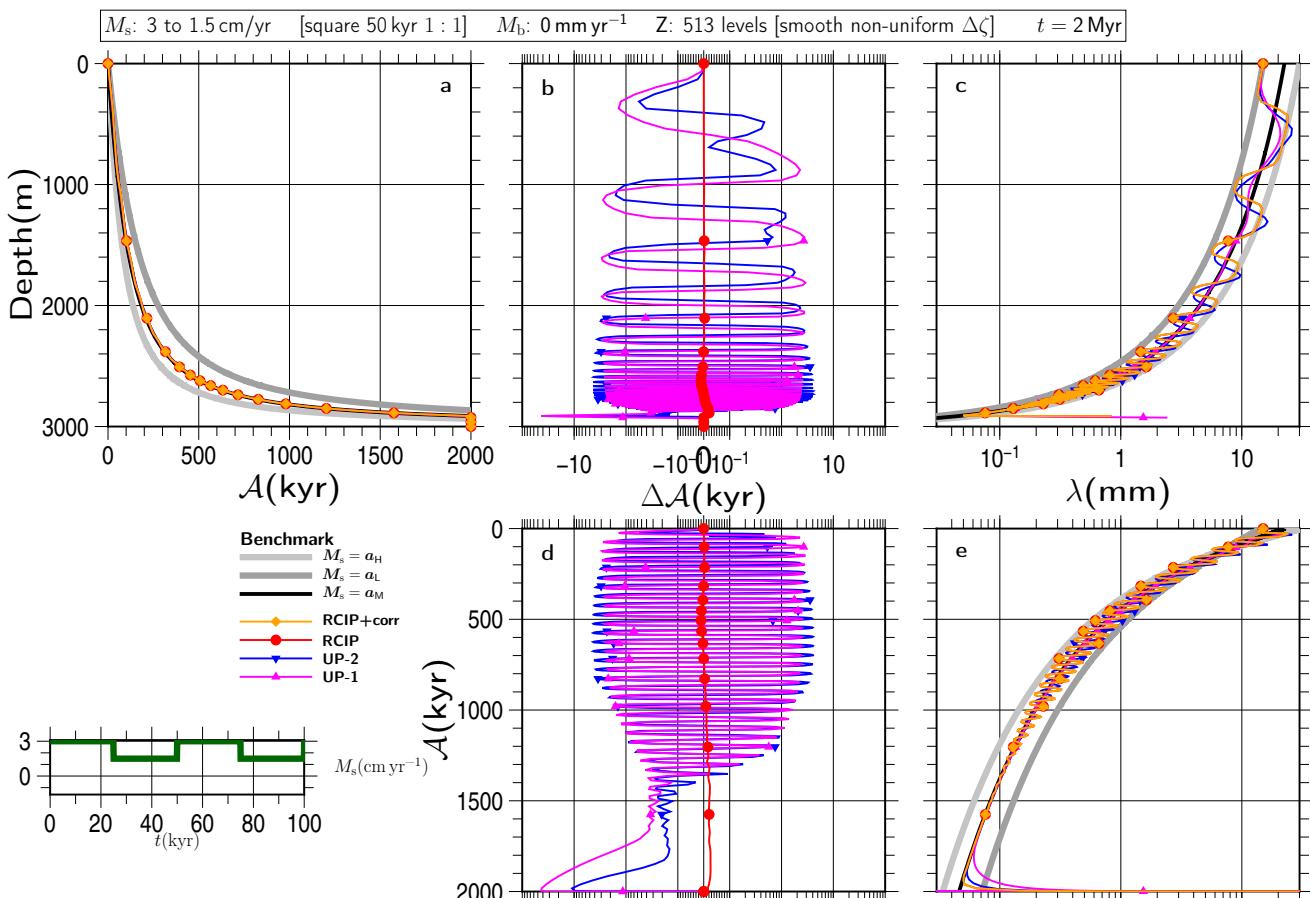


Figure S103

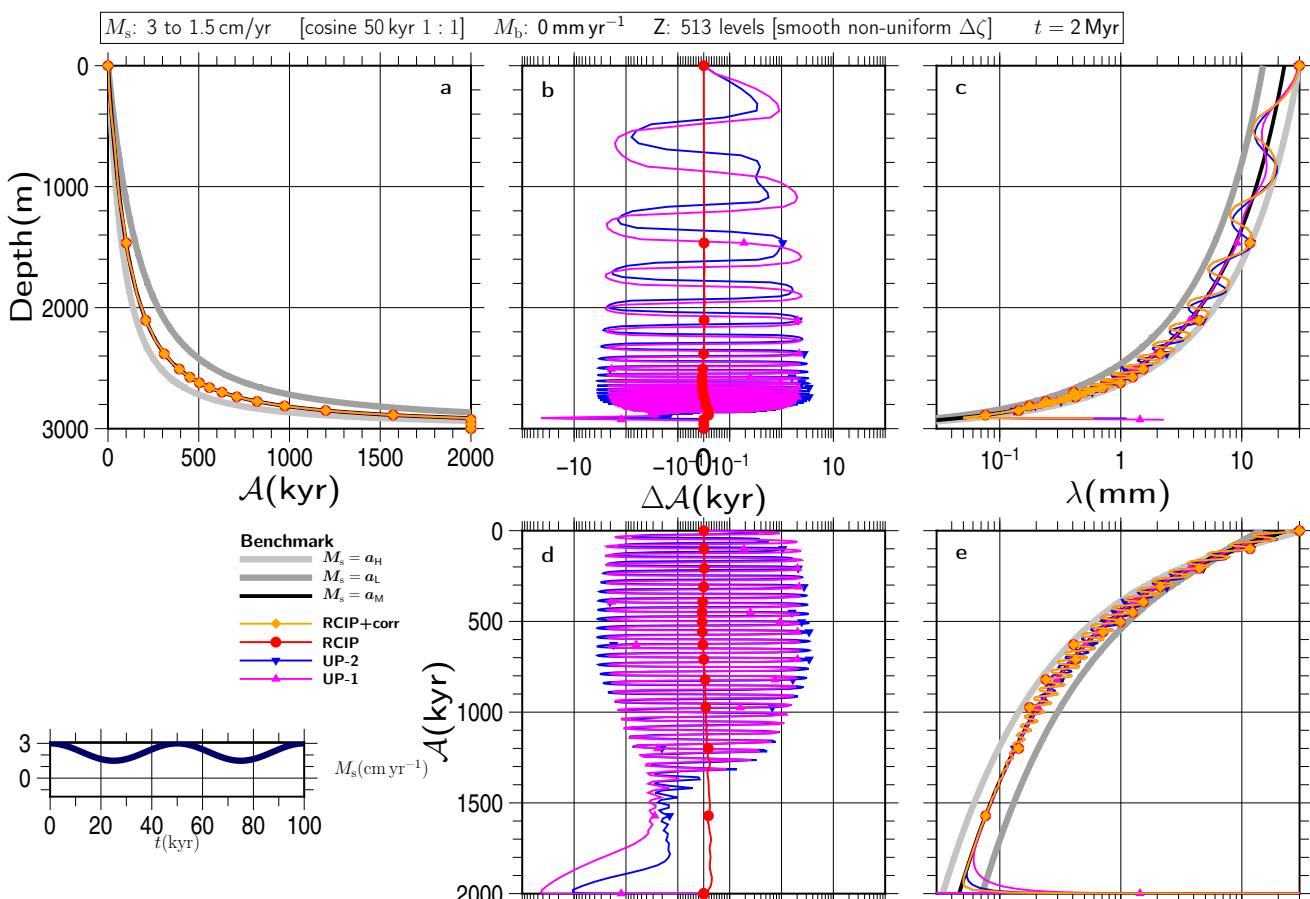


Figure S104

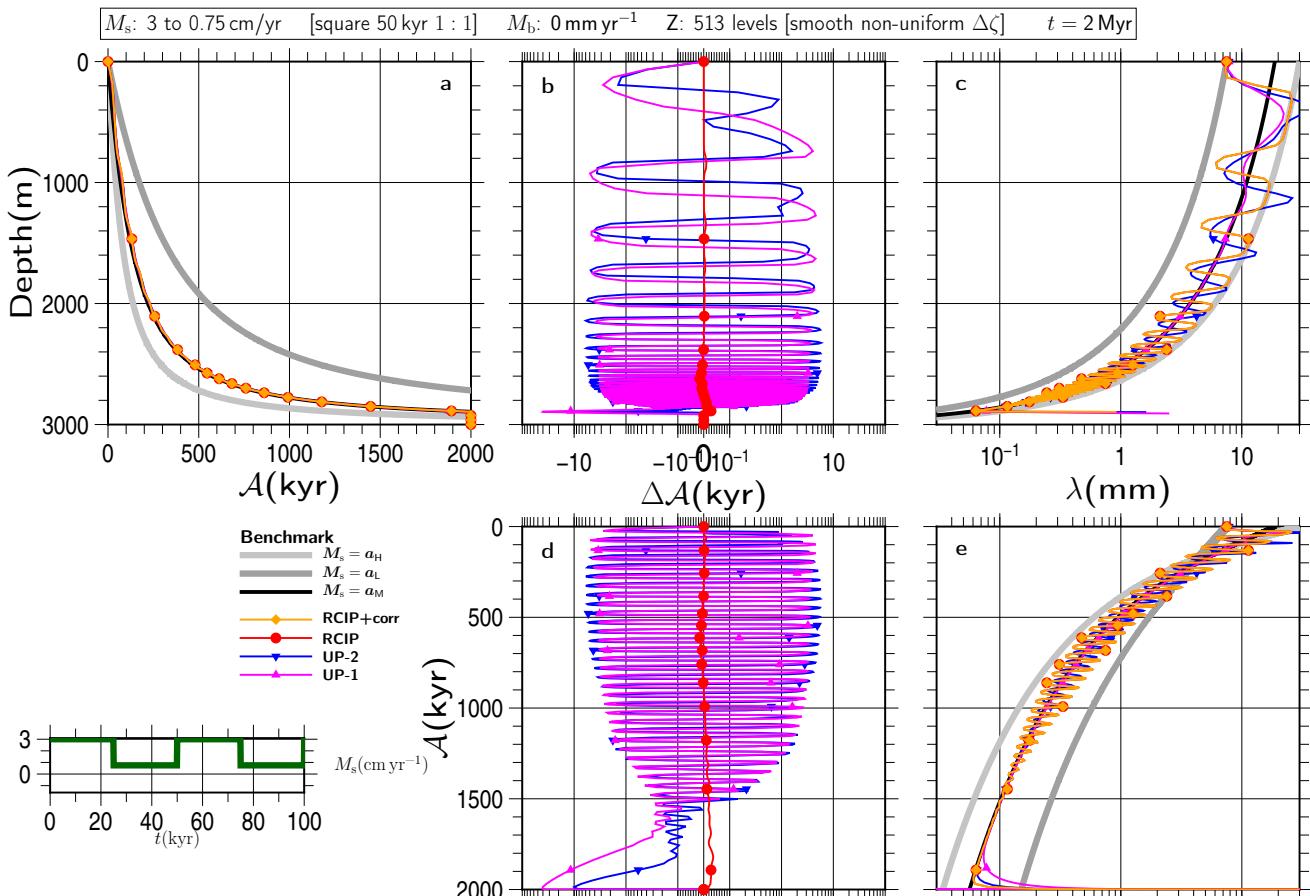


Figure S105

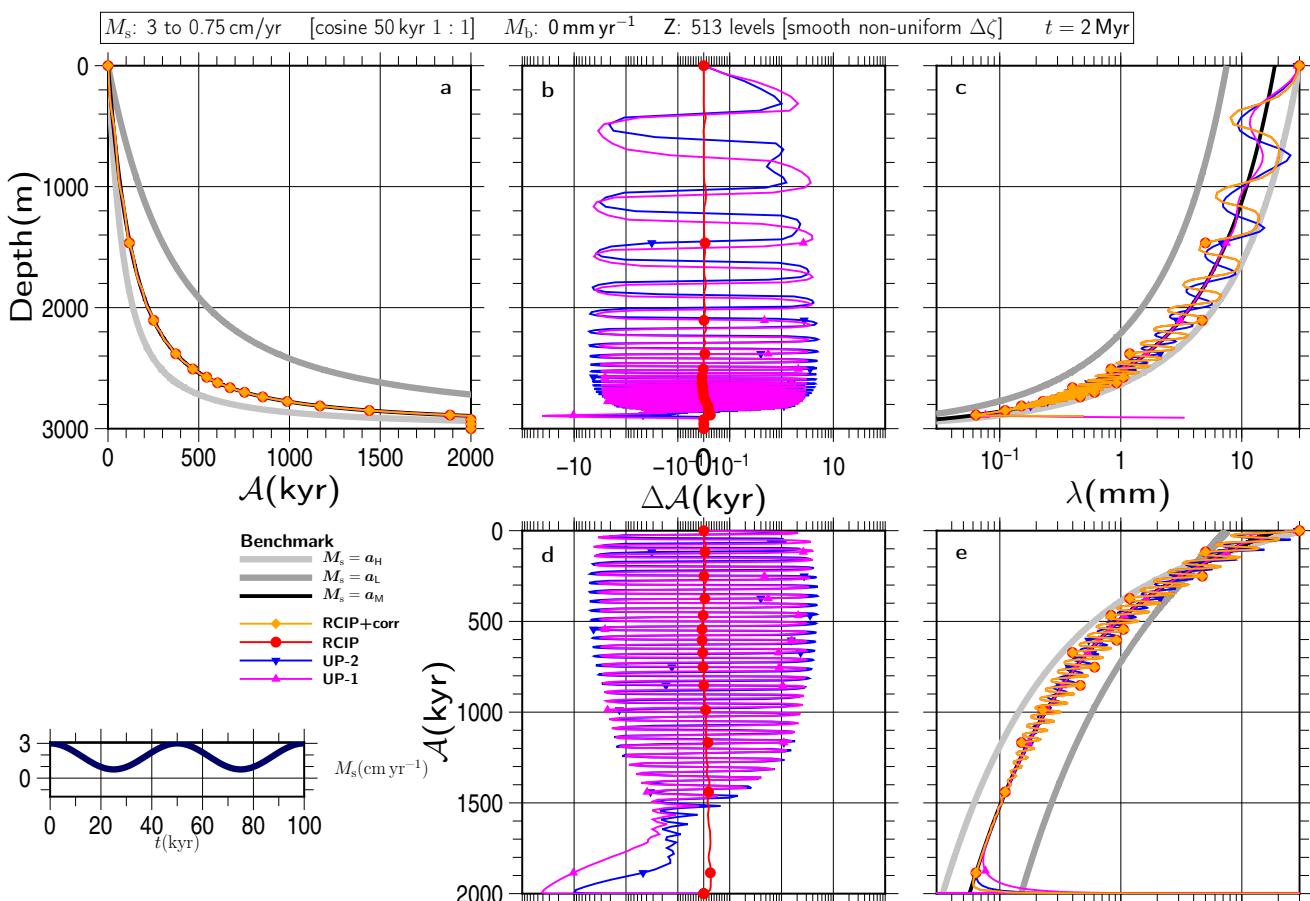


Figure S106

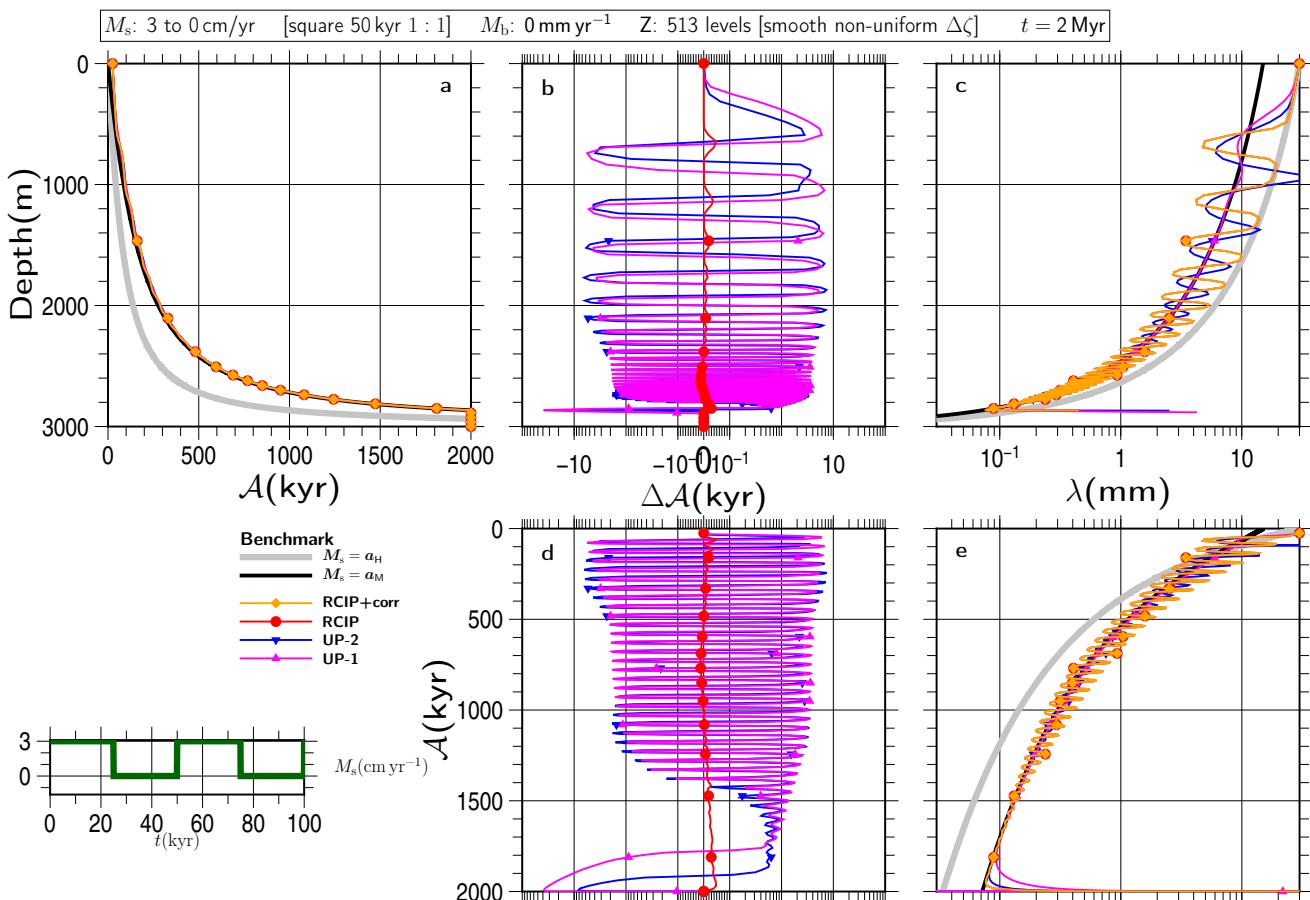


Figure S107

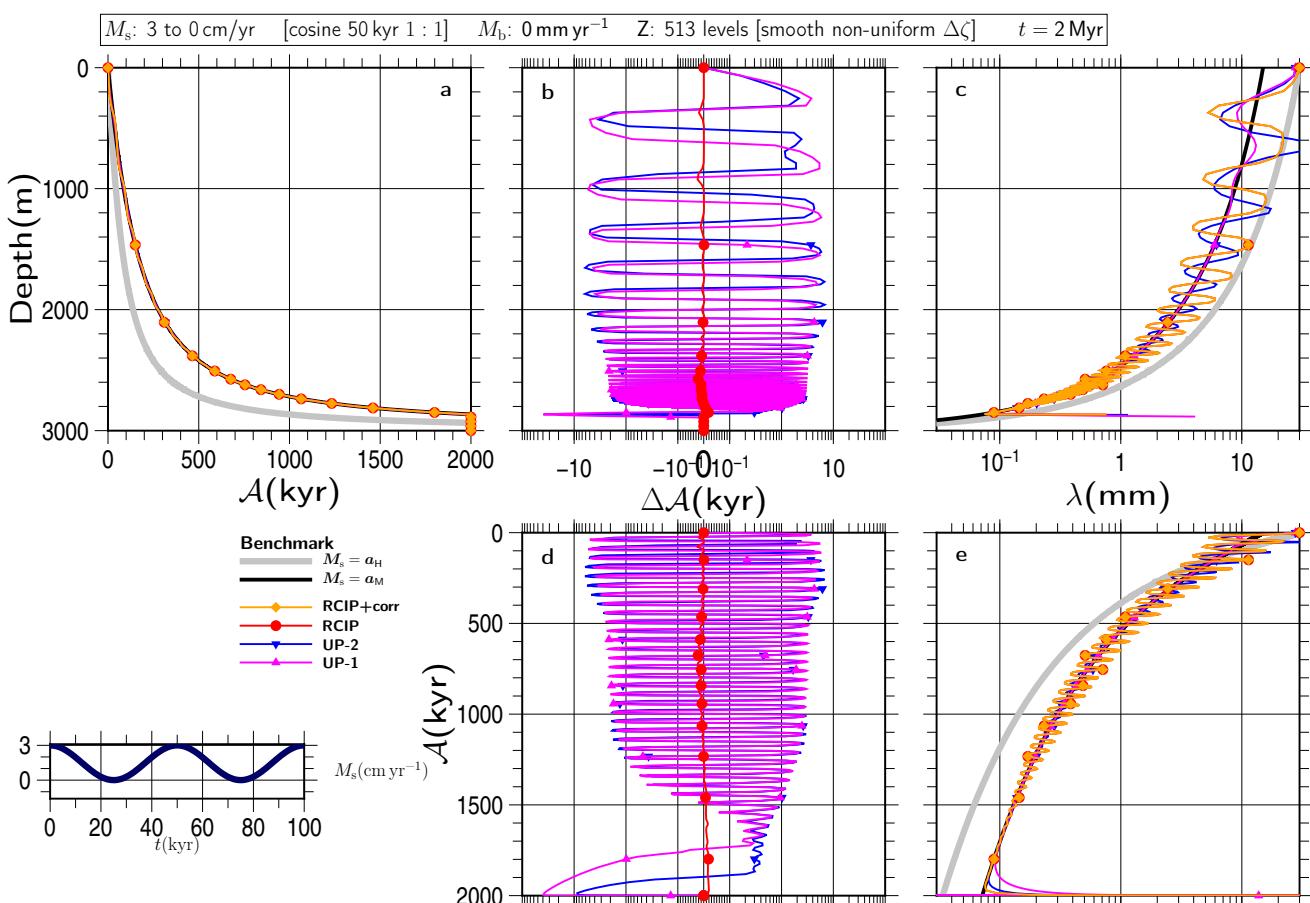


Figure S108

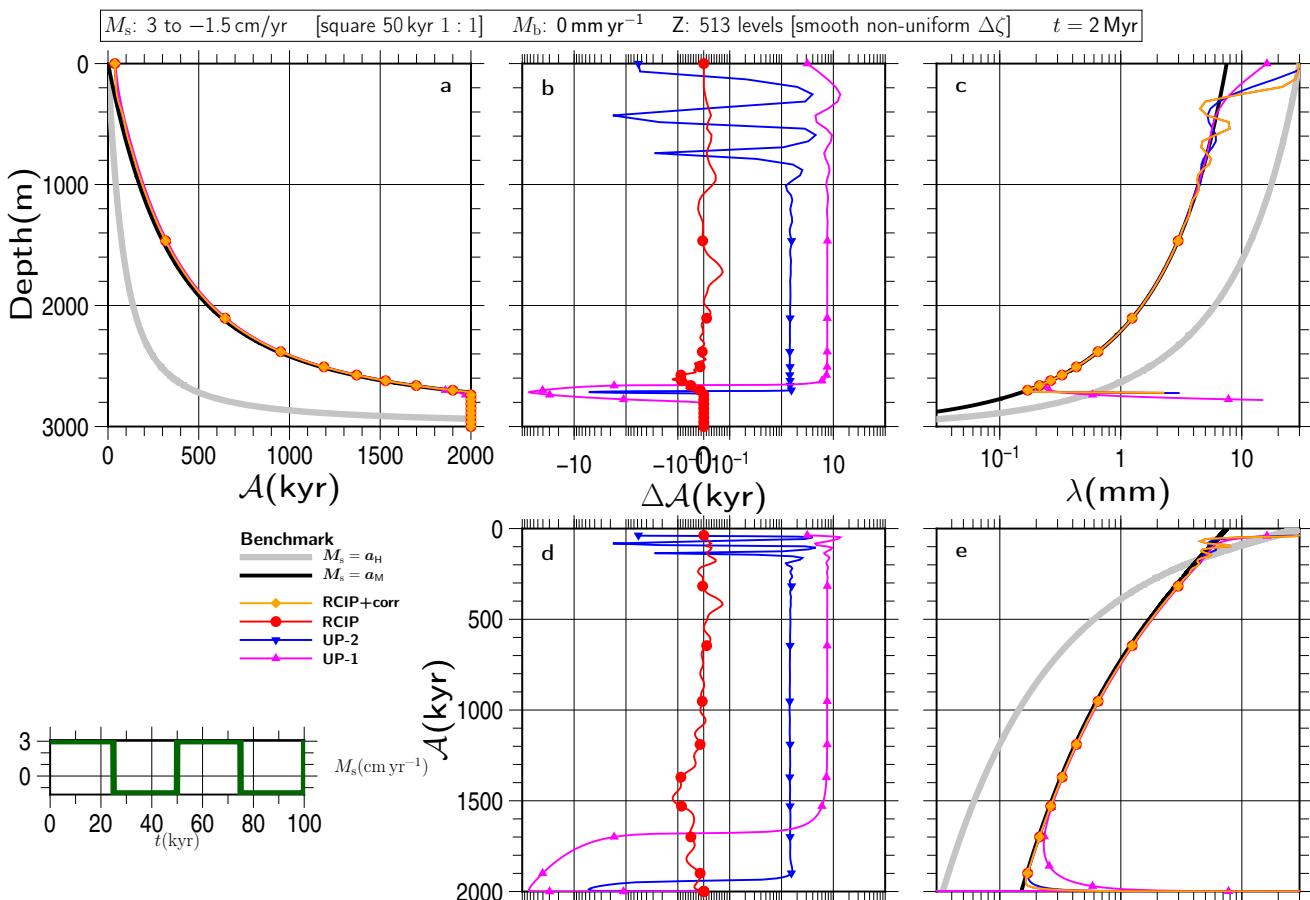


Figure S109

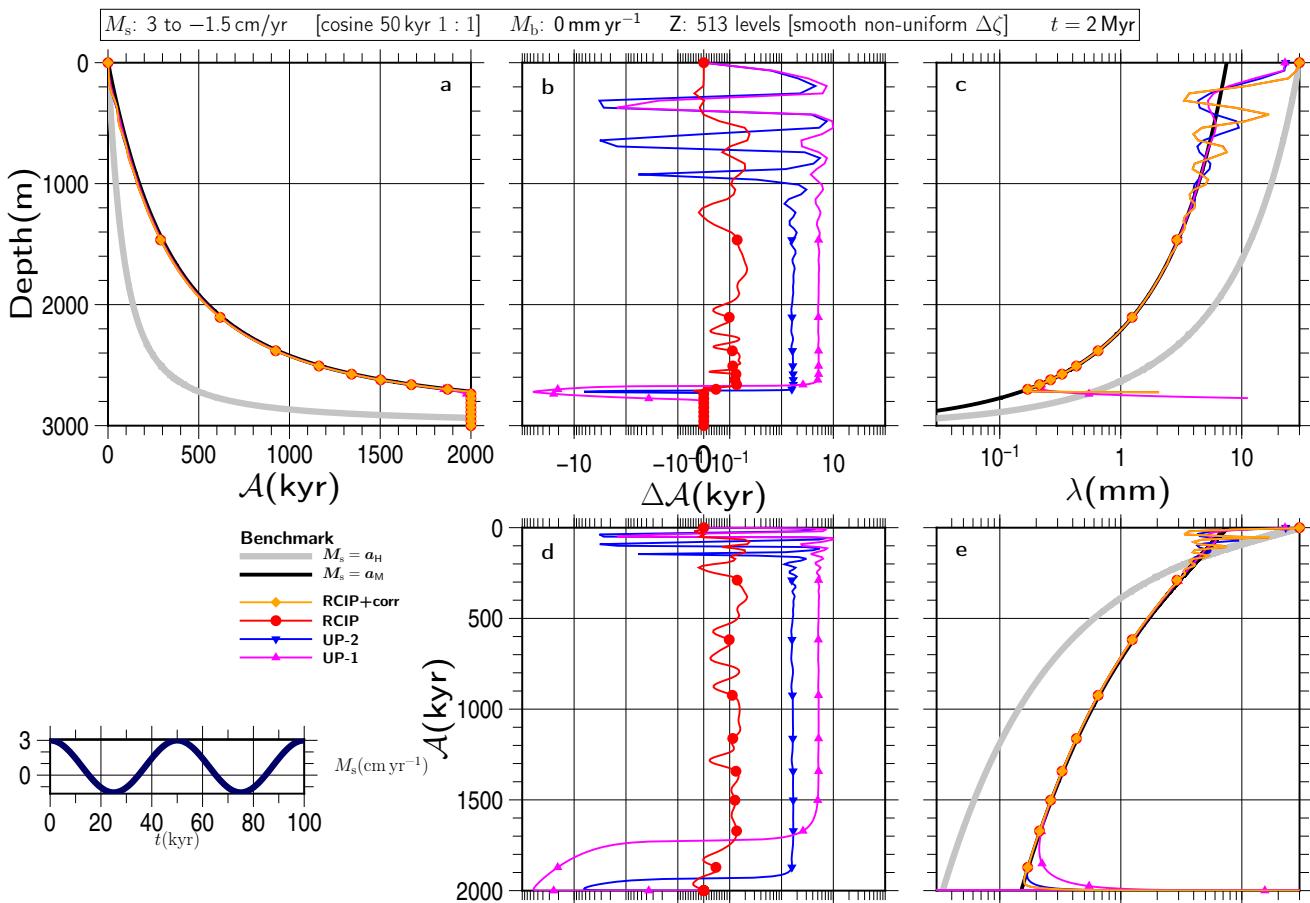


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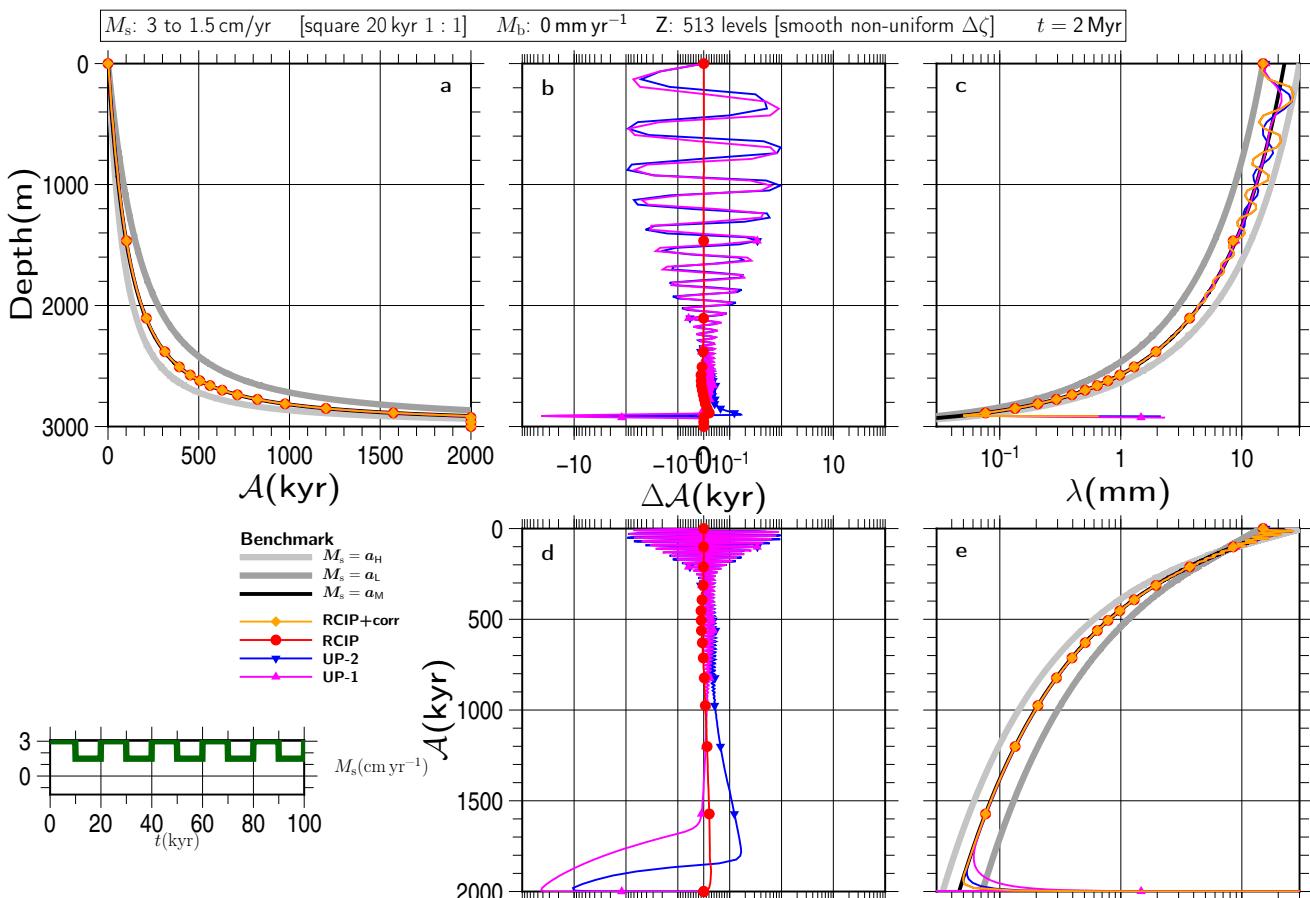


Figure S111

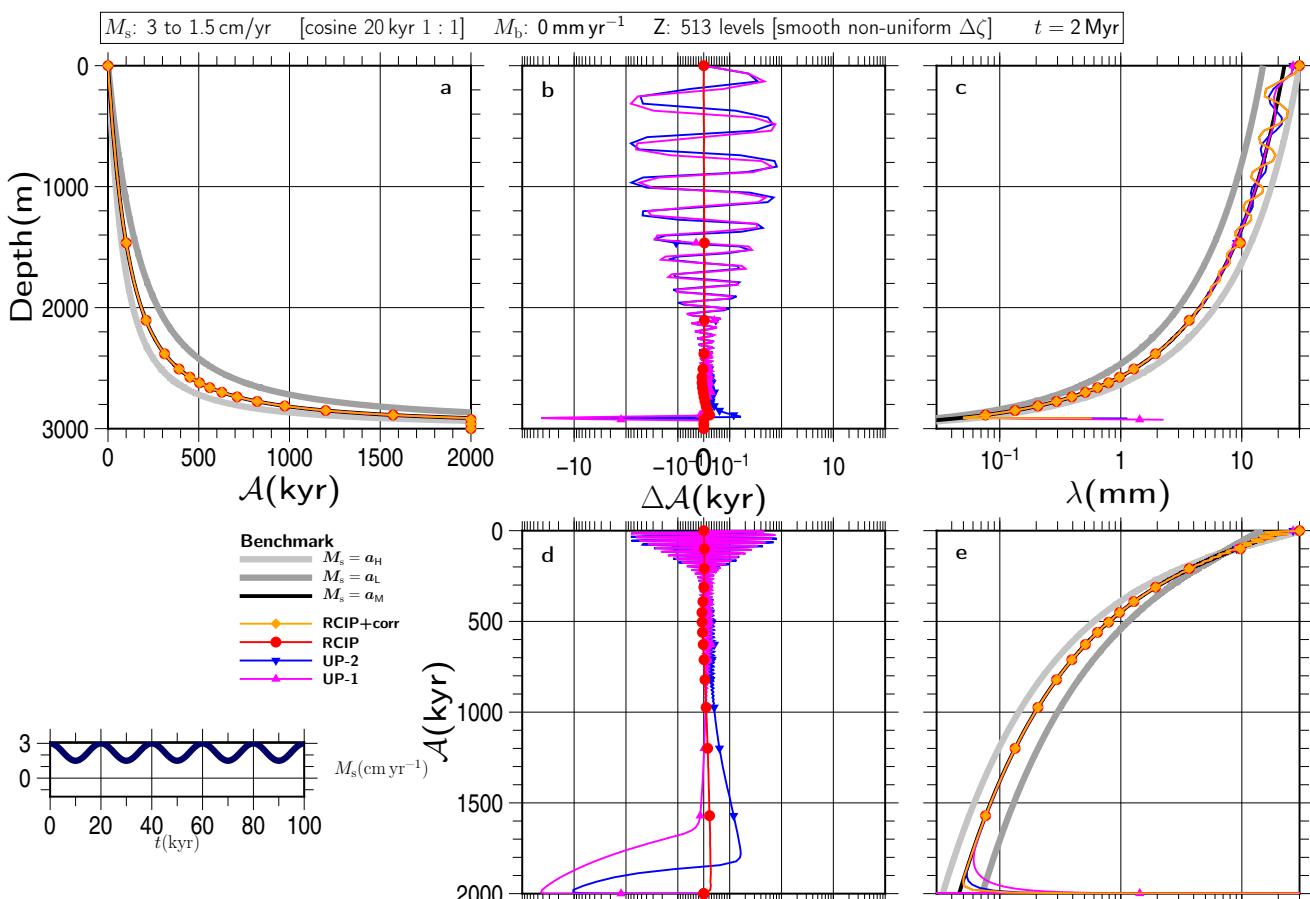


Figure S112

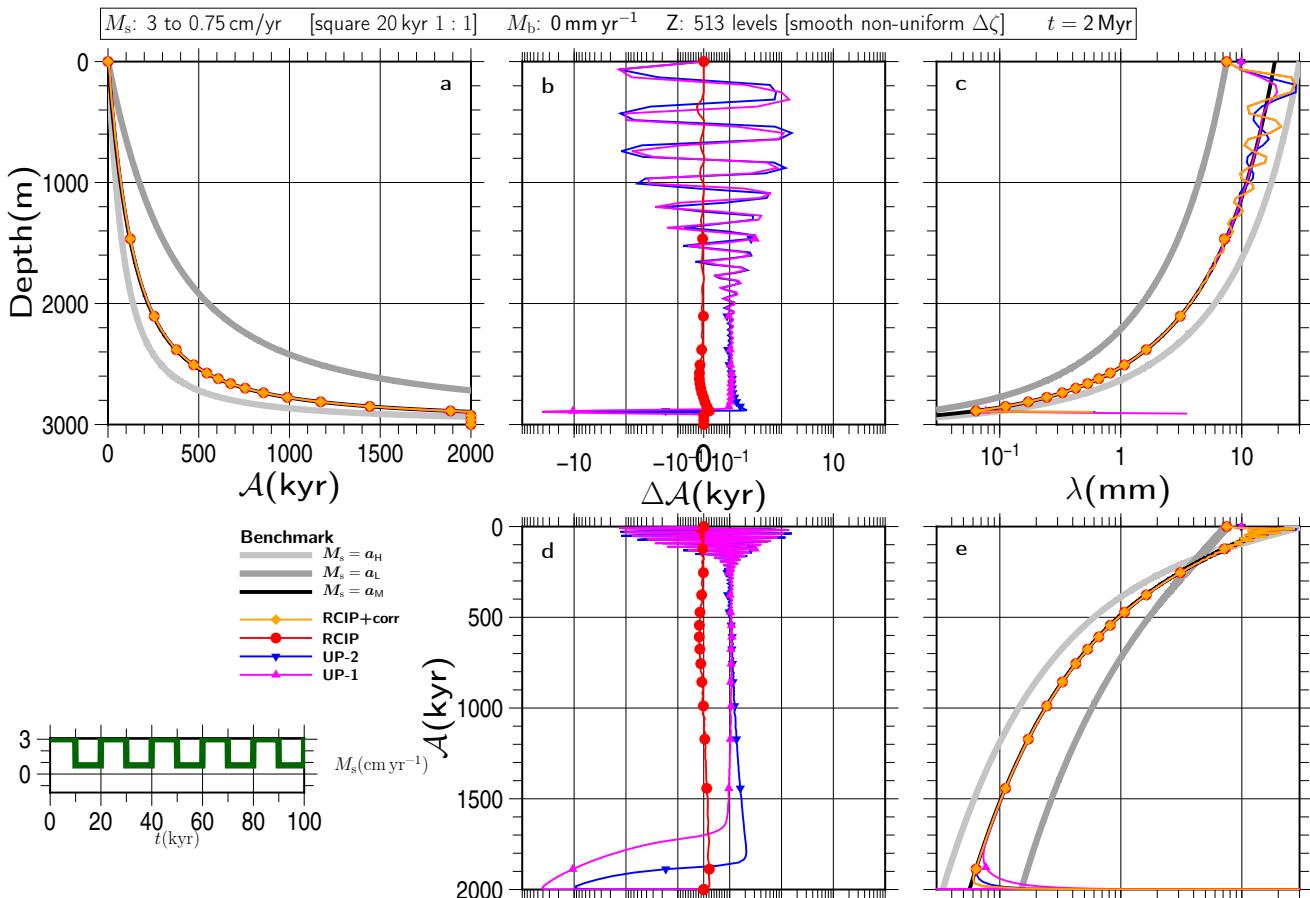


Figure S113

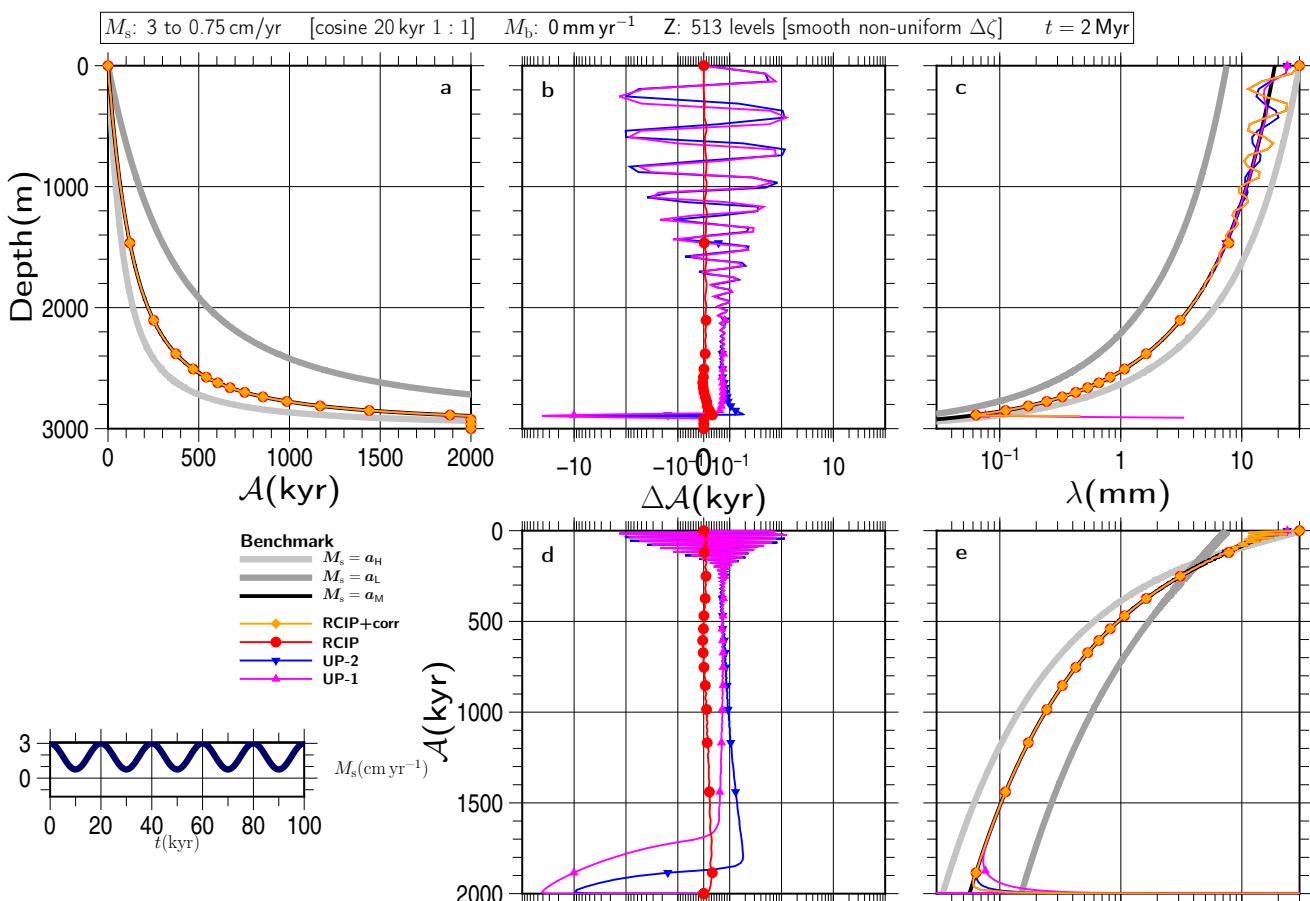


Figure S114

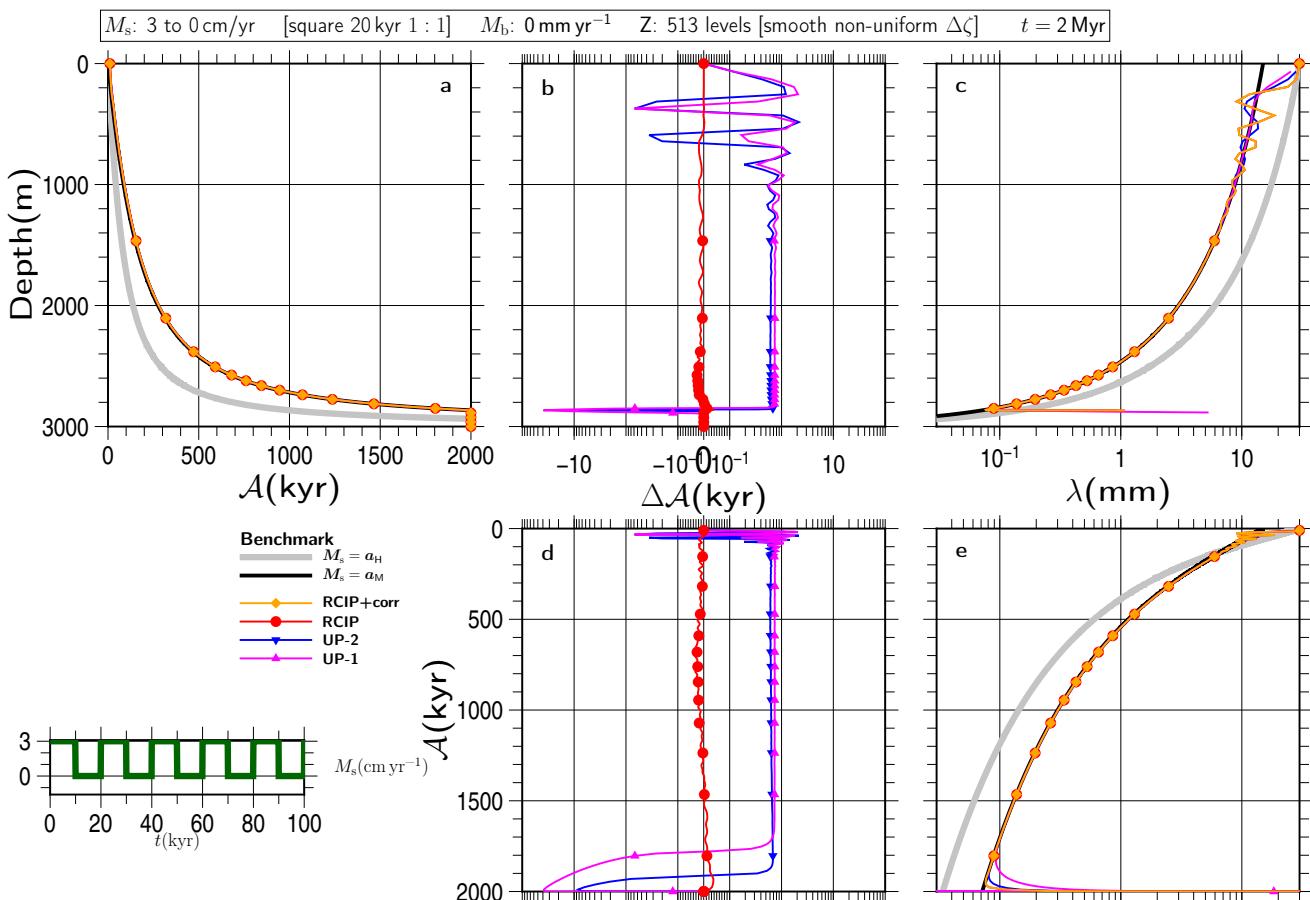


Figure S115

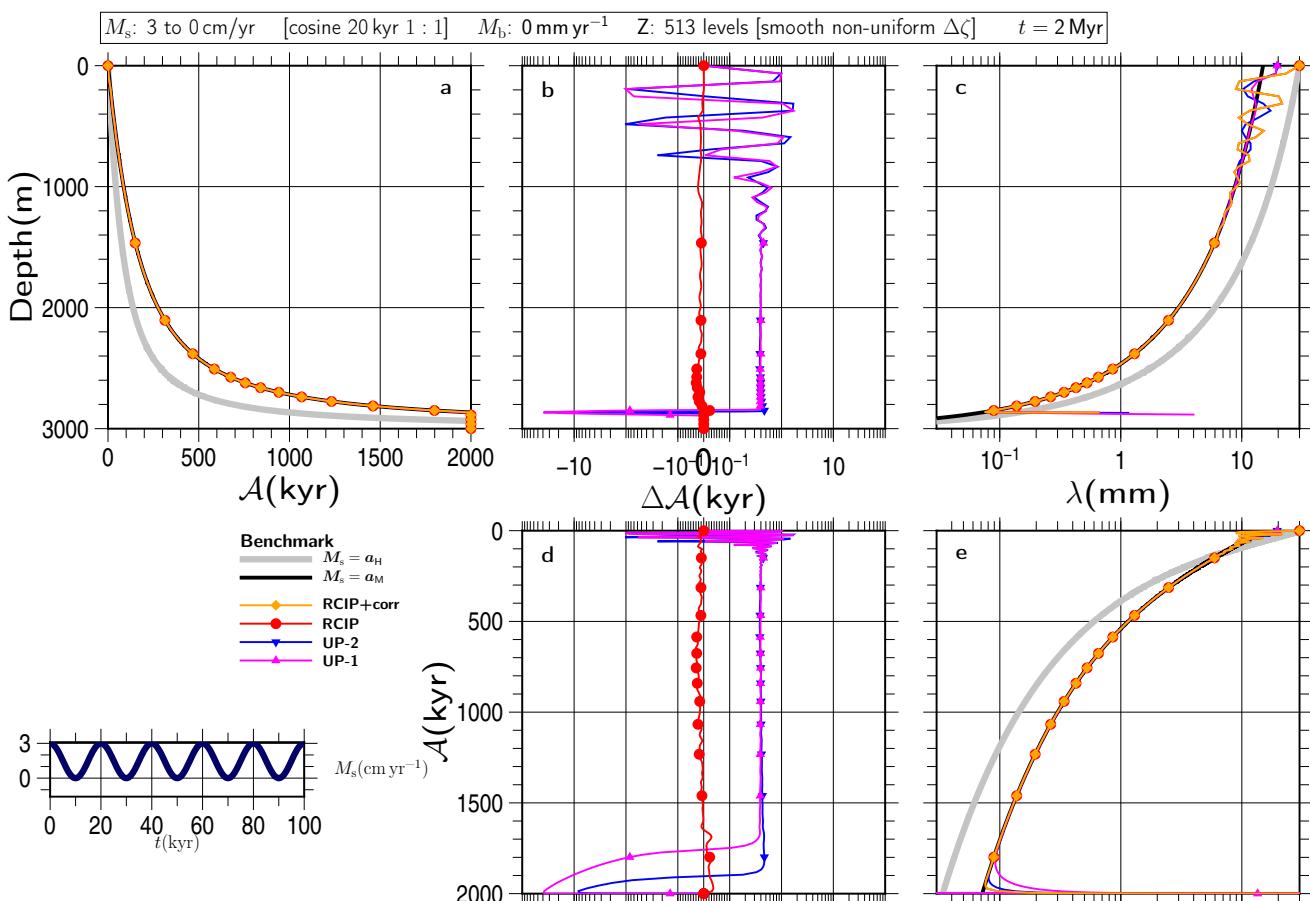


Figure S116

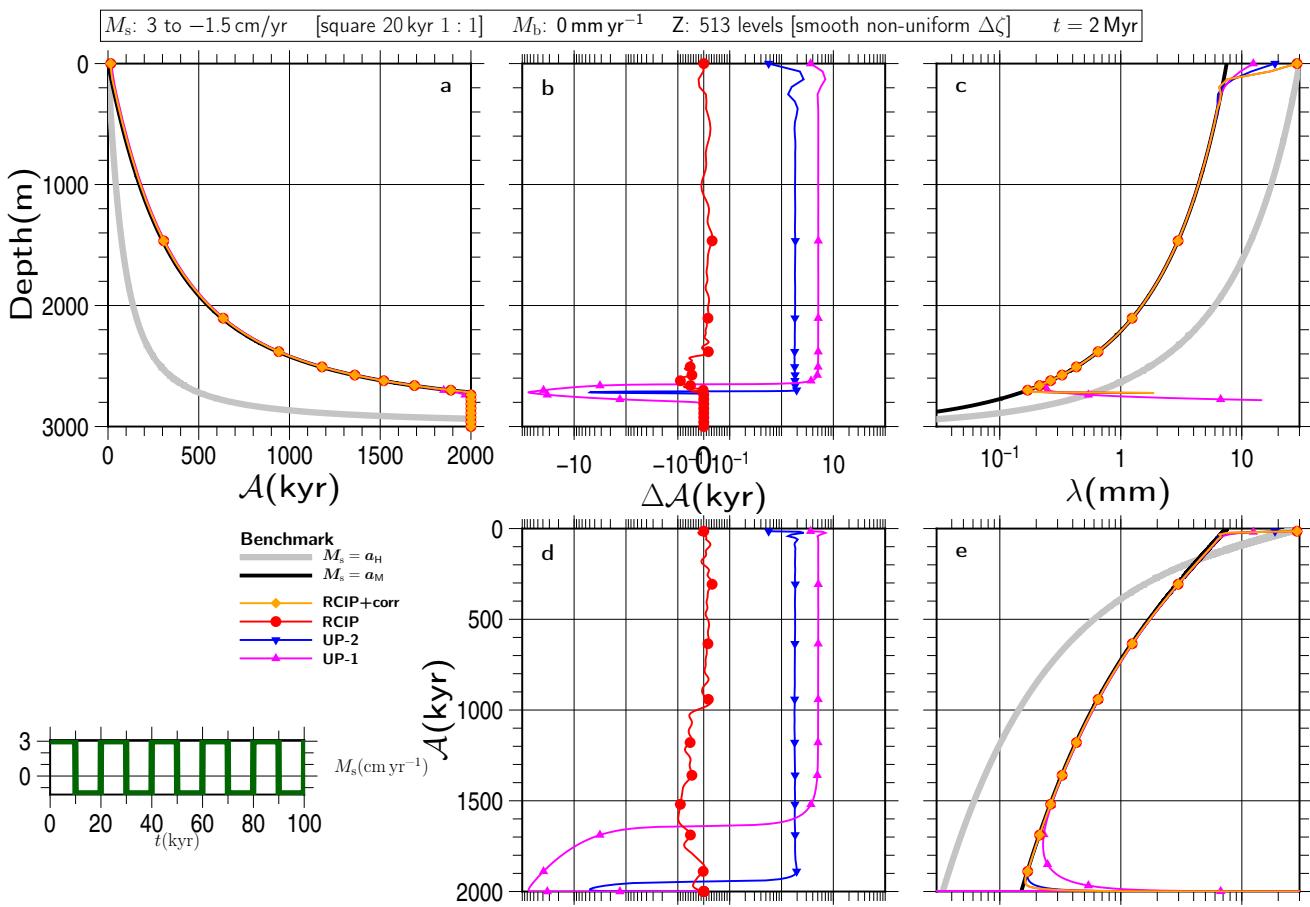


Figure S117

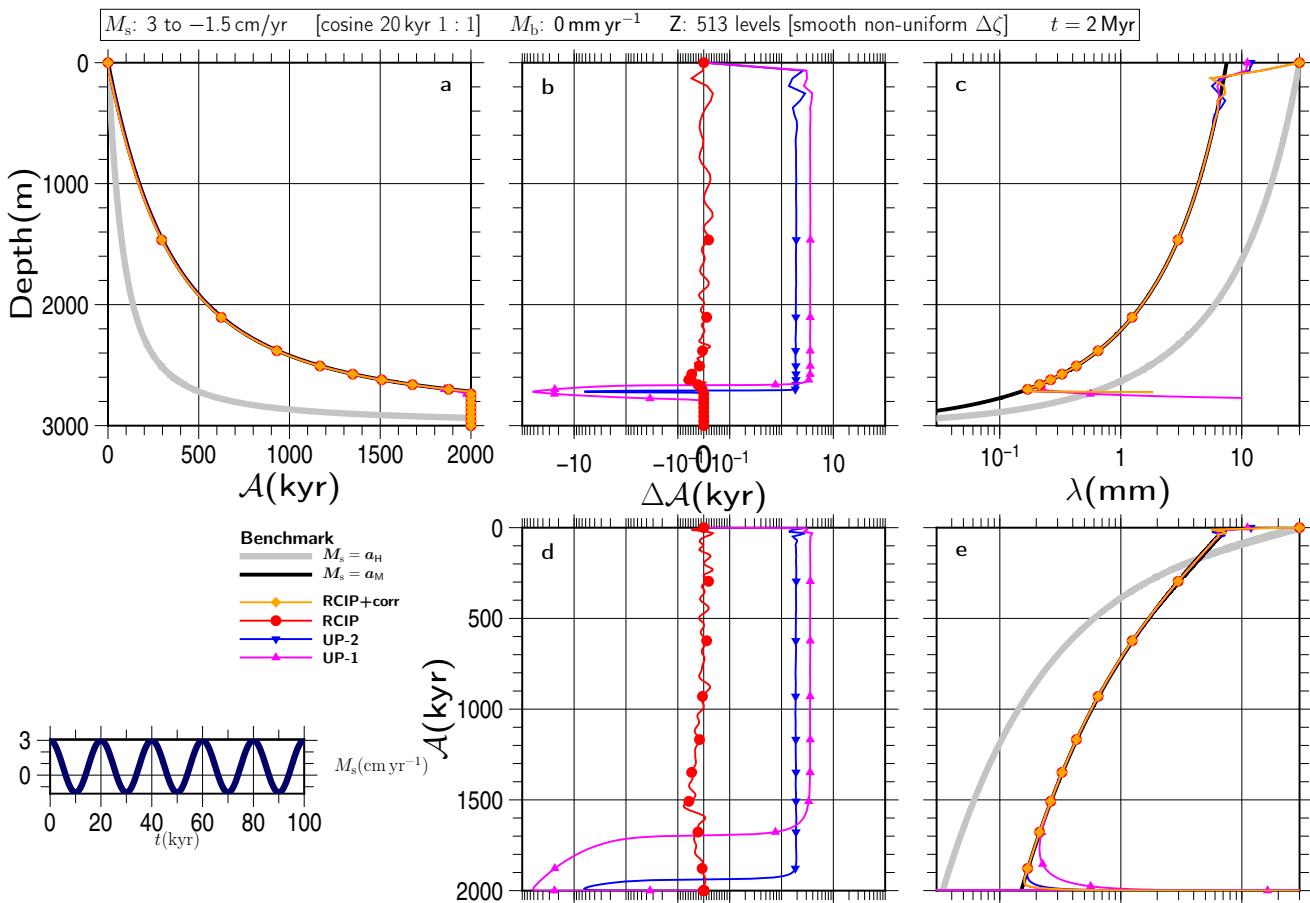


Figure S118

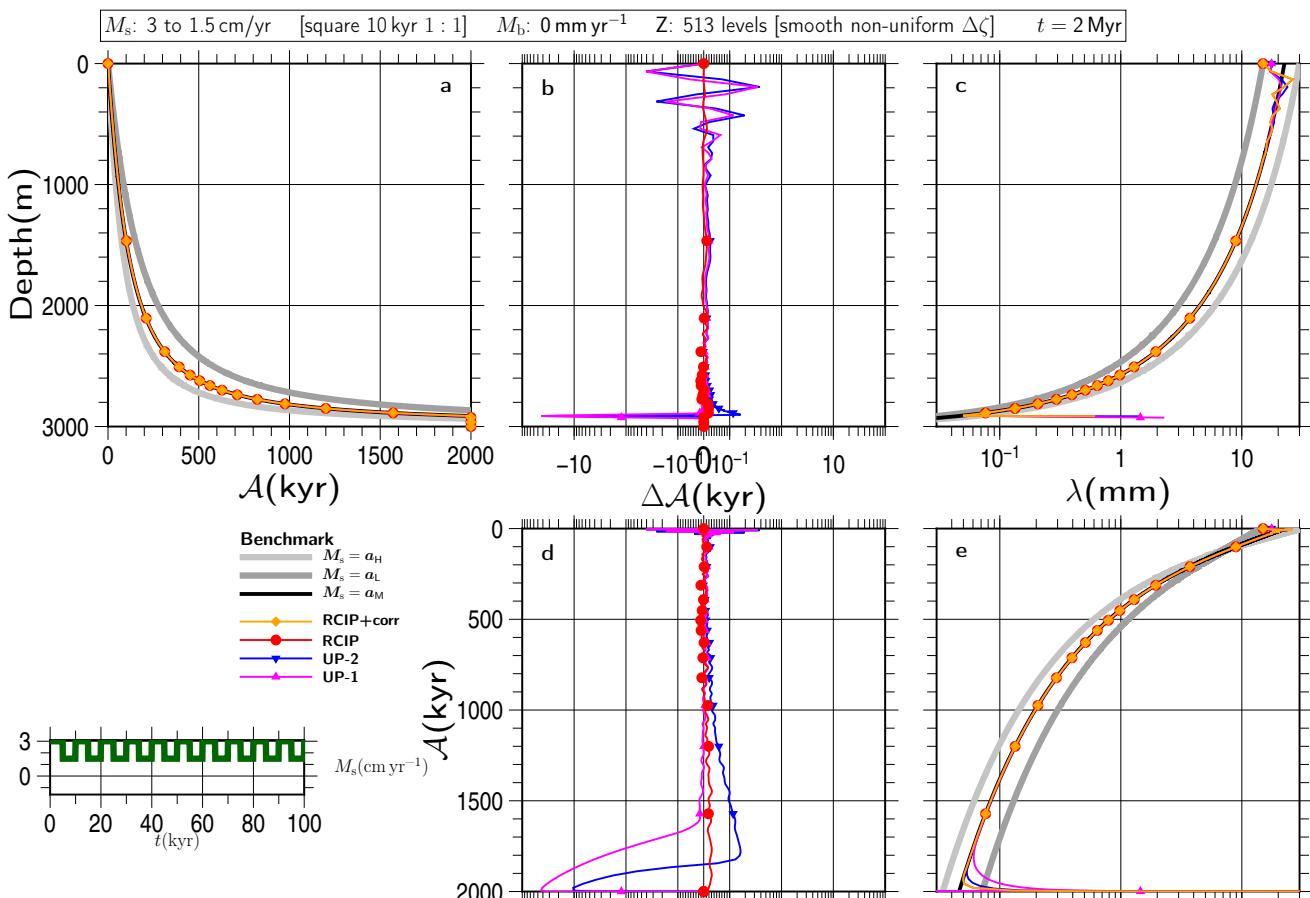


Figure S119

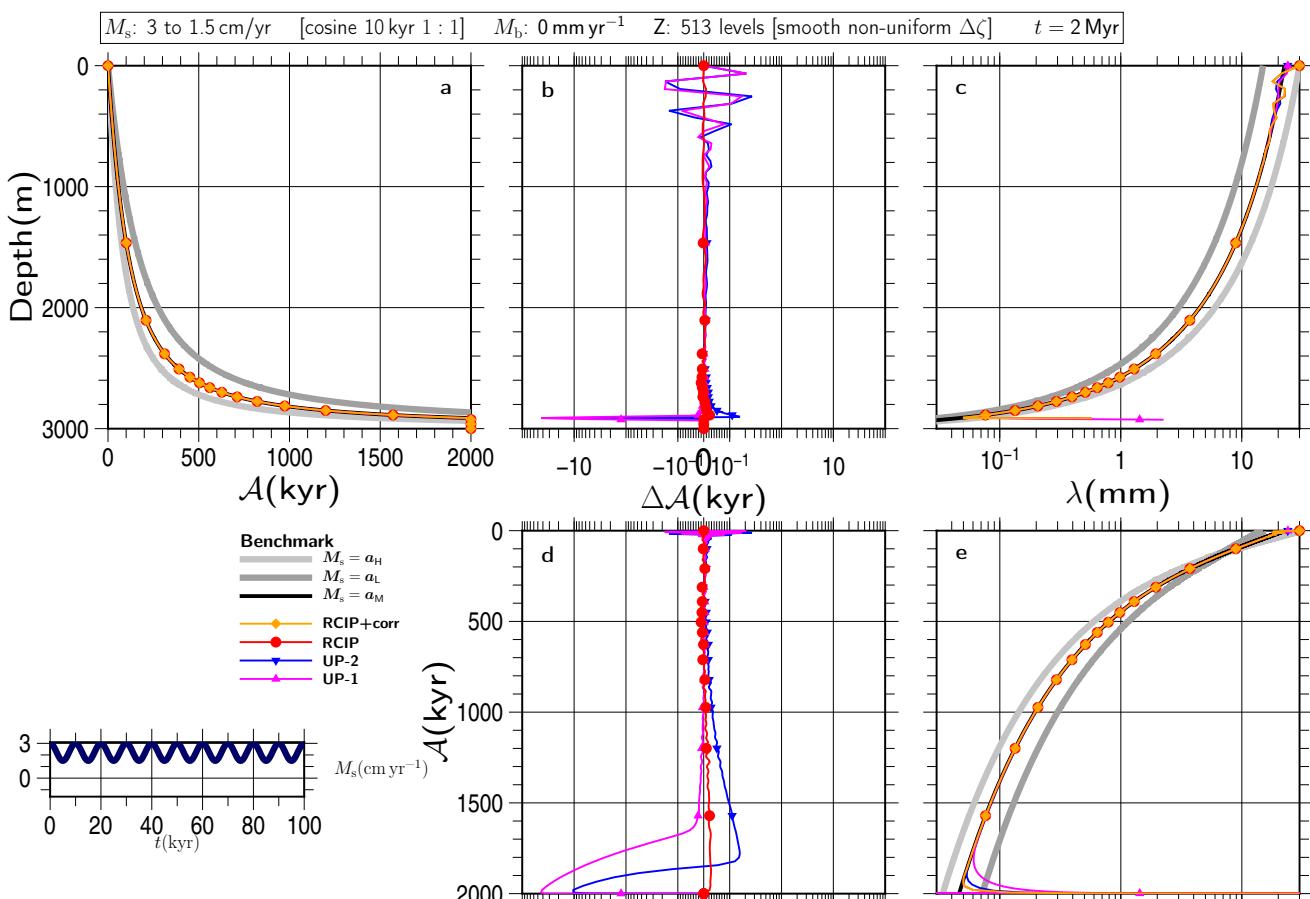


Figure S120

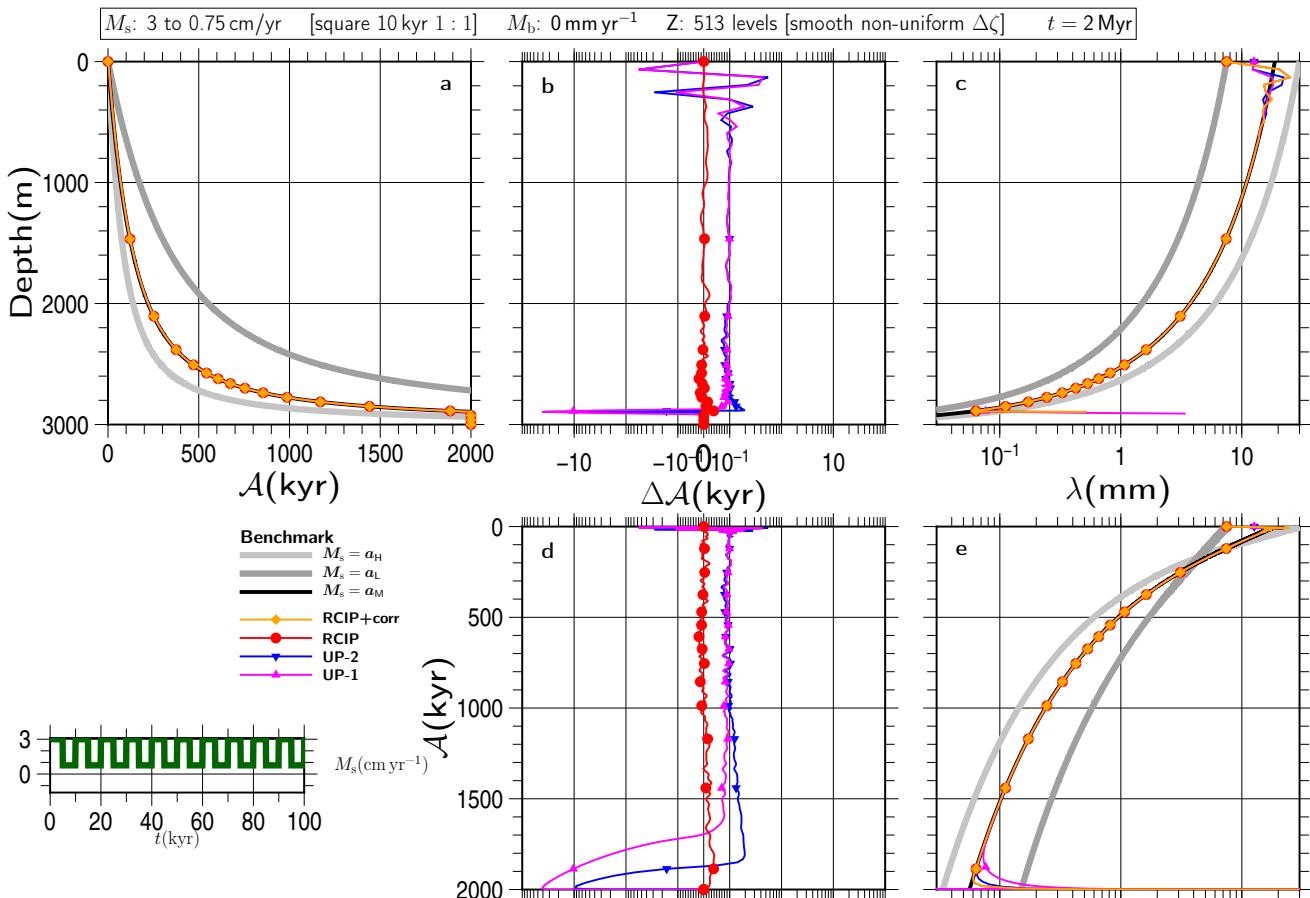


Figure S121

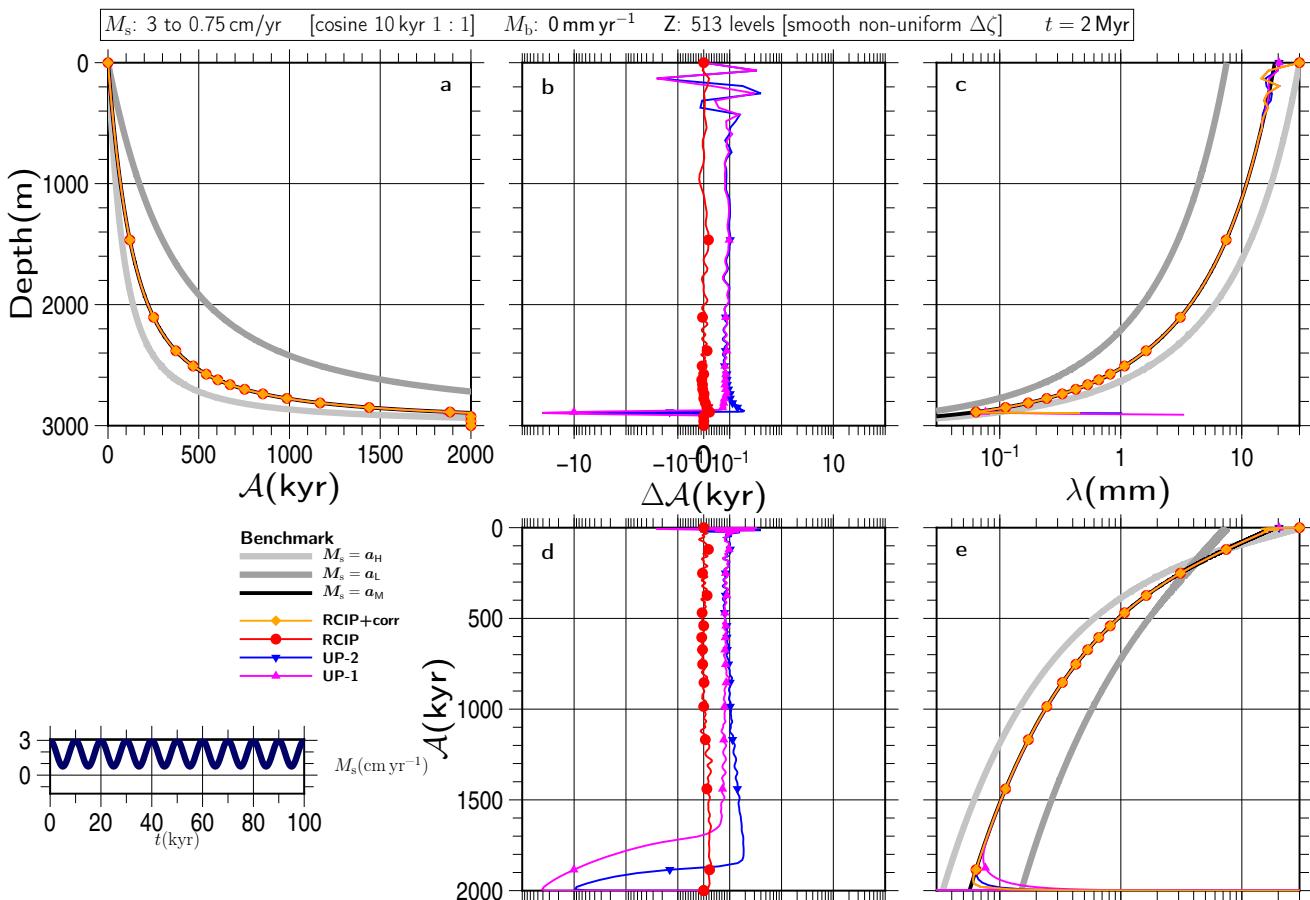


Figure S122

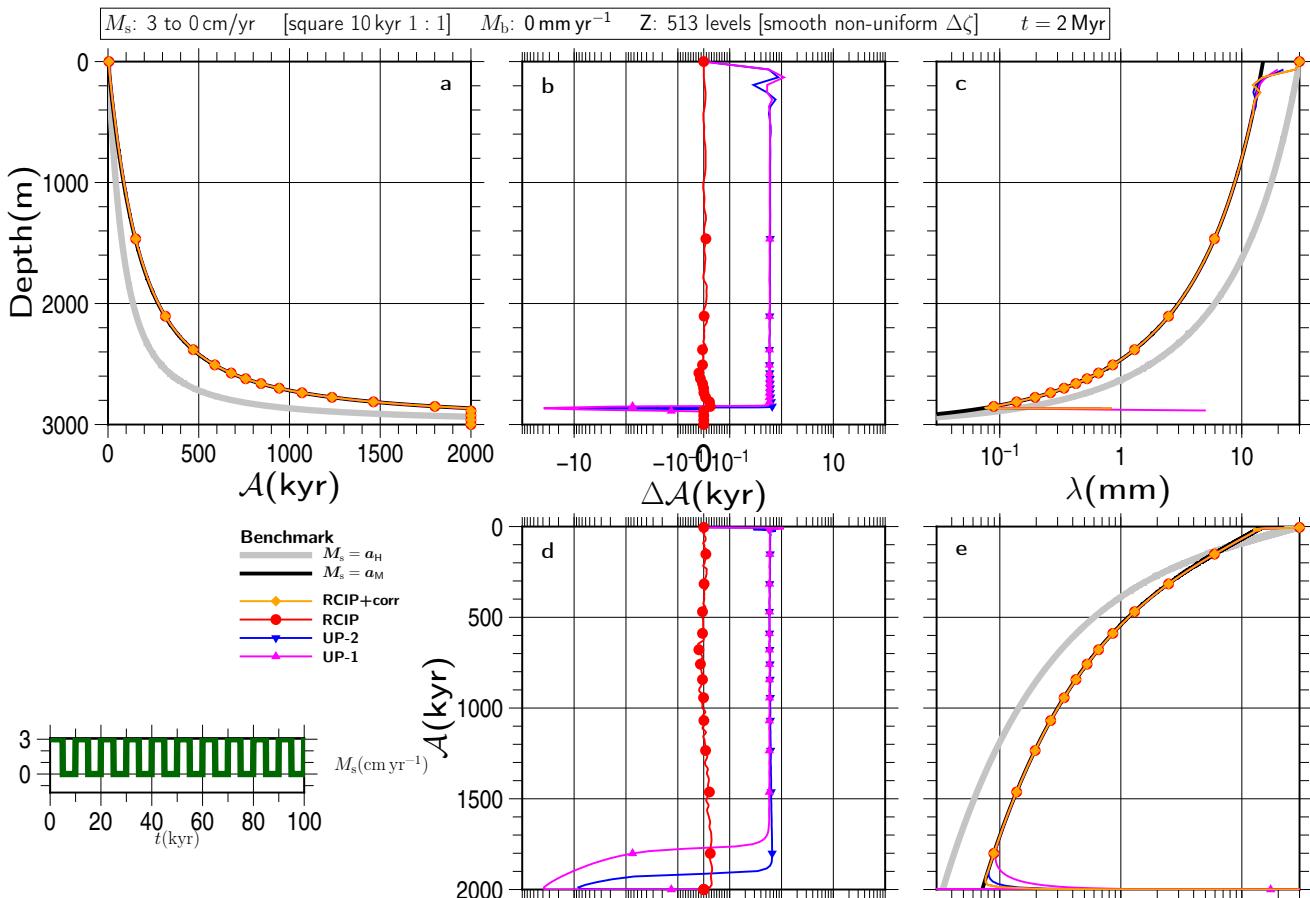


Figure S123

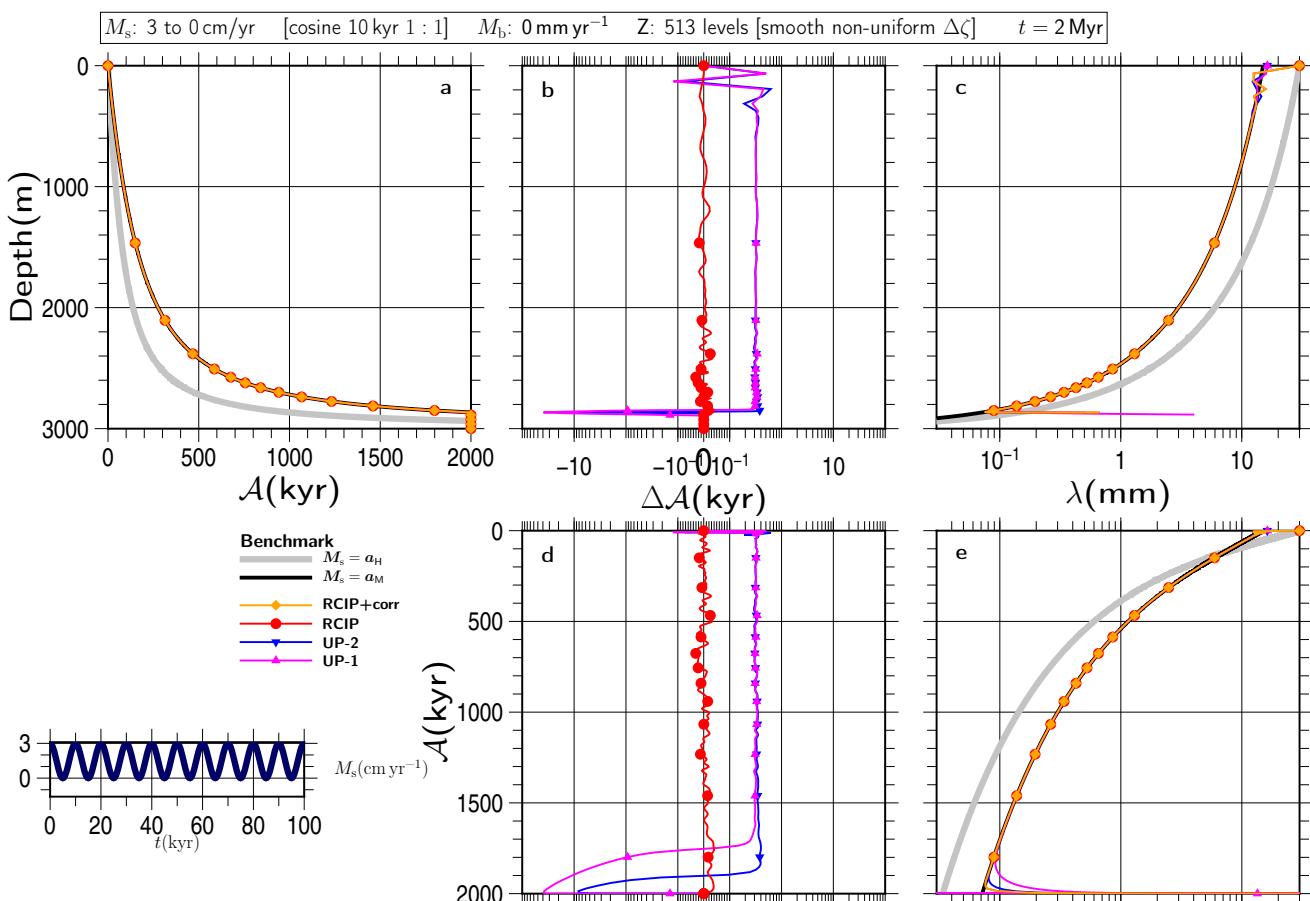


Figure S124

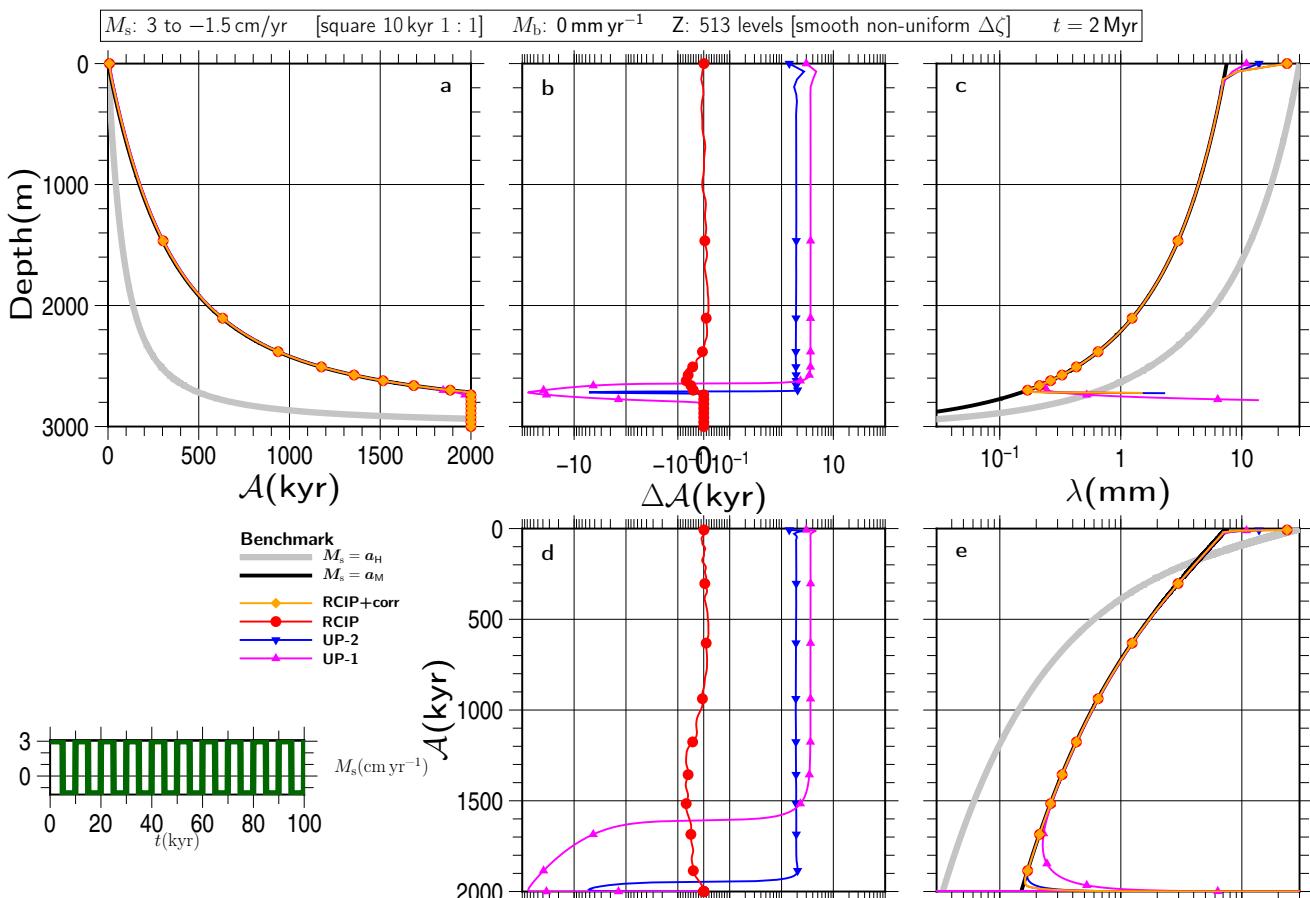


Figure S125

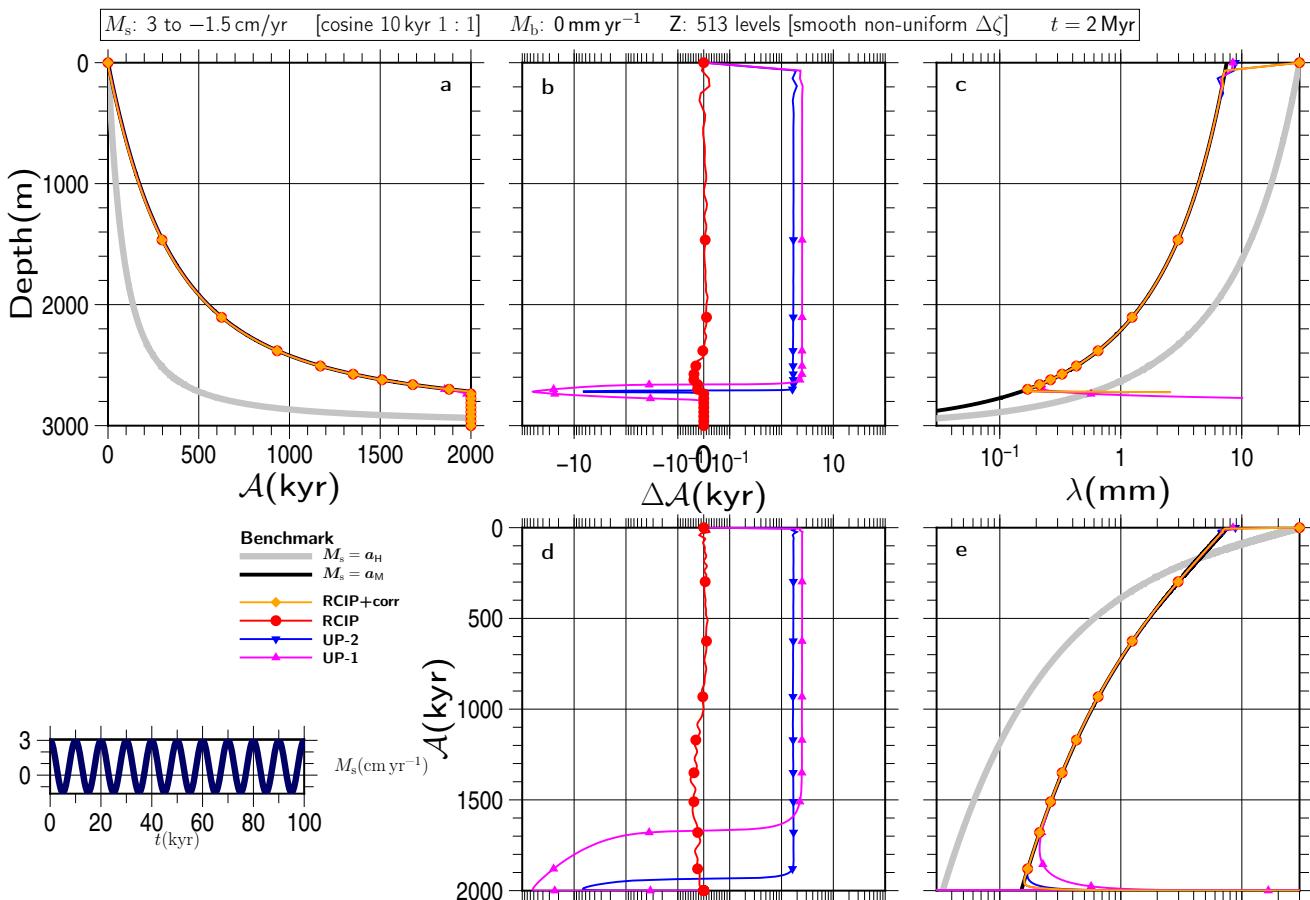


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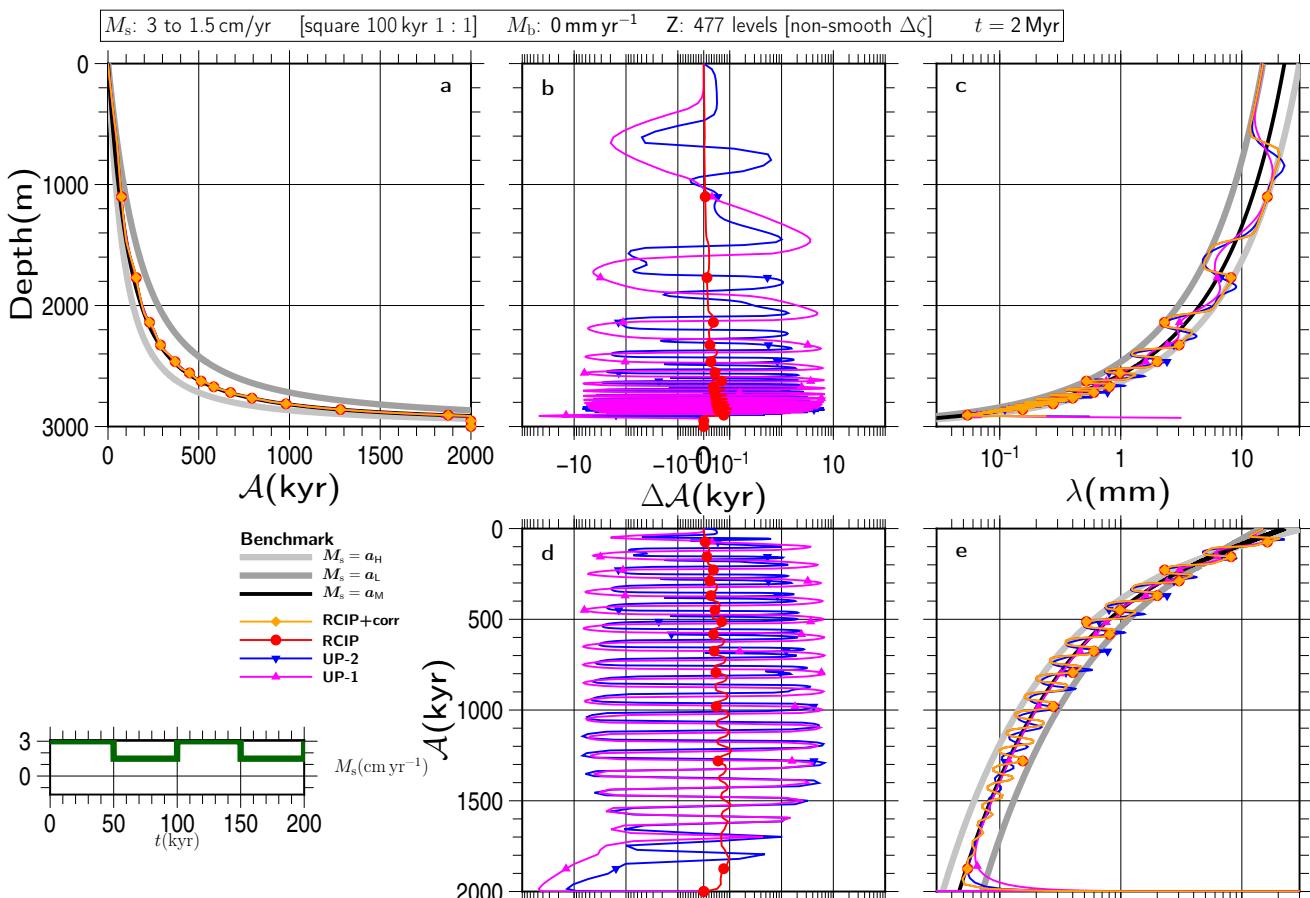


Figure S127

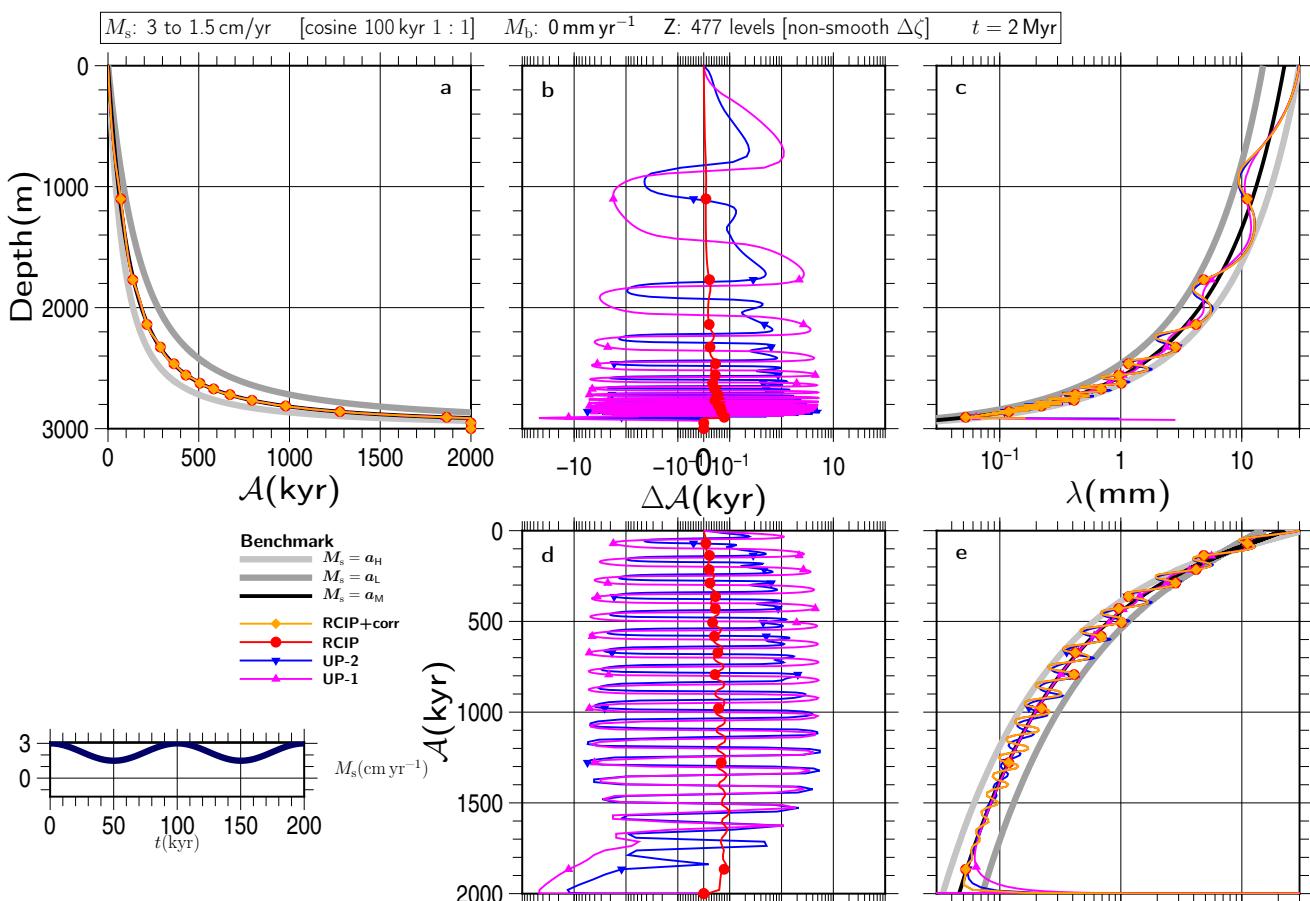


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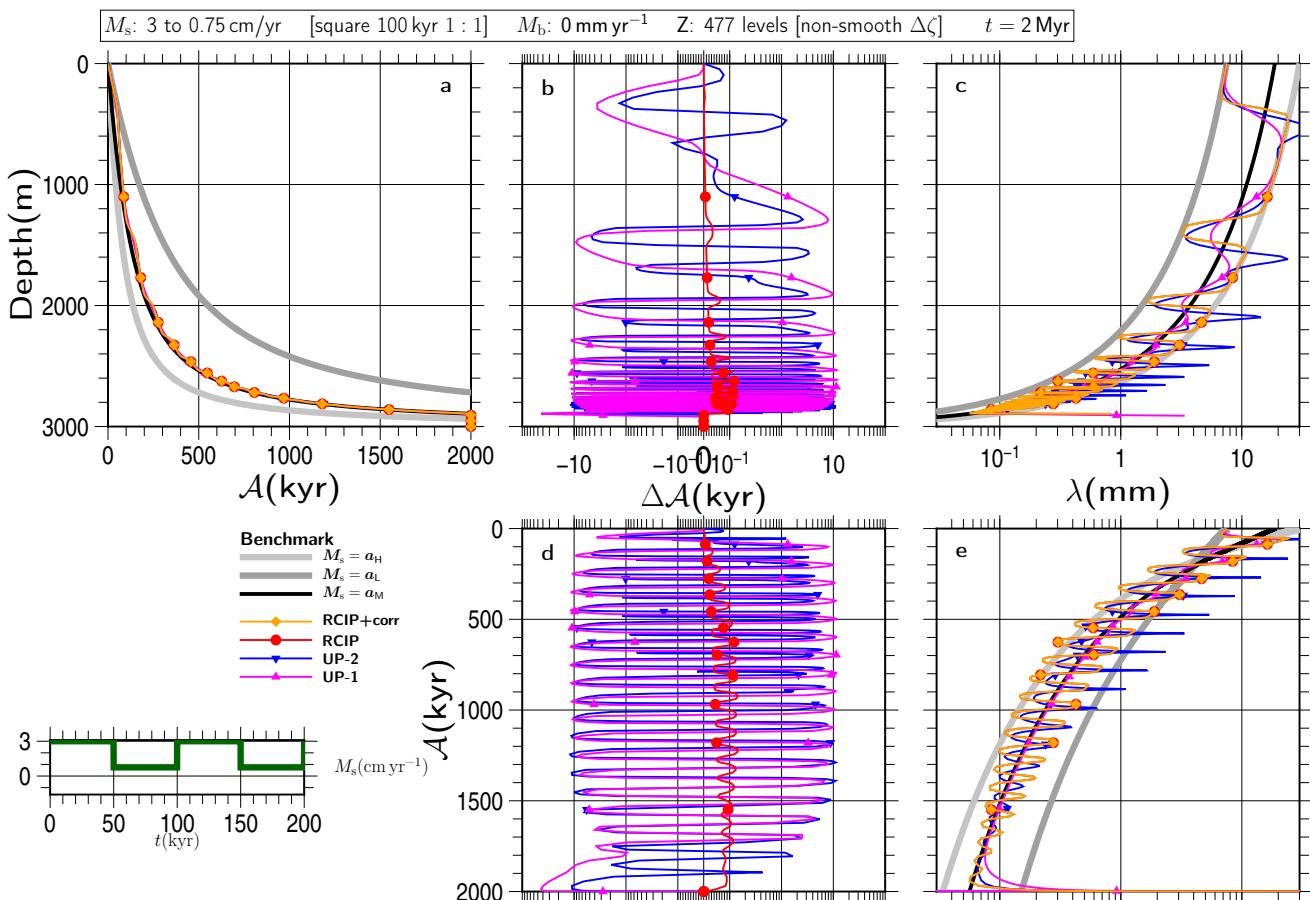


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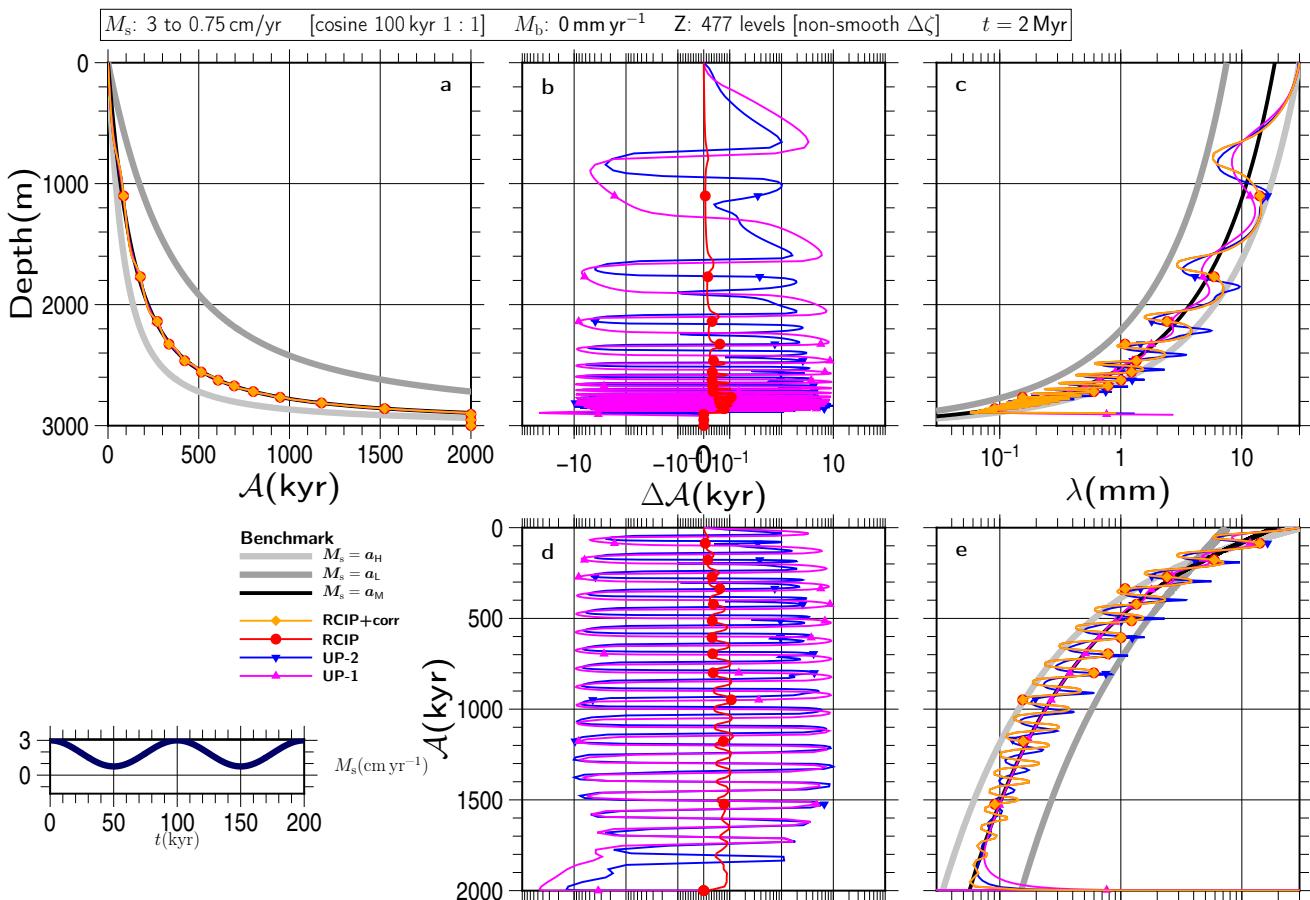


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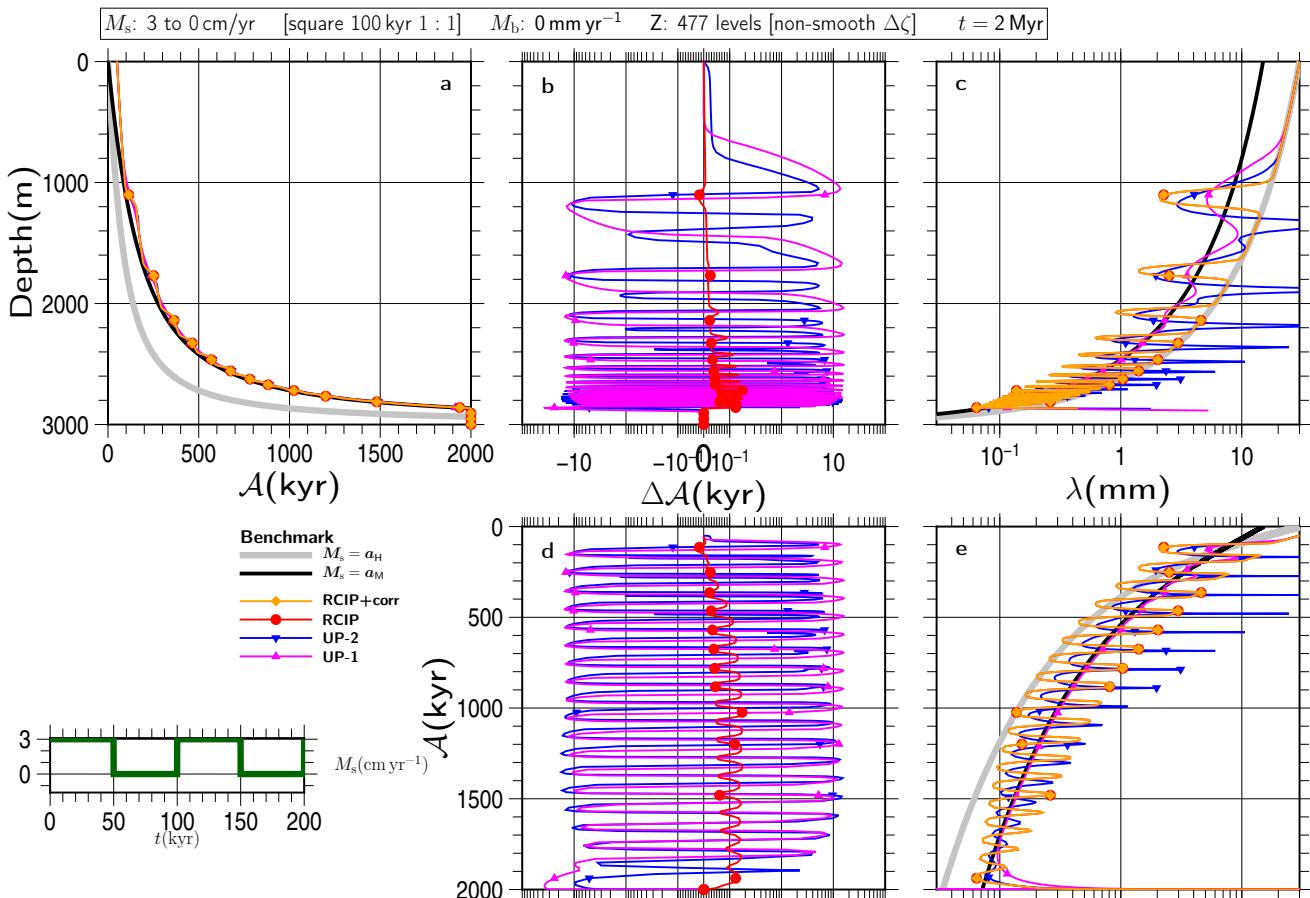


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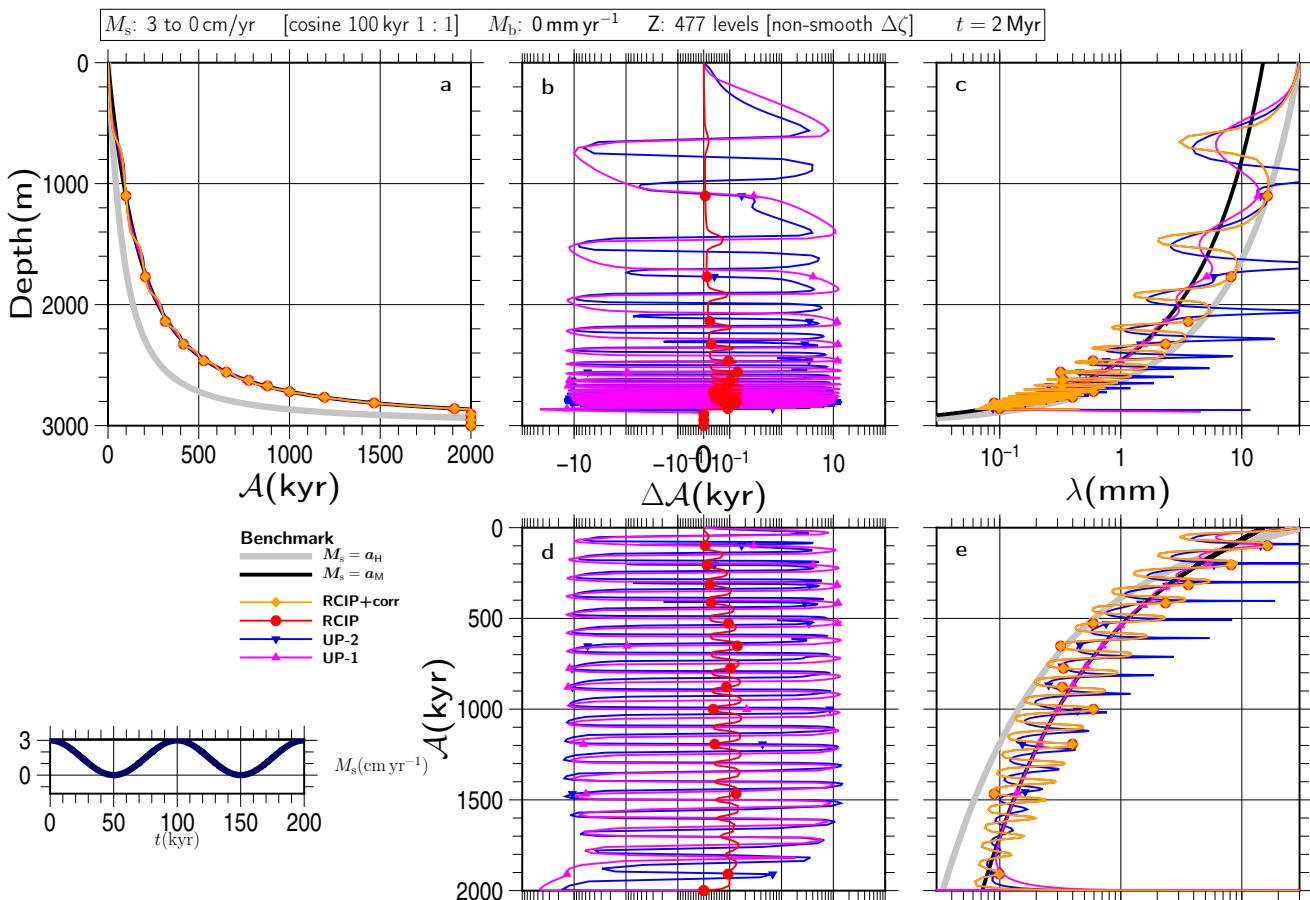


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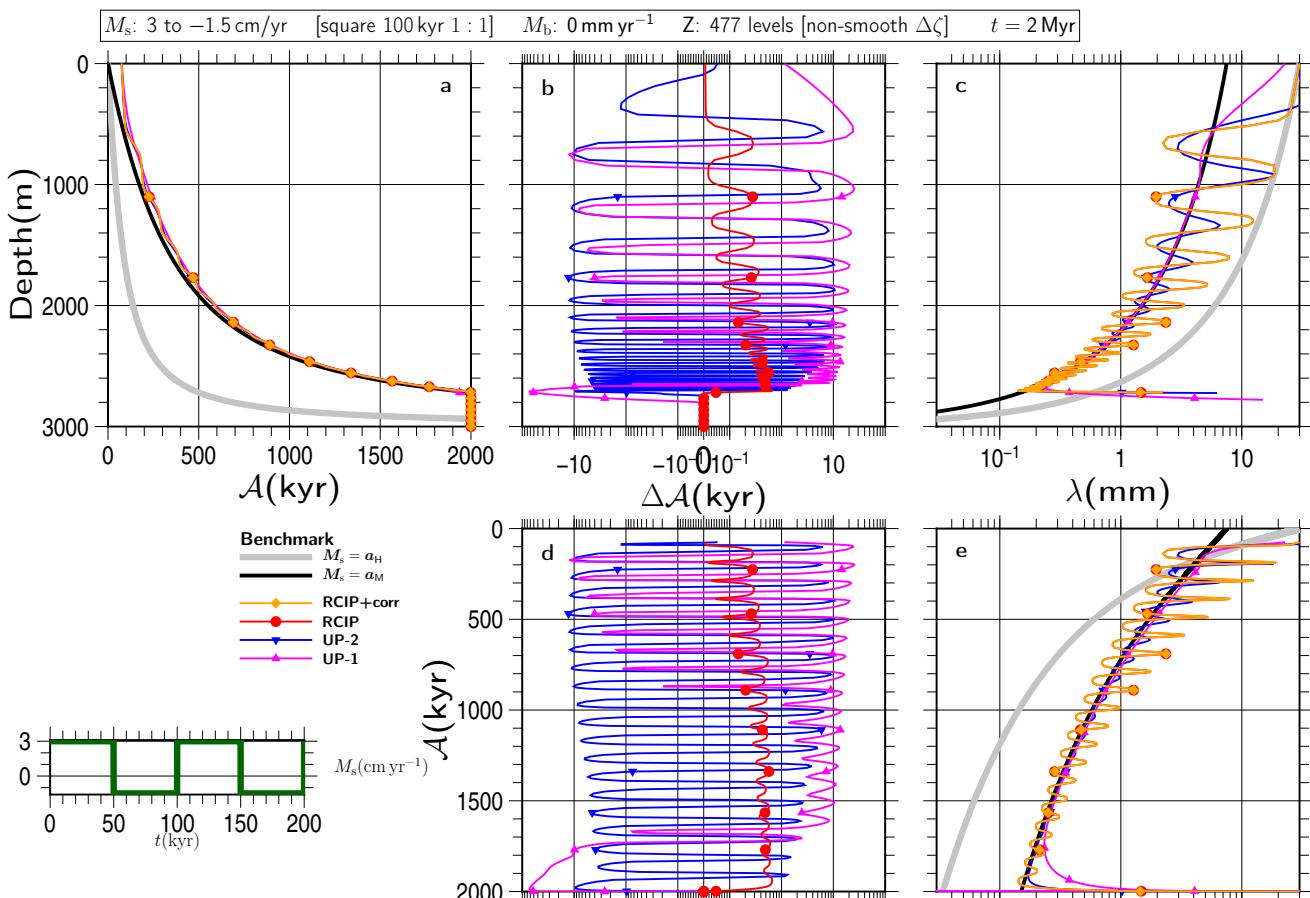


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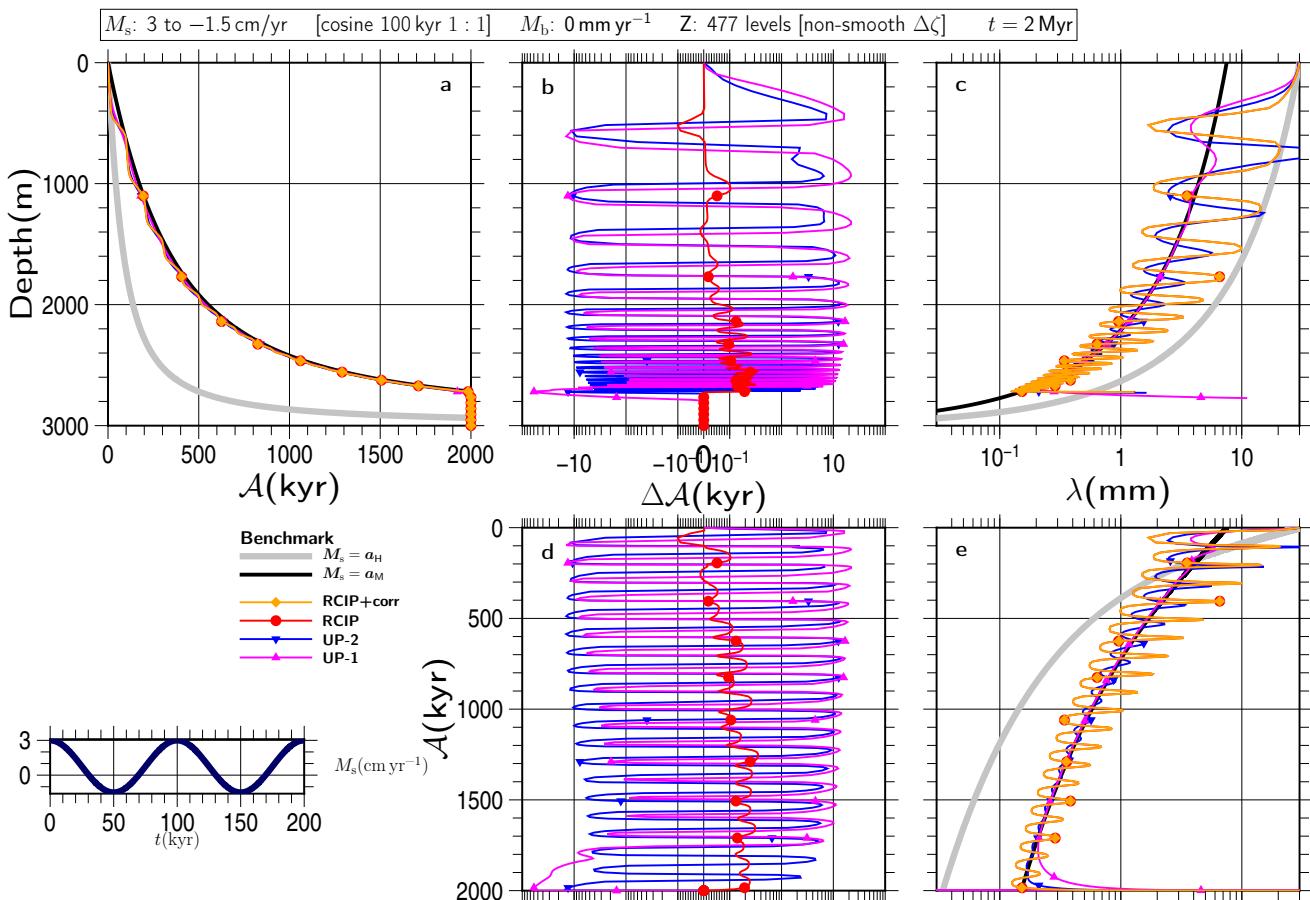


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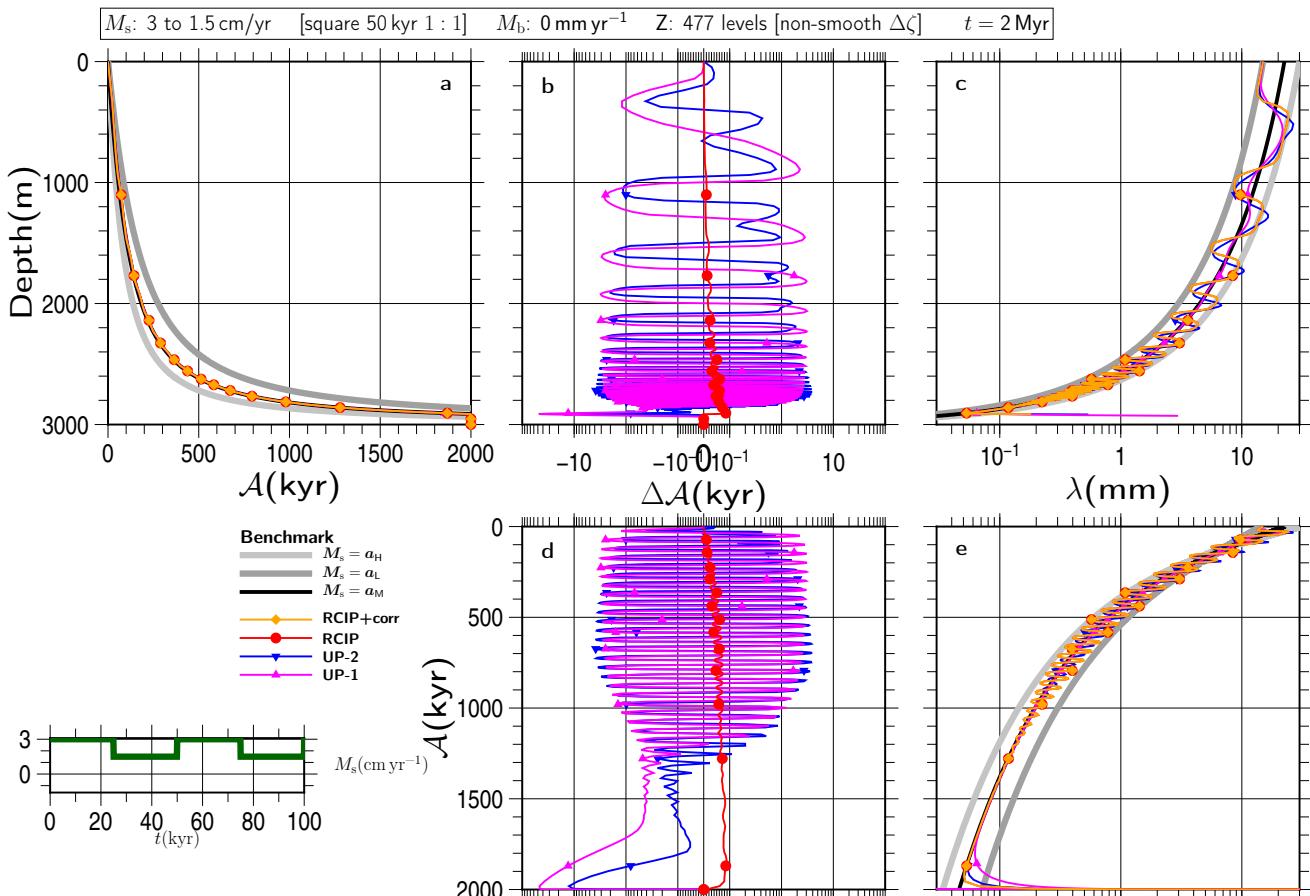


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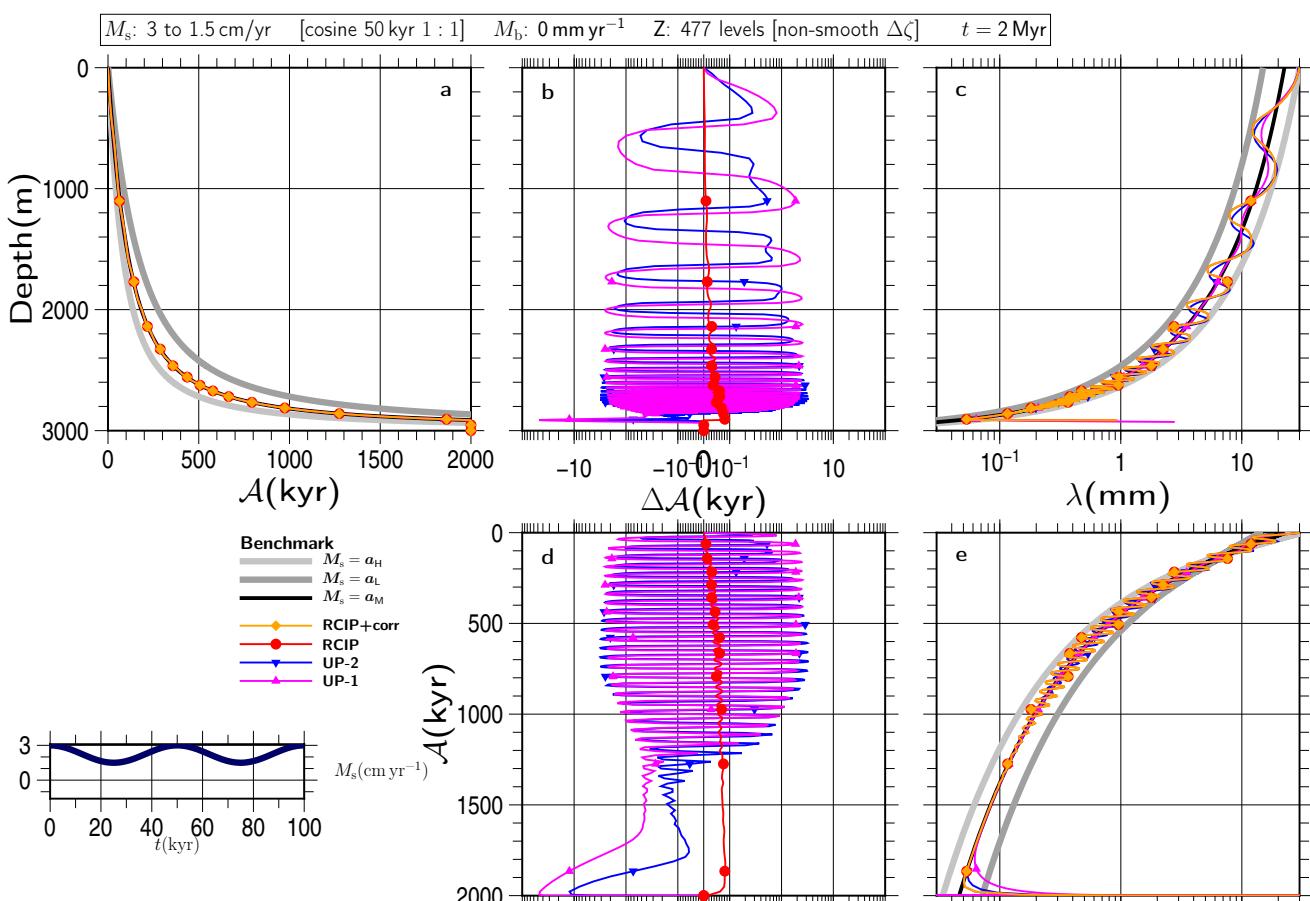


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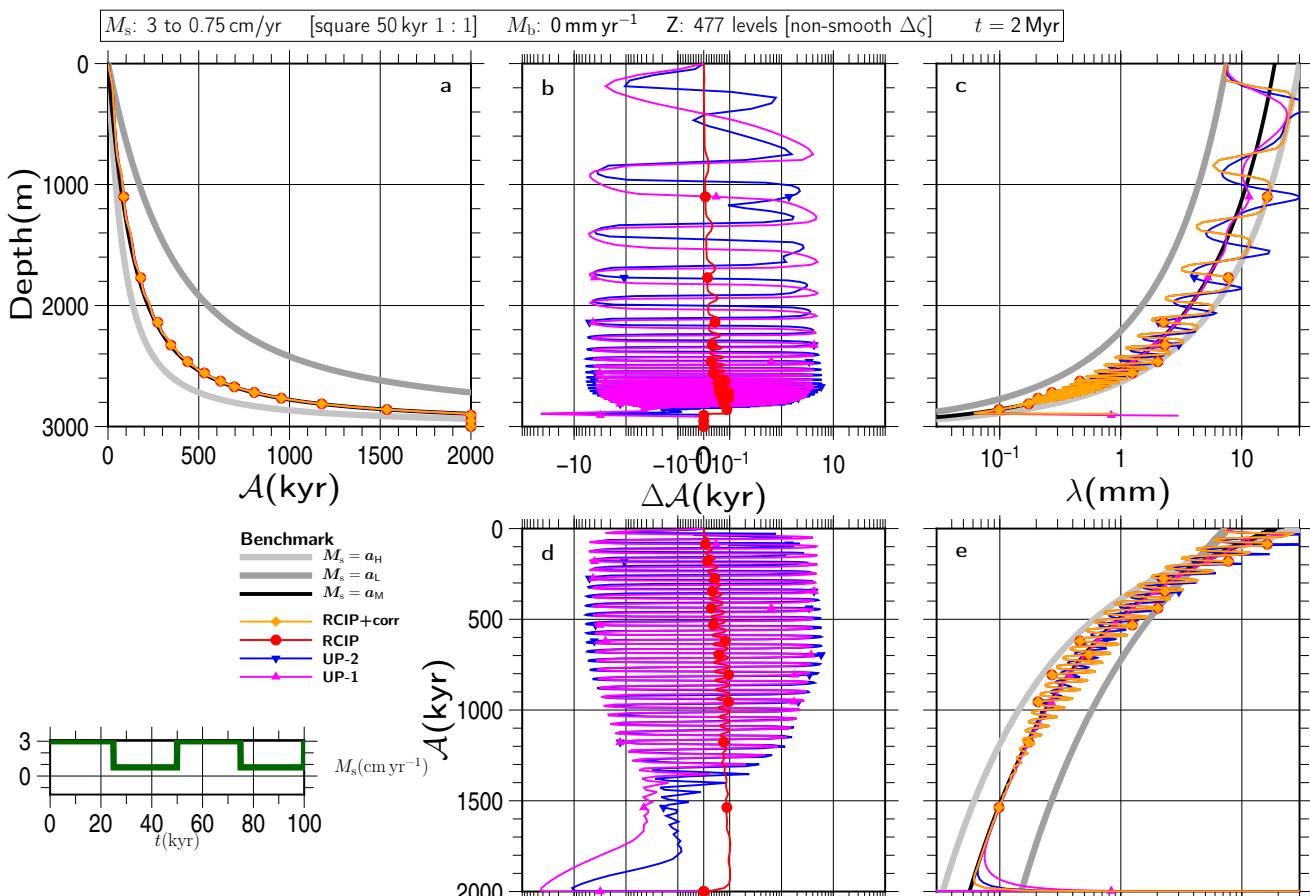


Figure S137

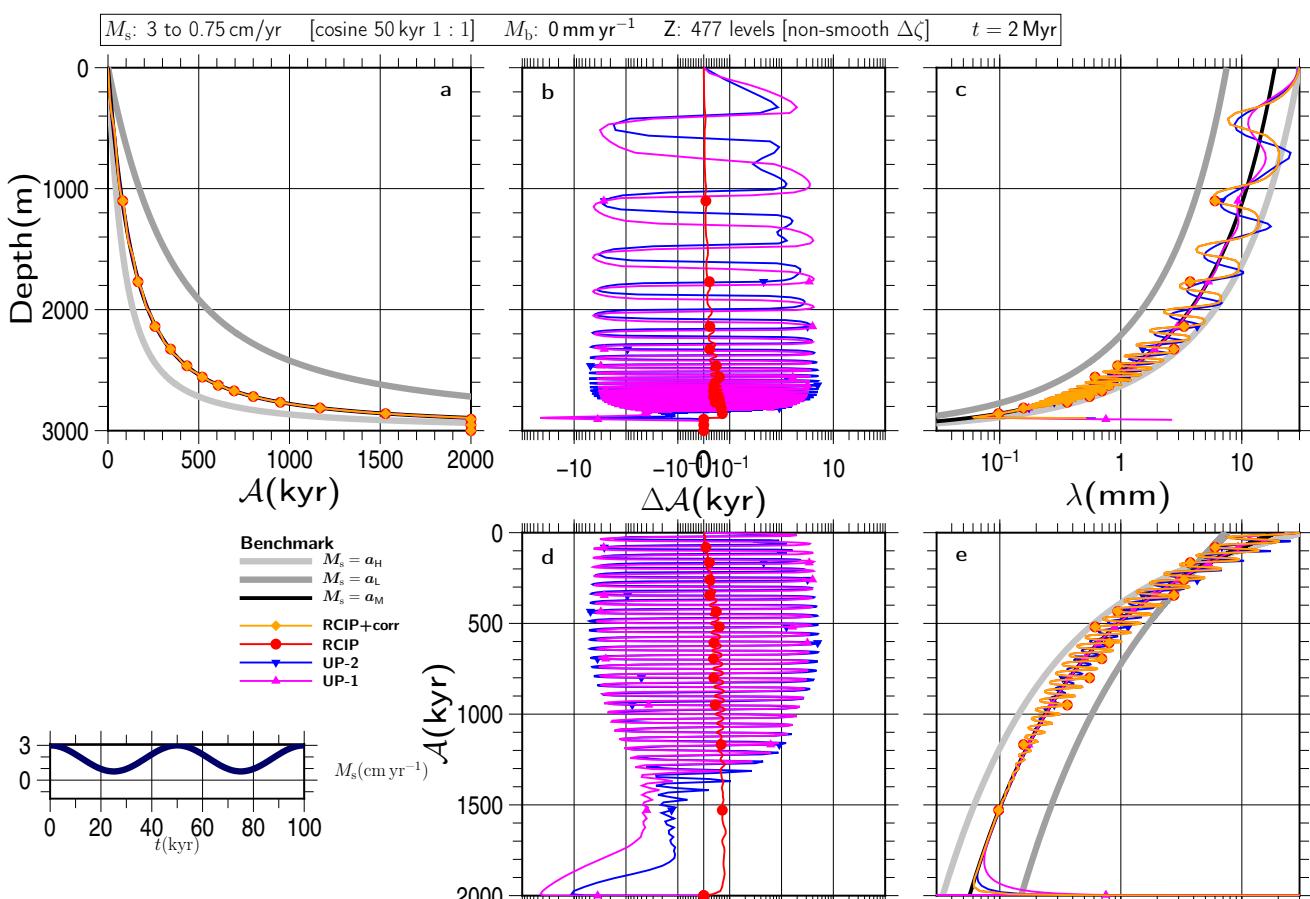


Figure S138

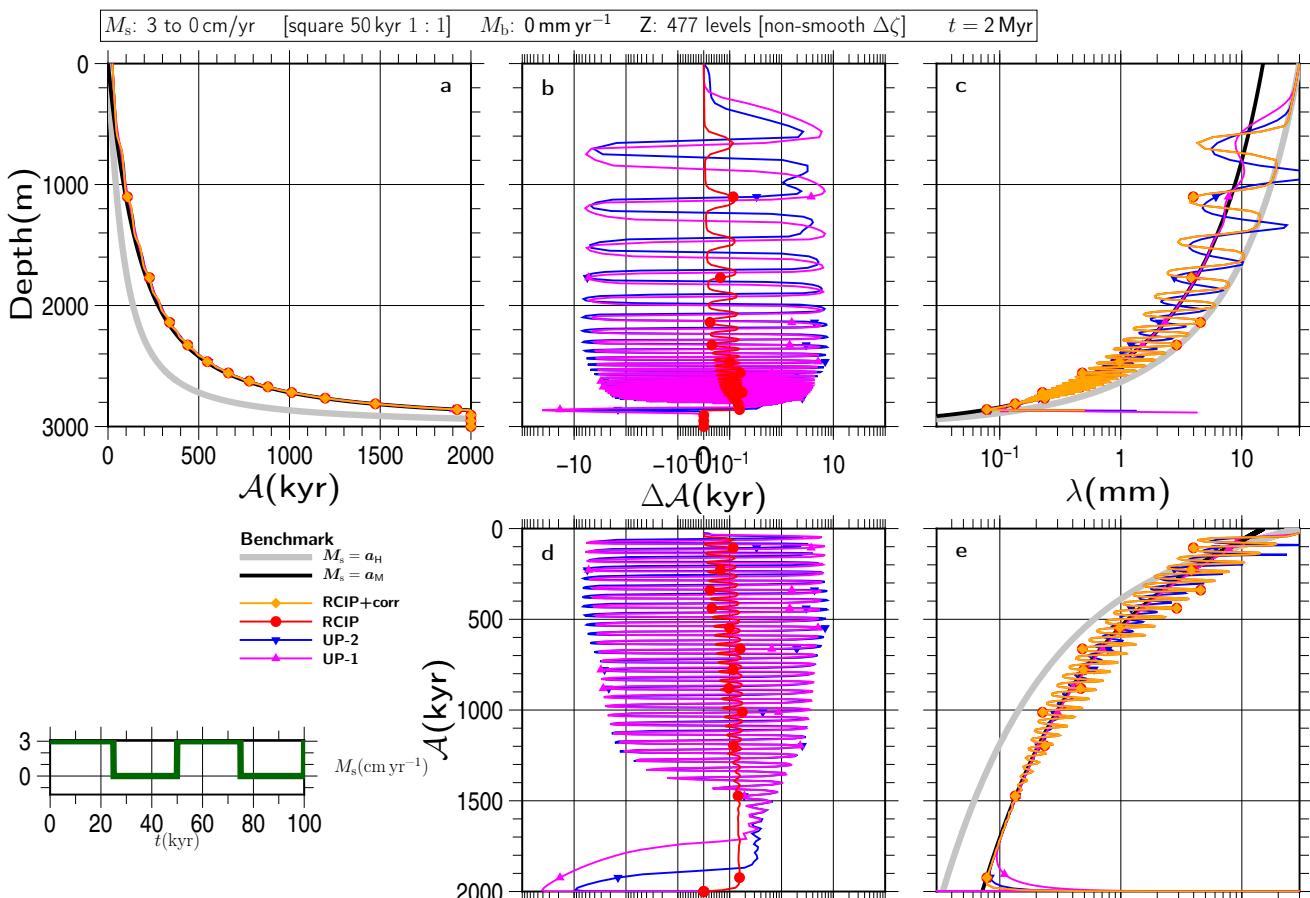


Figure S139

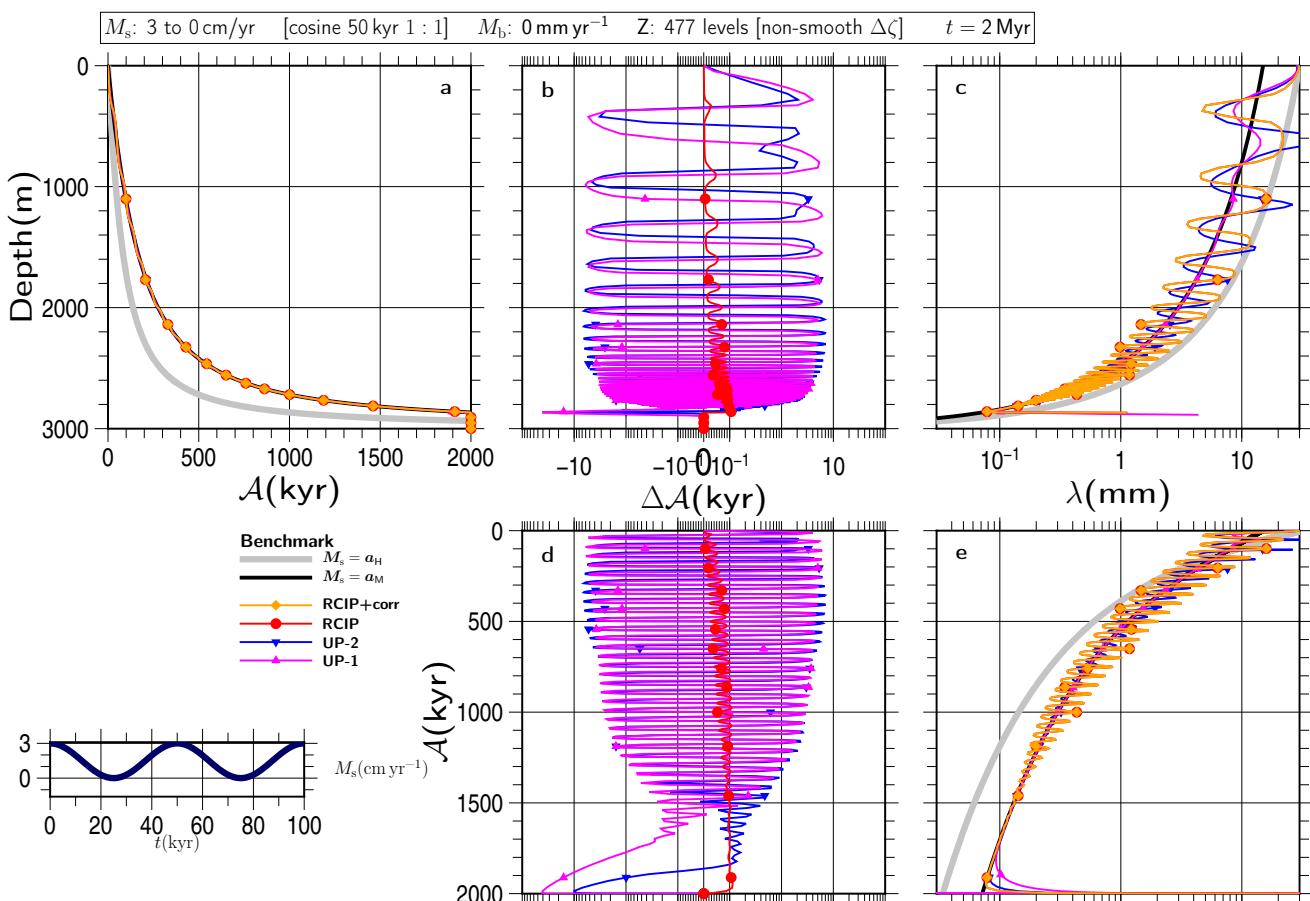


Figure S140

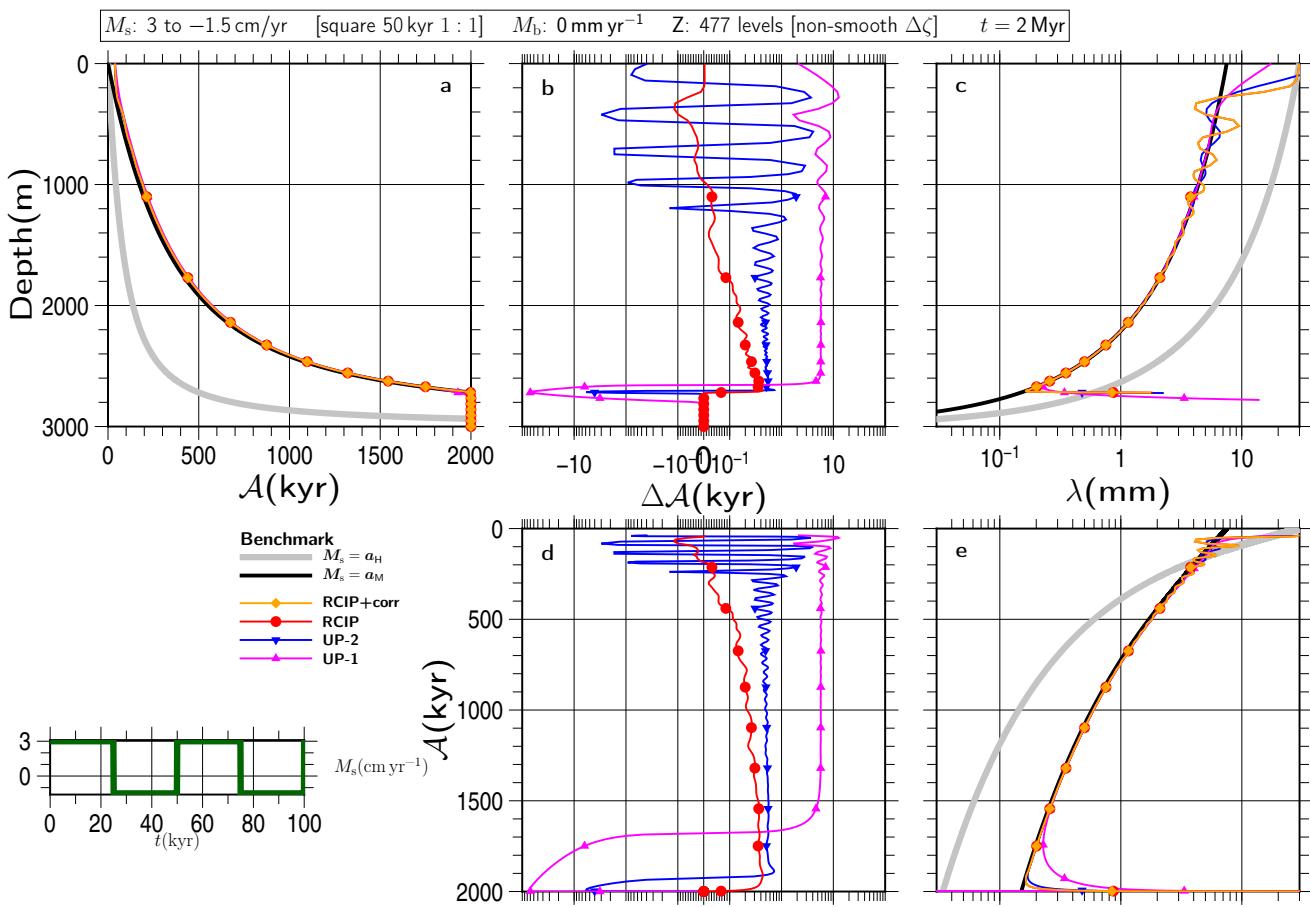


Figure S141

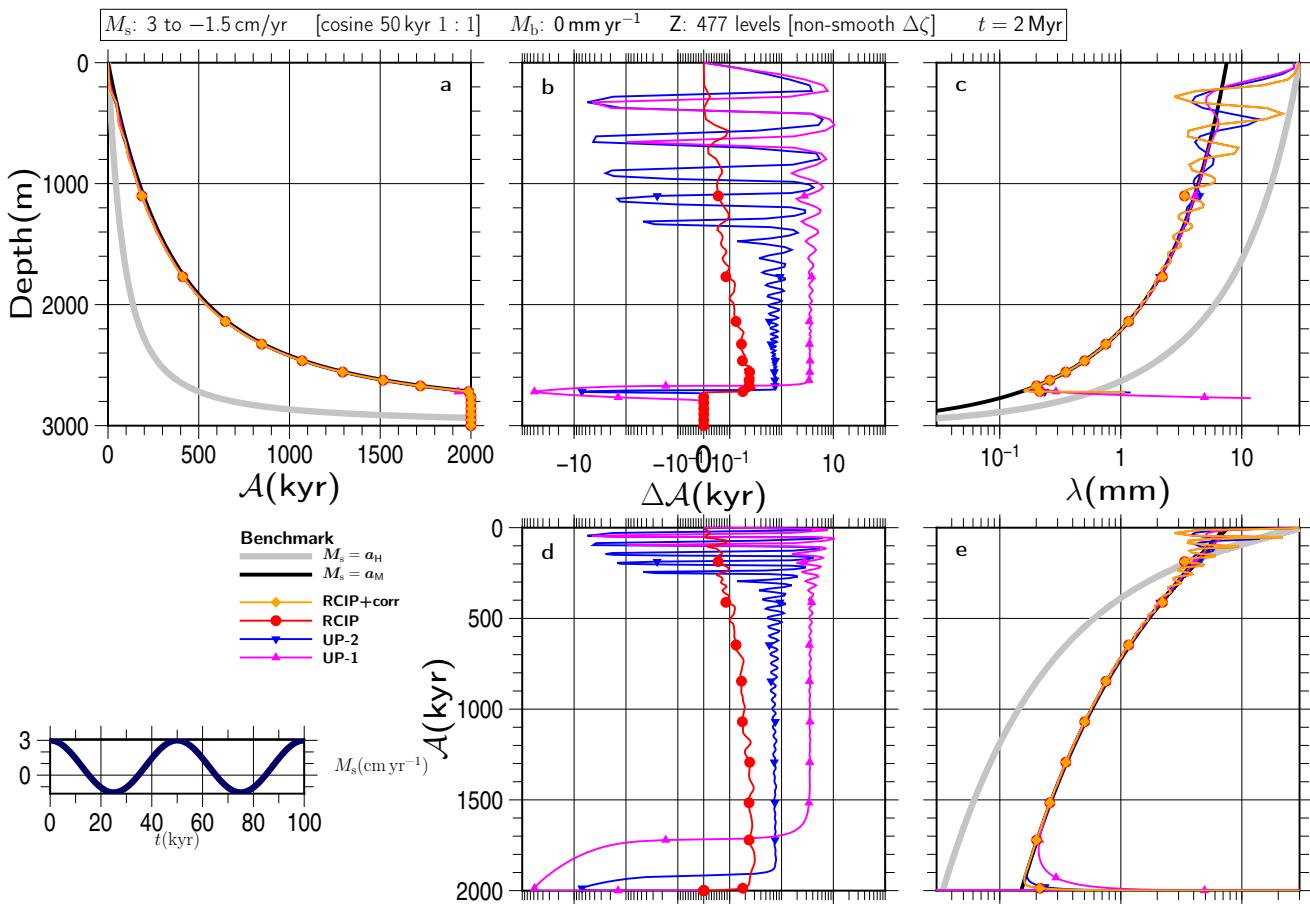


Figure S142

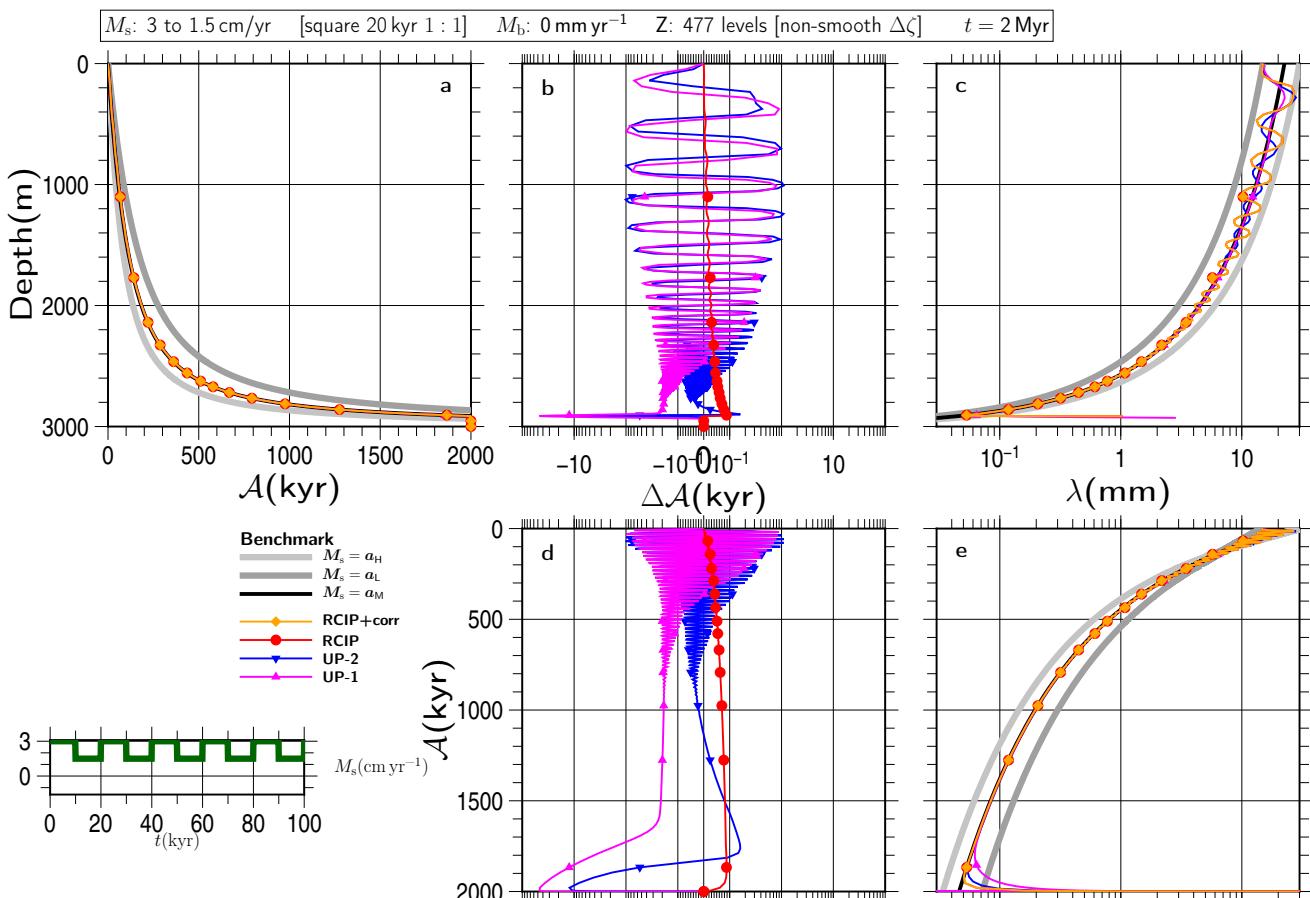


Figure S143

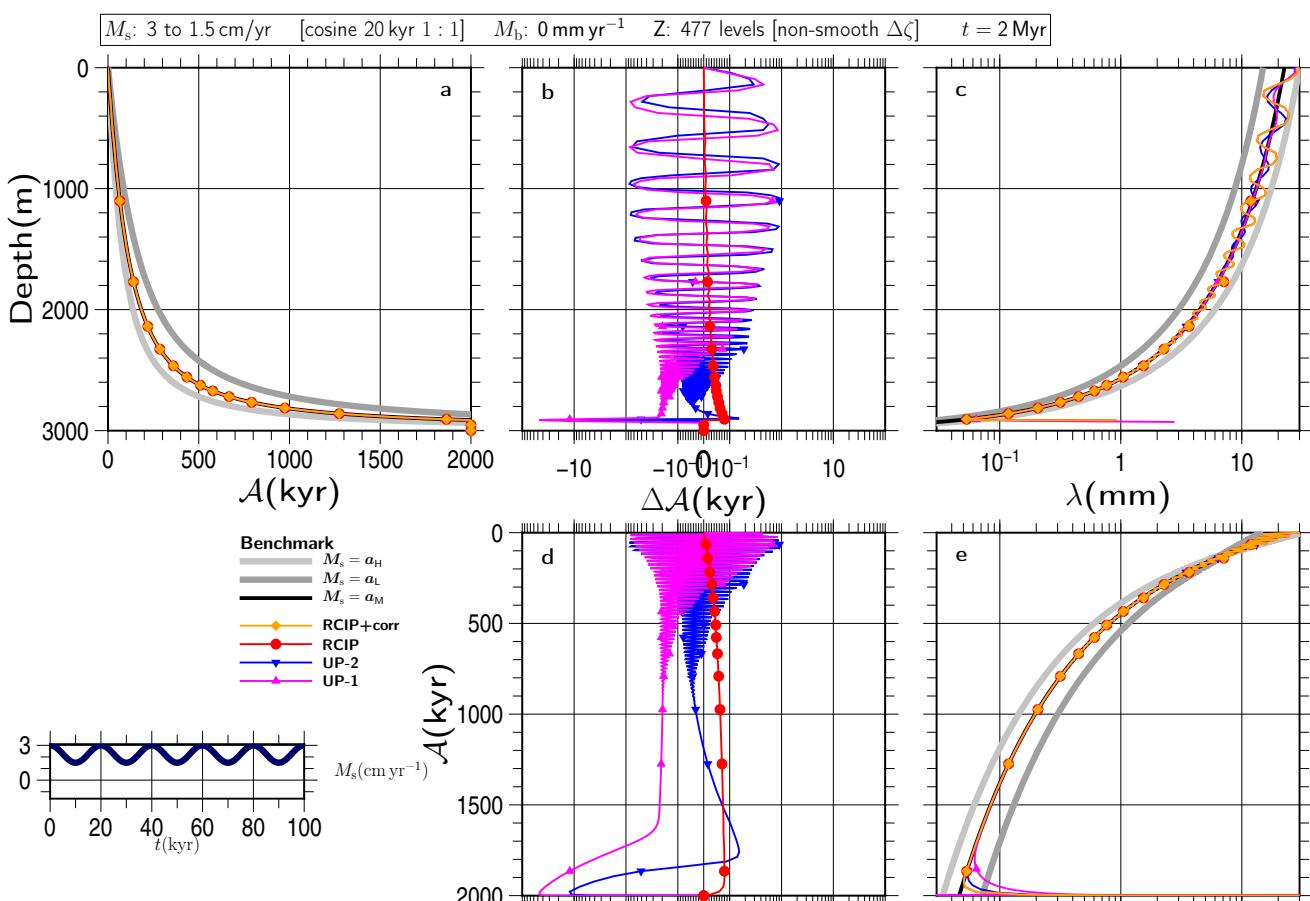


Figure S144

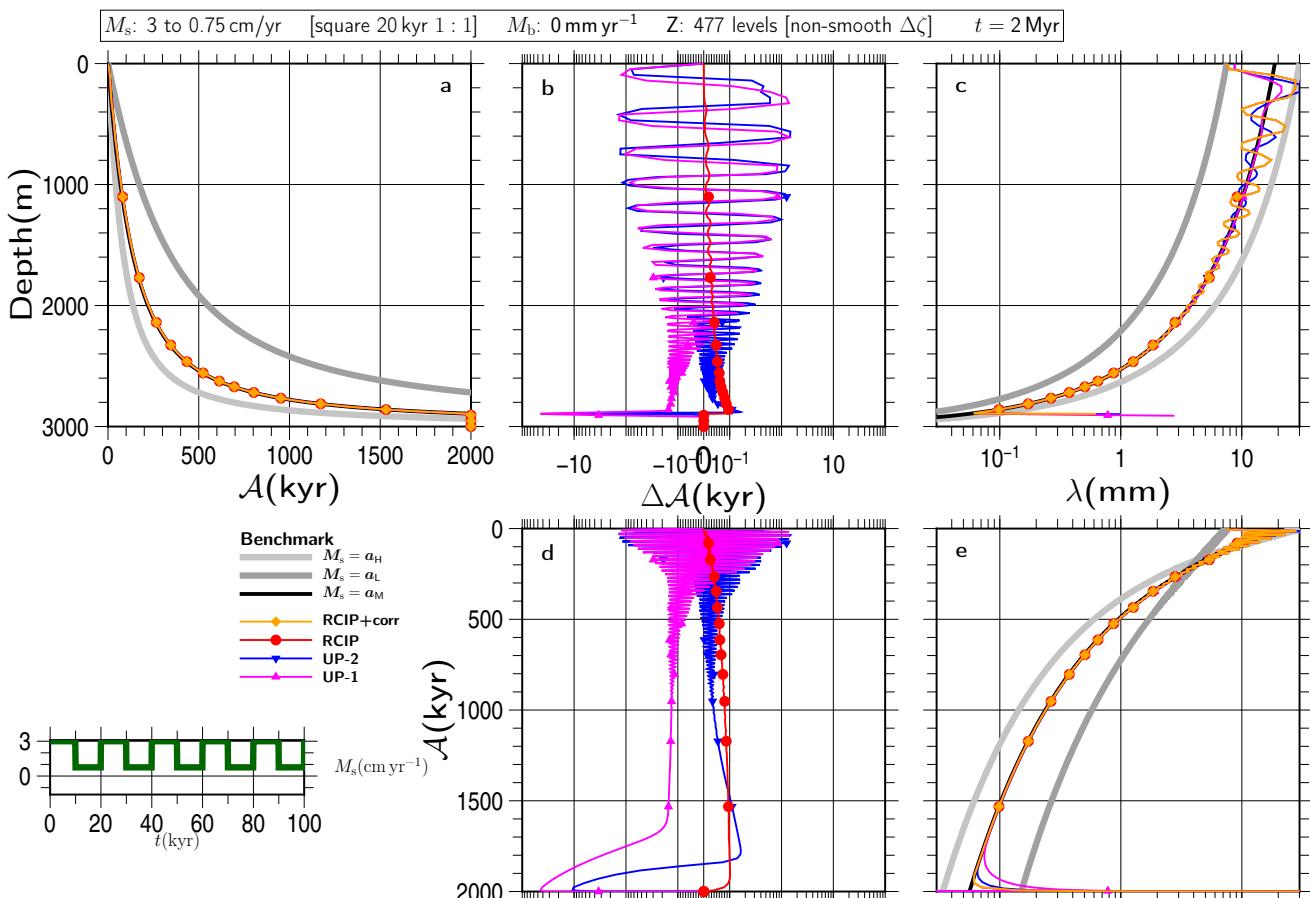


Figure S145

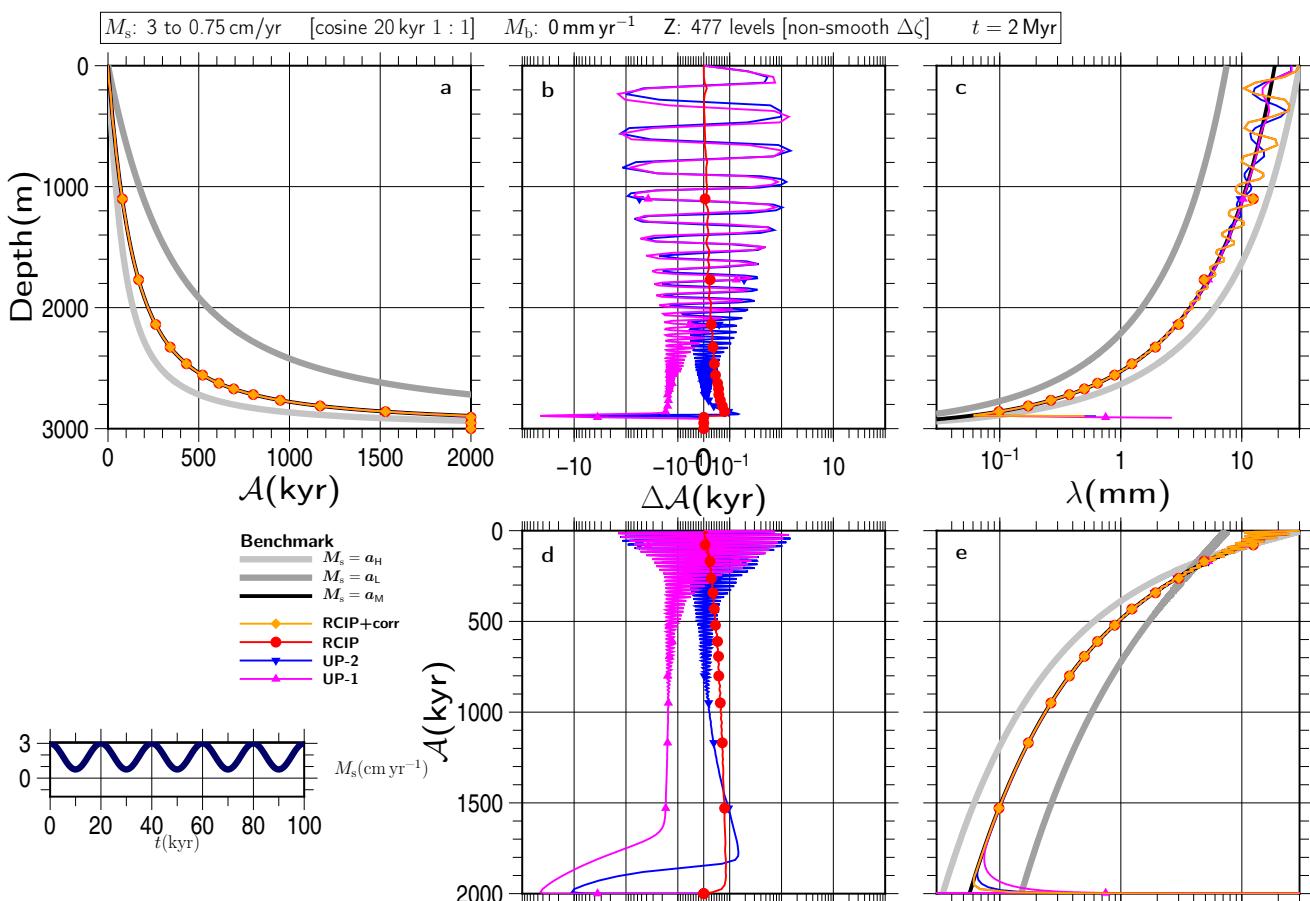


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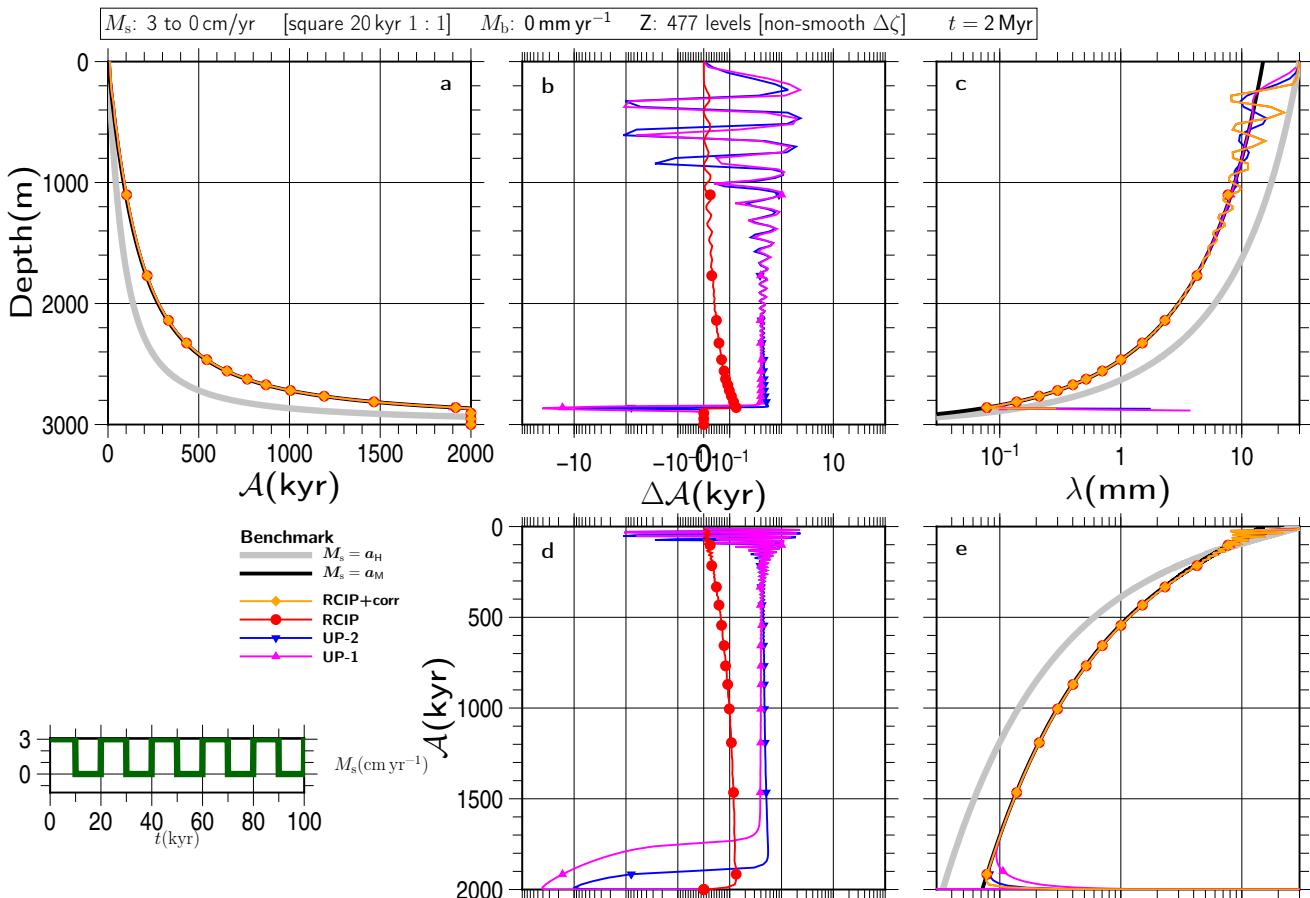


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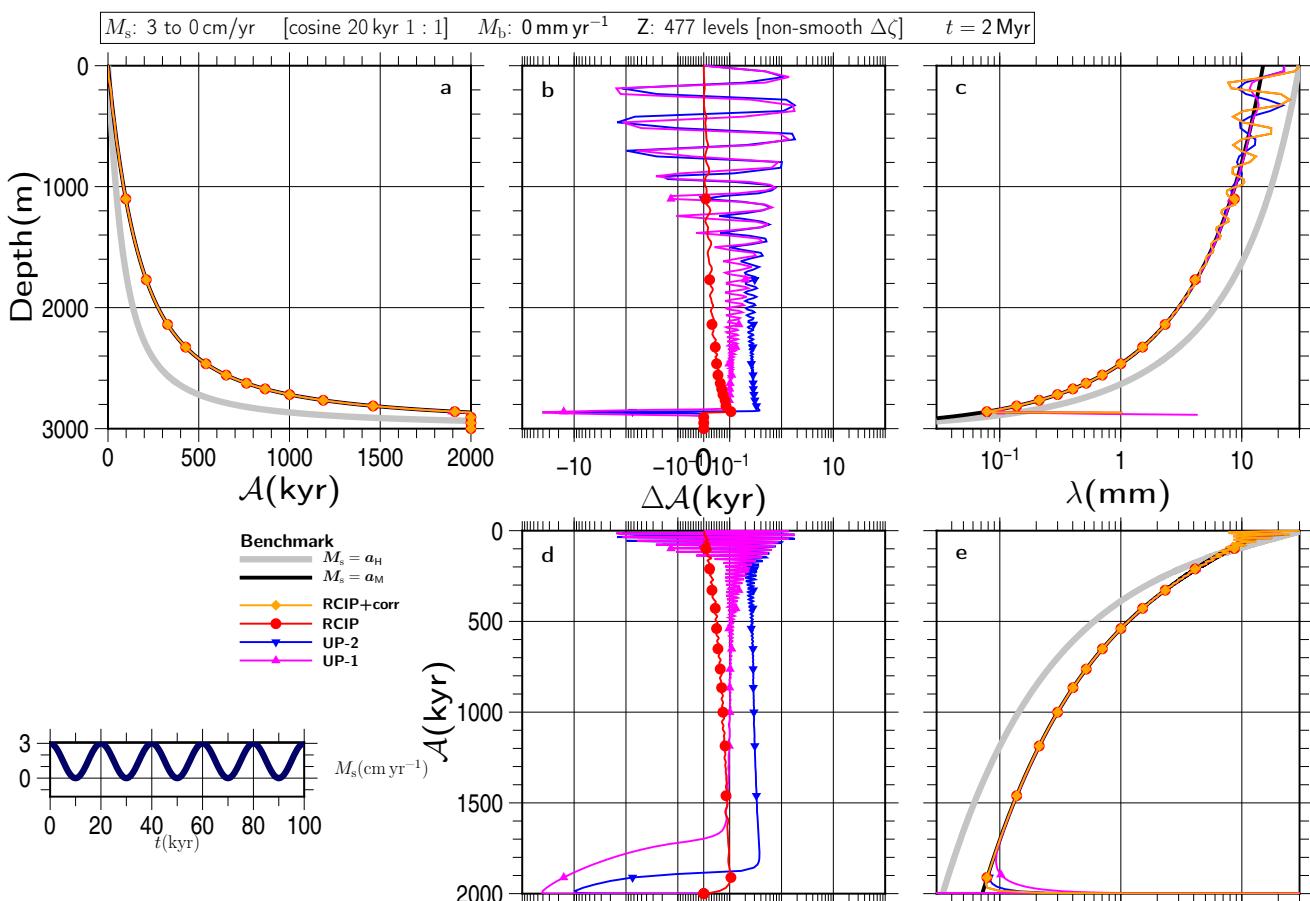


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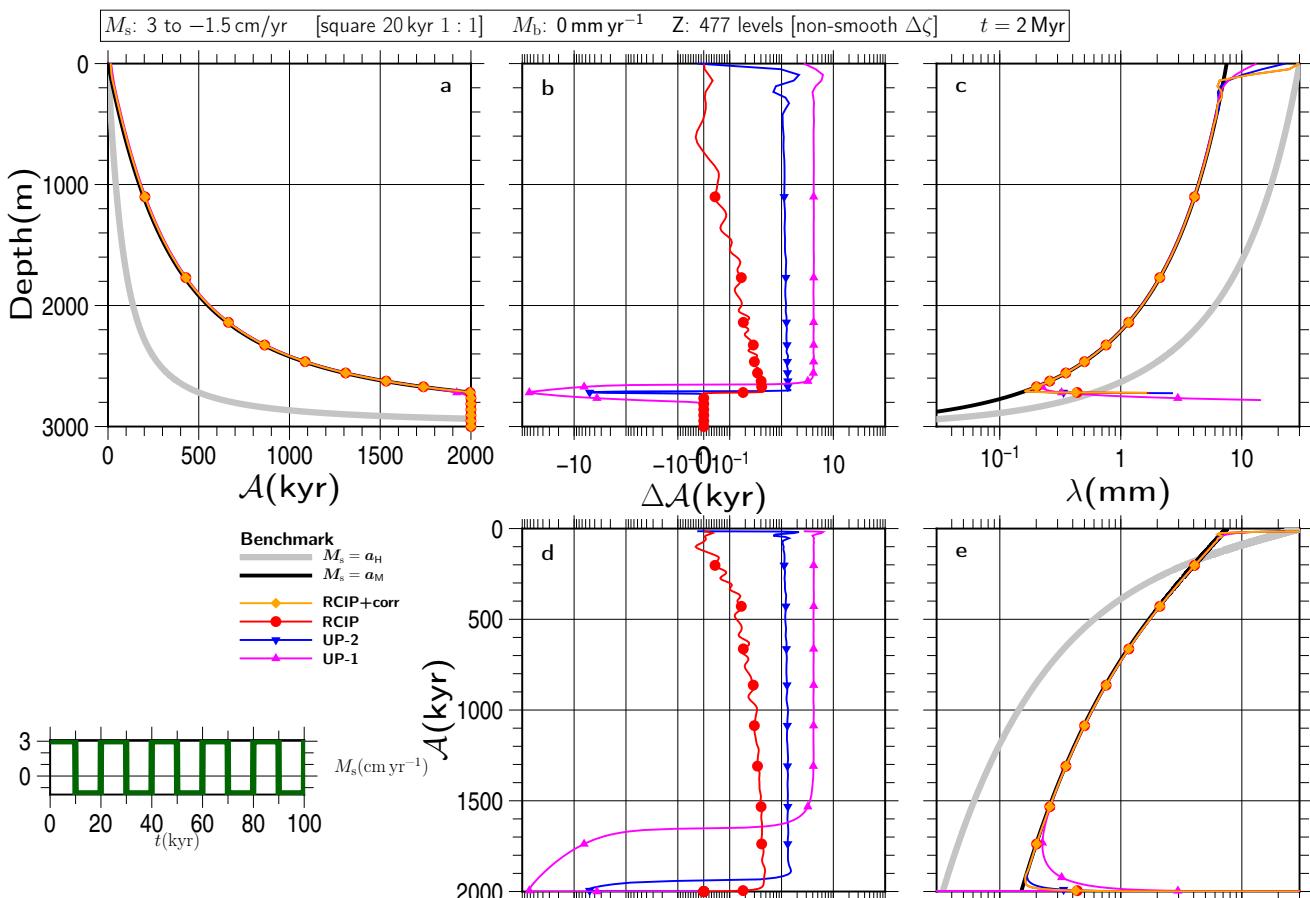


Figure S149

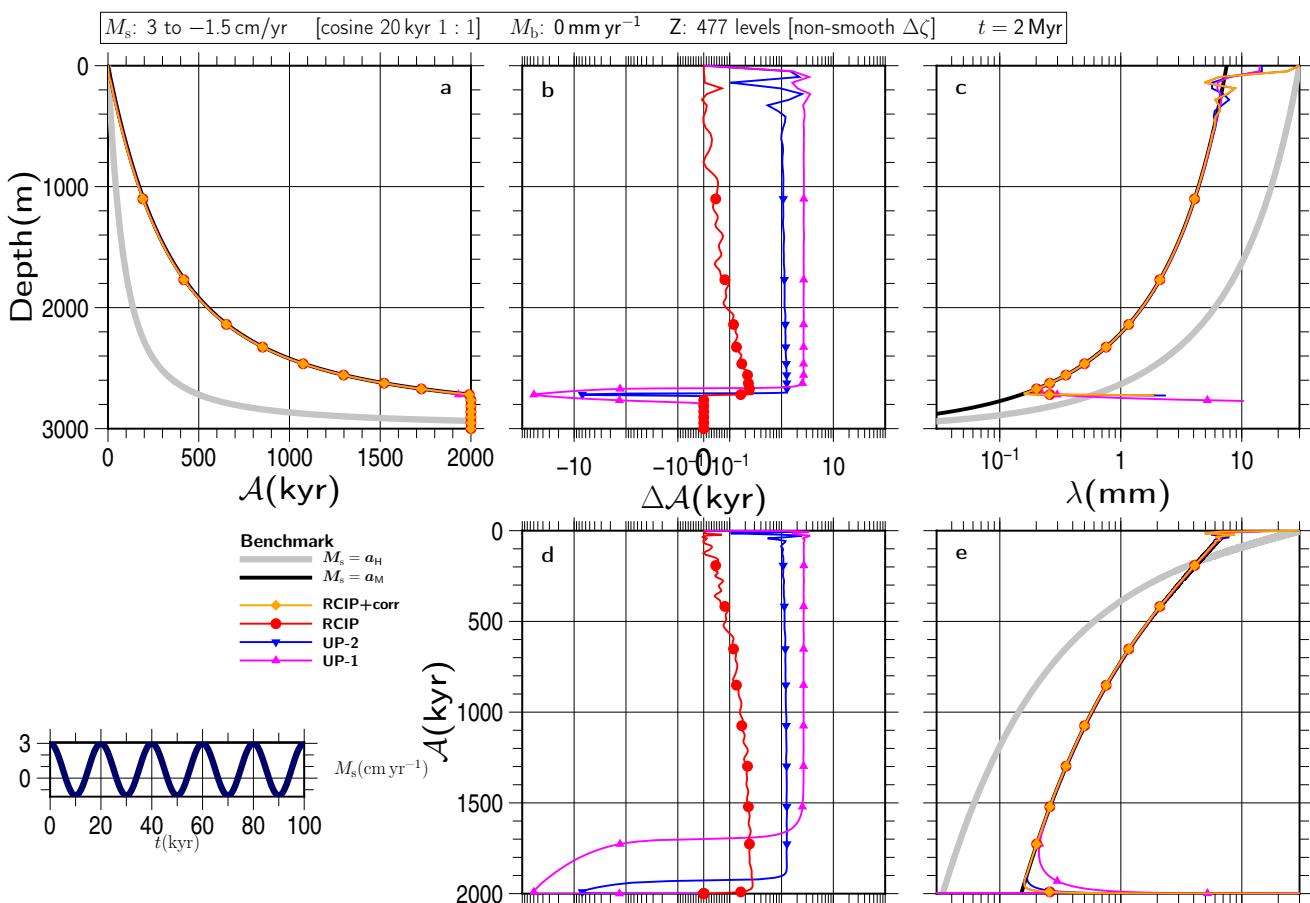


Figure S150

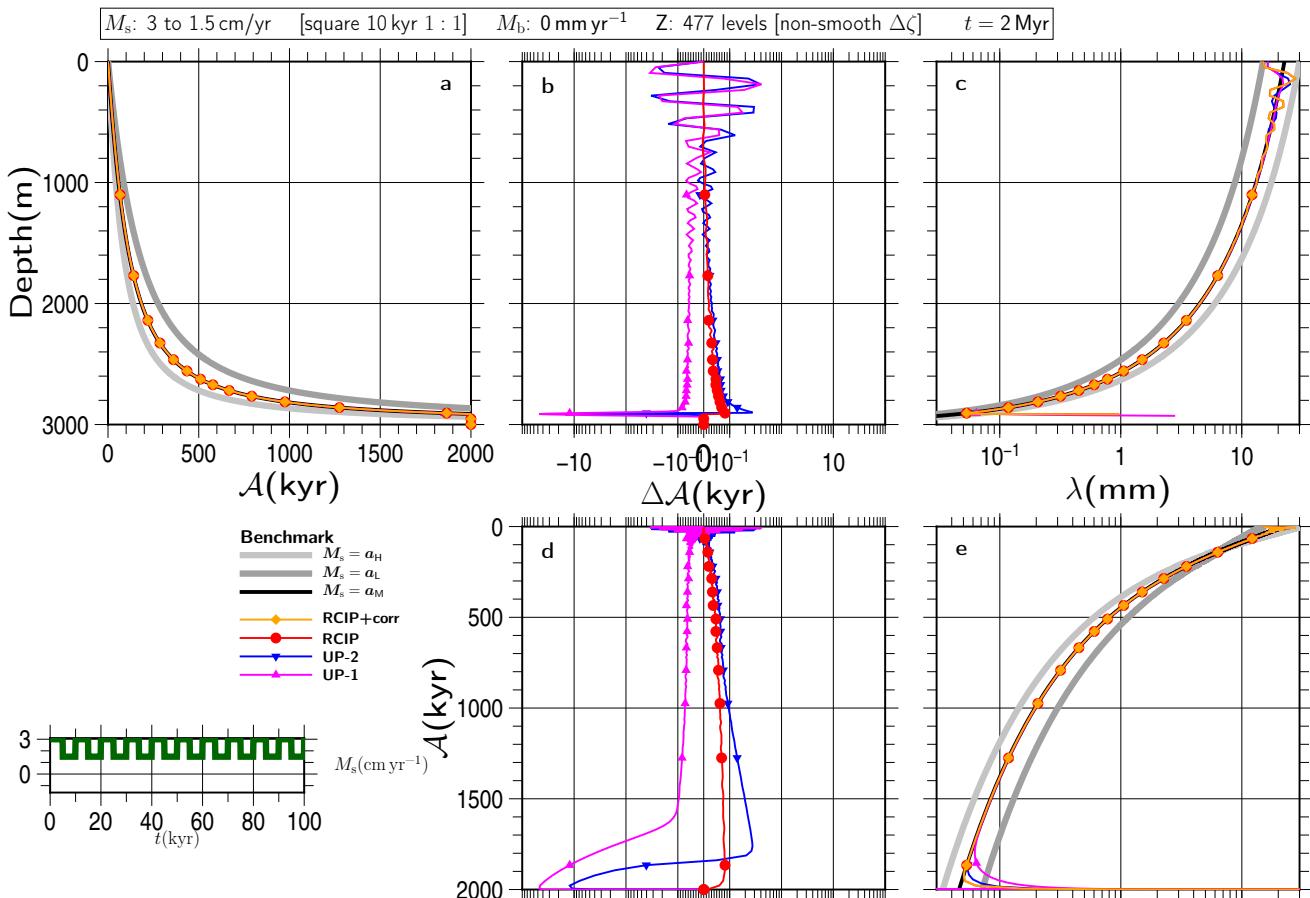


Figure S151

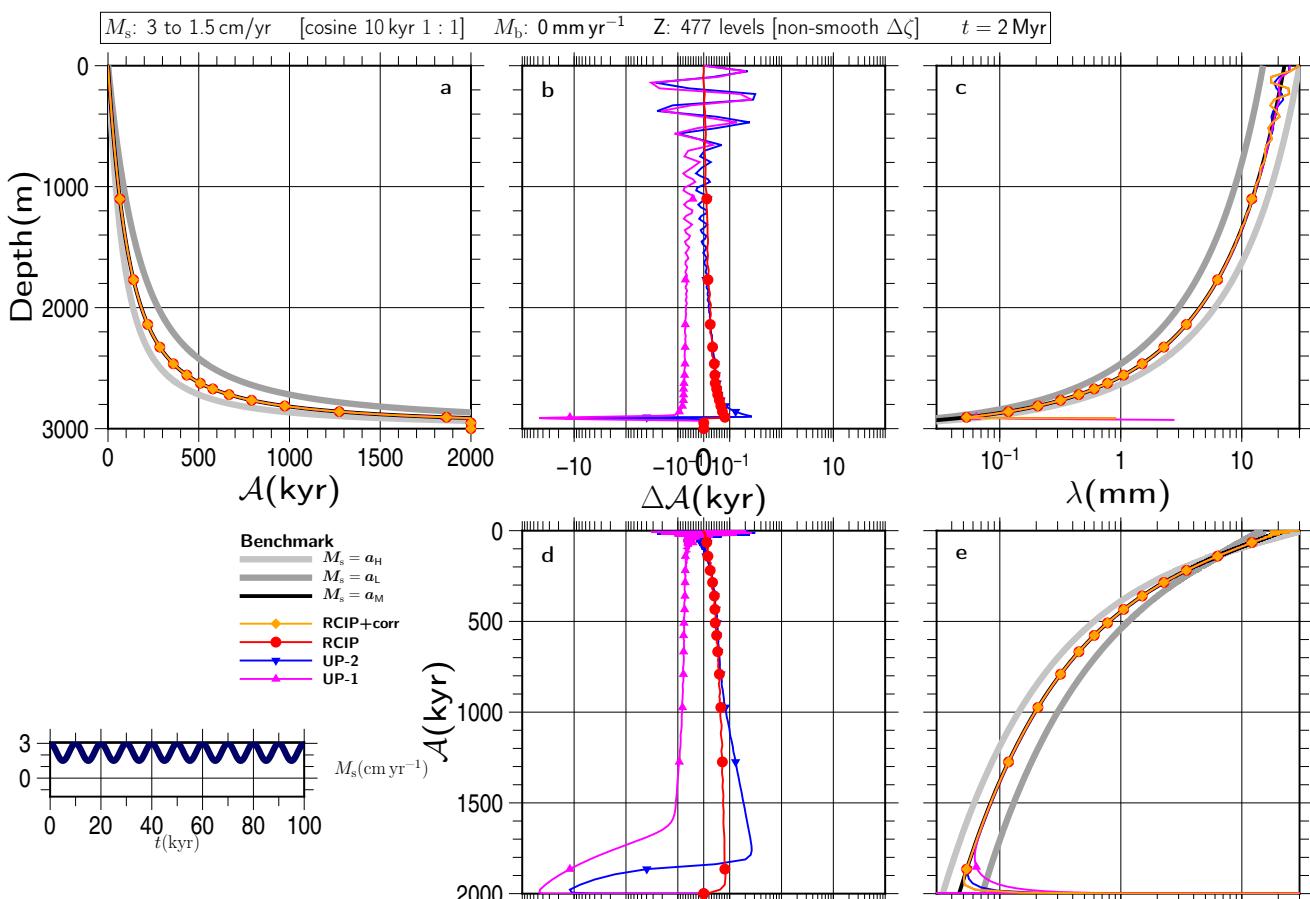


Figure S152

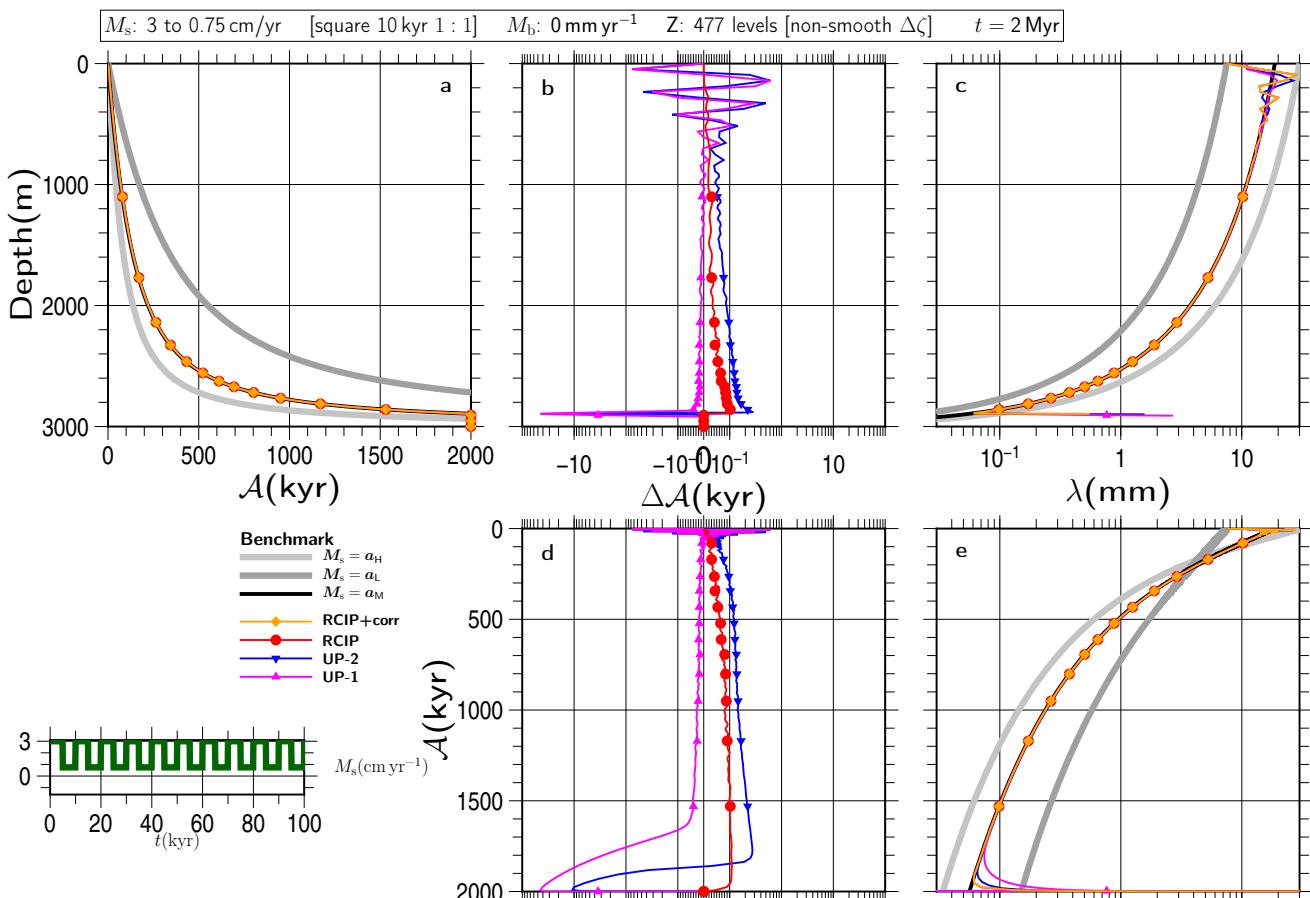


Figure S153

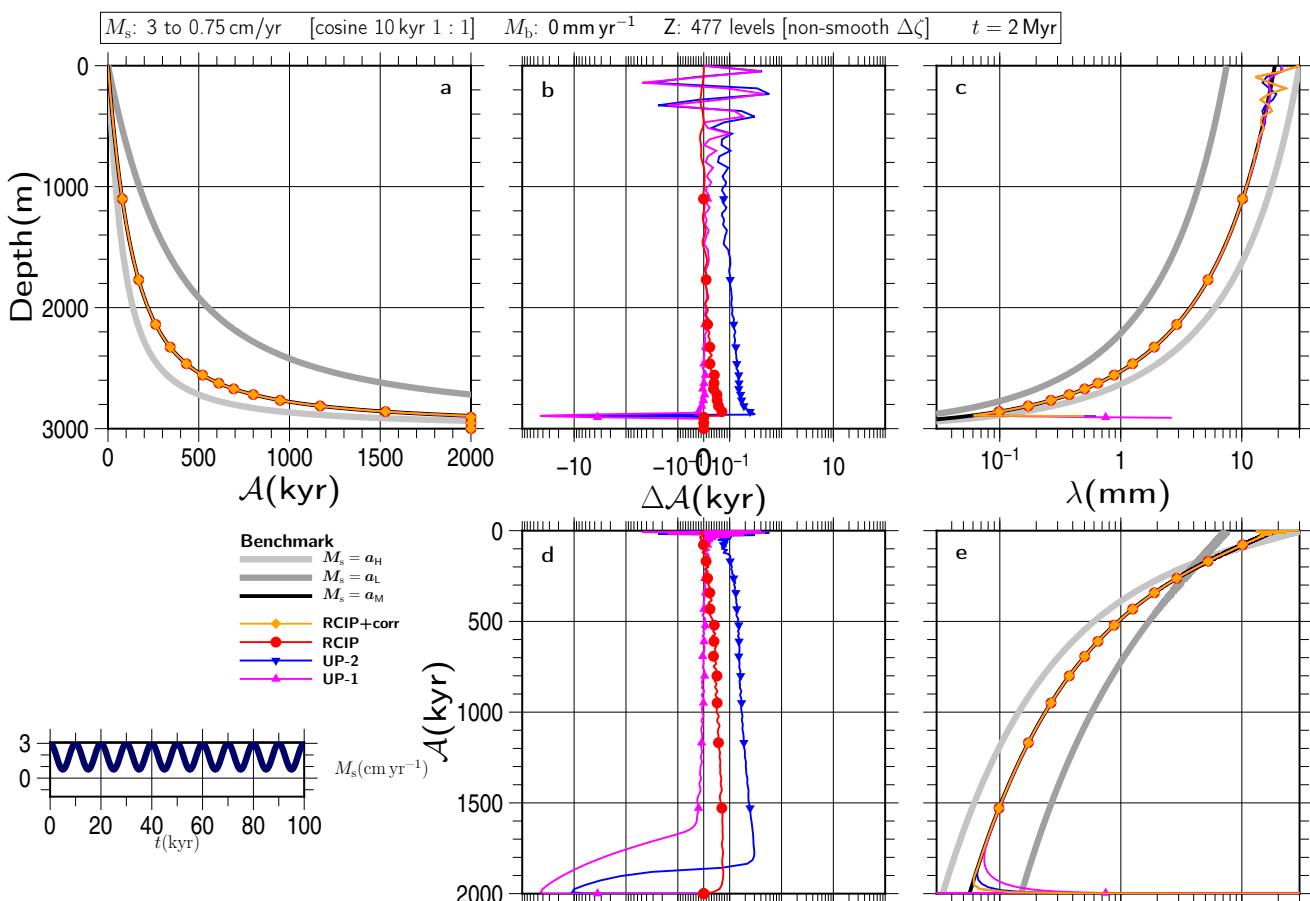


Figure S154

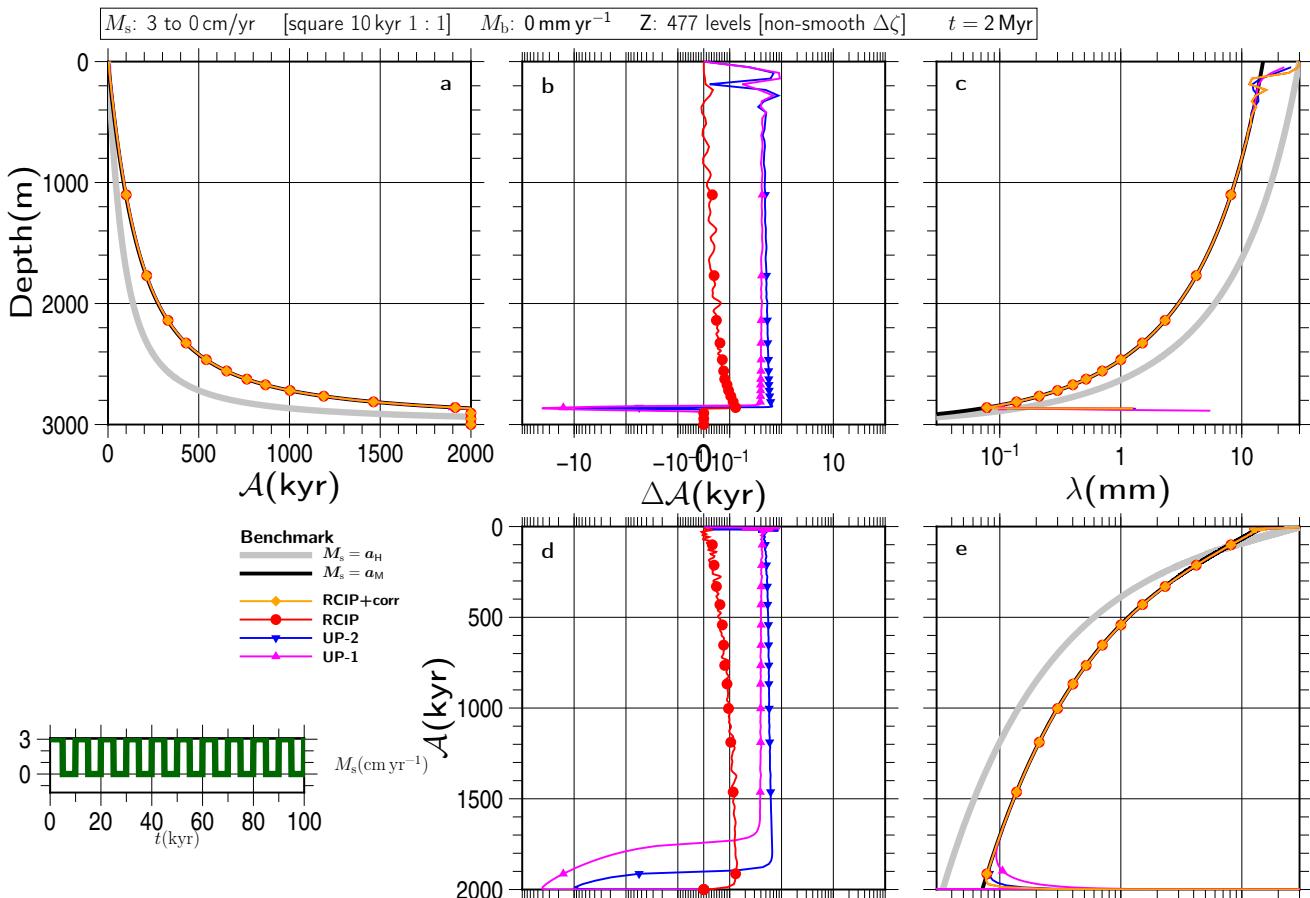


Figure S155

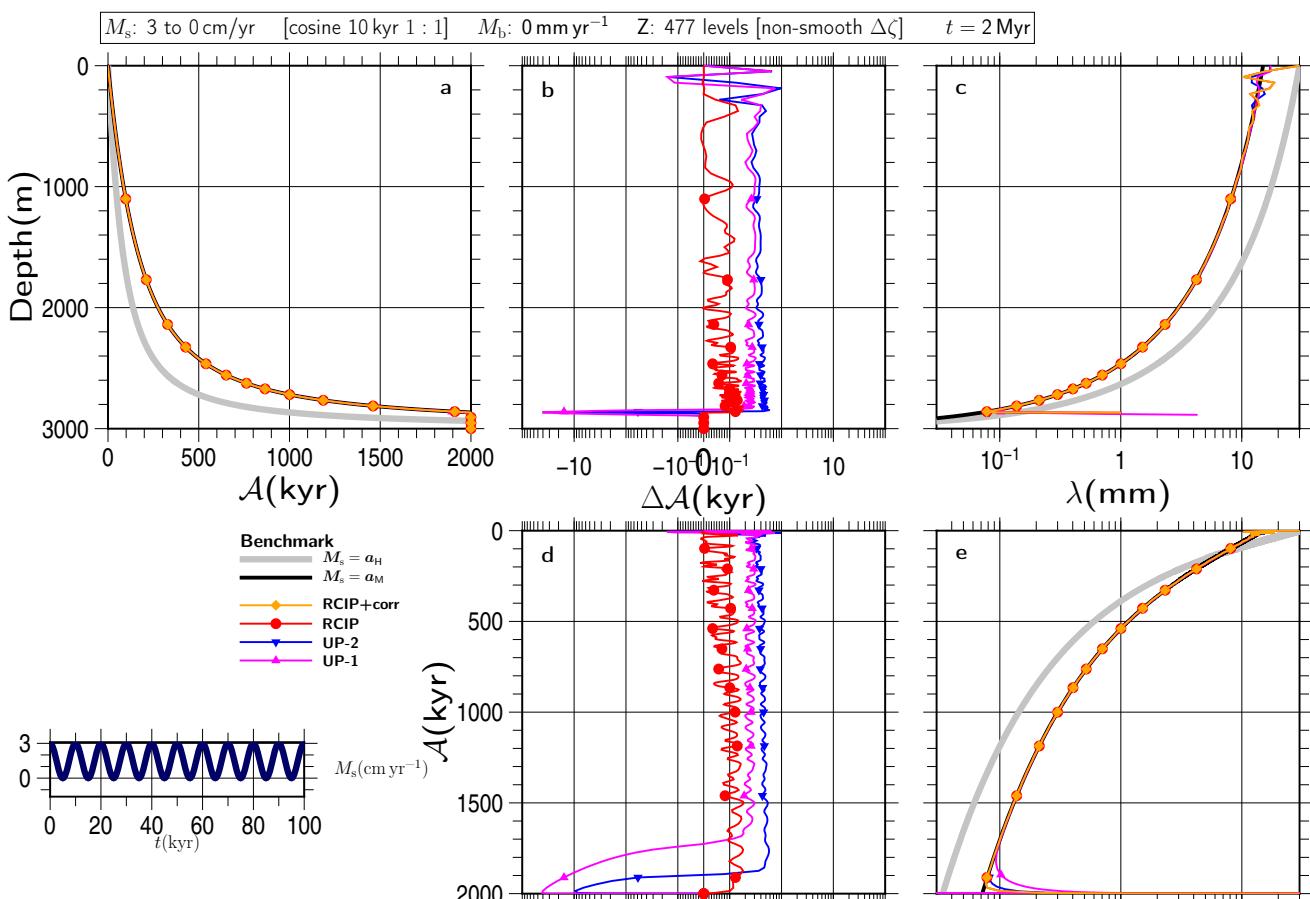


Figure S156

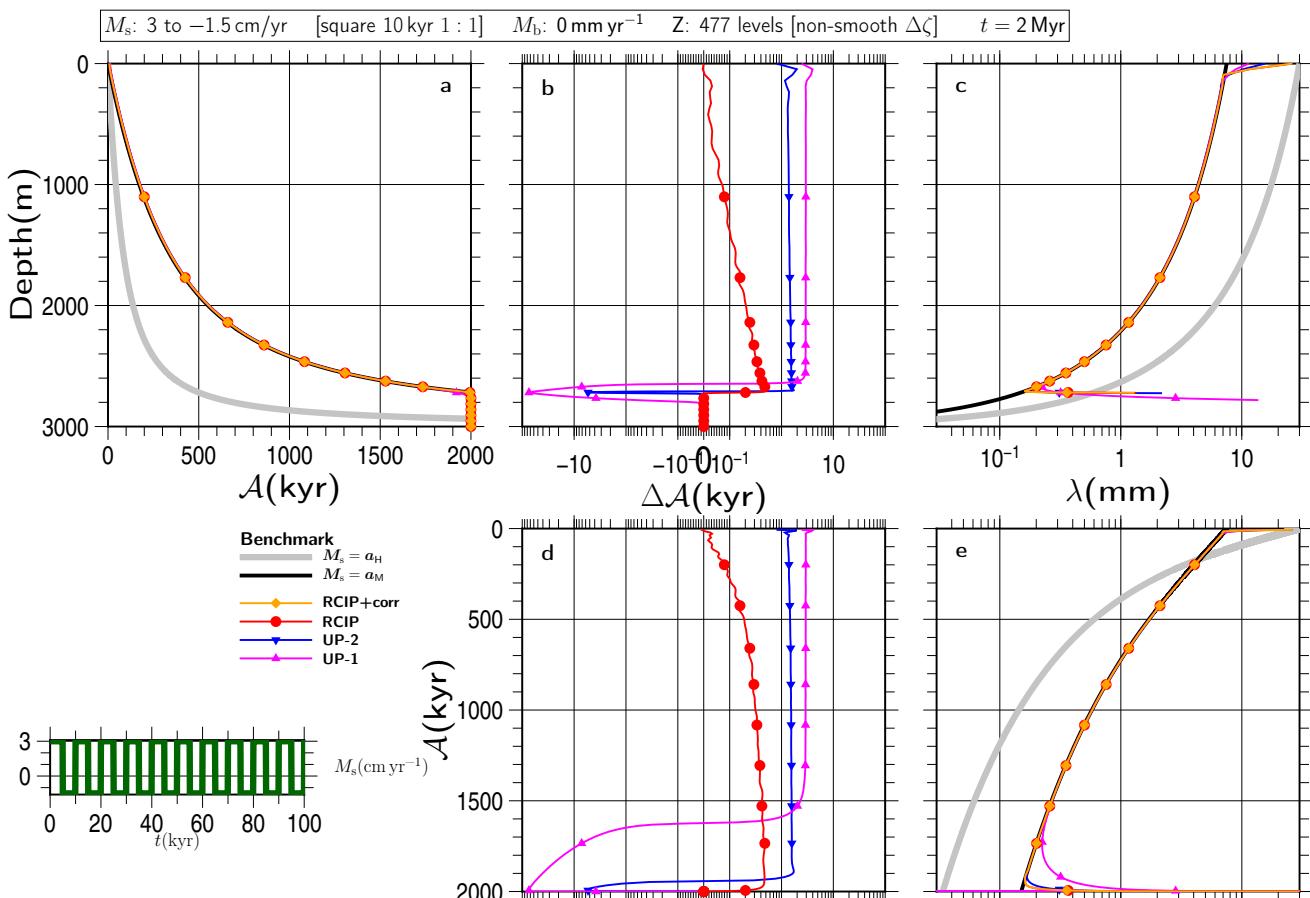


Figure S157

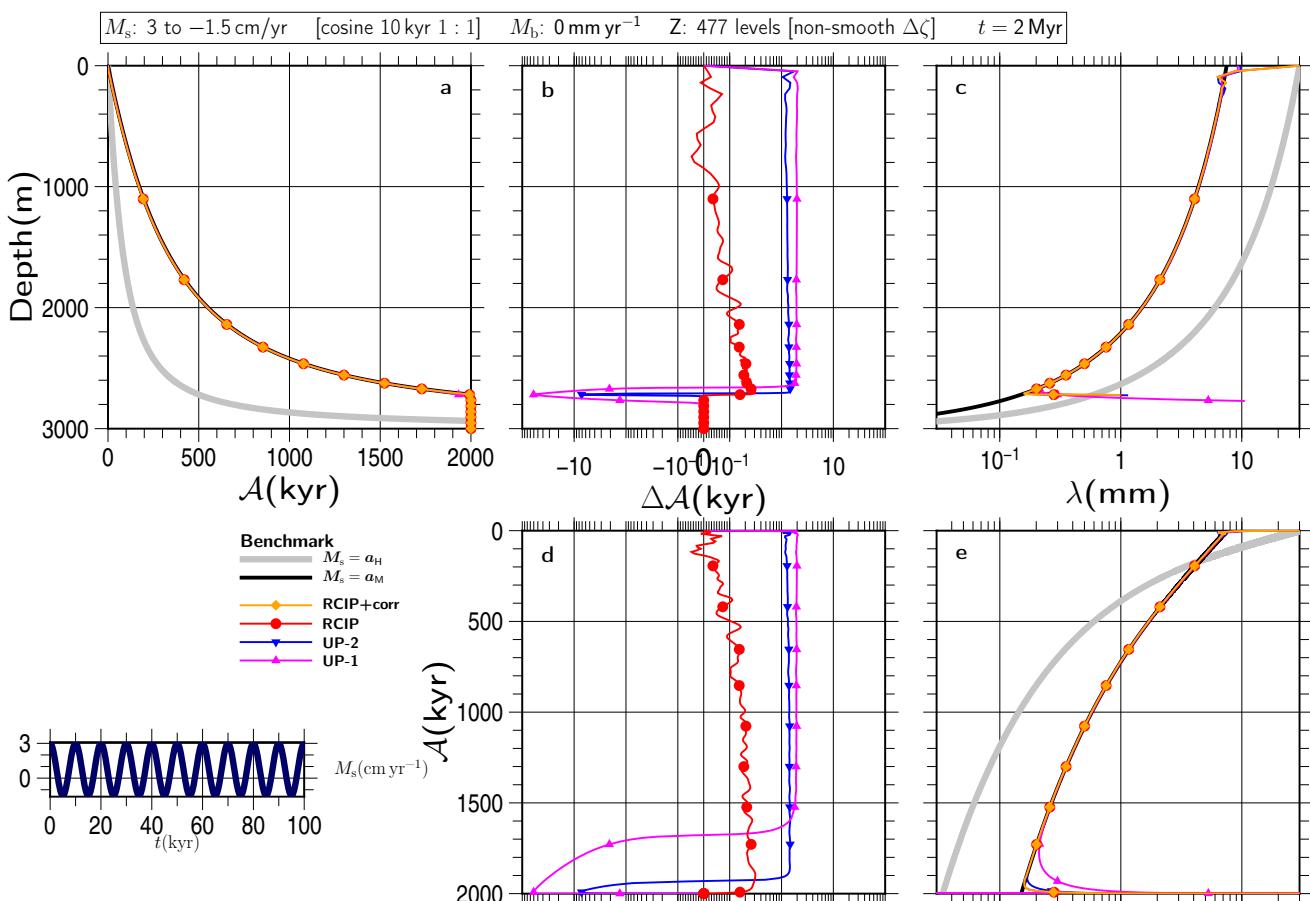


Figure S158

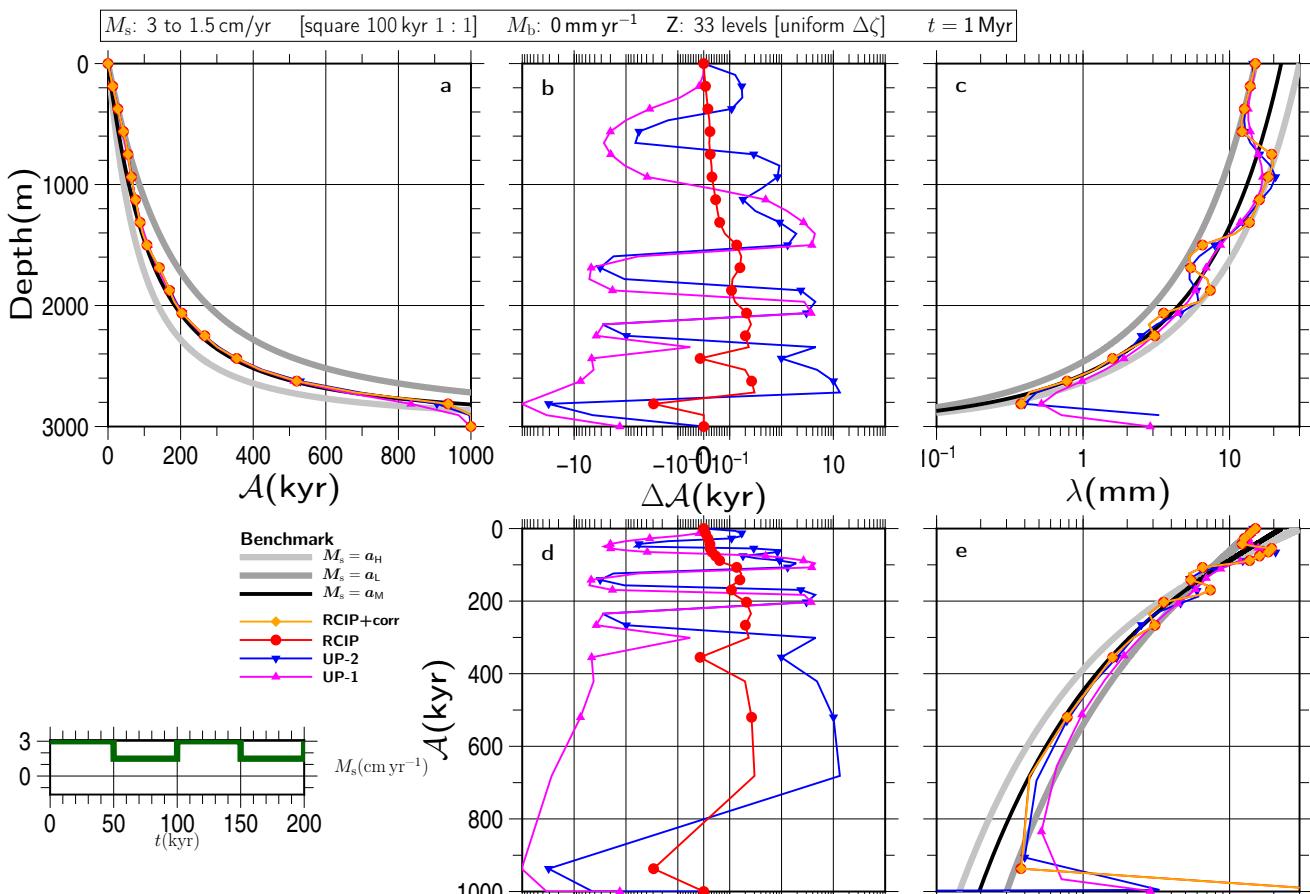


Figure S159

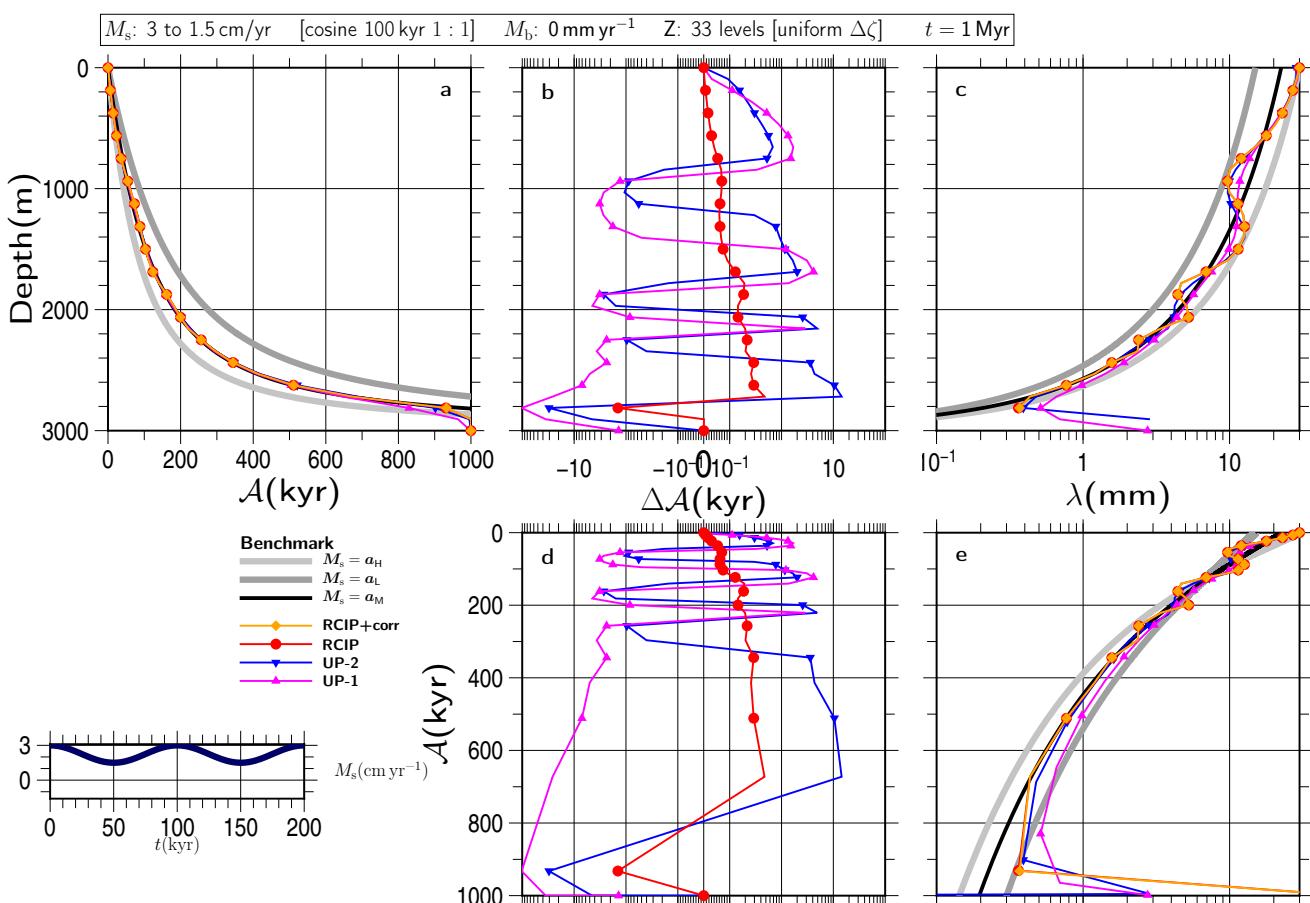


Figure S160

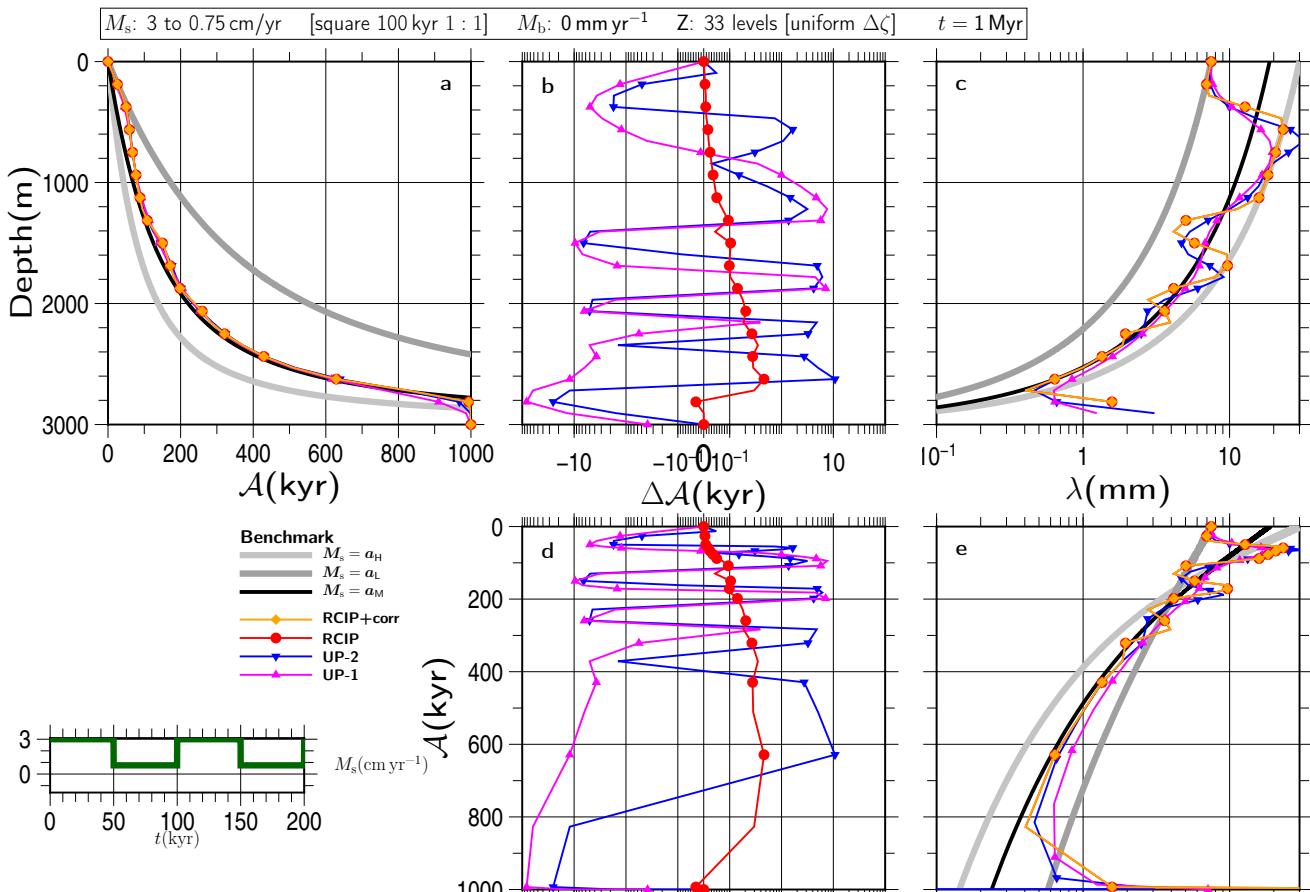


Figure S161

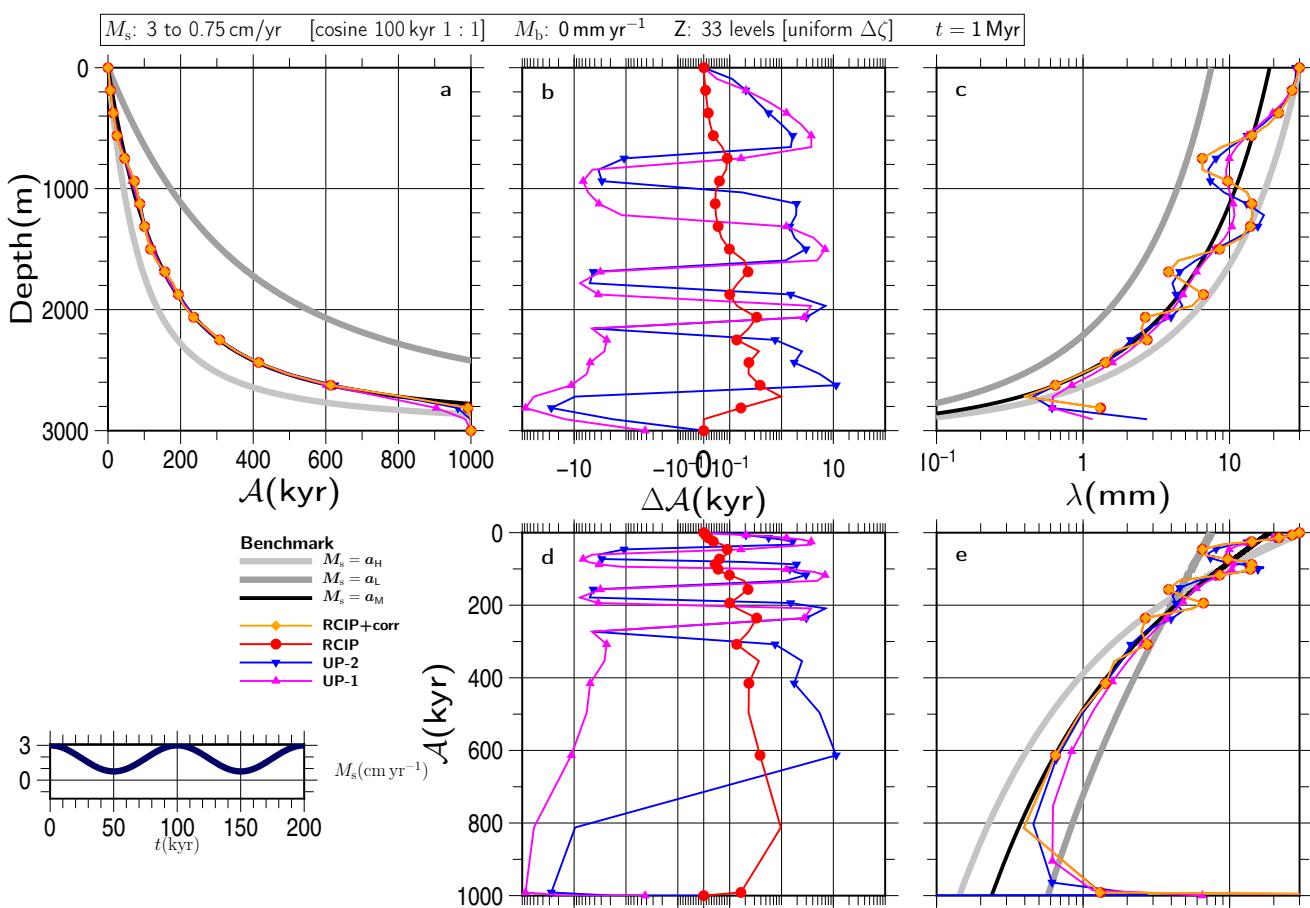


Figure S162

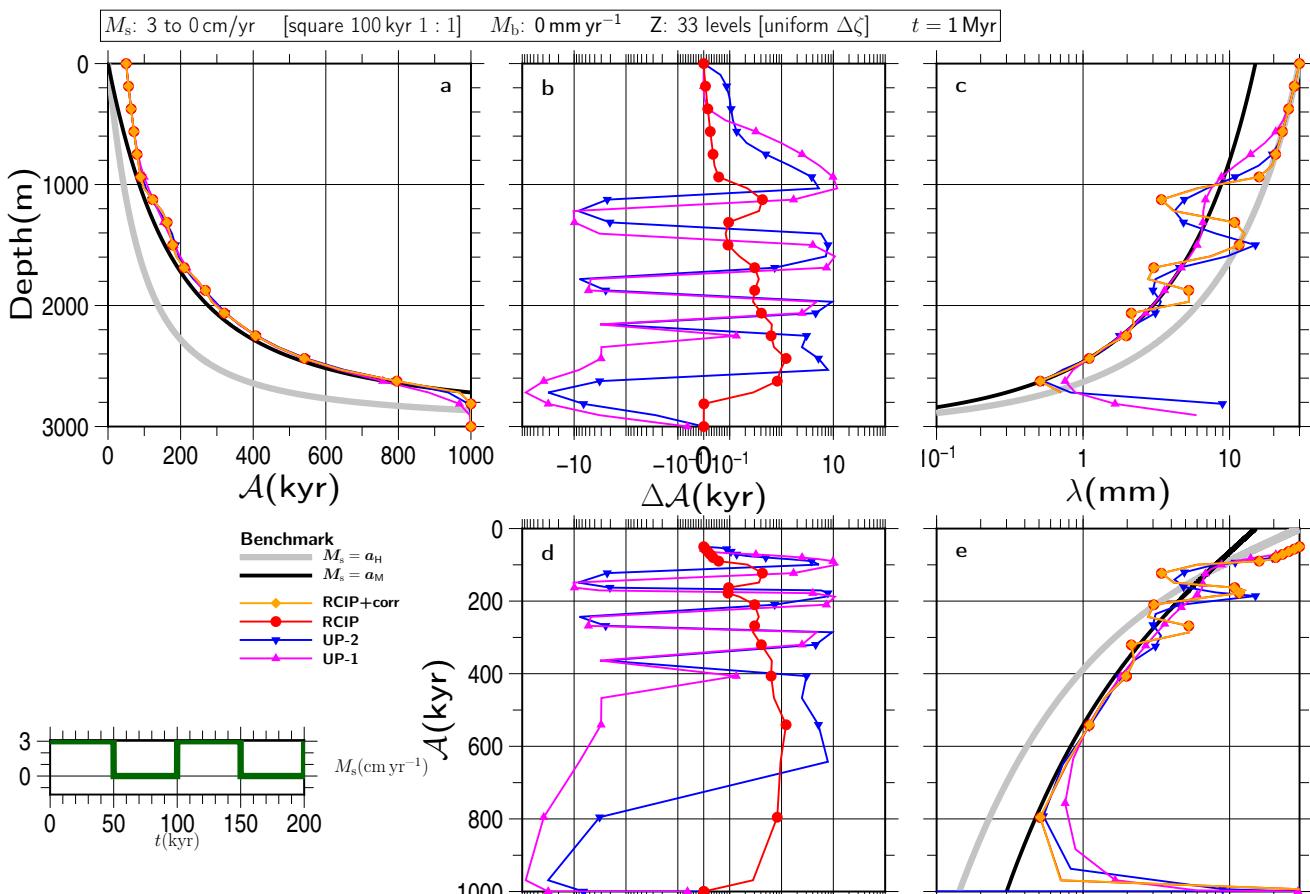


Figure S163

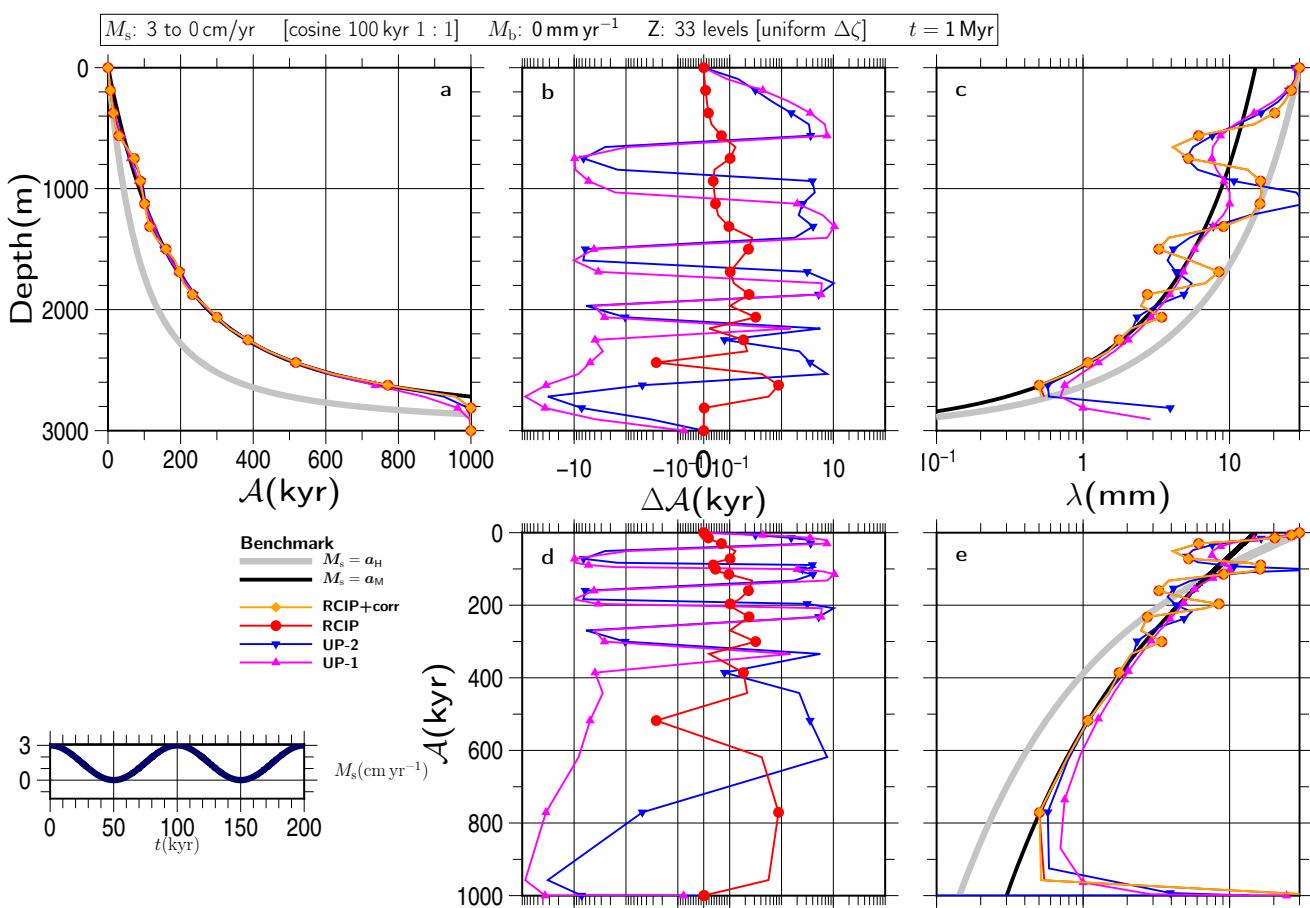


Figure S164

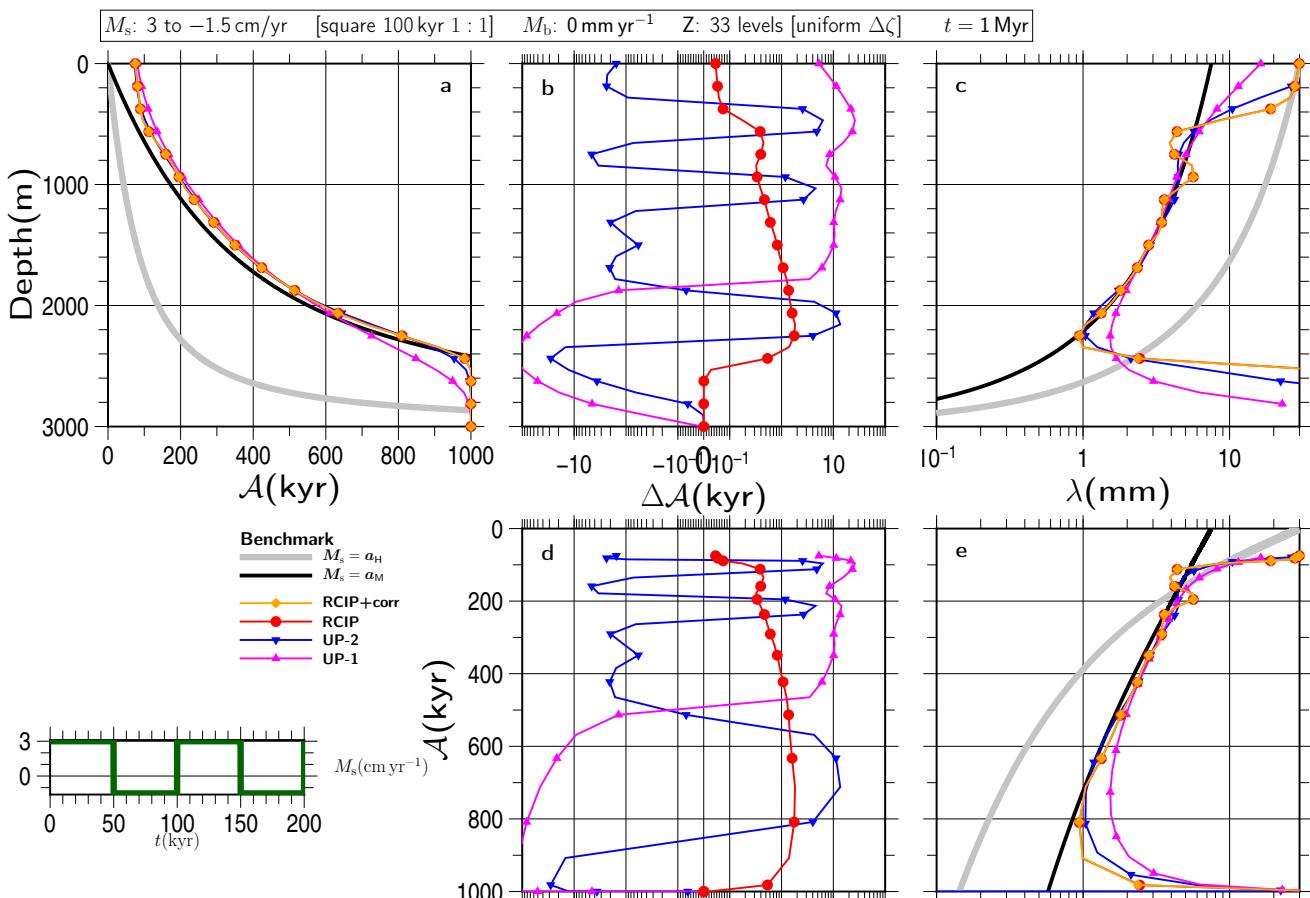


Figure S165

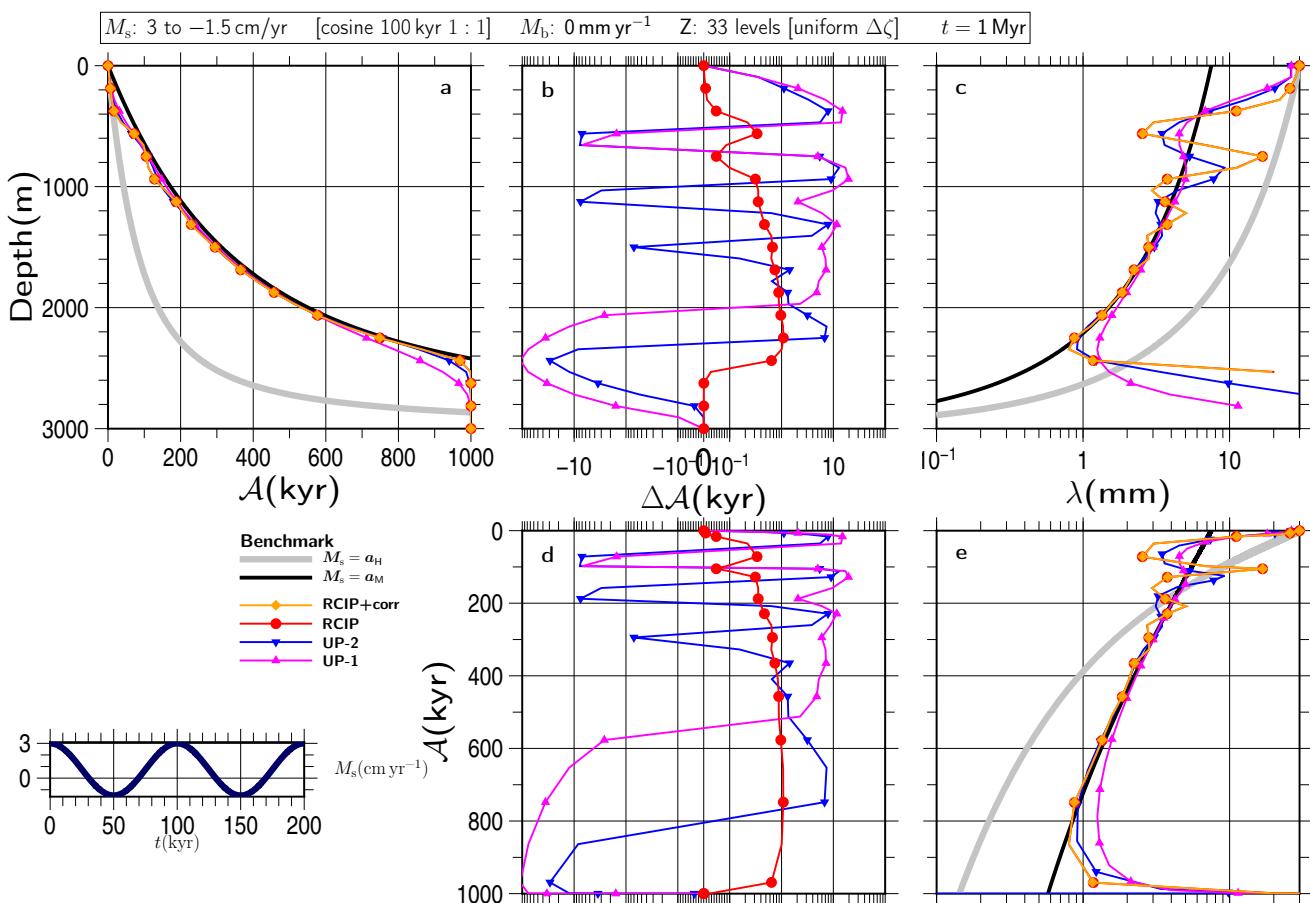


Figure S166