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Supplement of

PatCC1: an efficient parallel triangulation algorithm for spherical and planar grids with commonality and parallel consistency

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Table S1. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the cubed-sphere grid at the coarse resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	0.3	0.9	1.0	2.0	0.16
	OpenMP only	0.3	0.2	0.1	0.2	2.07
	MPI==OpenMP	0.3	-	0.4	-	-
2	MPI only	0.044	0.137	0.390	0.810	0.05
	OpenMP only	0.044	0.060	0.048	0.052	0.85
	MPI==OpenMP	0.044	-	2.265	-	-
3-1	MPI only	0.7	1.3	2.2	2.9	0.23
	OpenMP only	0.7	1.1	2.6	5.1	0.13
	MPI==OpenMP	0.7	-	3.4	-	-
3-2	MPI only	12.4	4.3	1.5	1.9	6.45
	OpenMP only	12.4	4.3	3.9	7.8	1.58
	MPI==OpenMP	12.4	-	2.0	-	-
4	MPI only	198.6	67.2	12.1	9.8	20.26
	OpenMP only	198.6	69.9	29.1	42.6	4.66
	MPI==OpenMP	198.6	-	17.5	-	-
5	MPI only	0.2	0.1	0.5	1.0	0.18
	OpenMP only	0.2	0.1	0.5	1.2	0.14
	MPI==OpenMP	0.2	-	0.6	-	-
Total	MPI only	212.1	73.9	17.8	18.4	11.55
	OpenMP only	212.1	75.7	36.3	56.9	3.73
	MPI==OpenMP	212.1	-	26.0	-	-

Table S2. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the cubed-sphere grid at the medium resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	4.4	6.6	11.0	22.6	0.20
	OpenMP only	4.4	2.0	1.6	1.8	2.49
	MPI==OpenMP	4.4	-	2.9	-	-
2	MPI only	0.049	0.119	0.412	0.824	0.06
	OpenMP only	0.049	0.054	0.055	0.059	0.83
	MPI==OpenMP	0.049	-	0.087	-	-
3-1	MPI only	3.9	14.7	32.9	69.5	0.06
	OpenMP only	3.9	8.2	16.1	19.6	0.20
	MPI==OpenMP	3.9	-	29.6	-	-
3-2	MPI only	71.3	29.2	9.5	15.9	4.49
	OpenMP only	71.3	30.9	10.5	17.5	4.08
	MPI==OpenMP	71.3	-	11.8	-	-
4	MPI only	2334.4	435.4	80.8	67.5	34.56
	OpenMP only	2334.4	461.0	124.5	131.7	17.73
	MPI==OpenMP	2334.4	-	111.0	-	-
5	MPI only	0.8	0.2	0.5	1.0	0.87
	OpenMP only	0.8	0.4	0.7	1.5	0.56
	MPI==OpenMP	0.8	-	0.7	-	-
Total	MPI only	2414.9	486.2	135.2	177.2	13.63
	OpenMP only	2414.9	502.6	153.4	172.1	14.03
	MPI==OpenMP	2414.9	-	155.9	-	-

Table S3. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the cubed-sphere grid at the fine resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	24.7	37.7	100.4	215.4	0.11
	OpenMP only	24.7	10.1	6.0	6.9	3.58
	MPI==OpenMP	24.7	-	24.4	-	-
2	MPI only	0.070	0.109	0.302	0.751	0.09
	OpenMP only	0.070	0.118	0.074	0.076	0.92
	MPI==OpenMP	0.070	-	0.142	-	-
3-1	MPI only	37.6	62.8	305.8	621.4	0.06
	OpenMP only	37.6	64.8	149.5	161.5	0.23
	MPI==OpenMP	37.6	-	201.0	-	-
3-2	MPI only	586.7	137.0	92.8	142.8	4.11
	OpenMP only	586.7	172.5	57.1	56.2	10.45
	MPI==OpenMP	586.7	-	76.7	-	-
4	MPI only	25043.7	4522.2	757.6	591.3	42.35
	OpenMP only	25043.7	4751.8	845.7	728.1	34.40
	MPI==OpenMP	25043.7	-	802.8	-	-
5	MPI only	1.8	0.5	0.7	1.3	1.39
	OpenMP only	1.8	1.1	0.7	2.1	0.82
	MPI==OpenMP	1.8	-	1.2	-	-
Total	MPI only	25694.6	4760.4	1257.6	1573.0	16.33
	OpenMP only	25694.6	5000.5	1059.1	954.9	26.91
	MPI==OpenMP	25694.6	-	1106.2	-	-

Table S4. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the latitude–longitude grid at the coarse resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	0.2	1.1	1.2	2.6	0.09
	OpenMP only	0.2	0.2	0.1	0.1	1.93
	MPI==OpenMP	0.2	-	0.4	-	-
2	MPI only	0.051	0.121	0.312	0.832	0.06
	OpenMP only	0.051	0.041	0.045	0.052	0.98
	MPI==OpenMP	0.051	-	2.021	-	-
3-1	MPI only	0.4	0.8	0.7	1.1	0.38
	OpenMP only	0.4	0.7	1.6	3.4	0.12
	MPI==OpenMP	0.4	-	1.2	-	-
3-2	MPI only	12.4	5.0	1.6	2.0	6.26
	OpenMP only	12.4	5.2	4.4	8.9	1.40
	MPI==OpenMP	12.4	-	2.0	-	-
4	MPI only	261.7	81.2	16.2	11.7	22.44
	OpenMP only	261.7	89.7	45.1	54.4	4.81
	MPI==OpenMP	261.7	-	23.9	-	-
5	MPI only	0.2	0.1	0.5	0.8	0.21
	OpenMP only	0.2	0.1	0.6	1.1	0.15
	MPI==OpenMP	0.2	-	0.6	-	-
Total	MPI only	274.9	88.4	20.5	19.0	14.50
	OpenMP only	274.9	95.8	51.8	68.0	4.04
	MPI==OpenMP	274.9	-	30.2	-	-

Table S5. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the latitude–longitude grid at the medium resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	2.7	9.1	14.4	30.0	0.09
	OpenMP only	2.7	1.3	0.8	0.8	3.27
	MPI==OpenMP	2.7	-	4.3	-	-
2	MPI only	0.063	0.109	0.361	0.773	0.08
	OpenMP only	0.063	0.064	0.067	0.075	0.84
	MPI==OpenMP	0.063	-	0.113	-	-
3-1	MPI only	2.7	7.3	9.5	18.5	0.15
	OpenMP only	2.7	4.2	7.7	9.5	0.28
	MPI==OpenMP	2.7	-	9.8	-	-
3-2	MPI only	80.7	34.7	11.8	16.0	5.03
	OpenMP only	80.7	38.5	12.1	22.5	3.59
	MPI==OpenMP	80.7	-	13.1	-	-
4	MPI only	3370.0	625.4	141.3	98.2	34.31
	OpenMP only	3370.0	642.8	154.1	161.5	20.86
	MPI==OpenMP	3370.0	-	137.2	-	-
5	MPI only	0.7	0.2	0.6	1.1	0.65
	OpenMP only	0.7	0.4	0.5	2.0	0.36
	MPI==OpenMP	0.7	-	0.8	-	-
Total	MPI only	3456.9	676.9	178.1	164.7	20.99
	OpenMP only	3456.9	687.3	175.3	196.5	17.59
	MPI==OpenMP	3456.9	-	165.2	-	-

Table S6. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the latitude–longitude grid at the fine resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/72 units)
		1 unit	6 units	36 units	72 units	
1	MPI only	18.5	71.2	125.7	276.4	0.07
	OpenMP only	18.5	14.9	12.7	11.0	1.68
	MPI==OpenMP	18.5	-	26.7	-	-
2	MPI only	0.073	0.171	0.446	0.883	0.08
	OpenMP only	0.073	0.070	0.124	0.081	0.90
	MPI==OpenMP	0.073	-	0.118	-	-
3-1	MPI only	24.5	35.2	82.8	159.3	0.15
	OpenMP only	24.5	37.7	46.6	50.2	0.49
	MPI==OpenMP	24.5	-	57.3	-	-
3-2	MPI only	704.4	163.1	99.6	137.0	5.14
	OpenMP only	704.4	194.4	68.0	69.3	10.17
	MPI==OpenMP	704.4	-	90.2	-	-
4	MPI only	49137.6	7272.5	1208.5	1004.5	48.92
	OpenMP only	49137.6	7275.6	1355.3	1058.6	46.42
	MPI==OpenMP	49137.6	-	1265.4	-	-
5	MPI only	1.7	0.9	1.1	1.8	0.94
	OpenMP only	1.7	1.3	1.3	3.8	0.46
	MPI==OpenMP	1.7	-	1.6	-	-
Total	MPI only	49886.9	7543.0	1518.2	1580.0	31.57
	OpenMP only	49886.9	7524.0	1484.1	1193.0	41.82
	MPI==OpenMP	49886.9	-	1441.3	-	-

35 **Table S7. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the cubed-sphere grid at the fine resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.**

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/800 units)
		1 unit	20 units	200 units	800 units	
1	MPI only	33.8	62.5	72.0	85.8	0.39
	5 OpenMP threads	33.8	15.3	15.0	16.0	2.11
	10 OpenMP threads	33.8	7.8	10.1	10.1	3.36
2	MPI only	2.0	1.3	3.5	6.6	0.30
	5 OpenMP threads	2.0	2.3	0.2	2.1	0.94
	10 OpenMP threads	2.0	0.1	0.2	2.0	0.97
3-1	MPI only	24.7	180.5	204.0	210.6	0.12
	5 OpenMP threads	24.7	96.5	104.1	105.0	0.24
	10 OpenMP threads	24.7	92.3	97.9	98.4	0.25
3-2	MPI only	701.8	167.8	111.9	148.1	4.74
	5 OpenMP threads	701.8	104.4	76.0	89.5	7.84
	10 OpenMP threads	701.8	76.8	72.5	90.5	7.75
4	MPI only	26395.2	1580.3	137.1	45.0	586.52
	5 OpenMP threads	26395.2	1615.0	140.9	46.4	569.19
	10 OpenMP threads	26395.2	1682.8	155.6	50.3	525.18
5	MPI only	2.4	27.2	61.1	81.7	0.03
	5 OpenMP threads	2.4	15.7	38.5	51.0	0.05
	10 OpenMP threads	2.4	1.0	34.9	41.7	0.06
Total	MPI only	27159.8	2019.5	589.7	577.8	47.01
	5 OpenMP threads	27159.8	1849.1	374.7	310.0	87.62
	10 OpenMP threads	27159.8	1860.8	371.2	292.9	92.73

40 **Table S8. Run time and parallel speedup of each main step of PatCC1 under different parallel settings, when using the latitude–longitude grid at the fine resolution level. “3-1” and “3-2” indicate the first stage (decompose the whole grid into kernel sub-grid domains) and second stage (expand each kernel sub-grid domain) of the third step, respectively.**

Main step ID	Settings of MPI+OpenMP	Run time (ms) under different numbers of computing resource units				Parallel speedup (1 unit/800 units)
		1 unit	20 units	200 units	800 units	
1	MPI only	50.5	87.3	98.0	97.7	0.52
	5 OpenMP threads	50.5	21.8	21.5	26.5	1.90
	10 OpenMP threads	50.5	15.2	14.7	15.6	3.24
2	MPI only	10.4	2.2	4.0	20.0	0.52
	5 OpenMP threads	10.4	2.2	1.9	0.4	26.97
	10 OpenMP threads	10.4	1.6	0.1	0.3	30.27
3-1	MPI only	45.3	86.1	78.6	86.2	0.53
	5 OpenMP threads	45.3	41.8	49.0	76.6	0.59
	10 OpenMP threads	45.3	40.8	65.2	71.9	0.63
3-2	MPI only	867.3	160.6	103.9	126.6	6.85
	5 OpenMP threads	867.3	112.6	84.8	50.2	17.29
	10 OpenMP threads	867.3	85.9	47.1	51.2	16.95
4	MPI only	50721.1	2382.9	312.5	139.0	364.95
	5 OpenMP threads	50721.1	2434.8	309.5	124.9	406.05
	10 OpenMP threads	50721.1	2563.1	322.4	129.4	392.06
5	MPI only	2.4	32.5	91.2	131.8	0.02
	5 OpenMP threads	2.4	15.8	36.5	77.0	0.03
	10 OpenMP threads	2.4	1.1	30.0	52.6	0.05
Total	MPI only	51696.9	2751.7	688.1	601.3	85.97
	5 OpenMP threads	51696.9	2628.9	503.3	355.6	145.40
	10 OpenMP threads	51696.9	2707.6	479.5	320.9	161.09