

True		Z and D grid	
Baroclinic modes:	Barotropic modes:	Baroclinic modes:	Barotropic modes:
$v = \frac{-\beta k}{(k^2 + \ell^2) + \frac{f_0^2}{N^2} \left( m^2 + \frac{1}{4H^2} \right)}$	$v = \frac{-\beta k}{k^2 + \ell^2}$	$v = \frac{-\beta \tilde{\xi} k}{(\xi^2 k^2 + \eta^2 \ell^2) + \frac{f_0^2}{N^2} \left( m^2 + \frac{1}{4H^2} \right)}$	$v = \frac{-\beta \tilde{\xi} k}{\xi^2 k^2 + \eta^2 \ell^2}$
$m \equiv \pi n / z_T \text{ for } n = 1, 2, 3, \dots$		$\xi \equiv \sin\left(\frac{1}{2}kd\right) / \left(\frac{1}{2}kd\right), \quad \eta \equiv \sin\left(\frac{1}{2}\ell d\right) / \left(\frac{1}{2}\ell d\right),$	
		$\tilde{\xi} \equiv \sin(kd) / (kd), \quad 0 \leq [kd, \ell d] \leq \pi$	

C grid		E grid	
Baroclinic modes:	Barotropic modes:	Baroclinic modes:	Barotropic modes:
$v = \frac{-\mu^2 \tilde{\xi} \beta k}{\xi^2 k^2 + \eta^2 \ell^2 + \frac{\mu^2 f_0^2}{N^2} \left( m^2 + \frac{1}{4H^2} \right)}$	$v = \frac{-\mu^2 \tilde{\xi} \beta k}{\xi^2 k^2 + \eta^2 \ell^2}$	Same as Z grid but for $0 \leq [kd, \ell d] \leq 2\pi$	
$\mu \equiv \cos\left(\frac{1}{2}kd\right) \cos\left(\frac{1}{2}\ell d\right)$			

### CD grid

Baroclinic modes:	Barotropic modes:
$e^{2v_r \tau} \left( \mu^2 N^2 L^2 + f_0^2 \sigma_m^2 \right) \sin(2v_r \tau) + \frac{1}{2} \tau e^{2v_r \tau} \mu^2 N^2 \beta \tilde{\xi} k \cos(2v_r \tau)$	$0 = \left[ \left( L^2 \right)^2 - \left( \frac{1}{2} \tau \beta \tilde{\xi} k \right)^2 \right] \sin(v_r \tau) + \tau \beta \tilde{\xi} k L^2 \cos(v_r \tau)$
$+ \tau e^{v_r \tau} \mu^2 N^2 \cos(v_r \tau) \beta \tilde{\xi} k + 2 f_0^2 e^{v_r \tau} \left( \mu^2 - 1 \right) \sigma_m^2 \sin(v_r \tau)$	$e^{v_r \tau} = L^2 / \left[ L^2 \cos(v_r \tau) - \frac{1}{2} \tau \beta \tilde{\xi} k \sin(v_r \tau) \right]$
$+ \frac{1}{2} \tau \mu^2 N^2 \beta \tilde{\xi} k = 0$	$L^2 \equiv \xi^2 k^2 + \eta^2 \ell^2, \quad \sigma_m^2 \equiv m^2 + 1 / \left( 4H^2 \right), \quad 0 \leq [kd, \ell d] \leq \pi$
$e^{v_r \tau} = \left( -b + \sqrt{b^2 - 4ac} \right) / (2a) \text{ for } a, b \text{ and } c; \text{ see Eqs. (38a)–(38c)}$	

A grid		B grid	
Baroclinic modes:	Barotropic modes:	Baroclinic modes:	Barotropic modes:
$v = \frac{-\beta \tilde{\xi} k}{\tilde{\xi}^2 k^2 + \tilde{\eta}^2 \ell^2 + \frac{f_0^2}{N^2} \left( m^2 + \frac{1}{4H^2} \right)}$	$v = \frac{-\beta \tilde{\xi} k}{\tilde{\xi}^2 k^2 + \tilde{\eta}^2 \ell^2}$	$v = \frac{-\xi \beta k}{L_B^2 + \frac{f_0}{N^2} \left( m^2 + \frac{1}{4H^2} \right)}$	$v = \frac{-\beta \tilde{\xi} k}{L_B^2}$
$\tilde{\eta} \equiv \sin(\ell d) / (\ell d), \quad 0 \leq [kd, \ell d] \leq \pi$		$L_B^2 \equiv \xi^2 k^2 + \eta^2 \ell^2 - \frac{1}{2} d^2 \xi^2 k^2 \eta^2 \ell^2$	

L grid		CP grid	
Baroclinic modes:	Barotropic modes:	Baroclinic modes:	Barotropic modes:
$v = \frac{-\mu_z^2 \beta k}{\mu_z^2 (k^2 + \ell^2) + \frac{f_0^2}{N^2} \left( \zeta^2 m^2 + \mu_z^2 \frac{1}{4H^2} \right)}$	$v = \frac{-\beta k}{k^2 + \ell^2}$	$v = \frac{-\beta k}{(k^2 + \ell^2) + \frac{f_0^2}{N^2} \left( \zeta^2 m^2 + \mu_z^2 \frac{1}{4H^2} \right)}$	$v = \frac{-\beta k}{k^2 + \ell^2}$
$\zeta \equiv \sin\left(\frac{1}{2}m\delta z\right) / \left(\frac{1}{2}m\delta z\right) \quad \mu_z \equiv \cos\left(\frac{1}{2}m\delta z\right) \quad 0 \leq m\delta z = n\pi \delta z / z_T \leq \pi \text{ for } n = 1, 2, 3, \dots$			